Ultraintriguing class of X-ray objects are the so called ultraluminous X-ray sources (ULXs). Here an ULX is defined as an X-ray source in an extra-nuclear region of a galaxy with an observed luminosity in excess of $10^{39}$ erg s$^{-1}$ in the 0.5–7 keV band.

1. Introduction

An intriguing class of X-ray objects are the so called ultraluminous X-ray sources (ULXs). Here an ULX is defined as an X-ray source in an extra-nuclear region of a galaxy with an observed luminosity in excess of $10^{39}$ erg s$^{-1}$ in the 0.5–7 keV band. These X-ray luminosities are higher than expected for spherical Eddington-limited accretion onto a $\sim 10 M_\odot$ black hole. ULXs
were known already from studies with Einstein, ROSAT, and ASCA (e.g. Fabbiano 1989; Colbert & Ptak 2002; Makishima et al. 2000), but it was after the advent of Chandra with its combination of high angular resolution and moderate spectral resolution that it has been possible to make significant progress in their study (e.g. Roberts et al. 2004; Swartz et al. 2004). There is a wide debate in the literature on the nature of these sources. They may be powered by accretion onto stellar-mass black holes assuming that there is relativistic beaming (e.g. Körding et al. 2002), or radiative anisotropy (e.g. King 2002), or they may be associated with super-Eddington disks (e.g. Begelman 2002). It has also been suggested that ULXs represent a new class of intermediate-mass (10^2−10^5 M_⊙) black holes (e.g. Colbert & Mushotzky 1999; Miller & Colbert 2004). These intermediate-mass black holes may be fed by Roche lobe overflow from a tidal captured stellar companion that is not destroyed by tidal heating (Hopman et al. 2004). Off-nuclear AGN activity could also be a signature of a recoiling massive black hole: a massive black hole binary coalesces and causes gravitational waves which can give a kick to the center of mass of the system. If the recoiling black hole retains the inner parts of its accretion disk, we could see its luminous phase as an off-nuclear AGN (see Volonteri & Madau 2008, and references therein). Finally, ULXs could also be the high-luminosity extension of supernovae (e.g. Swartz et al. 2004).

Many of the previous studies based on Chandra data are focused on local galaxies, where the Chandra angular resolution allows the detection of several off-nuclear sources in one single galaxy. In this paper, we select a sample of ULXs from the Chandra survey in the COSMOS field. We have here the advantage to combine deep X-ray observation with a wealth of multi-wavelength ancillary data that we will use to put constraints on the nature of these sources and on the properties of their host galaxies. The redshift range that we cover is up to z = 0.3. A study of off-nuclear sources in a similar redshift range was performed by Lehmer et al. (2006) on the Chandra Deep Fields (CDFs).

We quote in this paper magnitudes in the AB system and assume a cosmology with H_0 = 70 km s^{-1} Mpc^{-1}, Ω_M = 0.3 and Ω_Λ = 0.7.

2. Sample selection

We have selected off-nuclear X-ray candidates from the Chandra COSMOS Survey (C-COSMOS), which is a recently completed 1.8 Ms Chandra program to image the central 0.9 deg^2 of the COSMOS field with an effective exposure ranging from ~160 ks to ~80 ks going from the center to the borders of the field (Elvis et al. 2009). The limiting source detection depths are 1.9 × 10^{-16} erg cm^{-2}s^{-1} in the [0.5–2 keV] band, 7.3 × 10^{-16} erg cm^{-2}s^{-1} in the [2–10 keV] band, and 5.7 × 10^{-16} erg cm^{-2}s^{-1} in the [0.5–10 keV] band. We used a point source catalog including 1761 objects detected in at least one band (0.5–2, 2–7 and 0.5–7 keV) with a maximum likelihood ratio larger than detml = 10.8, corresponding to a probability of ~2 × 10^{-5} that a catalog source is instead a background fluctuation (Puccetti et al. 2009). The optical and infrared identifications of almost all (99.7%) of the sources are reported in Civano et al. (2010, in prep).1

As a first step to select off-nuclear X-ray sources, we verified the X-ray position accuracy that we have in the C-COSMOS observations following the procedure presented in Sect. 4.3 of Puccetti et al. (2009). A set of 49 Chandra ACIS-I pointings has been simulated with the MARX simulator, adopting the same exposure times, aim points, and roll-angles as the real C-COSMOS pointings. The detection code PWDetect (Damiani et al. 1997) was applied to the simulated data. We then compared the output of the detection algorithm with the input catalog of the simulation. In Fig. 1 we show the distribution of the difference between the detection algorithm positions and the input positions in units of the X-ray positional error. The last was estimated as the ratio of the PSF at the position of the source and the square root of the net background subtracted source counts. In comparison with Fig. 10 of Puccetti et al. (2009), we restricted the analysis only to sources that were detected at least in one image at an off-axis angle smaller than 5′ to take advantage of an excellent PSF. From the distribution in Fig. 1, we find that 94% of the sources have offsets below 1.8 times the positional error. We will adopt this value as a threshold to select off-nuclear candidates and therefore we expect that up to 6% of our sample is contaminated by nuclear X-ray sources with large astrometric errors. We will shortly come back to this issue. Another possible source of spurious off-nuclear objects could be a poor astrometric accuracy of the X-ray images. According to Fig. 6 of Elvis et al. (2009), 95% of the Chandra sources have an absolute astrometric accuracy better than 1.4′′. For our study we aim at even better astrometric accuracy, therefore we considered only the X-ray sources with an X-ray positional error smaller that 0.8′′. We show the comparison between X-ray coordinates and optical coordinates for sources with a secure identification in Fig. 2: 95% of the X-ray sources have an absolute astrometric accuracy better than 0.9″.

Summarizing, the off-nuclear candidates were selected with the following criteria:

1 The ULX candidates presented in this paper are flagged as “off-nuclear” sources in Civano et al. (2010, in prep.).

2 http://space.mit.edu/CXC/MARX.
with seven off-nuclear source candidates. Cutouts of these objects, obtained from the COSMOS HST/ACS F814W imaging (Koekemoer et al. 2007), are shown in Fig. 3, together with the corresponding Chandra [0.5−7 keV] image.

Each of our off-nuclear sources has an estimate of the X-ray flux in the [0.5−7] keV band reported in Elvis et al. (2009). These fluxes are derived from the counts estimated by EMLDetect\(^3\), corrected to an area including 90% of the PSF (Puccetti et al. 2009). In some cases such an area is large enough to include the whole host galaxy and therefore the X-ray flux could be the total integrated flux of the host galaxy itself. This would include the contribution from the population of X-ray binaries in the host, emission from diffuse gas and a possible weak central AGN. In order to estimate these possible contaminations on the measured X-ray fluxes, we performed aperture photometry for each off-nuclear source. The radii of the apertures were chosen with increasing size from a minimum of 1″ up to include the whole galaxy. In Fig. 4, we plot the net counts in the [0.5−7] keV band as a function of the aperture radius. For four of our sources (XID = 2418, 3441, 11100, 11938) the counts measured at different apertures are constant within the uncertainties. Therefore, we assume that the contribution of the host galaxy is not significant compared with the uncertainties on the measure. For the remaining three sources (XID = 1151, 1388, 1870) the counts rise with the aperture radius and there may be a significant contamination due to the integrated flux of the whole galaxy. In order to minimize this contamination, we considered the measured counts in the smaller aperture (1″). We then used the known PSF shape at the position of the source to estimate the expected fraction between the counts measured in an aperture of 1″ and those over an area corresponding to 90% of the PSF. We then used this ratio to convert our measured counts on the 1″ aperture into the expected ones on a 90% PSF area. These corrected counts are indicated with a filled circle in the plots of Fig. 4, and we used them to estimate the X-ray fluxes.

Full band 0.5−7 keV fluxes and errors were computed converting counts rates to fluxes with the formula Flux = \(B_{\text{raw}}/\text{CF} \times 10^{11}\), where \(B_{\text{raw}}\) is the count rate estimated as described above, and \(\text{CF}\) is the energy conversion factor. This conversion factor varies with the energy band and the spectral index \(\Gamma\) assumed for the power-law spectrum. We used the correction factor \(\text{CF} = 0.89\) counts erg\(^{-1}\) cm\(^{-2}\) reported in Table 4 of Elvis et al. (2009) obtained for the 0.5−7 keV band and \(\Gamma = 1.7\). We decided for this average value of the spectral index following the study of Swartz et al. (2004) that has found a mean power-law index of \(\Gamma = 1.74 \pm 0.03\) for a sample of 154 ULX candidates observed with Chandra. We finally report in Table 1 the 0.5−7 keV luminosities and errors for the seven off-nuclear sources. All sources have luminosities well in excess of \(10^{39}\) erg s\(^{-1}\) in the 0.5−7 keV band (the lowest X-ray luminosity in this band is \(\approx 9 \times 10^{39}\) erg s\(^{-1}\)) and are therefore classified as ULX sources, using either spectroscopic or photometric redshifts. We have secure spectroscopic redshifts for four host galaxies from zCOSMOS VIMOS observations at VLT (Lilly et al. 2007, 2009). For the remaining three objects we used the extremely accurate photometric redshifts available in the COSMOS field (Ilbert et al. 2009; Salvato et al. 2009) based on 30 broad, intermediate, and narrow bands from the UV to the mid-IR. We show in Fig. 5 the X-ray luminosity in the [0.5−7] keV band versus redshift of the seven ULXs. The X-ray luminosities were computed according to the formula

\[
L_X = 4 \pi d_L^2 f_X (1+z)^2 L_{\odot},
\]

\(^3\) http://xmm.esac.esa.int/sas/8.8.0/emldetect
Fig. 3. Cutouts in the HST/ACS F814W band (Koekemoer et al. 2007) of the seven X-ray off-nuclear sources in the C-COSMOS field. The red cross indicates the position of the X-ray centroid and the red circle the X-ray positional error (Elvis et al. 2009). We provide for each object the Chandra ID (top-left), the redshift (top-right), the logarithm of the X-ray luminosity in the [0.5−7] keV band (bottom-left), the maximum likelihood ratio for the X-ray detection (bottom-right), the morphological classification of the host galaxy (bottom-middle; see Sect. 3.1). The images have different sizes for display purposes; the vertical bar in each cutout corresponds to 2″. On the right of each ACS cutout is the corresponding Chandra [0.5−7 keV] image.

where \( d_L \) is the luminosity distance, \( f_X \) is the X-ray flux in the [0.5−7] keV band, and \( \Gamma \) is the X-ray photon index. We assumed \( \Gamma = 1.7 \) (see discussion in this section). Different symbols correspond to the morphological classes of the host galaxies (see Sect. 3.1). Squares are the off-nuclear sources from Lehmer et al. (2006); crosses are the collection of local ULXs by Liu & Mirabel (2005). The dashed line corresponds to the flux limit of the C-COSMOS survey, \( S_{\text{lim}}[0.5−7] = 4.7 \times 10^{-16} \text{ erg cm}^{-2} \text{ s}^{-1} \).

In order to estimate how many background sources we expect to contaminate our sample, we applied a random shift between 30′′ and 2′ to the C-COSMOS sources and searched for chance coincidences with \( R_{\text{AB}} < 22 \) and \( z < 0.3 \) galaxies. We repeated this procedure 10,000 times and found that on average the chance coincidences are \( \approx 1.3 \). Only for 2% of the 10,000 simulations we found more than three chance coincidences. Summarizing, we expect less than one misidentified AGN due to astrometric errors and on average 1.3 serendipitous background source matches.

3. Host galaxy properties

3.1. Galaxy classification

Studies of local samples of ULXs (e.g. Swartz et al. 2004) have shown that these sources are mainly present in late type galaxies. A visual inspection of Fig. 3 suggests that the ULXs at intermediate redshifts that we are studying are hosted in both early and late type galaxies (ETGs and LTGs, hereafter).

To confirm this impression we classified the host galaxies based on their morphology and colors (e.g. Mignoli et al. 2009).
| XID  | RA (J2000) | Dec (J2000) | Counts\(^b\) (0.5–7 keV) | log \(L_X\)\(^c\) (erg s\(^{-1}\)) | Pos. error\(^d\) (arcsec) | Offset (arcsec) | Offset (kpc) | Offset\(^e\) (arcmin) | Off-axis\(^f\) (arcmin) |
|------|------------|------------|-------------------------|-------------------------------|----------------------|---------------|-------------|----------------|----------------|------------------|
| 1151 | 10:00:10.39 | 02:09:23.40 | 28                      | 40.1 (40.3, 40.1)            | 0.5                  | 1.67          | 2.91        | 3.42           | 2.8            |
| 1388 | 10:01:08.46 | 02:01:06.05 | 17                      | 40.6 (40.4, 40.2)          | 0.6                  | 3.62          | 12.12       | 5.73           | 2.6            |
| 1870 | 10:01:03.76 | 02:30:50.22 | 9                       | 39.9 (39.9, 39.3)          | 0.4                  | 3.12          | 4.66        | 7.25           | 2.6            |
| 2418 | 10:00:08.43 | 02:14:47.65 | 6                       | 40.6 (40.1, 40.1)          | 0.3                  | 1.58          | 6.76        | 4.53           | 1.3            |
| 3441 | 09:59:33.78 | 01:49:06.92 | 5                       | 40.2 (40.5, 39.8)         | 0.5                  | 0.95          | 2.26        | 1.87           | 3.7            |
| 11100| 10:00:58.65 | 02:11:39.90 | 12                      | 40.1 (40.3, 39.9)          | 0.4                  | 0.92          | 1.85        | 2.37           | 3.4            |
| 11138| 10:00:43.02 | 02:00:32.74 | 7                       | 40.5 (40.7, 40.2)         | 0.8                  | 1.39          | 4.79        | 1.77           | 4.4            |

**Notes.**

\(^a\) ID of the Chandra source (Elvis et al. 2009).

\(^b\) X-ray counts in the [0.5–7] keV band.

\(^c\) Logarithm of the [0.5–7] keV X-ray luminosity.

\(^d\) X-ray positional error.

\(^e\) Ratio of the distance between the X-ray centroid and the optical centroid over the radius of the Chandra positional error circle.

\(^f\) Off-axis angle value in the image where the source is closer to the on-axis position.

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**Fig. 4.** Aperture photometry for each off-nuclear candidate. The vertical dot-dashed line indicates the distance between the X-ray position and the centroid of the host galaxy; the vertical dashed line is the Petrosian radius of the host galaxy; the horizontal line corresponds to the counts estimated by EMLdetect (Puccetti et al. 2009). For objects XID = 1151, 1388, and 1870, the filled circles represent the photometry on an area including 90% of the PSF obtained applying an aperture correction factor to the photometry measured on an aperture of 1” radius (see discussion in Sect. 2).
The slight preference for ULXs to be hosted in LTGs could be explained by the different shapes of the X-ray luminosity function (XLF) for Low-Mass X-ray Binaries (LMXBs) and High-Mass X-ray Binaries (HMXBs) derived for local galaxies (Grimm et al. 2003; Gilfanov 2004): the former has an abrupt cut-off at $L_X \approx 10^{39}$ erg s$^{-1}$, while the latter can be described with a power-law with a slope $\alpha = 1/6$. Because early-type stars are the dominant stellar population of LTGs, we expect X-ray binaries with O or B type companions, HMXBs, to be common in these objects. This translates into a higher chance to detect ULXs in LTGs or, in any case, in galaxies with current star formation activity.

### 3.2. Stellar masses and star formation rates.

Stellar masses ($M_*$) are derived from the stellar population synthesis model that represents the best fit to the observed photometry (from the $u^*$ band to 4.5 μm) using a χ$^2$ minimization technique. The procedure is explained in detail by Bolzonella et al. (2009). Here we only recall the basic ingredients of the Spectral Energy Distribution (SED) fitting procedure:

- stellar population synthesis models from the libraries of Bruzual & Charlot (2003);
- eleven “smooth” star formation histories for each library: one constant star formation model plus 10 $\tau$-model with e-folding time-scales $\tau = 0.1, 0.3, 0.6, 1, 2, 3, 5, 10, 15, 30$ Gyr;
- a Chabrier initial mass function;
- a Calzetti extinction law with $0 < A_V < 3$;
- solar metallicity ($Z = Z_\odot$).

The star formation rate (SFR) values were estimated using when possible (for three ULXs) the $H_\alpha$ 6563 line flux as measured by the routine Platefit (Lamareille et al. 2009, in prep.), with a correction for reddening. We used the Kennicutt (1998) relation between $H_\alpha$ and SFR: $\text{SFR}(M_\odot \ yr^{-1}) = (7.9 \times 10^{-18} L(H_\alpha))$ erg s$^{-1}$. The de-reddened flux of $H_\alpha$ was computed according to the formula $F_{\text{der}} = F_{\text{obs}} \times 10^{(1.0 + c)L(H_\alpha)}$ where $f(\lambda) = 3.15854 \times 10^{-0.121094 (\lambda - 1)}$ and $c = 1.47 E_{B-V}$ (Seaton 1979; Maier et al. 2005). If a measure of the $H\beta$ flux was available we estimated $E_{B-V}$ from the Balmer decrement, adopting the O'Donnell (1994) Milky Way extinction curve. Otherwise, we used the average value $E_{B-V} \sim 0.2$ mag derived by Moustakas et al. (2006). For the sources without $H_\alpha$ in the spectral range or for

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**Fig. 5.** X-ray luminosity in the 0.5–7 keV band vs. redshift of the seven off-nuclear sources. The different symbols correspond to the host galaxy classification based on morphology and rest-frame colors: circles are ETGs, while stars are LTGs (see Sect. 3.1). Squares are the off-nuclear sources from Lehmer et al. (2006); crosses are the collection of local off-nuclear sources by Liu & Mirabel (2005). The dashed line corresponds to the flux limit in the deepest region of the C-COSMOS survey: $S_{\text{lim}}(0.5–7) = 4.7 \times 10^{-16}$ cgs.

**Fig. 6.** Color-mass diagram: circles and stars are respectively ULX host galaxies classified as ETGs and LTGs based on their morphology/colors; the dots are galaxies in the C-COSMOS area with $z < 0.3$ and $R_{AB} < 22$. For the source XID = 1151 the photometric coverage is limited to few bands and we cannot constrain its stellar mass.
those where we have only a photometric redshift, we used the SFR estimate from the SED fitting procedure.

From the COSMOS catalog (Capak et al. 2007; Ilbert et al. 2009) we selected a comparison sample of galaxies inside the area covered by Chandra. We imposed the same constraints used to select the off-nuclear candidates: $z < 0.3$ and $R_{AB} < 22$. We also removed all sources that are best fitted by stellar SED templates (Ilbert et al. 2009). At the end, the comparison sample consists of 2066 galaxies. For all of them we derived stellar masses and SFR values as described above.

We now estimate the probability to have an off-nuclear source given a host galaxy with a particular stellar mass and SFR. We will consider both LMXBs and HMXBs.

For LMXBs we used the average XLF derived by Gilfanov (2004). This is described by a power-law with two breaks, from their Eq. (8):

$$\frac{dN}{dL_{38}} = \begin{cases} \frac{L_{38}}{L_{b,1}} \alpha_1 \exp\left(-\frac{L_{38}}{L_{b,1}}\right) & L_{38} < L_{b,1} \\ \frac{L_{38}}{L_{b,2}} \alpha_2 \exp\left(-\frac{L_{38}}{L_{b,2}}\right) & L_{b,1} < L_{38} < L_{b,2} \\ \frac{L_{38}}{L_{c,2}} \alpha_3 \exp\left(-\frac{L_{38}}{L_{c,2}}\right) & L_{b,2} < L_{38} < L_{c,2} \\ 0 & L_{38} > L_{c,2}. \end{cases} \quad (2)$$

where $L_{38} = L_X/10^{38}$ erg/s and normalizations $K_{1,2,3}$ are defined as

$$K_2 = K_1 (L_{b,1}/L_{b,2})^{\alpha_2}, \quad K_3 = K_2 (L_{c,2}/L_{c,3})^{\alpha_3}.$$  

We used the best-fitting parameter derived by Gilfanov (2004):

$$\alpha_1 = 1.0, \quad L_{b,1} = 0.19, \quad L_{b,2} = 1.86, \quad \alpha_3 = 5.0, \quad \alpha_3 = 4.8.$$  

The high-luminosity cut-off was fixed at $L_{c,2} = 500$. For the average normalization we used the best-fitting value given by Gilfanov (2004), $K_1 = 440.4 \pm 25.9$ per $10^{11} M_\odot$, and we will assume a linear relation between the number of X-ray sources and stellar mass as found by the same authors (see Sec. 5 of Gilfanov 2004). We note that up to $L_X = \times 10^{39}$ erg s$^{-1}$ the XLF of Gilfanov (2004) is consistent with later studies (e.g. see Fig. 14 of Humphrey & Buote 2008). Above this luminosity we extrapolated the XLF because no data are currently available and therefore the uncertainties are large. For the slope at the highest luminosities, we considered values in the range $\alpha_3 = [2, 6]$ and did not find any significant difference from the contours reported in Fig. 7.

For the HMXBs we instead used the luminosity function derived by Grimm et al. (2003). In particular, we used the cumulative form of it, corresponding to their Eq. (7):

$$N(> L_{38}) = 5.4 \text{ SFR} \left(L_{38}^{0.61} - 210^{0.61}\right), \quad (3)$$

where the SFR is in units of $M_\odot$ yr$^{-1}$.

We then calculated the number of X-ray binaries with $L_X > 10^{38}$ erg s$^{-1}$ that we expect in each galaxy integrating the XLFs for a given SFR and $M_\star$. In Fig. 7 we show the contours corresponding to regions where we expect more than 0.1 (red), 1 (green), 5 (cyan), 10 (yellow) X-rays with $L_X > 10^{38}$ erg s$^{-1}$. In reality these numbers have to be considered upper limits because we have not taken into account the limited Chandra spatial resolution that does not allow the detection of off-nuclear sources with small offsets (see Fig. 10 of Lehmer et al. 2006).

From Fig. 7 we find that all our ULX candidates are hosted in galaxies for which a large number of X-ray binaries is predicted. The dashed line in Fig. 7 is where we expect the same number of LMXBs and HMXBs with $L_X > 10^{38}$ erg s$^{-1}$. This line clearly divides a region (below the line) where the XLF of LMXBs is dominating and therefore the contours are mainly defined by the $M_\star$ values, from a region (above the line) where the HMXBs are more numerous and the contours are determined by the level of the SFR. Our morphological classification is consistent with this picture: ETGs, characterized by a lower SFR and high stellar masses, are located in the bottom-right part of the plot, where the expected number of LMXBs is higher than the number of HMXBs. However, we note that there are suggestions in the literature that no ULX LMXBs may actually exist. Irwin et al. (2004) have shown that the number of ULXs detected in a sample of 28 ellipticals observed with Chandra is equal to the number of expected foreground/background objects. Additionally, these ULXs are uniformly distributed and do not follow the optical light of the galaxies. Irwin et al. (2004) also verified that the same statements can be made for the ULXs associated to early-type galaxies presented in Colbert & Ptak (2002).

It would be interesting to repeat the same computation that generated Fig. 7 considering only X-ray binaries with $L_X > 10^{39}$ erg s$^{-1}$, and therefore to be able to verify the hypothesis that ULXs are the high-luminosity tail of normal X-ray binaries. Unfortunately, this is not possible due to the poor knowledge of the high luminosity slope of the XLF for LMXBs and HMXBs.

4. Fraction of galaxies hosting a ULX

As already pointed out by Ptak & Colbert (2004), useful constraints on the nature of ULXs can be obtained deriving the fraction of galaxies that harbor a ULX as a function of the X-ray luminosity. For example, Körding et al. (2002) have compared the luminosity distribution of X-ray point sources in nearby galaxies with that predicted by X-ray population synthesis models.
to check whether microblazars (microquasars with relativistically beamed jets pointing towards the observer) may represent an alternative to the intermediate mass black holes scenario for ULXs. In order to compute this fraction, we used the comparison sample selected in Sect. 3.2. We derived for each individual galaxy a 90% upper limit on its X-ray flux in the [0.5–2 keV] band according to the procedure described in Sect. 6.5 of Puccetti et al. (2009), to which we refer the reader for details. The top panel of Fig. 8 shows the number of galaxies for which we could detect an off-nuclear source of 0.5–2 keV luminosity $L_{0.5-2\text{ keV}}$ or larger. The bottom panel of the same figure shows the observed number of galaxies in each $L_{0.5-2\text{ keV}}$ bin hosting an ULX of luminosity $L_{0.5-2\text{ keV}}$ or higher.

The red points are the result of our analysis, and the dashed area is the 1σ confidence region. These fractions should be considered as lower limits due to the limited Chandra spatial resolution that does not allow the detection of off-nuclear sources with small offsets (see Fig. 10 of Lehmer et al. 2006). The agreement between our results and the CDFs points is reasonably good above $\log(L_{0.5-2\text{ keV}}) > 40$, although our point and the associated confidence contours are about a factor of two lower than, but consistent with, those derived by Lehmer et al. (2006).

In the lower luminosity bins, it seems that the two measures are discrepant; however, we do not consider this difference highly significant, since the measured fractions are consistent at the 2σ level. Also, at the faintest fluxes the differences between the two X-ray catalogs used is more severe. For these faint sources the positional uncertainties affecting our sample are larger than for the same sources detected in the longer Chandra exposures of the CDFs, and therefore we may be missing the faintest ULXs in the sample if their error box is consistent with the position of the nucleus. We also note that our selection criteria for off-nuclear sources reported in Sect. 2 are more conservative than those used by Lehmer et al. (2006). From Fig. 9 we found that ≃0.5% and ≃0.2% of the galaxies are hosting a ULX with $L_{0.5-2\text{ keV}} \gtrsim 3 \times 10^{39}$ and $L_{0.5-2\text{ keV}} \gtrsim 2 \times 10^{40}$ erg s$^{-1}$, respectively.

We now discuss the observed trend of the fraction of ULX as a function of their X-ray luminosities in the frame of the beaming model of King (2009). According to this model, ULX are stellar mass black holes accreting at a super-Eddington rate ($m \equiv M/\eta L_{\text{Edd}} c^2 > 1$, for a typical radiative efficiency $\eta \approx 0.1$ and accretion rate $M$). Matter accreting at these rates is easily blown away close to the inner edge of the accretion disk (Shakura & Sunyaev 1973); then, the radiative output from the resulting flow pattern is on the order of $L \approx L_{\text{Edd}} (1 + \ln m)$, but emerges collimated by the central funnel with a beaming factor $b \propto m^{-2}$, so that an external observer who happens to have its line of sight within the beaming cone would infer a spherical luminosity: $L_{\text{ULX}} \approx 10^{39} m_7 (1 + \ln m)/b$ erg/s (where $m_7$ is the black hole mass in units of 7 solar masses; see King 2009 for further details). Thus, neglecting the weak logarithmic dependence on $m$, this model directly links the observed luminosity of a ULX with its beaming factor $b$.

Let us now consider a population of ULX with a host galaxy space density (as a function of distance $d$): $n_g(d) \text{ Mpc}^{-3}$.6 Note that here “beaming” simply means geometrical collimation, and not relativistic beaming.

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**Fig. 8.** Top panel: the number of galaxies for which we could detect an off-nuclear source of a given 0.5–2 keV luminosity $L_{0.5-2\text{ keV}}$ or higher. Bottom panel: the observed number of galaxies in each $L_{0.5-2\text{ keV}}$ bin hosting an ULX of luminosity $L_{0.5-2\text{ keV}}$ or higher.

**Fig. 9.** Observed fraction of galaxies with an off-nuclear source with a luminosity of $L_{0.5-2\text{ keV}}$ or greater. The red points and associated 1σ confidence region were obtained by Lehmer et al. (2006) from the Chandra Deep Fields.
The results of Lehmer et al. (2006) imply an almost linear decline of the cumulative number of ULX per galaxy with observed luminosity, \( F_{\text{obs}} \approx F_0(L_{\text{ULX}}/10^{39})^{-1} \), where \( F_0 \approx 0.1 \) is the observed fraction of galaxies hosting a ULX with \( L_{\text{ULX}} > 10^{39} \). The differential fraction \( F_{\text{obs}} \), i.e. the fraction of galaxies containing a ULX with luminosity \( L_{\text{ULX}} \) per unit interval of luminosity can be derived by simply differentiating the above expression, to obtain \( F_{\text{obs}} \equiv \frac{dN}{dL}\log_{10}F_{\text{ULX}} = F_0(L_{\text{ULX}}/10^{39})^{-1} \approx F_0(b/m) \), where the last approximate equality was derived neglecting the logarithm dependence of \( L_{\text{ULX}} \) on \( b \).

We now consider the application of this model to a multi-wavelength survey like COSMOS. We define the limiting flux of the survey in the X-ray band as \( f_{\text{lim}} = f_{-16} \times 10^{-16} \text{ erg s}^{-1} \text{ cm}^{-2} \), so that an object of beaming factor \( b \) can be seen out to a distance of \( d(b) = (10^{39}m/4\pi f_{\text{lim}}b)^{1/2} \approx 313(b/m)^{-1/2} \text{ Mpc} \), and express, in full generality, the number density of galaxies as a function of distance as \( n_n(d) = n_n(d(b)) \equiv n_{n,0}(d(m)) \), where \( n_{n,0} \) is the number density of possible host galaxies in the survey at the maximum distance where an un-beamed source \( (b = 1) \) can be seen. This expression is a very general form appropriate for power-law luminosity functions in Euclidean Universes and is adopted here for the sake of simplicity; \( \alpha \) depends both on the galaxy luminosity function slope and on the survey selection function and can in principle be derived empirically for any given survey: typically we have for flux-limited \( \alpha > 0 \), while volume limited ones have \( \alpha = 0 \). Given the observed cumulative fraction \( F_{\text{obs}} \), and the corresponding differential \( F_{\text{obs}} \equiv F_0(b/m) \), one has to search through a space volume \( V \) \( \sim 1/n_n(d)F_0(b/m) \) to find a ULX with beaming factor \( b \) (within a unit logarithmic interval of \( b \)). From this expression for the volume we derive

\[
d(b) = 125 \left( \frac{A}{0.05} \right)^{1/3} \left( \frac{b}{m} \right)^{-\left(1+\alpha)/3 \right.}.
\]

Thus, the minimum beaming factor (corresponding to the maximal luminosity) of a ULX in a survey of an area \( A \) (in units of square degrees) is given by

\[
b_{\text{min}} = 0.4^\alpha \left( \frac{\gamma}{10^{-16}A^{-\gamma/3}} \right) \left( \frac{F_0}{0.05} \right)^{-\gamma/3} m_7.
\]

where \( \gamma = \frac{d\alpha}{d\log L} \). The overall efficiency of finding ULX scales as \( \ln L_{\text{ULX},\text{max}} \). We recall that \( L_{\text{ULX}} \) is the spherical luminosity that would be inferred by an external observer who happens to have his line of sight within the beaming cone. Applying this rough estimate with \( a = 1, m_7 = 1, n_0 = 0.05, F_0 = 0.1 \) to the COSMOS survey (\( f_{-16} \approx 2, A = 0.9 \)), we obtain \( b_{\text{min}} \approx 0.04, L_{\text{ULX},\text{max}} \approx 2.5 \times 10^{40} \text{ erg s}^{-1} \) in reasonable agreement with the present data. Interestingly, this also suggests that larger, but shallower, surveys could be more efficient in finding ULX (provided a similarly deep sample of host galaxies can be identified): the all sky eROSITA survey \( (f_{-16} = 100, A = 4 \times 10^4) \) could find a large number of ULX, including microblazars up to \( b_{\text{min}} = 2.6 \times 10^{-5}, L_{\text{ULX,\text{max}}} \approx 4 \times 10^{44} \).

\footnote{Although we applied a k-correction to the luminosity values in Eq. (1), we resolved to make the calculations in this paragraph under the assumption of a Euclidean Universe to simplify the derivation of Eq. (5).}

\footnote{We assume in this calculation that the fraction of galaxies hosting a ULX does not change as a function of distance. This is an approximation, because the star formation rate varies with redshift, and therefore it is plausible that the fraction of galaxies hosting a ULX varies too.}

Table 2. Properties of the host galaxies of ULXs in C-COSMOS.

<table>
<thead>
<tr>
<th>XID</th>
<th>i mag</th>
<th>Rb</th>
<th>z</th>
<th>Class</th>
<th>log(M*)</th>
<th>SFR</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>(AB)</td>
<td>(arcsec)</td>
<td></td>
<td></td>
<td>(M_\odot)</td>
<td>(M_\odot/yr)</td>
</tr>
<tr>
<td>1115</td>
<td>15.62</td>
<td>19.89</td>
<td>0.094</td>
<td>ETG</td>
<td>...</td>
<td>...</td>
</tr>
<tr>
<td>1388</td>
<td>20.39</td>
<td>5.20</td>
<td>0.204</td>
<td>LTG</td>
<td>10.1^0.02_0.01</td>
<td>3.0^0.8_1.1</td>
</tr>
<tr>
<td>1870</td>
<td>19.80</td>
<td>9.21</td>
<td>0.072</td>
<td>LTG</td>
<td>9.9^0.02_0.01</td>
<td>1.3^0.4_0.2</td>
</tr>
<tr>
<td>2418</td>
<td>19.45</td>
<td>3.99</td>
<td>0.283</td>
<td>ETG</td>
<td>10.9^0.03_0.01</td>
<td>0.3^0.1_0.1</td>
</tr>
<tr>
<td>3441</td>
<td>18.19</td>
<td>5.00</td>
<td>0.133</td>
<td>LTG</td>
<td>10.5^0.03_0.01</td>
<td>1.1^0.1_0.1</td>
</tr>
<tr>
<td>11100</td>
<td>18.48</td>
<td>6.90</td>
<td>0.110</td>
<td>LTG</td>
<td>10.4^0.01_0.01</td>
<td>1.7^0.1_0.1</td>
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<tr>
<td>11938</td>
<td>18.94</td>
<td>2.53</td>
<td>0.221</td>
<td>LTG</td>
<td>10.9^0.04_0.01</td>
<td>0.04^0.1_0.01</td>
</tr>
</tbody>
</table>

\textbf{Notes.} \( ^{(a)} \) ID of the Chandra source (Elvis et al. 2009). \( ^{(b)} \) Petrosian radius of the host galaxy (Petrosian 1976). \( ^{(c)} \) Redshift of the host galaxy: “s” for spectroscopic and “p” for photometric redshifts. \( ^{(d)} \) Morphological classification of the ULX host galaxy: early type galaxy (ETG) or late type galaxy (LTG). \( ^{(e)} \) The photometric coverage is limited to few bands and we cannot constrain its \( M_* \) or SFR.

5. Conclusions

We presented a sample of ultraluminous X-ray sources (ULXs) selected from the Chandra survey in the COSMOS area (C-COSMOS). From 1761 X-ray sources detected with a maximum likelihood threshold of detim = 10.8 in at least one detection band, we selected 7 ULX candidates covering the redshift range \( z = 0.072–0.283 \).

Taking advantage of the excellent ancillary data available in the COSMOS field, we studied the properties of their host galaxies. From a detailed morphological analysis of the ACS images and rest-frame colors, we found that ULXs are hosted both in late and in early type galaxies, with a slight preference for the former.

From the multi-band photometry and from the optical spectral lines, we measured stellar masses and star formation rates for the host galaxies. Using literature X-ray luminosity functions for HMXBs and LMXBs, we defined probability areas for having detectable off-nuclear sources in the plane SFR versus \( M_* \). All our ULXs candidates are hosted in galaxies for which we expect a large number of X-ray binaries with \( L > 10^{38} \text{ erg s}^{-1} \).

The presence of IMBHs \( (10^{-2}–10^2 M_\odot) \) in some of our ULXs cannot be excluded with the current data. The best candidates for this new class of accreting black holes are the ULXs hosted in early type galaxies (therefore not associated with recent star formation activity) and with X-ray luminosity above \( 10^{41} \text{ erg s}^{-1} \) that can be difficult to explain with high-mass stellar black holes. The objects that satisfy these criteria from our sample \( \text{XID} = 2418 \text{ and } 11938 \). Longer X-ray exposures could give us more insights into the real nature of these sources from a detailed study of the X-ray spectrum. Similarly, we cannot set constraints on the recoiling black-hole nature of our sources with the current data, but it is worth mentioning that recent predictions by Volonteri & Madau (2008) expect at most one of these objects in the C-COSMOS survey, assuming the most favorable scenario (spinning black holes, no bulge in the host galaxy, long active phase).

Finally, we derived the fraction of galaxies hosting a ULX as a function of the X-ray luminosity. We found that \( \approx 0.5\% \) and \( \approx 0.2\% \) of the galaxies are hosting a ULX with \( L_{0.5–2 \text{ keV}} \approx 3 \times 10^{39} \text{ and } L_{0.5–2 \text{ keV}} \approx 2 \times 10^{40} \text{ erg s}^{-1} \). This agrees reasonably well with the observed fraction derived in the Chandra Deep Fields by Lehmer et al. (2006) above \( \log(L_{0.5–2 \text{ keV}}) > 40 \text{ erg s}^{-1} \).
A possible discrepancy in the lower luminosity bins can be likely attributed to the differences in the limiting fluxes of the two catalogs and, therefore, to the different positional uncertainties affecting faint X-ray sources.

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