Emerging properties of animal gene regulatory networks

Eric H. Davidson

Division of Biology 156-29, California Institute of Technology, Pasadena, California 91125, USA.

Abstract

Gene regulatory networks (GRNs) provide system level explanations of developmental and physiological functions in the terms of the genomic regulatory code. Depending on their developmental functions, GRNs differ in their degree of hierarchy, and also in the types of modular sub-circuit of which they are composed, although there is a commonly employed sub-circuit repertoire. Mathematical modelling of some types of GRN sub-circuit has deepened biological understanding of the functions they mediate. The structural organization of various kinds of GRN reflects their roles in the life process, and causally illuminates both developmental and evolutionary process.

The body plan of an animal, and hence its exact mode of development, is a property of its species and is thus encoded in the genome. Embryonic development is an enormous informational transaction, in which DNA sequence data generate and guide the system-wide spatial deployment of specific cellular functions. GRNs also determine the main events of postembryonic development, including organogenesis and formation of adult parts and cell types. Beyond that, GRNs control a vast array of physiological capabilities and modes of response to environmental fluctuations and challenges. GRNs are composed of multiple sub-circuits, that is, the individual regulatory tasks into which a process can be parsed are each accomplished by a given GRN sub-circuit\(^1\)-\(^4\). Thus the operational significance of a GRN structure will be indicated by the types of sub-circuit it contains. However, GRNs have more global organizational properties as well. The comparative review below shows that GRNs may be deeply layered, generating successive regulatory transactions, or they may be shallow, in the sense that they mandate few transactions between the initial inputs and the terminal activation of effector genes.

The developmental GRN sub-circuit repertoire

Modular GRN sub-circuits are defined by their topologies, and the topology of a sub-circuit directly indicates its function in life. In this article I am concerned only with sub-circuits which perform developmental biology jobs that can be defined uniquely, and not with very common ‘motifs’ such as the coherent feed forward loop, which although it has specific dynamic properties\(^5\), appears in so many different contexts that no unique developmental biology function can be associated with it. Table 1 contains a compilation of sub-circuits drawn from all the various GRNs considered in this review, together with an abbreviated description of their regulatory functions, and abbreviated diagrams illustrating the canonical sub-circuit structures. Additional sub-circuits will be found as more developmental GRNs are explored, but the basic import of Table 1 is that there probably exists a small, finite number of sub-circuit topologies out of which developmental programs of all kinds are

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Correspondence should be addressed to the author. (Davidson@caltech.edu).
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constructed. The first entry, for example, is a spatial information processing sub-circuit called the double-negative gate, found in the sea urchin embryo GRNs. This sub-circuit consists of two genes encoding repressors wired in tandem, so that the target of the first repressor is the gene encoding the second, plus downstream regulatory genes which are targets of the second repressor. Its function is to ensure that the target genes are expressed only where the first repressor is (transiently) active (domain X), while these genes are shut down everywhere else (1 − X); what we term an X,1 − X processor.

References in Table 1 generalize the point that structurally similar sub-circuits, but composed of different regulatory genes, are repeatedly encountered doing similar developmental jobs in different GRNs. At root this is because what the circuit can do depends directly on its structure; for example, in a recent study, a search of all possible small sub-circuits based on 3-node topologies showed that only two are capable of response to a signal followed by return to the original state.

A given sub-circuit structure implies a given function, and in development there is a finite set of regulatory functions required. The biochemical complexity of the diverse cis-regulatory systems composing developmental GRN sub-circuits, and the diversity of the sets of transcription factors which animate them, thus may give way to a pleasingly simple set of logic-processing sub-circuit topologies. This would be a very important outcome, for it would make it possible to parse the apparently enormous mazes of interconnections in system level GRNs into modules of developmental logic function, and thus to understand how GRNs control the biology we see.

Deep structure of embryonic GRNs

The GRNs which control the de novo formation of embryonic territories typically include many different functional sub-circuits, which govern successive ‘layers’ of process. They are hierarchical in their overall structure. Their depth simply reflects the long sequence of regulatory steps required to complete any component of embryonic development. The concept of deep as opposed to shallow GRN structure can be simply considered as the number of successive changes in regulatory state required to generate an episode of embryological or other development, between the initial state and the terminal process which the GRN causes to happen. The terminal outcome is, by definition, the activation of cohorts of effector genes (that is, differentiation and cell biology genes, as opposed to only regulatory genes). In relatively shallow GRNs, some of which are considered below, the initial state may be a paused regulatory condition just upstream of expression of a differentiation gene battery.

The sea urchin embryo endomesoderm GRN serves as a reference point, as at present it is the most nearly complete, predictively useful, and validated large scale developmental GRN available. Structure/function aspects of this GRN have been reviewed recently, and an always current version, together with underlying data and dynamic presentations by domain, is available at http://sugp.caltech.edu/endomes/. The concept of GRN depth is illustrated in Fig. 1a by abstracting from the sea urchin GRN the sequence of sub-circuits deployed in order to specify its skeletogenic cell lineage, which produces only the one cell type, and is developmentally the simplest process modelled in the whole endomesoderm GRN. This portion of the network contains 24 regulatory genes and several signalling genes, as well as a sampling of downstream differentiation genes. Without detailing the individual genes and linkages in the skeletogenic GRN, its internal structure is abstractly represented in Fig. 1a as a series of interconnected boxes, each of which represents a GRN sub-circuit that executes the indicated regulatory task. Many of these sub-circuits are among the types listed in Table 1, as indicated by the colour coding, and the arrows show the linkages from one sub-circuit.
to another, that is, they represent transcription factors generated in one box and used for control of gene(s) in the next box, the inputs or ‘feeds’ into each sub-circuit. The boxes are layered hierarchically, with those that initiate the process at the top. Figure 1a includes various control processes that are common throughout embryonic development, because the problems that have to be solved are general: the initial spatial inputs have to be interpreted, the regulatory state then has to be locked down (the initial inputs are always transient), signals have then to be generated, other states have to be excluded, and differentiation drivers have to be activated. It is not surprising that all this requires a lot of sequential circuitry, even given the relative simplicity of skeleogenic lineage development. The GRNs underlying specification of the mesoderm, endoderm\(^\text{1,2,8}\) and of the oral and aboral ectoderm\(^9\) of the sea urchin embryo are similarly deep, layered and hierarchical.

GRNs for specification of mesoderm in \textit{Xenopus} embryos\(^10\), for specification of the gut and mesoderm cell lineages in \textit{Caenorhabditis elegans} embryos\(^11\), and for specification of endoderm and dorsal, anterior and ventral gene expression domains\(^12\), and of mesoderm\(^13\) in zebrafish, also display deep, hierarchical organizations. Some of these GRNs are compilations from the literature or from chromatin immunoprecipitation (ChiP)-chip observations, and have not been validated by direct perturbation analysis, let alone at the cis-regulatory level, but it is unlikely that their overall structure is illusory.

The GRN for dorsal/ventral patterning in \textit{Drosophila}\(^14\), which does have extensive cis-regulatory support, is also hierarchical, but its unusual structure reflects the unusual developmental process it controls. In this embryo regulatory state domains are initially set up very quickly in a syncytium, without intercellular signalling, although following cellularization, signalling dominates further transcriptional functions and the GRN henceforth has a typical structure. In the syncytial embryo spatial stripes of both dorsal/ventral and anterior/posterior regulatory gene expression, which specify the future multicellular embryonic territories, are generated by parallel cis-regulatory responses to maternally localized and zygotically expressed combinations of diffusing transcription factors\(^15–17\). Many of these factors act as repressors in setting spatial boundaries. Important initial inputs in this system are the transcription factors Dorsal and Bicoid, encoded by maternal messenger RNAs which become distributed in graded fashion in the syncytial embryo nuclei, from ventral to dorsal and anterior to posterior, respectively. Cis-regulatory modules have been isolated that control target genes expressed in stripes at given ranges of values of these ‘morphogens’. When associated with reporters, and introduced into the egg, these cis-regulatory modules produce stripes of expression at the appropriate positions along the respective axes. It has been assumed for a long time that the positions where they operate are determined by the quantitative values of the Dorsal or Bicoid concentrations at those locations, which in some way these cis-regulatory systems read. Much recent evidence, however, shows that the positions where these cis-regulatory modules act depend on combinatorial activator and repressor inputs\(^15–19\), and the quantitative values of these ‘morphogens’ alone do not by themselves predict the spatial expression domains of their target genes (except sometimes at the extreme positions where their concentrations are highest). The combinatorial inputs are the products of regulatory genes linked into the GRN\(^20\). Thus the concept that the position of target gene expression is determined solely by the quantitative value of the ‘morphogen’ is overly simplistic: the overall pattern, and the overall signal strength response mechanism, are actually network properties rather than a property of individual cis-regulatory modules that independently and quantitatively read single gradient values.

Vertebrate embryos also use graded inputs, but in this case the developmental systems are cellular, and the ‘morphogens’ are diffusible extracellular signal ligands. Distinct regulatory responses occur, dependent on the intensity of signalling, resulting in activation of different
genes in different locations in the embryo, for example in response to an activin gradient in the pre-gastrular Xenopus embryo. Modelling shows that this particular level-sensitive response could be mediated by a specific type of GRN sub-circuit, in which regulatory genes encoding repressors reciprocally damp each other’s expression, while responding differentially in a cooperative, thus nonlinear and discontinuous way, to the concentration of the signal (Table 1). However, as we see in the following there is more than one type of sub-circuit capable of discontinuous response to a graded signal.

**Structure of GRNs encoding body parts**

We now have bits and pieces of the GRNs controlling development of body parts and organs in later embryonic development, usually their initial stages. Like embryonic GRNs, they are deep and hierarchical, and indeed are in most ways structured similarly to the early embryo GRNs. The box diagram cartoon in Fig. 1b provides an example. This diagram is abstracted from a GRN for specification of pancreas and then of pancreatic β-cells. In adult body part formation, including organogenesis, the first step is always establishment of a given regulatory state in the field of cells from which the body part will form, the progenitor field, for example, the cardiac crescent, or the limb bud, or the imaginal disc. The progenitor field is positioned with respect to the coordinates of the developing organism, which always involves signal-mediated installation of a new regulatory state. But then the field is subdivided into the regulatory state domains of its subparts, and at each step the state is locked down. This used to be called ‘pattern formation’, when people were looking at only one or a few genes at a time. As in early embryo GRNs the main job in setting up the parts and future form of the organ is the progressive deployment of regulatory states in space. It is essential to realize that this process is not to be equated with terminal cell fate specification; the cells expressing patterned regulatory states are yet far upstream in the developmental process from their ultimate descendants, which will eventually differentiate in various directions, according to what part of the organ they arise in.

The similarity between GRNs encoding adult body part formation and those controlling earlier embryogenesis is also sustained at the sub-circuit level in that few additional types of sub-circuit are used. For instance, in pre-gastrular embryonic specification it can be confidently predicted that a feedback circuit locking two or three regulatory genes in a mutual positive embrace will be encountered just downstream of the initial inputs used to set up a given regulatory state (Table 1). This is seen at multiple locations in the sea urchin embryonic GRNs, and the same feature routinely appears in adult body part GRNs: for example, in those underlying development of neural crest in lamprey, gut specification in vertebrates, eye lens field specification in both vertebrates and Drosophila, haemangioblast specification in mouse, pharynx specification in C. elegans, heart specification in mammals and Drosophila, and pancreatic β-cell specification in mouse. Each of these GRNs include two- or three-gene positive feedback sub-circuits functioning to lock down newly installed spatial regulatory states. The similar feedback sub-circuits are constructed with different genes; again it is the sub-circuit topology that determines function, and many different regulatory genes can have the same roles. An additional type of sub-circuit that is commonly seen in later embryonic processes is a signal-mediated, mutual repression device that operates across a cellular boundary, such that, on either side, reception of a signal from the other side specifically causes repression of key genes of the alternate regulatory state (Table 1). Four examples from later development where this type of circuitry obtains are in the GRN that maintains the distinct regulatory states of anterior and posterior parasegment compartments in Drosophila, the GRN controlling establishment of dorsal/ventral neural tube domains in vertebrates, the GRN controlling anterior versus posterior specification in the vertebrate limb bud, and the GRN controlling cell type specification under signal control in the C. elegans vulva.
Postembryonic developmental GRNs: differentiation from pluripotent stem cells

A remarkably recurrent similarity in GRN circuit design has recently emerged in studies of the transcriptional pathways that control binary fate choices executed in the diversification of haematopoietic cell types from multipotent precursors (for reviews, see refs 36–38). At the cores of these circuits, which use some overlapping and some lineage-specific regulatory genes, are pairs of genes encoding transcription factors that mutually antagonize each other’s expression within the same nucleus. Often initially co-expressed at relatively low levels, the lineage fate choice depends on stepped up asymmetric expression of one or the other of the core repressor gene pair. Each of these genes also directly or indirectly promotes expression of positive regulators necessary for execution of one of the lineage fate choices. As the activity of one of the core repressors increases, it causes transcriptional extinction of the alternative choice, and the irreversible installation of its own positive regulatory state (see discussion of the mathematical features of such circuits below). An important point is that the genes of the antagonistic repressor pairs, and/or the regulatory genes that are their immediate targets, also provide direct positive or negative inputs into terminal differentiation genes of the alternate lineages\textsuperscript{37,39}. In other words, this apparatus is deployed immediately upstream of the drivers of the effector genes that generate the features of given cell types (Fig. 1c). In comparison to the embryonic GRNs just considered, these are relatively shallow networks. Ultimately the decisive inputs into one or the other of the core repressors are provided by extrinsic signalling ligands, for example cytokines and growth factors, including Notch and Tgfβ, or endogenous immune receptor signals. The binary choice transcriptional apparatus responds to signal intensity, so that a low input gives one result and a high input another. Different pairs of repressor genes perform similar roles in different lineage fate choices, but what is remarkable is the similar circuitry adduced throughout haematopoietic diversification. Transcriptional balance between pairs of cross-antagonistic repressors decides the outcome, for instance, in myeloid progenitors giving rise to macrophages or neutrophils\textsuperscript{37}; in precursors that may give rise to either B cells or macrophages\textsuperscript{38}, where there is cis-regulatory evidence of the transcriptional cross-repression; in the upper level decision point where erythroid versus myeloid fates bifurcate\textsuperscript{40–42}; in the erythroid versus platelet fate decision\textsuperscript{43}. Similarly, in T-cell diversification between helper vs killer fate\textsuperscript{44,45}, T-cell receptor signal strength indirectly controls repressor function, a compelling case because there is direct cis-regulatory evidence of the reciprocal transcriptional silencing interactions\textsuperscript{46}.

Although to some it is tempting to view all development through the same lens, there are fundamental differences between the terminal fate choice circuitry discussed here and the GRNs that execute early and mid-stage embryonic development of animal body parts. Differentiation gene batteries can be activated only at the end of the series of GRN transactions that decide exactly where they are to be deployed. Haematopoietic cell fate decisions occur at the end of a complex prior developmental process, and in fact as discussed below, the circuitry controlling very early haematopoietic stem cell pluripotentiality operates in an entirely different manner from the binary choice circuitry just considered\textsuperscript{28,47}. In their function, haematopoietic binary choice sub-circuits are similar to the terminal sub-circuits that elsewhere in development immediately determine deployment of differentiation gene batteries. This perhaps explains why a characteristic of the stem cell differentiation choice systems, in other words the simultaneous low level expression in the multipotent precursors of differentiation genes indicative of multiple possible fates\textsuperscript{48,49} (‘lineage priming’), is not seen in embryonic fate choices. That is, in embryonic body part development the spatial fate decision is made far up in the GRN hierarchy, and locked down, long before the differentiation gene battery is deployed. In contrast, in the production
of functional immune cell types the last steps in the decision have to be deferred until the multipotential cells can be told which of its potentialities is more needed. Similar binary choice circuitry is also used in non-haematopoietic developmental contexts, but again at late stages in a given process where a terminal fate choice is to be made. For example, after mammalian somites have formed, they generate spatially confined subdomains, one of which is the dermomyotome. This consists of multipotent stem-like cells, where the choice to generate vascular muscle versus smooth muscle cell types is controlled by a modulated signal, mutual repression between the Pax3 and Foxc2 genes \(^{50}\). Another non-haematopoietic circuit that in essence is remarkably similar to the antagonistic haematopoietic repressor pair sub-circuits was discovered in C. elegans, also operating at the terminus of much prior development \(^{51}\). This circuit maintains the expression of distinct sets of differentiation genes expressed in left versus right taste neurons, but the duelling repressors expressed alternately in these two neurons are in this case microRNAs that directly target the mRNAs encoding the alternate differentiation drivers. All of these kinds of sub-circuits, operate to choose, and/or to maintain the choice, of one of an alternative pair of differentiation gene driver sets.

A priori, development of the body plan cannot be reduced to differentiated cell type specification, the last step in the process, nor to binary decisions between alternative fates. This is at root because development of the body plan requires a long sequence of multidimensional spatial decisions: during pattern formation spatial regulatory states must be installed progressively within multiple (>2) diverse boundaries, and also in certain anterior-posterior and dorsal-ventral positions with respect to the body plan. In each structure of the body regulatory states that include differentiation gene battery drivers are finally installed. Thus it is not in principle surprising that if the set of differentiation gene battery regulators is changed by experimental intervention, a different cell type can be made to appear. Many recent studies show that insertion of vectors expressing sets of transcription factors or even single transcription factors can result in the change of differentiated state from one haematopoietic cell type to another \(^{36}\); from fibroblast to neuron \(^{52}\), from exocrine to pancreatic β cell \(^{53}\), etc. These cell fate changes all occur near the far downstream periphery of GRN hierarchy, as symbolized in Fig. 1. Growing a new cell type requires activation of a new differentiation battery, whereas growing a new body part requires a prior process of spatial pattern formation driven by a deep GRN. More generally, although there are embryonic processes that look superficially like the binary choices just discussed, they are effected very differently. As an example, in the sea urchin embryo, endomesodermal precursor cells give rise both to mesoderm and to endoderm, fates driven by entirely distinct regulatory states. But a careful experimental analysis \(^{8}\) shows that there is no pluripotential ‘endomesodermal’ GRN, and instead a Delta/Notch signal activates a set of regulatory genes which constitute a mesoderm GRN, while in the same cells a Wnt/Tcf signal activates a different set of regulatory genes which constitute the endoderm GRN. The genes of the mesoderm GRN and of the endoderm GRN are expressed independently of one another, without any interactions. The cells of each regulatory state are then separated physically by a cell division, so that the Notch signal is received exclusively by one ring of cells, which becomes mesoderm, while the other cells express the endoderm GRN exclusively \(^{8}\). Nor are the exclusion functions (Table 1) that in given regulatory states act to repress genes key to alternative regulatory states ‘bipotential switches’. These sub-circuits are used to lock down regulatory choices already installed rather than to make choices. They may look superficially like the mutual repression sub-circuits that switch lineages bipotentially, but they are not.

**Differentiation gene battery structure**

Differentiation gene batteries account for functional cell type specificity, and a canonical network structure can be associated with them. This structure describes the topology of the
regulatory relationships causing the protein coding differentiation genes of the battery to be expressed more or less coordinately. Differentiation gene batteries are per se shallow, relatively simply constructed types of sub-circuit, often wired in coherent feed forward format, as for example in sea urchin embryos, pancreatic β-cells, and macrophages. As the immediately upstream GRNs are being uncovered, an additional characteristic of differentiation gene battery regulatory circuitry is often encountered: this is the occurrence of feedback between the drivers of the differentiation genes just upstream of the linkages to the effector genes, either auto- or cross-regulatory, though this is not always seen. The canonical form is that of Fig. 2a. Differentiation gene batteries consist of a sometimes very large number of effector genes, the relevant cis-regulatory modules of which (per battery) respond to members of a small set of transcription factors present as part of the terminal regulatory state. However, each such cis-regulatory module may in addition be serviced by some additional factors, which accounts for the fact that all the genes of the battery are not exactly expressed in lockstep. For example, muscle protein genes are activated by two or three of the transcription factors orthologous to Srf, Mef2, and a myogenic bHLH factor in vertebrates, plus, individually, other factors; whereas in C. elegans the differentiation genes of each class of neuron are identified by their response to a single key transcription factor, sometimes together with other factors.

It is logically consistent that where there is direct repression of differentiation gene batteries by a proximal control circuit (‘anti-differentiation’) much the same architecture would be employed. In embryonic stem cells a hierarchical GRN that maintains the pluripotent state is headed by a recursive triple feedback system that links Nanog, Oct4 (also known as Pou5f1) and Sox2 genes. Apparently directly downstream of this are linkages to many genes encoding transcriptional activators and repressors, including a polycomb repressor that in turn targets regulatory genes associated with various differentiation states. But also among the immediate targets of the triple feedback loop is the Rest gene, which encodes a factor that directly represses neurogenic differentiation genes. This circuit is the mirror image of gene battery activation circuits.

Structure/function relations for GRNs controlling diverse kinds of biology

The downstream effector gene cassettes required for development include those executing morphogenetic cell biology functions, as well as differentiation gene batteries. A distinction is that by definition, differentiation genes are expressed cell type-specifically, whereas genes required for functions such as motility, ingestion, invagination, cell division, convergent extension, tube formation, branching, shape remodelling, epithelial-mesenchyme transition, etc., may be deployed in many diverse cell types and many diverse contexts in development.

If we imagine a canonical differentiation gene battery to be structured as in Fig. 2a, how different will be the topology of a morphogenetic gene cassette? One possible clue comes from various studies on GRN linkages that execute transcriptional control of cell replication in developing systems. The spatial patterns of cell replication of course affect morphology, because the size and shape of given portions of a structure depend on the number of rounds of cell division mediated by the regulatory state in each developing region. In several cases the exact outputs of a developmental GRN that specifically control cell cycle activity have been determined. For example in developing pituitary, several linkages from the specification GRN directly control proliferation: the Pitx1 gene provides inputs into the cyclin D1 gene; the Six1 gene acts to repress expression of a cell cycle arrest kinase; and Six1 plus other factors of the pituitary regulatory state activate c-myc (also known as Myc). In the developing zebrafish eye the GRN linkage to cell cycle control is regulation of cyclin D1 and c-myc (also known as myca/mycb) by the meis1 regulatory gene. Thus, so to speak,
these GRNs deploy the complex process of cell division by pressing a small number of regulatory ‘buttons’.

Perhaps only a subfraction of the effector genes in a morphogenetic gene cassette are transcriptionally regulated by direct inputs from the upstream GRN. This concept emerged from a study of the migration of heart precursor cells in developing Ciona\textsuperscript{65}, one of the few system-level investigations we have into the transcriptional control of a morphogenetic function. A large number of cell biology genes participate in the processes of membrane protrusion and motility required for heart cell migration, but most of these genes are widely expressed. Migratory activity is specifically deployed by transcriptional activation of the rhoDF gene, which encodes a key required GTPase, and it is this gene which is directly controlled by the cis-regulatory outputs of the upstream GRN. The same principle is evident in a study of trichome formation in Drosophila\textsuperscript{66}. Here again, an extensive patterning GRN lies upstream, and determines the location of the morphological features and its cellular progenitors. The remodelling of epidermal cell shape to produce trichomes (or alternately, smooth cuticle) is controlled by expression of the regulatory gene shavenbaby (also known as ovo), and some of its direct effector gene targets are known. But these are again only a fraction of the total genes whose products are required to build the trichome. If these examples are a guide, the wiring of differentiation gene batteries, in which every downstream gene is a specific target of the GRN (Fig. 2a), is distinct from the way morphogenetic gene cassettes may be wired (Fig. 2b). Many of the genes contributing to a morphogenetic cell biology process may be widely expressed and only a few key ‘button’ genes that functionally nucleate the whole process are transcriptionally controlled by GRN outputs, to deploy the process spatially. Were this a general result, it would promise the existence of simple regulatory levers by which morphogenetic cassettes could be re-deployed, either in evolution or in re-engineering projects, to which we return below.

A uniquely explanatory GRN analysis of innate immunity response mechanisms in dendritic cells, following stimulation of Toll-like receptors (TLRs)\textsuperscript{67}, shows how a classic physiological response is programmed at the genomic level. Stimulation of TLRs 2, 3 and 4 with various agonists activates two partly overlapping response programs of effector gene expression, in other words an antiviral program and an inflammatory program. This study included all regulatory genes specifically involved in the process, and the architecture of the GRN was based on a comprehensive, quantitative perturbation analysis, using small hairpin RNAs (shRNAs) to block regulatory gene transcription, although no direct cis-regulatory validation of the GRN structure was reported. Several interesting differences and also similarities emerge in comparing the structure of this physiological response GRN to that of the developmental GRNs considered above. A salient similarity is in the structure of the effector gene sets. Like many differentiation genes, the TLR response effector gene sets are largely wired to their drivers in coherent feed forward loops. Another now familiar feature is the use of positive feedback that will lock down the regulatory state following a transient input, here between stat genes high up in the antiviral response GRN hierarchy. This GRN is of moderate depth: downstream of the stat genes are three other regulatory genes linked to the stat genes and to one another by cross-regulatory interactions, and downstream of these in turn are further regulatory genes, and then the effector genes. A further device in these GRNs that also is often used in development, is exclusion of the alternate regulatory state by specific cross-repression, once one of the pathways is active. The depth of the inflammatory hierarchy is only that of the feed forward circuitry. Physiological systems are homeostatic, and a special feature of this one is a self-cancelling repression circuit the sequence-specific basis of which is, however, yet unknown. Some years ago a prescient analysis predicted that in general, developmental GRNs which control progressive irreversible regulatory processes would have considerably greater depth than does reversible physiological response circuitry\textsuperscript{68}, and this turns out to be exactly true.
One way of summarizing the result of a comparative meta-analysis of GRNs controlling diverse kinds of biological processes is to consider their similarities and differences in the same terms: they are similar in that all the GRNs considered here are modular constructs of a basic repertoire of sub-circuit topologies (Table 1); but they differ in their global hierarchical organization, which reasonably reflects the biological jobs they execute.

**Insights into process from mathematical models of GRNs and sub-circuits**

Space confines the following discussion to recently conceived models based *ab initio* on experimentally generated, largely validated network topologies. The major focus is on how, or whether, mathematical analyses of the models has succeeded in enriching our understanding of the biological functionalities of the observed circuitry.

Beginning with a known network topology, the common objective is to generate a dynamic mathematical model, either using continuous (ordinary differential equations or ODE) or Boolean approaches. For large scale temporal models of embryonic spatial specification systems involving many genes and interactions, this often involves a great number of unmeasured parameters, and epistemological issues immediately arise. In many such works arbitrary parameter values are systematically explored until the expected results emerge, but this is inherently at least a partially circular logic, since it assumes a priori that the model is right. Of course where there are applicable experimental measurements of the output kinetics, the model is better constrained, but then the novelty of the biological insights that can be expected is limited because both the input relationships and the results are assumed. *Drosophila* gap gene expression in the syncytial embryo provides the best known large developmental data set thus far subjected to mathematical kinetic analysis. Extensive genetic and cis-regulatory data partially specify the embryonic interaction networks of these genes. Mathematical models were built assuming the network topologies proposed in prior work, and fit to a very high quality set of quantitative kinetic measurements which capture the empirical dynamics of changing gap expression patterns in the pre-cellularization 13th–14th cleavage cycle. There were two outcomes relevant to the structure/function relationships of this developmental GRN: First, a dynamic image of how the gap gene transcription factors operate emerged, illuminating what might be called the cell biology of the process (were there cells). Second, the analysis suggested several additions and corrections of unresolved details of gap gene interactions. But largely the outcome was just that if one does the math and the measurements, everything turns out to make sense.

An important area of developmental biology in which modelling has contributed novel mechanistic understanding is transcriptional response to signals. We cannot here deal with the many studies focused on dynamic spatial distributions of signal ligands *per se*. But mathematical analyses of models capturing transcriptional network circuitry downstream of intercellular signalling have illuminated developmental signal response in multiple ways. These models concern smaller and well constrained sub-circuits, rather than whole GRNs, and often either parameters can be reasonably approximated, or dimensionless approaches can be found. The signal-driven transcriptional patterning process by which the two dorsal respiratory appendages on the roof of the *Drosophila* egg are positioned affords an example. An experimentally based network circuitry animated by spatially confined epidermal growth factor (EGF) and Dpp signalling was used to produce a dynamic mathematical model which satisfactorily interprets the changing pattern of expression of a key gene of the pro-appendage regulatory state in dorso-anterior follicle cells. The model thus explains how this system generates and positions the bilateral spots of gene expression where the appendages will form, which is not otherwise transparent. Furthermore, in consequence of a conflict between prediction and experimental observations, the analysis
required a hitherto unsuspected positive feedback loop by which Dpp controls expression of its own receptor. A second example concerns transcriptional interpretation of graded hedgehog (Hh) signals in the developing neural tube, which results in a ventral to dorsal series of spatial regulatory state domains each of which gives rise to certain neuronal types. When experimental measurements of signal intensity over time in the various transcriptional domains were analysed mathematically, it emerged that the successive ventral to dorsal transcriptional domains are defined by the integrals over duration and intensity of Hh signalling, rather than simply on ‘morphogen concentration’, as always assumed previously. A third example relates to the Wnt signalling required in Xenopus embryos to activate key regulatory genes of the dorsal organizer. Experimental perturbations of this canonical developmental signalling system showed that this system responds to the ratio of the (signal) input at some given time, to its level when the signalling began (‘fold change’), and not to absolute signal level (the same phenomenon is often seen in other contexts, for example, sensory physiology). A predicted explanation in terms of network sub-circuit topology was then derived from a dynamic mathematical analysis of the incoherent feed forward sub-circuit, which showed that this commonplace sub-circuit possesses the capacity to respond to fold change in input magnitude, rather than to absolute input magnitude.

As noted above, another general area in which modelling has illuminated process in respect to given sub-circuit topology is in binary cell fate choice, following a precursor phase in which both regulatory states are weakly expressed. Here the repeatedly observed sub-circuit structure features the opposition of two antagonistic repressors, each, if highly expressed, capable of shutting off the alternative regulatory state and generating its own, and each animated by inputs that reflect the external need for its pathway. A canonical approach to dynamic mathematical modelling of this type of sub-circuit has been repeatedly applied, based essentially on treating transcriptional activation abstractly as a catalytic Michaelis–Menton process, and repression in the same vein (for example, refs. 38, 81). The object is to demonstrate that these ‘duelling repressor’ sub-circuit topologies indeed encode regulatory systems that are capable of hysteretically moving from the precursor state to one or the other terminal regulatory states, depending on the inputs the system receives. But a problem with this approach is that as conventionally formulated, the bi-stable mathematical behaviour requires the completely ad hoc assumption of large exponential (Hill) coefficients in the repression functions (that is, coefficients >2, and often much larger values have to be assumed in order to generate the expected behaviour). Although Hill coefficients of these magnitudes physically imply cooperativity, or additional (unknown) reactions, they are customarily inserted in the computations despite lack of any direct biological evidence for cooperativity or other physical features that would justify them. Indeed, in one recent study of another very similarly wired haematopoietic choice system, the erythroid/myeloid fate choice, it was pointed out that the specific, mutually repressive cis-regulatory interactions which were obtained are known not to be multimeric and cooperative, nor is there any other biochemical justification for high Hill coefficients. Instead an alternative regulatory architecture was considered, the dynamic mathematical analysis of which resulted in the prediction that the sub-circuit should include in addition to the antagonistic repressors another gene or genes operating according to specified network linkages. The latter work, furthermore, used a now classic probabilistic thermodynamic treatment of cis-regulatory transcription factor binding that is directly based on transcription factor–DNA interaction physical chemistry. This same thermodynamic approach to modelling cis-regulatory transcription factor binding has been used for analysis of an entirely different type of sub-circuit operating at the initial developmental appearance of pluripotential haematopoietic stem cells. This sub-circuit consists of three positively active genes. There are no cross-regulating repressors in this sub-circuit, and the three genes are linked by multiple positive auto- and cross-regulatory linkages. In life and in the model, extrinsic signals switch it
irreversibly into an active state; otherwise, if one node is inhibited, it remains off. Thus there are multiple different designs that confer signal-dependent bi-stability.

The thermodynamic binding approach was also used earlier for dynamic modelling of sea urchin embryo gene cascades. The important insight emerged that in a cascade where a given gene activates a second downstream gene, significant expression of the second gene occurs long before the product of the first gene reaches steady state, and the whole dynamic system operates in a ‘forward drive mode’ relatively insensitive to levels of upstream activators. The kinetics of such embryonic regulatory interactions are not narrowly determinate, as emphasized by the kinetic ‘sloppiness’ of a process which operates successfully at different rates at different temperatures within and between similar species, and in which there is a significant range in the concentrations of many transcription factors embryo to embryo.

For other situations in embryonic development where the object is to encompass a complex, large scale spatial specification system rather than to follow a given small domain or cell type through time, conventional, stand-alone dynamical analysis is the wrong tool for the job that really needs to be done. Returning to Table 1, for example, we see that there are several kinds of spatial specification sub-circuit, that in cellular early embryos produce novel spatial regulatory state patterns, for example X,1 − X spatial processing sub-circuits and AND spatial logic processors. These, and indeed many other embryonic specification processes that define multicellular territorial regulatory states, result in a progressive Boolean-like pattern of diverse regulatory states confronting one another sharply across territorial cellular boundaries. A model that would capture what the GRN really does must address this kind of outcome, capturing the encoded input information-processing behaviour at each cis-regulatory module of the GRN.

Current developmental GRNs mainly concern, on the one hand, far upstream hierarchical transactions that essentially execute regulatory state pattern formation, or on the other, far downstream differentiation gene batteries and their immediate governance. These will have to be much better linked, so that we have a continuous understanding of the control systems from the top of the hierarchy to all the effector genes of a developing system. This kind of global GRN will be much larger than anything we have at present. Other kinds of global GRNs are on the horizon as well, such as those that encompass all parts of a developing embryo through time. Experimentally validated GRNs that include complete large regulatory systems will present enormous computational challenges for modelling, presentation, logic analysis and modular abstraction.

**Developmental GRNs and evolutionary mechanism**

Because development of the body plan is caused by the operation of GRNs, evolutionary change in the body plan is change in GRN structure occurring over deep time. Evolution and development emerge as twin outputs of the same mechanistic domain of regulatory system genomics. It is therefore to be expected that, at the level of GRN structure, each would illuminate the other, and so indeed they already do in several concrete ways. To start, it is obvious that if there is indeed a finite repertoire of network sub-circuits used to effect development, the evolution of development has to be considered as the process of assembly, reassembly, and redeployment of these sub-circuits. This general idea will become directly testable by widespread evolutionary comparisons, as the GRNs underlying the development of diverse animal forms become available. Structural comparison of GRNs between forms of known phylogenetic relation in turn reveals the modularity of GRN structure, by revealing sub-circuit boundaries, as when a sub-circuit is inserted wholesale into a new GRN context. Furthermore, the sub-circuits of which GRNs
are composed change during evolution at different rates, highlighting the linkages belonging to the most conserved sub-circuit in a GRN comparison. As discussed elsewhere, in general the oldest GRN features are certain differentiation gene batteries\(^3\),\(^{88}\), which are eumetazoan (cnidarian + bilaterian) in distribution. In contrast, the morphogenetic programs that pattern each form of body plan are by definition clade-specific\(^88\). Certain remarkably conserved regulatory sub-circuits that are located near the top of developmental GRN hierarchy may serve to lock down developmental process specific to given phyla or classes (GRN kernels)\(^86–91\). Thus GRNs are historically as well as structurally and functionally modular, in that they are a mosaic of sub-circuits of diverse antiquity and phylogenetic distribution. Systematic exploration of phylogenetically related GRNs at different distances is valuable not only to discover the evolutionary origins of each sub-circuit, but also to reveal which kinds of sub-circuits and linkages are inherently flexible and which not. This brings us to the most important point for the future. In order to probe control of spatial regulatory state, laboratory strategies will need to be designed for changing GRNs by insertion of network regulatory apparatus into developing systems. But this is the same kind of change that happened in evolution, and the results will be mutually informative. Thus a practical convergence is on the horizon. Re-engineering spatial developmental processes, and recreating evolutionary processes, while different in motivation, will both depend on fundamental understanding and experimental manipulation of the structure/function relations of developmental GRNs.

The processes we have been discussing, development and evolution of the body plan, and execution of physiological responses, devolve causally from the regulatory genome. We need to understand GRNs because they encompass the primary output of the regulatory genome, itself the fundamental and unique outcome of more than 600 million years of animal evolution\(^88\).

Acknowledgments

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Figure 1. ‘Birdseye’ views of structural properties of representative developmental GRNs

**a**−**c**, Diagrammatic view of sub-circuits and sub-circuit functions in three different GRNs. Each box represents a GRN sub-circuit consisting of a small number of regulatory genes and their functional linkages. Coloured dots and numbers refer to the similarly coded sub-circuit types in Table 1. Red arrows indicate linkages between sub-circuits, that is, regulatory feeds from one sub-circuit to another. **a**, GRN for skeletogenic mesoderm lineage specification in sea urchin embryos\(^1\). **b**, GRN for pancreatic developmental process\(^3\), leading to β cell specification and insulin gene transcription. **c**, GRNs typical of terminal binary fate choices in haematopoietic stem cells and other similar situations, as discussed in text.
Figure 2. Structural characteristics of downstream effector gene cassettes and their control functions

a. Typical differentiation gene battery, as discussed elsewhere\(^3\). Here each effector gene codes for a cell-type-specific protein required to generate the cell-specific output. These effector genes are all transcribed specifically in the given cell type in response to a small number of regulatory factors, which are themselves the output of the controlling specification GRN. Every effector gene of the battery is specifically controlled by these inputs. The immediate drivers of the battery shown cross-regulate (as is often the case).

b. Structure that may be typical of morphogenetic effector gene cassettes. Here the output of the specification GRN is used to control transcription of only a minor fraction of key genes required for morphogenetic function.
effector genes, and these in some way trigger or nucleate the process. But many of the proteins required for the function are widely expressed.
Table 1

Sub-circuit repertoire for developmental GRNs

<table>
<thead>
<tr>
<th>Regulatory state specification function</th>
<th>Sub-circuits</th>
<th>What they do</th>
<th>Topologies</th>
</tr>
</thead>
<tbody>
<tr>
<td>X,1 − X processors</td>
<td>Double negative gate (^{1,2,6})</td>
<td>Install regulatory state in X domain, prohibit same state everywhere else (^{a})</td>
<td><img src="image" alt="Diagram" /></td>
</tr>
<tr>
<td></td>
<td></td>
<td>1.1</td>
<td><img src="image" alt="Diagram" /></td>
</tr>
<tr>
<td>Signal-mediated switch (^2)</td>
<td></td>
<td>Activate regulatory gene(s) in cells receiving signal, repress same genes everywhere else (^f)</td>
<td><img src="image" alt="Diagram" /></td>
</tr>
<tr>
<td></td>
<td></td>
<td>1.2</td>
<td><img src="image" alt="Diagram" /></td>
</tr>
<tr>
<td>Spatial subdivision</td>
<td>Inductive signaling (^2)</td>
<td>Activation of new regulatory genes in a cellular domain by transcriptional response to signal ligands produced by other cells</td>
<td><img src="image" alt="Diagram" /></td>
</tr>
<tr>
<td></td>
<td></td>
<td>2.1</td>
<td><img src="image" alt="Diagram" /></td>
</tr>
<tr>
<td>AND logic circuitry (^2)</td>
<td></td>
<td>Overlapping but spatially non-coincidental inputs are generated and both are required for regulatory gene activation, which occurs only in overlap subdomain</td>
<td><img src="image" alt="Diagram" /></td>
</tr>
<tr>
<td></td>
<td></td>
<td>2.2</td>
<td><img src="image" alt="Diagram" /></td>
</tr>
<tr>
<td>Spatial repression (^2)</td>
<td></td>
<td>Boundaries of spatial regulatory state domains controlled by transcriptional repression.</td>
<td><img src="image" alt="Diagram" /></td>
</tr>
<tr>
<td></td>
<td></td>
<td>2.3</td>
<td><img src="image" alt="Diagram" /></td>
</tr>
<tr>
<td>Dynamic lockdown of regulatory state (^5)</td>
<td>Reciprocal repression of state (^2,5,39,51)</td>
<td>In each spatial regulatory state domain key activators of alternative states are transcriptionally repressed by ‘exclusion’ circuitry (^g)</td>
<td><img src="image" alt="Diagram" /></td>
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<tr>
<td></td>
<td></td>
<td>3.1</td>
<td><img src="image" alt="Diagram" /></td>
</tr>
<tr>
<td>Feedback circuitry (^1)</td>
<td></td>
<td>Two or three regulatory genes engage in positive intergenic feedback, stabilizing regulatory state</td>
<td><img src="image" alt="Diagram" /></td>
</tr>
<tr>
<td></td>
<td></td>
<td>3.2</td>
<td><img src="image" alt="Diagram" /></td>
</tr>
</tbody>
</table>

\(^a\) Double negative gates and signal-mediated switches are examples of feedback circuits, which typically involve negative feedback to tune regulatory state specification (see below).

\(^f\) Reciprocal repression of state 1,2,9,39,51

\(^g\) ‘Exclusion’ circuitry.

\(^1\) Feedback circuitry.

\(^2\) AND logic circuitry.

\(^3\) Spatial repression.

\(^4\) Spatial subdivision.

\(^5\) Dynamic lockdown of regulatory state.

\(^6\) Signal-mediated switch.

\(^7\) Double negative gate.

\(^8\) Inductive signaling.

\(^9\) Reciprocal repression of state.

\(^10\) Feedback circuitry.

\(^11\) AND logic circuitry.

\(^12\) Spatial repression.

\(^13\) Spatial subdivision.

\(^14\) Dynamic lockdown of regulatory state.

\(^15\) Signal-mediated switch.

\(^16\) Double negative gate.

\(^17\) Inductive signaling.

\(^18\) Reciprocal repression of state.

\(^19\) Feedback circuitry.

\(^20\) AND logic circuitry.

\(^21\) Spatial repression.

\(^22\) Spatial subdivision.

\(^23\) Dynamic lockdown of regulatory state.

\(^24\) Signal-mediated switch.

\(^25\) Double negative gate.

\(^26\) Inductive signaling.

\(^27\) Reciprocal repression of state.

\(^28\) Feedback circuitry.

\(^29\) AND logic circuitry.

\(^30\) Spatial repression.

\(^31\) Spatial subdivision.

\(^32\) Dynamic lockdown of regulatory state.

\(^33\) Signal-mediated switch.

\(^34\) Double negative gate.

\(^35\) Inductive signaling.

\(^36\) Reciprocal repression of state.

\(^37\) Feedback circuitry.

\(^38\) AND logic circuitry.

\(^39\) Spatial repression.

\(^40\) Spatial subdivision.

\(^41\) Dynamic lockdown of regulatory state.

\(^42\) Signal-mediated switch.

\(^43\) Double negative gate.

\(^44\) Inductive signaling.

\(^45\) Reciprocal repression of state.

\(^46\) Feedback circuitry.

\(^47\) AND logic circuitry.

\(^48\) Spatial repression.

\(^49\) Spatial subdivision.

\(^50\) Dynamic lockdown of regulatory state.

\(^51\) Signal-mediated switch.

\(^52\) Double negative gate.

\(^53\) Inductive signaling.

\(^54\) Reciprocal repression of state.

\(^55\) Feedback circuitry.

\(^56\) AND logic circuitry.

\(^57\) Spatial repression.

\(^58\) Spatial subdivision.

\(^59\) Dynamic lockdown of regulatory state.

\(^60\) Signal-mediated switch.

\(^61\) Double negative gate.

\(^62\) Inductive signaling.

\(^63\) Reciprocal repression of state.

\(^64\) Feedback circuitry.

\(^65\) AND logic circuitry.

\(^66\) Spatial repression.

\(^67\) Spatial subdivision.

\(^68\) Dynamic lockdown of regulatory state.

\(^69\) Signal-mediated switch.

\(^70\) Double negative gate.

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<th>Sub-circuits</th>
<th>What they do</th>
<th>Topologies</th>
</tr>
</thead>
<tbody>
<tr>
<td>Community effect circuitry</td>
<td>Cells within a territory all signal to one another, driving continued</td>
<td>irrespective of transient inputs</td>
<td>3.3</td>
</tr>
<tr>
<td></td>
<td>uniform expression both of ligand gene and signal-dependent regulatory genes</td>
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<td></td>
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<tr>
<td>Boundary maintenance</td>
<td>Different signals are produced by apposing cells and their reception triggers</td>
<td>External inputs tip the balance of repressor expression, resulting in</td>
<td>4</td>
</tr>
<tr>
<td></td>
<td>repressive circuitry excluding the cross-boundary regulatory state</td>
<td>activation of one differentiation program and exclusion of the other</td>
<td></td>
</tr>
<tr>
<td>Terminal binary cell fate choice</td>
<td>Alternate sub-circuits driven by reciprocal repressors</td>
<td>Circuitry generates differential stimulation of expression of reciprocal</td>
<td>5</td>
</tr>
<tr>
<td></td>
<td></td>
<td>repressors in low versus high signal intensity</td>
<td></td>
</tr>
<tr>
<td>Discontinuous transcriptional response</td>
<td>Reciprocal repressor genes responding cooperatively to inducer</td>
<td>Circuitry generates irreversible transitions, in stem cell regulatory state,</td>
<td>6.1</td>
</tr>
<tr>
<td>to signal intensity and/or duration</td>
<td></td>
<td>off versus on in response to signals of different strength and duration</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Reciprocal repressor genes, one activating an additional repressor gene, each</td>
<td>Produces alternative regulatory states, or low level indeterminate state,</td>
<td></td>
</tr>
<tr>
<td></td>
<td>with variable external positive inputs</td>
<td>depending on different</td>
<td>6.2</td>
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<tr>
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</tr>
<tr>
<td>----------------------------------------</td>
<td>-------------</td>
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<td>------------</td>
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<tr>
<td>6.3 positive inputs</td>
<td></td>
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</tbody>
</table>

The role of the sub-circuit is given in column 1; its name in column 2; a description of its function in column 3; and the sub-circuit structure in column 4. Numbers in column 2 are keyed to Fig. 1. See references indicated for actual occurrences, exact circuit topologies, and discussion of information processing specifics. In each case the functions of the circuit are hardwired in its cis-regulatory target sites. In Topologies column, all genes encode transcription factors unless otherwise noted.

* Regulatory genes that create initial regulatory state are controlled by widely expressed repressor, which is dominant over their positive inputs, and gene encoding this repressor is itself specifically repressed in a local region (X) by another gene encoding a different repressor; hence target genes are ON in X, specifically repressed elsewhere.

† Many developmental signalling systems (for example, Notch, Wnt) activate immediate early response factors in cells receiving ligand, but in absence of ligand, these factors act as dominant repressors of the same target genes.

‡ Dynamic in that continuing transcription is required.

§ Exclusion sub-circuits are activated as downstream outputs of specification GRNs.

‖ A unique circuit design here is that the ligand gene is activated by the same signal transduction mechanism reception of the ligand activates in recipient cells; a positive intercellular feedback.

¶ From ref 2.

# L, gene encoding signalling ligand.

☆ R encodes repressor; L encodes signalling ligand.

** This example was adapted from Ref 36.

†† Conceived as a means of obtaining different discrete transcriptional responses from a graded signal; see discussion of this type of circuitry in section on mathematical models below.

‡‡ S, signal; triangle represents graded signal strength

§§ S₁, S₂, different signal inputs gene B is subject to additional transcriptional repression in certain regulatory states.

|| This design precludes necessity for ad hoc Hill coefficients as in 5, 6.1; see section on mathematical models below.

¶¶ Autoregulatory loops lock on whichever state the system goes to.