**Herschel** observations of ortho- and para-oxidaniumyl \((H_2O^+)\) in spiral arm clouds toward Sagittarius B2(M)**

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**ABSTRACT**

\(H_2O^+\) has been observed in its ortho- and para- states toward the massive star forming core Sgr B2(M), located close to the Galactic center. The observations show absorption in all spiral arm clouds between the Sun and Sgr B2. The average \(o/p\) ratio of \(H_2O^+\) in most velocity intervals is 4.8, which corresponds to a nuclear spin temperature of 21 K. The relationship of this spin temperature to the formation temperature and current physical temperature of the gas hosting \(H_2O^+\) is discussed, but no firm conclusion is reached. In the velocity interval 0–60 km s\(^{-1}\), an ortho/para ratio of below unity is found, but if this is due to an artifact of contamination by other species or real is not clear.

**Key words.** astrochemistry – line: profiles – molecular processes

1. **Introduction**

Simple di- and triatomic molecules and ions are fundamental constituents of interstellar chemistry which eventually leads to the formation of complex molecules. Many of these species have ground state transitions at submillimeter- and THz wavelengths, and are therefore either difficult or not at all observable from the ground, yet they constitute the building blocks of chemistry, and are therefore fundamental to its understanding in various environments. Among those are spiral arm clouds, located in the plane of the Galactic disk, where the line-of-sight toward a strong continuum source passes through by chance. This setup allows sensitive absorption measurements, and the clouds have been observed by this method against the Sgr B2, W31c, W49, W51 and CasA millimeter continuum sources using molecular species such as CO, HCN, HCO\(^+\), CS, CN, SO, and \(c\)-C\(_2\)H\(_2\) etc (e.g. Greaves & Williams 1994; Tieftrunk et al. 1994; Greaves & Nyman 1996; Menten et al. 2010; Gerin et al. 2010; Ossenkopf et al. 2010). The results demonstrate that spiral arm clouds have low gas density and low excitation temperatures, and represent diffuse and translucent clouds.

One of the best sources for these absorption studies is Sgr B2, located close to the Galactic center, \(\sim 100\) pc from Sgr A\(^+\) in projection, and one of the strongest submillimeter sources in the Galaxy (e.g. Pierce-Price et al. 2000). The dense cores Sgr B2(N) and Sgr B2(M) within the cloud are at different evolutionary stages, and constitute well-studied massive star forming regions in our Galaxy. The flux ratio of the continuum between Sgr B2(M) and Sgr B2(N) is less than unity at 1 mm and rises at shorter wavelengths so that Sgr B2(M) dominates above \(\sim 500\) GHz (Goldsmith et al. 1990; Lis & Goldsmith 1991). Sgr B2(M) also shows fewer molecular emission lines than Sgr B2(N) (Nummelin et al. 1998), hence less confusion and therefore is better suited for absorption studies. The line-of-sight toward the Sgr B2(M) continuum will pass almost all the way to the center of our Galaxy, providing a more complete census in studying physical and chemical conditions towards the Galactic center clouds and all spiral arm clouds simultaneously. HIFI, the Heterodyne Instrument for the Far-Infrared (de Graauw et al. 2010) on board the *Herschel* Space Observatory (Pilbratt et al. 2010) is an ideal instrument for making these observations.

2. **Observations**

Full spectral scans of HIFI bands 1a, 1b, and 4b toward Sgr B2(M) (\(\alpha_{2000} = 17^h47\min20.35\sec\) and \(\delta_{2000} = -28\deg23'03.0''\)) have been carried out respectively on March 1, 2, and 5 2010, providing coverage of the frequency range 479 through 637 GHz and 1051 through 1121 GHz. HIFI spectral scans are carried out in dual beam switch (DBS) mode, where the DBS reference beams lie approximately...
3\textdegree apart. The wide band spectrometer (WBS) is used as a back-end, providing a spectral resolution of 1.1 MHz over a 4-GHz-wide intermediate frequency (IF) band. A HIFI spectral scan consists of a number of double-sideband (DSB) spectra, tuned at different local oscillator (LO) frequencies, where the spacing between one LO setting and the next is determined by the “redundancy” chosen by the observer (Comito \& Schilke 2002). The molecular spectrum of Sgr B2(M) in band 1a and 4b has been scanned with a redundancy of 4, that of band 1b with a redundancy of 8, which means that every frequency has been observed respectively 4 and 8 times in each sideband. Multiple observations of the same frequency at different LO tunings are necessary to separate the lower-sideband (LSB) from the upper-sideband (USB) spectrum.

The data have been calibrated through the standard pipeline released with version 2.9 of HIPE (Ott et al. 2010), and subsequently exported to CLASS\textsuperscript{1} using the HiClass task within HIPE. Deconvolution of the DSB data into single-sideband (SSB) format has been performed on CLASS. All the HIFI data presented here, spectral features and continuum emission, are deconvolved SSB spectra. Although both horizontal (H) and vertical (V) polarizations have been obtained, we will show only H-polarization spectra. The intensity scale is main-beam temperature, and results from applying a beam efficiency correction of 0.69 for band 1a, 0.68 for band 1b, and 0.669 for band 4b (Roelfsema et al. 2010).

3. Spectroscopy of H$_2$O$^+$

Removal of an electron from oxidane, H$_2$O, also known as water, yields oxidiumyl, H$_2$O$^+$. Its bond lengths and bond angle are slightly larger than those of H$_2$O, see e.g. Strahan et al. (1986). Quantum-chemical calculations (Weis et al. 1989) yielded a ground state dipole moment of $\sim$2.4 D, considerably larger than in H$_2$O. The transitions are of $b$-type, meaning $\Delta K_a \equiv \Delta K_c \equiv 1 \pmod{2}$. The electronic ground state changes from $^1\text{A}_g$ in the neutral to $^2\text{B}_1$ in the cation which leads to a reversal of the ortho and para levels with respect to water. $K_a + K_c$ is even and odd for ortho- and para-H$_2$O$^+$, respectively. The para levels do not show any hyperfine splitting while the ortho levels are split into three because of the $^1\text{H}$ hyperfine structure. The strong lines have $\Delta F = \Delta J = \Delta N$, i.e. they do not involve a spin-flip. At low quantum numbers spin-flipping transitions have appreciable intensity.

Further details of the spectroscopy of H$_2$O$^+$ are discussed in the Appendix. Table A.1 provides calculated rest frequencies for the two rotational transitions discussed in the present investigation. Figure A.1 shows the lowest energy levels of H$_2$O$^+$ with allowed transitions.

4. Results

Determining the opacities and thus column densities of absorption lines is traditionally done using the line-to-continuum ratio. In the present case, this is not straightforward, because the ortho-H$_2$O$^+$-line has hyperfine structure with closeby components (Fig. 1), which distorts the simple correspondence of line-to-continuum ratio with column density at a given velocity, and also because the line background of the Sgr B2(M) core cannot necessarily be neglected. We therefore fitted the lines using the XCLASS\textsuperscript{2} program, which performs an LTE fit using the molecular data discussed in Sect. 3, using the automated fitting routine provided by MAGIX\textsuperscript{3}. For all velocity components, an excitation temperature of 2.7 K was assumed. For molecules that react strongly with H$_2$ (see the discussion in Black 1998; Stäuber & Bruderer 2009), the collisional processes in diffuse gas are unimportant relative to radiative excitation in controlling the excitation temperatures of observed transitions of species with high dipole moments such as H$_2$O$^+$, since inelastic collisions with H, H$_2$ and electrons compete with reactive collisions. The excitation temperature employed here may still not be entirely correct, since particularly at 1115 GHz the general FIR background of the Galaxy contributes to a radiation temperature of 4.8 K even in the vicinity of the Sun, and for the spiral arm clouds one expects similar or slightly higher values (Wright et al. 1991; Paladini et al. 2007). Our analysis is not affected however if the excitation temperature is dominated by this radiation field, and stays significantly smaller compared with the upper level energies for the para- and ortho-H$_2$O$^+$ ground state lines $h\nu/k = 29$ and 54 K, respectively, which is a well justified assumption. The maximum opacities of the ortho-H$_2$O$^+$ line are about 2, so the lines are only moderately opaque.

For para-H$_2$O$^+$, only the 607 GHz line was used to perform the fit, since this is the strongest and least contaminated para-line, but it can be seen from Fig. 2 that predictions from this reproduce the other para lines rather well. To predict contamination, we used the fit of all species in Sgr B2(M) (Qin et al., in prep.) as background. This is a preliminary version of the fit, and we cannot exclude the existence of additional contamination by unknown lines. Thus we estimate the error of the fit due to uncertainties of this nature very conservatively to be 20%, but in the presence of strong unknown lines it could be larger at certain frequencies. This is particularly true for the possible D$_2$O contamination of the para-H$_2$O$^+$-line at 607 GHz. The relatively small variation of the ortho/para ratio in the absorption cloud range (see below) argues against contamination by a strong unknown line however. All para-H$_2$O$^+$ components are optically thin. In the following, we make the assumption that the excitation of all upper levels can be approximated as LTE with an excitation temperature of 2.7 K, and that thus the ortho- and para-H$_2$O$^+$ lines have the same excitation temperature.

\textsuperscript{1} Continuum and Line Analysis Single-dish Software, distributed with the GILDAS software, see http://www.iram.fr/IRAMFR/GILDAS.

\textsuperscript{2} We made use of the myXCLASS program (https://www.astro.uni-koeln.de/projects/schilke/XCLASS), which accesses the CDMS (Müller et al. 2001, 2005 http://www.cdms.de) and JPL Pickett et al. 1998 http://spec.jpl.nasa.gov) molecular data bases.

\textsuperscript{3} https://www.astro.uni-koeln.de/projects/schilke/MAGIX
para-H$_2$O$^+$ column densities can be measured by observations of the ground state. This assumption is reasonable for the spiral arm clouds, but most likely violated for the clouds associated with the Sgr B2(M) envelope (see below).

It appears that the absorption lines of different species toward Sgr B2(M) cannot be fitted with a unique set of physical components of fixed velocity and velocity width. This probably reflects the different origins of the species in atomic, low density molecular and high density molecular gas with a different velocity structure. A detailed study of the different distributions will have to await the complete data set of the survey. Apart from that, particularly in species which have hyperfine structure and are very abundant, that is in species which absorb at all velocities, the decomposition into basically Gaussian components would not necessarily be unique. The fit rather represents a deconvolution of the hyperfine pattern. We therefore prefer to present the results as depicted in Fig. 3, as column densities/velocity interval and ratio as a function of velocity, as a sum over the components. The component of the Sgr B2(M) envelope, which is located at 64 km s$^{-1}$, is most uncertain, because here the para-H$_2$O$^{+}$ 607 GHz line is most contaminated, and there the assumption of uniformly low excitation temperature for all levels is most likely to be violated, since this is warm and dense gas with a strong FIR field which may dominate the excitation.

Since H$_2$O$^+$ is expected to originate in mostly atomic gas at the edge of diffuse and translucent clouds, giving abundances relative to H$_2$ or H does not make sense, since it exists neither in purely atomic, nor in purely molecular gas. Menten et al. (2010) and Qin et al. (2010) give column densities of H$_2$ of typically a few times 10$^{21}$ cm$^{-2}$ and H column densities of typically 10$^{25}$ cm$^{-2}$, so the average H$_2$O$^+$ abundance relative to the number of H nuclei is a few times 10$^{-8}$, but could be much higher locally. The o/p ratio was calculated using the column densities, and has a mean of 4.8 ± 0.5 for the spiral arm clouds, with little variation.

We calculated the nuclear spin temperature using

$$\frac{N(ortho-H_2O^+)}{N(para-H_2O^+)} = e^{\Delta E/kT_{nuclear}} \frac{Q_o}{Q_p}$$

(1)

with $\Delta E = 30.1$ K, and $Q_{o,p}$ the partition function of ortho-H$_2$O$^+$/para-H$_2$O$^+$, respectively, given in the Appendix. The $Q_{o,p}$ include the rotational and nuclear spin part, and are referenced to a ground state energy of zero for both. Toward the spiral arm clouds, we find the mean nuclear spin temperature to be almost constant at 21 ± 2 K. At this temperature range, the ratio of the partition functions is almost equal to one, and the temperature is mostly determined by the exponential factor.

In the velocity range from about 0 to 60 km s$^{-1}$, the o/p ratio drops to unity, much below the high-temperature limit of 3. This does not reflect any thermal equilibrium and cannot be explained by any known formation mechanism: at low temperatures, the o/p ratio is extremely high, since all the molecules are in their lowest (ortho) state, and at high temperatures the limit 3 is reached, given by the nuclear spin statistics. We can only speculate about the cause of this unexpected result: it could be either a measurement error, or a real effect. If it is a measurement error, either the ortho-H$_2$O$^+$ column density is underestimated, which could be caused by contamination from a strong emission line, or the para-H$_2$O$^+$ column density is overestimated, which could be due to contamination from another absorption line, or the excitation temperatures deviate from the 2.7 K we assumed in such a way to produce this effect. The latter could e.g. be produced by a bright FIR field at the location of the clouds. Taking the measured ratio at face value as the o/p ratio would imply that a process exists which produces ortho-H$_2$O$^+$ and para-H$_2$O$^+$ in equal amounts.

5. Discussion

Since there are no fast radiative transitions between para-H$_2$O$^+$ and ortho-H$_2$O$^+$, the derived nuclear spin temperature is thought to be determined by chemical processes, either at formation or afterwards, since para-ortho transformation can only occur accompanied with a proton exchange reaction of one of the hydrogen nuclei. The only observed kinetic temperature estimates in these clouds are from Tieftrunk et al. (1994), based on NH$_3$, and show values of 35 ± 5 K in the ~100 km s$^{-1}$ component (which is believed to originate in the Galactic center), below 20 K in the velocity range in the spiral arm clouds, while the ~10 to 20 km s$^{-1}$ component (also from the Galactic center) has temperatures exceeding 100 K (Gardner et al. 1988), and is most likely shock heated. There is no similarity to the more or less constant nuclear spin temperature of 21 K we derive for H$_2$O$^+$ formation in this range, which suggests that H$_2$O$^+$ and NH$_3$ trace very different gas components: H$_2$O$^+$ the warm outer photon dominated edge of clouds, NH$_3$ either the shielded and cold interior, or hot shocked gas, which also seems to be devoid of H$_2$O$^+$. This picture of H$_2$O$^+$ formation at the edges of clouds, actually
in regions where the gas is mostly atomic, is supported by Gerin et al. (2010) and Neufeld et al. (2010) based on studies of OH+ and H2O+ with Herschel/HIFI. PDR models of diffuse clouds (Le Petit et al. 2006) predict temperatures of 50 to 100 K for the formation region of H2O+ in diffuse clouds (AV ≳ 1–3) with densities of about 102 and 103 cm−3 with radiation fields of 1–3 times ambient.

The relationship of nuclear spin temperature and formation or ambient temperature needs to be discussed in somewhat more detail (see Flower et al. 2006, for a discussion on this ratio for molecular hydrogen). H2O+ is a very reactive ion, and particularly it reacts exothermically with H2 to form H3O+, so the reaction para−H2O+ + H2 → ortho−H2O+ + H2, which would equilibrate the o/p ratio to the kinetic gas temperature, might not be relevant. If an equivalent reaction with atomic hydrogen (para−H2O+ + H → ortho−H2O+ + H) could happen, is unknown. If it does, it most likely will equilibrate to the current gas temperature, if not, the observed o/p ratio is the one established at formation. How this depends on the kinetic temperature at formation is not well understood. H2O+ is produced by the highly exothermic reaction of OH+ with H2, so the variables determining the H2O+ o/p ratio are:

1. the o/p ratio of H2;
2. how much and in which way the excess energy of the exothermic reaction is available for o/p conversion of H2O+; 3. the temperature of the gas at the time of formation, typically above 50–100 K based on PDR models.

The latter two processes would push the o/p ratio down toward 3:1, the high temperature value, which means toward a spin temperature higher than the 21 K we measure. The influence of the o/p ratio of H2 is hard to assess: if the reaction proceeds by way of a collision complex, then the nuclear spin of H2 will have an effect on the nuclear spin of product H2O+, but not if the reaction proceeds through direct atom transfer. The measured o/p of H2 in diffuse clouds is about unity (Savage et al. 1977; Rachford et al. 2009). Clearly, this is an interesting area of molecular physics that needs further study. From our observations, it seems that we see an excess of ortho−H2O+ relative to what one would expect based on the formation temperature and available reaction energy in the spiral arm clouds and, if the measurement of an ortho−H2O+/para−H2O+ ratio in the 0 to 60 km s−1 region is real, an excess of para−H2O+. This velocity range is nominally assigned to the Sagittarius/Cuttern arm systems (Vallée 2008), outside of the Galactic center, where no exotic conditions are expected. However, this velocity range is also bracketed by gas local to Sgr B2 at 0 to 10 km s−1 and around 60 km s−1, so it could represent diffuse gas belonging to this complex, which could be the cause of unusual excitation or chemical conditions, e.g. due to shocks. In the lower velocity range overlapping with this (~10 to 20 km s−1), Lis et al. (2010) also find water with an o/p ratio of 3, indicating high temperatures.

Lis et al. (2010) find an average spin temperature of 27 K for water toward the the spiral arms lines of sight. H2O in these clouds is formed in the gas phase, through dissociative recombination of H2O+, in a region where the gas is at about this temperature. The correspondence between physical temperature and spin temperature may be more easily traced by the more stable water molecule, although in general the contribution of grain surface chemistry for water complicates the issue (see discussion in Lis et al. 2010). From this study it is clear that by determining the ortho/para-ratio of H2O+ (and, by proxy, from other simple hydrides) one can learn a lot about the formation processes, but also that many fundamental physical and chemical processes are still not fully understood. We can look forward to the wealth of data HIFI will bring!

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References


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Appendix A: The spectroscopy of H₂O⁺

The rotational spectrum of oxidaniumyl was measured by laser magnetic resonance (LMR) (Strahan et al. 1986; Mürtz et al. 1998); further infrared and electronic spectral measurements have been summarized in Zheng et al. (2008). Observations of the N,J,K = 1,1,0 transition, J = 1.5–0.5 fine structure component near 1115 GHz with Herschel/HIFI (Ossenkopf et al. 2010) as well as subsequent observations raised the issue which of the two sets of spectroscopic parameters from LMR measurements provide more reliable frequency predictions. Latest observations as well as reinterpretations of older ones favor the parameters from Mürtz et al. (1998) even though there seem to be small discrepancies of order of ±5 MHz or 1.35 km s⁻¹ between various observations for the specific transition mentioned above. Observations carried out toward Sgr B2(M) or Orion KL for the HEXOS program are probably less suited to derive rest frequencies than certain other observations. Therefore, a preliminary catalog entry has been constructed for the CDMS catalog (Müller et al. 2001, 2005); the final entry is intended to be a common CDMS and JPL (Pickett et al. 1998) catalog entry.

All infrared data and all ground state combination differences (GSCDS) derived from electronic spectra as summarized in Zheng et al. (2008) were used in the fit as long as they were deemed reliable. These data are uncertain to between 0.005 and 0.030 cm⁻¹ or between 150 and 900 MHz. Mürtz et al. (1998) provided for their measured data extrapolated zero-field frequencies as well as residuals between observed and calculated frequencies along with uncertainties. From these data weighted averages of the hypothetical experimental zero-field frequencies and of their uncertainties were derived; these uncertainties were of order of 2 MHz with a considerable scatter. Strahan et al. (1986) do not give sufficient data for this purpose. However, Mürtz et al. (1998) published calculated frequencies for the 111−000 transition. Because of the importance of this transition for the astronomical observation as well as for the fit, these calculated frequencies were also used in the fit with presumable uncertainties corresponding to 2 MHz. The quantum numbers, calculated frequencies, and uncertainties for the two observed rotational transitions are given in Table A.1. Even though the LMR data fit well within their uncertainties, the calculated frequencies should be viewed with some caution because it is not clear how reliable the zero-field extrapolation is. Moreover, the large centrifugal distortion effects affecting the spectra of this ion require additional caution with respect to any extrapolation. It is worthwhile mentioning that the 111−000 frequency transitions in that table are essentially identical to the ones given in Mürtz et al. (1998). The situation is different for the 100−010 transition. The J = 1.5–1.5 fine structure splitting derived from term values given in Table V of Mürtz et al. (1998) differs from the value in Table A.1 by less than 4 MHz whereas the remaining fine structure intervals differ by up to 80 MHz. On the other hand, calculations directly from the Mürtz et al. (1998) parameters differ from values in Table A.1 by less than 10 MHz. As can be seen in Fig. A.1, the ground state para level 100 of H₂O⁺ is ~30.13 and 30.01 K above the 000 level for the J = 0.5 and 1.5 fine structure components respectively. Both para and ortho ground state levels are split into 2 because of the fine and hyperfine structure splitting, respectively. The quantum numbers are 0.5 and 1.5 in both cases, giving g = 2 and 4, respectively, and hence Q ~ 6 at low temperatures if ortho and para states are treated independently. This 1 : 1 ratio for Q at low temperatures approaches 3 : 1 at room temperature; it is about 1.5:1 and 2:1 at ~40 and 75 K, respectively. Table A.2 gives selected partition function values for para- and ortho-H₂O⁺, assuming they are completely non-interacting species.

The mixing of ortho and para states can be mediated by terms such the off-diagonal electron spin-hydrogen nuclear spin coupling term T_{ab} or the off-diagonal hydrogen nuclear spin coupling term C_{ab} + C_{ba}. The radical NH₂ and PH₂ are isoelectronic and isovalent to H₂O⁺. Model calculations have shown the largest perturbations to occur between the 100 and 111 levels, but

<table>
<thead>
<tr>
<th>N, K, J’a</th>
<th>N, K, J”a</th>
<th>J = F’ − F”</th>
<th>F’ − F”</th>
<th>frequency</th>
<th>E₂0</th>
<th>A</th>
</tr>
</thead>
<tbody>
<tr>
<td>100−000</td>
<td>100</td>
<td>1.5−0.5</td>
<td>b</td>
<td>604678.6 (25)</td>
<td>0.005</td>
<td>1.3</td>
</tr>
<tr>
<td>1.5−1.5</td>
<td>b</td>
<td>607227.3 (19)</td>
<td>0.000</td>
<td>6.2</td>
<td></td>
<td></td>
</tr>
<tr>
<td>0.5−0.5</td>
<td>b</td>
<td>631724.1 (37)</td>
<td>0.005</td>
<td>5.6</td>
<td></td>
<td></td>
</tr>
<tr>
<td>0.5−1.5</td>
<td>b</td>
<td>634272.9 (24)</td>
<td>0.000</td>
<td>2.8</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Notes. (a) Numbers in parentheses are 1σ uncertainties in units of the least significant figures. These values should be viewed with some caution, in particular for the para transition, see text. (b) F is redundant for para transitions; F = J may be assumed. The lowest para state is 30.01 K above the lowest ortho state.

Fig. A.1. Detail of the energy level diagram of H₂O⁺. Hyperfine splitting has been omitted for the ortho-levels. Rotational level assignments N,J,K are given below the levels, fine structure level assignments J to the side. Magenta arrows mark transitions observed in the course of the present investigation. All other transitions shown can be observed with HIFI. The thickness of the arrows indicates the relative strengths of the transitions and the numbers the approximate frequencies. Frequencies of the weaker components are given in parentheses. The only transitions connecting to levels with N = 1 which are not shown are 211−100 and 200−111 near 2.85 and 3.0 THz which are not observable with HIFI but with PACS.
Table A.2. Partition functions for para- and ortho-H$_2$O$^+$, assuming LTE.

<table>
<thead>
<tr>
<th>$T$</th>
<th>$Q$(para)</th>
<th>$Q$(ortho)</th>
</tr>
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<tbody>
<tr>
<td>300.0</td>
<td>109.1787</td>
<td>296.3567</td>
</tr>
<tr>
<td>225.0</td>
<td>73.4887</td>
<td>192.9372</td>
</tr>
<tr>
<td>150.0</td>
<td>43.0579</td>
<td>105.7512</td>
</tr>
<tr>
<td>75.0</td>
<td>19.0770</td>
<td>38.3647</td>
</tr>
<tr>
<td>37.5</td>
<td>10.4751</td>
<td>14.5910</td>
</tr>
<tr>
<td>18.750</td>
<td>7.3879</td>
<td>7.3124</td>
</tr>
<tr>
<td>9.375</td>
<td>6.2329</td>
<td>6.0584</td>
</tr>
<tr>
<td>5.000</td>
<td>5.9680</td>
<td>5.9982</td>
</tr>
<tr>
<td>2.725</td>
<td>5.9123</td>
<td>5.9961</td>
</tr>
</tbody>
</table>

they are with less than 5 (Gendriesch et al. 2001) and less than 3 kHz (Margulès et al. 2002), respectively, rather small, maybe even negligible. Model calculations suggest that perturbations of the two rotational transitions described in the present study are less than 3 kHz. Slightly larger perturbations may occur at higher quantum numbers.