Observation of the $Y(1^3D_J)$ bottomonium state through decays to $\pi^+\pi^-Y(1S)$

Based on $122 \times 10^6 Y(3S)$ events collected with the BABAR detector, we have observed the $Y(1^3D_J)$ bottomonium state through the $Y(3S) \to \gamma \gamma Y(1^3D_J) \to \gamma \gamma \pi^+\pi^- Y(1S)$ decay chain. The significance for the $J = 2$ member of the $Y(3S)$ triplet is 5.8 standard deviations including systematic uncertainties.
The mass of the $J = 2$ state is determined to be $10.164.5 \pm 0.8\text{(stat)} \pm 0.5\text{(syst)}$ MeV/c$^2$. We use the $\pi^+\pi^-$ invariant mass distribution to confirm the consistency of the observed state with the orbital angular momentum assignment of the $Y(1^3D_j)$.

Heavy quark bound states below open flavor thresholds provide a key probe of the interactions between quarks. The mass spectrum and branching fractions of these states can be described by potential models and quantum chromodynamics [1–3]. S-wave and P-wave bottomonium ($b\bar{b}$) states were first observed in the 1970s and 1980s. Only recently [4] has a D-wave bottomonium state, the triplet $Y(1^3D_j)$ [5], been observed, where $J = 1, 2, 3$. The separation between the members of the triplet (intrinsic widths about 30 keV/c$^2$) is expected to be on the order of 10 MeV/c$^2$ [2]. A single state, interpreted to be the $J = 2$ member of the $Y(1^3D_j)$ triplet, was observed [4] by the CLEO Collaboration in the radiative $Y(1^3D_j)\to \gamma \gamma Y(1S)$ decay channel, but the quantum numbers $L$ and $J$ [5] and parity $P$ were not verified.

In this paper, we report the observation of the $J = 2$ state of the $Y(1^3D_j)$ in the hadronic $\pi^+\pi^- Y(1S)$ decay channel, with $Y(1S) \to \ell^+\ell^-$ ($\ell = e, \mu$). This decay channel has been of interest for decades [2,6–8]. Predictions for the branching fraction vary widely [6–8]. It provides better mass resolution than the $\gamma\gamma Y(1S)$ channel and allows $L$, $J$, and $P$, for which there is currently no experimental information, to be tested, through measurement of the angular distributions of the $\pi^\pm$ and $\ell^\pm$. The only previous result for this channel is the 90% confidence level (C.L.) branching fraction upper limit $B_{Y(1S)\to\gamma\gamma Y(1^3D_j)} \times B_{Y(1^3D_j)\to\pi^+\pi^- Y(1S)} \times B_{Y(1S)\to\ell^+\ell^-} < 6.6 \times 10^{-6}$ [4].

The analysis is based on a sample of $(121.8 \pm 1.2) \times 10^6$ $Y(3S)$ decays collected with the BABAR detector at the PEP-II asymmetric-energy $e^+e^-$ storage rings at the SLAC National Accelerator Laboratory, corresponding to an integrated luminosity of 28.6 fb$^{-1}$. The BABAR detector is described elsewhere [9]. Monte Carlo (MC) event samples that include simulation of the detector response are used to determine the signal and background characteristics, optimize selection criteria, and evaluate efficiencies. Pure electric-dipole transitions [10] are assumed when generating radiative decays.

The $Y(1^3D_j)$ in our study are produced through $Y(3S) \to \gamma \chi_{bJ}(2P) \to \gamma Y(1^3D_j)$ transitions, with $J' = 0, 1, 2$. To reconstruct the $Y(3S) \to \gamma\gamma\pi^+\pi^-\ell^+\ell^-$ final states, we require exactly four charged tracks in an event, two of which are identified as pions with opposite charge and the other two as either an $e^+e^-$ or $\mu^+\mu^-$ pair. Pion candidates must not be identified as electrons. To reject Bhabha events with bremsstrahlung followed by $\gamma$ conversions, we require the cosine of the polar angle of the electron with respect to the $e^-$ beam direction to satisfy $\cos\theta_{e^-} < 0.8$ in the laboratory frame. To improve the $e^\pm$ energy measurements, up to three photons are combined with $e^\pm$ candidates to partially recover bremsstrahlung [11].

The $Y(1S)$ candidate is selected by requiring $-0.35 < m_{e^+e^-} - m_{Y(1S)} < 0.2 \text{ GeV/c}^2$ or $|m_{\mu^+\mu^-} - m_{Y(1S)}| < 0.2 \text{ GeV/c}^2$, where the invariant mass of the lepton pair $m_{e^+e^-}$ is then constrained to the nominal $Y(1S)$ mass value [12]. The pion pair is combined with the $Y(1S)$ candidate to form a $Y(1^3D_j)$ candidate (mass resolution $3 \text{ MeV/c}^2$). To eliminate background from $\gamma \to e^+e^-$ conversions in which both the $e^+$ and $e^-$ are misidentified as pions, we reject events with a cosine for the laboratory $\pi^+\pi^-$ opening angle $\cos\theta_{\pi^+\pi^-}$ greater than 0.95 if the converted $e^+e^-$ mass is less than 50 MeV/c$^2$ and events with a laboratory angle between the $\pi^+\pi^-$ pair and $\ell^-$ that satisfies $|\cos\theta_{\ell^-\pi^+\pi^-}| > 0.98$.

Photons from $Y(3S) \to \gamma \chi_{bJ}(2P) \to \gamma Y(1^3D_j)$ decays have energies between 86 and 122 MeV [12] (80 and 117 MeV [2]) in the $Y(3S)$ center-of-mass (c.m.) frame. Our resolution for 80 MeV photons is about 6.6 MeV. We require at least two photons in an event: one (the other) with c.m. energy larger than 70 MeV (60 MeV). Photons from final-state radiation are rejected by requiring the cosines of the laboratory angles between the cascade photons and leptons to satisfy $\cos\theta_{\ell^-\gamma} < 0.98$. In the case of multiple photon combinations, we choose the one that minimizes $\chi^2 = \sum_i (E_{i\text{exp}} - E_{i\text{MC}})^2/\sigma_{E_i}^2$, where $E_{i\text{exp}}$ are the nominal [12] for $Y(3S) \to \gamma \chi_{bJ}(2P)$ or expected [2] for $\chi_{bJ}(2P) \to \gamma Y(1^3D_j)$ photon energies that correspond to one of the six possible $Y(3S) \to \gamma \chi_{bJ}(2P) \to \gamma\gamma Y(1^3D_j)$ transition paths allowed by angular momentum conservation, with $E_{\gamma}$ the measured energies (resolutions). We verified that the $\chi^2$ procedure does not bias our results, using simulated data samples in which the assumed $Y(1^3D_j)$ mass values are varied.

The $Y(1^3D_j)$ candidate is combined with the two photons to form a $Y(3S)$ candidate, whose c.m. momentum must be less than 0.3 GeV/c. The $Y(3S)$ mass is then constrained to its nominal value [12]. The $Y(3S)$ laboratory energy (resolution 25 MeV) is required to equal the summed $e^+$ and $e^-$ beam energies to within 0.1 GeV.

We identify four background categories within our fit interval $10.11 < m_{\pi^+\pi^-\ell^+\ell^-} < 10.28 \text{ GeV/c}^2$; $Y(3S)$ decays to (I) $\gamma \chi_{bJ}(2P)$ with $\chi_{bJ}(2P) \to \omega Y(1S)$ and $\omega \to \pi^+\pi^-\pi^0\pi^0$, (II) $\pi^+\pi^- Y(1S)$ with final-state radiation, (III) $\eta Y(1S)$ with $\eta \to \pi^+\pi^0\pi^0\gamma$, and (IV) $\gamma\gamma Y(2S)$.
or $\pi^0\pi^0 Y(2S)$ with $Y(2S) \rightarrow \pi^+\pi^- Y(1S)$. Categories I and II are the main backgrounds.

An extended unbinned maximum likelihood fit is applied to the sample of 263 events in the fit interval. The fit has a component for each of the three $Y(1^3D_J)$ signal states and four background categories. The likelihood function is

$$L = \exp(-\sum n_j \prod_{j=1}^{\infty} \frac{1}{\mathcal{P}_j!} \frac{1}{\mathcal{P}_j} (m_i)),$$

where $N$ is the number of events, $n_j$ is the yield of component $j$, and $\mathcal{P}_j$ is the probability density function (PDF) for component $j$, and $m$ is the $\pi^+\pi^- \ell^+\ell^-\gamma$ invariant mass.

The PDFs are derived from MC simulations. Each signal PDF is parameterized by the sum of two Gaussians and the crystal ball function [13]. For background category I, we use the sum of a crystal ball function, which describes the $\omega \rightarrow \pi^+\pi^-\pi^0$ events, and two Gaussians, which model the two peaks from $\chi_{b1,2}(2P)$ decays to $\omega Y(1S)$ with $\omega \rightarrow \pi^+\pi^-$. A bifurcated Gaussian, a high statistics histogram, and a Gaussian model the PDFs for backgrounds II, III, and IV, respectively.

A large data control sample of $Y(3S) \rightarrow \gamma\chi_{bJ}(2P) \rightarrow \gamma\gamma Y(2S)$ events with $Y(2S) \rightarrow \pi^+\pi^- Y(1S)$ and $Y(1S) \rightarrow \ell^+\ell^-$ is used to validate the signal PDFs and mass reconstruction. The control sample is selected using similar criteria to those used to select the $Y(1^3D_J)$. The background contamination is about 2%. Only a small difference is observed between the shapes of the $Y(2S) \rightarrow \pi^+\pi^-\ell^+\ell^-$ invariant mass distributions in the data and simulation. The signal PDF is adjusted to account for this difference. The reconstructed $Y(2S)$ mass is shifted downwards by $0.70 \pm 0.15(\text{stat})$ MeV/c$^2$ compared to its nominal value [12]. We apply this shift as a correction to the $Y(1^3D_J)$ mass results presented below.

Eleven parameters are determined in the fit: the three signal yields and three masses, the yields of background categories I and II, and—within background category I—the $\chi_{b1}(2P)$ mass and the relative yields of the $\chi_{b1}(2P)$ and $\chi_{b2}(2P)$ peaks from $\omega \rightarrow \pi^+\pi^-\pi^0$ decays. The mass difference between the $\chi_{b1}(2P)$ and $\chi_{b2}(2P)$ peaks is fixed to its measured value [12]. The yields of background categories III and IV are fixed to their expected values based on the measured branching fractions [12,14].

Figure 1 shows the $\pi^+\pi^-\ell^+\ell^-$ mass distribution and fit results. The results for the separated $Y(1S) \rightarrow e^+e^-$ and $Y(1S) \rightarrow \mu^+\mu^-$ channels are shown in Fig. 2. The $e^+e^-$ channel has a smaller efficiency than the $\mu^+\mu^-$ channel in part because of the criteria to reject Bhabha events. The differences in efficiency between the $e^+e^-$ and $\mu^+\mu^-$ channels, including those for the $\chi_{bJ}(2P) \rightarrow \omega Y(1S)$ background events, are consistent with the expectations from the simulation within the uncertainties. We find $10.6^{+5.7}_{-4.9}\ Y(1^3D_1)$, $33.9^{+8.3}_{-7.5}\ Y(1^3D_2)$, and $9.4^{+6.2}_{-5.2}\ Y(1^3D_3)$ events. The positions of the three signal peaks in Fig. 1 are stable with respect to different initial assumptions about their masses within the fit interval. The fluctuations at around 10.13 and 10.18 GeV/c$^2$ are discussed below.
Fit biases are evaluated by applying the fit to an ensemble of 2000 simulated experiments constructed by randomly extracting events from MC samples. The numbers of signal and background events and the $Y(1^3D_J)$ masses correspond to those of the fit. The biases are $1.6 \pm 0.1$, $-1.8 \pm 0.2$, and $1.0 \pm 0.1$ events for the $Y(1^3D_1)$, $Y(1^3D_2)$, and $Y(1^3D_3)$, respectively. We subtract these biases from the signal yields. The biases on the masses are negligible.

Multiplicative systematic uncertainties arise from the uncertainty in the number $N_{Y(3S)}$ of $Y(3S)$ events in the initial sample (1.0%) and in the reconstruction efficiencies for tracks (1.4%), photons (3.0%), and particle identification (2.0%). Additive systematic uncertainties originate from signal and background PDFs, evaluated by varying the PDF parameters within their uncertainties, background yields, evaluated by varying the background category IV (III) yield by its uncertainties (by $\pm 100\%$), the fit bias, and the $Y(2S)$ mass calibration. The fit bias uncertainties are defined as the quadratic sum of half the biases and their statistical uncertainties. The mass calibration uncertainty is taken to be half the $Y(2S)$ mass shift added in quadrature with the $Y(2S)$ mass uncertainty [12]. The overall additive uncertainties for the signal yields (masses) are 1.5–2.0 events (0.48 MeV/$c^2$) and are dominated by the contribution from the background yields [$Y(2S)$ mass calibration].

As a check, we repeat the fit with an additional background term, given by a second-order polynomial. The purpose of this check is to test for the effect of potential unmodeled background. The parameters of the polynomial are left free in the fit (thus there are 14 free parameters). The fitted $Y(1^3D_J)$ yields are affected by less than 0.5 events compared to our standard fit, for all $J$ values. The shifts in the fitted mass values are less than 0.05 MeV. Since this polynomial background term is not motivated by any known source and since the description of the background without the additional term is good, we do not use this alternate background model to define a systematic uncertainty.

We define the statistical significance of each $Y(1^3D_J)$ state by the square root of the difference over the value of $-2 \ln \mathcal{L}$ for zero signal events and assuming the bias-corrected signal yield, with the masses and yields of the other two states held at their fitted values. These results are validated with frequentist techniques. Systematics are included by convoluting $\mathcal{L}$ with a Gaussian whose standard deviation ($\sigma$) equals the total systematic uncertainty. The significances of the $Y(1^3D_1)$, $Y(1^3D_2)$, and $Y(1^3D_3)$ observations are 2.0 (1.8), 6.5 (5.8), and 1.7 (1.6) $\sigma$ without (with) systematics included, respectively. If we use the raw signal yields, rather than the bias-corrected yields, the statistical significances of the $J = 1$, 2, and 3 states are 2.4, 6.2, and 2.0 $\sigma$, respectively.

From Fig. 1 it is seen that the data exhibit upward fluctuations at $\pi^+\pi^-\ell^+\ell^-$ masses around 10.13 and 10.18 GeV/$c^2$. To investigate the significance of these fluctuations, we reperform the fit with the $J = 1$ mass constrained to 10.13 GeV/$c^2$ rather than leaving it as a free parameter. An analogous fit is made with the $J = 3$ mass constrained to 10.18 GeV/$c^2$. The statistical significance for this alternate $J = 1$ ($J = 3$) peak, evaluated using the raw signal yield, is $2.0\sigma$ ($1.3\sigma$), compared to $2.4\sigma$ ($2.0\sigma$) for our standard fit. The $J = 2$ signal yield and mass shift by less than 1 event and 0.04 MeV/c$^2$, respectively, in these alternate fits.

We determine branching fractions by dividing the bias-corrected signal yields by the selection efficiencies and $N_{Y(3S)}$. The significances of the $Y(1^3D_1)$ and $Y(1^3D_3)$ peaks are low and we do not have clear evidence for them. For the $J = 1$ and 3 states, we also present upper limits on the branching fractions assuming the fitted masses. The efficiencies for the six allowed $Y(3S) \to \gamma \chi_{bJ}(2P) \to \gamma \gamma Y(1^3D_J)$ paths differ by up to 7.5% and therefore do not factorize, leaving six unknown branching fractions but only three measured signal yields. However, 91.4% of the $Y(3S) \to \gamma \gamma Y(1^3D_1)$ and 88.7% of the $Y(3S) \to \gamma \gamma Y(1^3D_2)$ transitions are predicted [2] to proceed through the $\chi_{b1}(2P)$ state, while $Y(3S) \to \gamma \gamma Y(1^3D_3)$ transitions can only proceed through the $\chi_{b2}(2P)$. Therefore, we evaluate the branching fractions for the dominant modes only, using the predicted ratios of the branching fractions to account for the nondominant transitions. The efficiencies of the dominant modes, averaged over the $Y(1S) \to e^+e^-$ and $\mu^+\mu^-$ final states, are 26.7 ± 0.1%, 26.7 ± 0.1%, and 25.7 ± 0.2% for the $Y(1^3D_1)$, $Y(1^3D_2)$, and $Y(1^3D_3)$, respectively.

The branching fraction products for the dominant modes $B_{J/J} = B_{Y(3S)\to \gamma \chi_{bJ}(2P)} \times B_{\chi_{bJ}(2P)\to \gamma Y(1^3D_J)} \times B_{\gamma Y(1^3D_J)\to \pi^+\pi^-\ell^+\ell^-}$ (or the upper limits at 90% C.L. with systematics included) are, in units of $10^{-7}$, $B_{11} = 1.27^{+1.81}_{-1.69} \pm 0.28 (<2.50)$, $B_{12} = 4.9^{+0.81}_{-1.00} \pm 0.3$, and $B_{23} = 3.8^{+0.83}_{-0.83} \pm 0.24 (<2.80)$. We determine the $Y(1^3D_2)$ mass to be $10.164.5 \pm 0.8 \pm 0.5$ MeV/c$^2$, which is consistent with, and more precise than, the result 10.161.1 ± 0.6(stat) ± 1.6(syst) MeV/c$^2$ from CLEO [4].

From the $Y(3S) \to \gamma \chi_{bJ}(2P)$ branching fractions and uncertainties [12] and $\chi_{bJ}(2P) \to \gamma Y(1^3D_J)$ branching fraction predictions [2] we determine $B_{Y(1^3D_j)\to \pi^+\pi^-\ell^+\ell^-}$ (or 90% C.L. upper limits including systematics) to be $0.42^{+0.27}_{-0.23} \pm 0.10\% (<0.82\%)$ for the $Y(1^3D_1)$, $0.66^{+0.15}_{-0.14} \pm 0.06\%$ for the $Y(1^3D_2)$, and $0.29^{+0.22}_{-0.18} \pm 0.06\% (<0.62\%)$ for the $Y(1^3D_3)$, which lie between the predictions of about 0.2% from Ref. [7] and 2% from Ref. [8].

Figure 3(a) shows the $\pi^+\pi^-$ mass distribution for events in the $Y(1^3D_2)$ signal region $10.155 < m_{\pi^+\pi^-\ell^+\ell^-} < 10.168$ GeV/c$^2$ after subtraction of the backgrounds using the estimates from the fit. The data are corrected for mass-dependent efficiency variations. Shown in comparison are the expectations for the decay
of a $D$ [15], $S$ [15], or $^1P_1$ [16] bottomonium state to $\pi^+\pi^-Y(1S)$. The resulting $\chi^2$ probabilities of 81%, 11%, and 10%, respectively, strongly favor the $D$ state.

The distribution of the angle $\chi$ between the $\ell^+\ell^-$ and $\pi^+\pi^-$ planes in the $Y(1^3D_2)$ rest frame, for events in the $Y(1^3D_2)$ signal region, is shown in Fig. 3(b), where $\theta_{\pi}$ is the angle of the $\pi^+$ in the $\pi^+\pi^-$ rest frame with respect to the boost from the $Y(1^3D_2)$ frame. For $D$-state decays to $\pi^+\pi^-Y(1S)$, $\theta_{\pi}$ follows a $1 + \xi(3\cos^2\theta_{\pi} - 1)$ distribution, where $\xi$ is a dynamical parameter to be determined experimentally. For $S$-state decays, the $\theta_{\pi}$ distribution is flat ($\xi = 0$). A fit to data yields $\xi = -1.0 \pm 0.4(\text{stat}) \pm 0.1(\text{syst})$, disfavoring the $S$ state.

In summary, we have observed the $Y(1^3D_2)$ bottomonium state through decays to $\pi^+\pi^-Y(1S)$. The significance is $5.8\sigma$ including systematic uncertainties. We improve the measurement of the $Y(1^3D_2)$ mass and determine the $Y(1^3D_2) \rightarrow \pi^+\pi^-Y(1S)$ branching fractions or set upper limits. We use the $\pi^+\pi^-$ invariant mass, the angle between the $\pi^+\pi^-$ and $\ell^+\ell^-$ planes, and the $\pi^+$ helicity angle, to test the consistency of the observed state with the expected quantum numbers $L = 2$ and $J = 2$ and parity $P = -1$ for the dominant member of the triplet $Y(1^3D_2)$.

We are grateful for the excellent luminosity and machine conditions provided by our PEP-II colleagues and for the substantial dedicated effort from the computing organizations that support BABAR. The collaborating institutions thank SLAC for its support and kind hospitality. This work is supported by DOE and NSF (USA), NSERC (Canada), CEA and CNRS-IN2P3 (France), BMBF and DFG (Germany), INFN (Italy), FOM (The Netherlands), NFR (Norway), MES (Russia), MEC (Spain), and STFC (United Kingdom). Individuals have received support from the Marie Curie EIF (European Union) and the A.P. Sloan Foundation.

[5] Fermion-antifermion bound states are denoted $n^{2S+1}L_J$, where $n$, $S$, $L$, and $J$ are the radial, spin, orbital angular momentum, and total angular momentum quantum numbers of the pair, respectively.