Mechanistic basis of otolith formation during teleost inner ear development

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Abstract

Otoliths, which are connected to stereociliary bundles in the inner ear, serve as inertial sensors for balance. In teleostei, otolith development is critically dependant on flow forces generated by beating cilia; however, the mechanism by which flow controls otolith formation remains unclear. Here, we have developed a non-invasive flow probe using optical tweezers and a viscous flow model in order to demonstrate how the observed hydrodynamics influence otolith assembly. We show that rotational flow stirs and suppresses precursor agglomeration in the core of the cilia-driven vortex. The velocity field correlates with the shape of the otolith and we provide evidence that hydrodynamics is actively involved in controlling otolith morphogenesis. An implication of this hydrodynamic effect is that otolith self-assembly is mediated by the balance between Brownian motion and cilia-driven flow. More generally, this flow feature highlights an alternative biological strategy for controlling particle localization in solution.

INTRODUCTION

Biominerals are diverse materials that give shape, rigidity and functionality of numerous specialized organs (Bouligand, 2004). Their material properties and design have played an important role in the evolutionary success of vertebrates (Wilt, 2005). Yet the biological mechanisms that control biomineralization are poorly understood. The most obvious type of biominerals in vertebrates is bone but many other structures rely on mineral aggregation such as teeth, carapaces, and otoliths. Multiple types of biomineralization processes have been described to explain the genesis of the multiplicity of shapes, sizes, and compositions of organic and mineral components that come out of the biomineralization process. In particular, the otoliths in teleost are ovoid biominerals which form the ear stone or otoconia located in the vestibular labyrinth of the inner ear. They are millimeter-sized particles,
composed of calcium carbonate and an organic matrix made of glycoproteins, proteoglycans and collagens (Hughes et al., 2006), and they provide an inertial mass that facilitates deflection of ciliary bundles in response to vibration, gravity and linear acceleration essential for hearing and balance.

In zebrafish, early growth of otoliths is tightly controlled in time, with a period of fast growth between 19 and 24 hours post fertilization (hpf). Saturating growth occurs for the rest of the fish's adult life (Riley et al., 1997). The otic cavity contains precursor 1–3 micron particles, or spherules, secreted from the apical portions of the epithelial cells of the inner ear (Riley et al., 1997). Time lapse analysis and electron microscopy show that otolith growth starts as a nucleus of spherules aggregating at the top of a tether cilium (Clendenon et al., 2009; Pisam et al., 2002). At 30hpf, a mineralized ovoid otolith is visible (Pisam et al., 2002; Sollner et al., 2003) and concentric arrays of spherule deposition are seen at the periphery of the nascent otolith (Pisam et al., 2002).

The early process of otolith assembly (19–24 hpf) is particularly interesting because it requires the presence of biological flow generated by beating cilia (Colantonio et al., 2009; Riley et al., 1997). The otolith-forming region has a specific topology: a cluster of motile cilia located next to the tether, stationary cilia at each pole (anterior and posterior) of the ovoid-inner ear (Colantonio et al., 2009). The inner ear also contains shorter cilia lining the entire vesicle that are immotile (Colantonio et al., 2009). Previous experiments demonstrated that motile cilia are essential for normal otolith number, size and position (Colantonio et al., 2009). However, the roles of flow for the mechanism of otolith formation during the period of fast growth is not yet well understood. It was first proposed that the motile cilia act as a dispersant to mix fluid and spherules throughout the inner ear (Riley et al., 1997). More recently, it was suggested that motile cilia act locally as dynamic attractor of spherules and that flow at the poles increases the likelihood of spherules to meet the tether cilia (Colantonio et al., 2009). Nevertheless, the hydrodynamic basis of spherule transport towards the otolith and the role of cilia mixing remains unclear in this model. Furthermore, while it seems that the position, size, and number of otoliths in any given inner ear could be controlled by beating cilia (Colantonio et al., 2009), it is still unclear if flow can account for otolith shape.

In this study, we developed a flow probe based on optical tweezers to assess the fluid dynamics at work in the inner ear. This approach allowed us to define two hydrodynamic features essential for otolith formation. First, a global, vortical flow generated around the tether cilia favors spherules transport toward the growing otolith. Second, a local mixing flow located at the base of the forming otolith that paradoxically reduces agglomeration. Diffusion dominates outside this stirred region, allowing for agglomeration of the transported spherules. Finally, we use a simple physical model to clarify the role of cilia in the process of spherule transport. Altogether, these results suggest that the dual action of stirring and vortical flow cause the otolith to take on its typical shape and establish the hydrodynamic basis of asymmetric transport through cilia mediated flow.
RESULTS

Mapping inner ear flow reveals motile cilia transport spherules towards tether cilia

The relative strength of deterministic flows relative to the stochastic motion of the spherules is parameterized by the Peclet number, $Pe = \frac{v_{\text{max}} l}{D}$, ($v_{\text{max}}$ is the maximum velocity in the system, $l$ the diameter of the observed particle, and $D$ the diffusion constant). A system with $Pe \ll 1$ is primarily diffusive whereas a system with $Pe \gg 1$ is advective, dominated by flow. Near the motile cilia, the maximum inner ear $Pe$ can reach upwards of 60–100, as determined by cilium speed, assuming a particle with the lateral dimension of a cilium, and its medium of travel being water. We tested two implications of such a $Pe$ for otolith biogenesis: namely, whether (i) the rapid reduction in flow propagation, due to the viscous nature of inner ear fluid, results in a transition to dominantly Brownian motion near the tether cilia, and therefore correlates with otolith nucleation, and whether (ii) the high velocity of motile cilia in an enclosed structure results in spherule localization near the tether cilia in vivo.

To investigate the nature of the cilia-induced flow propagation, we developed a non-invasive strategy to visualize the paths followed by spherules near the motile cilia. We used in vivo optical trapping within the inner ear in order to accumulate hundreds of spherules and release them into the flow field, much as smoke can be used to visualize the flow field around a car in a wind tunnel (Figure 1, A–E). We trapped spherules at 1064 nm, a non-phototoxic wavelength (Svoboda and Block, 1994), so that embryonic ($n = 6$) and otolith development was not affected when compared to non-manipulated siblings ($n = 11$). This approach allowed us to generate and map the time-averaged (stationary) flow field (Fig. 1, F–J; Sup. Movies 1–3) and show that spherules are propelled through fluid along helical paths inside the cavity. When trapped further from the cilia, we see spherules advected towards the cilia and becoming entrained in the vortical flow, effectively localizing spherules near the nascent otolith (Fig. 1, G, J; Sup. movies 2, 3). The time for one revolution of released particles was $T=4.6 \pm 0.9$ sec, although the cilium beating frequency was much faster, at 44 $\pm 4$ Hz. A clear separation between a disordered and an ordered regime was seen (Fig 1, F; Sup. Movie 2, 3). The deterministic portion of the induced flow encompasses the near field of the cilia next to the otolith (3.1 $\pm 0.5$ microns) and drops off quickly into purely diffusive behavior (to 10% of the maximum velocity, as measured by particle image velocimetry), as shown by the transition from correlated to uncorrelated vectors in Fig. 1, F–G. Similar flow patterns were observed for anterior and posterior otoliths. Altogether, these data suggest that the flow can affect the transport of spherules towards and about the growing otolith (Fig. 1, K).

The otolith emerges at the juxtaposition between the well-stirred near field and the diffusion dominated far field

In order to mark the transition between diffusion-dominated versus advection-dominated flow, we investigated spherule behavior around the otolith independent of the global streamlines, by examining shorter time periods of motion. By using the blinking optical trap technique (BOTS) (Lin et al., 2000), we measured spherules’ mean-squared displacement (MSD) behavior at a single point over 30 ms (Fig. 2, A–I; Sup. Movie 4) for a range of...
positions in the inner ear. This technique is ideally suited for performing in vivo MSD measurements, as there is no requirement for knowing the precise optical and hydrodynamic properties of the system a priori. By fitting the MSD to a Langevin model of fluid motion,

$$\langle x(t)^2 \rangle \approx 2Dt + \frac{a_c^2}{\omega^2} (1 - \cos \omega t)$$

we were able to extract the relevant physical parameters (Fig. 2, G and H) and generate short-time flow maps (Fig. 2, I): $D$ is the diffusion coefficient, $a_c$ is the local amplitude of the oscillating velocity, and $\omega$ is the frequency of the oscillation (see Supplementary Experimental Procedures and Sup. Fig. S1). Fit parameter $a_c$ quantifies the degree of influence the motile cilia exert on the interrogation point of the BOTs (Fig. 2, D–F, I), and serves as a way to map the field strength of the cilia beat in the absence of global flows (Fig. 2, I). The fitted parameters were strikingly similar to measured and expected parameters in vivo (frequency, $\omega$, 43, +/-8.6 Hz, and diffusion coefficient, $D$, 0.1 +/- 0.1 $\mu$m$^2$/sec), thereby allowing us to use the $a_c$ fitted parameter with confidence. Note that motile cilia circumscribe a ~3–5 micron trajectory at their tip; at 43 Hz, this corresponds up to 33 $\mu$m/sec. We found that flows induced by the motile cilia dropped to within 10% of their initial value in less than 4 $\mu$m (Fig. 2, I); this corresponds to the thickness of the advection dominant zone in the zebrafish inner ear. The otolith - always located within a few microns of the motile cilia - thus emerges at the juxtaposition between the well-stirred near field and the diffusion dominated far field, which is determined by the strength of the cilia.

**Cilia mixing is necessary to prevent agglomeration and controls otolith shape**

To gain insight into the physiological role of cilia-induced fluid mixing in controlling otolith shape, we addressed the after-effects of motile cilia ablation during the period of rapid otolith growth (18–24 hpf) (Riley et al., 1997). Since the otolith acts as a self-aggregation point, we used focal laser ablation to inactivate motile cilia beating after nucleation occurred (Fig. 3 A–D; Sup. Movie 5), and addressed the effect of flow cessation on otolith shape. The primary process of diffusion-limited aggregation ($Pe \ll 1$) is less dependent on cilia-induced flow since we found that total growth was not significantly affected by cilia ablation (Fig. 3, E–K). In order to analyze the shape of the otolith, we segmented the otolith shape before and after laser ablation by measuring the mean of the sum of squared residuals (SSR) relative to a circle (Fig. 3 E–J, L–M; Fig. S2, A–D and Supplementary Information). For this analysis, a SSR closer to 0 implies that the shape is more spherical. The mean SSR in ablated embryos was 0.31 (n=24), and the wild-type 0.53 (n=33). The significance of the difference was validated by a bootstrap analysis (p-value < 0.03) (see Supplemental Information). The difference is still visible 17 hours after ablation (Fig. 3 N, O) and is independent of the side where the ablation was performed (both anterior or posterior otoliths were ablated and the contralateral side was used as control, n=5). Thus, a secondary effect of cilia-induced flow is the formation of an aspherical otolith, often mushroom-top-shaped. These observations correspond to a subclass of otolith phenotypes observed after genetic ablation of gas8, an essential gene for cilia beating and inner ear development (Colantonio et al., 2009), and suggest that cilia motility is required at several steps of otolith assembly. This result implies that pure Brownian motion prefers to form a more spherical otolith, whereas
directed flow ($Pe \sim 60–100$) near the tether cilia locally diminishes the spherules aggregation, resulting in the classic mushroom-top shape of zebrafish otoliths (Blasio et al., 2006; Pisam et al., 2002; Schibler and Malicki, 2007; Sollner et al., 2003). Thus, in addition to inducing global transport of spherules to the poles of the inner ear, cilia motion induces a high-speed flow field around the tether cilia beneath the nascent otolith; stagnation areas are immediately superior, at the sides and top of the nascent otolith, because of the quick decay of cilia influence (Fig. 2, I). This biases spherule deposition away from the bottom of the otolith, resulting in an aspherical shape ($SSR > 0$) (Fig. 3, P).

**Stokes flow explains preferential spherule location**

An important experimental result is that spherules become entrained by the motile cilia according to their averaged trajectories in the inner ear (Fig. 1, F). To investigate in more detail whether flow can bias spherule localization, we used a physical model that captures the essential features of the system by simulating cilium-induced flow inside a spherical cavity. Our model for the cilium consists of a small sphere which traverses an elliptical track (Fig. 4, A) (Vilfan and Julicher, 2006). Since the Reynolds number is much less than unity and the cilia are much smaller than the overall scale of the cavity, flow inside the inner ear can be approximated by the Stokes equation with a singular force −$\nabla p + \mu \nabla^2 v = -F_\delta(x - x_i)$ with constraint $\nabla \cdot v = 0$ ($p$ is the pressure, $\mu$ the viscosity, $v(x)$ the velocity field, and $F$ the cilium’s effective point force located at $x_i$ imparted by the cilium). The equation admits analytical solutions inside a sphere (Maul and Kim, 1994), which we chose to model the inner ear cavity (Fig. 4, B). The hydrodynamic velocity field is $v(x) = G(x, x_i)F_i$. Here, the Green’s function, $G$, consists of the Oseen tensor which describes the flow generated by a singular force in a boundless fluid in addition to a complex set of terms that enforce no-slip, no penetration boundary conditions on the inside surface of the spherical inner ear ((Maul and Kim, 1994) and Supplemental Information). The flow-field is calculated as a time average of the cilium motion, and diffusive transport of the spherules is included using Brownian dynamics. We adjust $Pe$ most easily through changing the frequency of the cilium. For the simulation, we randomly seed 1 μm particles on the cavity surface as a starting condition, which is in accordance with the origin of spherules in vivo (Pisam et al., 2002), and set parameters based on the known hydrodynamic characteristics of the inner ear (see Supplemental Information). We ran all the simulations until the system reached a statistically stationary condition, typically hundreds of seconds in real time. The model predicts that flux towards the region of the motile cilium is a non-linear function of the Peclet number (Fig. 4, C), suggesting that motile cilium pull spherules towards the tether cilium, as shown in Sup. Movie 6. Moreover, the presence of a dipole-type of flow field increases particle circulation near the motile cilium (Fig. 4, D), which accounts for the entrainment observed in Fig. 1, F. A particle moving along a streamline at some velocity $v$ in each time interval $dt$ has probability $k \times dt$ of randomly walking off the streamline; $k$ is related to diffusion - $k \sim D/A$, where $A$ is some diffusion area. Therefore the average distance a particle will travel on a streamline before wandering away is $v/k$. For a circulating streamline of radius $r$, the average number of times a particle will circulate cilium is thus $<N_{circ}> = v/(2\pi kr)$. Since the streamlines have smaller radii and faster velocity near the motile cilium (Fig 4, D–F), particles near the motile cilium will, on average, circulate around the cilium more times than particles traveling on streamlines far away through a dipole-like flow pattern (Fig 4, E).
and F). Altogether, the increasing velocity along inner radii increases advective stirring around the otolith. Brownian motion is still, of course, a requirement for enhanced particle circulation: without diffusion, particles do not exchange streamlines and cannot therefore get closer to the otolith \((\langle N_{\text{circ}} \rangle \text{ goes to } 0)\). Moreover, particles that are on the size scale of velocity gradients in shear flow potentially experience a force directed towards higher velocities (Gavze and Shapiro, 1997). Thus, our model demonstrates that cilia can increase spherule transport through a dipole-like flow and due to the quick decay of flows in viscous fluids, a stagnation zone is apparent in the immediate vicinity, thereby suggesting that a mechanical mechanism can account for the observed biased location of otolith formation near motile cilia (Figure 4, G).

**DISCUSSION**

Through the application of *in vivo* flow visualization technologies, we have taken a closer look at the flow generated by beating cilia in the zebrafish inner ear and identified two hydrodynamic features explaining the effects of flow during otolith formation: (i) transport towards tether cilia and subsequent rapid reduction in flow propagation results in a transition to Brownian motion, which leads to preferential spherule localization near the tether cilia and (ii) high velocities nearer to the base of the otolith results in asymmetric shape production of the growing otolith. These features clarify the role of advection in the inner ear cavity showed previously (Colantonio et al., 2009) and suggest a better model for otolith assembly whereby the role of diffusion is included, and whereby the shape of the otolith is directly coupled to the flow forces. Here, motile cilia transports precursor particles towards tether cilia accounting for number, position, and size (Colantonio et al., 2009), and locally stirs the fluid (Riley et al., 1997), accounting for the flat bottom shape of the otolith. Since it is clear from zebrafish mutants that otolith shape is highly stereotyped and is critical for sensory organ function in the inner ear (Hughes et al., 2006; Nicolson, 2005; Schibler and Malicki, 2007; Sollner et al., 2003), we speculate that the flat-bottomed shape of the otolith allows orthogonal cilia implantation within the otolith that could maximize sensitivity of stereocilia bundles to linear displacements (Karavitaki and Corey, 2010).

The hydrodynamics mediated by inner ear cilia is similar in action to what has been described in bi-flagellae *Chlamydomonas reinhardtii* and *Chlamydomonas* colony *Volvox carteri*, which uses the same type of linear advection-diffusion system to drive metabolite uptake and waste exchange (Short et al., 2006; Solari et al., 2006). The flux towards the cilia, as well as spherule entrainment, depends on the particular physical boundaries of the inner ear wall, the frequency of the cilia, and the ability of the tether cilia to immobilize spherules. As a consequence, these observations suggest a basic mechanism where self-organizing properties of otolith formation could solely depend on the hydrodynamics mediated by cilia, diffusion and the self-aggregation properties of the spherules. It is thus tempting to speculate that changes in the inner ear morphology will have a direct effect on hydrodynamics and can account for the variability of otolith shape observed in teleosts.

Ciliated organs affect the distribution of many other biological products in vertebrates’ cavities, such as signaling molecules during stem cell migration in the brain (Sawamoto et al., 2006) and in the left right organizer (Okada et al., 2005; Schweickert et al., 2007) where...
the fluidic motion is also highly stereotyped. However, the complexity of cilia activities as well as the multiplicity of biological outcomes they can control during development is far from being understood (Cartwright et al., 2009). Our study demonstrates that the use of non-invasive optical methods of probing flow are accurate enough to precisely address microscopic flows. Furthermore, as there is increasing evidence that congenital diseases are rooted in multifactorial processes involving cilia in the developing embryo (Gerdes et al., 2009), precise flow probing becomes critical to understand the biological principles that govern cilia driven flow and their potential involvement in diseases. In this context, our method to quantify the dynamics of flow could be applied to study cilia driven flows in a variety of developing organs.

METHODS

Bright-field imaging

Imaging was performed on a home built microscope incorporating a 60× 1.2 NA Olympus IR corrected water immersion objective, coupled with a 200 mm focal length tube lens. Either a Basler A602f CMOS camera (10 um pixel size) or a Prosilica GC1380H (6.4 um pixel size) was used for imaging. Data were taken using custom Matlab scripts. Embryos were mounted in agarose using a micromachined mold so that the neural tube is facing the objective for the flow mapping using PIV (dorsal view, Figure 1 G, H). Side views of the otolith were obtained by mounting the embryos slightly on the side so that the neural tube is at a 45 degree angle relative to the objective (side view, Figure 1 F and figure 2 D, F, I).

Particle Image Velocimetry of the flow field

By shining focused laser light (1064 nm, 100 mW) through the microscope objective (as described under “Bright field imaging”) for a few seconds (< 30 sec), particles were accumulated to perform particle image velocimetry (PIV). PIV was calculated over 8×8 sub-samples of the movies using custom Matlab scripts. The imaging frame rate was 30 Hz. The embryos showed no obvious signs of damage from the laser. Correlation was performed between two adjacent frames in time. The PIV algorithm also detects otolith movement, causing arrows to show up in Fig. 1, F and G; the otolith itself is always moving. The short period of time, and low laser power employed, were not enough to cause irreversible particle aggregation, compared to the powers and times used in Riley et al., 1997.

Blinking optical trapping (BOT)

A 1064 nm laser was used in conjunction with an acousto-optic deflector (AOD) utilizing digitally synthesized frequencies. A custom Labview program was used to control the modulator. We found that the best switching frequency for single spherule trapping and tracking was 10 Hz. The laser output power (after the AODs) was 100 mW. A 532 nm notch filter was used to block laser light. Imaging was performed as described above under “Bright field imaging”, at 492 fps. Microscope construction was the same as used in PIV (above).
Laser inactivation of cilia beat

A 532 nm laser at 1 W focused on beating cilia was used in 30 seconds increments to evaluate if the cilia had been inactivated. Typically, cilia were illuminated for 1 minute to reach motion stasis. Otolith shapes were checked 1, 2 or 5 hours, and 17 hours post ablation.

Otolith segmentation

We regularized the otolith orientation by rotating the otolith along an axis defined by the tether cilia. The mid-point of the otolith was then determined by the largest width along an axis perpendicular to the tether cilia. We next fitted a circle to the otolith using the largest width as a constraint and calculated the sum of squared residuals (SSR). Since the expected distribution of SSR is unlikely to be Gaussian, we employed a bootstrap algorithm to determine the significance of the difference of the means (see Supplementary Information for more details).

Analysis of BOTs

Using Matlab, one-dimensional Brownian dynamics simulations of a particle released by a trapping laser and subjected to a sinusoidal external force, was performed. The resulting mean squared displacement was compared to the analytical result and demonstrates near exact agreement (see Supplementary Information). Since the tracked cilia tips also moved according to an approximate sinusoidal motion, we fitted the BOTs movies to the same analytical result and extracted the parameters. For BOTs analysis, depth of focus does not affect data analysis, as long as we could find the centroid of the particle, since we only measured lateral displacements. If the centroid could not be found, then the data was discarded. Depth of focus of images was 1 micron.

Simulations of flow and diffusion

We used Matlab to compute the velocity field inside a sphere according to the Green’s function solution to Stokes’ equation. We used a spherical cilium similar to that of Vilfan et al. (see Supplementary Information). The velocity field was then incorporated into a finite-difference Langevin equation as an external force that impinges upon the Brownian particles of 1 μm in diameter. The simulation was run until it reached a statistically stationary state. Pe was defined based upon the largest velocity in the simulation; i.e., the tip of the cilium.

Supplementary Material

Refer to Web version on PubMed Central for supplementary material.

Acknowledgments

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Figure 1. Mapping the global flow field of the inner ear

(A) Side view of a zebrafish embryo at the stage (18–24 hpf) of optical tweezing. The red box outlines the inner ear. (B) Magnified version of the inner ear corresponding to the red box in (A). White arrows point to spherules, which are numerous at this stage, and blue arrows point to the otoliths. (C) Schematic view of the optical tweezing approach, depicting the use of focused light to position spherules in the inner ear. (D) Cilia implantation next to the otolith. Drawing depicting motile cilia (in red) position with respect to tether cilia (in back) and otolith (depicted as an aggregates of spherules). (E) Parcels of spherules are aggregated using the optical trap for up to 30 seconds and positioned at a desired location in the inner ear. The trap is then turned off and the particles are “released” following the flow field generated by beating cilia (F). See also Supplementary Movie S1. In order to compute the flow maps as depicted in (G) and (H), this process was repeated at least twice near each otolith. (F) A montage sequence of released particles near a motile cilium in a side viewed embryo. White arrows show released particles that were trapped initially (red arrowhead, upper left box) and followed through a 1 sec (upper right box, lower left box, lower right box, respectively) sequence after trap is turned off (dotted lines). (G, H) Particle image velocimetry (PIV) of the flow field near an otolith inside a typical inner ear viewed dorsally, calculated from released particles. See Supplementary Movie S2 and S3 for comparison. In (G), the trapped particles (dotted lines) were placed in the plane of the otolith; this is indicated in the schematic (K) which depicts an orthogonal cut through the inner ear. Particles are advected into the flow field (yellow arrows), indicating that the cilia have the ability to localize particles near the nascent otolith. Asterisks point to motile cilia underlined by the rotational flow observed in supplemental Movie S1. In (H), the trapped particles (dotted lines) are displaced 5 microns from the plane otolith, as depicted in schematic (K).
Particles are still able to be advected into the otolith region (yellow arrows). This is better shown in the supplemental movies. Note that in the center of the high-advection region of (G) is an area of low flow (blue arrows), indicating that stagnation occurs near the otolith. (I, J) The magnitude of the velocities of the images shown in (G) and (H) are displayed in surface relief along the z-axis. The color of the arrows in (G) and (H) correspond directly to peaks in (I) and (J), respectively. The xy axis in (I) and (J) represents the dimension of the G and H images, respectively. There is a much broader area of large velocity magnitude in (G) compared to (H), indicating that the flow field far from the otolith is strongly diffusive. The gradient of velocities changes from tens of microns per second to background values within 4 microns or less. (K) Relative position of the focal planes where the measurements were performed in (G) and (H) (5 microns distance). The red lines indicate the position of the motile cilia. (L) Schematic representation of the flow field near the motile cilia (blue arrows), spherules (blue circles), and the tether cilia attached to the growing otolith. Near field flow is advective, as denoted by the yellow shading; the far field is dominated by diffusion. Scale bars: (B) 10 microns, (F) 5 microns, (G, H) 5 microns.
Figure 2. Mapping local hydrodynamics using blinking optical traps
(A–F) Schematic view of the optical tweezing depicting the sequence of trap and release used to measure Brownian dynamics at single point inside the inner ear. *In vivo*, spherules are trapped (A) and released (B) roughly 1000 times (C) at a frequency of 10 Hz, and imaged at 492 Hz, in order to resolve accurate sub-second dynamics of flow, as opposed to global flows in Figure 1 in side viewed embryos. (D) The white circle indicates the location of trapped particles (red arrow) and the white arrow in (E) points to the spherules position 0.02 seconds after release and reveals its displacement after the trap is turned off (dotted lines, F). See Supplementary Movie S4 for demonstration of blinking optical traps. (G–H) Mean-squared spherule displacement plotted as a function of time illustrating a typical diffusive spherule motion (G) and driven motion (H) in both $x$ (circles) and $y$ (squares). The particular curves chosen demonstrate the strong effect of boundary conditions on the Brownian dynamics. The error (standard deviation) on the MSD curves are approximately equal to the value of the MSD at each point. 30 ms of MSD was calculated at each BOTs point to avoid global flow effects (see Supplementary Information), as described in Figure 1. (I) Flow map reconstituted using the BOTs model shows a velocity (parameter $a_c$) field that decays with increasing distance from the cilium (the black arrow points at the motile cilium which is better seen in Sup. Movie S4). Here, the tether cilium is not visible in this still image because it is out of focus. Note that the otolith (the central bright object) itself moves, and is therefore responsible for increased flow near itself. The velocity decreases to 10% of maximum 4 microns from the cilium. Scale bars: (F, I) 5 microns.
Figure 3. Laser ablation of motile cilia

(A–D) Schematic of the experiment. A 532 nm laser was aimed squarely at the motile cilium (A, C) until the cilia paused their movement (B, D, black arrow, see Sup. Movie 5). The dotted line indicates the ablation spot (C). See Supplementary Movie S5 for example. (E–F) Control otolith before and after sham ablation. Otolith before (H) and after 1 hour after local cilium ablation (I). The otolith clearly grows as seen in the schematic representing the overlay of the otoliths before (dashed line) and after (solid line) 1 hour after sham ablation (G) and true ablation (J). (K) Segmentation of the otoliths (see Supplemental Information) shows that ablation does not affect gross accumulation, as measured by relative area, of spherules on the growing otolith 5 hours after ablation. Errors are by standard error of the mean. (L, M) Distribution of the otolith shape (measured in units of SSR/micron) in controls (L) and cilia ablated embryos (M) less than 5 hours after ablation shows a clear difference, confirming the necessity of cilia beat for maintaining aspherical otolith shape (p < 0.03) (see Supplemental Information). (N, O) Shape difference 17 hours after ablation. The black line underlines the surface of the inner ear which is aligned with the otolith's flat base in control
(N, black line), but not in the ablated, contralateral otolith (black arrow) (O). (P) Schematic of the proposed mechanism for formation of aspherical otolith shape. The high-speed flow at the base of the otolith due to the motile cilia (in red) prevents agglomeration (yellow area) while diffusion in stagnant areas (white area) permits agglomeration of particles, resulting in aspherical otolith formation (normal). After cilia ablation, the otolith grows uniformly, forming a grossly circular spherical shape. Scale bars: (I, N, O) 10 microns.
Figure 4. Inner ear viscous flow model

(A) The hydrodynamic model of the inner ear represents the cilium by a small sphere (black dot) moving on a tilted elliptical trajectory (in red), placed at the bottom (0,0,−45 μm) of the inner ear (white arrow), which is represented by a larger sphere, with a radius of 50 μm (B). (C) The flux of particles (Mols/sec) towards the cilium-sphere as a function of $Pe$. Particles are released along the edge of the inner ear-sphere at $t = 0$, and the average time particles take to reach the cilium is computed at different cilium frequencies, which is directly related to the $Pe$. The gray shaded region is the standard deviation of flux. (D) Maximum projection of the time-averaged flow field (arrows) inside the inner ear-sphere along the planes $z < −35 μm$, for cilia frequency of 54 Hz. This plane illustrates the principle of cilium induced flow. The coloring of the arrows indicates speed in logarithmic units. Red arrows indicate fast velocities (~60 μm/s), whereas blue arrows indicate slow velocities (~1 μm/s). Dots indicate the average position of a particle in a 100 ms interval. The color of the dot shows the variance of position in that 100 ms interval, in linear units. Near the cilium, which is located in at (0,0), particles are orange indicating a small degree of position variance (< 1 μm²), whereas particles are blue immediately outside the location of the cilium (> 10 μm²). Particles closest to the cilium circulate around the cilium many times before diffusing away, due to entrainment, resulting in a small position variance (orange), whereas particles immediately outside the cilium are advected towards the cilium, so their position variance is high (blue). Particles on the edge of (D) are primarily orange and yellow because they are far away from the cilium and therefore do not feel its effect; thus, their variance is determined for the most part by temperature. See Supplementary Movie S6 for a demonstration of the simulation. (E) Schematic representation of flow field in (D) and the orthogonal flow field ($x$–$z$ plane) (F). In the $x$–$y$ plane (E), the flow is dipole-like, whereas
flow in the x–z plane (F) is circulatory. Particles traveling along each streamline have uniform probability of leaving it, due to Brownian motion. However, faster velocities (green lines) shape particles' trajectories into a stereotyped flow pattern, resulting in entrainment. (G) Schematic representation of flow field at work in the inner ear (side view) summarizing the knowledge gained from model. The white object in the middle is the otolith; the two red wavy lines represent motile cilium. Black lines supporting the otolith are tether cilia.