Results are presented from a reanalysis of the entire five-tower data set acquired with the Cryogenic Dark Matter Search (CDMS II) experiment at the Soudan Underground Laboratory, with an exposure of 969 kg-days. The analysis window was extended to a recoil energy of 150 keV, and an improved surface-event background-rejection cut was defined to increase the sensitivity of the experiment to the inelastic dark matter (iDM) model. Three dark matter candidates were found between 25 keV and 150 keV. The probability to observe three or more background events in this energy range is 11%. Because of the occurrence of these events, the constraints on the iDM parameter space are slightly less stringent than those from our previous analysis, which used an energy range of 10–100 keV.

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Cosmological observations [1] strongly suggest that nonluminous, nonbaryonic matter constitutes most of the matter in the Universe. This dark matter should be distributed in dark halos of galaxies such as the Milky Way, enabling the direct detection of the dark matter particles via their interactions in terrestrial detectors [2]. The movement of the Earth around the Sun would provide an annual modulation of the counting rate, caused by the change in the relative velocity of the dark matter particles with respect to the earthbound target [3].

The DAMA collaboration claims the observation of such a modulation in two different NaI(Tl) scintillation detector arrays [4,5]. The observed signal is in the 2–6 keV electron-equivalent energy range with a periodicity of $0.999 \pm 0.002$ years and a phase of $146 \pm 7$ days [6]. The observed modulation signature is consistent with the expected signature of galactic dark matter particles interacting in a terrestrial detector. Other experimental results [7–12], however, are inconsistent with the interpretation of the DAMA result as a signal from weakly interacting massive particles.
Inelastic dark matter (iDM) scattering has been proposed as a way to resolve this tension [17]. The inelastic scenario assumes that WIMPs ($\chi$) can only scatter off baryonic matter ($N$) by transition into an excited state at a certain energy above the ground state ($\chi N \rightarrow \chi' N$), while elastic scattering is forbidden or highly suppressed. There is a minimal velocity required to produce recoil energy $E_R$ in such an inelastic scatter,

$$v_{\text{min}} = \frac{1}{\sqrt{2m_N E_R}} \left( \frac{m_N E_R}{\mu} + \delta \right),$$

where $m_N$ is the mass of the target nucleus, $\mu$ is the reduced mass of the WIMP-nucleus system, and $\delta$ is the WIMP-mass splitting; $\delta = 0$ keV is equivalent to elastic scattering. If $E_R$ is too small or too large, $v_{\text{min}}$ is above the cutoff imposed by the galactic escape velocity, and the event cannot occur. Important consequences of this model for direct detection experiments are differential rates that peak at tens of keV recoil energy, and a significant suppression of the recoil spectrum at low recoil energies. In addition, the annual modulation signature is significantly enhanced, because of the increased dependence on the high-velocity tail of the WIMP-velocity distribution, which in turn is due to the larger minimal velocity (see Eq. (1)). Therefore, the iDM scenario is also particularly sensitive to the escape-velocity cutoff in the WIMP-velocity distribution. Finally, it is important to note that the scattering rate is enhanced for heavy target nuclei (e.g. Xe and I).

The Cryogenic Dark Matter Search (CDMS II) experiment operated in the Soudan Underground Laboratory a total of 19 Ge ($\sim 230$ g each) and 11 Si ($\sim 105$ g each) detectors at a temperature of $\sim 40$ mK [18,19]. These semiconductors were stacked into five towers (T1-T5) with six detectors (Z1-Z6) each. They were instrumented with four channels of superconducting transition-edge sensors on the top side to detect phonons and two concentric electrodes on the bottom side to detect ionization. The primary ionization signal was read out by an inner electrode covering $\sim 85\%$ of the detector surface. A thin outer electrode served as a guard ring to identify and reject events at the edge of the detector, which was subject to higher background and reduced charge collection. The recoil energy was reconstructed from the phonon and the ionization signal [20]. The ratio of ionization to recoil energy (“ionization yield”) was lower for nuclear recoils, produced by WIMP candidates, than for electron recoils, caused mostly by background photons. Fewer than $10^{-4}$ of the electron recoils in the bulk of the detector were misidentified as nuclear recoils. The main source of misidentified electron recoils were events with interactions in the first few $\mu$m of the detector surfaces. Because of incomplete charge collection, these events had reduced ionization yield, and occasionally the reduction was severe enough to mimic a WIMP-nucleus interaction. The phonon signals of these surface electron-recoil events had faster-rising pulses than bulk nuclear recoils and occurred closer in time to the more prompt ionization pulses. As discussed in detail in this paper, a cut based on these timing parameters was employed to reject interactions at the detectors’ surfaces. Misidentified surface events constituted the dominant background for the CDMS II experiment, while the neutron background from cosmogenics and radioactive processes was much less significant.

Initial constraints from CDMS on the iDM model interpretation of the DAMA claim were set using a recoil-energy range of 10–100 keV [7]. This paper presents a dedicated iDM analysis of the entire CDMS II five-tower data set, taken during two periods of stable operation between October 2006 and July 2007 (internally denoted as runs 123–124) [21], and four periods between July 2007 and September 2008 (internally denoted as runs 125–128) [7]. Note that the constraints on the WIMP-parameter space shown in [7] were a combination of the final results from all data sets taken at the Soudan Underground Laboratory which, however, were analyzed separately. In particular, the surface-event rejection cuts, as discussed below, were set at fixed backgrounds for runs 123–124 and runs 125–128 separately. For the analysis presented here, the whole acquired data were combined in advance and surface-event rejection was based on the entire data set. There were two main reasons for performing this reanalysis. The iDM parameter space allowed by our previous analysis (see Fig. 4 of [7]) includes WIMP masses $m_W \sim 100$ GeV/$c^2$ and mass splittings $\delta \sim 120$ keV. As shown in Fig. 1, these parameters result in a significant
expected rate above our previous analysis upper limit of 100 keV, so a simple extension to 150 keV increases the expected sensitivity. Moreover, the expected rate drops to zero for low recoil energies, in contrast to the elastic-scattering case, obviating the need for a low threshold. Since most of the dominant surface-event background occurred at energies just above our 10 keV threshold [21], where no IDM signal is expected, the sensitivity could be further improved by redefining a looser surface-event rejection cut based upon the estimated background with recoil energy between 25 keV and 150 keV, while leaving the lower boundary for the analysis at 10 keV. Thus, a significant number of surface-background events was expected in the 10–25 keV range which, however, had only a minor effect on the results in the parameter space region of interest (\(m_w \sim 100 \text{ GeV}/c^2, \delta \sim 120 \text{ keV}\)).

The same data-quality selection cuts used in previous analyses [7,21] for ensuring detector stability and removing periods of poor detector performance, e.g. due to insufficient neutralization, causing incomplete charge collection owing to impurities in the detector crystal, resulted in a total Ge exposure of 969 kg-days for this reanalysis. The Si detectors were omitted due to their lower sensitivity to inelastic scattering. Because both data sets had already been analyzed, this analysis was not “blind.” However, the analysis was performed in a similar manner to minimize bias: selection criteria and background estimates were defined and evaluated using only WIMP-search data outside the signal region and calibration data.

The detectors were exposed to gamma rays from \(^{133}\text{Ba}\) and neutrons from \(^{252}\text{Cf}\) at regular intervals to calibrate their response and define criteria for data-quality cuts and the WIMP-acceptance region. The latter was defined to be the \(\pm 2\sigma\) band around the mean nuclear-recoil ionization yield in the yield versus recoil-energy plane. An illustration is given in Fig. 2, which shows \(^{252}\text{Cf}\) calibration data from a representative detector in one of the six data runs.

In addition to the quality cuts, most of the selection criteria for WIMP-nucleon interactions remained unchanged from the previous analyses [7,21]. This included the single-scatter cut, requiring there to be no signal exceeding the phonon-noise level by more than \(4\sigma\) in any of the other 29 detectors; the ionization-based fiducial-volume cut, rejecting events near the edges of the detectors; and the muon-veto cut, demanding negligible incident energy deposited in the active muon veto surrounding the apparatus.

Extending the analysis window to 150 keV was hindered by the fact that statistics from the \(^{252}\text{Cf}\) neutron source were low above \(\sim 100\) keV which can be seen in Fig. 2. Thus, we extrapolated the nuclear-recoil bands at higher energies from the fits below 100 keV. The extrapolation showed good agreement with Lindhard theory [22,23] when statistics from all six runs were combined for each detector, and both the band locations and the nuclear-recoil cut efficiencies had only a minor energy dependence above \(\sim 25\) keV.

The surface-event rejection was based upon a “timing parameter” consisting of the sum of the rise time of the largest phonon pulse and its delay relative to the ionization pulse. This timing cut was set in the 25–150 keV energy range using Ba and Cf calibration data. Since surface events in WIMP-search data did not have the same recoil-energy and ionization-yield distributions as in Ba calibration data [7], this cut was not expected to be optimal, although corrections based on WIMP-search multiple scatters were applied to the distributions to diminish these differences. Thus, the cut performance had to be tested on WIMP-search data before “unblinding.” The cut setting and testing are discussed in more detail in the following two sections.

Each detector had its own timing-parameter cut. We tuned the set of cuts to yield a given expected “leakage” (number of background events) for the whole data set, while maximizing the signal for a WIMP of mass 100 GeV/c\(^2\) and a mass splitting of 120 keV. For each given expected leakage, using values in steps of 0.1 between 0.1 and 1.5, we ran Monte Carlo simulations to find the average upper limit we could obtain if there were no true WIMP signal. For each expected leakage, \(10^5\) surface-event mock data sets were generated, each with number and energies of background events chosen randomly according to the given expected leakage and the expected energy distribution as estimated from WIMP-search multiple scatters. As was to be done with the actual data, a 90% C.L. upper limit on the spin-independent WIMP-nucleon cross section \(\sigma_{SI}\) was calculated for each mock data set, using the optimum interval method [24] with the WIMP...
recoil-energy distribution [23,25] for the chosen WIMP parameters \(m_W = 100 \text{ GeV}/c^2, \delta = 120 \text{ keV}\). Figure 3 shows the mean upper limit obtained as a function of the expected leakage used in selecting the set of timing-parameter cuts. The timing-parameter cuts were finalized at the values obtained for a fixed expected leakage of 0.6 events, where the minimum was reached.

As explained above, the leakage value chosen for optimizing cuts was not a sufficiently accurate estimate of the expected background. Thus, as with our earlier analysis [7], we used WIMP-search data to improve our estimate of the expected leakage. We estimated the leakage by multiplying the number of WIMP-search nuclear-recoil single scatters failing the timing cut by pass-fail ratios deduced from event samples which were assumed to resemble the population of background events. For detectors that were not located at the top or bottom of their towers (interior detectors), two classes of multiple-scatter events in the WIMP-search data were used independently to estimate the ratios, and therefore the expected background: events with ionization yield within the nuclear-recoil band, and events in which a detector had yield just above or below the nuclear-recoil band. We estimated the leakage in the energy range the cut was defined on (10–25 keV for the previous analysis and 25–150 keV for the analysis presented here). Even though an exposure

![Figure 3](image-url)  
**FIG. 3.** Expected sensitivity of this analysis for a WIMP of mass 100 GeV/c\(^2\) and mass splitting 120 keV for different predefined surface-event leakages at which the timing cut could be fixed. The cut corresponding to the minimum of 0.6 events was chosen as the final cut for this analysis before looking at the WIMP-search signal region.

...
which was larger by a factor of 1.6 was considered for the setting of the timing cut, the final efficiency increased by a factor of $\frac{1}{24}$. This improvement in efficiency was possible because we neglected background at energies below where a signal is expected from iDM.

Neutrons, induced by muons and produced by radioactive processes within the experimental apparatus, constituted an additional background which was indistinguishable from a WIMP interaction in the detectors. Extensive simulations carried out with GEANT4 [27,28] and FLUKA [29,30] indicated that the neutron background in the 25–150 keV energy range inducted by muons is expected to be $0.04 \pm 0.05$ (stat), and the background from radioactive processes is estimated to be between 0.03 and 0.06. The background between 10 keV and 25 keV is predicted to be $0.06 \pm 0.04$ (stat) from muon-induced neutrons and between 0.04 and 0.08 from radiogenic neutrons. These estimates are valid for the reanalyzed exposure and include cut acceptances.

After “unblinding,” 11 events were observed within the acceptance region passing the surface-event rejection cut, three within the 25–150 keV range and eight between 10 keV and 25 keV. Figure 6 shows these candidates, along with all other WIMP-search events in or close to the signal region, which pass all constraints except for cuts on the ionization yield and timing parameter. Most events fail the timing cut (green dots), while most of the few dozen that pass the timing cut ($\times$) fall outside the nuclear-recoil band (blue/solid lines). Eleven events pass all the selection criteria, with three occurring within the 25–150 keV range upon which the surface-event rejection cut was defined, and eight between the 10 keV recoil-energy threshold and 25 keV. The ionization-energy threshold is also shown (blue/dashed-dotted). This threshold and the shown nuclear-recoil band represent the exposure-weighted means over all runs and detectors.

TABLE I. Distribution of the 11 event candidates over detectors and time.

<table>
<thead>
<tr>
<th>Energy (keV)</th>
<th>Detector</th>
<th>Run</th>
<th>Date</th>
</tr>
</thead>
<tbody>
<tr>
<td>10.8</td>
<td>T2Z3</td>
<td>127</td>
<td>31.05.2008</td>
</tr>
<tr>
<td>11.8</td>
<td>T4Z6</td>
<td>124</td>
<td>31.05.2007</td>
</tr>
<tr>
<td>12.3</td>
<td>T1Z5</td>
<td>125</td>
<td>27.10.2007</td>
</tr>
<tr>
<td>12.8</td>
<td>T3Z6</td>
<td>127</td>
<td>01.06.2008</td>
</tr>
<tr>
<td>13.0</td>
<td>T4Z6</td>
<td>125</td>
<td>05.10.2007</td>
</tr>
<tr>
<td>14.7</td>
<td>T3Z6</td>
<td>123</td>
<td>10.12.2006</td>
</tr>
<tr>
<td>15.5</td>
<td>T3Z4</td>
<td>125</td>
<td>05.08.2007</td>
</tr>
<tr>
<td>16.4</td>
<td>T4Z6</td>
<td>123</td>
<td>30.10.2006</td>
</tr>
<tr>
<td>37.3</td>
<td>T4Z6</td>
<td>126</td>
<td>02.02.2008</td>
</tr>
<tr>
<td>73.3</td>
<td>T4Z2</td>
<td>126</td>
<td>04.02.2008</td>
</tr>
<tr>
<td>129.5</td>
<td>T1Z2</td>
<td>123</td>
<td>24.12.2006</td>
</tr>
</tbody>
</table>

*The two marked events are the candidates already found in our previous analysis of runs 125–128 [7]*.
the timing parameter relative to the actual cut position. The black/solid line denotes the timing-cut boundary on the given detector, and the shaded box indicates the acceptance region. The top plot is for T4Z6, with a WIMP candidate at 37.3 keV and three additional candidates below 25 keV. T4Z6 was a detector at the bottom of its tower with reduced background rejection capability. The middle plot shows events in T4Z2, where an event occurred just above the timing-cut boundary with a recoil energy of 73.3 keV. Finally, we show events from T1Z2 in the bottom plot with a candidate above the analysis range from previous analyses at 129.5 keV. This event is far above the timing-cut boundary and would be rejected neither by the surface-event cut from the previous analysis [7], nor by a tighter timing cut tuned to a leakage as low as 0.1 (instead of 0.6) events, which was the most stringent timing cut we tested. No additional events appear in the signal region above 25 keV until the timing cut is loosened to an estimated surface-event leakage of more than 2.0 events.

The probability to observe three or more surface-leakage events between 25 keV and 150 keV given the background distribution \( f(\mu) \) shown in Fig. 4 was calculated as

\[
p = \int_0^\infty d\mu f(\mu) \cdot \sum_{k=3}^{\infty} \frac{e^{-\mu} \mu^k}{k!}
\]

and yields 9%. Inclusion of the estimated neutron background increases this probability to 11%, which is low but not negligible. Thus, this analysis does not constitute a significant detection of WIMP scattering. The probability for eight or more surface-background events between the 10 keV threshold and 25 keV was calculated based on a background distribution obtained analogously to the distribution in the 25–150 keV range and is 29%, which indicates compatibility of our result with the background expectation. The inclusion of the neutron background has a negligible effect on the low-energy range due to the dominant surface-event background.

We used the optimum interval method [24] to compute the 90% C.L. upper limit on the spin-independent cross section as a function of WIMP mass and splitting. All 11 WIMP candidates were included as possible signal, with no background subtraction. The differential rates were calculated under standard halo assumptions according to [25], which gives an updated version of the standard formula from [23], correctly taking the effect of the Earth’s velocity on the escape-velocity cutoff into account. We assumed this escape velocity \( v_{\text{esc}} \) to be 544 km/s [31], while the standard value of 220 km/s was applied for the dispersion \( v_0 \) of the Maxwellian dark matter velocity distribution. Helm form factors and a three-dimensional parametrization of the Earth velocity \( v_E \) were used following [23].

Regions allowed by DAMA/LIBRA at two different C.L.s (90, 99.9%) were computed based on the published modulated spectrum in [6] from an exposure of 1.17 ton-years. As in [7], we followed the \( \chi^2 \) goodness-of-fit technique advocated in [25] to investigate the compatibility between the results from DAMA/LIBRA and CDMS. Quenching factors of 0.30 and 0.09 were applied for Na...
and I nuclei in the DAMA/LIBRA setup, respectively [32]. Possible channeling effects [33] were not included in this study since they do not have a significant impact on the results from an iDM analysis where a signal is expected at tens of keV recoil energy [34].

Selected results from these computations are shown in Fig. 8 in the cross section versus WIMP-mass plane for two chosen WIMP-mass splittings. The left plot shows the standard case with $\delta = 0$ keV, equivalent to assuming elastic scattering, while $\delta = 120$ keV is used for the right plot, a value which is not experimentally excluded by our previous analysis. Apart from the DAMA/LIBRA allowed regions, and constraints emerging from the analysis presented in this paper, the plots also contain cross section limits from our previous analysis of the 10–100 keV energy range [7]. Constraints from the new analysis are less stringent. This was anticipated for the elastic scattering case and low WIMP-mass splittings in general, since more surface-background events were expected at low energies due to the looser timing cut defined in the 25–150 keV energy range. The limits are slightly weaker at $\delta = 120$ keV, due to the occurrence of the three candidates above 25 keV, where the rate is expected to peak for higher WIMP-mass splittings. The eight low-energy events have no effect on this part of the parameter-space due to the utilization of the optimum interval method. WIMP masses above $\sim 100 \text{ GeV/c}^2$ are excluded for this mass splitting by the current and previous analysis.

![Fig. 8](image1.png)

**FIG. 8** (color online). 90% C.L. upper limits on the scalar WIMP-nucleon cross section for WIMP-mass splittings of 0 keV (left) and 120 keV (right) from this analysis (red/dashed) and from our previous analysis (black/solid) [7]. The red/dotted line in the right plot indicates the expected sensitivity for this analysis based on our estimate of the total background. The colored regions represent DAMA/LIBRA allowed regions at two different C.L.s (90, 99.9%) calculated following a $\chi^2$ goodness-of-fit technique [25]. The cross ($\times$) marks the parameter space point which yields the minimum $\chi^2$ in the shown cross section versus WIMP-mass plane given the WIMP-mass splitting.

![Fig. 9](image2.png)

**FIG. 9** (color online). The blue/shaded regions represent WIMP masses and WIMP-mass splittings for which cross sections exist that are compatible with the modulation spectrum observed by DAMA/LIBRA at 90% C.L. The hatched regions show constraints on these parameters from the analysis presented in this paper (red/dashed) and from our previous analysis (black/solid) [7]. The black/dashed line represents the maximum reach of the CDMS II experiment.
Since the iDM parameter space is three-dimensional, consisting of the cross section, WIMP mass, and WIMP-mass splitting, we defined excluded regions by requiring the 90% C.L. upper limit on the cross section from CDMS to completely rule out the corresponding DAMA/LIBRA allowed cross sections (also at 90% C.L.) for given WIMP mass and WIMP-mass splitting. The results are shown in Fig. 9. The only remaining allowed parameter space is within a narrow region at WIMP masses of ~100 GeV/c^2 and WIMP-mass splittings between 85 keV and 135 keV. In the case of the new analysis presented in this paper there is also a tiny area in the low-mass region which is not excluded. The black/dashed line represents the maximum reach in the shown parameter space of an experiment using a Ge target like CDMS II. It is computed based entirely on kinematics by demanding \( v_{\text{min}} = v_{\text{esc}} + v_E \), and is therefore independent of the cross section parameter. Even with higher exposure and increased sensitivity, CDMS II cannot rule out the entire DAMA/LIBRA allowed parameter space simply because

FIG. 10 (color online). Constraints from CDMS on the iDM parameter space allowed by DAMA/LIBRA. Same as Fig. 9 but with different velocity-distribution parameters, as given in the plots. All other parameters remain unchanged.
(relative to an I nucleus) the Ge nucleus is too light. This is the main reason why the constraints from ZEPLIN-III [35], which employs a Xe target, are more stringent. Nevertheless, the results from CDMS II currently have competitive sensitivity compared to the constraints from other Xe based experiments [36,37].

The iDM scenario with a nonzero $\delta$ is particularly sensitive to the high-velocity tail of the dark matter velocity distribution due to the increased minimal velocity (see Eq. (1)). Therefore, it exhibits a strong dependence on the velocity-distribution parameters $v_0$ (the dispersion) and $v_{\text{esc}}$ (the galactic escape velocity) [38]. To examine these dependencies, in Fig. 10 we show plots similar to Fig. 9 but with different values of $v_{\text{esc}}$ and $v_0$. The top plots explore the $v_{\text{esc}}$ 90% C.L. lower and upper limits found in [31] (498 km/s and 608 km/s), while all other parameters remain unchanged relative to Fig. 9. In the bottom plots we varied only $v_0$, assigning a (convenient) lower value of 200 km/s for the left plot and a higher value of 254 km/s (the preferred value according to [39]) for the right plot. The capability of CDMS to constrain an iDM interpretation of the DAMA/LIBRA results is relatively independent of the actual velocity-distribution parameters. However, the shape and location of the parameter space region, which is still allowed by CDMS, has a considerable dependence on $v_{\text{esc}}$ and $v_0$, as expected. Non-Maxwellian velocity distributions as discussed in [40,41] are beyond the scope of this study.

In this paper, we presented the first CDMS analysis which includes recoil energies up to 150 keV. The entire five-tower data set was used in a combined analysis. Because of the occurrence of the three candidate events between 25 keV and 150 keV, the constraints on the iDM parameter space are slightly weaker than from our previous analysis for which no events were observed at intermediate energies where the rate is expected to peak. The only remaining parameter space allowed by CDMS data is within a narrow region at WIMP masses of $\sim$100 GeV/c$^2$ and WIMP-mass splittings between 85 keV and 135 keV, assuming standard values for the WIMP-velocity distribution parameters. Varying the values of these parameters changes this region considerably but has only a minor effect on the capability of CDMS to constrain an iDM interpretation of the DAMA/LIBRA results. Finally, though this analysis was performed with regard to the iDM scenario, the expansion of the analysis range to 150 keV could be useful to test other models predicting a signal at tens of keV recoil energy.

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