Backwater controls of avulsion location on deltas

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River delta complexes are built in part through repeated river-channel avulsions, which often occur about a persistent spatial node creating delta lobes that form a fan-like morphology. Predicting the location of avulsions is poorly understood, but it is essential for wetland restoration, hazard mitigation, reservoir characterization, and delta morphodynamics. Following previous work, we show that the upstream distance from the river mouth where avulsions occur is coincident with the backwater length, i.e., the upstream extent of river flow that is affected by hydrodynamic processes in the receiving basin. To explain this observation we formulate a fluvial morphodynamic model that is coupled to an offshore spreading river plume and subject it to a range of river discharges. Results show that avulsion is less likely in the downstream portion of the backwater zone because, during high-flow events, the water surface is drawn down near the river mouth to match that of the offshore plume, resulting in river-bed scour and a reduced likelihood of overbank flow. Furthermore, during low-discharge events, flow deceleration near the upstream extent of backwater causes enhanced deposition locally and a reduced channel-fill timescale there. Both mechanisms favor preferential avulsion in the upstream part of the backwater zone. These dynamics are fundamentally due to variable river discharges and a coupled offshore river plume, with implications for predicting delta response to climate and sea level change, and fluvo-deltaic stratigraphy.


1. Introduction

Avulsion of rivers near their mouths is one of the main processes that control coastal deposition patterns including land building, delta morphology, and sedimentary basin stratigraphy [e.g., Mackey and Bridge, 1995; Slingerland and Smith, 2004]. Moreover, much of the world’s population lives near deltas, areas subject to catastrophic flooding as a result of river avulsion [e.g., Svistski et al., 2005; Paola et al., 2011]. In light of rising sea level, we need mechanistic models that predict the location of river avulsions to mitigate future hazards and guide wetland restoration efforts.

The necessary conditions for river avulsion have been the subject of ongoing debate [e.g., Bryant et al., 1995; Reitz et al., 2010]. Most workers have focused on controls on avulsion frequency [e.g., Törnqvist et al., 1996; Jerolmack and Mohrig, 2007] and the effect of avulsion on stratigraphic architecture [e.g., Mackey and Bridge, 1995]. For example, using data from the rock record, laboratory experiments, and modern rivers, Mohrig et al. [2000] and Jerolmack and Mohrig [2007] found that the characteristic timescale for avulsion (i.e., the reciprocal of avulsion frequency), $T_A$, is proportional to the time needed to fill one channel depth with sediment, $T_h = h_v/v_A$, where $h_v$ is a characteristic flow depth and $v_A$ is vertical aggradation rate.

There has been less work on the controls on avulsion location, which sets the fundamental length scale of deltas [e.g., Jerolmack, 2009]. Many deltaic rivers tend to avulse at a distance, $L_A$, upstream from the shoreline (i.e., $x = L_A$), where $x$ is the distance along river upstream of the shoreline) with each successive avulsion creating a new depositional lobe that fans out from the avulsion node [e.g., Slingerland and Smith, 2004]. Edmonds et al. [2009] showed in experiments that avulsions tend to occur at locations with persistent overbank flow caused by bed aggradation. Jerolmack and Swenson [2007] showed that $L_A$ scales roughly with a characteristic backwater length, $L_b$, which is the upstream distance over which river hydraulics are affected by the receiving ocean or lake basin [e.g., Chow, 1959] and is typically approximated by $L_b = h_v/S$, where $S$ is the channel bed slope [e.g., Paola, 2000]. Nittouer et al. [2012a] showed that Mississippi River deposition rates are enhanced in the upstream part of the backwater zone, a region coincident with four major avulsions during the Holocene. Our own compilation of the avulsion length scale for different river deltas confirms these observations (Figure 1; see auxiliary material (Text S1, section S1)).

Herein we offer an explanation for the observation that the avulsion length scale correlates with the backwater length (i.e., $L_A \approx L_b$) using a quasi-2D morphodynamic model of a coupled river and river plume system subject to a range of water discharges.

2. Model Goal and Formulation

The avulsion process is complex and a complete model for avulsion location may need to include dynamics at both geomorphic (e.g., levee and delta morphodynamics) and flood (e.g., sediment transport and levee breaching) timescales [e.g., Slingerland and Smith, 2004; Edmonds et al., 2009]. Herein we aim to test two potential controls on the locus of avulsion on deltas that span this range in timescales. First, we hypothesize that the characteristic time for channel filling (which scales with the avulsion timescale, i.e., $T_f \approx T_h$ [Mohrig et al., 2000; Jerolmack and Mohrig, 2007]) is spatially variable and is minimized at $x = L_A$ due to the effect of backwater hydrodynamics on river channel depth and bed aggradation. Second, we hypothesize that the capacity of a channel to contain flood water and therefore mitigate levee...

1Auxiliary materials are available in the HTML. doi:10.1029/2011GL050197.
breaks is spatially variable and increases near the river mouth due to drawdown of the river water surface to match the water depth in the receiving basin [e.g., Lane, 1957]. We quantify the second effect using the water depth during a flood event, $h$, normalized by the normal-flow water depth (i.e., the depth upstream of the backwater zone) for a 2-year recurrence interval flood event, $h_c$.

To test our hypotheses quantitatively, we formulate a mechanistic model for a coupled river and river plume. Most previous models for fluvio-deltaic evolution neglect backwater dynamics either by assuming uniform flow [e.g., Flemings and Jordan, 1989; Swenson et al., 2005] or a single characteristic river discharge [e.g., Parker et al., 2008], which prevents the backwater zone from being dynamic [Lamb et al., 2012]. Herein, we solve the 1-D non-uniform shallow-water flow equations for conservation of fluid mass and momentum [Chow, 1959] (auxiliary material (Text S1, section S2)). We treat the offshore plume as a depth-averaged, steady, homopycnal current, where momentum is balanced in 1-D between a hydrostatic pressure gradient and drag along the bed. We neglect drag and entrainment along the lateral margins of the plume and represent lateral spreading of the plume geometrically by assigning a set spreading angle of $5.7^\circ$ beyond the shoreline ($x < 0$), consistent with theory, experiments, and field observations of planar turbulent jets [e.g., Wright and Coleman, 1971; Rajaratnam, 1976; Rowland et al., 2010]. Lamb et al. [2012] found that backwater dynamics are insensitive to plume spreading for spreading angles greater than $\sim1^\circ$, which is sufficient to render the water-surface elevation at the river mouth relatively insensitive to changes in river discharge as compared to farther upstream. Our model couples these hydrodynamic equations with a semi-empirical transport formula for bed-material load transport and sediment mass conservation that accounts for bed aggradation and degradation (auxiliary material (Text S1, section S2)).

Our goal is to model backwater effects on avulsion over geomorphic timescales as generically as possible, which necessarily neglects the full complexity of a given river (e.g., meandering, overbank flow and bifurcations). Nonetheless, to explore the model results it is useful to use input parameters that scale roughly after a natural river. Here the lower Mississippi River, USA, (auxiliary material, Text S1) is used because it is a large lowland river where backwater and sediment dynamics have been investigated [e.g., Lane, 1957; Karadogan et al., 2009; Nittrouer et al., 2011]. Model simulations were focused on the lower 700 km of the Mississippi River because this incorporates the backwater zone ($x < \sim500$ km) and a comparative region upstream; however, we neglect tributaries and distributaries for simplicity. Model simulations were run for 1500 years, which is the approximate characteristic timescale for avulsion on the Mississippi Delta [e.g., Coleman, 1988].

Three model simulations are presented. For the first case we show results for a constant inflow discharge, a common assumption in fluvial morphodynamic models [e.g., Paola et al., 1992], which does not produce a strong preferential avulsion zone. Second, we show how variable flood discharges force a dynamic backwater zone and may control the avulsion length scale over flood and geomorphic timescales. Third, we show how relative sea-level rise affects the preferential zone for avulsion.

3. Results

For the case of constant river discharge, we set $Q_w = 2.9 \times 10^4 \, \text{m}^3/\text{s}$, which has a 2-year peak-annual-flood recurrence on the Mississippi River and allow the channel to evolve for 1500 yrs. We define the characteristic channel length that accounts for bed aggradation and degradation (auxiliary material (Text S1, section S2)).
depth \((h_c)\) as the normal flow depth for \(Q_w = 2.9 \times 10^4 \text{ m}^3/\text{s}\) at \(x = 700 \text{ km}\) (i.e., far upstream of backwater effects). Model simulations show the expected result that spatial patterns of erosion and deposition shape channel morphology toward a graded state, where deposition occurs only in response to delta progradation [e.g., Muto and Swenson, 2006] (Figure 2a). The water depth in the channel is approximately uniform thereby creating a nearly equal likelihood of levee breaching everywhere (Figure 3a). Likewise, the time to aggrade one channel depth, \(T_h\), gradually decreases downstream and shows no preferential avulsion location at \(x \approx L_b\) (Figure 3b). For this case, the offshore plume has little effect on fluvial morphodynamics, except at the river mouth where spreading forces deposition (Figure 2a).

[10] To explore the effect of variable discharges, we linearly divided the last 88 years of observed daily discharge on the lower Mississippi River (Tarbert Landing, MS; U.S. Army Corps of Engineers) into six bins (Figure 2b and auxiliary material (Text S1, section S2)). In the simulation, a complete cycle of these six discharge events was run (from lowest to highest discharge) for a period of 30 years, which corresponds to the peak-annual-flood recurrence interval of the largest flood event considered \((Q_w = 3.9 \times 10^4 \text{ m}^3/\text{s})\). This cycle was repeated to reach \(T_q = 1500\) years of total run time. A sensitivity analysis revealed using the six discharge bins was sufficient to capture the model dynamics (i.e., further sub-divisions did not significantly change model results) and that model results are insensitive to the order in which the discharge-events occur.

[11] In contrast to the case of steady discharge, variable discharge combined with the spreading offshore river plume results in distinctly different model results. Even after 1500 years the model predicts a backwater zone for low discharges that extends from the shoreline to \(~400 \text{ km}\) upstream (Figure 2a). The backwater zone shows a characteristic downstream increase in water depth because the water depth at the shoreline is greater than the normal flow depth (i.e., \(M_1\) profile; [Chow, 1959]). This creates a zone of spatial deceleration and deposition (Figures 2b and 2c). For \(Q_w < 2 \times 10^4 \text{ m}^3/\text{s}\), as discharge is increased the maximum rate in deposition rate shifts downstream and increases in magnitude. Because the river plume is allowed to spread, the water surface elevation for \(x < 0\) is relatively insensitive to discharge as compared to farther upstream [e.g., Lane, 1957] and is very near sea level, consistent with stage-height measurements that show < 1 m variation near \(x = 0\) [e.g., Karadogan et al., 2009]. For high discharges \((Q_w > 3 \times 10^4 \text{ m}^3/\text{s})\), this results in a water depth at the shoreline that is smaller than the normal-flow depth, which creates a drawdown zone characterized by spatial acceleration and scour [Lamb et al., 2012] (Figure 2). For the high discharge events, deposition only occurs for \(x < 0\) where plume spreading...
forces spatial deceleration. Over many discharge cycles, topography evolves to the suite of discharges such that deposition during low flow is nearly compensated for by erosion during high flow events (Figure 2c), resulting in net aggradation. The net aggradation rate is controlled in part by hydrodynamic feedbacks with the aggrading and prograding delta ($x < 0$; Figure 2a) [e.g., Muto, 2001].

[12] The result of coupling the river to an offshore spreading plume under a range of discharges is a persistent backwater zone that shows deposition at low flows and erosion at high flow, which is consistent with observations from the modern Mississippi River [Nittrouer et al., 2011; Lamb et al., 2012; Nittrouer et al., 2012a]. This has a significant effect on the avulsion length scale metrics. Avulsions occur during floods when rivers are most likely to break or overtop their levees [e.g., Slingerland and Smith, 2004; Edmonds et al., 2009]. Model results show that the flow depth during large flood events is relatively insensitive to discharge for $x < L_b$ due to water-surface drawdown (Figure 3a). In this region, higher discharges are accommodated by increasing the water surface slope rather than increasing the water depth, the latter of which dominates upstream of the backwater zone [Nittrouer et al., 2012b]. This produces a diminished normalized water depth ($h/h_c$) for $x < L_b$, and therefore less likelihood for river avulsion within that zone.

[13] In addition to inducing spatial changes in normalized river depth during high magnitude flood events, backwater dynamics affect the characteristic timescale for channel aggradation, $T_h$. For the variable discharge case, $T_h$ increases in time everywhere because the net aggradation rate, $v_A$, decreases as the channel bed approaches a quasi-steady state (Figure 3b). Due to the persistent backwater zone, deposition rates for low-flow events tend to be greatest within the upstream end of the backwater zone owing to deceleration caused by spatial divergence of the bed and water surface. Furthermore, high discharge events tend to focus scour within the downstream portion of the backwater zone ($x < 0.5 L_b$), which lowers net aggradation rates and increases the channel depth (Figures 2b and 2c), making avulsion less likely there (Figure 3b). The combined effect is a channel-fill timescale ($\frac{T_h}{v_A}$) that has a minimum at about $x = X_{\text{min}} = 0.5 L_b$ after 300 years of model simulation (Figure 3b). The minimum in $T_h$ becomes less pronounced in time and its

**Figure 3.** (a) Modeled water depth ($h$) normalized by the characteristic upstream flow depth ($h_c$) as a function of distance from the shoreline for the case of the Mississippi River with $\sigma = 0$. The lines marked “Constant $Q_w$ run” are the model case with a constant characteristic discharge (2-year flood). The remaining lines show predictions for the model run with variable discharges ($Q_w$) at different model run times ($t$). (b) Model results for channel-fill timescale ($\frac{T_h}{v_A}$) as a function of distance from the shoreline for the case with no base level rise ($\sigma = 0$) and (c) $\sigma = 3$ mm/yr. Arrows indicate the locations of minimum channel-fill time ($X_{\text{min}}$), which suggest a preferential avulsion zone. Results from the variable discharge case are shown at various run times, whereas results from the constant discharge case are shown for $t = 1500$ years. (d) $X_{\text{min}}$ normalized by the calculated backwater length ($L_b$) as a function of time for different rates of base level rise ($\sigma$).
The Mississippi River is inconsistent with observations that the avulsion timescale for the constant discharge case which shows near constant years (Figure 3d). These results are in strong contrast to the Th increases deposition rates everywhere which causes smaller and deposition over longer timescales (Figure 3c). Greater has little effect on the predicted water surface elevation over time.

Blum and Roberts (2009), Kim et al. (2009). Base level rise has little effect on the predicted water surface elevation over flood timescales, but it affects the spatial patterns of erosion and deposition over longer timescales (Figure 3c).

4. Discussion

[15] Our model predicts a channel-fill timescale of \( T_h \approx 6500 \) yrs for the Mississippi River after 1500 years of run time for the case of \( \sigma = 0 \) (Figure 3b). This, however, is inconsistent with observations that the avulsion timescale for the Mississippi River is \( T_D \approx 1500 \) years [e.g., Coleman, 1988]. The inclusion of base level rise in our model increases the predicted deposition rates (i.e., from \( \sim 4 \) mm/yr to \( \sim 5 \) mm/yr in the case \( \sigma = 3 \) mm/yr), which in turn decreases \( T_h \) to values that are more similar to the measured \( T_D \) (Figure 3c). This notwithstanding, a scaling ratio of unity between \( T_h \) and \( T_D \) may not be expected. As noted by Jerolmack (2009), \( T_h > T_D \) for many large rivers and this might be because the height of levees with respect to the neighboring floodplain (i.e., superelevation height, \( \Delta z \)) is a more appropriate length scale for predicting avulsion frequency than the channel depth. For the lower Mississippi River, the inter-avulsion superelevation height is about 5 m (e.g., Törnqvist et al., 1996), which if used in place of channel depth would reduce our predicted avulsion timescales (i.e., \( T_h = \Delta z/v_A \)) by about a factor of five, but would not affect our predictions of avulsion location.

[16] Our model simulations show a zone of drawdown during high flow events and backwater during low flow events, which result in lower flow stages near the river mouth as compared to farther upstream (Figure 3a) and a minimum in the channel-fill timescale upstream of the river mouth (Figures 3b–3d). Both of these effects should lead to a zone of preferential avulsion some distance upstream from the river mouth that scales with the backwater length. Following Bresse [1860], Lamb et al. [2012] showed that for highly subcritical flows (\( Fr < 1 \), where \( Fr \) is the Froude number), the maximum upstream length influenced by drawdown is \( 0.5 h_p/S \) where \( h_p \) is normal flow depth, whereas the maximum extent of backwater at low flows is \( h_p/S \) where \( h_p \) is the depth at the shoreline. Because avulsions are one of the main controls on delta evolution, these scaling relationships explain why delta lobes are more extensive in deep, low gradient rivers (e.g., Figure 1), and they provide a means for estimating delta response to perturbations that affect flow depth, channel depth at the shoreline, and channel slope (e.g., climate-induced changes in river discharge, sea level or sediment supply) [e.g., Jerolmack, 2009]. These scaling relationships may also be useful for reconstructing ancient fluviodeltaic systems from stratigraphy on Earth and Mars [e.g., Paola, 2000]; for example, by allowing estimation of river-channel dimensions from observations of the size of delta lobes and channel slope.

5. Conclusions

[17] To explain the observation that river avulsions on deltas tend to occur at the upstream extent of the backwater zone, we performed a numerical simulation of a coupled river and river plume system subject to variable flow discharges. Results show that there is an exclusion zone, where avulsion is less likely than other locations, that persists throughout the inter-avulsion time period for the Mississippi River (\( \sim 10^3 \) years) and that corresponds roughly to half the backwater length (i.e., \( x < 0.5L_b \)). Within this zone, relative flow stage heights (i.e., \( h/h_s \)) are diminished and the deposition timescales to fill a channel (i.e., \( h_s/v_A \)) are large; both metrics indicate that avulsion is less likely in the downstream portion of the backwater zone. Moreover, the channel fill timescale shows a minimum in the upstream portion of the backwater zone due to preferential deposition there, resulting in a predicted heightened frequency of avulsions. This preferential zone for avulsion exists because variable flow discharges result in backwater hydrodynamics at low flows and drawdown hydrodynamics at high flows, which in turn create spatial variations in deposition patterns and flow depths. These dynamics do not exist for simulations with constant river discharge, which suggests that variable discharges and an offshore spreading plume may be needed to accurately simulate fluviodeltaic morphodynamics.

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References


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