Experimental Investigation of Rotor–Stator Interaction in a Centrifugal Pump With Several Vaned Diffusers

This paper describes an experimental investigation of rotor–stator interaction in a centrifugal pump with several vaned diffusers. Steady and unsteady diffuser vane pressure measurements were made for a two-dimensional test impeller. Unsteady impeller blade pressure measurements were made for a second two-dimensional impeller with blade number and blade geometry identical to the two-dimensional impeller used for the diffuser vane pressure measurements. The experiments were conducted for different flow coefficients and different radial gaps between the impeller blade trailing edge and the diffuser vane leading edge (5 and 8 percent of the impeller discharge radius). The largest pressure fluctuations on the diffuser vanes and the impeller blades were found to be of the same order of magnitude as the total pressure rise across the pump. The largest pressure fluctuations on the diffuser vanes were observed to occur on the suction side of the vane near the vane leading edge, whereas on the impeller blades the largest fluctuations were observed to occur at the blade trailing edge. However, the dependence of the fluctuations on the flow coefficient was found to be different for the diffuser vanes and the impeller blades; on the vane suction side, the fluctuations were largest for the maximum flow coefficient and decreased with decreasing flow coefficient, whereas at the blade trailing edge, the fluctuations were smallest for the maximum flow coefficient and increased with decreasing flow coefficient. Increasing the number of the diffuser vanes resulted in a significant decrease of the impeller blade pressure fluctuations. The resulting lift on the diffuser vanes was computed from the vane pressure measurements; the magnitude of the fluctuating lift was found to be larger than the steady lift.

Introduction

Blade and vane design in diffuser pumps, and also in centrifugal compressors, is currently based upon the assumption that the flow in both the impeller and the diffuser is steady. This, however, implies that the radial gap between the impeller discharge and the diffuser inlet is large so that no flow unsteadiness of any kind due to rotor–stator interaction may occur. If, however, the radial gap between the impeller blades and the diffuser vanes is small, i.e., of the order of a small percentage of the impeller discharge radius, as it actually is for many diffuser pumps, there may be a strong interaction that may influence both the aerodynamic and the structural performance of the impeller blades and the diffuser vanes. Cavitating damage observed at the trailing edges of the impeller blades of high-speed centrifugal pumps, such as the High Pressure Oxygen Turbopump (HPOTP) of the Space Shuttle Main Engine (SSME) may also result from fluctuating blade pressures, which are due to rotor–stator interaction.

The rotor–stator interaction may be divided into two different mechanisms: potential flow interaction and wake interaction (Dring, 1982). The potential flow interaction between the two blade rows moving relative to each other arises because of the circulation about the blades and because of the potential fields, other than circulation, about the blades that are due to the finite thickness of the blades (Lefcourt, 1965). The potential flow fields about a blade extend both upstream and downstream of a blade. The wake interaction refers to the unsteadiness induced at a blade row by the wakes shed by the blades of an upstream blade row and convected downstream. Both potential flow interaction and wake interaction may result in unsteady forces of significant size on both the impeller blades and the diffuser vanes. If the radial gap between the impeller blades and the diffuser vanes is small both interaction mechanisms will occur simultaneously, and will influence each other.

1Present address: MTU (Motoren-und Turbinen Union München GmbH), Postfach 500640, 8000 München 50, Federal Republic of Germany.
Most of the work on blade row interaction with the aim of measuring unsteady blade pressures has been carried out on axial turbomachinery. Among others, Dring et al. (1982) investigated blade row interaction in an axial turbine and found both potential flow and wake interaction for closely spaced blade rows (15 percent based on chord). Significant pressure fluctuations of up to 72 percent of the exit dynamic pressure were measured near the leading edge of the rotor. Gallus (1979) and Gallus et al. (1980) reported measurements on axial compressors. The blade rows were spaced relatively far apart (60 percent based on chord), such that the potential flow interaction between the rotor and the stator was weak; i.e., the pressure fluctuations on the compressor stator were found to be considerably larger than those on the compressor rotor. In radial turbomachinery, impeller blade pressure measurements were reported by Inoue and Kasai (1985). The radial gap between the impeller blades and the diffuser vanes was small, so that significant pressure fluctuations on the impeller blades were observed. Furthermore, it was found that blade and vane angle have an important influence on the blade pressure fluctuations. Flow field investigations in centrifugal compressors have been reported among others by Inoue and Cumptsy (1984) and Stein and Rautenberg (1988). Diffuser vane pressure measurements using the impeller of the High Pressure Turbopump of the Space Shuttle Main Engine were made by Arndt et al. (1989). Experiments were made for radial gaps of 1.5 and 4.5 percent (based on the impeller discharge radius) between the impeller blades and the diffuser vanes. The pressure fluctuations were found to be of the same order of magnitude as the total pressure rise across the pump.

To investigate the complete rotor-stator interaction mechanism, unsteady pressure measurements have to be made on both the impeller blades and the diffuser vanes. In this paper, the results of such measurements using a two-dimensional centrifugal test impeller and different vaned radial diffusers will be presented. To the authors' knowledge, this is the first publication reporting both unsteady impeller blade and unsteady diffuser vane pressure measurements in a diffuser pump. All measurements were obtained for noncavitating flow.

Data will be presented on steady and unsteady diffuser vane pressure measurements along midvane height. Superimposing the steady and ensemble-averaged unsteady vane pressure, the ensemble-averaged vane pressure was obtained (it was assumed that the steady pressure value measured with mercury manometers was identical to the time mean pressure about which the piezoelectric pressure transducers, used for the unsteady measurements, measure the unsteady pressure). Steady and unsteady computations of the force on the vane were made from those pressure measurements. A second two-dimensional impeller, referred to as Impeller Z2, with the same blade number and the same blade geometry as Impeller Z1, was used for the impeller blade pressure measurements. For those measurements, different diffuser vane configurations were used to investigate the influence of the vane number and the vane leading edge mean line angle (also referred to as vane angle) on the impeller blade pressure fluctuations.

During the tests, the impellers could only be positioned at locations on an orbit concentric to the diffuser center (orbit radius = 1.27 mm), so that the radial gap between the impeller blade trailing edge and the leading edge of any instrumented diffuser vane could be varied between 5 and 8 percent of the impeller discharge radius. Similarly, for the impeller blade pressure measurements, the radial gap between the in-

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**Nomenclature**

\[ a_i, b_i = \text{coefficient of the } i\text{th cos and the } i\text{th sin term in a Fourier series, normalized by } (1/2)\omega u_l^2 \]

\[ A_2 = \text{impeller discharge area} \]

\[ b_2 = \text{impeller discharge width} \]

\[ b_3 = \text{diffuser inlet width} \]

\[ c = \text{vane chord} \]

\[ c_{b_0} = \text{blade pressure coefficient} = p_{b_0} / (1/2)\omega u_l^2 \]

\[ c_{l} = \text{magnitude of } n\text{th Fourier coefficient} = \sqrt{a_i^2 + b_i^2} \]

\[ c_L = \text{life coefficient} = L / (1/2)\omega u_l^2 \]

\[ \bar{c}_p = \text{steady vane pressure coefficient} = (p_v - p_{\text{amb}}) / (1/2)\omega u_l^2 \]

\[ \bar{c}_{p,\text{av}} = \text{ensemble-averaged unsteady vane pressure coefficient} = \bar{p}_v / (1/2)\omega u_l^2 \]

\[ c_{p, \text{av}} = \text{ensemble-averaged vane pressure coefficient} = c_{\text{av}} + \bar{c}_{p,\text{av}} \]

\[ d_2, d_3 = \text{impeller discharge diameter, diffuser inlet diameter} \]

\[ F = \text{force vector on diffuser vane} \]

\[ f = \text{frequency} \]

\[ f_b = \text{impeller blade passage frequency} = z_b / (\text{rpm}/60) \]

\[ f_s = \text{shaft frequency} = (\text{rpm}/60) \]

\[ f_v = \text{diffuser vane passage frequency} = z_v / (\text{rpm}/60) \]

\[ L = \text{lift (component of the force vector on the vane normal to the chord joining the vane leading edge and the vane trailing edge)} \]

\[ \phi = \text{flow coefficient} = \phi / u_L A_2 \]

\[ \psi = \text{total head coefficient} = (\rho_{\text{down}} - \rho_{\text{up}})/\rho u_v^2 \]

\[ \omega = \text{radian frequency} = 2 \pi f \]

**Subscripts**

\[ a_v = \text{ensemble averaged} \]

\[ b = \text{impeller blade} \]

\[ \text{down} = \text{downstream} \]

\[ \text{max} = \text{maximum} \]

\[ s = \text{shaft} \]

\[ \text{up} = \text{upstream} \]

\[ v = \text{diffuser vane} \]

**Superscripts**

\[ \sim = \text{steady} \]

\[ \sim = \text{unsteady} \]

**Abbreviations**

FP = pressure side of impeller blade
FS = suction side of impeller blade
LE = diffuser vane leading edge
PCB = PCB Piezoelectronics, Inc., Depew, NY 14043
PS = diffuser vane pressure side
SS = diffuser vane suction side
TE = diffuser vane trailing edge
measured on the particular instrumented impeller blade and diffuser vane.

Test Facility and Instrumentation

The experiments were conducted in a recirculating water test loop. The facility has been described in detail by Arndt (1988). A simplified view of the test section with the two-dimensional test impeller for impeller blade pressure measurements, Impeller Z2, installed is shown in Fig. 1.

The two two-dimensional impellers have identical blade number and identical blade shape (five logarithmic spiraled blades with a blade angle of 25 deg). Impeller Z1 existed from previous work when the current investigation was started, and was used for most of the diffuser vane pressure measurements, but difficult to modify for impeller blade pressure measurements. Subsequently, Impeller Z2 was designed and built to permit impeller blade pressure measurements by mounting pressure transducers to the impeller. A photograph of Impeller Z2 installed in the test facility is shown in Fig. 2 (the front shroud of the impeller was removed to show the impeller blade shapes). Impeller blade pressure measurements were made at three pressure taps on the impeller blades, one on the blade pressure side \( (R/R_2 = 0.987) \), one at the impeller blade trailing edge \( (R/R_2 = 1.0) \), and one on the impeller blade suction side \( (R/R_2 = 0.937) \). The signals from the pressure transducers were transmitted by cables from the pressure transducers to a slip ring assembly and from there to the pressure transducer power supply.

Diffuser vane pressure measurements were made using a straight wall constant width diffuser with nine vanes, referred to as Diffuser S. No volute, however, is provided. Thus, the flow is discharged from the diffuser into a large housing. The shape of a vane, with the pressure taps at midvane height, is shown in Fig. 3. It is identical to the one used in an early version of the diffuser of the High Pressure Oxygen Turbopump (HPOTP) of the Space Shuttle Main Engine (SSME); however, the number of diffuser vanes was reduced from seventeen to nine. Unsteady vane pressure measurements using this diffuser and one half of the double-suction pump impeller of the HPOTP of the SSME have been reported by Arndt et al. (1989).

A second diffuser, of side wall geometry and diffuser channel width identical to Diffuser S, but permitting variable diffuser vane configurations was used to investigate the effects of the number of diffuser vanes and of the vane leading edge mean angle (also referred to as the vane angle), \( \beta^* \), on the impeller blade pressure measurements. This diffuser employed circular arc vanes with the geometry listed in Table 2.

Four different diffusers were used for the unsteady impeller blade pressure measurements (diffuser vane pressure measurements could only be made with Diffuser S); the details
are listed in Table 3. In Fig. 2, a photograph showing Impeller Z2, with the front shroud removed to show the impeller blade shapes, and Diffuser G is presented.

Steady pressure measurements were obtained by using conventional mercury manometers. The wall pressure about 350 mm upstream of the impeller inlet, \( \rho_{w} \), was used as reference pressure. The experimental error on the steady pressure measurements, i.e., on \( (\hat{\rho} - \hat{\rho}_{w}) \), was estimated to be \( \pm 0.5 \) percent of \( (\hat{\rho} - \hat{\rho}_{w}) \).

Piezoelectric pressure transducers with built-in amplifiers from PCB Inc. were used for the unsteady measurements. This particular transducer (Model 105B02) was selected because of its small size (diameter: 2.54 mm), high resonant frequency (250 kHz), and high resolution (~70 N/m²). Because of the relatively short discharge time constant of the transducer of 1 s, static calibration means could not be used. Instead, the dynamic calibration provided by the manufacturer was used. The linearity of the calibration was within 2 percent. The resonant frequency of the impeller blade and the diffuser vane pressure taps, the geometry of which is shown in Fig. 4, was estimated to be approximately 8000 Hz. The spectrum of unsteady pressure measurements (Fig. 5) shows that the estimate of the resonant frequency was reasonable. It can be seen that the blade passage frequency and its higher harmonics are “far” removed from the resonant frequency of the pressure tap, so that amplification and phase shift were negligible.

The data were sampled and discretized in a 16-channel data acquisition system. An encoder on the main shaft was used to trigger the data acquisition system and to provide a clock for the data acquisition system. 1024 data points were taken during one shaft revolution. Since the signal contained some noise, the unsteady data were ensemble averaged over one impeller revolution. The experimental error was found to be less than \( \pm 5 \) percent for the magnitude and less than \( \pm 2 \) percent (360 deg corresponding to one impeller blade passage) for the phase of the ensemble-averaged unsteady pressure measurements.

Overall Performance

Performance curves for Impeller Z2 and the different vaned diffusers are shown in Fig. 6. The largest flow coefficients were obtained using Diffuser S (the modified SSME diffuser) and Diffuser G (\( z_{p} = 6, \beta^{*} = 20 \) deg). For those diffusers, the head rise for large flow coefficients, \( \phi \geq 0.9 \), was larger than for Diffuser F (\( z_{p} = 12, \beta^{*} = 20 \) deg) and for Diffuser H (\( z_{p} = 6, \beta^{*} = 10 \) deg). For low flow coefficients, \( \phi \leq 0.07 \), Diffuser F had the largest head rise. Diffuser H had the smallest head rise of all diffusers in the range of flow coefficients investigated.

Diffuser Vane Pressure Measurements for Diffuser S

Steady Vane Pressure Measurements and Steady Vane Lift Computations. The steady vane pressure measurements are presented as a steady pressure coefficient, normalized by the dynamic pressure based on impeller tip speed, \( (1/2)\rho u_{t}^{2} \),

\[
\hat{c}_{p} = \frac{\hat{\rho}_{v} - \hat{\rho}_{w}}{(1/2)\rho u_{t}^{2}}
\]

Steady diffuser vane pressure measurements were made for three flow coefficients, \( \phi = 0.135, 0.10, \) and \( 0.06 \), two radial gaps between diffuser vanes and impeller blades (5 and 8 percent of the impeller discharge radius), and a rotational speed of 1200 rpm. The steady vane pressure distribution for the medium flow coefficient, \( \phi = 0.10 \), is shown in Fig. 7. The pressure distribution on the vane changes only slightly with increasing radial gap. Furthermore, the diffusion on the vane suction side can be clearly seen.

From the steady vane pressure measurements at midvane height, the steady force on the vane at midvane height was computed. The steady pressure distribution around the vane...
was obtained by fitting a third-order periodic spline through the measured data. A periodic spline fit was chosen to get continuity for the pressure and the first two pressure derivatives at the vane leading and the vane trailing edge. Hence, the steady force was computed from

$$
\mathbf{F} = -\frac{1}{3} \int \left( \hat{p}_v - \hat{p}_{up} \right) (\xi) n d\xi
$$

The lift on the vane was defined as the component of the force on the vane normal to the chord joining the vane leading and trailing edges. The lift on the vane was defined as positive if the force component normal to the vane chord was in the positive y direction (Fig. 3). The lift is presented as a lift coefficient, normalized by the dynamic pressure based on impeller tip speed, $(1/2)\rho u_t^2$, and the vane chord c,

$$
\bar{c}_L = \frac{L}{(1/2)\rho u_t^2 c}
$$

The steady lift on the diffuser vane versus flow coefficient vanes is shown in Fig. 8. It can be seen that the steady lift increases significantly with decreasing flow coefficient. With the exception of the lowest flow coefficient, $\phi = 0.06$, the steady lift and moment decrease slightly with increasing radial gap.

**Ensemble-Averaged Unsteady Vane Pressure Measurements and Spectra of Unsteady Vane Pressure Measurements.** The unsteady vane pressure measurements were ensemble averaged, and will be presented as an ensemble-averaged vane pressure coefficient, normalized by the dynamic pressure based on impeller tip speed,

$$
\bar{c}_{p,av} = \frac{1}{N} \sum_{j=1}^{N} \bar{p}_j (i,j) \left( \frac{1}{2} \rho u_t^2 \right)
$$

where $N$ is the number of averaging periods, $i$ the $i$th data point taken in any of the $N$ averaging periods, and $j$ the $j$th of the $N$ averaging periods. During one averaging period, corresponding to one main shaft revolution (or five impeller blade passages), 1024 data points were taken. A total of 512 averaging periods was used for the ensemble averages. Furthermore, spectra of the unsteady data were obtained. In Fig. 9, a sample of the ensemble-averaged vane pressure fluctuations is presented. The measurements were made at pressure tap S2C, for the medium flow coefficient, $\phi = 0.10$, and $R_3/R_2 = 1.05$ (the pressure tap S2C was selected since the largest vane pressure fluctuations occurred at that measurement location). The ensemble-averaged vane pressure fluctuations are shown in the upper half of the figure. The position of the impeller blades is referenced to the diffuser vane leading edge. The magnitude of the Fourier coefficients relative to the magnitude of the largest Fourier coefficient ($c/c_{max}$) is shown versus frequency (upper horizontal scale) and frequency normalized by impeller blade passage frequency ($f/f_p$) (lower horizontal scale) in the lower half of the figure.

It is evident that the pressure fluctuations are periodic with the impeller blade passage frequency, and of the same order of magnitude as the total pressure rise across the pump. The largest pressure at this particular measurement location (S2C) occurs right before the pressure side of the impeller blade trailing edge reaches the diffuser vane leading edge. As the blade trailing edge passes the vane leading edge, the pressure decreases sharply and attains its minimum as the suction side of the blade trailing edge reaches the vane leading edge. Then, the pressure rises sharply as the impeller blade moves away from the vane leading edge. Hence, most of the pressure fluctuations occur during a rather short time, corresponding to about one third of the impeller blade passage period. The spectrum of the unsteady pressure measurements at tap S2C is dominated by the impeller blade passage frequency and its higher harmonics. In fact, the second harmonic is slightly larger than the first.

**Magnitude of Ensemble-Averaged Diffuser Vane Pressure Fluctuations.** In the following figures, data on the magnitude of the ensemble-averaged unsteady vane pressure measurements at midvane height are presented. The magnitude of the pressure fluctuations is defined as the difference between the maximum and minimum pressure value in the averaging period, which corresponds to one impeller
revolution. The largest fluctuations, independently of flow coefficient or radial gap, occur at the vane leading edge and on the front half of the vane suction side. Those fluctuations are of the same order of magnitude as the total pressure rise across the pump. The fluctuations are larger on the vane suction than on the vane pressure side. On the vane pressure side, they decrease monotonically from the leading edge to the trailing edge, whereas on the vane suction side they have a relative minimum at pressure tap S1C, and they decrease from pressure tap S2C monotonically to the vane trailing edge. For the two flow coefficients investigated, the largest fluctuations occur either at the vane leading edge or at pressure tap S2C.

Figure 10 shows the dependence of the fluctuations on the radial gap between impeller blades and diffuser vanes, \( R_1/R_2 = 1.05 \) and 1.08, for \( \phi = 0.10 \) and 3000 rpm. The large pressure fluctuations on the front half of the suction side, at the leading edge, and at the pressure tap on the pressure side closest to the leading edge decrease significantly with increasing radial gap. However, at the pressure taps on the rear half of the vane suction side and at the other pressure taps on the pressure side, the pressure fluctuations remain virtually unchanged.

Figure 11 compares the fluctuations for the two flow coefficients, \( \phi = 0.135 \) and 0.10, at 3000 rpm and \( R_1/R_2 = 1.05 \). At the leading edge and at all the pressure taps on the suction side, the fluctuations are larger for \( \phi = 0.135 \) than for \( \phi = 0.10 \). With the exception of pressure tap P1C, where the fluctuations are larger for \( \phi = 0.10 \) than for \( \phi = 0.135 \), the magnitude of the pressure fluctuations on the vane pressure side is nearly identical for the two flow coefficients.

For one pressure tap, S2C, unsteady vane pressure measurements were made over a range of flow coefficients, ranging from maximum flow coefficient, \( \phi_{\text{max}} = 0.135 \), to \( \phi = 0.06 \). The shaft speed during those tests was 1500 rpm (comparing the normalized pressure measurements for \( \phi = 0.135 \) and 0.10 made at 1500 and 3000 rpm, virtually no shaft speed dependence was found). In Fig. 12, the magnitude of the fluctuations as functions of flow coefficient and radial gap, relative to the magnitude of the fluctuation for maximum flow, \( \phi = 0.135 \), at a radial gap of 5 percent, are presented. It can be seen that the fluctuations are largest for the maximum flow coefficient and decrease with decreasing flow coefficient. Increasing the radial gap between impeller blades and diffuser vanes resulted in about a 50 percent decrease of the fluctuations. Comparing the normalized total pressure rise across the pump (Fig. 6) to the normalized impeller blade pressure fluctuations, it can be seen that the magnitude of the vane pressure fluctuations for the maximum flow coefficient, \( \phi = 0.135 \), is about 95 percent of the total pressure rise across the pump.

Steady and unsteady diffuser vane pressure measurements using one half of the double-suction pump of the High Pressure Oxygen Turbopump of the Space Shuttle Main Engine were reported by Arndt et al. (1989). The vane pressure fluctuations for comparable radial gaps between impeller blades and diffuser vanes were found to be of similar magnitude.

**Magnitude and Phase of Fourier Coefficients of Ensemble-Averaged Vane Pressure Fluctuations.** The magnitude and the phase of the Fourier coefficients corresponding to impeller blade passage frequency \( f_3 \), twice impeller blade passage frequency \( 2f_3 \), and three times the impeller blade passage frequency \( 3f_3 \), will be presented for the medium flow coefficient, \( \phi = 0.10 \), and a radial gap of 5 percent. A curve is drawn through the data points in Figs. 14 and 15 (magnitude and phase of the blade passage harmonics). The drawn curve has no significance other than to connect the data points as an aid in viewing the data.

The magnitudes of the Fourier coefficients are presented in Fig. 14. Note that the vertical scale, for the magnitude of the coefficients, is not a linear but a logarithmic one. The magnitude of the first harmonic, i.e., the impeller blade passage harmonic, is approximately equal at most pressure taps on the front half of the vane suction and the vane pressure side (taps P1C, P2C, S0C, S2C, and S3C).
Fig. 14 Magnitude of the Fourier coefficients of impeller blade passage harmonics for Impeller Z1 and Diffuser S (φ = 0.10, R3/R2 = 1.05, rpm = 1200)

Fig. 15 Phase of the Fourier coefficients of impeller blade passage harmonics for Impeller Z1 and Diffuser S (φ = 0.10, R3/R2 = 1.05, rpm = 1200)

The magnitudes of the second and third blade passage harmonics, however, are significantly larger on the front half of the vane suction than on the vane pressure side. In fact, the magnitude of the second harmonic at the pressure taps on the front half of the vane suction side is as large or larger than the magnitude of the first harmonic. On the rear half of the vane suction side, the magnitude of the first harmonic is, however, significantly larger than the second harmonic. In contrast, on the rear half of the vane pressure side, the magnitude of the second harmonic is larger than the magnitude of the first harmonic.

Hence, higher impeller blade passage harmonics do contribute significantly to the diffuser vane pressure fluctuations and cannot be neglected in an analysis.

The phase angle of the blade passage harmonics is shown in Fig. 15. The reference configuration, i.e., the geometric configuration at which the data-taking process was started, is shown schematically in Fig. 13. It can be seen that there is a significant difference in phase, of ~70 deg, between the first impeller blade passage harmonic on the front half of the vane suction side and the front half of the vane pressure side.

**Ensemble-Averaged Lift Computations.** From the vane pressure measurements described earlier, the force on the vane at midvane height was computed. Since those measurements were obtained on different vanes, they had to be phase shifted to one reference vane for the force computations. Superimposing the steady and ensemble-averaged unsteady pressure measurements, the ensemble-averaged vane pressure distribution was obtained. From the ensemble-averaged pressure distribution, the ensemble-averaged force was computed. The ensemble-averaged pressure distribution on the vane was obtained by fitting a third order periodic spline through the measured pressure values. A periodic spline fit was chosen to get continuity for the pressure and the first two pressure derivatives at the leading and trailing edge. The ensemble-averaged force was computed from

\[ F_{av} = -\int (\bar{p}_e + \bar{p}_{u,av} - \bar{p}_{up}) (\xi) n d\xi \]

where \( \bar{p}_e \) is the ensemble-averaged pressure, \( \bar{p}_{u,av} \) is the ensemble-averaged unsteady pressure, and \( \bar{p}_{up} \) is the ensemble-averaged pressure at the upstream location.

The lift on the vane was defined as the component of the force on the vane normal to the chord joining the vane leading and trailing edge. The lift on the vane was defined as positive if the force component normal to the vane chord was in the positive \( y \) direction (Fig. 3). The ensemble-averaged lift is presented as an ensemble-averaged lift coefficient, normalized by the dynamic pressure based on impeller tip speed, \( (1/2)\rho U_e^2 \), and the vane chord, \( c_v \)

\[ c_{L,av} = \frac{L_{av}}{(1/2)\rho U_e^2} \]

In Figs. 16 and 17 data on the ensemble-averaged lift on the ratio of ensemble-averaged to steady lift are presented. The position of the impeller blade is referenced to the diffuser vane leading edge. The averaging period for ensemble averaging was one shaft revolution, corresponding to five impeller blade passages; the data for the first half of the shaft revolution are presented.
Fig. 17 Ratio of ensemble-averaged lift to steady lift on the diffuser vane at midvane height for Impeller Z1 and Diffuser S (\(\phi = 0.10\), \(R_3/R_2 = 1.05\) and \(1.08\), rpm = 1200)

In Fig. 16, the ensemble-averaged lift for the two flow coefficients investigated, \(\phi = 0.135\) and \(\phi = 0.10\), is shown for a radial gap of 5 percent. It can be seen that the lift fluctuations are larger for the maximum flow coefficient than for the medium flow coefficient. Minimum lift is attained as the pressure side of the impeller blade trailing edge reaches the vane leading edge. As the blade trailing edge passes the vane leading edge, the lift increases from its minimum to its maximum value, which is attained as the suction side of the impeller blade trailing edge reaches the vane leading edge. As the impeller blade moves away from the diffuser vane trailing edge, the lift does first decrease to approximately its mean value. Then the lift stays relatively constant for about a third of the blade passage period before dropping to its minimum value.

This behavior, i.e., the relatively constant lift on the diffuser vane for a significant part of the impeller blade passage period, is in contrast to the results on diffuser lift fluctuations using one half of the double-suction impeller of the High Pressure Oxygen Turbopump of the Space Shuttle Main Engine and Diffuser S (Arndt et al. 1989). For the impeller of the SSME, the lift on a diffuser vane of the same impeller decreased strongly monotonically from its maximum to its minimum value. The impeller of the SSME has more blades, eight in contrast to five for Impeller Z1. Hence, due to the smaller number of impeller blades, there is an interval of time in a blade passage period during which the influence of the impeller blade–diffuser vane interaction on the unsteady lift is small; i.e., the ensemble-averaged pressure distribution about the vane was observed to be nearly identical to the steady pressure distribution about the vane \(\left(c_{p,v} = c_p\right)\). The magnitude of the lift fluctuations, however, was found to be approximately equal for the two impellers for comparable flow coefficients and radial gaps between impeller blades and diffuser vanes.

The ratio of the ensemble-averaged lift to the steady lift for the medium flow coefficient, \(\phi = 0.10\), and radial gaps of 5 and 8 percent is shown in Fig. 17. For both radial gaps, the ratio is about 2, decreasing slightly with increasing radial gap.

Unsteady Impeller Blade Pressure Measurements Using Diffuser S

Unsteady impeller blade pressure measurements were made at three pressure taps on the impeller blades, one on the pressure side \((R/R_2 = 0.987)\), one on the suction side \((R/R_2 = 0.937)\), and one on the trailing edge \((R/R_2 = 1.00)\). Herein, the measurements made for Diffuser S and the two-dimensional impeller are presented. Data were taken for eight flow coefficients, ranging from \(\phi = 0.135\) to \(\phi = 0.06\) at 1500 rpm. Since the impeller was positioned eccentrically to the diffuser center, the radial gap between impeller blade trailing edge and diffuser vane leading edge varied during one impeller revolution from 5 to 8 percent of the impeller discharge radius.

Fig. 18 Ensemble-averaged unsteady blade pressure measurements and spectrum of unsteady blade pressure measurements at the blade trailing edge pressure tap for Impeller Z2 and Diffuser S (\(\phi = 0.10\), rpm = 1500)

Ensemble-Averaged Unsteady Blade Pressure Measurements and Spectra of Unsteady Blade Pressure Measurements. Similarly to the unsteady vane pressure measurements, the unsteady blade pressure measurements were ensemble averaged, and will be presented as an ensemble-averaged blade pressure coefficient, normalized by the dynamic pressure based on impeller tip speed. Furthermore, spectra of the unsteady measurements were obtained.

In Fig. 18, the ensemble-averaged unsteady blade pressure measurements and the corresponding spectrum of the unsteady blade pressure measurements at the blade trailing edge pressure tap are presented for a medium flow coefficient, \(\phi = 0.10\). In the upper part, the ensemble-averaged blade pressure fluctuations are shown. The pairs of broken lines indicate the passage of the pressure side and the suction side of the impeller blade trailing edge past the diffuser vane leading edge. The one pair of the solid lines indicates the passage of the pressure side and the suction side of the impeller blade trailing edge past the diffuser vane leading edge at the smallest radial distance between the instrumented impeller blade and the diffuser vanes. That smallest radial gap between the impeller blade trailing edge and diffuser vane leading edge is 5 percent of the impeller discharge radius. In the lower part of the figure, the magnitude of the Fourier coefficients relative to the largest Fourier coefficient \(c_{p,max}\) is shown versus frequency (upper horizontal scale) and frequency normalized by impeller vane passage frequency \(f/f_0\) (lower horizontal scale).

It can be seen that the magnitude of the fluctuations varies significantly during one impeller revolution. This is due to the varying distance between the impeller blade trailing edge and the diffuser vane leading edges as the impeller completes one revolution. The trailing edge pressure fluctuations are largest during the vane passage following the smallest gap between the specific instrumented impeller blade and the diffuser vanes. The minimum pressure at the trailing edge pressure tap within each diffuser vane passage is attained after the impeller blade trailing edge has passed the diffuser vane leading edge. The trailing edge pressure then rises sharply to its maximum value, which is attained before the impeller blade trailing edge reaches the next vane leading edge.

In the corresponding spectrum of the unsteady blade pressure measurements, four different discrete frequency components can be found. First, vane passage frequency and its higher harmonics, \((f/f_0) = 1, 2, \ldots\), are the dominant fre-
In contrast to the trailing edge pressure fluctuations, the pressure fluctuations at the pressure and suction side pressure taps are not significantly dependent upon flow coefficient. Maxima are attained for \( \phi = 0.11 \) at the pressure side pressure tap, for \( \phi = 0.10 \) at the suction side pressure tap, and for \( \phi = 0.06 \) at the suction and pressure side pressure tap. Minima are attained for maximum flow, \( \phi = 0.135 \), at both the pressure and suction side pressure tap, and for \( \phi = 0.09 \) at the pressure side pressure tap, and for \( \phi = 0.08 \) at the suction side pressure tap. The magnitude of the fluctuations at the pressure and suction side pressure tap, however, was found to be quite different. At the pressure side pressure tap, the fluctuations were about two to three times larger than at the suction side pressure tap. For maximum flow, the fluctuations at the pressure side pressure tap were even slightly larger than those at the trailing edge pressure tap. Not increasing significantly with decreasing flow coefficient, however, the fluctuations at the pressure side pressure tap for low flow coefficients were only about half as large as those at the trailing edge pressure tap.

**Unsteady Impeller Blade Pressure Measurements Using Different Diffusers**

Unsteady impeller blade pressure measurements were also made for a second diffuser, with sidewall geometry identical to that of Diffuser S, but permitting variable diffuser vane configurations. Three different vane configurations employing circular arc vanes were tested (see also Table 3). Diffuser F employed twelve vanes with a vane angle \( \beta^* \) of 20 deg, Diffuser G six vanes with a vane angle of 20 deg, and Diffuser H six vanes with a vane angle of 10 deg. Hence, the different diffuser vane configurations permitted an investigation of the influence of the diffuser vane number and of the diffuser vane angle on the impeller blade pressure fluctuations.

**Magnitude of Ensemble-Averaged Blade Pressure Fluctuations.** The influence of the different diffuser vane configurations on the unsteady impeller blade pressure measurements is presented in Fig. 20 for the trailing edge pressure tap, in Fig. 21 for the pressure side pressure tap, and in Fig. 22 for the suction side pressure tap. The largest pressure fluctuations occurred independently of the diffuser vane configuration at the impeller blade trailing edge. The number of diffuser vanes and the diffuser vane angle, however, were observed to have a significant influence on the pressure fluctuations at all three impeller blade pressure taps. The increase in vane number from six to twelve at a fixed vane angle of 20 deg resulted in a decrease of the blade pressure fluctuations at all blade pressure taps and for all flow coefficients. The reduction varied, depending upon flow coefficient and pressure tap, between 15 and 70 percent. At the trailing edge and at the pressure side pressure tap, the fluctuations decreased more strongly for the lower flow coefficients, whereas at the suction side pressure tap the fluctuations decreased more strongly for the large flow coefficients. Decreasing the vane angle from 20 deg to 10 deg for a constant number of diffuser vanes \( (\beta^* = 6) \) resulted for the pressure taps on the blade pressure and on the blade suction side in an increase of the pressure fluctuations for the large flow coefficients of up to 75 percent, whereas for low flow coefficients the fluctuations decreased by up to 30 percent. For the trailing edge pressure tap, the magnitude of the pressure fluctuations remained unchanged for large flow coefficients and decreased for low flow coefficients.

**Discussion of the Impeller Blade Pressure Measurements.** The impeller blade pressure fluctuations are assumed to be primarily the result of the potential interaction between the diffuser vanes and the impeller blades (Dring, 1982;
very likely the result of the reduced circulation about a single diffuser vane, and may therefore confirm that the impeller blade pressure fluctuations are primarily the result of the potential flow interaction between impeller blades and diffuser vanes.

Summary and Conclusion

An experimental investigation of unsteady flow in a centrifugal pump with different vaned diffusers was carried out focusing on impeller blade–diffuser vane interaction. Steady and unsteady diffuser vane pressure measurements were made for a two-dimensional test impeller and a vaned diffuser for radial gaps of 5 and 8 percent of the impeller discharge radius.

It was found that:
- The pressure fluctuations were larger on the suction side than on the pressure side.
- The largest vane pressure fluctuations occurred on the vane suction side close to the leading edge. For a large flow coefficient, \( \phi = 0.135 \), and a radial gap of 5 percent, the magnitude of those fluctuations reached \( 95 \) percent of the total pressure rise across the pump for that particular flow coefficient.
- Increasing the radial gap between impeller blades and diffuser vanes from 5 to 8 percent resulted in a significant decrease of the large pressure fluctuations on the front half of the vane suction side.
- The fluctuating lift on the diffuser vane was about twice as large as the steady lift.

Unsteady impeller blade pressure measurements were made for a second two-dimensional test impeller with blade number and blade geometry identical to the two-dimensional impeller used for the diffuser vane pressure measurements, but permitting pressure transducers to be mounted to the impeller. Those measurements were made for the vaned diffuser used for the diffuser vane pressure measurements and a second diffuser of identical side wall geometry but permitting variable diffuser vane geometry to investigate the influence of the vane number and the influence of the vane angle on the impeller blade pressure fluctuations.
- The largest blade pressure fluctuations occurred at the impeller blade trailing edge, independently of the diffuser vane configuration.
- Those fluctuations increased significantly with decreasing flow coefficient, in contrast to the large pressure fluctuations at the diffuser vane suction side, which decreased with decreasing flow coefficient. For a low flow coefficient, \( \phi = 0.06 \), and a radial gap of 5 percent, the magnitude of

(Gallus, 1980). This was qualitatively confirmed by the unsteady impeller blade pressure measurements presented herein.

From the steady vane pressure measurements for Diffuser S, a significant increase in the lift on the diffuser vanes (and hence of the circulation about a diffuser vane) was observed when the flow coefficient was reduced (Fig. 8). Hence, the circulation about a single diffuser vane, sensed by the rotating impeller blades as a periodic fluctuation, was found to increase with decreasing flow coefficient. This may cause the increase of the pressure fluctuations at the blade trailing edge with decreasing flow coefficient observed for the unsteady impeller blade pressure measurements using Impeller Z2 and Diffuser S (Fig. 19).

Increasing the number of diffuser vanes in a vaned diffuser results in a decrease of the loading of a single diffuser vane. Therefore, the circulation about a single diffuser vane, sensed by the rotating impeller blades as a periodic fluctuation, also decreases. Comparing the results of the unsteady impeller blade pressure measurements for Impeller Z2 and Diffuser F (\( \alpha_0 = 12, \beta^* = 20 \) deg) and Impeller Z2 and Diffuser G (\( \alpha_0 = 6, \beta^* = 20 \) deg), it can be seen that the impeller blade pressure fluctuations, at all three pressure taps and for the entire range of flow coefficients investigated, were smaller for the twelve-vaned than for the six-vaned diffuser (Figs. 20–22). This is
those fluctuations reached ≈ 60 percent of the total pressure rise across the pump for that particular flow coefficient.

- Increasing the vane number from six to twelve resulted in a significant decrease of the blade pressure fluctuations at all blade pressure taps (with the exception of low flow coefficients, the total pressure rise across the pump, however, was reduced as a result of the increased vane number).
- Decreasing the vane angle from 20 to 10 deg (for six diffuser vanes) resulted in a decrease of the large pressure fluctuations at the blade trailing edge, and in an increase of the pressure fluctuations at the suction side pressure tap (the total pressure rise across the pump, however, was reduced as a result of the decreased vane angle for all flow coefficients investigated).

In summary, it was found that pressure fluctuations, of the same order of magnitude as the total pressure rise across the pump, can occur on the impeller blades and the diffuser vanes if the radial gap between the impeller blades and the diffuser vanes is small, i.e., of the order of a small percentage of the impeller discharge radius. The large pressure fluctuations at the impeller blade trailing edge may be responsible for the cavitation damage occurring at the trailing edges of the impeller blades of high-speed centrifugal pumps. Furthermore, it was shown that the fluctuating lift on the diffuser vanes can be larger than the steady lift. For high-speed, high-performance pumps with closely spaced blade rows, this result should be considered in the structural design of the vane.

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