Tectonic synthesis of the Olympic Mountains segment of the Cascadia wedge, using two-dimensional thermal and kinematic modeling of thermochronological ages

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Abstract. A fully coupled two-dimensional kinematic and thermal model of a steady state accretionary wedge, constrained by an extensive data set of fission track and (U-Th)/He ages for apatite and zircon, is here used to investigate the development of the Olympic Mountains segment of the Cascadia accretionary wedge. The model has two main free parameters: $\varepsilon_{\text{max}}$, the maximum rate of erosion for a generic erosion function operating at the top of the wedge, and $\alpha$, the distribution of sedimentary accretion into the wedge. The best fit values for $\varepsilon_{\text{max}}$ and $\alpha$ and their confidence limits are determined through an iterative search of parameter space. This study represents the first time that such inversion methods have been used to quantify the thermal-kinematic evolution of an accretionary wedge. Our results suggest that horizontal transport plays an important role in the exhumation trajectories experienced by material passing through the Cascadia wedge. At a 95% confidence interval, 80 to 100% of the sedimentary sequence from the subducting Juan de Fuca Plate has been accreted at the front of the wedge offshore of the Olympics over the past 14 m.y. This frontally accreted material must then traverse the entire width of the wedge prior to its eventual exposure in the Olympic forearc high. Assessed in this two-dimensional framework, the fission track and (U-Th)/He age data sets from the Olympic Mountains are all best fit by $\varepsilon_{\text{max}}$ of 0.9-1.0 mm yr$^{-1}$, despite variation in the timescales relevant to the three chronometers. This result supports the hypothesis that the Olympic Mountains segment of the Cascadia accretionary wedge has been in a flux steady-state since $\sim$14 Ma. The demonstration of a flux balance across the Cascadia margin also suggests that margin-parallel transport has not had a significant role in driving uplift of the Olympic Mountains.

1. Introduction

The Olympic Mountains in northwest Washington are the topographically highest and most deeply exhumed segment of the coastal mountain range extending along the Cascadia margin from the Klamath Mountains of northern California to the Insular Range of Vancouver Island (Plate 1). This high separates a relatively continuous forearc depression to the east (Willamette, Puget, and Georgia lowlands) from the accretionary wedge to the west. Dickinson and Seely [1979] refer to this arrangement as a ridged forearc and note that it is typical of mature continental convergent margins and ancient subduction complexes around the world.

Brandon and Vance [1992] and Brandon et al. [1998] use zircon and apatite fission track data from the Olympic subduction complex to investigate the late Cenozoic evolution of the Olympic Mountains. Fission track ages record the length of time that radiation damage caused by the spontaneous fission of $^{238}$U has been accumulating in the dated mineral [e.g., Price and Walker, 1962, 1963; Fleischer and Price, 1964; Price et al., 1964]. In deeply eroded regions, this retention is generally linked to cooling of the sample during progressive exhumation, and thus fission track (and other isotopic) ages provide a measure of rates of material exhumation [e.g., Sardarov, 1957; Hurley et al., 1962; Clark and Jager, 1969; Doherty and Lyons, 1980].

Brandon et al. [1998] derive broad patterns of exhumation across the Olympic Mountains and conclude that for the past 14 m.y. the Cascadia wedge has been in a flux steady state, defined as a balance between the accretionary flux of material into the wedge and the flux of material removed by erosion of the forearc high. However, the significance of their analysis, which accounted only for vertical transport of material through the wedge, is questionable because both the thermal structure of the
Plate 1. Key geographical features of the Cascadia margin. Indicated plate velocity (arrow) is for motion of the Juan de Fuca Plate relative to continental North America at the latitude of the Olympic Peninsula [DeMets et al., 1990; DeMets and Dixon, 1999].
Cascadia wedge [Lewis et al., 1988; Hyndman and Wang, 1993] and the uplift and exhumation rates experienced in the Olympic Mountains [Brandon et al., 1998, Pazzaglia and Brandon, 2001] vary across the margin. The overall material path of a rock through the Cascadia wedge and the thermal consequences of that path may thus be strongly influenced by any horizontal component of motion.

We build on the work of Brandon et al. [1998] by analyzing the tectonic significance of thermochronological data from the Olympic Mountains using a two-dimensional kinematic and thermal framework. The thermal evolution of the deforming wedge is modeled using a Lagrangian-Eulerian finite element method, which enables us to track the passage of selected material points through the model domain and to integrate their thermal histories. This modeling allows us to interpret thermochronological data in a context more consistent with the actual tectonic setting of the Cascadia wedge.

This approach is used to investigate two issues. First, what is the primary deformation mode driving uplift in the Olympics? The three options are (1) frontal accretion of the incoming sedimentary section of the Juan de Fuca Plate at the toe of the Cascadia wedge [e.g., Davis and Hyndman, 1989], (2) underplating of subducted material at depth beneath the orogen [e.g., Clowes et al., 1987; Brandon and Calderwood, 1990], and (3) margin-parallel deformation [e.g., Beck, 1991; Mccaffrey and Goldfinger, 1995; McCaffrey, 1996; McCrory, 1996; Wang, 1996]. The second issue concerns the long-term evolution of the Cascadia margin. More specifically, has the Olympic segment been in a flux steady state during the Late Cenozoic [Brandon et al., 1998]?

The model allows the thermochronological data to be used as a direct test of the steady state hypothesis.

2. Regional Setting

The continental framework inboard of the Cascadia forearc (Figure 1) was assembled in the late Cretaceous. The forearc region itself was subsequently built by the accretion of the Coast Range terrane and the more outboard Cascadia wedge. The Coast Range terrane (CRT) consists of a thick fault-bounded slab of lower Eocene oceanic crust and overlying marine clastic sediments informally known as the Peripheral sequence. This assemblage extends 750 km from southwest Oregon to the continental shelf west of Vancouver Island [Wells et al., 1984; Clowes et al., 1987] (Plate 1 and Figure 1). The origin of the ophiolitic basement of the CRT is ambiguous and may relate to collision of an intra-Pacific seamount province or to either back arc or forearc rifting at the North American margin [Wells et al., 1984; Clowes et al., 1987; Babcock et al., 1992]. The suture separating the basaltic CRT on its inboard side from the uplifted pre-Tertiary continental framework of North America is exposed only on southermmost Vancouver Island, where it is known as the Leech River Fault (Figure 1). Crosscutting relations broadly delimit suturing along this boundary to between 42 and 24 Ma [Brandon and Vance, 1992]. Conglomerates shed southwestward from pre-Tertiary rocks north of the Leech River Fault on Vancouver Island indicate that the fault may have been active during the late Eocene. These conglomerates are exposed in the Lyre Formation within the Peripheral sequence on the north side of the Olympic Peninsula, and detrital zircon fission track ages reported by Garver and Brandon [1994] suggest that they have a depositional age of circa 38 Ma.

The modern configuration of the Cascadia margin, with hot young sediment-mantled oceanic lithosphere of the Juan de Fuca Plate being subducted west of the CRT, was considered by Brandon and Vance [1992] to have originated in latest Eocene time (circa 35 Ma). A late Eocene initiation is suggested by suturing of the CRT to the continental framework of North America between 42 and 24 Ma, as discussed above, initiation of the Cascade Volcanic Arc at circa 36 Ma [Armstrong and Ward, 1991; Brandon and Vance, 1992], and the timing of slip on the Hurricane Ridge Fault in the Olympic Mountains [Brandon and Vance, 1992]. This interpretation contrasts with previous syntheses of the region that infer initiation of Cascadia subduction at circa 50 Ma [e.g., Wells et al., 1984; Heller et al., 1987; Snavely, 1987]. Plate reconstructions [Engebretson et al., 1985; Lonasdale, 1988; Wilson, 1988] and the volcanic record of the Cascade arc [Smith, 1989; Sherrod and Smith, 1989] suggest that after initiation of the Cascadia subduction zone, plate convergence proceeded in a fairly steady and continuous fashion.

The Cascadia wedge formed outboard of the CRT and has grown by offscraping at the front of the wedge, and possibly underplating beneath the wedge as well [Clowes et al., 1987; Brandon and Calderwood, 1990]. Cascadia wedge sediments underlie most of the offshore continental margin [e.g., Clowes et al., 1987] but are only subaerially exposed in the Olympic Mountains. There, uplift and erosion have tilted the Peripheral sequence into a steep east plunging anticline (Figure 1), exposing the Cascadia wedge sediments underlying the Hurricane Ridge Fault in the interior of the massif [Stewart, 1970; Rau, 1973; Tabor and Cady, 1978a, 1978b] where they are known as the Olympic subduction complex (OSC) [Brandon and Vance, 1992] (Figure 1).

The anomalous uplift (Plate 1) and deep exhumation (Figure 1) of the Olympic Mountains are attributed by Brandon and Calderwood [1990] to the presence of a 10-km-high arch in the underlying Juan de Fuca Plate beneath the orogen. They argue that the low angle of slab dip beneath the Olympics resulted in a correspondingly early emergence of the region and rapid uplift of the Olympic massif, relative to adjacent regions of the subduction zone (see Pazzaglia and Brandon [2001] for further discussion of this interpretation). This effect may be further accentuated by the progressive northward increase in sediment flux rate along the Cascadia margin [e.g., Brandon et al., 1998] feeding the growth and deformation of the accretionary wedge.

As an alternative, regional scale plate motion and GPS data have been used to attribute the anomalous uplift of the Olympics to margin parallel motion, with the Olympic Peninsula supposedly caught between the northward moving Oregon Coast Range block and the relatively stable “buttress” of Vancouver Island and uplifted rapidly as a result [e.g., Wells et al., 1984; McCaffrey and Goldfinger, 1995; McCaffrey, 1996; McCrory, 1996; Wang, 1996]. Pazzaglia and Brandon [2001] refute major margin-parallel deformation by using deformed erosional benchmarks to estimate long-term permanent strain rates across the Olympics. Pazzaglia and Brandon [2001] argue that long-term permanent shortening is mainly occurring across the orogen, parallel to the Juan de Fuca-North America convergence direction at a rate of 3 km Myr$^{-1}$ over a 140 km baseline. At the core of this argument is the observation that rates of rock uplift and erosion across the Olympic Mountains appear to be in close agreement with the accretionary flux associated with convergence. Orogen-parallel shortening would increase.
accretionary flux above this level, which runs against other evidence that the Olympic Mountains segment of the Cascadia wedge has maintained a steady-state size for the last 14 Myr [Brandon et al., 1998; Pazzaglia and Brandon, 2001]. Our modeling here provides a test of the steady-state hypothesis, and thus a bearing on this debate over the relative importance of orogen-parallel versus orogen-normal shortening in the Olympics.

3. Modeling

We aim to resolve two questions here: (1) What is the basic accretionary mode of the Olympics? (2) Has the distribution of erosion rates across the orogen varied on the million-year timescale constrained by the available thermochronological data? We begin below by describing an approach for modeling the coupled physical and thermal evolution of an eroding accretionary wedge. This coupling of physical and thermal behavior allows us to use thermochronology as a direct constraint on orogenic development. The model calculates ages by taking selected material points at the surface at the nominal "present-day" and back tracking their passage to their points of entry into the wedge. Exhumational and thermal histories are then compiled using points along the calculated material paths and compared to the thermal response of different thermochronometers (the zircon fission track, apatite fission track, and apatite (U-Th)/He dating
Table 1. Model Parameters

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
<th>Reference</th>
</tr>
</thead>
<tbody>
<tr>
<td>Time step length (\Delta t), kyr</td>
<td>36</td>
<td></td>
</tr>
<tr>
<td>Crustal thermal conductivity (k_c), W m(^{-1})K(^{-1})</td>
<td>2.0</td>
<td>Brandon and Vance [1992]</td>
</tr>
<tr>
<td>Mantle thermal conductivity (k_m), W m(^{-1})K(^{-1})</td>
<td>2.9</td>
<td>Hyndman and Wang [1993]</td>
</tr>
<tr>
<td>Crustal heat capacity (C_p), J kg(^{-1})K(^{-1})</td>
<td>1200</td>
<td>Dumitru [1991]</td>
</tr>
<tr>
<td>Heat production (H), (\mu W m^{-3})</td>
<td>0.6</td>
<td>Lewis et al. [1988]</td>
</tr>
<tr>
<td>Mantle density (\rho_m), kg m(^{-3})</td>
<td>3700</td>
<td></td>
</tr>
<tr>
<td>Crustal density (\rho_c), kg m(^{-3})</td>
<td>2900</td>
<td></td>
</tr>
</tbody>
</table>

Since systems (e.g., Morin and Lister, 1987; Lewis et al., 1988; Hyndman and Wang, 1993), we assume that heat flow occurs primarily by conduction, with advection of heat by moving fluids playing a negligible role. This simplification is probably appropriate, as we are interested primarily in the rear of the wedge, well removed from any influence that rapid dewatering during accretion might have on the thermal structure of the wedge [Davis et al., 1990; Hyndman et al., 1993; Wang et al., 1993]. In the absence of fluid transport, the time-dependent temperature field in a deforming medium, such as the active accretionary wedge, is described by [Carslaw and Jaeger, 1959]

\[
\frac{\partial T}{\partial t} + \mathbf{u} \cdot \nabla T = \kappa \nabla^2 T + \frac{H}{C},
\]

where \(\mathbf{u}\) is material velocity, \(T\) is temperature, \(t\) is time, \(\kappa\) is the thermal diffusivity of the medium, \(C\) is the heat capacity of the medium, and \(H\) is the internal heat production per unit volume (Table 1).

Thermal conductivity for the Olympic subduction complex is estimated to be 2.0 W m\(^{-1}\)K\(^{-1}\) [Brandon and Vance, 1992]. This value is derived as a weighted harmonic mean of compiled thermal conductivity data from Oxburgh [1980] and Oxburgh and Wilson [1989], assuming an average vertical section through the wedge consisting of 50% Coast Range basalt and 25% sandstone and 25% mudstone in the underlying OSC. Internal heat production is taken as 0.6 \(\mu W m^{-3}\) of solid rock, as measured in shelf sediments from offshore wells on the Vancouver Island Margin [Lewis et al., 1988]. The underlying slab of oceanic crust is assumed to have a negligible heat production because of low concentration of radioactive isotopes.

Although frictional heating can also be included as a...
contribution to $H$ in this calculation (Equation 1), this parameter is set to zero in the final models presented below. In their analysis, Hyndman and Wang [1993] concluded that surface heat flow data did not support friction as a significant heat source for the Cascadia wedge. Our modeling similarly suggests that frictional heating must be very low in order to account for the observed thermochronological data of the Olympics. Low frictional heating is further supported by the multichannel seismic observations of Fisher et al. [1999] offshore of Washington State and other regional observations [e.g., Hyndman and Wang, 1995; MacKay, 1995; Wang et al., 1995], which suggest only weak coupling at the basal décollement.

In the model, the wedge surface is maintained at a fixed temperature (Figure 2a). Onshore, the mean annual surface temperature of the Olympics of 8°C is [Brandon and Vance, 1992], while offshore, oceanographic and ocean bottom thermal probe measurements suggest surface temperature decreases progressively seaward, reaching −0°C at the deformation front of the accretionary wedge [Davis et al., 1990]. The left and right boundaries of the wedge are assumed to have no net heat-flux across them.

The basal boundary temperature of the wedge is set according to the method of Molnar and England [1995], which provides an analytical approximation for temperature at the base of an accretionary wedge as a function of the rate and geometry of slab subduction, and the age of the slab. Because of the young age of the Juan de Fuca Plate, which is only 8 Ma at the Cascadia subduction zone offshore of the Olympics [Moran and Lister, 1987], the contribution of heat from the downgoing oceanic slab is considerable. Surface heat flux levels at the Cascadia subduction zone approach 70 mW m$^{-2}$, with temperatures at the top of the basaltic oceanic crust beneath the accumulated sedimentary blanket estimated to be as high as 200°C [e.g., Yorath et al., 1985; Lewis et al., 1988].

Internal motions within the wedge play an important role in the cooling history of a sample [Jamieson et al., 1996; Batt and Braun, 1997]. To interpret the significance of isotopic ages, we must consider both the thermal structure of the wedge and the path taken by the sample during its passage through that thermal structure. We use a simple kinematic model from Pazzaglia and Brandon [2001] to represent the key features of the velocity field in the wedge.

Our null hypothesis is that the wedge is in a flux steady state throughout the model run time (Figure 3). The entire sedimentary section of the subducting Juan de Fuca Plate is assumed to be incorporated into the Cascadia wedge, either by accretion at the toe or underplating beneath the deforming wedge (Figures 2b and 3). This displacement field is assumed to be two-dimensional (plane strain) and oriented parallel to the Juan de Fuca-North America convergence direction. Motion of material perpendicular to this section is not explicitly included in the model but is addressed instead in terms of its additional contribution to the material budget of the deforming wedge, as any such orogen parallel deformation would prevent balance being attained between accretionary influx and erosional outflux in our models.

The compaction of sediment is assumed to occur instantaneously during the initial stage of subduction, so that matrix within the wedge is effectively incompressible [e.g., Dahlen and Suppe, 1988]. We consider two competing mechanisms for the accretion of sedimentary material into the wedge. The first is underplating, where sediments are carried beneath the wedge together with the underthrust oceanic plate and then decoupled from the subducting slab and incorporated into the wedge at depth beneath the orogen. The second alternative is frontal accretion, where material is scraped off the oceanic crust at the point of subduction and incorporated into the toe of the wedge. The underplating and frontal accretion solutions provide end-members of behavior where vertical or horizontal velocities, respectively, are maximized. It is important to consider this range of velocity fields because of the highly two-dimensional (2-D) (and perhaps three-dimensional) setting of the Cascadia wedge. At the latitude of the Olympics the Juan de Fuca Plate is converging with stable North America at a rate of 36 mm yr$^{-1}$ oriented at 054°, nearly orthogonal to the modern subduction zone (option 2 for Juan de Fuca/Pacific of DeMets et al. [1990], and "NA-PA combined" of DeMets and Dixon [1999] (Plate 1).

The frontally accreted influx of material at the toe of the wedge is given by

$$\Omega_f = \alpha (1 - \bar{\eta}) h_0 V_c,$$

where $h_0$ and $\bar{\eta}$ are the thickness (2 km [after Kulm et al., 1984]) and average porosity (27% [from Yuan et al., 1994]) of the incoming sedimentary section, respectively, $V_c$ is the orthogonal convergence velocity (36 mm yr$^{-1}$, as discussed above), and $\alpha$ is the fraction of the sedimentary section accreted at the toe of the wedge.

The remainder of the sedimentary material is assumed to be underplated. In the absence of lateral motion, underplating would be expected to lead to the compensatory uplift of the overlying column of rock. Adopting this kinematic simplification, we distribute the underplating flux in direct proportion to the surface uplift velocity across the Olympics. This construction is useful because it is similar to the 1-D thermal analysis used by Brandon.

![Figure 3](image-url)

**Figure 3.** Figurative cross section illustrating the accretionary wedge behavior assumed in the model.
the surface $w(x,0)$ is everywhere equal and opposite to the erosion. The flux steady-state condition specifies that vertical velocity at rate $3\{x\}$. The transition to the stable North American plate at the rear of the wedge occurs where a balance is attained between deformation front. The vertical velocity $w$ can then be obtained from the continuity equation $\partial w/\partial z = 0$, such that we can differentiate (4) to obtain

$$w(x,z) = w(x,0) - \frac{z \left( \frac{1}{h(x)} \right) \tan \theta}{h(x)^2} \int \epsilon(x) dx.$$

The flux steady-state condition specifies that vertical velocity at the surface $w(x,0)$ is everywhere equal and opposite to the erosion rate $\epsilon(x)$. The transition to the stable North American plate at the rear of the wedge occurs where a balance is attained between accretionary and erosional fluxes, such that $w$ and $w$ equal zero.

The model assumes a rock uplift and erosion function of the form defined for recent Olympic Mountains uplift by Pazzaglia and Brandon [2001], but with its amplitude as a free parameter. The Pazzaglia and Brandon [2001] uplift function is mainly derived from fluvial incision rates over the last 140 kyr in the western Olympics, together with evidence that the east and west coasts of the Peninsula have seen little long-term Neogene uplift and erosion. Pazzaglia and Brandon [2001] also showed that the pattern in the western Olympics was similar to that indicated by long-term (3-7 Ma) exhumation rates derived from apatite fission track ages. If it holds true across the entire peninsula, this correspondence allows estimation of the rates of uplift and erosion across almost the entire Olympic orogen.

Calculated erosion rates rise rapidly from zero at the west coast of the Olympic Peninsula, reach a peak in the west of the Olympic Mountains, and then decrease progressively to the east (Figure 2b). This asymmetric form may be a result of orographic rainfall focussed on the western, seaward side of the peninsula [Pazzaglia and Brandon, 2001]. Our modeling here will allow us to test more closely how the thermochronological data fit the short-term geomorphic indicators of uplift presented by Pazzaglia and Brandon [2001].

As noted previously, the first step in calculating model isotopic ages is to select material points at the surface of the model at the nominal present day and to track their path back to their entry into the wedge. The exhumational and thermal histories of these points are then compiled using model results from different time steps corresponding to the calculated material paths.

Apatite fission track ages are predicted by modeling the annealing of fission tracks as a function of time and temperature. This model is based on the experimentally derived annealing response of fission tracks in fluorapatite, as evaluated by Willett [1997]. The results of Willett's model closely match those of other popular annealing models [e.g., Duddy et al., 1988; Crowley, 1993].

The thermal history of each selected point is divided into a number of time steps $m$, each of length $\Delta t$. At each time step, a new set of tracks are assumed to form according to the $^{238}\text{U}$ decay rate. The apatite fission track annealing response [Willett, 1997] is then integrated over the remainder of the modeled thermal history, thereby giving the predicted track length distribution. The final fission track age of the sample is calculated as a sum of the relative contributions of the tracks created at each time step, weighted for track length and observational bias [Laslett et al., 1987; Green, 1988; Willett, 1997].

This method is not applied to zircon fission track ages here because of the lack of an accepted track length model for the annealing of fission tracks in zircon over geological timescales. Laboratory annealing studies [e.g., Tagami et al., 1990; Yamada et al., 1993] suggest a closure temperature for the zircon fission track system some 50 to 100°C higher than that derived from studies of the geological record [e.g., Zann and Wagner, 1985; Brandon and Vance, 1992; Foster et al., 1996]. Following Kassuya and Naeser [1988], Brandon and Vance [1992] and Brandon et al. [1998] argue that this discrepancy is due to the influence of accumulated $\alpha$ damage (lattice damage due to the decay of $\text{U}$ and $\text{Th}$ by $\alpha$ particle emission) on the thermal stability of fission tracks in zircon.

In light of this issue, we instead utilize effective closure temperatures, calculated from the relationship [Dodson, 1979]

$$\tilde{T} = \frac{-RT_t^2}{E \beta e^{E/RT_t}},$$

where $R$ is the gas constant, $E$ is the "average" activation energy

$$E = 49.77 \text{ kcal mol}^{-1},$$

and for $\beta = 3.160 \times 10^{22}$ Myr.

**Figure 4.** Variation of zircon fission track closure temperature with cooling rate. Derived from (6) assuming $E = 49.77$ kcal mol$^{-1}$, and for $\beta = 3.160 \times 10^{22}$ Myr.
(as evaluated at 50% annealing), $B$ is a materially dependent proportionality constant, and $T$ and $T_c$ are the cooling rate and effective closure temperature, respectively. Brandon and Vance [1992] and Brandon et al. [1998] estimate the constants in (6) from the annealing data of Zaw and Wagner [1985] and Tagarni et al. [1990], arriving at values of 49.77 kcal mol$^{-1}$ for $E$ and 3.160 x $10^{-22}$ Myr for $B$. These values yield the relationship shown in Figure 4. Zircon fission track ages in the model are calculated by determining the time at which temperature falls below $T_c$ for the relevant cooling rate $T$. This calculation requires iterative solution of (6) because the equation cannot be recast to give an analytical solution for time. The effective closure temperatures predicted by this model (Figure 4) are consistent with the study of Foster et al. [1996], which used time-temperature histories determined by $^{40}$Ar-$^{39}$Ar analysis of potassium feldspar to estimate closure temperatures for associated zircon fission track ages as a function of cooling rate.

Apatite (U-Th)/He ages are calculated directly by modeling the production and diffusion of helium in apatite as a function of time and temperature, after the approach described by Wolf et al. [1996]. Assuming uniform distribution of uranium and thorium within the sample, the change in $^4$He concentration over a time step is given by numerically solving for the balance of diffusion and production of $^4$He over the duration of the step $t$, as a function of radial position $r$ within a spherical diffusion domain of radius $a$. The governing equation is

$$\frac{dC}{dt} = \frac{D(t)}{a^2} \left[ \frac{\partial^2 C}{\partial r^2} + \frac{2}{r} \frac{\partial C}{\partial r} \right] + \int_0^t f(r,t) \, dt, \quad (7)$$

where $a$ is the characteristic diffusion dimension of the system, $C$ is the concentration of $^4$He, and $f(r,t)$ is the production rate of $^4$He. $D(t)$ is the temperature-dependent diffusion coefficient given by

$$D(t) = D_0 \, e^{-E/RT(t)}, \quad (8)$$

where $D_0$ is the diffusion coefficient at infinite temperature, $R$ is the gas constant, $T(t)$ is the absolute temperature of the sample at time $t$, and $E$ is the activation energy of the system. Following the experimental work of Farley [2000] on Durango apatite, we adopt helium diffusion characteristics of $E = 33\pm0.5$ kcal mol$^{-1}$ and $\log(D_0) = 1.5\pm0.6$ cm$^2$ s$^{-1}$ for apatite. The characteristic diffusion dimension $a$ is believed to be the radius of the apatite grain [Farley, 2000]. For our model, this is taken to be 50 $\mu$m, approximately corresponding to the average radius of the grains analyzed in this study (Table 2).

4. Thermal and Thermochronological Data

The Olympic Peninsula is covered by a dense set of zircon and apatite fission-track ages from Brandon and Vance [1992] and Brandon et al. [1998] (Figures 1 and 5). Fission track samples are characterized as either reset or unreset. Unreset samples generally display discordant grain ages older than the deposition age of the sediments, reflecting the heterogeneous cooling histories of their sedimentary provenance regions. As these ages are inherited by the detrital material, they offer no direct constraint on the recent thermal history of the region. Samples are considered to be reset when (1) the observed age falls below the deposition age of the sample and (2) the wide age variation typical of an unreset sample is replaced by a narrow range of grain ages [Brandon and...
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Figure 5. Thermochronological data used to constrain the model, plotted as apparent age versus distance along section A-A' (Figure 1). Error bars indicate 1σ uncertainty for age and an assumed ±2 km variability in relative position to account for the projection of geographically distributed points onto a single section line. Unreset ages are identified by the population characteristics of individual samples (as discussed in the text) and are marked as individual ages along the top boundary. These reset ages are inherited from their sedimentary source and are not reflective of the recent deformation and exhumation of the Olympic subduction complex. Zircon fission track ages come from Brandon and Vance [1992] and Garver and Brandon [1994], apatite fission track ages from Brandon et al. [1998], and (U-Th)/He ages are presented in this study in Table 2.

Brandon et al. [1998] delineate a discrete zone of reset zircon fission track ages exposed in the center of the Olympic Mountains (Figure 5). The metamorphic grade and degree of ductile deformation support the conclusion that this region is the most deeply exhumed part of the Olympics [e.g., Tabor and Cady, 1978a; 1978b; Brandon et al., 1998]. For our analyses here, we group together ages along a transect parallel to the direction of plate convergence across the Olympic Peninsula, centered on this reset zircon zone and wide enough to encompass it (see area outlined around section line A-A' in Figure 1). This grouping includes a total of 50 apatite fission track samples covering a total of 100 km of the ~120 km width of the Olympic Peninsula at this point, and 13 zircon fission track samples covering 75 km of the peninsula (Fig. 6). Sample density along this transect is sufficient to constrain the boundaries between unreset and reset apatite fission track ages to within ±2 km (Figure 5). For zircon fission track ages the eastern boundary of the reset zone is similarly well constrained to ~2 km, while less dense sample coverage limits resolution of the western boundary of the reset zone to ~4 km (Figure 5).

Apatite and zircon fission track ages display the same broad patterns of variation across the Olympics. For both chronometers, ages are reset and youngest (5-6 Ma for apatite, 13 Ma for zircon) in the more deeply exhumed interior of the orogen, increase markedly toward both east and west, and undergo a transition to unreset ages toward the boundaries of the Olympic Peninsula (Figure 5). Notably, the age minima of the zircon and apatite fission track chronometers are offset from one another by some 20 km (Figure 5).

Eleven new apatite (U-Th)/He ages from the Olympic subduction complex (OSC) are presented here (Figure 5 and
Table 2), spanning a geographic range of 60 km, or half the width of the Olympic Peninsula (Figure 5). These samples comprise partially volcanigenic graywackes, with mixed apatite morphologies ranging from euhedral and prismatic to rounded and abraded. The most euhedral grains possible were picked from each sample and were analyzed using the techniques outlined by House et al. [1997]. The reported errors represent the estimated analytical precision of the analyses to one standard deviation [Wolf et al., 1996]. Analysis AR-13(a) is rejected from analysis as both anomalously old and unreproducible, possibly due to the presence of small undetected inclusions of other U- and Th-bearing phases in the apatite sample. All other replicated analyses agree to within estimated uncertainties on sample age (Table 2).

Eight samples from the central core of the Olympic Mountains (Figures 1 and 5) display relatively consistent ages of 2 to 3 Ma, and although not sampled to define a specific topographic profile, their ages are broadly correlated with elevation (Table 2). When the more peripheral samples from the Clearwater River are included, a general increase in age can be observed from the core of the orogen toward its western margin, as observed in the higher-temperature fission track systems (Figure 5).

5. Model Results

The model provides three general observables that vary with the interaction of the kinematic and thermal conditions of the wedge. The most important of these are the synthetic age profiles developed for each of the three modeled chronometers (apatite and zircon fission track ages and apatite (U-Th)/He ages). Where the exhumation path leading to a surface point is such that material cooled through the relevant closure temperature during the model run, the observed ages are indicators of model kinematics. Such “reset” ages reflect the time between thermochronological closure at depth in the wedge and exposure.
at the surface and hence are functions of the path-averaged exhumation rate. As seen in Figure 6, this gives low ages in the central part of the orogen where erosion rates are high, with ages increasing toward the margins of the wedge as erosion rates fall to zero. The exact distribution of ages depends on α, which controls the horizontal component of the velocity field.

The second observable is the distribution of reset ages along the section. Over time as the total accumulated exhumation increases, the lateral extent of the domain of reset ages expands to include areas of lower mean erosion rate. If material at a given point is being exhumed from deeper in the wedge than the relevant closure temperature, a reset age will eventually be exposed at that location by progressive exhumation. If exhumation paths leading to a point are so shallow that they do not sample below the relevant closure temperature, then reset ages will never be observed at that point. The expansion limit of the reset area thus depends, ultimately, not on exhumation rate but on the material paths within the wedge. Because of the varying temperatures and depths relevant for different chronometers, this limiting state develops on different timescales for various thermochronological systems.

The third observable is the residence time of material in the wedge. Brandon and Vance [1992] argue that for the Cascadia region the presence of a contemporaneous volcanic source (the Cascade arch) ensures that the minimum zircon fission track age of an unreset sample closely approximates its depositional age. For the trench-basin turbidites of the Olympic subduction complex, with the rapid subduction of the Juan de Fuca Plate offshore of the Olympics (36 mm yr⁻¹), this depositional age can reasonably be equated with the timing of subduction and accretion of sediments into the wedge system [Brandon and Vance, 1992]. Unreset minimum ages can thus be used as a proxy for residence time in the wedge, which range from 39 Ma in the east of the OSC to as low as 15 Ma at the west coast of the Olympic Peninsula [Brandon and Vance, 1992; Brandon et al., 1998] (Figure 5).

The relative veracity of our models is judged on fit of these observables to measured thermochronological data across the Olympic Mountains (Figure 6). We use the reduced chi square statistic, \( \chi^2 \), [Press et al., 1988]

\[
\chi^2 = \frac{1}{N-2} \sum_{i} \left( \frac{e_{o,i} - e_{m,i}}{e_{o,i}} \right)^2,
\]

where \( e_{o,i} \) and \( e_{m,i} \) are the observed and predicted model ages respectively, and \( e_{o} \) is the standard error. The fit is summarized for each of the datasets of Zc (apatite fission tracks, zircon fission tracks, and apatite (U-Th)/He ages) by calculating the \( \chi^2 \) value for the model age distribution. The calculated values of \( \chi^2 \) are normalized by the number of degrees of freedom in each data set (N-2) to allow comparison between the different chronometers, despite the different number of ages for each data set. The best fit model is found by iterating models varying in \( \alpha \) and until \( \chi^2 \) is minimized.

### 5.1. Wedge Kinematics

Mass balance calculations for the Cascadia margin at Vancouver Island [Clowes et al., 1987] suggest that most, if not all, of the sedimentary sequence on the incoming Juan de Fuca Plate is accreted into the wedge. This conclusion appears to hold over the long term as well. To the south of the Olympics in southwest Washington, the compositions of the recent Cascade Volcanics do not provide evidence for subducted sediment in their mantle source [Leeman et al., 1990]. Lack of sediment subduction would require full accretion of the Juan de Fuca sedimentary cover into the Cascadia wedge.

The mechanism by which this sediment is incorporated into the wedge, however, may vary significantly along the margin. To the north, offshore of Vancouver Island, the subduction thrust appears to cut deeply through the incoming sedimentary section, which implies that much or all of that section is being frontally accreted at present [Davis and Hyndman, 1989; Hyndman et al., 1990; Westbrook et al., 1994]. In contrast, along the western edge of the Oregon margin, landward dipping thrusts at the front of the wedge flatten out into a décollement lying approximately in the middle of the incoming sedimentary section at 2 km depth [Cochrane et al., 1994]. The implication is that the remaining sedimentary section is accreted at deeper levels beneath the wedge (Figure 3). Thus, the relative balance of frontal accretion and underplating of sedimentary material at the Olympic margin is an unknown variable that will have important implications for predicted material paths and thermal histories. Sediments accreted at the front of the wedge must pass through the entire wedge before exposure in the eroding forearc high. Such material thus experiences a markedly 2-D history. In contrast, deeply underplated sediments could, in the extreme, have a purely 1-D vertical exhumation history. This problem is investigated here using the parameter \( \alpha \), the relative proportion of the sedimentary section incorporated into the wedge by frontal accretion. The remaining balance of the sedimentary budget (1-\( \alpha \)) is assumed to be deeply underplated beneath the wedge. For the purposes of the scenarios considered here, \( \alpha \) is assumed to be time invariant.

For \( \alpha = 0 \), where the entire sedimentary sequence is carried beneath the Cascadia wedge and underplated at depth, exhumation paths are purely vertical. The underplated material experiences a constant rate of exhumation during its residence in the wedge, corresponding to the erosion rate at the overlying surface point. This velocity field predicts that horizontal gradients in erosion rate are accommodated by related gradients in the vertical shear strain rate. For this end member, calculated reset ages are simply related to the erosion rate function (Figure 2b) by

\[
\tau_m(x) = \frac{z_c}{\varepsilon(x)},
\]

where \( z_c \) is the depth at which isotopic closure occurs for the relevant chronometer. The \( \alpha = 0 \) model notably fails to satisfactorily account for the observed pattern of zircon fission track ages (Figure 6). The predicted ages of the reset zircon fission track samples are approximately correct (circa 12 to 14 Ma), but the predicted position of the reset zircon fission track zone falls 30 km to the west of the observed zone (Figure 6) because the model erosion rates are highest to the west of the zircon reset zone. In contrast, the position and ages of the reset zone in the \( \alpha = 0 \) model are reasonably well fit for both fission track and (U-Th)/He ages in apatite. This result illustrates an important feature of using multiple chronometers. Chronometers with high closure temperatures provide more information about the two-dimensional nature of the exhumation path, whereas the lower \( T_c \) thermochronometers are less sensitive to lateral motion of material but provide better resolution of recent erosion rates and surface processes.
The introduction of frontal accretion into the model affects the predicted distribution of ages in several ways (Figure 6). Toward the inland margin of the wedge, the rear no-flow boundary condition (Fig. 3b) results in particle motions that approach vertical, so there is little difference between age distributions predicted by different $\alpha$ values in that area. As horizontal motion becomes progressively more important toward the front of the wedge, (1) the location of the reset zone boundaries are moved landward by the horizontal motion and (2) material experiences a range of exhumation rates as it is advected through the laterally varying velocity field (Figure 2b). As a result, ages become a function of the average exhumation rate along the material path, rather than being indicative of erosion rates at any particular spatial point. The impact of these effects scales with the closure temperature of the relevant chronometer. Assuming identical kinematic conditions, higher-temperature thermochronometers integrate exhumation rates over a longer period and travel farther horizontally after closure than lower-temperature systems, prior to their eventual exposure at the surface.

Model sensitivity to this variation in accretion pathway is shown by the $x$ axis in Figure 7. Apatite (U-Th)/He ages display only minor response to $\alpha$ variation, due to the relatively low closure temperature for the system ($\sim$65°C), and the correspondingly short time interval over which any horizontal motions are integrated. Apatite fission track ages display somewhat higher sensitivity (Figure 7). Minor improvements in fit are observed for this system with increasing $\alpha$ due to improved fit to ages in the west of the orogen, with model residence times approaching the observed ages in this area (Figure 6). The sensitivity of this data set is limited by the high relative errors of apatite fission track ages from this region (Figure 5), which maintains $\chi_r^2$ at high levels, even for relatively well-fit models.

The influence of $\alpha$ on model fit is strongest for zircon fission track ages. As $\alpha$ increases and lateral migration of material through the wedge becomes more significant, the reset zone for zircon fission track ages is progressively widened and pushed farther eastward (Figure 6), improving model fit to the observed age distribution (Figure 7). At a 95% confidence level, optimal fit to the observed zircon fission track ages requires $\alpha > 0.80$, and favors higher values of $\alpha$, up to 1.0.

5.2. Flux Steady State

On the basis of age-elevation trends and paired cooling ages from the Olympic Mountains, Brandon et al. [1998] suggest that long term erosion rates in the center of the Olympics have remained relatively constant since circa 14 Ma. This consistency indicates that erosion rates apparently reached modern levels within several million years following initial emergence of the forearc high at circa 18 Ma [Brandon et al., 1998]. Because of the influence of material flux balance on the deformation of an accretionary wedge [Barr and Dahlen, 1990], such an erosional steady state would also require a flux steady-state since 14 Ma for the Olympics, where the rate of accretionary influx would balance the erosional outflux from the wedge.
fission tracks. The three thus close at varying depths in the wedge, with their ages integrating exhumational histories after closure over different time spans.

As discussed in section 3, the basic distribution of erosion rates across the Olympics appears to reflect the topography and orographic rainfall patterns of the Olympic Mountains, with erosion highest on the wet ocean-facing western side of the massif [Pazzaglia and Brandon, 2001]. Assuming that this geographic influence has been consistent throughout the history of the orogen, we take the form (but not the amplitude) of the erosion function as a constant, with peak rates in the west of the Olympic Peninsula decreasing to zero at either coast (Figure 2b). We then vary \( \dot{e}_{\text{max}} \) and assess the resulting fit of the model. By minimizing \( \chi^2 \) for each data set in this analysis, we find the best fitting conditions for the orogen on a range of timescales. If the Olympic Mountains have been in a flux steady state since 14 Ma (the oldest reset zircon fission track age from the massif), then the varying timescale of the chronometers should be irrelevant, and all three data sets should be consistent with a single set of erosion rates.

All three thermochronometers display high sensitivity to \( \dot{e}_{\text{max}} \) (Figure 7). At a 95% confidence interval (Figure 8), the optimal fits of the three systems overlap for peak erosion rates of ~0.9-1.0 mm yr\(^{-1}\). The hypothesized flux steady state is thus consistent with the available data. Such a fit is notable in the context of the marked climatic variation and oscillation of glacial and interglacial conditions during the late Cenozoic [e.g., Mathewes et al., 1993; Booth, 1994; Peizhen et al., 2001]. The evidence of consistent erosion rates suggests that at least on the million-year timescale relevant to the chronometers considered here, tectonic uplift, and not climate, is forcing erosion. Such tectonic control would require the limiting factor in the landscape evolution to be
insensitive to climatic conditions. Bedrock landsliding, as an example, may satisfy this requirement. As long as sediment transport rates are sufficient to remove the evolved debris, landform evolution and erosion in an environment controlled by bedrock landsliding are insensitive to further variation in climate and become dominated instead by uplift and the development of steep slopes [e.g., Hovius et al., 1997, 1998]. Note that our age data are insensitive to the shorter timescale effects of climate variation (e.g., the ~100 kyr glacial cycle). Such climatic variations will undoubtedly produce cyclic variations in erosion rates.

Our modeling results provide only an averaged measure of rates on longer timescales and indicate that on average, the erosion rates in the Olympics have remained steady, even with the onset of Quaternary "icehouse" conditions.

The predicted thermal structure and surface heat flow of our best fit model (with an erosion rate of 0.95 mm yr\(^{-1}\), and \(\alpha=1.0\)) are shown in Plate 2. In the submarine portion of the wedge the dominant heat source is the young, hot subducting Juan de Fuca Plate. With the eastward thickening of the accreted Cascadia wedge sediments progressively insulating this heat source, model surface heat flux steadily decreases landward from ~75 mW m\(^{-2}\) at the Cascadia subduction zone to 40 mW m\(^{-2}\) at the west coast of the Olympic Peninsula. Across the Olympic Peninsula, surface heat flow then increases sharply again to ~60 mW m\(^{-2}\) over a distance of 50 km before tapering off to 45 mW m\(^{-2}\) at the east coast (Plate 2). This asymmetric heat flux high is centered over the high topography of the Olympic Mountains and approximately parallels the variation in erosion rate across the orogen (Figure 2b). This correlation is due to advection of heat by exhumation. Heat flow measurements made in exploration wells offshore of Vancouver Island [Lewis et al., 1988] and Oregon [Blackwell et al., 1990] are shown projected into the model section. Despite their relatively high uncertainty (conservatively estimated at ~20% by Lewis et al. [1988]) these data support our assertion that the background thermal structure of the model adequately represents the thermal conditions of the offshore Cascadia wedge (Plate 2). No surface heat flow measurements are available from the exhumed interior of the Olympic Mountains, so that despite its potential as an indicator of kinematics and thermal structure, this variable cannot be used to directly constrain the model.

6. Conclusions

The two-dimensional model described here produces a thermal structure and model distributions for zircon and apatite (U-Th)/He ages comparable to those observed in the Olympic Mountains segment of the Cascadia wedge. The success of the model is assessed with reference to the kinematic context.

Variation in model fit with changing accretional and erosional fluxes indicates that most, and possibly all, of the sedimentary section on the subducting Juan de Fuca Plate is incorporated into the Cascadia wedge seaward of the Olympic Peninsula by frontal accretion at or near the wedge toe. The thermal and exhumational histories experienced by material passing through the wedge are thus sensitive to the convergent component of motion. Material accreted at the front must pass horizontally through a large part of the deforming wedge prior to its eventual exhumation in the forearc high at the rear of the wedge, and accreted materials experience an accompanying range of thermal and erosional conditions during their passage. Two-dimensional models, such as those developed here, are desirable in this setting to place the physical interpretation of thermochronological data in a valid kinematic context.

The variety of isotopic age systems available for the Olympic Mountains provide insight into the evolution of the wedge over a variety of timescales, ranging from Pleistocene (2-3 Ma) for (U-Th)/He ages in apatite to late Miocene (7 Ma) for fission tracks in apatite and to early Miocene (13-14 Ma) for fission tracks in zircon. The earliest of these constraints occurred not long after the initial subaerial exposure of the Olympic Peninsula at circa 18 Ma. Our model results support the hypothesis that the wedge has been in a flux steady state since circa 14 Ma, with the accretionary flux into the wedge balanced by an erosional flux from the subaerial forearc high. This indicates that climatic variation over this interval has not played a significant role in the overall uplift and erosion of the massif. These characteristics must be controlled by tectonic rather than climatic conditions for the Olympic Mountains, at least on the timescales relevant to thermochronologic data. The apparent balance of accretionary and erosional fluxes in our models is consistent with the argument that margin-parallel transport along the Cascadia Margin has not played a significant role in the development of the Olympic Mountains [e.g. Brandon et al., 1998; Pazzaglia and Brandon, 2001].

Acknowledgments. This work was completed while G.B. was funded by a Damon Wells post doctoral fellowship at Yale University. Detailed and thorough reviews of this manuscript by Peter Reiners and Phil Armstrong helped to significantly improve the clarity of our arguments.

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