Global Feed-Forward Vibration Isolation in a km scale Interferometer

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Using a network of seismometers and sets of optimal filters, we implemented a feed-forward control technique to minimize the seismic contribution to multiple interferometric degrees of freedom of the LIGO interferometers. The filters are constructed by using the Levinson-Durbin recursion relation to approximate the optimal Wiener filter. By reducing the RMS of the interferometer feedback signals below \( \sim 10 \) Hz, we have improved the stability and duty cycle of the joint network of gravitational wave detectors. By suppressing the large control forces and mirror motions, we have dramatically reduced the rate of non-Gaussian transients in the gravitational wave signal stream.

I. INTRODUCTION

The Laser Interferometer Gravitational-wave Observatory (LIGO) consists of detectors located in Livingston, Louisiana (LLO) and Hanford, Washington (LHO). The goal of the experiment is to measure minute disturbances in the relative positions of test mass mirrors generated by gravitational waves, using laser interferometry. Passing gravitational waves are expected to produce a quadrupolar strain in the local space-time metric, resulting in a differential phase shift between the laser fields traveling in the two arms of the interferometer. Potential astrophysical sources of gravitational waves include supernovae and compact binary inspirals. The expected strain from such sources requires a detector sensitive to displacements on the order of \( 10^{-19} \text{m} / \sqrt{\text{Hz}} \) over a few km baseline, at frequencies ranging from \( \sim 50 \) Hz to 7 kHz. Figure 1 shows a typical displacement sensitivity for the LIGO interferometers.

Using Fabry-Perot cavities for the interferometer arms as well as power recycling helps improve the detector’s sensitivity. Figure 2 shows a simplified schematic of a LIGO interferometer. The motion of the ground is many orders of magnitude above the required sensitivity, so the mirrors are seismically isolated, using both passive and active techniques. The cavities are held on optical resonance by suppressing external disturbances with a family of length and alignment feedback control loops. Suspending the mirrors as pendulums provides passive vibration isolation above the pendular resonance, which is arranged to be \( \sim 1 \) Hz. The support point of the pendulum is attached to a passive in-vacuum seismic isolation stack, consisting of four mass and spring layers. This payload is attached to tubes which exit the vacuum and are supported by an external active seismic isolation system. Small magnets are glued to the backs of the mirrors to allow for actuation via magnetic fields generated by currents flowing in nearby wire coils. Above \( \sim 50 \) Hz, where ground vibrations have been sufficiently suppressed, the detector is fundamentally limited by thermal noise in the mirrors and seismic isolation systems and by photon shot noise.

There are four length degrees of freedom that need to be controlled. They are defined in terms of differential and common length changes,

\[
L_+ = \frac{L_x + L_y}{2}
\]
\[
L_- = \frac{L_x - L_y}{2}
\]
\[
l_+ = \frac{l_x + l_y}{2}
\]

FIG. 1. Typical displacement sensitivity for the LIGO interferometers. L1 and H1 refer to the detectors at Livingston and Hanford, respectively. The black curve is the initial LIGO design sensitivity, which was not specified below 10 Hz.
The Fabry-Perot arm cavities have lengths $L_x \simeq L_y \approx 4 \text{km}$.

$$l_- = l_x - l_y$$

where $L_x$, $L_y$, $l_x$, and $l_y$ are as shown in Figure 2. An RF modulation scheme is used to generate control signals by relating position and angle fluctuations of the test mass mirrors to power fluctuations measured by photodetectors at various locations around the interferometer. The detector is brought to and held at its operating point using piezoelectric actuators and filters created via system-identification. During commissioning of the detector, using piezoelectric actuators and filters created via system-identification.

At frequencies where the motion of the ground and the length fluctuations in the cavity are coherent the seismic noise can be actively subtracted from the cavity motion using a feed-forward signal. Feed-forward cancellation of the microseism was demonstrated at LLO during the commissioning of the detector, using piezoelectric actuators and filters created via system-identification.
II. METHOD

In order to optimize the noise subtraction we want to find the Wiener filter $h$, that processes the witness seismometer signals, $w$, into the best possible estimate of the targeted cavity length control signal, $t$. We find $h$ by minimizing the mean square error between $t$ and $w$,

$$MSE = \frac{1}{2} \sum_i \left( t_i - \sum_{j=0}^{N} h_j w_{i-j} \right)^2$$

(1)

with respect to $h_j$, where $N$ is the filter order (number of taps). This is done by setting the derivative,

$$\frac{\partial MSE}{\partial h_j} = 0$$

(2)

which yields the Wiener-Hopf equations,

$$p_i = \sum_{j=0}^{N} h_j R_{i-j}$$

(3)

where $R$ is the autocorrelation matrix of the seismometer signal and $p$ is the cross-correlation between the seismometer and the control signals. The FIR Wiener filters were estimated in MATLAB using the Levinson-Durbin algorithm, and then fit to a set of IIR coefficients to reduce the computational time in the real-time control system. The conversion from FIR to IIR was done with the Vectfit software package. The intermediate FIR filters were composed of 1000's of taps and processed data with a sample rate of 64 Hz, allowing for subtraction down to a few 10's of mHz. Approximately 1 hour of data was used to train each filter. Each test mass is in the vicinity of at least one seismometer (see Figure 3), which measures motion in three perpendicular directions, X, Y, and Z, where Z is vertical and the two horizontal directions are roughly aligned to the arms of the interferometer. The length control is coupled most strongly to motion along the axes of the respective cavities, but cross-couplings to the other directions are non-negligible. Regardless of the direction of the witness signal generating a feed-forward correction the actuation is applied in the direction in which the laser beam is propagating for that particular chamber.

Offloading control signals to actuators located in the external seismic isolation systems mitigates several of the problems mentioned in Section I. In order to properly subtract the filtered witness signals, the transfer function from our point of actuation to the cavity control signal must be measured and divided out. A diagram showing the relevant pieces of the mechanical structure can be seen in Figure 4. The number of mechanical components separating the mirrors from the ground creates a complicated transfer function with many resonant features.

At LLO, the active seismic isolation system is HEPI (hydraulic external pre-isolator). A similar system installed at LHO, PEPI, used piezoelectric actuation. HEPI is an Advanced LIGO (aLIGO) system which will be in place at both LLO and LHO in the future. Figure 5
shows a schematic of the HEPI system. The Wiener filter feed-forward path was added in parallel to the existing sensor correction path, which contained hand-tuned filters designed to match HEPI’s position sensors to local seismometers on the ground. Typically this sensor correction reduced the differential motion sensed by the suspended cavities to 1/10th of the ground motion, in the microseismic band. All results shown are improvements on top of this existing isolation. The HEPI actuators provide the ability to move its payload by ±700 μm; the maximum range of PEPI was ±7 μm. We excited these actuators while the detector was locked and monitored the mirror motion to measure the mechanical response. We again used Vectfit to fit these measurements. An example of these transfer function measurements can be seen in Figure 6. An example Wiener filter can be seen in Figure 7. Both the Wiener filter and mechanical response are only fit accurately up to few Hz. Low-pass filtering was applied to the feed-forward signal to prevent noise injection at higher frequencies.

III. RESULTS AND LIMITATIONS

Before the laser beam enters interferometer, higher order spatial modes are removed by a suspended, triangular cavity called the code cleaner (MC). The length of the mode cleaner is controlled such that only the TEM00 mode is resonant. The cavity is ~12 m long, with its mirrors split between isolated tables in two vacuum tanks, MC1 and MC2, as shown in Figure 3. At LLO these chambers are equipped with HEPI and served as the initial testbed for the Wiener filter feed-forward implementation. Figure 8 shows the control signal holding the mode cleaner on resonance with and without the Wiener feed-forward signal path enabled. A factor of up to ~5 improvement was realized around the microseismic peak, and the RMS of the signal was reduced by a factor of ~2. The pre-existing sensor correction filters are left in their nominal state for all results shown in this paper.

Successful implementation of Wiener filter feed-forward on the mode cleaner length control prompted commissioning of feed-forward paths for the other interferometric control signals, starting with the power recycling cavity control at LLO. This work was performed during a time of particularly high microseismic activity which impaired the Livingston detector’s ability to remain in lock. As can be seen in Figure 9(a), a significant reduction in control signal was achieved, with the RMS being reduced by more than a factor of 2. As a result there was also a reduction in the power fluctuations in the recycling cavity, which tended to drive the interferometer control loops towards instability, and greatly improved the instrument’s duty cycle. This cavity is nearly geometrically degenerate (g-factor ~1) and therefore is especially sensitive to misalignments.

Sending feed-forward signals developed to minimize one cavity control signal may inject noise into other length controls, since the cavities share mirrors. To avoid this problem, feed-forward paths were implemented in a serial fashion, such that extra motion injected into other degrees of freedom could be corrected by the Wiener filters constructed for subsequent feed-forward paths. For example, Figure 9(b) shows the effect of filters designed to minimize the short Michelson control signal, calculated on top of the existing power recycling feed-forward path. Above ~0.2 Hz the Michelson signal is reduced, with the improved isolation of the power recycling cavity preserved, albeit with some noise injection above ~1 Hz. Since the overall RMS is still reduced this noise injection was considered an acceptable tradeoff. Global feed-forward for the differential arm length control was implemented at both observatories with similar results. Since the DARM degree of freedom is sensitive

FIG. 5. The external isolation systems measure the motions of their payloads using position sensors and geophones, providing feedback via hydraulic or piezoelectric actuators. Ground motion is also measured with a nearby seismometer, which is digitally processed and subtracted from the position sensor signal, a process called sensor correction. For chambers containing test mass optics this signal is then blended with the geophone signal into a so-called ‘super-sensor’ which has good combined sensitivity over a wider frequency band than either sensor individually. ‘Super-sensor’ signals are fed to the actuators. The presence of conversion matrices indicates a transformation between the different coordinate bases used by particular sensors/actuators. The use of four horizontal and four vertical position sensors/geophones allows for the sensing and control of 8 degrees of freedom: 3 translational, 3 rotational, and 2 over-constrained. This schematic is adapted from Figure 3.8 of Wen.
FIG. 6. Example plant transfer function, fit using Vectfit. The average statistical error of points shown was \(\sim 2.5\%\) in magnitude and \(\sim 1.5^\circ\) in phase.

FIG. 7. Example Wiener filter, corrected for the mechanical plant response, also fit using Vectfit.

to the motions of mirrors in both the end buildings as well as the corner station seismometers in all three locations were incorporated into the calculation of the optimal feed-forward filter. Figures 10 and 11 show that the overall RMS of the control signal is reduced by a factor of \(\sim 2.5\) for each interferometer. For LLO this improvement in performance was balanced by a slight noise increase above 1 Hz. Some noise was also injected by Wiener filter feed-forward at LHO, below 0.1 Hz, and above 3 Hz.

The couplings of ground motion to the feedback signal can potentially be time dependent. Since the approach used here is not adaptive, this could lead to a degradation of the filter’s subtraction efficacy over time. Figure 12 shows the performance of DARM feed-forward at LLO when first implemented and 8 months later. While the overall reduction in RMS motion was originally a factor of \(\sim 2.5\) the same feed-forward filters provided \(\sim 20\%\) less isolation after 8 months, reducing the RMS motion by a factor of 2. There is no obstacle to retraining new Wiener filters to potentially recover subtraction performance, however if there is a change in the mechanical plant remeasuring the transfer function is a time consuming process, due to the high accuracy required.

As mentioned in Section I, we have observed that the rate of non-Gaussian events in the gravitational wave band increases when large forces are required to main-
FIG. 10. Reduction in differential arm length control from Wiener filter feed-forward signals at LLO. The overall RMS of the feedback control was reduced by a factor of almost 3, with some noise injection above 1 Hz.

FIG. 11. Reduction in differential arm length control from Wiener filter feed-forward signals at LHO. The RMS is reduced in a similar fashion to LLO, with some excess noise at a few Hz and below 100 mHz.

FIG. 12. Performance of DARM Wiener filter feed-forward at the time of filter training (upper traces) and 8 months later (lower traces). The two sets of spectra are from times with significantly different seismic input. The lower plot shows the ratio of feed-forward off/on for the two time periods.

FIG. 13. Reduced low frequency control signal in the DARM degree of freedom also results in reduced transient rates at higher frequencies. This histogram shows the number of transient events per second between 40 and 150 Hz in the L1 interferometer, over 30 minute stretches with and without global feed-forward.

Fundamentally the ability to provide feed-forward subtraction is limited by the coherence between the witness signals and the cavity control signal. A drawback particular to the scheme detailed in this paper is the lack of witnesses measuring all signals which contribute to the cavity motion. Since the seismometers cannot distinguish between translation and tilt, additional sensors such as tilt meters could contribute additional isolation through more feed-forward paths. There is the potential to be

tain detector lock. To measure the effect of improved isolation on the rate of background events, two 30 minute segments of data were collected for L1, with the DARM Wiener feed-forward first enabled and then disabled. A templated search, using a sine-Gaussian waveform basis, was performed and the number of triggers per second reported are shown in Figure 13. Only triggers with frequencies between 40 and 150 Hz are included, and the threshold SNR was set to 5. While both distributions show an excess of non-Gaussian events, reducing the low frequency control signal clearly results in a lower rate of signal band transients. The stationary noise floor of the detector did not vary significantly during the time this data was taken.
limited by the noise floors of motion sensors, however at the microseismic peak the signal to noise ratio is very large; see Figure 14. Numerical errors can arise in the calculation of the FIR Wiener filter as well as in the fitting of both the IIR coefficients and the mechanical transfer function. These inaccuracies also have the potential to limit the feed-forward subtraction.

IV. CONCLUSIONS

We have demonstrated the ability to use the LIGO detector’s active seismic isolation system to reduce the relative motion between optics on a 4 km scale through seismometer feed-forward control. By sending the filtered seismometer signals to the HEPI/PEPI actuators we were able to quiet the relative motion of the mirrors, offloading control signal from the test mass actuators to the seismic isolation system. During times of elevated microseismic activity this allowed for unprecedented interferometer stability. The rate of audio band transients is significantly reduced by having less motion and less applied force. This method will be directly applicable to the second generation gravitational-wave detectors.

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