Measurement of the top-quark mass in $t\bar{t}$ events with dilepton final states in pp collisions at $\sqrt{s} = 7$ TeV

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Abstract The top-quark mass is measured in proton-proton collisions at $\sqrt{s} = 7$ TeV using a data sample corresponding to an integrated luminosity of 5.0 fb$^{-1}$ collected by the CMS experiment at the LHC. The measurement is performed in the dilepton decay channel $t\bar{t} \rightarrow (\ell^+\nu_\ell)(\ell^-\nu_\ell\bar{b})$, where $\ell = e, \mu$. Candidate top-quark decays are selected by requiring two leptons, at least two jets, and imbalance in transverse momentum. The mass is reconstructed with an analytical matrix weighting technique using distributions derived from simulated samples. Using a maximum-likelihood fit, the top-quark mass is determined to be $172.5 \pm 0.4$ (stat.) $\pm 1.5$ (syst.) GeV.

1 Introduction

The top-quark mass is an important parameter of the standard model (SM) of particle physics, as it affects predictions of SM observables via radiative corrections. Precise measurements of the top-quark mass are critical inputs to global electroweak fits [1, 2], which provide constraints on the properties of the Higgs boson.

The top quark constitutes an exception in the quark sector as it decays, primarily to a W boson and a b quark, before it can hadronize. Thus, in contrast to all other quarks, the mass of the top quark can be measured directly and is currently known with the smallest relative uncertainty. All measurements of the top-quark mass to date are based on the decay products of top pairs, using final states with zero, one, or two charged leptons. The mass of the top quark has been measured very precisely in $p\bar{p}$ collisions by the Tevatron experiments, and the current world average is $m_t = 173.18 \pm 0.56$ (stat.) $\pm 0.75$ (syst.) GeV [3].

In the dilepton channel, in which each W boson decays into a charged lepton and a neutrino, the top-quark mass has been measured to be $m_t = 170.28 \pm 1.95$ (stat.) $\pm 3.13$ (syst.) GeV by the CDF Collaboration [4] and $m_t = 174.00 \pm 2.36$ (stat.) $\pm 1.44$ (syst.) GeV by the D0 Collaboration [5]. The combination of these two measurements yields a top-quark mass of $m_t = 171.1 \pm 2.1$ GeV [3]. Measurements of $m_t$ in pp collisions at $\sqrt{s} = 7$ TeV were performed at the Large Hadron Collider (LHC) in the dilepton channel by the Compact Muon Solenoid (CMS) Collaboration [6] and in the lepton + jet channel, in which one W boson decays into quarks and the other into a charged lepton and a neutrino, by the ATLAS [7] and CMS [8] Collaborations.

Of all $t\bar{t}$ decay channels, the dilepton channel has the smallest branching fraction and is expected to be the least contaminated by background processes. The dominant background process is Drell–Yan (DY) production. Single top quark production through the $tW$ channel as well as diboson production also mimic the dilepton signature but have much lower cross sections. The production of multijet events has a large cross section at the LHC, but the contamination of the dilepton sample is small as two isolated leptons with high transverse momentum ($p_T$) are very rarely produced. The presence of at least two neutrinos in dilepton $t\bar{t}$ decays gives rise to an experimental $p_T$ imbalance, which allows a further discrimination between background and $t\bar{t}$ events. However, the kinematical system is underconstrained as only the $p_T$ imbalance can be measured.

Here we report an update of the measurement of $m_t$ performed in dileptonic final states, containing electrons or muons, with an analytical matrix weighting technique. An alternative measurement is performed using a full kinematic analysis. The data samples used in this analysis were recorded by the CMS experiment at a centre-of-mass energy of 7 TeV and correspond to a total integrated luminosity of 5.0 $\pm$ 0.1 fb$^{-1}$.
2 The CMS detector

The central feature of the CMS detector is a superconducting solenoid, 13 m in length and 6 m in diameter, which provides an axial magnetic field of 3.8 T. The bore of the solenoid is outfitted with various particle detection systems. Charged particle trajectories are measured by the silicon pixel and strip subdetectors, covering $0 < \phi < 2\pi$ in azimuth and $|\eta| < 2.5$, where the pseudorapidity $\eta$ is defined as $\eta = -\ln[\tan(\theta/2)]$, with $\theta$ being the polar angle of the trajectory of the particle with respect to the anticlockwise-beam direction. A lead tungstate crystal electromagnetic calorimeter (ECAL) and a brass/scintillator sampling hadronic calorimeter (HCAL) surround the tracking volume; in this analysis the calorimetry provides high-resolution energy and direction measurements of electrons and hadronic jets. Muons are measured in drift tubes, cathode strip chambers, and resistive plate chambers embedded in the flux-return yoke of the solenoid. The detector is nearly hermetic, allowing for $p_T$ imbalance measurements in the plane transverse to the beam directions. A two-level trigger system selects the most interesting pp collision events for use in physics analysis. A detailed description of the CMS detector can be found in Ref. [9].

3 Simulation of signal and background events

The simulation of $t\bar{t}$ events is performed using the MADGRAPH [10] event generator (v. 5.1.1.0), where the generated top-quark pairs are accompanied by up to three additional high-$p_T$ jets. The parton configurations generated by MADGRAPH are processed with PYTHIA 6.424 [11] to provide showering of the generated particles. The parton showers are matched using the $k_T$-MLM prescription [12]. The underlying event is described with the Z2 tune [13] and the CTEQ6.6L [14] set of parton distribution functions (PDFs) are used. The TAUOLA package (v. 27.121.5) [15] is used to simulate decays of the $t$ leptons. Events in which the $t$ leptons decay to electrons or muons are taken as part of the signal.

For the reference sample, a top-quark mass of $m_t = 172.5$ GeV is used. Additional samples with masses of 161.5 GeV and between 163.5 and 187.5 GeV in steps of 3 GeV are used. Furthermore, in order to estimate systematic effects in the modelling of dilepton events, simulated signal samples using alternative settings of the parameters are also considered. The following parameters are varied: the QCD factorisation and renormalisation scale (defined as the squared sum of the four-momenta of the primary partons in the event which is transferred dynamically in the hard interaction) and the threshold used for the matching of the partons from matrix elements to the parton showers. The uncertainty on the choice of the $Q^2$ or matching scales are considered by varying the corresponding nominal value by a factor of two, up and down.

Electroweak production of single top quarks is simulated using POWHEG (v. 301) [16]; MADGRAPH is used to simulate $W/Z$ events with up to four jets. Production of $WW$, $WZ$, and $ZZ$ is simulated with PYTHIA.

Signal and background processes used in the analysis of $t\bar{t}$ events are normalised to next-to-leading order (NLO) or next-to-next-to-leading order (NNLO) cross section calculations, where calculations are available. The production cross section of $\sigma_{t\bar{t}} = 164^{+13}_{-10}$ pb computed with HATHOR [17, 18] at approximate NNLO is used. The single top quark associated production ($tW$) cross section is taken to be $\sigma_{tW} = 15.7 \pm 1.2$ pb at NNLO [19]. The inclusive NNLO cross section of the production of $W$ bosons (multiplied by the leptonic branching fraction of the $W$ boson) is estimated to be $\sigma_{W^\pm} = 31.3 \pm 1.6$ nb using FEWZ [20] with a $Q^2$ scale of $(m_W)^2 + \Sigma(p_{T\text{parton}}^2)$, where $m_W = 80.4$ GeV and $p_{T\text{parton}}$ are the transverse momenta of the partons in the event. The DY production cross section at NNLO is calculated using FEWZ to be $\sigma_{Zj^\rightarrow\ell\nu} = 5.00 \pm 0.27$ nb, where $m_\ell$ is the invariant mass of the two leptons. In the computation, the scales are set using the $Z$-boson mass $m_Z = 91.2$ GeV [21]. The normalisation of $WW$, $WZ$, and $ZZ$ production is defined using the inclusive cross sections of $43.0 \pm 1.5$ pb, $18.8 \pm 0.7$ pb, and $7.4 \pm 0.2$ pb respectively (all calculated at NLO with MCFM [22]).

All generated events are passed through the full simulation of the CMS detector based on GEANT4 [23]. We simulate additional soft Monte Carlo events corresponding to a number of collisions distributed as seen in data.

4 Event selection

The $t\bar{t}$ candidate events are required to contain at least two jets, two energetic isolated leptons (electrons or muons), and missing transverse energy ($E_T^{\text{miss}}$) which is defined as the magnitude of the $p_T$ imbalance vector. Events are selected by dilepton triggers in which two muons, two electrons, or one electron and one muon are required to be present. The instantaneous luminosity increased significantly during the data taking period thus the lepton $p_T$ thresholds were increased during the data taking period to keep the trigger rates within the capabilities of the data acquisition system. For the dimuon trigger, the $p_T$ requirements evolved from 7 GeV for each muon to asymmetric requirements of 17 GeV for the highest-$p_T$ (leading) muon and 8 GeV for the second-highest $p_T$ muon. For the dielectron trigger, the requirement was asymmetric with a threshold applied to the energy of an ECAL cluster projected onto
the plane transverse to the nominal beam line ($E_T$). The cluster of the leading electron is required to have $E_T > 17$ GeV and the second-leading electron $E_T > 8$ GeV. For the electron-muon trigger, the thresholds were either $E_T > 17$ GeV for the electron and $p_T > 8$ GeV for the muon, or $E_T > 8$ GeV for the electron and $p_T > 17$ GeV for the muon.

All objects are reconstructed using a particle-flow algorithm [24]. The particle-flow algorithm combines the information from all subdetectors to identify and reconstruct all particles produced in the collision, namely charged hadrons, photons, neutral hadrons, muons, and electrons. Jets are reconstructed by the anti-$k_T$ jet clustering algorithm [25] with a distance parameter $R = 0.5$. Jet energy corrections are applied to all the jets in data and simulation [26]. The $E_T^{\text{miss}}$ vector is calculated using all reconstructed particles.

Events are selected with two isolated, oppositely charged leptons with $p_T > 20$ GeV and $|\eta| < 2.4$, and at least two jets with $p_T > 30$ GeV and $|\eta| < 2.4$. The lepton isolation $I_{\text{rel}}$ is defined as the sum of the transverse momenta of stable charged hadrons, neutral hadrons and photons in a cone of $\Delta R = \sqrt{(\Delta \eta)^2 + (\Delta \phi)^2} = 0.3$ around the lepton track, divided by its transverse momentum. A lepton candidate is not considered as isolated and is rejected if the value of $I_{\text{rel}}$ is $>0.20$ for a muon and $>0.17$ for an electron. The two leptons of highest $p_T$ are chosen for the reconstruction of the top quark candidates. The choice of the jets is different in each analysis and is described later. The reconstructed $E_T^{\text{miss}}$ of events with same-flavour lepton pairs is required to be above 40 GeV to reject DY events. No such selection is applied to $e\mu$ events. The selected leptons and jets are required to originate from the primary pp interaction vertex, identified as the reconstructed vertex with the largest $\sum p_T^2$ of its associated tracks. Events with same-flavour lepton pairs in the dilepton mass window $76 < m_{ll} < 106$ GeV are removed to suppress the dominant DY production background. Dilepton pairs from heavy-flavour resonances as well as low-mass DY production are also removed by requiring a minimum invariant mass of 20 GeV. A highly efficient b-tagging algorithm based on a likelihood method that combines information about impact parameter significance, secondary vertex reconstruction, and jet kinematic properties, into a b-tagging discriminator, is used to classify the jets [27]. We require at least one b-tagged jet in the event.

The observed number of events is consistent with the expected signal and background yields, as shown in Table 1. Simulated events are reweighted to account for differences in trigger, lepton, and b-tagging selection efficiency between data and simulation. The b-tagging efficiency is estimated from a sample of top-quark candidates [28] while the probability of tagging light-quark jets (mistag rate) is estimated from multijet events [27]. The lepton selection efficiency data-to-simulation scale factors are estimated using dileptons inside the Z-boson mass window.

### Table 1
Numbers of observed and expected events in each dilepton channel after all selection requirements have been applied. Event yields correspond to an integrated luminosity of 5.0 fb$^{-1}$. The uncertainties quoted correspond to the limited statistics in simulation. The total uncertainty associated to the estimates from data of the $t\bar{t}$ background and DY production are included as well.

<table>
<thead>
<tr>
<th>Processes</th>
<th>ee</th>
<th>$e\mu$</th>
<th>$\mu\mu$</th>
</tr>
</thead>
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<td>$2359 \pm 71$</td>
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<tr>
<td></td>
<td>$t\bar{t}$ background</td>
<td>$10.6 \pm 0.3$</td>
<td>$101.8 \pm 3.1$</td>
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<td></td>
<td>Single top</td>
<td>$40.7 \pm 1.2$</td>
<td>$172.2 \pm 5.2$</td>
</tr>
<tr>
<td></td>
<td>Drell–Yan</td>
<td>$107 \pm 24$</td>
<td>$241 \pm 27$</td>
</tr>
<tr>
<td></td>
<td>Dibosons</td>
<td>$11.4 \pm 0.3$</td>
<td>$39.7 \pm 1.2$</td>
</tr>
<tr>
<td></td>
<td>Total prediction</td>
<td>$767 \pm 30$</td>
<td>$2914 \pm 76$</td>
</tr>
<tr>
<td></td>
<td>Data</td>
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<td>$2788$</td>
</tr>
<tr>
<td>$\geq 2$b-tagged jets</td>
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<td>$1057 \pm 32$</td>
<td>$4312 \pm 129$</td>
</tr>
<tr>
<td></td>
<td>$t\bar{t}$ background</td>
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<td></td>
<td>Data</td>
<td>$1151$</td>
<td>$4365$</td>
</tr>
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</table>
5 Analytical matrix weighting technique

Since the dilepton channel contains in the final state at least two neutrinos which can not be detected, the reconstruction of $m_t$ from dilepton events involves an underconstrained system. For each $t\bar{t}$ event, the kinematic properties are fully specified by 24 parameters, which are the four-momenta of the six particles in the final state: two charged leptons, two neutrinos and two jets. Out of the 24 free parameters, 14 are inferred from measurements (the three-momenta of the jets and leptons, and the two components of the $E_{T}^{miss}$) and 9 are constrained. Two constraints arise from demanding that the reconstructed W-boson masses be equal to the world-average measured value [21] and one constraint is imposed by assuming the top quark and antiquark masses to be the same [30]. Furthermore, the masses of the 6 final-state particles are taken as the world-average measured values [21]. This leaves one free parameter that must be constrained by using some hypotheses.

Several methods have been developed for measuring the top-quark mass in the dilepton decay channel. We use an improved version of the Matrix Weighting Technique (MWT) [31] that was used in the first measurements in this channel [31, 32]. The algorithm is referred to as the analytical MWT (AMWT) method. A key improvement with respect to the original MWT is the selection of the jets used to reconstruct the top quark candidates. Instead of taking the two leading jets (i.e. the jets with the highest $p_T$), two or more b-tagged jets. For the DY background, the fraction of events affected by this singularity is below 0.1%, and a numerical method is used to determine the solutions in these rare cases [35].

The kinematic equations are solved many times per event using a series of top-quark mass hypotheses between 100 and 400 GeV in 1 GeV steps. Typically, solutions are found for the neutrino momenta that are consistent with all constraints for large intervals of mass hypotheses. In order to determine a preferred mass hypothesis, a weight $w$ is assigned to each solution [36]:

$$w_i = \frac{\sum f(x_1) f(x_2) p(E_{T}^{miss})}{\sum f(x_1) f(x_2) p(E_{T}^{miss})},$$

(1)

where $x_i$ are the Bjorken $x$ values of the initial-state partons, $f(x)$ are the parton distribution functions, and the summation is over the possible leading-order initial-state partons ($u\bar{u}$, $\bar{d}d$, $\bar{d}d$, and $gg$). Each term of the form $p(E_{T}^{miss})$ is the probability density of observing a massless charged lepton of energy $E_{T}$ in the rest frame of the top quark, for a given $m_t$ [36]:

$$p(E_{T}^{miss}) = \frac{4m_t E_{T}^{miss} (m_t^2 - m_b^2 - 2m_t E_{T})}{(m_t^2 - m_b^2)^2 + M_W^2 (m_t^2 - m_b^2 - 2m_t E_{T})^2}.$$  

(2)

Detector resolution effects are accounted for by reconstructing the event 1000 times, each time varying the $p_T$, $\eta$, and $\phi$ of each jet according to the measured detector resolution, and correcting the $E_{T}^{miss}$ accordingly. For each mass hypothesis, the weights $w$ from all solutions are summed. For each event, the top-quark mass hypothesis with the maximum weight is taken as the reconstructed top-quark mass $m_{AMWT}$. Events that have no solutions or that have a maximum weight below a threshold are discarded. This removes 14.6% of the events, and 9934 events remain in the data, 1550 ee events, 6222 $e\mu$ events, and 2110 $\mu\mu$ events.

A likelihood $L$ is computed for values of $m_t$ between 161.5 and 184.5 GeV, from data in the range $100 < m_{AMWT} < 300$ GeV. For each value of $m_t$, the likelihood is computed by comparing the reconstructed mass distribution in data with the expectation from simulation. For the background, the reconstructed mass distribution of each individual process is added according to its expected relative contribution. Two different templates are used according to the b-tag multiplicity of the event, either one b-tagged jet, or two or more b-tagged jets. For the DY background, the relative contribution is derived from data in the $Z$-boson mass window. For the other processes, the contributions predicted by the simulation are used. The value that maximises the likelihood is calculated after fitting a quadratic function to the $-\ln L$ values obtained for all mass points and it is taken as the measurement of $m_t$. Using all the mass points in this fit yields pull widths that are closer to unity.

We determine the bias of this estimate using ensembles of pseudo-experiments based on the expected numbers of signal and background events, as shown in Fig. 1. Given the fit
Fig. 1 Mean mass bias (top) and pull width (bottom) for different top-quark masses in pseudo-experiments for the AMWT method. The red solid line represents the linear fit used to determine the correction to apply in order to minimise the residual bias and the blue dashed line show the expectation for an unbiased fit. The average pull width for the different top-quark masses is 0.99 to the data, a correction of $-0.34 \pm 0.20$ GeV is applied to the final result to compensate for the residual bias introduced by the fit (Fig. 1, top). This correction is obtained from the fit of a linear function to the average top-quark masses measured for different mass hypotheses. The width of the pull distribution is within 10% of unity for all the mass points, indicating that the statistical uncertainties are correctly estimated (Fig. 1, bottom).

After correction for the bias, the top-quark mass is measured to be $m_t = 172.50 \pm 0.43$ (stat.) GeV. The predicted distribution of the reconstructed masses $m_{\text{AMWT}}$ for a simulated top quark with mass $m_t = 172.5$ GeV, superimposed on the distribution observed in data, is shown in Fig. 2. The inset shows the distribution of the $-2\ln(L/L_{\text{max}})$ points with the quadratic fit used to measure $m_t$. The $\chi^2$ probability of the fit is 0.36.

6 Systematic uncertainties

The contributions from the different sources of uncertainty are summarised in Table 2. The uncertainty of the overall jet energy scale (JES) is the dominant source of uncertainty on $m_t$. The JES is known with an uncertainty of 1–3%, depending on the $p_T$ and $\eta$ of the jet [26]. Even in a high-pileup regime such as the one observed throughout the 2011 data taking period, the JES uncertainty is mostly dominated by the uncertainties on the absolute scale, initial- and final-state radiation, and corrections arising from the fragmentation and single-particle response in the calorimeter. It has been evaluated for 16 independent sources of systematic uncertainty. To estimate the effect of each source on the measurement of $m_t$, the $(p_T, \eta)$-dependent uncertainty is used to shift concurrently the energy of each jet by $\pm 1\sigma$ with respect to its nominal value, and correcting the $E_{\text{miss}}$ accordingly. For each source, pseudo-experiments are generated from simulated event samples for which the JES is varied by the relevant uncertainty, and the reconstructed top-quark mass distributions are fitted with the templates derived with the nominal JES. The average variation of the top-quark mass is used to estimate the systematic uncertainty. The quadratic sum of
the variation for each source is taken as the systematic uncertainty. The uncertainty on pileup corrections to the jet energy calibration (five sources) correspond to a combined uncertainty of 0.53 GeV on \( m_t \). Another important contribution is the overall data-to-simulation scale calibrated in photon + jet events, yielding a 0.51 GeV uncertainty. Other contributions are related to limited knowledge of the single-pion response (\( ^{+0.2}_{-0.3} \) GeV) and fragmentation models (0.3 GeV) used in the extrapolation as a function of jet \( p_T \). We also include a time-dependent effect (0.2 GeV) related to variations in calorimeter response in the endcaps. Residual \( \alpha_s \)-dependent corrections based on dijet balance studies (six sources) yield a negligible uncertainty on \( m_t \) (0.03 GeV).

All these sources added in quadrature give a combined JES uncertainty of \( ^{+0.096}_{-0.097} \) GeV. The final component of JES uncertainty corresponds to the uncertainty on the modeling of jet flavour dependence of the jet energy scale (\( ^{+0.76}_{-0.66} \) GeV) which is quoted separately in Table 2.

The uncertainty due to jet energy resolution is evaluated from pseudo-experiments where the jet energy resolution width in the simulation is modified by \( \pm 1 \sigma \) with respect to its nominal width. The uncertainty on the lepton energy scale is observed to have an almost negligible effect on the measurement of \( m_t \). The uncertainty in the \( E_{T}^{miss} \) scale is propagated to the measurement of \( m_t \) after subtracting the clustered (i.e. jet energy) and lepton components, which are varied separately as previously described. This procedure takes into account possible correlations between the different sources of uncertainty. The scale of the residual unclustered energy contribution to the \( E_{T}^{miss} \) is varied by \( \pm 10 \% \) and the corresponding variation of the top-quark mass measurement is evaluated from pseudo-experiments.

The uncertainty due to b-tagging efficiency was evaluated by varying the b-tagging efficiency and mistag rates of the algorithm by their respective uncertainties [27, 28]. The tagging rate was varied according to the flavour of the selected jet as determined from the simulation. This affects the multiplicity of b-tagged jets and the choice of the jets used in the reconstruction of \( m_t \).

The effect of statistical fluctuations in the templates is estimated by splitting the \( t \bar{t} \) sample in four independent subsamples and producing independent templates for each. Pseudo-experiments are performed using each new signal template, and the RMS variation of the average top-quark mass from each template is taken as an estimate of this uncertainty. The uncertainty on the calibration of the fit is added to the systematic uncertainty. The contribution from the uncertainty in the ratio between the signal and the background used in the fit is evaluated by varying by the corresponding uncertainty the expected number of events. The variation of the top-quark mass fit is assigned as a systematic uncertainty.

The effect due to the scale used to match clustered jets to partons (i.e. jet-parton matching) is estimated with dedicated samples generated by varying the nominal matching \( p_T \) thresholds from the default of 20 GeV down to 10 GeV and up to 40 GeV. Effects due to the definition of the renormalisation and factorisation scales used in the simulation of the signal are studied with dedicated Monte Carlo samples with both scales varied by factors of 2 or \( \frac{1}{2} \).

The uncertainty due to pileup is evaluated from pseudo-experiments where the total inelastic cross section used to simulate the pileup is varied within its uncertainty, which is estimated to be 8 %. The uncertainties related to the parton distribution function (PDF) used to model the hard scattering of the proton-proton collisions is evaluated from pseudo-experiments for which the distribution of \( m_t \) was obtained after varying parameters of the PDF by \( \pm 1 \sigma \) with respect to their nominal values and using the PDF4LHC prescription [14, 37, 38]. The differences found with respect to the nominal prediction are added in quadrature to obtain the total PDF uncertainty. The uncertainties due to the underlying event [13] and the colour reconnection [39] are evaluated with dedicated samples. The uncertainties due to the underlying event are estimated by comparing two alternative PYTHIA tunes with increased and decreased underlying event activity relative to a central tune. The results for the top-quark mass measured in pseudo-experiments using the Perugia 2011 tune are thus compared to the Perugia 2011 ‘mpiHi’ and Perugia 2011 Tevatron tunes [40]. The difference found between the two samples is taken as an estimate of the uncertainty in the modelling of the underlying event in our simulation. The Perugia 2011 ‘noCR’ tune is a variant in which colour reconnection effects are not taken into account.
account. The difference in the average top-quark mass, measured with and without colour reconnection effects, is taken as the estimate for the colour reconnection systematic uncertainty. Finally, the uncertainty due to the modelling of the signal templates by the Monte Carlo generator are studied by comparing the results of the pseudo-experiments using the reference sample to that from a sample generated with the POWHEG generator.

7 Measurement with the full kinematic analysis

An alternative measurement is performed using the KINb method [6] and a tighter event selection. The jet \( p_T \) is required to be at least 35 GeV and the reconstructed \( E_T^{\text{miss}} \) of \( e\mu \) events is required to be at least 30 GeV. These tighter requirements are expected to improve the resolution of the method. In KINb, as in the AMWT method, the kinematic equations describing the \( t\bar{t} \) system are solved many times per event for each lepton-jet combination. The longitudinal momentum of the \( t\bar{t} \) system \( (p_T^{\text{fit}}) \) is used as the extra constraint required to solve the equations. The jet \( p_T \), the \( E_T^{\text{miss}} \) direction, and the \( p_T^{\text{fit}} \) are varied independently according to their resolutions in order to scan the kinematic phase space consistent with the \( t\bar{t} \) system. The jet \( p_T \) resolution is obtained from the data [26]; the \( p_T^{\text{fit}} \) description, that is minimally dependent on \( m_t \), is taken from simulation. The solution with the lowest invariant mass of the \( t\bar{t} \) system is accepted if the mass difference between the top quark and antiquark masses is less than 3 GeV. The combination of leptons and jets yielding the largest number of solutions is chosen, and the mass value \( m_{\text{KINb}} \) is estimated by means of a Gaussian fit to the distribution of solutions in a 50 GeV window built around the most probable value. A key point in the method is the choice of the jets used to reconstruct the top-quark candidate, favouring jets that have higher value of the b-tagging discriminator. Simulations demonstrate that the proportion of events in which the jets used for the reconstruction are correctly matched to partons from top quark decays is increased significantly with respect to a choice based on the two jets with highest \( p_T \). Only events with solutions contribute to the \( m_t \) measurement; in simulation, solutions are found for 80% of signal events and 70% of background events.

We use a two-component unbinned maximum-likelihood fit to the \( m_{\text{KINb}} \) distribution to mitigate the effect of background and signal events with misreconstructed top-quark masses and obtain an estimate of \( m_t \). The free parameters of the likelihood are \( m_t \) and the numbers of signal and background events. The main background contribution is from the DY events, which is estimated from data using a template fit to the angle between the momenta of the two leptons. Depending on \( m_t \), the signal and background templates may resemble each other; therefore the number of background events is constrained by a Gaussian term in the likelihood function. The parameters of signal and background templates are taken from simulation and fixed in the fit. The signal shape is obtained with a simultaneous fit of simulated \( t\bar{t} \) samples to a Gaussian plus Landau function template with parameters that are linear functions of \( m_t \). Separate templates are used for the four samples corresponding to the same or different flavour dileptons with one or two and more b-tagged jets. In each category the backgrounds are added in the expected proportions. The expected distribution from DY events is determined from data near the \( Z \) peak \((76 < M_{\ell\ell} < 106 \text{ GeV})\) for same-flavour dileptons. From simulation, the template obtained near the \( Z \) peak is expected to describe well DY events in the signal region. In the case of different-flavour dileptons we estimate the contribution from DY events using a data sample of \( Z \rightarrow \mu\mu \), by replacing the muons with fully simulated decays of \( \tau \) leptons [41] and applying the event selection and top-quark mass reconstruction. For single top quark, diboson, and other residual backgrounds the templates are taken from simulation.

The fit is performed separately for same- and different-lepton flavour events with either one or at least two b-tagged jets using an unbinned likelihood method, where the inputs are the mass value returned by the KINb method in the data, and the probability density function for signal and background. The data in the range \( 100 < m_{\text{KINb}} < 300 \) GeV is used in the fit. Figure 3 (inset) shows the variation of \(-2\ln(L/L_{\text{max}})\) as a function of \( m_t \), for the different categories individually and for all categories combined. For each event category the corresponding likelihood is maximised, yielding an estimate of the top-quark mass value as well as the expected numbers of signal and background events. The result of the fit for the category of events with the smallest background contamination \((e\mu \text{ events with at least two b-tagged jets})\) is shown in Fig. 3.

The expected contamination from background events and the result obtained from the fit in each category agree well. A combined unbinned likelihood is constructed in order to extract the final measurement of \( m_t \) from data. To minimise any residual bias resulting from the parameterisations of the signal and background \( m_{\text{KINb}} \) distributions, pseudo-experiments are performed using simulated dilepton events generated with different \( m_t \) values. The resulting \( m_t \) distributions are used to calibrate the parametrisation of the signal template. We find an average bias on \( m_t \) of \( 0.4 \pm 0.2 \) GeV, which we use to correct our final value. We assign the envelope of the residual bias (0.2 GeV) as the systematic uncertainty associated with the fit.

Other sources of systematic uncertainty are similar and fully correlated with those in the AMWT analysis. We observe however that the KINb method is affected by larger
uncertainties compared to the AMWT method, reflecting the fact that the mass resolution is slightly poorer. The degradation of the resolution is related to the fact that a choice is made for the lepton-jet assignment in the event and that there is no reweighting of the solutions found based on any expectation for the kinematic properties, such as polarization effects which are intrinsically modelled by Eq. (2). We find no improvement in combining the AMWT and KINb given the difference in statistical uncertainty achieved and the dominance of the correlated systematic uncertainties. The KINb analysis is thus used as a cross-check, and we measure $m_t = 171.8 \pm 0.6 \text{ (stat.)} \pm 2.2 \text{ (syst.) GeV}$, in agreement with the AMWT measurement.

8 Summary

In summary, a measurement of the top-quark mass from $t\bar{t}$ decays to dilepton final states is presented, using a data sample corresponding to an integrated luminosity of 5.0 fb$^{-1}$ recorded by the CMS experiment at $\sqrt{s} = 7$ TeV. The measurement yields $m_t = 172.5 \pm 0.4 \text{ (stat.)} \pm 1.5 \text{ (syst.) GeV}$. An alternative measurement gives a consistent result. With respect to the previous measurement in the dilepton channel performed by CMS on the 36 pb$^{-1}$ data collected in 2010 [6], the systematic uncertainty could be reduced substantially by improved understanding of the effect of pileup, underlying event and the uncertainty on the JES. To date, this measurement is the most precise determination of the top-quark mass in the dilepton channel.

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