Vapor pressures of substituted polycarboxylic acids are much lower than previously reported

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Received: 30 November 2012 – Published in Atmos. Chem. Phys. Discuss.: 10 January 2013
Revised: 4 June 2013 – Accepted: 7 June 2013 – Published: 12 July 2013

Abstract. The partitioning of compounds between the aerosol and gas phase is a primary focus in the study of the formation and fate of secondary organic aerosol. We present measurements of the vapor pressure of 2-methylmalonic (isosuccinic) acid, 2-hydroxyxymalonic (tartronic) acid, 2-methylglutaric acid, 3-hydroxy-3-carboxy-glutaric (citric) acid and DL-2,3-dihydroxy succinic (DL-tartaric) acid, which were obtained from the evaporation rate of supersaturated liquid particles levitated in an electrolydynamic balance. Our measurements indicate that the pure component liquid vapor pressures at 298.15 K for tartronic, citric and tartaric acids are much lower than the same quantity that was derived from solid state measurements in the only other room temperature measurement of these materials (made by Booth et al., 2010). This strongly suggests that empirical correction terms in a recent vapor pressure estimation model to account for the inexplicably high vapor pressures of these and similar compounds should be revisited, and that due caution should be used when the estimated vapor pressures of these and similar compounds are used as inputs for other studies.

1 Introduction

The production of secondary organic aerosol (SOA) by gas-to-particle partitioning is generally represented by an equilibrium partitioning model such as that of Pankow (1994, 2003). This framework has recently been applied in box models and large scale atmospheric models by means of a volatility basis set (VBS; see, e.g., Donahue et al., 2011, and references therein). A key physical parameter which governs gas-particle partitioning is the pure component vapor pressure ($p^v$), which is difficult to accurately measure at atmospheric temperatures for low- and semi-volatile organic compounds (L/SVOC) such as polycarboxylic acids. Note that throughout this article, the term “vapor pressure” is used as defined by chemical thermodynamics to denote the partial pressure of a compound in equilibrium with a liquid or solid phase, which is sometimes emphasized by the equivalent term “equilibrium vapor pressure”.

Vapor pressure measurements of L/SVOC may be made by following the volatilization of bulk samples (e.g., Verevkin et al., 2000; Ribeiro da Silva et al., 2001; Booth et al., 2010; Bruns et al., 2012), ensembles of airborne or deposited droplets (e.g., Cappa et al., 2007; Salo et al., 2010), and single trapped airborne droplets (e.g., Zardini et al., 2006; Pope et al., 2010; Soonsin et al., 2010; Krieger et al., 2012) or by other techniques such as gas–liquid chromatography (see review by Letcher and Naicker, 2004). Generally, the agreement of different techniques is reasonable for measurements in which the sample state is positively identified and unexpectedly poor for measurements where the physical state is not well controlled (Soonsin et al., 2010; M. Bilde, personal communication, 2012). Vapor pressures are generally reported for the liquid state $p^{v, L}$ (not to be confused with $p^v$, which we will use to denote the vapor pressure of a pure compound in an unspecified physical state), which is the reference state for most models of atmospheric partitioning. However, vapor pressure measurements of polycarboxylic acids are generally made in the solid state ($p^{v, S}$) as these compounds have
a melting point above room temperature. The measured solid state vapor pressure \( p^{\alpha,S} \) can be converted to the liquid vapor pressure \( p^{\alpha,L} \) by the enthalpy of fusion, the melting temperature, and the change in heat capacity upon melting (Prausnitz et al., 1999). While it is possible to measure either \( p^{\alpha,S} \) or \( p^{\alpha,L} \), it is preferable to measure directly in the liquid state when reporting \( p^{\alpha,L} \) to circumvent the phase conversion and its associated uncertainty. As these compounds are solid at room temperature, measurements of \( p^{\alpha,L} \) can only be made directly in small droplets, in which strong supersaturations or subcoolings can be maintained without crystallization.

There are several cases (e.g., tartaric compared with succinic acid) in which the \( p^{\alpha,L} \) reported by Booth et al. (2010) increases upon functionalization of the carbon backbone with an oxygen-bearing substituent, a counterintuitive result. There have been a few specific cases reported in the literature where addition of an oxygen-bearing functional group to a parent structure can lead to an increase of the solid-state vapor pressure. As discussed in Zuend and Seinfeld (2012), such effects have been reported, e.g., by Chattopadhyay and Ziemann (2005) for substitutions where a ketone group is added in \( \alpha \)-position to a carboxyl group. While keto substitutions in \( \alpha \)-position of a carboxyl group can raise the solid-state vapor pressure of a dicarboxylic acid with respect to the unsubstituted parent structure, keto substitutions at a \( \beta \)-position or further away from the carboxyl group always resulted in decreased solid-state vapor pressure. Chattopadhyay and Ziemann (2005) suggest that a ketone group in \( \alpha \)-position may form an internal hydrogen bond with the carboxyl group. Such an internal hydrogen bond may reduce the level of intermolecular hydrogen bonding and may lead to an increase in vapor pressure relative to the unsubstituted parent carboxylic acid. However, such effects on the pure compound vapor pressure have been observed only for samples measured in the solid state. Although the presence of intermolecular group interactions may lessen the reduction in vapor pressure as compared to the prediction of a simple “additive” group-contribution model, the typical behavior observed is that addition of an oxygen-bearing functional group to an organic structure lowers the pure compound vapor pressure. In this study, we present \( p^{\alpha,L} \) measured using an electrodynamic balance (EDB) technique to directly access supersaturated liquid-state conditions in single droplets of five compounds, including three of the functionalized polycarboxylic acids for which Booth et al. (2010) reported unexpected high volatility. To the authors’ knowledge, these are the first measurements of \( p^{\alpha,L} \) obtained directly from the liquid state for 2-hydroxymalonic acid (2-hMA), 2-methylglutaric acid (2-mGA), and tartaric acid (TA).

The number of different compounds present in atmospheric aerosols necessitates the use of estimation methods that rely on structure–activity relationships, such as the Nannoolal et al. (2008) or Moller et al. (2008) methods or EVAPORATION (Estimation of VApour Pressure of ORganics, Accounting for Temperature, Intramolecular, and Non-additivity effects) (Compernolle et al., 2011) to estimate the aerosol mass generated by chemical processing of volatile and semivolatile organic compounds in the gas and particle phases. In this study, we focus on comparison of our measurements to the EVAPORATION model, which is intended to enable the prediction of \( p^{\alpha,L} \) for polyfunctional molecules that occur in SOA. The model has been optimized to account for the influence of hydrogen bonding and intramolecular group interactions on \( p^{\alpha,L} \) and has been parameterized with the most recent experimental data for polyfunctional acids. Although Compernolle et al. (2011) endeavor to reproduce measurements of \( p^{\alpha,L} \) for substituted polycarboxylic acids reported by Booth et al. (2010) by implementing an empirical correction term, they are not able to rationalize these effects. Because only few measurements are available for such compounds, a danger of overfitting exists (see discussion in Barley and McFiggans, 2010), especially since some compounds have been measured only with a single technique. This highlights the need for accurate measurements of \( p^{\alpha} \) (and especially direct measurements of \( p^{\alpha,L} \)) to assure the accuracy of models of partitioning-driven aerosol formation. In their manuscript, Compernolle et al. (2011) noted that measurements using the methodology of Soonsin et al. (2010) were needed for these compounds. The measurements presented in this work begin to address that need, but are not intended to be an exhaustive set that will allow for a re-fitting of models such as EVAPORATION. Rather, we intend them to demonstrate the existence of substantial deviations from previous experimental data and as an immediate caveat to anyone using EVAPORATION or similar models to predict partitioning of substituted polycarboxylic acids. Finally, we show that the EVAPORATION model can be modified to yield predictions in better agreement with our measurements.

2 Method

Vapor pressures of pure melts and aqueous solutions of substituted polycarboxylic acids were measured using the electrodynamic balance (EDB) apparatus and technique described in Soonsin et al. (2010). In this technique, the evaporation rate of a levitated particle is related to vapor pressure via continuum theory (see discussion in Sect. IV of Krieger et al., 2012). The EDB apparatus consists of a three-wall temperature-controlled glass chamber containing a levitated charged particle held in place through applied electric AC and DC fields. A constant flow (typically 25 sccm) of a \( \text{N}_2/\text{H}_2\text{O} \) gas mixture with a controlled \( \text{H}_2\text{O} \) partial pressure is pumped continuously through the chamber at a constant total pressure adjustable between 200 and 1000 hPa. The temperature can be varied between 330 K and 160 K with a stability better than 0.1 K and an accuracy of ±0.5 K. The relative humidity in the chamber is set by automatic mass flow controllers regulating the \( \text{N}_2/\text{H}_2\text{O} \) mixing ratio. During an experiment, the temperature and the relative humidity
are kept constant while measuring a particular evaporation rate. Note that the N₂/H₂O gas flow is completely free of any evaporated organic molecules prior to entering the glass chamber as the gas flow is freshly generated from a purified liquid N₂ reservoir, part of which is flowing over an enclosed temperature-controlled liquid solution of purified, deionized water containing 2.5 wt-% of dissolved sulfuric acid to scrub any ammonia from laboratory air potentially leaking into the system. Injection solutions had an ana-lyte content between 0.5 % and 4 % by weight, leading to particles of approximately 2 to 9 μm dry radius. Evaporation of the solvent from the particle was judged to be complete when a steady shrink rate was established under constant temperature (T) and relative humidity (RH). Highly supersaturated particles with respect to solid phases can be obtained due to the small (micrometer-range) particle radius and wall-free containment of the EDB. For simplicity, we will refer to measurements as being on a “solution” without specifying if the sample was supersaturated, or on the “subcooled melt” for the pure component. All measurements were taken on spherically symmetric (i.e., non-crystalline) particles, as judged by the regularity of the angular fringes of scattered laser light (see Zardini et al., 2006), and measurements were made on at least two particles for all investigated substances.

Throughout each measurement, T, RH, and background gas pressure were held constant (to within 0.25 K, 0.5 %, and 1 torr, respectively), and the particle radius was measured to a high degree of precision using morphology (radius) dependent resonance spectroscopy (Zardini et al., 2006). Vapor pressure measurements were made on subcooled melt droplets or solution droplets with the organic concentration in water controlled by the RH in the EDB. A continuous flow of 20–35 cm³ min⁻¹ organic-free N₂ gas with a known water content was applied and the ambient pressure was regulated to 600 ± 1 torr (79.99 ± 0.13kPa). As the partial pressure of the organic decreases with decreasing organic solute activity on the mole fraction basis (aorg), measurements were most often performed at low to moderate humidity (RH < 40 %).

After the particle was equilibrated with respect to T and RH, any change in size was attributed to evaporative loss (cf., Sect IV of Krieger et al., 2012), and the vapor pressure (p) of the organic substance under those conditions (RH, T) was calculated using Eq. (1) of Soonsin et al. (2010):

\[
p = -\frac{1}{2} \frac{d\rho^2}{dr} \times \frac{x \rho R T}{(x M_{\text{org}} + (1-x) M_w) D_v}.
\]

where r is the particle radius, x is the mole fraction of the organic solute, ρ is the density of the condensed phase, R is the gas constant, M is molar mass, D_v is the diffusivity of the organic vapor in the buffer atmosphere, and “org” and “w” refer to the organic component and water, respectively. Strictly, Eq. (1) is valid for stagnant conditions. However, the geometry of our EDB together with the flows used keeps the enhancement in evaporation rate due to the gas flow below 0.1 % (Zhang and Davis, 1987). On the other hand, the flow needs to be sufficiently large to avoid any significant contamination of the gas phase by the organic vapor evaporating from the particle. The partial pressure of the organic substance far from the particle, p∞, has to be only a small fraction of the vapor pressure p. Our flows are sufficient to keep the ratio p∞/p below 1 %, (cf., Zhang and Davis, 1987). The derivation or measurement of each term in Eq. (1) will be discussed below.

2.1 Radius

The particle radius as a function of time was determined by combining an absolute radius from the two-dimensional scattering pattern at one point in time with the fractional change in particle radius as a function of time from morphology dependent resonance spectroscopy (Zardini et al., 2006):

\[
r(t) = r(t_0) \times \frac{\lambda(t)}{\lambda(t_0)},
\]

where t₀ is the initial time and λ is the wavelength at which the Mie resonance occurs. Each particle was sized at one stage of the experiment, and the radius was calculated at all other times based on that initial radius and the change in radius calculated from Mie spectra, such that the retrieved radius of the particle was self-consistent. In this calculation of particle radius, we have neglected any shift in Mie peaks arising from changes in the index of refraction due to changing RH. Examples of raw radius data as a function of time at constant T and RH are given for 2-mGA, CA, and TA in Appendix A and shown in Fig. A1.

The absolute radius of the particle at one point in time was retrieved from the spacing of fringes of the two-dimensional scattering pattern at 90° following the method outlined in Eq. (25) of Glantschnig and Chen (1981). Using the small angle approximation, we equate the angular separation of fringes Δθ with their linear separation on the detector. Calibration was performed by injecting a single latex sphere (Polyscience Inc., Warrington, PA, nominal diameter 10 μm) and measuring the separation of the fringes.

The fractional change in particle radius was measured by tracking the change in wavelength of a Mie scattering resonance from a single particle as a function of time (Δλ/Δt). As in Zardini et al. (2006), the particle was illuminated with a LED (λ_center = 589 nm, FWHM = 16 nm, radiant power 150 μW) and backscattered light was collected and imaged using a 150 mm spectrograph with a CCD detector. The quantity Δλ/Δt is directly related to the change in size of a particle when following a single Mie resonance (Zardini et al., 2006), if the index of refraction of the particle is constant. The change in wavelength of a group of Mie resonances as a function of time, Δλ/Δt, was retrieved using a custom script based on a digital image correlation algorithm in the Mathworks Matlab environment. This quantity was then used along with the retrieved r(t₀) to calculate r(t) via Eq. (2).
2.2 Mole fraction of solute

The mole fraction of organic compound in an aqueous particle was calculated from the RH in the EDB by assuming that the particle concentration is equivalent to measured RH, i.e., that the particle is homogeneous and in thermodynamic equilibrium. The thermodynamic group-contribution model AIOMFAC (Aerosol Inorganic-Organic Mixtures Functional groups Activity Coefficients) developed by Zuend et al. (2008, 2011) was used to calculate activity coefficients of water and organic compounds as a function of the droplet mixture composition. The activity coefficients account for non-ideal mixing, which influences vapor pressure via modified Raoult’s law (Zuend et al., 2010). For simplicity, AIOMFAC was run in this study are summarized in Table 1 and the raw data for 2-mGA density were made using a 10 mL pyrometer (Blaubrand, 43408) on solutions from 0.11 to 0.75 weight fraction organic in water. We determined \( V_{\text{org}} \) of 119.7 \( \pm \) 0.3 \( \text{cm}^3 \text{mol}^{-1} \) for 2-mGA by fitting \( V_{\text{org}} \) to experimentally determined densities of aqueous solutions using Eq. (3). Experimental data from Laguerie et al. (1976) and Washburn et al. (1926) were used to calculate the molar volume of CA and TA, respectively. All density parameters used in this study are summarized in Table 1 and the raw data for 2-mGA density as a function of solute weight fraction in water are given in Table 2.

2.3 Density

Density was parameterized by assuming additivity of the molar volumes of the components and fitting experimental data to the equation

\[
\rho = \frac{x \times M_{\text{org}} + (1-x) \times M_w}{x \times V_{\text{org}} + (1-x) \times V_w},
\]

where \( V \) is the molar volume, and all other variables and subscripts are defined as above. Such a fit is necessary because density measurements are available only for (sub-)saturated bulk solutions, while measurements often took place under highly supersaturated conditions. The molar volumes of 2-hydroxymalonic acid and 2-methylmalonic acid were retrieved from the SciFinder website, which provides \( V_{\text{org}} \) calculated by the Advanced Chemistry Development, Inc. software (ACD/Labs, 2012). Measurements of 2-methylglutaric acid density were made using a 10 mL pyrometer (Blaubrand, 43408) on solutions from 0.11 to 0.75 weight fraction organic in water. We determined \( V_{\text{org}} \) of 119.7 \( \pm \) 0.3 \( \text{cm}^3 \text{mol}^{-1} \) for 2-mGA by fitting \( V_{\text{org}} \) to experimentally determined densities of aqueous solutions using Eq. (3). Experimental data from Laguerie et al. (1976) and Washburn et al. (1926) were used to calculate the molar volume of CA and TA, respectively. All density parameters used in this study are summarized in Table 1 and the raw data for 2-mGA density as a function of solute weight fraction in water are given in Table 2.

2.4 Diffusivity of organic vapor

The diffusivity of organic vapor in nitrogen was estimated following the method of Bilde et al. (2003): the group contribution method of Lydersen (1955) was used to determine the critical volume \( V_c \) and the diffusivities used in this study were calculated using Eqs. (17.3–12) from Bird et al. (2007):

\[
D_v = 0.0018583 \times T^3 \times \left( \frac{1}{M_{N_2}} + \frac{1}{M_{\text{org}}} \right) \times \frac{1}{P \times \sigma_{\text{AB}}^2 \times \Omega},
\]

where \( P \) is the ambient gas pressure, \( \sigma_{\text{AB}} \) is one of the Lennard-Jones parameters for the organic material in \( N_2 \), \( \Omega \) is the collisional integral, and all other symbols are defined as above. The values of \( D_v \) for each material are given for \( T = 298.15 \text{K} \) in Table 3.

2.5 Materials

Materials were as follows: Millipore water (resistivity > 18.2 M\( \Omega \) cm, total organic content < 5 ppb) was used as the injection solvent for 2-methylmalonic acid (2-mMA, 2-methylpropanedioic acid, Sigma-Aldrich > 99%), 2-hydroxymalonic acid (2-hMA, 2-hydroxypropanedioic acid, > 97%, Sigma-Aldrich), 2-methylglutaric acid (2-mGA, 2-methylpentanedioic acid, > 99% ABCR, Karlsruhe, Germany and > 98%, Fluka), and citric acid monohydrate (CA, 3-carboxy-3-hydroxypentanedioic acid, Fluka, > 99.5%). A mixture of approximately 1:1 by volume diethyleneglycol (Fluka, > 99%) with Millipore water was used as an injection solvent for DL-tartaric acid (TA, 2,3-dihydroxybutanedioic acid, > 99%, Aldrich) to prevent crystallization upon injection that occurs when pure water is used. All reagents were used as received with no additional purification. Organic-free, very low humidity nitrogen carrier gas was obtained from the blowoff of a dewar containing liquid nitrogen.
Table 3. Parameters for estimation of organic compound vapor diffusivity in \( \text{N}_2 \) at 600 torr (~ 80 kPa) at 298.15 K.

<table>
<thead>
<tr>
<th>Material</th>
<th>( V_c ) (cm(^3))</th>
<th>( \sigma_B ) (Å)</th>
<th>( \epsilon_{AB}/k_B ) (K)</th>
<th>( \Omega )</th>
<th>( D_x ) (cm(^2)s(^{-1}))</th>
</tr>
</thead>
<tbody>
<tr>
<td>2-Methylmalonic acid</td>
<td>306</td>
<td>4.667</td>
<td>279.7</td>
<td>1.40</td>
<td>0.0835</td>
</tr>
<tr>
<td>2-Hydroxymalonic acid</td>
<td>269</td>
<td>4.548</td>
<td>287.4</td>
<td>1.42</td>
<td>0.0867</td>
</tr>
<tr>
<td>2-Methylglutaric acid</td>
<td>380</td>
<td>6.091</td>
<td>260.1</td>
<td>1.347</td>
<td>0.0777</td>
</tr>
<tr>
<td>Citric acid</td>
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<td>6.440</td>
<td>285.8</td>
<td>1.406</td>
<td>0.0681</td>
</tr>
<tr>
<td>DL-Tartaric acid</td>
<td>338</td>
<td>5.858</td>
<td>291.6</td>
<td>1.440</td>
<td>0.0762</td>
</tr>
</tbody>
</table>

3 Analysis

3.1 Extraction of \( \rho^{\circ\text{L}} \) as a function of temperature

While \( \rho^{\circ\text{L}} \) is the quantity of interest in this study, higher quality data are achieved by measuring \( \rho^L \) of aqueous solutions of the organic compound at several concentrations to extract \( \rho^{\circ\text{L}} \) at \( a_{\text{org}} = 1 \). When measurements of \( \rho^L \) were available at multiple \( a_{\text{org}} \), a weighted linear least-squares fit of the data through \( (a_{\text{org}} = 0, \ \rho = 0 \text{Pa}) \) was used to extract \( \rho^{\circ\text{L}} \). The data in Fig. 1 are an example of the retrieved \( \rho^L \) of 2-mGA as a function of \( a_{\text{org}} \) at a single \( T \). The error of the resulting fit slope was propagated from the calculated error on each point following the method of Lyons (1986, p. 127) and used in the calculation of the error on \( \rho^{\circ\text{L}} \) at each \( T \); in general, points with longer duration measurement or at lower water activity \( (a_w) \) have smaller error bars. As discussed in Soonsin et al. (2010), the linear fit of \( \rho^L \) against \( a_{\text{org}} \) provides a more robust measure of \( \rho^{\circ\text{L}} \) than a single measurement at \( a_{\text{org}} = 1 \).

As the materials under study here have lower \( \rho^{\circ\text{L}} \) than those in the preceding study by Soonsin et al. (2010), which employed the same EDB apparatus, it was not always possible to quantify the evaporative loss of particle mass. Therefore, a detailed error analysis was performed that allows us to report an upper limit for measurements below the limit of quantitation \( (\text{LoQ}) \) and used in the calculation of the error on \( \rho^{\circ\text{L}} \) at each \( T \); in general, points with longer duration measurement or at lower water activity \( (a_w) \) have smaller error bars. As discussed in Soonsin et al. (2010), the linear fit of \( \rho^L \) against \( a_{\text{org}} \) provides a more robust measure of \( \rho^{\circ\text{L}} \) than a single measurement at \( a_{\text{org}} = 1 \).

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Table 4. Vapor pressure data from this study and comparison to data from the literature. Abbreviations are: 2-mMA, 2-methylmalonic acid; 2-hmA, 2-hydroxymalonic acid; 2-mGA, 2-methylglutaric acid; 3-mGA, 3-methylglutaric acid; TA, DL-tartaric acid; CA, citric acid. Data are organized as experimental studies reporting liquid-state vapor pressure (\(p^{\nu,L}\)), experimental studies reporting solid-state vapor pressure (\(p^{\nu,S}\)), and model predictions of liquid-state vapor pressure (\(p^{\nu,L}\)), including 3-methylglutaric acid for comparison to 2-methylglutaric acid. All data are reported in Pa at \(T^\ominus = 298.15\) K unless stated otherwise. For citric and tartaric acids, extrapolations to \(T^\ominus\) are reported along with data obtained at \(T > T^\ominus\). Superscript letters indicate notes on data or reference.

<table>
<thead>
<tr>
<th></th>
<th>2-mMA</th>
<th>2-hmA</th>
<th>2-mGA</th>
<th>3-mGA</th>
<th>TA</th>
<th>CA</th>
</tr>
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<tr>
<td>Experimental liquid-state measurements</td>
<td>(1.1±0.3)×10^{-3}</td>
<td>(4.4±1.2)×10^{-6}</td>
<td>(1.0±0.2)×10^{-3}</td>
<td>–</td>
<td>(3.2±1.0)×10^{-7} (~305 K)</td>
<td>&lt;1.6×10^{-7} (~311 K)</td>
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<td>This Measurement</td>
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<td>–</td>
<td>–</td>
<td>–</td>
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<td>–</td>
<td>–</td>
<td>–</td>
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</tr>
<tr>
<td>Booth et al. (2010)</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>(1.8 – 4.9)×10^{-8}</td>
<td>&lt;1.4×10^{-9}</td>
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<td>Matster et al. (2004)</td>
<td>(5.3±4.0)×10^{-3}</td>
<td>(5.6±4.2)×10^{-3}</td>
<td>(9.6±7.2)×10^{-4}</td>
<td>(9.2±6.9)×10^{-4}</td>
<td>(3.2±2.4)×10^{-5}</td>
<td>(3.1±2.3)×10^{-3}</td>
</tr>
<tr>
<td>Yaws et al. (2009)</td>
<td>(9.1±3.2)×10^{-4}</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>(1 – 40)×10^{-9}</td>
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<tr>
<td>Experimental solid-state measurements</td>
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<td>–</td>
<td>–</td>
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<td>Booth et al. (2010)</td>
<td>(3.3±1.3)×10^{-4}</td>
<td>(2.5±1.0)×10^{-4}</td>
<td>(1.9±0.7)×10^{-4}</td>
<td>(1.8±0.7)×10^{-4}</td>
<td>(1.8±0.7)×10^{-4}</td>
<td>(3.8±1.5)×10^{-5}</td>
</tr>
<tr>
<td>Ribeiro da Silva et al. (2000)</td>
<td>(5.8±2.9)×10^{-4}</td>
<td>–</td>
<td>–</td>
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<td>Ribeiro da Silva et al. (2001)</td>
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<tr>
<td>de Wit et al. (1983)</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>(1.3–2.6)×10^{-9}</td>
<td>–</td>
</tr>
<tr>
<td>Model liquid-state predictions</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
</tr>
<tr>
<td>Compernolle et al. (2011) (^b)</td>
<td>(5.0^{+1.7}_{-1.1})×10^{-3}</td>
<td>(1.9^{+0.2}_{-0.1})×10^{-3}</td>
<td>(5.4^{+2.1}_{-1.0})×10^{-4}</td>
<td>–</td>
<td>(4.0^{+0.6}_{-0.2})×10^{-3}</td>
<td>(5.0^{+0.7}_{-0.2})×10^{-5}</td>
</tr>
<tr>
<td>Compernolle et al. (2011) (^c)</td>
<td>(5.0^{+1.3}_{-1.0})×10^{-3}</td>
<td>(9.1^{+1.4}_{-1.5})×10^{-5}</td>
<td>(5.4^{+2.3}_{-1.2})×10^{-4}</td>
<td>–</td>
<td>(2.8^{+0.7}_{-0.1})×10^{-7}</td>
<td>(8.7^{+3.1}_{-5.2})×10^{-10}</td>
</tr>
<tr>
<td>Nannoolal et al. (2008) (^d)</td>
<td>(3.7±3.1)×10^{-2}</td>
<td>(2.0±1.7)×10^{-6}</td>
<td>(3.1±2.7)×10^{-3}</td>
<td>–</td>
<td>(1.4±2.0)×10^{-9}</td>
<td>(9.1±7.8)×10^{-13}</td>
</tr>
<tr>
<td>Moller et al. (2008) (^h)</td>
<td>(1.1±0.3)×10^{-1}</td>
<td>(2.1±0.5)×10^{-4}</td>
<td>(8.2±0.2)×10^{-3}</td>
<td>–</td>
<td>(6.9±1.7)×10^{-8}</td>
<td>(2.7±0.6)×10^{-10}</td>
</tr>
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</table>

\(^a\) Extrapolation to \(T^\ominus\) using \(\Delta \text{H}_{\text{vap}}=75\) kJ mol\(^{-1}\).
\(^b\) Extrapolation to \(T^\ominus\) using \(\Delta \text{H}_{\text{vap}}=250\) kJ mol\(^{-1}\).
\(^c\) Assumed liquid (the physical state was not specified), see Sect. 4.1.
\(^d\) Extrapolation of data from 426 K < \(T < 451\) K.
\(^e\) Extrapolation of data from 341 K < \(T < 354\) K.
\(^f\) Extrapolation of data from 338 K < \(T < 348\) K.
\(^g\) Extrapolation of sublimation data from 411 K < \(T < 440\) K.
\(^h\) EVAPORATION model.
\(^i\) EVAPORATION model without correction for substituted polycarboxylic acids.
\(^j\) The method of Nannoolal et al. (2008) was used with the \(T_0\) estimate of Nannoolal et al. (2004).
\(^k\) The method of Moller et al. (2008) was used with the \(T_0\) estimate of Nannoolal et al. (2004).

4 Results and discussion

The \(p^{\nu,L}\) determined here, along with a comparison to previous measurements in both the liquid (\(p^{\nu,L}\)) and solid states (\(p^{\nu,S}\)) and to a few common models of vapor pressure, are summarized in Table 4 and graphically depicted in Fig. 2. Figures 3 through 7 show the pure compound vapor pressure \(p^{\nu,L}\) obtained in this study as a function of inverse temperature (cf., Eq. 5) for each compound. Experimental data are shown as open symbols with error bounds extending to two standard errors; within each plot, different particles are shown using different symbols. The dashed fit line in these figures is made by weighting the data by the square of their inverse relative error, and extends to \(T^\ominus = 298.15\) K. The 2\(\sigma\) bounds of fit lines are shown as dotted lines. Data that are indistinguishable from zero are reported as the highest value allowed by the statistical (propagated) error, and displayed in plots with their bottom error bar off-scale.

4.1 2-Methylmalonic acid

The \(p^{\nu,L}\) of 2-mMA as a function of inverse \(T\) is displayed in Fig. 3. Based on the fit of Eq. (5) to these data, we determine \(\Delta \text{H}_{\text{vap}} = (89 \pm 15)\) kJ mol\(^{-1}\). Measurement times shown were a few hours to a few days per point, not including instrument settling time. The calculated \(p^{\nu,L}(T^\ominus)\) of (1.1 ± 0.3) \times 10^{-3} Pa is just inside the lower error bound of the measurements of Booth et al. (2010) and is in excellent agreement with the measurement of Mønster et al. (2004) for this compound.

Although the physical state of the aerosol was not reported in the study of Mønster et al. (2004), we assert that it was liquid as our measurements of 2-mMA carried out under dry (RH < 3%) conditions for many days did not result in particle crystallization. Measurements in the tandem differential mobility analyzer (TDMA) used by Mønster et al. (2004) were performed on a shorter timescale and used aerosol particles of smaller size than our measurement, both of which decrease the probability of crystallization. This assertion is supported by Riipinen et al. (2007), who determined that
Fig. 2. Pure component vapor pressures at $T = 298.15 \text{ } (^\circ\text{C})$ for 2-methylmalonic acid (2-mMA), 2-hydroxymalonic acid (2-hMA), 2-methylglutaric acid (2-mGA), DL-tartaric acid (TA), and citric acid (CA) – from this work (liquid) and from previous measurements reported in the liquid state, the solid state and the EVAPORATION model with and without empirical correction term as well as two commonly used models (all in liquid state). CA from this study is shown using the most conservative (largest) upper limit. Counter intuitively, the liquid vapor pressure measured here for 2-hMA, TA and CA is smaller than the solid-state vapor pressure reported by Booth et al. (2010). See Table 4 for full reference list.

Fig. 3. Pure component vapor pressure $p^{\circ\text{L}}$ of 2-methylmalonic acid (open symbols, denoting two different particles). Fit line (dashed) is to Eq. (5) with 2$\sigma$ error bounds shown as dotted lines.

malonic acid was in the liquid state during vapor pressure measurements, employing the same technique and apparatus as that of Mønster et al. (2004).

4.2 2-Hydroxymalonic acid

The $p^{\circ\text{L}}$ of 2-hMA is displayed in Fig. 4 using the same axes and fitting procedure as for 2-mMA in Sect. 4.1. We determine $\Delta H_{\text{vap}}^{\circ} = (120 \pm 19) \text{ } \text{kJ mol}^{-1}$ from a fit of Eq. (5) to experimental data. Measurement times shown were many hours to a few days per point, not including instrument settling time. The calculated $p^{\circ\text{L}}(T^{\circ})$ of $(4.4 \pm 1.2) \times 10^{-6} \text{ Pa}$ is around three orders of magnitude lower than the value of $p^{\circ\text{L}}$ reported by Booth et al. (2010).

4.3 2-Methylglutaric acid

The $p^{\circ\text{L}}$ of 2-mGA is displayed in Fig. 5 using the same axes and fitting procedure as for 2-mMA in Sect. 4.1. We determine $\Delta H_{\text{vap}}^{\circ} = (97.3 \pm 3.5) \text{ } \text{kJ mol}^{-1}$ by fitting Eq. (5) to the experimental data. Measurement times shown in Fig. 5 were a few hours to several days per point, not including instrument settling time. These data demonstrate that the EDB method is reliable over a broad range of pressures and can
retrieve pressures of $1 \times 10^{-6}$ Pa and lower. The calculated $p^{\circ,L}(T^\ominus)$ of $(1.0 \pm 0.2) \times 10^{-3}$ Pa agrees very well with the value reported by Booth et al. (2010).

We also compare our results to previous measurements of 3-methylglutaric acid (a structural isomer of 2-mGA that is expected to have a similar $p^{\circ,L}$). Our measurements of 2-mGA are in very good agreement with the $p^{\circ,L}(T^\ominus)$ for 3-methylglutaric acid reported by Booth et al. (2010) and by Mønster et al. (2004). As in Sect. 4.1, we assume that the measurements of Mønster et al. (2004) represent the liquid state. Once again, measurements of 2-mGA were made under very dry (RH < 3 %) conditions and no crystallization of the particle was observed.

### 4.4 Tartaric acid

Two measurements of DL-tartaric Acid (TA) $p^{\circ,L}$ are shown in Fig. 6. Measurement times were 2 days (312 K) and 11 days (305.5 K), not including instrument settling time. As only one point was distinguishable from zero, a fit to determine $H_{vap}^{\ominus}$ is not possible, so we extrapolate to $T^{\ominus}$ using Eq. (5) and two values of $H_{vap}^{\ominus}$, which should cover the range of possibilities: 75 and 250 kJ mol$^{-1}$ (cf., Fig. 2 of Compernolle et al., 2011). Using $H_{vap}^{\ominus} = 75$ kJ mol$^{-1}$, $p^{\circ,L}$ is calculated to be in the range $(8.6–24) \times 10^{-8}$ Pa, while $H_{vap}^{\ominus} = 250$ kJ mol$^{-1}$ yields a $p^{\circ,L}$ of $(1.8–4.9) \times 10^{-8}$ Pa. This result is approximately six orders of magnitude lower than the measurement of Booth et al. (2010). We note that tartaric acid has several stereoisomers and can be purchased as D-, L-, DL-, and meso-tartaric acid. The measurement of Booth et al. (2010) was also performed on the DL-stereoisomer (A. M. Booth, personal communication, 2013), so the results of this study should be strictly comparable to

the results of Booth et al. (2010) for tartaric acid. However, comparison to measurements of other stereoisomers are also reasonable, as all are expected to have a similar vapor pressure and the six order of magnitude discrepancy lies outside the expected range of variance due to stereoisomerism.

### 4.5 Citric acid

The $p^{\circ,L}$ measured for CA, shown in Fig. 7, were both indistinguishable from zero. Measurement times were 4 days (∼311 K) and ∼12 days (∼308 K), not including instrument settling time. The measurement at 311 K, < $1.6 \times 10^{-7}$ Pa, is a crude upper bound that is also valid at $T^{\ominus}$. However, following the logic employed for TA, we extrapolate from this point to $T^{\ominus}$, again using $H_{vap}^{\ominus}$ of 75 and 250 kJ mol$^{-1}$. The two upper limits from this extrapolation are < $4.0 \times 10^{-8}$ Pa for 75 kJ mol$^{-1}$ and < $1.4 \times 10^{-9}$ Pa for 250 kJ mol$^{-1}$. All three of these upper limits are at least four orders of magnitude below the value reported by Booth et al. (2010).

We also compare our measurement with measurements made above the melting point of CA ($T > 426$ K, Yaws et al., 2009). Using Eq. (5), $H_{vap} = 146$ kJ mol$^{-1}$ was extracted by fitting the lowest 25 K of the parameterization. Assuming a 10 % error on this $H_{vap}$ and extrapolating from the lower point of validity in the parameterization ($T = 426$ K, $p = 0.34$ Pa), we calculate $p^{\circ,L}$ at $T^{\ominus}$ is in the range $(1–40) \times 10^{-9}$ Pa, consistent with our upper limits.
4.6 Comparison to empirical models of vapor pressure

The EVAPORATION model described in Compernolle et al. (2011) was run both with and without the empirical correction term (Eq. 31 of Compernolle et al., 2011) to \( p^\circ \) for functionalized polyacids. For 2-mMA and 2-mGA, the correction terms do not apply and both model outputs are identical. The model has a mean absolute deviation of 0.4 orders of magnitude for polyacids (Compernolle et al., 2011), which we take as the uncertainty in model output. The results of these calculations are displayed in Fig. 2, along with the outputs of two other frequently-used vapor pressure estimation methods (Nannoolal et al., 2008; Moller et al., 2008) for comparison, both of which were calculated using the same estimated normal boiling points \( T_b \) (at a total pressure of 101.325 kPa) (Nannoolal et al., 2004) as inputs.

In the following analysis, we will focus on comparison to the EVAPORATION model as this model includes the empirical correction for substituted polyacids. The measurements of 2-mMA presented here are around a factor of two below the lower bound of model output, while 2-mGA is within the bounds of EVAPORATION model output. We view these agreements as reasonable, if not entirely satisfactory. In contrast, the substituted polyacids 2-hMA, TA, and CA have measured \( p^\circ \) that are a factor of \( \sim 500 \) (2-hMA), three orders of magnitude (TA) and at least three orders of magnitude (CA) lower than the lower bound of the EVAPORATION model output, which includes the empirical correction term. Predictions from the EVAPORATION model without the empirical correction are consistent with (TA, CA) or only one order of magnitude higher than (2-hMA) the EDB-derived \( p^\circ \). Altogether, these measurements are more consistent with the EVAPORATION model output that does not use the empirical correction term for substituted polyacids.

4.7 Comparison to solid-state results

The disagreement between \( p^\circ (T^\circ) \) for the compounds studied here and previous measurements is currently unexplained. As discussed in Soonsin et al. (2010), one possibility is that the physical state in other measurements was not fully controlled. This error would occur if some amorphous material was present in the KEMS apparatus of Booth et al. (2010), at which point the measurement reported as “solid” \( (p^S (T^\circ)) \) might actually reflect the vapor pressure of amorphous liquid, namely \( p^\circ (T^\circ) \). The hypothesis can be tested by comparing \( p^\circ (T^\circ) \) and \( p^S (T^\circ) \) from different measurement techniques.

Measurements of \( p^S \) for all compounds studied here are available, including direct measurement by KEMS (Booth et al., 2010), extrapolation from \( T \approx 340 \) K using Knudsen mass-loss effusion (Ribeiro da Silva et al., 2000; Ribeiro da Silva et al., 2001), and extrapolation from 411 K < \( T < 440 \) K using a simultaneous torsion and mass-loss effusion technique (de Wit et al., 1983). These measurements are summarized in Table 4 and graphically depicted in Fig. 2. For 2-mMA and 2-mGA (which are in reasonable agreement with previous results), our \( p^\circ (T^\circ) \) is larger than previously reported \( p^S (T^\circ) \), as expected. A similar enhancement in \( p^\circ (T^\circ) \) over \( p^S (T^\circ) \) was calculated by Booth et al. (2010) for these two compounds, and the measurements of \( p^S (T^\circ) \) of Booth et al. (2010) are in agreement with the
measurements of Ribeiro da Silva et al. (2000) and Ribeiro da Silva et al. (2001). However, the $p^{o,S}(T^\circ)$ reported by Booth et al. (2010) for 2-hMA, CA, and TA are all at least one order of magnitude larger than the largest upper limit or value of $p^{o,L}(T^\circ)$ reported here. Thus, the physical state of the sample cannot be the only factor leading to the large differences between this work and previously reported values.

To the authors’ knowledge, the only measurements of $p^{o,S}(T^\circ)$ for CA and 2-hMA are provided by Booth et al. (2010). However, measurements of meso-tartaric acid (a stereoisomer of tartaric acid that is expected to have similar physical properties to DL-tartaric acid) were made by de Wit et al. (1983) in the range 411 K $<$ $T$ $<$ 440 K. Using the reported $\Delta H_{sub}$ of 156.9 kJ mol$^{-1}$ in de Wit et al. (1983) and assuming 2% error on that value, extrapolation to $T$ = 298.15 K using Eq. (5) yields $p^{o,S} = (1.3-2.6) \times 10^{-9}$ Pa at 298.15 K. This value is around 5 orders of magnitude smaller than the reported $p^{o,S}(T^\circ)$ for TA in Booth et al. (2010) and is consistent with (i.e., less than or equal to) the extrapolated $p^{o,L}(T^\circ)$ of Yaws et al. (2009).

5 Implications

5.1 Partitioning of atmospheric aerosols

The propensity of organic material to re-enter the gas phase after condensation to an aerosol is postulated to be a crucial control on further chemical processing (e.g., Salo et al., 2011). However, at some point a substance that has sufficiently low $p^{o,L}$ is expected to remain in the condensed phase during the residence time of the particle in the atmosphere. Donahue et al. (2011) suggests that compounds with a $p^{o,L}$ of $\sim 1.3 \times 10^{-6}$ Pa or lower will be “almost completely condensed under typical ambient conditions”. The measurements of $p^{o,L}(T^\circ)$ for 2-hMA, CA and TA presented here are near or below this value, while other published values for the same compounds (see Table 4) are above the cutoff by a few orders of magnitude. Thus, the accurate determination of the $p^{o,L}$ of these compounds will influence not only estimations of their partitioning between the gas and condensed phase, but also the mechanism by which they are further oxidized. This conclusion is not limited to 2-hMA, CA, and TA, but extends to all compounds that may have a $p^{o,L}$ which is significantly over-estimated by current vapor pressure calculation techniques.

5.2 Evaporation rates in laboratory measurements

The time needed for a single-component particle to evaporatively shrink to $\frac{1}{\epsilon}$ of its original radius is

$$\Delta t = \left(1 - \frac{1}{\epsilon^2}\right) \times \frac{(r(t_0))^2 \rho RT}{2D_v p^o M},$$

where $\Delta t$ is the elapsed time, and other symbols are defined as above (Davis and Ray, 1977). Using the $D_v$ given in Table 3, the e-folding evaporation times for a 10 $\mu$m radius particle of pure TA at $T^\circ$ is 8.3 min for $p^{o,L} = 0.31$ Pa (Booth et al., 2010) and $\sim 15$ yr for $p^{o,L} = 3.2 \times 10^{-7}$ Pa (this work) (details and calculation given in Appendix D). Similarly for CA, the e-folding evaporation time would be 10.9 h for $p^{o,L} = 3.1 \times 10^{-3}$ Pa (Booth et al., 2010) and $\sim 23$ yr for $p^{o,L} = 1.6 \times 10^{-7}$ Pa (this work). Thus, the fast evaporation times associated with the measurements of Booth et al. (2010) are not compatible with these EDB observations, which did not show any discernible evaporation of CA for several days even at $\sim 310$K.

For particles of radius 100 nm (similar to those used in TDMA experiments), the e-folding evaporation times would be four orders of magnitude smaller, roughly 50 ms and 14 h for the two $p^{o,L}$ for TA given above. Such a large difference should be easy to observe in a TDMA and we suggest that measurements of these and other compounds on such an instrument could be used to corroborate our results.

6 Conclusions

Measurements of the pure component liquid vapor pressure ($p^{o,L}$) of several substituted polycarboxylic acids were made by tracking the decreasing size of an evaporating particle in an EDB. As the measurements in the current study were taken on a solution already in the liquid state or on the pure subcooled melt, they preclude the possibility of error introduced via the conversion from solid-state to liquid-state vapor pressure.

Our measurements $p^{o,L}(T^\circ)$ agree reasonably well with previous measurements of 2-methylmalonic and 2-methylglutaric acids, and with an extrapolation of measurements taken above the melting point of citric acid ($T > 426$ K), but are at least a factor of 500 lower than the only other measurements of 2-hydroxymalonic, tartaric, and citric acids performed near room temperature by Booth et al. (2010). The discrepancy between our measurements and previous studies may be partially explained by the presence of liquid or amorphous semi-solid inclusions in a bulk sample that was assumed to be crystalline, but the disagreement among the vapor pressures of some of the polycarboxylic acids is so large that there is no obvious solution that brings these EDB measurements and the KEMS measurements of Booth et al. (2010) into agreement.

The substantial disagreement between these two techniques shows that measurements of the vapor pressure of substituted polycarboxylic acids should be revisited. The agreement for the methyl-substituted polycarboxylic 2-mMA and 2-hMA shows that these two techniques can provide consistent results. Indeed, the measurements of unsubstituted oxalic, succinic, and glutaric acids made by Soonsin et al. (2010) using this same EDB apparatus and technique are all consistent with the $p^{o,L}(T^\circ)$ reported by Booth et al. (2010) for those compounds.
The measurements presented here are more consistent with the EVAPORATION model which excludes the empirical correction of polyacids. Perhaps coincidentally, the methyl-substituted polyacids for which agreement with other methods was found did not require an empirical correction term in the EVAPORATION model, while 2-hMA, CA and TA did. Altogether, these data suggest that the discrepancy between the EDB and KEMS technique (and by extension, the EVAPORATION model, which includes the empirical polyacid correction) arises in polyacids with oxygen-bearing (or at least non-aliphatic) substituent groups. This suggests very strongly that for the time being, the EVAPORATION model should be used without the empirical correction for substituted polyacids.

Appendix A

Examples of radius data

Examples of the raw radius data as a function of time for 2-mGA, TA, and CA are shown in Fig. A1. Each experimental trace starts after the particle is equilibrated with respect to RH and T, and shows a very small but discernible shrinking of the particle over the course of many days. These signals correspond to vapor pressures of (a) $1.1 \times 10^{-6}$ Pa, (b) $3.6 \times 10^{-7}$ Pa, and (c) $1.6 \times 10^{-7}$ Pa. Measurements of 2-mMA, Fig. A1a, were easily above limit of quantitation, as evidenced by the observable evaporation even at reduced temperature. The measurement of TA, Fig. A1b, is approaching the limit of quantitation, as instrumental noise is visibly overlaid with evaporative shrinking. Finally, measurements of CA, Fig. A1c, are below limit of quantitation. The ~10 day experiment shown here shows a quasi-exponential profile that is typical of, e.g., the loss of residual water from the particle and not of slow evaporative loss of CA. In this case, the assumption that the particle is in equilibrium with its surroundings (i.e., that $a_{w} = \text{RH}$) is violated. The error analysis procedure described in Appendix B correctly yields a vapor pressure indistinguishable from zero without any manual intervention. However, we can still place an upper limit on the vapor pressure of CA by observing that its evaporation is small enough to be masked by these very small shrinking rates due to evaporation of traces of water (2 nm in 7 days).

Appendix B

Error analysis

B1 Statistical error

Standard error propagation was used to calculate the statistical error in $p_{\text{EVAP}}(T, \text{RH})$ derived from experiments at multiple $T$ and RH. In general, the statistical error on a measurement depends on the duration of the measurement, the RH of the measurement, and the steepness of the hygroscopic growth factor that is unique to each compound. For LVOC, the calculated error is dominated by the particle response to slight changes in RH, while experimental uncertainties for materials with higher $p_{\text{EVAP}}^\text{d}$ depend primarily on the accuracy of the retrieval of the absolute radius.

The assumed statistical errors in the variables of Eq. (1) are estimated as follows:

- Radius, the larger of (i) 10 %, based on the retrieval of $r(t_0)$ from the angular scattering pattern, or (ii) the error due to variations in $r$ due to small changes in RH (cf., Sect. B2).
- Mole fraction, 2 %, based on the variation of AIOM-FAC outputs with respect to the temperature range of the measurements and response of $x$ to small changes in RH.
- Density, 5 %, a conservative estimate due to the extrapolation from bulk measurements.
- Temperature, 0.25 K, the maximum allowed variation in temperature over one experimental measurement
- Diffusivity of vapor, 20 %, following the suggested value of Krieger et al. (2012).

B2 Error arising from response of particles to changes in RH

In addition to the standard statistical uncertainty expected in a measurement, a potential error exists due to the response...
of the particle to fluctuations in RH. In this case, the measurement of Mie resonance wavelength (and thus the change in particle radius) is highly accurate but the assumption that evaporation is the only process causing the particle to change size (at constant $T$ and RH within instrumental stability) may be incorrect, leading to a confounding error in $\frac{dr}{dT}$. Thus, while our ability to measure $\frac{dr}{dT}$ is excellent, the error in $\frac{dr}{dT}$ was increased for the purpose of error propagation as follows. The measurement technique described here assumes that the change in particle size is only due to evaporation of organic molecules and an associated amount of water molecules, i.e., that the particle is equilibrated with its environment in $T$ and especially with respect to water vapor. Thus, a particle shrinking due to decreasing RH might be interpreted to have high $p$, while a particle growing due to increasing RH might display an artificially slow decrease in radius. Fits to data were made such that measured $\Delta RH < 0.5 \%$ and $\Delta T < 0.25 \text{K}$ over the course of the measurement. We estimate that the ability of our RH sensor to detect drifts in measured RH is at worst 0.5 %, meaning that a drift of 0.5 % actual RH could occur without registering a trend in measured RH.

Calculation of the false signal resulting from these small variations in RH requires a knowledge of the response of the particle to changes in RH, which is highly non-linear. Above 100 % RH, the particle grows without bound, and at high RH the particle is extremely sensitive to small variations in RH, while under low RH conditions the growth is relatively small. For this analysis, the AIOMFAC model results were inverted to produce a growth factor:

$$GF = \frac{V_{org} + (\frac{1}{x} - 1) \times V_w}{V_{org}}. \quad (B1)$$

The growth factor $GF$ is normalized to be unity at $x = 1$ (pure organic component) and is generated by assuming that the number of moles of organic compound are conserved during hygroscopic growth and that partial molar volumes are additive. Each measurement occurs at a specific RH, which defines a range of growth factors depending on the steepness of $GF$ at that point. The error is then derived by assuming a totally non-volatile particle and calculating the largest possible positive and negative changes in radius from the starting RH plus or minus the tolerance of 0.5 % RH. For substances with higher vapor pressures such as 2-mmA, this error plays a minor role in the calculation of the total statistical error, while for very short experiments (small $dr$) or very low $p$ measurements (small true $dr$), this term becomes dominant.

**B3 Systematic errors**

As the $p$ calculated in Eq. (1) depends on the square of the absolute particle radius, a systematic error is possible due to error in the determination of $r(t_0)$. This error would be apparent only when comparing several particles of the same material, as each particle is self-consistent with respect to initial radius. Such an error would appear as a set of data from one particle that is increased or decreased in $p/(T)$ by a constant factor. Based on the six particles shown in Fig. 5, we do not observe any systematic shifting of the data from one particle away from the others. Thus, the systematic error in the determination of $r(t_0)$ is smaller than the statistical error and can be neglected.

Another systematic error that is very difficult to evaluate arises from the gas-phase diffusivity ($D_v$) of the organic compound (see discussion in Krieger et al., 2012). The $p$ in Eq. (1) is inversely proportional to gas-phase organic diffusivity, which is calculated based on two estimated parameters (as detailed in Sect. 2.4). Unlike the potential error in $r(t_0)$, we have no ability to isolate the influence of systematic error in $D_v$ as all experiments with the same material used the same parameterization. In a future comparison to these results, the influence of any systematic error in $D_v$ can be minimized by taking into account the actual values that were used (given in Table 3).

**Appendix C**

**Miscellaneous effects**

Here we present a justification for neglecting the influence of the Kelvin effect and the reduction in vapor pressure of polarizable species in a charged droplet, and for neglecting the influence of dimerization on the gas-phase diffusivity of the organic component.

**C1 Influence of droplet size and charge**

The Kelvin effect, the enhancement of vapor pressure over a curved surface, is well known and must be considered as part of aerosol growth or evaporation in small particles. In addition to the Kelvin effect, recent work by Nielsen et al. (2011) showed that the near-surface partial pressure of water vapor or other gasses with a permanent dipole or high polarizability is increased above a charged particle. Using the formalism of Lapshin et al. (2002), Eq. (11) expressed in SI units is

$$\ln \frac{p}{p_0} = \frac{2\sigma v}{kT} - \frac{\mu_D Q}{4\pi \epsilon_0 kTr^2} \times L \left( \frac{\mu_D Q}{4\pi \epsilon_0 kTr^2} \right) - \frac{vQ^2}{32\pi^2 \epsilon_0 kTr^4} \left( 1 - \frac{1}{\epsilon_L} \right), \quad (C1)$$

where $L$ is the Langevin function $L(x) = \coth(x) - 1/x$ and all symbols are defined as in Lapshin et al. (2002) except radius $r$, which has been changed from $R$ to avoid confusion with the gas constant. Using the values in Table C1, the value of $p/p_0$ was calculated as 1.0004, a predicted enhancement of 0.04 % in the vapor pressure. Thus, the combined Kelvin effect and charge stabilization effect are minor compared to...
C2 Dimerization of gas-phase organics

An additional consideration in estimating the organic vapor-phase diffusivity in these materials is the possibility of carboxylic acid dimer formation. Dimerization of carboxylic acids is well known, especially in the case of smaller molecules such as, e.g., formic acid; dicarboxylic acid dimers have been studied in the context of new particle nucleation (see, e.g., Hallquist et al., 2009, and references therein). Substantial dimerization would result in reduced gas-phase diffusivity and would influence the apparent vapor pressure of the organic (and the monomer) vapor pressure. However, dimerization of the vapor is unlikely to influence the measurements due to the low gas-phase concentration of the organic component in the experimental apparatus. For a droplet in thermodynamic equilibrium, the vapor pressure specifies the partial pressure of that material in the vapor phase in the diffusion-limited region nearest the droplet. Thus, the mixing ratio of organic vapor (partial pressure of order 1 × 10^-3 Pa or less) in an atmosphere of ~ 80 × 10^3 Pa continuously flowing organic-free N\(_2\) would be of order 1 × 10^-8 or lower. Assuming that di- and mono-carboxylic acids have similar dimerization properties (the dissociation constants for monocarboxylic acids in the gas phase are large, e.g., formic acid, 3.6 × 10^2 Pa at 296 K, Vander Auwera et al., 2007), that the effect of chain length on enthalpy of dimerization is minimal (cf., Eq. 7 of Tsonopoulos and Prausnitz, 1970) and solving the quadratic equation as described in, e.g., Zuend et al. (2011), the fraction of molecules dimerized would be ~ 1 per 1 × 10^6 for a sample with \( p^0 T^{5} \approx 1 \times 10^{-6} \) Pa. Even at the highest vapor pressures observed in this study of ~ 1 × 10^{-3} Pa, less than 1 molecule in 1 × 10^5 is predicted to be dimerized. Thus, dimerization is unlikely to play a major role in these experiments.

### Appendix D

**Evaporation times sample calculation**

Beginning with Davis and Ray (1977), Eq. (3), and substituting \( r \) for \( a \) to maintain consistency with our earlier nomenclature,

\[
r^2(t) = r^2(t_0) + S_{12} \times (t - t_0).
\]

Now let \( \Delta t \equiv (t - t_0) \) and let \( r(t) = \frac{1}{2} \times r(t_0) \) to find the e-folding evaporation time for a pure particle. Then

\[
\frac{1}{e^2} \Delta t^2 (t_0) = r^2(t_0) + S_{12} \times \Delta t
\]

\[
\left(1 - \frac{1}{e^2}\right) r^2(t_0) = -S_{12} \times \Delta t. \tag{D1}
\]

Now \( S_{12} \equiv \frac{2D_v p^0 M}{\rho RT} \) so that

\[
\Delta t = \left(1 - \frac{1}{e^2}\right) \frac{r^2(t_0) \rho RT}{2D_v p^0 M}. \tag{D2}
\]

Using the values in Table D1 for TA,

\[
\Delta t = \left(1 - \frac{1}{e^2}\right) \frac{1 \times 10^{-10} \text{m}^2 \times 1.749 \text{g cm}^{-3} \times 8.314 \text{J mol}^{-1} \text{K}^{-1} \times 298.15 \text{K}}{2 \times 0.08 \text{cm}^{2} \text{s}^{-1} \times 0.31 \text{Pa} \times 150.08 \text{g mol}^{-1}} = 5.04 \times 10^2 \text{s} = 8.4 \text{min}
\]

and ~ 15 yr for \( p^0 = 3.2 \times 10^{-7} \) Pa. For CA, using \( M = 192 \text{g mol}^{-1} \) and \( p^0 = 3.1 \times 10^{-3} \) Pa or 1.6 × 10^{-7} Pa, we calculate 10.9 h and ~ 23 yr, respectively. Due to the squared dependence on initial particle radius, changing from 10 \( \mu \)m to 100 nm radius particle results in a four order of magnitude decrease in e-folding time.

### Table C1.

<table>
<thead>
<tr>
<th>Variable</th>
<th>Description</th>
<th>Value</th>
<th>Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \sigma )</td>
<td>Surface tension</td>
<td>( 7.2 \times 10^{-2} )</td>
<td>Nm^{-1}</td>
</tr>
<tr>
<td>( v )</td>
<td>Molecular volume</td>
<td>( 2.99 \times 10^{-29} )</td>
<td>m³ molecules^{-1}</td>
</tr>
<tr>
<td>( \epsilon_0 )</td>
<td>Vacuum permittivity</td>
<td>( 8.85 \times 10^{-12} )</td>
<td>m(^{-3}) kg(^{-1}) s(^{4}) A(^{2})</td>
</tr>
<tr>
<td>( k )</td>
<td>Boltzmann constant</td>
<td>( 1.38 \times 10^{-23} )</td>
<td>JK^{-1}</td>
</tr>
<tr>
<td>( T )</td>
<td>Temperature</td>
<td>298</td>
<td>K</td>
</tr>
<tr>
<td>( r )</td>
<td>Particle radius</td>
<td>( 2.5 \times 10^{-6} )</td>
<td>m</td>
</tr>
<tr>
<td>( \mu_D )</td>
<td>Dipole moment</td>
<td>( 5.99 \times 10^{-30} )</td>
<td>Cm</td>
</tr>
<tr>
<td>( Q )</td>
<td>Charge</td>
<td>( 1.6 \times 10^{-15} )</td>
<td>C</td>
</tr>
<tr>
<td>( \epsilon_s )</td>
<td>Static relative permittivity</td>
<td>80</td>
<td>unitless</td>
</tr>
</tbody>
</table>

### Table D1.

<table>
<thead>
<tr>
<th>Variable</th>
<th>Description</th>
<th>Value</th>
<th>Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>( r(t_0) )</td>
<td>Initial particle radius</td>
<td>( 1 \times 10^{-5} )</td>
<td>m</td>
</tr>
<tr>
<td>( \rho )</td>
<td>Density</td>
<td>1.749</td>
<td>g cm^{-3}</td>
</tr>
<tr>
<td>( R )</td>
<td>Gas constant</td>
<td>8.314</td>
<td>J mol^{-1} K^{-1}</td>
</tr>
<tr>
<td>( T )</td>
<td>Temperature</td>
<td>298.15</td>
<td>K</td>
</tr>
<tr>
<td>( D_v )</td>
<td>Gas phase diffusivity of organic</td>
<td>0.08</td>
<td>cm² s^{-1}</td>
</tr>
<tr>
<td>( p^0 )</td>
<td>Vapor pressure</td>
<td>0.31</td>
<td>Pa</td>
</tr>
<tr>
<td>( M )</td>
<td>Molar mass</td>
<td>150.08</td>
<td>g mol^{-1}</td>
</tr>
</tbody>
</table>
## Acknowledgements
This material is based upon work supported by the United States National Science Foundation under award no. IRFP 1006117, by ETH Zürich, and by the Competence Center Environment and Sustainability of the ETH Domain (CCES) project IMBALANCE and OPTIWARES. Any opinions, findings, and conclusions or recommendations expressed in this material are those of the authors and do not necessarily reflect the views of the US National Science Foundation. Figure 2 was produced using the bar2.m code written by Mike Sheppard of the MIT Lincoln Laboratory. The authors thank Daniel Lienhard of ETH Zürich for performing measurements of the density of 2-methylglutaric acid.

Edited by: M. Petters

## References

### Table E1. List of symbols and abbreviations.

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Meaning</th>
<th>SI Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>ΔH_vap</td>
<td>Enthalpy of vaporization at T ⊖</td>
<td>kJ mol⁻¹</td>
</tr>
<tr>
<td>λ</td>
<td>Peak wavelength of a Mie resonance</td>
<td>m</td>
</tr>
<tr>
<td>ρ</td>
<td>Density</td>
<td>kg m⁻³</td>
</tr>
<tr>
<td>a</td>
<td>Activity coefficient</td>
<td>–</td>
</tr>
<tr>
<td>L/SVOC</td>
<td>Low- and semi-volatile organic compound</td>
<td>–</td>
</tr>
<tr>
<td>D_vap</td>
<td>Vapor phase diffusivity</td>
<td>m² s⁻¹</td>
</tr>
<tr>
<td>GF</td>
<td>(radius) growth factor</td>
<td>–</td>
</tr>
<tr>
<td>EDB</td>
<td>Electrodynamic balance</td>
<td>–</td>
</tr>
<tr>
<td>KEMS</td>
<td>Knudsen effusion mass spectrometry</td>
<td>–</td>
</tr>
<tr>
<td>M</td>
<td>Molar mass</td>
<td>kg mol⁻¹</td>
</tr>
<tr>
<td>p</td>
<td>Vapor pressure</td>
<td>Pa</td>
</tr>
<tr>
<td>p_L</td>
<td>p of liquid state sample</td>
<td>Pa</td>
</tr>
<tr>
<td>p_°</td>
<td>Pure component vapor pressure in unspecified physical state</td>
<td>Pa</td>
</tr>
<tr>
<td>p_°(T ⊖)</td>
<td>p_° at T ⊖</td>
<td>Pa</td>
</tr>
<tr>
<td>p_L°</td>
<td>p_° of liquid state sample</td>
<td>Pa</td>
</tr>
<tr>
<td>p_S°</td>
<td>p_° of solid state sample</td>
<td>Pa</td>
</tr>
<tr>
<td>r</td>
<td>Particle radius</td>
<td>m</td>
</tr>
<tr>
<td>RH</td>
<td>Relative humidity</td>
<td>–</td>
</tr>
<tr>
<td>T</td>
<td>Temperature</td>
<td>K</td>
</tr>
<tr>
<td>T ⊖</td>
<td>Reference temperature, here 298.15 K</td>
<td>K</td>
</tr>
<tr>
<td>TDMA</td>
<td>Tandem differential mobility analyzer</td>
<td>–</td>
</tr>
<tr>
<td>V</td>
<td>Molar volume</td>
<td>m³ mol⁻¹</td>
</tr>
<tr>
<td>x</td>
<td>Mole fraction of the organic component</td>
<td>–</td>
</tr>
</tbody>
</table>


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