Radio Transients from the Accretion Induced Collapse of White Dwarfs

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Abstract

It has long been expected that in some scenarios when a white dwarf (WD) grows to the Chandrasekhar limit, it can undergo an accretion induced collapse (AIC) to form a rapidly rotating neutron star. Nevertheless, the detection of such events has so far evaded discovery, likely because the optical, supernova-like emission is expected to be dim and short-lived. Here we propose a novel signature of AIC: a transient radio source lasting for a few months. Rapid rotation along with flux freezing and dynamo action can grow the WD’s magnetic field to magnetar strengths during collapse. The spindown of this newly born magnetar generates a pulsar wind nebula (PWN) within the $\sim 10^{-3} - 10^{-1} M_\odot$ of ejecta surrounding it. Our calculations show that synchrotron emission from the PWN may be detectable in the radio, even if the magnetar has a rather modest magnetic field of $\sim 2 \times 10^{14}$ G and an initial spin period of $\sim 10$ ms. An all-sky survey with a detection limit of 1 mJy at 1.4 GHz would see $\sim 4 (f/10^{-2})$ above threshold at any given time, where $f$ is the ratio of the AIC rate to Type Ia supernova rate. A similar scenario may result from binary neutron stars if some mergers produce massive neutron stars rather than black holes. We conclude with a discussion of the detectability of these types of radio sources in an era of facilities with high mapping speeds.

Subject headings: stars: magnetic fields — stars: neutron — stars: winds, outflows — white dwarfs

1. Introduction

As an accreting white dwarf (WD) grows toward the Chandrasekhar limit, a well-known potential outcome is ignition of its nuclear fuel, leading to a Type Ia supernova (SN Ia). Hillebrandt & Niemeyer (2000). However in some cases (e.g. mass transfer onto O/Ne/Mg WDs and C/O WD mergers: Canal & Schatzman 1976; Nomoto & Kondo 1991) electron capture can rob the core of its degeneracy pressure support leading to formation of a neutron star (NS). This “Accretion Induced Collapse” (AIC) has been invoked to explain millisecond pulsars (e.g. Usov 1992). As an accreting white dwarf grows toward the Chandrasekhar limit, a well-known potential outcome is ignition of its nuclear fuel, leading to a Type Ia supernova (SN Ia, Hillebrandt & Niemeyer 2000). However in some cases (e.g. mass transfer onto O/Ne/Mg WDs and C/O WD mergers: Canal & Schatzman 1976; Nomoto & Kondo 1991) electron capture can rob the core of its degeneracy pressure support leading to formation of a neutron star (NS). This “Accretion Induced Collapse” (AIC) has been invoked to explain millisecond pulsars (e.g. Battacharya & van den Heuvel 1991), subsets of gamma-ray bursts (e.g. Dar et al. 1992; Metzger et al. 2008b), magnetars (e.g. Usov 1992), and may be a source of r-process nucleosynthesis (Hartmann et al. 1985; Fryer et al. 1999).

Despite its potential importance, there has been no reported detection of an AIC event. To start with, the expected AIC rate is no more than $\approx 1$% of that of SNe Ia (Yungelson & Livio 1998). Next, relative to Type I and Type II SNe, the ejecta mass is expected to be small ($\lesssim 10^{-1} M_\odot$), produce little $^{56}$Ni ($\lesssim 10^{-2} M_\odot$), and move at high velocity ($\approx 0.1 c$). The resulting optical transient is thus considerably fainter than a typical SN (5 magnitudes or more) and lasts $\approx 1$ day (Metzger et al. 2009b; Darbha et al. 2010).

Rapid rotation should accompany AIC due to the accretion of mass and angular momentum. Furthermore, a strong magnetic field may be amplified through flux freezing during collapse and via dynamo action (Duncan & Thompson 1992). Therefore a plausible outcome of AIC is creation of a quickly spinning magnetar (Usov 1992; King et al. 2001; Levan et al. 2006). The WD collapse unbinds material (Dessart et al. 2006), and the remnant disk loses mass via outflows driven by neutrino heating, turbulent viscosity, and recombination of free nuclei into helium (Lee & Ramirez-Ruiz 2007; Metzger et al. 2008a, 2009a; Lee et al. 2009). This leads to $M_{ej} \approx 10^{-3} - 10^{-1} M_\odot$ of ejecta with velocity $v_{ej} \approx 0.1 c$. Such a configuration will also follow a double NS merger if the total binary mass is below the maximum NS mass.

Following the implosion of the WD and subsequent disk outflows, the ejecta expands with velocity $v_{ej} \approx 0.1 c$ and kinetic energy $E_{ej} \approx M_{ej} v_{ej}^2 / 2 \approx 10^{50}$ erg. This plows into the ISM with particle density $n_0$, which can vary greatly from $10^{-6}$ cm$^{-3}$ for events outside of their host galaxy to $\sim 1$ cm$^{-3}$ in denser environments. Once the ejecta has swept up a mass comparable to its own, it decelerate as it enters the Sedov-Taylor phase on a timescale (McKee & Truelove 1995)

$$\tau_{ST} = 0.5 E_{ej}^{-1/2} M_{ej}^{-4/6} (m_p n_0)^{-1/3} \approx 16 E_{50}^{-1/2} M_{-2}^{-5/6} n_0^{-1/2} \text{ yr},$$

where $E_{50} = E_{ej} / 10^{50}$ erg and $M_{-2} = M_{ej} / 10^{-2} M_\odot$. Since $\tau_{ST}$ is much longer than the times of interest (especially when $n_0$ is small), the ejecta is always in an ejecta-dominated (or free-expansion) phase. In this case the ejecta maintains constant velocity with radius $R_{ej} \approx v_{ej} t$. The forward shock is merely a distance $\approx (4/3)^{1/3} R_{ej}$ ahead of $R_{ej}$, and the reverse shock has barely developed behind it. The pressure behind the forward shock and down to the reverse shock is roughly constant and given by the strong shock limit $\approx (4/3) m_p n_0 v_{ej}^2$. The magnetar injects energy in the form of magnetic fields and relativistic particles at a rate

$$L(t) = L_0 / (1 + t / \tau)^P.$$
Here we assume dipole spin-down\(^1\) and thus \( p = 2 \). For a magnetic moment \( \mu \), initial spin frequency \( \Omega_0 = 2\pi / P_0 \), and moment of inertia \( I = 0.35 M_R R_0^2 \) (Lattimer & Prakash 2001),

\[
L_0 = \mu^2 \Omega_0^4 / 6 c^3 = 1.2 \times 10^{47} \mu_3^2 P_3^4 \text{erg s}^{-1},
\]

and

\[
\tau = 6 c^3 / \mu_3^2 \Omega_0^2 = 4.8 \times 10^4 \mu_3^2 P_3^2 \text{s},
\]

where \( \mu_3 = \mu / 10^{33} \) G cm\(^3\), \( P_3 = P_0 / 3 \) ms, and we use \( M_\ast = 1.4 M_\odot \) and \( R_\ast = 12 \) km.

The energy input from the magnetar powers a PWN with radius \( R_p \). Deeper inside, a wind termination shock forms at radius \( R_t \), where the ram pressure of the pulsar wind equals the PWN pressure \( P \) (Gaensler & Slane 2006).

\[
R_t \approx (L / 4 \pi c P)^{1/2},
\]

where \( R_t \ll R_p \). The general picture developed from galactic PWNes is that particles are accelerated at or near \( R_t \). This seeds the PWN with relativistic electrons out to \( R_p \).

A central issue is the content of the PWN. As a pulsar wind flows from the light cylinder, it is inferred to have a large magnetization \((\sigma \sim 10^5 \) G cm\(^3\))

\[
\text{where } \sigma = \text{the ratio of Poynting flux to particle energy flux; } \text{Arons 2002.}
\]

However multiple lines of evidence, including the expansion velocities and high-energy modeling of PWNe, require that the magnetization decreases significantly \((\sigma \ll 1)\) by the time the wind reaches \( R_t \). In the region where the radiation arises, \( R_t < r < R_p \), we define \( \eta_e \) and \( \eta_B \) as the fraction of the magnetar luminosity that goes into electrons and magnetic fields, respectively, with typical values of \( \eta_e \approx 0.999 \) and \( \eta_B \approx 10^{-3} \).

Following Reynolds & Chevalier (1984) we assume the energy density of electrons and magnetic fields evolve independently and obey a relativistic equation of state. Thus

\[
\frac{d}{dt} (4\pi P_R R_p^2) = (\eta_B L - \Lambda) R_p,
\]

where \( \Lambda \) is the radiative loss rate, and

\[
\frac{d}{dt} (4\pi P_B R_p^2) = \eta_B L R_p,
\]

where \( P_B = B^2 / 8 \pi \). Note that in the adiabatic limit \( \eta_B L \approx 0 \), this predicts \( P_B \propto R_p^4 \) and \( B \propto R_p^{\frac{3}{2}} \), as expected from flux freezing. Momentum conservation is given by

\[
M_t \frac{d^2 R_p}{dt^2} = 4\pi R_p^2 \left[ P - \rho_{\text{ej}} \left( v_p - \frac{R_p}{t} \right)^2 \right],
\]

where \( v_p = dR_p / dt \) and \( P = P_e + P_B \) is the total pressure.

The PWN sweeps up ejecta and creates a shell with mass

\[
M_t = \left\{ \begin{array}{ll}
M_{\text{ej}} (P_p / \sigma_{\text{eff}})^3 & \text{if } R_p < v_{\text{ej}} t \\
M_{\text{ej}}, & \text{if } R_p \geq v_{\text{ej}} t
\end{array} \right.
\]

Once \( R_p \approx v_{\text{ej}} t \), the PWN reaches material that has been shock-heated by its interaction with the ISM. Since we generally find \( P \gg (4/3)\mu m_0 v_{\text{ej}}^2 \), we do not expect the shock-heated pressure to have a large dynamical effect on the PWN. This is in contrast to PWNe growing within a SN remnant, where the large pressure behind the reverse shock (on a timescale \( t \gg \tau_{ST} \)) can cause significant compression and magnetic field amplification (Reynolds & Chevalier 1984).

Equations (6), (7), and (8) with \( dR_p / dt = v_p \) provide four first-order differential equations for the four dependent variables \( P_e, P_B, R_p, \) and \( v_p \), respectively. For simplicity, we calculate the PWN evolution using \( \Lambda \approx 0 \), so that equations (6) and (7) are combined using \( P = P_e + P_B \) and \( \eta_e + \eta_B = 1 \). When \( L \) is constant, the analytic result is (Chevalier 1977)

\[
R_p \approx 1.3 \times 10^{16} L_{47}^{1/5} E_{50}^{3/10} M_2^{-1/2} t_6^{6/5} \text{ cm},
\]

and

\[
B \approx 6\pi B_{15} L_{47}^{1/5} E_{50}^{9/20} M_2^{-3/4} t_6^{13/10} \text{ G},
\]

where \( L_{47} = L / 10^{47} \) erg s\(^{-1}\), \( t_6 = t / 10^6 \) s, and \( \eta_e - \eta_B \approx \eta_B / 3 \). This gives some idea of the rough values expected, although for our detailed calculations, \( R_p \) and \( B \) deviate slightly from these scalings when \( t \gtrsim \tau \).

Rayleigh-Taylor instabilities can act at \( R_p \) due to the low density PWN pushing up against high density ejecta. The growth time for a large density contrast is \( \tau_{RT} \approx (g_{\text{eff}} k^2)^{-1/2} \), where \( g_{\text{eff}} \) is the effective gravitational acceleration at the boundary and \( k \) the wavenumber. For \( R_p \) given by equation (10), \( g_{\text{eff}} \approx d^2 R_p / dt^2 \approx (6 / 25) R_p / t^2 \) and the growth rate for \( k \approx n / R_p \) is \( \tau_{RT} \approx (25 / 6 n t)^{1/2} / t \). For sufficiently small wavelengths \((large n)\), \( \tau_{RT} \lesssim t \) and instability results. This is not surprising since similar systems, like the Crab Nebula, have morphologies strongly impacted by instabilities. But for the current analysis we do not include this complication.

3. SYNCHROTRON RADIO EMISSION

A power-law spectrum of relativistic electrons \( n(E) \propto KE^{-\alpha} \) are accelerated near the termination shock at \( R_t \) and fill the PWN out to \( R_p \), where \( n(E) \) is in units of electrons erg\(^{-1}\) cm\(^{-3}\).

The power-law parameters within the PWN can change via cooling and injection of new electrons (e.g. Gelfand et al. 2009; Bucciantini et al. 2011). For the present work we estimate the synchrotron spectrum at any time by fixing \( P_e \) and \( P_B \) from our dynamical calculations.

Our discussion of synchrotron emission largely follows the work of Pacholczyk (1970). Synchrotron emission is self-absorbed below a frequency

\[
\nu_{\text{SA}} = 2 c_1 (R_p c_6)^{3 / (\nu + 4)} K^{2 / (\nu + 4)} (B \sin \theta)^{(\nu + 4) / (\nu + 4)},
\]

where \( c_1 = 6.27 \times 10^{38} \) in cgs units, \( c_6 \) depends on \( s \) and can be found in Appendix 2 of Pacholczyk (1970), and \( \theta \) is the pitch angle. Throughout we assume an average of \( \sin \theta = (2 / 3)^{1/2} \). In the optically thick limit the flux is

\[
F_{\nu} = \frac{\pi R_p^2 c_5 (B \sin \theta)^{-1 / 2}}{D^2 c_6} \left( \frac{\nu}{2 c_1} \right)^{5 / 2},
\]

where \( D \) is the distance and \( c_5 \) is another constant. In the optically thin limit,

\[
F_{\nu} = \frac{4 \pi R_p^2 c_5 K (B \sin \theta)^{(\nu + 1) / 2}}{3 D^2 c_6} \left( \frac{\nu}{2 c_1} \right)^{-(\nu - 1) / 2},
\]

which assumes an emission filling factor of order unity. We use a simple interpolation between these two limits for the total emission spectrum \( F_\nu \). The location of the spectrum’s peak at \( \nu_{\text{SA}} \propto B^{(\nu + 2) / (\nu + 4)} \) shifts to lower frequencies as \( B \) decreases during expansion (eq. (11)). The peak flux scales \( \propto B^{(\nu + 3) / (\nu + 4)} \), and thus also decreases with time.

\(^1\) When the magnetar is spinning \( P_0 \leq 3 \) ms and radically radiating neutrinos, this can give rise to a neutrino-driven, magneto-centrifugal wind (Thompson et al. 2004) which could greatly enhance the spindown.
The synchrotron cooling time scales as $E/|E| \propto \nu^{-1/2}$. Therefore there is a $\nu_c$ above which synchrotron cooling beats adiabatic expansion (Reynolds & Chevalier 1984)

$$\nu_c = \frac{c_1}{c_2 B^3 \sin^2 \theta} \left( \frac{v_p}{R_p} \right)^2,$$

where $c_2 = 2.37 \times 10^{-3}$ in cgs units. Electrons that evolve adiabatically maintain their spectrum, while electrons that cool from synchrotron emission steepen, therefore

$$n(E) = \begin{cases} KE^{-\gamma_e}, & E < E_c \\ KE_c E^{-(\gamma_e+1)}, & E \geq E_c \end{cases},$$

where $E_c$ is the energy of electrons emitting a frequency $\nu_c$. The prefactor $K$ is set by the total energy density of electrons $U_e \approx \frac{3}{2} P_0$, found by integrating

$$U_e = \int_{E_{\text{min}}}^{E_{\text{max}}} n(E) E dE,$$

where $E_{\text{min}}$ and $E_{\text{max}}$ are the minimum and maximum energies of electron spectrum, respectively. For $s \approx 1.5$ and the limit $E_{\text{max}} \gg E_c \gg E_{\text{min}}$, $U_e \approx 4 K E_c^{-2-\gamma_e}$. The energy density is roughly set by $E_c$ since the spectrum steepens for $E > E_c$.

We next consider potential free-free absorption. The absorption coefficient is (Rybicki & Lightman 1979)

$$\alpha_f \approx 1.9 \times 10^{-2} T^{-3/2} Z^2 n_e n_i \nu^{-2} \rho_{\text{ff}} \text{ cm}^{-1},$$

for $h \nu \ll k_B T$, where $T$ is the temperature, $Z$ is the average charge per ion, $n_e$ and $n_i$ are the electron and ion densities, respectively, $\rho_{\text{ff}} \approx 1$ is the Gaunt factor, and all quantities are in cgs units. Just behind the forward shocks (see §3), the temperature is high ($\gg 10^9$ K), and free-free absorption is negligible. But at the front edge of the ejecta, with density $\rho_{\text{ff}}$ and temperature $T$, pressure continuity across the contact discontinuity requires $\rho_{\text{ff}} k_B T / m_p \sim n_0 m_p v_{\text{ff}}^2$. From this we estimate that $T \sim 10^5 - 10^6$ K at $t \sim 10^5 - 10^6$ s. For $Z/A \approx 1/2$ (where $A$ is the average atomic number) we estimate $Z^2 n_e n_i \sim (\rho_{\text{ff}}/m_p)^2$. The observed flux is thus $F_{\nu,\text{obs}} \approx F_{\nu,\text{obs}} e^{-\tau_f}$, where $\tau_f \approx \alpha_f \Delta R_p$ and $\Delta R_p \approx 0.1 R_p$ is the shell thickness.

In the top panel of Figure 1 we plot the evolution of the key frequencies $\nu_{\text{SA}}$ (eq. [12]), $\nu_c$ (eq. [15]), and $\nu_{\text{ff}}$, where the latter is defined by $\tau_f \approx 1$. From this one can follow the spectrum peak (at $\nu_{\text{SA}}$) and determine when it is detectable. For example, 10 GHz emission peaks at $t \approx 6 \times 10^6$ s. In the bottom panel we explore the lightcurves at 1.4 GHz as we vary $T$ and $\eta_{\text{ff}}$. Typical timescales are ~ months with a peak of ~ 3–10 mJy. Free-free absorption is mostly negligible unless $T \lesssim 10^4$ K. The peak flux and time of peak are sensitive to $\eta_{\text{ff}}$.

In Figure 2 we plot the peak flux at 1.4 GHz for a range of dipole field strengths and initial spin periods. The general trend is that faster spins and larger fields result in a more luminous radio source. This reverses in the top left corner where $\tau$ is sufficiently short that $L(t)$ has decreased significantly by the time of peak. Over most of this parameter space, the magnetar winds are not expected to be strong enough to generate a collimated outflow (Bucciantini et al. 2012).

4. DETECTION RATES

AIC can result from both channels popularly discussed for SNe Ia (single-degenerate and double-degenerate; see §1). Thus it makes sense to normalize the AIC rate to that of the SN Ia rate. The Lick Observatory Supernova Search finds a rate of $(3.01 \pm 0.062) \times 10^{-7}$ Ia Mpc$^{-3}$ yr$^{-1}$ (Li et al. 2011), which corresponds to $(4.0 - 7.1) \times 10^{-3}$ Ia yr$^{-1}$ for the Milky Way. Using population synthesis, Yungelson & Livio (1998) find AIC rates of $8 \times 10^{-7} - 8 \times 10^{-5}$ IAC yr$^{-1}$ for the Milky Way, depending on assumptions about the common-envelope phase and mass transfer. Their upper bound is similar to the constraint obtained from observed abundances of neutron rich isotopes (Hartmann et al. 1985, Fryer et al. 1999).
For a typical peak 1.4 GHz flux of \( F_{p,100} \approx 5 \, \text{mJy} \) at a distance of 100 Mpc, and an AIC rate that is a fraction of \( f \) of the SN Ia rate, the detection rate of radio transients from AIC is

\[
\text{Rate}(> F_{p,100}) \approx 14 \left( \frac{f}{10^{-4}} \right) \left( \frac{F_{p,100}}{5 \, \text{mJy}} \right)^{-3/2} \, \text{yr}^{-1},
\]

where \( f \approx 10^{-4} \). For a \( \sim 3 \) month duration emitting above \( \sim 1 \, \text{mJy} \), we expect \( \sim 4/f^{-1/2} \) AICs above threshold at a given time. In contrast, merely a few AICs are estimated to be detected as kilonovae per year (Metzger et al. 2009b), and this number could be much less if a lack of differential rotation during WD accretion (Piro 2008) inhibits disk formation upon collapse (Abdikamalov et al. 2010).

Similar radio emission is possible if some NS mergers produce a massive NS. This would then provide an electromagnetic counterpart following months after the gravitational wave emission during coalescence\(^2\) (Metzger & Berger 2012; Nissanke et al. 2012). In fact, the distance at which the radio emission can be detected is similar to that probed by the next generation of “advanced” ground-based laser-interferometers. The NS merger rate is comparable or greater than the AIC rate. For example, Kim et al. (2005) estimate a Galactic rate of \( \sim (0.1-3) \times 10^{-4} \, \text{yr}^{-1} \). The detection frequency is thus similar to equation (19) with \( f \approx 10^{-2} \), with the caveat that it may be much less if most NS mergers produce black holes.

### 5. DETECTION & IDENTIFICATION OF AIC EVENTS

This is a timely topic to discuss given the renascence that is now occurring in decimetric radio astronomy. Refurbished (EVLA) and new facilities promise high mapping speeds by using small diameter antennas to realize a given total area (e.g. MeerKAT), through the use of focal plane arrays instead of a grating on the sky (as opposed to slewing antennas or observing calibrator sources). For “on-the-fly” mapping, the efficiency of time spent integrating on the sky (as opposed to slewing antennas or observing calibrator sources). For “on-the-fly” mapping, \( \eta \approx 0.9 \) (S. Myers, private communication) and a 250-hour allocation results in observing \( \sim 19,000 \) square degrees (comparable in area and depth to FIRST; Becker et al. 1995). Another strategy would be to use the same allocation for several epochs focused on fields selected by their richness in nearby galaxies (as was done for the PTF key project “Investigation of Transients in the Local Universe,” Kasliwal 2011). A systematic optical mapping of the sky should be undertaken a week or more prior to the radio observations and continued for a week after (for instance with PTF; Law et al. 2009; Rau et al. 2009).

The EVLA radio survey would yield roughly two AICs. The signature of these events would be unique: they would be coincident with galaxies in the nearby Universe, would not be accompanied by any optical supernovae of the sort that have detected so far, and would often occur outside of the nuclear regions of the host galaxy. For especially interesting radio detections, it may be worth conducting followup in the infrared to rule out the presence of an extinguished, radio-bright supernova. The issue of associated X-ray emission is less certain. It is possible that young magnetars shine in the X-rays, but if the ejecta is dominated by heavy elements then the classical X-ray emission is suppressed. A background AGN or a foreground active star would be revealed by the distinctive spectra of the astrometric coincident quiescent source.

The future is quite bright. The soon-to-be-commissioned APERTIF (Verheijen et al. 2008) mapper could do the same survey 30% faster or alternatively redo the survey every few months. In the future ASKAP and MeerKAT mappers could undertake the survey five times faster.

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### REFERENCES


Chevalier, R. A. 1977, Supernovae, 66, 53


Kulkarni, S., & Kasliwal, M. M. 2009, Astrophysics with All-Sky X-Ray Observations, 312


Usov, V. V. 1992, Nature, 357, 472

Verheijen, M. A. W., et al. 2008, AIPC, 1035, 265


\(^2\) Also see the work of Nakar & Piran (2011), which focuses on emission from the interaction of ejecta with the ISM.

\(^3\) In using a low threshold (7σ) we take advantage of the fact that galaxies in the local universe (say out to 100 Mpc) occupy a small solid angle (\(\sim 100\) square degrees, excluding the nearest large galaxies), so chance coincidences are suppressed by three orders of magnitude (Kulkarni & Kasliwal 2009).