Differential Measurement and Model Calculations of Cosmic Ray Latitudinal Gradient With Respect to the Heliospheric Current Sheet

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Simultaneous magnetic field and charged particle measurements from the Voyager spacecraft with heliographic latitude separations of >10° are used to investigate the distribution of ~1-GeV galactic cosmic ray protons with respect to the heliospheric current sheet in the outer solar system. By comparing the ratio of cosmic ray flux at Voyager 1 to that at Voyager 2 during periods of relatively quiet interplanetary conditions when the spacecraft are either both north or both south of the heliospheric current sheet, we derive an average latitude component of the gradient of the cosmic ray flux on opposite sides of the current sheet under restricted interplanetary conditions of -0.22 ± 0.03%/deg, equivalent to a decrease of ~1%/AU away from the current sheet at ~12 AU. Our results for these limited periods are in qualitative agreement with propagation models incorporating particle drifts.

INTRODUCTION

The latitudinal variation in the intensity of galactic cosmic rays with respect to the heliospheric current sheet is an indicator of the relative importance of particle drifts and diffusion in heliospheric propagation. Symmetries in the interplanetary magnetic field due to the sun's rotation, i.e., wrapped up spiral field lines at the equator in contrast to nearly radial field lines at either pole, should result in a latitudinal organization of the flux about the heliographic equator [Fisk, 1976; Newkirk and Fisk, 1985]. Transport modeling including only the effects of diffusion, convection, and adiabatic deceleration can produce latitudinal variations of cosmic ray flux for selected choices of the model parameters [see Newkirk and Fisk, 1985, and references therein], but in these two-dimensional models, intensity minima are symmetrically displaced with respect to the heliographic equator, and the effects of azimuthal variations in the solar wind velocity have not been evaluated. In contrast, if particle drifts are important in cosmic ray transport, minima in the cosmic ray flux should be symmetrically placed with respect to the heliospheric current sheet, as has recently been demonstrated in a three-dimensional model of cosmic ray transport including particle drifts [Kota and Jokipii, 1983] and reported in various investigations below.

The geometry of the wavy current sheet is an important factor in propagation models including particle drifts. Examples of the spatial distribution of 1.6-GeV cosmic ray protons at 1 AU and 5 AU predicted by the numerical model of Kota and Jokipii [1983] for the present half of the 22-year solar magnetic activity cycle are displayed in Figure 1. Parameters producing differences between the examples are listed in the figure caption. Effects of the wavy current sheet are evident in the isointensity curves at all latitudes and longitudes, although there are significant differences in detail due mainly to the relative importance of drift and diffusion for the two diffusion coefficients used. The calculated intensities depend on a balance among (1) diffusion from the heliospheric boundary, (2) outward convection with the solar wind, (3) sunward drift along the current sheet in this solar epoch, and (4) subsequent diffusion and drifting away from the current sheet. In addition to different tilt angles, the diffusion coefficient $K_0$ used in Figures 1a and 1b is a factor of 3 smaller than that used in Figures 1c and 1d, with the same 400-km/s solar wind velocity in both examples. The two values of $K_0$ used represent approximate upper and lower limits for 1- to 2-GeV protons at 1 AU. As a result of the difference in $K_0$, diffusion from the polar regions is much more important in Figures 1c and 1d, while the effects of drift and diffusion away from the current sheet are more evident in Figures 1a and 1b. There is no single parameter, such as heliographic latitude $\delta$, or the angular distance from the current sheet $\lambda_0$ which will completely organize the complex gradients.

Newkirk and Lockwood [1981], Newkirk and Fisk [1985], and Newkirk et al. [this issue] used heliomagnetic latitude $\lambda_{m0}$ and angular distance from the current sheet $\lambda_p$ to organize their observations. In their studies, ground-based synoptic observations of the $K$ corona are used to determine the shape of the current sheet at the corona. This synoptic coronal information was then used in combination with solar wind velocity data to infer the position of the current sheet in latitude and longitude at 1 AU (for details, see Appendix C of Newkirk and Fisk [1985]). They found a 2-3% decrease in the average flux of 5-GeV galactic cosmic rays measured at 1 AU for $\leq 45^\circ$ displacements from the inferred position of the heliospheric current sheet, giving an average latitudinal gradient with respect to the current sheet $G_{\lambda_m}$ of $-0.04$ to $-0.07%/deg$. Sub-

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Fig. 1. Model calculations of intensity contours for 1.6-GeV protons near 1 AU and 5 AU for current sheet tilts of 30° (Figures 1a and 1b) and 60° (Figures 1c and 1d) during the present 11-year portion of the solar cycle. Normalization is made to the interstellar intensity, and the heavy line indicates the position of the current sheet. Other relevant model parameters are (Figures 1a and 1b) \( K_0 = 5 \times 10^{21} \text{ cm}^2 \text{s}^{-1} \) and \( R_b = 10 \text{ AU} \) and (Figures 1c and 1d) \( K_0 = 1.5 \times 10^{22} \text{ cm}^2 \text{s}^{-1} \) and \( R_b = 15 \text{ AU} \). These and other model parameters are defined by Kota and Jokipii [1983].

Subsequently, Newkirk et al. [this issue] found latitude gradients at 1 AU corresponding to \( G_{\phi m} \sim -0.4/\text{deg} \) and \(-0.03/\text{deg} \) (\( \sim -23/\text{AU} \) and \(-2/\text{AU} \), respectively) for cosmic rays with kinetic energies of \( >100 \text{ MeV} \) and \( <13 \text{ GeV} \), respectively. These results are shown by Jokipii and Kota [this issue] to be in reasonably good agreement with models in which drift plays an important role.

Badruddin et al. [1985], using a superposed epoch analysis of neutron monitor measurements of the flux of GeV energy cosmic rays in combination with observations of the current sheet at 1 AU (i.e., interplanetary magnetic field sector boundaries), demonstrate that cosmic ray intensity generally decreases with increasing time from current sheet encounters and interpret this as indicative of a latitudinal variation, although they do not quantify their results. These observations by Badruddin et al. are consistent with the results of Duggal et al. [1981], although Duggal et al. were primarily interested in determining which subsets of stream-stream interaction regions and sector boundaries were responsible for statistically significant cosmic ray variations. As elegant as these earth-oriented analyses are, they are nevertheless single-point measurements in which the reported latitudinal effects are very small compared to other temporal variations in intensity and for which the latitudinal distance to the current sheet is not directly measured and must be estimated.

Latitude variation of the galactic cosmic ray flux may also be investigated using the ratio of cosmic ray flux and observations of the current sheet at two spacecraft separated in latitude. Using Voyager 1 and 2 data from early 1981 through mid-1982, Decker et al. [1984] found a negligible latitudinal gradient with respect to the heliographic equator in the outer solar system. Our study of Voyager 1 and 2 data from late 1981 through mid-1983 complements the Decker et al. study by investigating the latitudinal organization of cosmic ray flux with respect to the heliospheric current sheet in the outer solar system. The model calculations in Figure 1 suggest that if two-point observations at low heliographic latitudes can be organized so one observation point is always closer to the current sheet than the other, then average gradients may be directly measured. In order to illustrate this approach, we first describe the analysis technique and apply it to model calculations of the intensity such as those in Figure 1. We then apply the same technique to the observations. A preliminary report of our results can be found in the article by Christon et al. [1985].

**Differential Measurement Technique**

As an illustration, assume that the cosmic ray flux at an observation point in the heliosphere is given by

\[
i_i = i_0 \exp \left[ G_r (r_i - R_b) \right] \exp \left\{ G_\phi \left( \Theta_i - \Theta_0 (r_i, \varphi_i) \right) \right\}
\]  

(1)

where \( G_r \) is the average radial component of the gradient, \( G_\phi \)
is the colatitude component of the gradient, $R_\phi$ is the heliocentric distance to the boundary of the heliosphere, $j_b$ is the cosmic ray flux at $R_\phi$, assumed constant, $\Theta_\phi(r, \varphi)$ is the colatitude of the current sheet, and $r$, $\varphi$, and $\Theta$ are the heliocentric distance, longitude, and colatitude of the point of observation, respectively. Colatitude $\Theta$ with the range $[0^\circ, 180^\circ]$ and latitude $\varphi$ with the range $[90^\circ N, 90^\circ S]$ are related by $\varphi = 90^\circ - \Theta$. Magnetic latitude $\lambda_m$ is related to colatitude by $\lambda_m = \Theta - \Theta_m$.

When a set of simultaneous observations is available at two or more well-separated points in interplanetary space, estimates of the latitudinal gradient can be obtained for each set of observations by selecting those observations when one spacecraft is, on the same side of the current sheet and solving

$$G_\Theta = \left[ \ln \left( \frac{1}{1 - G_b(r_1 - r_2)} \right) / (\Theta_1 - \Theta_2) \right] \left( \sum \text{w}_{gi} \text{G}_{gi} \right) / \sum \text{w}_{gi}$$

where $i$ runs from 1 to $n_{gi}$ or $n_{gg}$, i.e., is when the spacecraft are both north (NN) or both south (SS) of the current sheet, and $\text{w}_{gi}$ is the inverse square of $\Theta_{gi}$, the uncertainty in $G_{gi}$. The first letter of the two-character subscript identifies the magnetic field polarity followed by two shorter sectors of opposite magnitude and direction by $\sim 180^\circ$, the region of change being called an interplanetary sector boundary. Either spacecraft intercepting this current sheet would measure two longer sectors of opposite magnetic field polarity followed by two shorter sectors of opposite magnetic field polarity during each sequence, with the polarity determined by the magnetic hemispheres. The time from or until sector boundary crossings is a direct measure of the longitudinal distance of the spacecraft to the current sheet, and observed sector lengths are a direct measure of the longitudinal extent of waves in the current sheet.

In this study we explore the possibility that the sector lengths may also be an indication of the amplitude of the waves and therefore of the observer's longitudinal separation from the current sheet. For example, in Figure 2, Voyager 1 at point A is as close to the current sheet azimuthally as at point B, but since the sector length at B is much shorter than that at A, B may be closer to the current sheet in latitude than in longitude. Although the amplitude of the wavy current sheet is not necessarily smaller for shorter sectors, we will show below that such a relationship appears to be consistent with our measurements.

Although the heliospheric current sheet in Figure 2 is represented as a simple combination of nearly sinusoidal curves, the topology of the heliospheric current sheet is more complex near the sun and is unknown in interplanetary space. For example, the near-sun current sheet is at a distance of 2.5 solar radii, which is the footprint of the heliospheric current sheet, often has a more square wave than sine wave appearance with unequal north and south amplitudes during the period of this study [e.g., Hoeksema, 1984]. Though the general solar pattern may persist inside 1 AU, there is evidence for distortions of the current sheet beyond the near-sun region [e.g., Svalgaard and Wilcox, 1976; Seuss and Feynman, 1977; Trikakis, 1984]. In addition to probable near-sun distortions, interaction of solar wind streams beyond 1 AU significantly modifies the interplanetary structure from that observed at 1 AU. Thus at present there is no way to determine the latitudinal distance of a given observation from the current sheet in the outer solar system, as was done by Newkirk et al. for observations at 1 AU. Moreover, the current sheet is not always thin even at 1 AU, and the transition through the boundary may last for hours or even days [see Klein and Burlaga, 1980; Behannon et al., 1983].

The latitudinal separation of our observations can, however, be utilized in combination with the magnetic field observations to extract general information about the cosmic ray spatial distribution. We use field polarities to ensure that both spacecraft are on the same side of the current sheet, sector lengths to order the measurements in terms of the latitudinal separation from the current sheet (latitudinal restriction), and times from sector boundary crossings to order the measurements in terms of the azimuthal separation from the current sheet (azimuthal restriction). We can therefore restrict our observations to those occasions in which one spacecraft is, on the average, closer to the current sheet than the other. As can be seen by comparing Figures 1 and 2, when both spacecraft are north of the current sheet at low heliographic latitudes, Voyager 1 will tend to observe a lower flux whenever Voyager 2 is closer to the current sheet, and when both are south at low heliographic latitudes, Voyager 2 will tend to observe a lower flux whenever Voyager 1 is closer. Restriction of observation positions and sectors in this manner qualitatively ensures that the observer longitudinally closer to the current sheet in a shorter sector is also more likely to be closer to the current sheet both in absolute angular distance and in latitudinal distance.

The signs of colatitude gradients should be opposite at symmetrical locations on either side of the current sheet in a drift-dominated transport regime. Therefore we evaluate $G_{\Theta}$.
in which \(G_{NN} = G_{\Theta N}\) and \(G_{SS} = -G_{\Theta S}\). The average
\[
\langle G_\Theta \rangle = \left( \frac{\sum w_{G_i} G_{\Theta i} - \sum w_{G_i} G_{\Theta j}}{\left( \sum w_{G_i} + \sum w_{G_j} \right)} \right)
\]
where \(i(j)\) runs from 1 to \(n_{NN}\)(\(n_{SS}\)), \(w_{G_i}\) is the inverse square of \(\sigma_{G_{\Theta i}}\), the uncertainty in \(G_{\Theta i}\), should be independent of the detailed longitudinal structure of the current sheet \((\Theta_j)\). With the aid of the numerical transport model we will demonstrate that the technique of calculating \(\langle G_\Theta \rangle\), while placing restrictions on spacecraft positions relative to the current sheet, provides a useful diagnostic for investigating the distribution of cosmic rays in the heliosphere.

A Transport Model With Current Sheet Organization

The role of particle drift terms in the Fokker-Planck transport equation governing the propagation of galactic cosmic rays within the heliosphere has been explored theoretically only recently [see Kata and Jokipii, 1983, and references therein]. Diffusion enters into the model through the symmetric components of the diffusion tensor \(\kappa\), which are assumed proportional to \(K_\Phi B_j^2/|B|\), where \(K_\Phi\) is the magnitude of the diffusion coefficient, \(P\) is particle rigidity, \(\beta\) is the particle speed relative to the speed of light, and \(\beta\) is the magnitude of the magnetic field [Jokipii and Davila, 1981]. Drift enters into the model through the antisymmetric components of \(\kappa\), which are assumed proportional to \(P\beta\Phi B_j/|B|\) [Jokipii et al., 1977].

These drift terms had not been included in previous evaluations of cosmic ray transport. The most recent refinement of calculations involving the drift terms [Kata and Jokipii, 1983] results in a three-dimensional, corotating, numerical model of the spatial variation of galactic cosmic ray flux.

In this model, cosmic ray transport is strongly influenced by the drift terms, and the flux is roughly symmetric about the heliographic poles and organized by the heliospheric current sheet. The intensity contours in Figure 1 resulting from this model are qualitatively representative of the model solutions for \(\sim 1.6\) GeV protons (rigidity \(P = 2.3\) GV) throughout the region of our investigation.

In the model calculations for the current phase of the 22-year cycle, particles diffuse down in latitude from the poles and drift and diffuse upward in latitude from the current sheet, resulting in intensity minima away from the current sheet and gradients at low heliographic latitudes of opposite signs in opposite sectors. Although the gradient depends on both the heliographic latitude and the magnitude of the diffusion coefficient, at low heliographic latitudes the intensity in a given sector tends to be higher nearer the current sheet.

In an attempt to focus on model predictions appropriate to our situation, i.e., one in which the true separation from the current sheet is not well known but in which the longitudinal distance from current sheet encounters is known, we use the following procedure. The flux is evaluated at points equally spaced \((10^\circ)\) in latitude between the current sheet and equally spaced \((5^\circ)\) in latitude. Results are obtained in the latitude range bounded above by \(20^\circ\) N and below by \(4^\circ\) S, the extremes of Voyager latitudes during this period. We calculate the colatitude gradient \(G_{\Theta i}\) in \(\Gamma/\Delta\Theta\) from these model predictions, where \(\Gamma\) is the ratio of the flux at the more northerly point (Voyager 1) to that at the more southerly point (Voyager 2) and \(\Delta\Theta\) is a representative colatitude spacecraft separation. Expectation values \(\langle G_{\Theta i} \rangle\), relatively independent of the relative longitudinal positions of the spacecraft, are calculated via equation (3), using equal uncertainties by averaging over all possible combinations of observation points while keeping the sign and magnitude of the colatitude separation fixed. This simulates the actual experimental situation to some degree. Since Voyager 1 is at north latitudes and Voyager 2 is near the equator, one generally expects \(G_{\Theta} < 0\) when both spacecraft are north of the current sheet and \(G_{\Theta} > 0\) when both spacecraft are south of it.

As an illustrative example we have analyzed the model calculations corresponding to Figures 1a and 1b for observations at 1 and 5 AU, where \(K_\Phi = 5 \times 10^{21}\) cm\(^2\) s\(^{-1}\), \(R_\Phi = 10\) AU, and \(\alpha = 30^\circ\). A set of model parameters in which the effects of drift are clearly important. A representative spacecraft separation of \(15^\circ\) is chosen. The histograms in Figure 3, including both the shaded and unshaded portions, are distributions of unrestricted data whose averages at 1 AU are \(\langle G_{\Theta} \rangle_{NN} = -0.18 \pm 0.02\) and \(\langle G_{\Theta} \rangle_{SS} = 0.25 \pm 0.01\%/\text{deg}\) and at 5 AU are \(\langle G_{\Theta} \rangle_{NN} = -0.10 \pm 0.01\) and \(\langle G_{\Theta} \rangle_{SS} = 0.14 \pm 0.01\%/\text{deg}\). The shaded portions are the azimuthally restricted subsets whose averages at 1 AU are \(\langle G_{\Theta} \rangle_{NN} = 0.45 \pm 0.02\) and \(\langle G_{\Theta} \rangle_{SS} = +0.40 \pm 0.01\%/\text{deg}\) and at 5 AU are \(\langle G_{\Theta} \rangle_{NN} = -0.24 \pm 0.01\) and \(\langle G_{\Theta} \rangle_{SS} = +0.21 \pm 0.01\%/\text{deg}\).

Restriction of the azimuthal positions of the observation points in the manner described in the previous section selects the subsets of observations indicated by the shaded distributions in Figure 3. The lowercase letter in the two-character identifier indicates the observation point closer to the current sheet. Note that the averages (listed in the figure caption) and modes of these azimuthally restricted data are more clearly separated than they were for the unrestricted data. The super­script indicates the type of selection criterion applied. The azimuthally restricted average at 1 AU is \(\langle G_{\Theta} \rangle_{NN} = -0.44 \pm 0.01\%/\text{deg}\) and at 5 AU is \(\langle G_{\Theta} \rangle_{SS} = -0.23 \pm 0.01\%/\text{deg}\), showing a factor of 2 enhancement of \(\langle G_{\Theta} \rangle\) at both sampling radii due to the application of the azimuthal restriction. Note that because of the simple sinusoidal form of the model current sheet the azimuthal restrictions discussed previously are neither applicable nor necessary.

The model calculations depend on a number of parameters,
such as tilt angle $\alpha$, diffusion coefficient $K_0$, and distance of the outer boundary $R_o$, for example. These parameters are responsible for the general differences between the model predictions in Figures 1a and 1b and those in Figures 1c and 1d. Sampling parameters such as the radial distance $r$, spacecraft latitude separation $\Delta \theta$, and latitude band sampled also produce differences in the values of $\langle G_\alpha \rangle$ obtained from each set of model parameters. The effects of varying the model parameters and sampling parameters are demonstrated by intercomparing the values of $\langle G_\alpha \rangle$ derived from the four different sets of model parameters listed in Table 1 for various choices of sampling parameters. Relative uncertainties in the model predictions in Table 1 are always $\leq 0.25$ and $\leq 0.06$ for unrestricted and azimuthally restricted subsets, respectively, and are suppressed in the Table for clarity and ease of reading. Because of the unrealistically small values of $R_o$ used here, the predictions at 5 AU merely suggest conditions expected well beyond 1 AU but not yet close to the boundary of the heliosphere and should not be interpreted as specific predictions of cosmic ray intensity variations at 5 AU. However, in all of the model and sampling situations displayed in Table 1 one major factor is apparent: application of the azimuthal restriction results in a larger, more negative value of $\langle G_\alpha \rangle$, reflecting a general decrease in cosmic ray flux with increasing separation from the current sheet.

The effects of varying the modeling and sampling parameters are demonstrated by comparing the values of $\langle G_\alpha \rangle$ in Table 1. For example, values of $\langle G_\alpha \rangle$ for $K_0 = 1.5 \times 10^{22}$ cm$^2$ s$^{-1}$ are larger than those for $K_0 = 5 \times 10^{21}$ cm$^2$ s$^{-1}$, as might be expected. The model also yields increased values of $\langle G_\alpha \rangle$ at 1 AU for larger current sheet tilts, but slightly decreased values at 5 AU, implying that at low heliographic latitudes, $\langle G_\alpha \rangle$ is not strongly dependent on $\alpha$, which is unknown in the experimental situation. Our analysis of the model also predicts systematically smaller values of $\langle G_\alpha \rangle$ and $\langle G_\alpha \rangle$ at 5 AU than at 1 AU, suggesting that observations in the inner and outer heliosphere may differ. Finally, differences in $\langle G_\alpha \rangle$ and $\langle G_\alpha \rangle$ due to differences in latitude separation are small, suggesting that the accumulation of data from an extended period will not compromise our ability to discern important trends in $G_\alpha$.

**DATA SELECTION**

This study covers the period from day 240, 1981, until day 190, 1983, during which the separation of the Voyagers increased from 1.9 to 4.7 AU in radial distance from the sun (Voyager 1 traveled from 11 to 17 AU) and from 10° to 21° in latitude (Voyager 1 traveled from 6°N to 20°N). The Voyagers were separated by $\leq 16°$ in longitude. Because of the separation in longitude and radius the probability that the spacecraft are both in the same magnetic sector during this period is low. In order to determine the instantaneous radial and latitudinal gradients represented in Figure 1, daily samples of the counting rates of protons with kinetic energies of $>75$ MeV and a median energy of $\sim 0.95$ GeV ($\sim 1.6$-GV rigidity) measured by the nearly identical High Energy Telescopes of the Cosmic Ray Subsystem on the Voyager 1 and 2 spacecraft [Stone et al., 1977] were compared (see Figure 4). Ratios of the Voyager 1 to Voyager 2 counting rates, adjusted for the difference in geometrical factors of the telescopes [Cummings and Webber, 1983], are plotted in the upper panel of Figure 4. The relative uncertainty in this adjustment is $\sim 0.2\%$ and is applied identically to all values of $\Gamma$. Uncertainties in

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<th>Model Parameters</th>
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<td>$R_o$, AU</td>
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Fig. 4. (Top) The ratio of daily samples of the Voyager 1 to the Voyager 2 counting rate of $>75$-MeV protons. The ratios have been adjusted for a difference in geometrical factors of the telescopes. Underlined periods indicate data used in this study to estimate the latitude gradient. (Bottom) Daily samples of the counting rates of $>75$-MeV protons from Voyagers 1 and 2. Voyager 1 is offset for clarity.
North rotational pole, and positive fields are associated with the predominant polarity of the sun's magnetic field direction leading either toward the sun (negative, shown to denote negative and positive polarity fields, respectively).

Although shorter magnetic sectors exist, the longer magnetic sector remains predominantly within the 22-year magnetic activity solar cycle, negative fields at the earth, and positive fields are most similar to sector boundaries near earth. Below: days labeled with "SN" or "NN" are included in this study.

From late 1981 until late 1982 the cosmic ray fluxes are dominated by three rather long (≈100-day) periods during which the overall flux levels neither increase nor decrease appreciably with time. A moderate recovery for ~50 days at the start of 1982 separates the late 1981 and early 1982 level flux periods. Dramatic flux decreases (Forbush decreases) in mid-1982 mark the passage of solar flare shocks and transient material. At the start of 1983 the fluxes at both Voyagers start to increase steadily with time as they continue to recover from solar modulation.

Figure 5 shows the magnetic field azimuth and elevation angles measured by the Voyager Magnetic Field Experiment [Behannon et al., 1977] are used in this study. Figure 5 is an example of the magnetic field data plots which were used to determine the sector polarities, sector boundaries, and periods of field turbulence.

A magnetic sector, for use in this study, is required to be a time period greater than 4.5 days during which the field azimuth remains predominantly within 90° of the expected spiral field direction leading either toward the sun (negative, shown as a minus sign on the figure) or away from the sun (positive, shown as a plus sign). The expected field azimuth is ~85° at the Voyagers for this time period, and the expected elevation is within ~45° of the heliographic equator. During the present portion of the 22-year magnetic activity solar cycle, negative fields are associated with the predominant polarity of the sun's north rotational pole, and positive fields are associated with the sun's south rotational pole. (Below, N and S will be used to denote negative and positive polarity fields, respectively). Although shorter magnetic sectors exist, the longer magnetic sectors (≥4.5 days) most probably result from plasma flow from the larger near-equatorial coronal holes that are often linked to the sun's poles. A sector boundary is here defined to be at the centroid of the transition region from adjacent sectors of opposite polarities. If a sector boundary occurs within a data gap ≤1 day long, the center of the gap was taken to be the time of the sector boundary. Sector boundaries occurring in longer data gaps were not included.

Data days were first selected by a computer search through lists of the field azimuth, in which calendar days were accepted for analysis if 0.75 of those hourly averages collected fell within the current magnetic sector. Subsequently, detailed plots similar to Figure 5 were scanned to assure that the selection is valid and that there are ≥8 hours of usable magnetic field data at each Voyager, and to determine the length of the sectors in which the data day appeared. This selection procedure is analogous to those used in similar analyses of sector structure [e.g., Klein and Burlaga, 1980; Hoeksema 1984]. Some of the sector boundaries shown in Figure 5 (double-headed vertical arrows) appear as sharp divisions between fields of opposite polarity. These sharp divisions, labeled with "SB," are typical of what one might call "classical" sector boundaries observed at 1 AU. At other boundaries the separation of sectors is not so clear, but the fields at ±2 days from the boundary are often definitely of opposite polarities. Extremely turbulent periods, for example, from day 160 to 163 and after day 170 (see Figure 5), are not included in the data sets. The turbulent periods are most probably due to solar transients propagating through the region.

Data Set Selection

Criteria for the initial data collection, as detailed above, are: (1) the spacecraft were required to be completely in a region of magnetic field pointing either generally toward or away from the sun; (2) all periods with probable contamination from solar flare particles were removed; and (3) all periods surrounding Forbush decreases, such as those encountered on
~ 175, 1982, and 220, 1982, were eliminated. This produced data set I (DS I), which includes the subsets NN, SS, NS, and SN. Data subsets NS and SN are used below as an independent data set in order to determine the radial gradient. Following this selection procedure, ~22% of our total data remained, there being a total of 42 magnetic sectors at Voyagers 1 and 2 that are used in 16 NN and 7 SS combinations. Proceeding with more restrictive selection criteria, we eliminated from the DS I NN and SS subsets the days in which segments of sectors were not recognizable, i.e., days with large fluctuations in field direction, with systematic departures from the spiral direction in azimuth or elevation, or with insufficient data. The resulting subset of DS I data retained for analysis is called DS II. DS II was divided into two subsets: DS IIa, in which sectors were clearly defined, and DS IIb, in which sectors might have been present but were disturbed or distorted. Specifically, in DS IIa, the magnetic field direction was uniform and close to the expected spiral direction, whereas on days in DS IIb the magnetic field direction fluctuated somewhat or showed systematic deviations from the spiral direction.

Azimuthal and Latitudinal Restrictions

Restrictions are applied so that on the average, in the north, Voyager 2 is expected to be closer to the current sheet than Voyager 1 (NN), and in the south, Voyager 1 is expected to be closer to the current sheet than Voyager 2 (SS). Specifically, the azimuthal restriction (az) is applied by averaging only those days during which Voyager 2 (1) is closer in time from the current sheet than Voyager 1 (2) (corresponding to a smaller azimuthal separation) in north (south) polarity fields. The latitudinal restriction (lat) is applied by averaging only those days during which the sector length at Voyager 1 (2) is longer than that at Voyager 2 (1) (corresponding to a greater latitudinal separation) in north (south) polarity fields.

RESULTS AND DISCUSSION

The Radial Gradient

Determination of \( \langle G_N \rangle \) requires knowledge of the value of \( G_n \) which can be estimated directly from the NS and SN subsets, since latitude variations having opposite signs should cancel on the average in either of these subsets. \( G_n \) can also be determined from the NN and SS data sets analyzed in combination, since the latitude gradients, which have opposite signs in the magnetic hemispheres above and below the current sheet, should average to zero in combination. We use DS I subsets to calculate our estimate of the radial gradient

\[
\langle G_n \rangle = \left[ \frac{\sum_i w_i \ln \Gamma_i / (r_{1i} - r_{2i})}{\sum_i w_i} \right] \]

where \( i \) runs from 1 to the number of observations in the subset and \( w_i \) is the inverse square of \( \sigma_{ri} \), the uncertainty in \( \Gamma_i \). Distributions of the daily estimates \( G_n = \ln \Gamma_i / (r_{1i} - r_{2i}) \) for the NS, SN, NN, and SS subsets plotted in Figure 6 show that the most likely value of \( \langle G_n \rangle \) is \(~2\%/AU\), consistent with the value obtained by Decker et al. [1984], and that any splitting of these subsets due to latitude variations is not apparent. Note that NS, SN, NN, and SS are independent data sets. The two combinations NS, SN and NN, SS are likewise independent data. Our estimates of \( G_n \) calculated from the combined NS and SN subsets, \( \langle G_{n,NS,SN} \rangle = 2.21 \pm 0.11\%/AU \), and from the combined NN and SS subsets, \( \langle G_{n,NN,SS} \rangle = 2.29 \pm 0.13\%/AU \), are consistent, suggesting that the best estimate is an average over all 152 days of data combined (bottom panel of Figure 6), which yields \( \langle G_n \rangle = 2.25 \pm 0.08\%/AU \). Our estimate \( \langle G_n \rangle \), compared to other recent estimates of \( G_n \) in Table 2, shows the greatest similarity to the values obtained by Decker et al. [1984], over nearly the same time interval as ours, and by Van Allen and Randall [1985], over many years of data. Note that in all except two of the radial gradient studies listed in Table 2, observation times have been adjusted for a delay due to propagation of information with the solar
wind before analysis. In addition to the instantaneous analysis which forms the basis of this paper, we have also performed a "shifted" analysis of the early 1983 data and find that the shifted value of $\langle G \rangle$ is 2.24 ± 0.09%/AU. Inspection of equations (2) and (3) reveals that the average dependence of $\langle G \rangle$ on $G_s$ is $r_1 - r_2/\langle \Theta_1 - \Theta_2 \rangle$, so that an uncertainty of 0.1%/AU in the assumed $G_s$ introduces an error of only 0.02%/deg in the derived $\langle G \rangle$.

### Latitude Variations

Figure 7 shows the distributions of $G_s$ corrected for $G_e = 2.25$/AU for DS I subsets SN, NS, SS, and NN. The modes of these distributions are generally centered on $G_s = 0$. In addition, the s$s^*$ and $Nn^*$ DS I subsets show only a very small splitting due to a latitudinal gradient, as might be expected, since in this data set we have not been selective about the presence of turbulence or the structure of the boundaries between magnetic sectors. Histograms of the distributions of $G_s$ for DS II unrestricted, azimuthally restricted, latitudinally restricted, and latitudinally and azimuthally restricted subsets are plotted in Figure 8. Average values appear in Table 3 and may be qualitatively compared to the model distributions in Figure 3, since similar restrictions have been applied to data and model predictions. Note that once the spacecraft positions are restricted either azimuthally or latitudinally, the averages and modes of the $Nn^*$ $G_s$ distributions shift to generally more negative values, a trend consistent with our analysis of the model calculations.

Figure 9 shows the distributions of $G_s$ for DS II. Average values appear in Table 3. Unrestricted averages are consistent with no latitude gradient, while restricted averages are statistically significant and negative. Since differences between $\langle G_s \rangle$ for DS IIa and DS IIb are statistically insignificant in all cases, we may conclude that moderate deviations or fluctuations of the magnetic field direction from the spiral direction do not significantly affect these values of $\langle G_s \rangle$, and we therefore consider the $\langle G_s \rangle$ for DS II as our best estimates in restricted and unrestricted subsets. The trend displayed in Table 3 through the application of restrictions to our data is consistent with the trend displayed in Table 1 through the application of restrictions to the model. Both trends indicate a decrease in cosmic ray flux with increasing distance from the current sheet. Note, however, that at 5 AU, (1) for unrestricted data the values of $\langle G_s \rangle$ are consistent with $\langle G_s^* \rangle$ for $K_0 = 1.5 \times 10^{22} \text{ cm}^2 \text{ s}^{-1}$ but smaller than $\langle G_s^* \rangle$ for $K_0 = 5 \times 10^{21} \text{ cm}^2 \text{ s}^{-1}$, and (2) for azimuthally restricted data, the values of

### TABLE 2. Recent Estimates of Cosmic Ray Radial Gradient

<table>
<thead>
<tr>
<th>Study/Reference</th>
<th>Averaging Period, Days</th>
<th>Spacraft Used</th>
<th>$V_{out}$, km/s</th>
<th>Time Period</th>
<th>$G_s$, %/AU</th>
</tr>
</thead>
<tbody>
<tr>
<td>Lockwood and Webber [1984]</td>
<td>26</td>
<td>V1, V2, P10, IMP 8</td>
<td>(800, 400, $\infty^*$)</td>
<td>1975-1982</td>
<td>3.0 ± 0.3</td>
</tr>
<tr>
<td>Venkatesan et al. [1984]</td>
<td>27</td>
<td>V1, V2, IMP 8</td>
<td>500 and $\infty$</td>
<td>1977-1982</td>
<td>2.4</td>
</tr>
<tr>
<td>Decker et al. [1984]</td>
<td>26</td>
<td>V1, V2</td>
<td>$\infty$</td>
<td>1981-1982</td>
<td>2*</td>
</tr>
<tr>
<td>Van Allen and Randall [1985]</td>
<td>25</td>
<td>P10, P11</td>
<td>$\approx 440^*$</td>
<td>1972-1984</td>
<td>2.06 ± 0.20</td>
</tr>
</tbody>
</table>

NOTES:
- Values in %/deg. Numbers in parentheses are days of observation.
- No shift corresponds to an instantaneous propagation speed.
- Three different values intermixed.
- Either $G_e = 2$/AU assuming $G_s = 0$ or $G_s = 0.4$/deg assuming $G_e = 0$. Values range from 250 to 750.

---

**TABLE 3. $\langle G_s \rangle$ and $\langle G_s^* \rangle$**

<table>
<thead>
<tr>
<th>Data Sets</th>
<th>I</th>
<th>II</th>
<th>IIa</th>
<th>IIb</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Unrestricted Average</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\langle G_s \rangle_{un}$</td>
<td>0.02 ± 0.03 (52)</td>
<td>0.03 ± 0.04 (29)</td>
<td>-0.02 ± 0.05 (21)</td>
<td>0.14 ± 0.09 (8)</td>
</tr>
<tr>
<td>$\langle G_s^* \rangle_{un}$</td>
<td>-0.02 ± 0.04 (22)</td>
<td>-0.01 ± 0.04 (19)</td>
<td>-0.06 ± 0.03 (6)</td>
<td>0.01 ± 0.05 (13)</td>
</tr>
<tr>
<td>$\langle G_s \rangle_{ds}$</td>
<td>0.02 ± 0.03 (74)</td>
<td>0.02 ± 0.03 (48)</td>
<td>-0.01 ± 0.04 (27)</td>
<td>0.06 ± 0.05 (21)</td>
</tr>
<tr>
<td><strong>Azimuthally Restricted Average</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\langle G_s \rangle_{un,az}$</td>
<td>-0.12 ± 0.04 (21)</td>
<td>-0.18 ± 0.05 (10)</td>
<td>-0.18 ± 0.05 (10)</td>
<td>⋯ (0)</td>
</tr>
<tr>
<td>$\langle G_s^* \rangle_{un,az}$</td>
<td>0.09 ± 0.07 (7)</td>
<td>0.12 ± 0.09 (5)</td>
<td>-0.06 ± 0.08 (1)</td>
<td>0.20 ± 0.09 (4)</td>
</tr>
<tr>
<td>$\langle G_s \rangle_{az}$</td>
<td>-0.11 ± 0.03 (28)</td>
<td>-0.16 ± 0.04 (15)</td>
<td>-0.15 ± 0.05 (11)</td>
<td>-0.20 ± 0.09 (4)</td>
</tr>
<tr>
<td><strong>Latitudinally Restricted Average</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\langle G_s \rangle_{un,lt}$</td>
<td>-0.15 ± 0.04 (24)</td>
<td>-0.22 ± 0.03 (11)</td>
<td>-0.21 ± 0.03 (10)</td>
<td>-0.30 ± 0.09 (1)</td>
</tr>
<tr>
<td>$\langle G_s^* \rangle_{un,lt}$</td>
<td>0.09 ± 0.13 (2)</td>
<td>0.09 ± 0.13 (2)</td>
<td>⋯ (0)</td>
<td>0.09 ± 0.13 (2)</td>
</tr>
<tr>
<td>$\langle G_s \rangle_{lt}$</td>
<td>-0.15 ± 0.04 (26)</td>
<td>-0.20 ± 0.03 (13)</td>
<td>-0.21 ± 0.03 (10)</td>
<td>-0.15 ± 0.10 (3)</td>
</tr>
<tr>
<td><strong>Azimuthally and Latitudinally Restricted Average</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\langle G_s \rangle_{un,az,lt}$</td>
<td>-0.16 ± 0.04 (17)</td>
<td>-0.22 ± 0.04 (8)</td>
<td>-0.22 ± 0.04 (8)</td>
<td>⋯ (0)</td>
</tr>
<tr>
<td>$\langle G_s^* \rangle_{un,az,lt}$</td>
<td>0.23 ± 0.08 (1)</td>
<td>0.23 ± 0.08 (1)</td>
<td>⋯ (0)</td>
<td>0.23 ± 0.08 (1)</td>
</tr>
<tr>
<td>$\langle G_s \rangle_{az,lt}$</td>
<td>-0.16 ± 0.04 (18)</td>
<td>-0.22 ± 0.03 (9)</td>
<td>-0.22 ± 0.04 (8)</td>
<td>-0.23 ± 0.08 (1)</td>
</tr>
</tbody>
</table>
...the results for the latitudinal restriction are consistent with our initial interpretation that the sector lengths may be a measure of the amplitude of the current sheet waves. The latitude restriction selects a subset of the $NN$ data (see Figure 8) in which the Voyager 1 fluxes in longer sectors are generally lower than the Voyager 2 fluxes in shorter sectors, an effect which is consistent with Voyager 1 being more distant from a local flux intensity maximum at the current sheet than Voyager 2. The complementary subset of $NN$ data eliminated by the latitude restriction, i.e., those days with Voyager 2 sectors longer than Voyager 1 sectors, is consistent with Voyager 2 being further from the current sheet than Voyager 1.

Under restricted interplanetary conditions our measurements during the period from mid-1981 until mid-1983 are consistent with the interpretation that there exists a small, negative latitudinal gradient with respect to the heliospheric current sheet in the outer solar system as would result from the presence of local intensity minima symmetrically displaced from the current sheet in the two hemispheres. Further studies are required to determine whether such gradients are typical of other time periods.

Our results for the latitudinal gradient can be most directly compared with the gradient derived from single-point observations by experiments on IMP 8 at 1 AU reported by Newkirk et al. [this issue] and summarized in Table 4. Although exact quantitative comparison is not straightforward because of the different measuring techniques, it does appear that there are no large differences in these "angular" gradients, even though measured in subsequent 11-year solar cycles and at different radial locations. Understanding the implications of this similarity for the relative importance of drifts and perpendicular diffusion requires further consideration of the dependence of model calculations on these factors.

Discussion

A number of features have not yet been addressed by theoretical modeling or by most of the experimental studies. Those features, which may have considerable and as yet unknown effects on our understanding of drift-dominated cosmic ray transport, are the effects of complicated current sheet topologies, variable solar wind speeds, and large-scale magnetic field intensity perturbations. For example, high-speed solar wind streams restructure the interplanetary medium by overtaking and interacting with slower speed solar wind as they propagate outward from the sun, generating corotating interaction regions (CIRs) [e.g., Smith and Wolfe, 1979] or merged

---

**TABLE 4. Recent Estimates of Cosmic Ray Angular Gradient**

<table>
<thead>
<tr>
<th>Study</th>
<th>$r$, AU</th>
<th>Time Period</th>
<th>Energy Threshold, MeV</th>
<th>Median Rigidity, GV</th>
<th>Gradient</th>
</tr>
</thead>
<tbody>
<tr>
<td>Newkirk et al. [this issue]</td>
<td>1</td>
<td>1974–1977</td>
<td>106</td>
<td>0.9</td>
<td>$G_{106} = -0.4%/\text{deg}$ ($-23%/\text{AU}$ at 1 AU)</td>
</tr>
<tr>
<td>This study</td>
<td>$\sim12$</td>
<td>1981–1983</td>
<td>75</td>
<td>1.6</td>
<td>$G_{1.6} = -0.2%/\text{deg}$ ($-1%/\text{AU}$ at 12 AU)</td>
</tr>
</tbody>
</table>

Measurements of cosmic rays with kinetic energies greater than energy threshold.
interaction regions [e.g., Burlaga et al., 1983; Burlaga, 1984]. The effect of the presence of CIRs on cosmic ray transport has been addressed in a number of studies [e.g., Morfill et al., 1980; Duggal et al., 1981; Thomas and Gall, 1982; Newkirk and Fisk, 1985], with quite different interpretations. Most sector boundaries in the outer solar system are expected to be embedded in CIRs (see, for example, the discussion of Figures 7–9 by Thomas and Smith [1981]) or in merged interaction regions [e.g., Burlaga et al., 1985], so that their presence at each of our sector boundaries is implicit, and therefore we have not specifically addressed effects due to the interaction regions observed by the Voyager spacecraft during this period [Burlaga et al., 1985]. As Voyager 1 continues to rise in heliographic latitude and as the sun approaches a new period of minimum activity, the effects of CIRs on cosmic rays should be monitored closely in order to detect any changes as the spacecraft encounters the heliospheric current sheet less frequently. In addition, CIRs both with and without embedded current sheets should be incorporated into the three-dimensional model calculations in order to further investigate the relative importance of CIRs and current sheets on measurements of the type presented in this paper.

CONCLUSIONS

We have combined measurements of the interplanetary magnetic field and fluxes of >75-MeV protons at the Voyager spacecraft in the outer solar system from mid-1981 to mid-1983 to derive \( G_{\alpha} \), an estimate of the latitudinal gradient of cosmic ray intensity with respect to the heliospheric current sheet. We find (1) results consistent with a zero gradient when the magnetic field is disturbed and magnetic field sectors are not well defined and (2) a statistically significant result \( \langle G_{\alpha} \rangle = -0.22 \pm 0.03 \%/\text{deg} \) when the solar wind and particle fluxes are undisturbed by Forbush decreases and solar flares and when sectors are well defined or only moderately disturbed. The result for undisturbed times indicates a net decrease in cosmic ray intensity with increasing distance from the heliospheric current sheet in the outer solar system during the present portion of the 22-year solar magnetic activity cycle. Our result is qualitatively consistent with various aspects of predictions for \( \sim 1\)-GV protons from a three-dimensional model of heliospheric particle transport including drift, in which the current sheet organizes cosmic ray flux, and is in general agreement with the experimental results of Newkirk et al. [this issue] for cosmic rays at 1 AU. It is important both to improve the model calculations and to extend the measurements to solar minimum conditions, when the interplanetary medium should have the simplest structure.

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