An Experimental Study of Centrifugal-Pump Impellers

By A. J. Acosta and R. D. Bowerman

Experimental investigations were made on four two-dimensional impellers and on a well-designed commercial three-dimensional Francis impeller. The over-all performance of each of these impellers was measured and internal-energy loss and pressure-distribution data were also obtained for several impellers. The exit angle of the two-dimensional impellers was fixed and the inlet angle was systematically varied. However, the hydraulic characteristics of these impellers were all found to differ, the source of the variation being in the various loss distributions and hence internal flow patterns in the impellers. The two-dimensional and three-dimensional impeller-loss distributions were also different. The Francis-impeller performance agreed better with potential theory than that of the two-dimensional impellers, and it is concluded that the different loss distributions of the two types are responsible.

Nomenclature

The following nomenclature is used in the paper:

- \( A \) = area
- \( C \) = absolute velocity
- \( C_n \) = pressure coefficient = \( p_{2} - p_{1}/\rho U_{2}^2/2 \)
- \( H \) = head, ft
- \( H_d \) = head developed by impeller
- \( Q \) = flow rate, \( ft^3/sec \)
- \( T \) = torque
- \( U \) = tangential velocity of impeller (\( ft/sec \))
- \( W \) = relative velocity
- \( g \) = gravitational constant
- \( p \) = pressure
- \( r \) = radius
- \( z \) = axial co-ordinate
- \( \alpha \) = angle of attack
- \( \beta \) = vane angle
- \( \zeta \) = loss coefficient = \( p_T - p_1/\rho U_{1}^2/2 \) (measured in relative flow)
- \( \eta \) = efficiency = \( \phi \) \( \zeta \)/\( \tau \)
- \( \theta \) = angular co-ordinate
- \( \rho \) = density
- \( \sigma \) = Thoma cavitation parameter = \( \frac{\text{inlet total head minus vapor pressure}}{\text{developed head}} \)
- \( \phi \) = bow-rate coefficient = \( Q/\rho A_2 U_2 = C_{m2}/U_2 \)
- \( \tau \) = torque coefficient = \( T/\rho A_2 U_2^2 A_2 \)
- \( \psi \) = head coefficient = \( H/U_2^2/\rho g \)
- \( \phi' \) = input head or work coefficient = \( \tau/\psi \)
- \( \omega \) = angular speed

Subscripts

- \( d \) = developed head
- \( e \) = design point for impeller
- \( l \) = loss
- \( m \) = meridional (or radial) component
- \( s \) = static pressure
- \( T \) = total pressure (or head) in impeller inlet
- \( t \) = total pressure (or head) at any other location
- \( u \) = tangential component
- \( 1 \) = impeller inlet
- \( 2 \) = impeller exit

Introduction

This paper summarizes experimental work on centrifugal-pump impellers carried out by the hydraulic machinery group of the Hydrodynamics Laboratory over a period of about three years. Some of the work discussed herein has been reported already as individual investigations by this project (1, 2, 3, 4). This paper embodies these earlier results together with more complete and recent investigations.

In the past, industry has developed a line of highly efficient pumps by considering only gross effects by a one-dimensional theory and then resorting to empirical development based on many years of experience in order to obtain acceptable designs. This procedure is partly justified by the fact that there is little actually known about the internal flow in pump passages even though the body of fluid-dynamic theory is available and applicable. The problem of turbomachine design (and in particular centrifugal-pump design) is complicated by the fact that only a relatively few of the factors involved can be included in a practical mathematical or analytical solution. However, the basic difficulty facing any rational analysis has been the lack of knowledge of the important internal-flow details. Thus in most instances the general applicability of analytical results must be left open until sufficient experimental evidence is available.

One of the objectives of an experimental program on pump-impeller research must be to obtain a sufficient amount of information on the internal and over-all flow characteristics so that their main features become clear and are understood. Although such knowledge may only substantiate design practices developed by experience, this result would in itself be of considerable interest. Moreover, this type of information, which is not generally available, makes possible, through the knowledge of the experimental coefficients found, extension of designs into new fields of application.

The preceding discussions outline the motivation for the work reported herein. A series of experiments was conducted on four "two-dimensional" impellers in which the inlet angle was the only variable. These data include head, torque, and efficiency measurements in addition to internal loss, velocity profiles, and pressure distributions. As an aid in the qualitative description of the flow, photographic techniques also were used.

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Meridian cross-section profiles of impellers range from those of the very narrow width, radial flow, through the Francis or mixed-flow type of impeller sections built on cones, and ultimately to the straight axial profile. Attention in the present work has been confined to that of the "three-dimensional" or Francis impeller in which the meridian flow is generally curved but leaves radially. The flow pattern for such geometries is quite complex, so, in order to reduce the variables involved, "two-dimensional" impellers were made. These test impellers have plane, annular shroud shapes with a fairly quick transition from the axial to radial direction at the inlet. Such shapes are of limited practical application; however, they are of value in experimental work because of the relative ease of observation and measurement offered. Thus, in order to complete the investigation, additional work was carried out on a "three-dimensional," high-efficiency, commercial impeller with similar operating characteristics, and the results compared with those of the two-dimensional experiments.

DESCRIPTION OF LABORATORY FACILITIES, INSTRUMENTATION, AND IMPELLERS

Facilities. A detailed description of the laboratory facilities may be found in references (1) and (2) so that only the salient features will be mentioned here. The test facility consists of a closed hydraulic circuit using water as the fluid medium with a circulating pump, venturi flowmeters, and a system of piping to distribute the flow to any one of three test basins in which the experimental models can be installed. Although the flow may be made to circulate in either direction through the test basin, for pump work the circuit is arranged so that flow approaches the impeller axially and leaves radially, discharging into the test basin at atmospheric pressure. The impellers are driven by a vertically mounted d-e dynamometer which is equipped with an accurate speed control. Fig. 1 shows the impeller and test-basin arrangement and Fig. 2 is a view of the experimental setup.

Impellers. In this program two types of impellers were used; namely, a two-dimensional design with parallel shrouds and a well-designed commercial three-dimensional or Francis-type runner. A series of four of the two-dimensional impellers was used, each of which had the shroud-inlet design shown in Fig. 3. The unconventional shape of the eye resulted from a desire to have a symmetric flow at the vane-inlet edges. These impellers form a series

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Fig. 1 CROSS SECTION OF IMPELLER AND TEST-BASIN ASSEMBLY

Fig. 2 VIEW OF EXPERIMENTAL SETUP

Fig. 3 CROSS SECTION OF TWO-DIMENSIONAL IMPELLER
of similar designs all with the same radius ratio, breadth, and exit-vane angle but with systematically varied inlet angles.

In order to obtain a smooth and systematic variation of blade angle from inlet to exit, it was first assumed that the relative flow followed the blade shape exactly (i.e., an infinite number of vanes) and then the growth of the whirl or tangential component in the absolute flow was specified. In this particular case a linear variation was chosen. Even though it was realized that the foregoing assumption is incorrect, at least the resulting vane shapes are not completely arbitrary, and furthermore this procedure obviates shapes with excessive curvature. The various impeller geometrical constants are given in Table 1. Inasmuch as only the impeller-inlet angles are different for the four runners, they will be designated by these values throughout the text.

### TABLE 1 IMPELLER GEOMETRICAL AND DESIGN CONSTANTS

<table>
<thead>
<tr>
<th>Inlet angle $\beta_i$ (impeller designation), deg.</th>
<th>Two-dimensional</th>
<th>Three-dimensional</th>
</tr>
</thead>
<tbody>
<tr>
<td>20</td>
<td>17</td>
<td>14.5</td>
</tr>
<tr>
<td>23.5</td>
<td>23.5</td>
<td>23.5</td>
</tr>
<tr>
<td>0.086</td>
<td>0.086</td>
<td>0.086</td>
</tr>
<tr>
<td>0.117</td>
<td>0.110</td>
<td>0.083</td>
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<tr>
<td>6</td>
<td>6</td>
<td>6</td>
</tr>
<tr>
<td>10.30</td>
<td>10.30</td>
<td>10.30</td>
</tr>
</tbody>
</table>

$^a$ Suction shroud values.

**Impeller Manufacture.** The shape of the two-dimensional impeller series made fabrication particularly simple. The top shrouds were turned from lucite to permit photographic and visual observations to be made, and the bottom shroud was black anodized aluminum. The vanes were rolled to shape from $\frac{1}{16}$-in. 2-8 aluminum sheet, or from brass sheet in some cases, and were recessed in slots milled in the shrouds, six equally spaced vanes being employed in each case. The resulting impeller assembly was held together with $\frac{1}{16}$-in. through-bolts at the exit edge of the individual blades. For reasons of economy, two sets of slots were installed in each of two sets of shrouds, the unused slots being walled-in during operation. An assembled impeller is shown in Fig. 4.

**Test Setup.** The impeller was installed in the basin as shown in Fig. 2. Since only low rotative speeds were used, sealing was not a problem and in all cases running clearances of about 0.010 in. were found to be satisfactory. The flow from the impeller discharges into a set of parallel diffuser shrouds which serve to guide the flow and eliminate exterior disturbances.

In operation, the water surface was maintained slightly above the level of the impeller. The impeller was operated at a constant speed of 225 rpm. The flow rate was regulated by a manual throttle valve in the suction line and the speed-controlled circulating pump.

**Instrumentation.** Two types of information were sought in this work; namely, the over-all operating characteristics, i.e., head, torque, and flow rate; also internal flow data, viz., pressure distributions, velocity, and total head-loss profiles.

(a) **Flow Rate.** The volume flow rate was established and measured by any one of the three venturi meters available and a differential mercury manometer.

(b) **Torque.** The reaction torque of the motor case was balanced by graduated weights connected to the dynamometer torque arm by means of a wire and pulley system. A Statham electric strain gauge attached to the arm was used as an indicator for the null position. Mechanical stops limit the motion to a few thousandths of an inch and protect the gauge. The strain gage output was read by an optical galvanometer. Thus the procedure consisted of balancing the torque with small weights until the null position was achieved. This arrangement allows torque to be measured with zero displacement, thus minimizing bearing friction. The resultant sensitivity of the system was about $\frac{1}{5000}$ of the full-scale reading. With the relatively small torques measured in these tests (1.5 ft-lb max), vibration was found to be a problem so that to improve accuracy several readings at each operation point were taken and averaged.

With the setup employed, the zero reading was fairly large. In particular, the bearing friction and water drag on the shroud surfaces were large and as they took no part in the pumping operation their corresponding torques were treated as a tare.

(c) **Head.** The head developed by the impeller was measured with a water-air manometer and total-head probes, one being installed in the impeller inlet, or eye, and the other mounted at the impeller discharge. Both simple impact probes and Kiel venturi-type total-head probes were used at the impeller exit and were usually installed only $\frac{1}{16}$ in. away from the vane tips.

(d) **Internal-Flow Measurements.** All of the internal-flow measurements consist of pressures [except the photographic observations (1)] and hence a device to measure these pressures quickly and easily is necessary. For the work in this laboratory it was found to be expedient to use a manometer attached to and rotating concentric with the impeller (3, 4). The manometer employed consisted of thirty 6-mm tubes about 18 in. long with a common manifold to all tubes. One tube was reserved for a reference pressure (which was taken to be the inlet total head) and others were connected to various static or total-head piezometer connections. Thus, with a maximum economy of effort, static-pressure distributions, relative velocities, and relative "energy losses" could be found.

Static piezometer taps in the vane surfaces were installed by drilling down the breadth of the vane to an 0.030-in. perpendicular...
Fig. 5 HEAD COEFFICIENT, TORQUE COEFFICIENT, AND EFFICIENCY VERSUS FLOW-RATE COEFFICIENT FOR TWO-DIMENSIONAL IMPELLERS. IMPELLERS, (A) 20°, (B) 17.5°, (C) 15°, (D) 12.5°
lar hole and by soldering \( \frac{1}{16} \)-in. brass tubing into vertically milled slots on the vane surface before it was bent to the proper contour. Both methods were found to be practicable.

Relative velocity heads were obtained with \( \frac{1}{16} \)-in. simple impact probes mounted in the impeller passages and directed into the relative flow. In order to prevent flow asymmetry, such tubes usually were distributed throughout all of the passages.

It should be noted that the rotating manometer does not give the static-pressure distribution directly and that, in order to obtain it, the centrifugal effects in the connecting tubing must be accounted for (Appendix 2).

(e) Flow Visualization. The light shrouds of the test impellers permit both visual and photographic observation, as described in reference (1). Briefly, these techniques consist of injecting immiscible liquid globules into the flow and observing their subsequent history either in the relative or absolute reference frames. Both motion pictures and multiple-flash exposures on a single plate were taken. Some use also was made of stroboscopic photography.

Flow visualization by these methods has been found extremely valuable for qualitative exploratory investigations and provides a necessary complement to the internal flow measurements.

(f) Accuracy. Both the flow rate and speed were capable of being measured with an error of less than \( \frac{1}{2} \) per cent. However, owing to the large tare, torque values were only known to within 1.5 per cent or so. The greatest difficulty was experienced in the determination of the pump head. Since the head reading varied somewhat over the passage height and depended also on the distance away from the impeller exit, there is some question as to what value of "head" should be used. The over-all accuracy of the performance measurements is thus about 3 to 4 per cent, depending somewhat on the value of the head.

Most of the relative measurements cannot be determined accurately. Instrumentation errors, manometer errors, and so on, probably are within 2 per cent for the most part and such variation would be typical of the pressure-distribution results also. Flow asymmetries, incorrect angles on the relative total head tubes, and the like, could cause additional errors that are quite difficult to detect.

Experimental Work

Complete characteristic diagrams for the four two-dimensional impellers are presented in Fig. 5 in terms of the dimensionless developed head coefficient \( \psi_d \), torque coefficient \( \tau \), flow-rate coefficient \( \phi \), and efficiency \( \eta \). As mentioned in the preceding paragraphs, there is some arbitrariness in the definition of the impeller head. In particular, it was found that the distance between the discharge total-head probe and the impeller periphery was important. Fig. 6 shows this variation with the probe \( \frac{1}{16} \) and \( \frac{5}{8} \) in. from the impeller exit. The major difference is seen to occur at flow rates less than the design point. At such low flow rates, considerable mixing, and other real fluid effects can come into play since the path lines between the impeller and probe are long, flat spirals. Thus, in the rest of this work the \( \frac{1}{16} \)-in. position was used as a standard. Any additional losses due to
equalization and mixing of the flow are therefore not counted in the determination of head or efficiency.

For purposes of comparison, the developed head is plotted versus flow rate for all four impellers (Fig. 7) and efficiency versus flow rate in Fig. 8. Fig. 9 shows the "input" head or work coefficient $\psi' = \psi_d/\eta$ versus $\phi$ for the four impellers together with a theoretical estimate (6). Similar data also were taken on the three-dimensional impeller studied and are shown in Fig. 10. Performance data for other similar three-dimensional impellers may be found in reference (2).

The design flow rate for the two-dimensional impellers is designated by $\phi_d$ in Figs. 7 to 9 and was obtained by making the inlet relative-flow angle equal to the inlet-vane angle with the assumption that there is no prewhirl. It is realized that this procedure is inaccurate for potential flow (5, 6) but as the basis of a comparative study it should suffice. Typical inlet and outlet-velocity triangles for a pump are shown in Fig. 11.

Pressure-distribution data on the blade surfaces were obtained only for the 20 and 12.5-deg impellers. A typical piezometer-tap drilling schedule for the 20-deg impeller is shown in Fig. 13 and the static pressure distributions are given in Figs. 14 and 15.

Viscous and real fluid effects are most readily shown by contour plots of energy loss or defect. It can be shown (Appendix 2) that the head difference between any total-head tube in the relative flow and the inlet total head as read on the rotating manometer represents a loss of energy in the flow due to friction. In the remainder of this paper "loss" refers to loss of relative total head; i.e.

$$p/\rho g + \frac{1}{2} W^2$$

Energy-loss contours are given in terms of the per cent of input head or work coefficient for the 20-deg impeller for various flow rates at the exit section of the passage (Fig. 16), for the 15-deg impeller at the exit and mid-radius position (Fig. 17), and for the 12.5-deg impeller at three locations; i.e., exit (Fig. 18), mid-radius (Fig. 19), and inlet (Fig. 20). Static-pressure distributions between the vanes along top and bottom shrouds also were taken...
for the 12.5-deg impeller, so that with the aid of the loss coefficients relative velocities in the passage section could be computed. Velocity profiles across the height of the passage and for several positions between the vane tips are given for the 12.5-deg impeller at three radial stations in Fig. 21.

Similar data also were taken for the three-dimensional impeller. Loss contours at the exit are shown in Fig. 24 and at the inlet in Fig. 25. Relative velocity computations also were made at the exit section, but owing to the high curvature of the meridional flow at the inlet, static pressures could not be measured there, hence velocities could not be determined.

The three-dimensional impeller performance was obtained with a setup quite similar to that of the other impeller (Fig. 2), i.e., with plane annular diffuser shrouds. However, the exit-loss measurements had to be made without the top shrouds. Additional work also was done on the effect of these shrouds by removing the bottom shroud as well.

The results of these tests and their interpretation will be discussed in the following section.

**Discussion**

**Two-Dimensional Impellers**

*Over-All Characteristics.* It is immediately clear from the plots of head versus flow rate for the four impellers in Figs. 7 and 9 that the inlet angle has a profound effect upon the entire characteristic. In general, the best efficiency point is seen to move to the left (Fig. 8) for the reduced inlet angles, as would be expected. At relatively high rates of flow ($\phi = 0.1 - 0.12$) larger heads are seen to be developed for the high inlet angles than for the smaller ones, and the slope of the $H-Q$ curve progressively steepens as the inlet angle is reduced. The developed head for all impellers is seen to be more or less the same at about $\phi = 0.06$, indicating that in this region the flow does not depend much on the inlet angle.

One should not assume that the losses which occur away from the best efficiency point are solely responsible for the variations in performance even though this assumption is commonly found in pump literature (7). A study of the brake horsepower or torque coefficient for the four impellers (Fig. 5) shows that the input work is different for each of them. The maximum peak value goes from about $\tau = 0.061$ for the 20-deg impeller to about 0.051 for the $12^{1/2}$-deg impeller, and the flow-rate coefficient for the maximum decreases from 0.135 to 0.11. The difference between each of these quantities is thus on the order of 20 per cent and from the torque characteristics one can see that attributing the variations in head performance to internal fluid losses cannot alone explain the discrepancies. It should be pointed out also that inlet-blade-angle variations of the magnitude in these tests can only account for about 1 or 2 per cent change in the $H-Q$ characteristic on the basis of potential-flow calculations (10). Also it is of interest to note that in each case the maximum efficiency is seen to fall to the left of the maximum torque.

The design points of these impellers were taken to be the flow rate for shockless entry as calculated by the elementary one-dimensional theory. Vector-velocity triangles for the impeller inlet and outlet are shown in Fig. 11. In order to show the influence of local angle of attack or incidence angle to the blade-inlet edges, the angle of attack for the 90 per cent efficiency range versus flow rate is plotted for each of the four impellers in Fig. 12. The angle of attack for the best efficiency point is seen to vary from the $-2$ deg for the 20-deg impeller to about $11/4$ deg for the 12-deg impeller. From the slope of the 90 per cent envelope it is doubtful whether an impeller with a 10-deg inlet angle would ever achieve this efficiency. Again, this observation is taken to be a result of operation at extremely low flow-rate coefficients and not primarily a result of the inlet angle. This effect also shows up in the fact that the ratio of the high-efficiency operating range to the design flow rate is smaller for the low angles than the larger ones. If the inlet angle of attack were the sole criterion, this ratio should increase as the inlet angle is reduced.

*Correlation With Potential-Flow Theory.* In Figs. 7 and 9 are shown theoretical $\psi-\phi$ curves computed on the basis of potential-flow theory (6). Although these ideal characteristics were determined for logarithmic spiral vane shapes, small perturbations in inlet angle do not affect the $\psi-\phi$ characteristic materially. The outstanding feature on both of these figures is the rather large discrepancy in slope between the ideal performance and both developed and input heads. The same phenomenon also was noticed in reference (5) in which a series of experiments was conducted on 30-deg log-spiral, two-dimensional impellers. In this work the discrepancy was attributed to the influence of the inlet boundary layer arising from the sharp turn.

In Fig. 9 it is seen that the design points of the four impellers all fall nearly on the computed characteristic. The experimental $\psi-\phi$ curves must intersect the ideal $\psi-\phi$ characteristic at some flow rate. However, the coincidence of the design $\psi'$ values with the computed characteristic must be regarded as fortuitous, at least for the present. This question will be considered again when the three-dimensional impeller results are discussed.

**Pressure-Distribution Measurements**

Knowledge of the static-pressure distributions on the vanes gives a direct measurement of the vane loading and hence evaluation of the design of the blade shape. Pressure-distribution measurements on the 20-deg impeller were first reported in reference
In both Figs. 14 and 15 it is seen that the pressure distributions of leading curves near the design point are relatively smooth and show no unusual reversals. This fact is, no doubt, a consequence of the smooth curvature of the vanes, and supports the contention that for radial-flow machinery, the exact blade design is not of paramount importance provided abrupt changes in curvature are avoided, and that the blade angle smoothly increases or decreases.

"Shockless" Flow Rate. As mentioned before, the design points of these impellers were chosen so that the relative flow would stream smoothly onto the leading edge with no velocity discontinuities. The flow rate for this operating condition is termed "shockless entry" in the pump literature. For the 20-deg impeller the nearest approach to shockless entry occurs about \( \phi = 0.110 \), whereas according to the simple theory, shockless entry should occur at \( \phi = 0.117 \). Thus, shockless entry occurs at a flow rate greater by 20 per cent than that computed on the basis of the infinite-vane theory. According to potential-flow calculations (6, 10) the shockless flow rate for this impeller geometry should be 32 per cent greater than that based on the infinite-vane theory. It seems reasonable that boundary-layer blockage and other real fluid effects could account for the discrepancy between this and the observed value. Similar results also were observed in reference (5) in experiments conducted on impellers with 30-deg log-spiral vanes.

The pressure-distribution measurements of Fig. 15 on the 121/2-
deg impeller show that shockless entry is about at \( \phi = 0.06 \), whereas the design calculations were for \( \phi = 0.007 \). This result does not fall on the trend established by the 20-deg impeller (5) or the theoretical predictions. As previously pointed out, real fluid effects become of increasing importance for such low flow coefficients, and the different behavior is attributed to this effect.

**Loading Distribution.** At or near the shockless-entry operating point it is clear from the head-flow rate characteristic that the vanes of the 12.5-deg impeller are considerably less loaded than those of the 20-deg impeller. The fact is reflected in the pressure-distribution diagrams which are slimmer and more elongated for the smaller angle. As previously noted, the load distributions for both of these impellers is 'reasonable' near shockless, indicating that as long as the change in angle from inlet to outlet is not rapid and continuously increases (or decreases), any blade design should be satisfactory. This observation is mainly qualitative and is principally intended to point out the difference in importance that the vane shape has for axial and radial pumps. It will be shown later that the 12.5-deg impeller, although having a smooth increase in vane angle, does have certain undesirable internal-flow features as compared with the 20-deg impeller.

At flow rates less than shockless entry, large velocity discontinuities are seen to appear at the inlet on both impellers. In a similar fashion at high flow rates, the distributions on the two faces intersect and cross over.

**Operation at Low Flow Rates.** At shockless entry there is a stagnation point at the leading or inlet edge of the blade. As the flow rate is reduced, it is evident from the pressure distributions and also from physical considerations that the stagnation point moves onto the leading or pressure face of the blade. This point continues to move away from the inlet edge toward the outlet as the flow rate is reduced until shut-off has been reached. The final position of the stagnation point depends upon the blade angle, radius ratio, and so on. Thus, whatever the particular design, back flow can occur over a considerable extent of the pressure side of the blade at low flow rates. Such back flows are not conducive to high efficiency or stable operation. The excessive path length and highly unfavorable pressure gradient that must exist may cause large-scale separation and other real fluid effects. At shut-off these effects become even more predominant. Motion pictures show that, in general, the fluid in the inner portions of the impeller rotates like a solid body and that an irregular pulsating rotation opposite to the direction of impeller rotation occurs at the exit.

The foregoing sequence of events which occur as the flow rate is lowered, as determined by motion pictures, is that a separation zone appears first on the suction side of the blade. With a further decrease in flow rate, alternate passages are seen to 'stall out' completely, the flow then being much like a solid body rotation. The stalled pattern seems to be stable with respect to the impeller and does not propagate around the periphery as is observed in axial-flow compressors (11). This situation occurs at about a flow rate of \( \phi = 0.05 \) or so and can be verified by the pressure distributions taken in alternate passages on the 20-deg impeller shown in Fig. 14. This configuration remains until the flow rate becomes very low, and finally near shut-off all the passages stall out with the inner portions rotating like a solid body. Near the exit there is a large-scale irregular eddy rotating in the opposite sense to the impeller direction. The pressure distributions for \( \phi = 0 \) are shown in Figs. 14 and 15. It can be seen that at the inlet the static pressure is near zero and is considerably below the forced vortex line, indicating that there is little or no rotation of the fluid in the impeller eye. From the inlet edge to about \( r/r_2 = 0.8 \) the pressure is distributed like that of rigid-body rotation and the small loop in the discharge portions represents the work going into the eddy maintained at the exit.

**Cavitation Susceptibility.** The knowledge of the pressure distributions permits one to make some estimation of the cavitation susceptibility of an impeller. In terms of the pressure coefficient \( C_p \), it can be shown that the value of Thoma's \( \sigma \) for the inception of cavitation is

\[
\sigma_{\text{inception}} = \frac{C_p(\text{min})}{2 \psi}
\]

where \( \psi \) is the head coefficient. For the 20-deg impeller near the design flow rate \( \phi = 0.117 \) this becomes [Graphs and diagrams related to the text]
Fig. 15 Static-Pressure Distributions on Vanes of 12.5-Deg Impeller for Several Flow Rates
shockless, the absolute value of the minimum pressure continues and at shockless entry comes slightly positive. This from the shape of the pressure curves one than prevent cavitation as the flow is reduced (7).

It is interesting to note that as the flow rate is reduced from shockless, the absolute value of the minimum pressure continues to increase and the values of \( \sigma_{\text{incept}} \) increase. However, when stall is encountered, \( |C_{p,\text{min}}| \) decreases and near shut-off even becomes slightly positive. This means that lower absolute pressures are required for cavitation inception at very low flow rates than at the design points. This situation is in contrast to that of the axial-flow pump which requires increasing suction pressure to prevent cavitation as the flow is reduced (7).

Unfortunately, the knowledge of the noncavitating pressure distribution tells nothing of the performance during cavitating conditions or of cavitation “breakdown” or choking. However, from the shape of the pressure curves one can make some rough deductions: At or near shockless entry the pressure distributions are smooth and the pressure is nearly constant on the suction side. If this pressure is below the known vapor pressure of the liquid, the fluid must boil or cavitate. For a first approximation, the work represented by the area between the vapor-pressure line and pressure loop is not put into the flow as head. An inspection of these distributions at low flow rates shows that there are quite sharp pressure peaks of small area. Hence, one would infer that less head may be lost when cavitating under circumstances than at shockless, although cavitation inception occurs sooner.

According to these ideas, serious cavitation from the standpoint of head loss would not occur before \( \phi = 0.08 \) or so at a flow rate coefficient of \( \phi = 0.117 \) for the 20-deg impeller. For the given characteristics of this impeller, this value agrees with the expected cavitation performance.4

Loss Contours. The internal velocity and relative total-head profiles probably give the best indication of the location and magnitude of real fluid effects possible with the experimental setup. The energy-loss contours at the exit section for the 20-deg impeller (Fig. 10) give a qualitative idea of the distribution of these effects for various flow rates. In these and the following contour plots, the loss in relative head is expressed as a fraction of the total developed head. It can be seen that up to and somewhat beyond the design point the regions of high loss are concentrated on the trailing (suction) side of the vane. At higher flow rates, the low-loss fluid moves over to the leading (pressure) side of the passage in accordance with the adverse negative angle of attack existing then at the vane-inlet edge.

Loss contours are also shown for the 15-deg impeller at a high flow rate (about 70 per cent greater than design) midway through the passage \( (r/r_2 = 0.75) \) and at the exit (Fig. 17). The high rate of flow is responsible for gross separation and flow detachment seen in the loss contours at mid-radius.

It is well known that such nonuniformities in relative total head give rise to circulating or secondary flows perpendicular to the main stream direction. Such evidence is offered by the outlet survey of Fig. 17 which shows how the areas of high-loss fluids have been distorted and displaced toward the trailing or suction side of the passage.

More extensive loss data are shown in Figs. 18 to 20 for the 12.5-deg impeller. Fig. 18 shows loss contours at the exit \( (r/r_2 = 1.00) \) at various flow rates. A difference between these distributions and those of the 20-deg impeller is immediately clear; namely, that a zone of large energy loss is always located next to the trailing side of the vane, even for flow rates about 60 per cent greater than the design. In fact, the percentage loss continuously increases with flow rate starting at the lowest value of \( \phi = 0.018 \). The inner surveys \( (r/r_2 = 0.73) \) of Fig. 20 shows, in general, a thick region of relative energy defect on the trailing side of the passage and on the bottom shroud. These loss distributions remain more or less unchanged until the flow rate exceeds about \( \phi = 0.072 \). At flow-rate coefficients greater than this value, high loss areas are seen to occur on the pressure face of the vane. The pressure-distribution data, Fig. 15, for these flow rates show the static-pressure curves on leading and trailing-blade surfaces of the inlet crossing over at about this flow rate, so that unfavorable incidence angles occur at the inlet. Any further increase in flow rates results in regions of extreme loss probably associated with local flow detachment.

This sequence of events is roughly followed by the internal surveys at \( r/r_2 = 0.89 \) (Fig. 19) except that, in general, the profiles indicate greater losses near the trailing surfaces and less near the pressure (leading) surface. This behavior may be expected to follow from the general shape of the leading pressure-distribution curves.

Thus, it can be seen that the exit surveys on the 12.5-deg impeller do not follow the trend established by the inner surveys or the 20-deg impeller. The possibility that the flow separates along the trailing side of the vane near the exit immediately suggests itself. The velocity surveys discussed in the next paragraph further support this idea.

Velocity Profiles. From the loss measurements and static-pressure determinations on the impeller top shroud it is possible to calculate the relative velocity in the passage. Fig. 21 presents this information as relative velocity plotted against the channel height for several stations across the passage. An outstanding feature of each of these diagrams is that the velocity profile near

\[ \sigma_{\text{incept}} = \frac{0.3}{(2)(0.5)} = 0.3 \]

\[ \sigma_{\text{incept}} = 0.10 \]

\( \text{As given in reference (7), p. 267.} \)
the suction side of the vane progressively deteriorates from the inner to the outer radial stations. In fact, for all flow rates except the very highest, the velocity distributions near the exit strongly suggest that flow separation occurs near there. The other salient feature of Fig. 21 is the pronounced boundary layer that appears on the lower shroud at the inner radius at a flow rate coefficient of about $\phi = 0.06$. Also interesting is the "inverted" shape of the exit-velocity profiles somewhat above the design point. It would appear that the low-energy regions are being centrifuged out of the impeller. This behavior has been noted before on rotating shrouds with no blades (12), wherein it was observed that a substantially separated main stream could be stabilized and reattached by sufficient shroud rotation.

**Loss Coefficients.** With the velocity profiles having been determined, it became possible to calculate weighted loss coefficients through the impeller. A true loss coefficient would be weighted with the radial velocity to account for variations in work of each fluid stream. Because flow angle was difficult to
measure, the loss coefficients were computed with relative velocity. Consequently, for flow rates much different from the design condition, errors must occur, and the resulting value must be too low. Fig. 22 shows this coefficient for the inlet and exit stations as a function of flow rate. At the design point it is seen that about 60 per cent of the total loss through the impeller has occurred at the inlet station $r/r_2 = 0.73$. It is interesting to note that the inlet loss rises sharply on either side of the design point. The exit-loss coefficient fails to show a rise for flow rates less than $\phi_c$ probably because of the afore-mentioned errors incurred in the weighting procedure. At the design point, however, computation of efficiency by means of the weighted loss coefficients agrees to within a per cent or so with the measured value.

Comparison of Two-Dimensional Impellers. The overall characteristics of the four two-dimensional impellers are similar and show the trends to be expected from the progressive decrease in inlet-vane angle. The internal flow patterns are unquestionably different, however, because of their different torque or brake-horsepower curves (Fig. 5). Qualitative information to this effect is offered by the loss contour plots of the 20 and 12.5-deg impellers. It is seen that, in general, fluid of low energy tends to be concentrated more behind the trailing side of the vane for the 12.5-deg impeller than the 20-deg one for all flow rates. Because of this fact the 12.5-deg impeller actually shows separated profiles near the exit at the design point, whereas the 20-deg impeller showed a much more uniform profile there. The difference is probably due to the excessive vane length of the 12.5-deg runner coupled with a continuous adverse pressure gradient.

It should be noted that separated flow in a pump will have a forced vortex-pressure rise through it rather than constant pressure as would be found on a stationary airfoil or blade of a cascade. The result is to centrifuge the separated region radially outward. Thus, separation in radial-flow machinery will not in general have as deleterious effects as it does in axial-flow machinery.

Three-Dimensional Impeller

Over-All Characteristics. In reference (2) Osborne and More
present complete characteristic data on several “three-dimensional” impellers, and the data on a 17-deg-exit-angle impeller is reproduced in Fig. 10. Fig. 23 shows a profile sketch of the impeller. It is clear from Fig. 10 and those of reference (2) that the three-dimensional characteristics agree much better with the theoretical calculations than do the two-dimensional ones. The fact that the measured head on the 17-deg impeller is slightly higher than the theoretical prediction is not understood at the present time, and in (2) this difference is attributed to real fluid effects. A surprising fact is that the head curves of the 17-deg three-dimensional impeller do not fall off with increasing flow rate as rapidly as do the 23.5-deg two-dimensional impellers. This result appears (as is discussed later) to be due to the differences in inlet loss and velocity distribution of the two impeller types.

**Internal-Loss Distributions.** Loss contours for different flow rates are shown in Fig. 24 at the exit and in Fig. 25 at the inlet. Near and above best efficiency conditions the exit contours indicate a moderate boundary layer on the bottom shroud and some
DIMENSIONLESS RELATIVE VELOCITY, $W/U_2$

**Fig. 21** Relative Velocity Profiles for 12.5-Deg Impeller at Three Radii for Several Flow Rates

(Fraction of passage width, measured from pressure-face of vane: ○ = 0.2, △ = 0.5, □ = 0.8, ◇ = 0.95.)
As mentioned in a foregoing section, the exit measurements were made with the top collecting plate removed as indicated in Fig. 23. This was necessitated by the fact that the impact tubes were attached to the impeller exit by means of small brass blocks that protruded beyond the impeller. The water level in the test basin was normally such that the impeller was submerged with no possibility of air entering the passages. To investigate the influence of the bottom collecting ring, it was removed and the loss data were retaken. Surprisingly enough it was found that "negative" losses occurred over about 1/2 of the passage next to the pressure face of the vane and lower half of the passage for flow rates less than about $\phi = 0.10$. These values were far in excess of what could be accounted for by experimental error and based on $U^2/2g$ have maximum values of about $|\theta_2| = 0.075$.

It is known that if the flow proceeds from the impeller inlet to the exit, the loss must be greater than, or equal to, zero. Hence it is concluded the negative losses arise from an external recirculating flow of higher relative energy. This situation could occur if fluid of small absolute velocity (and thus higher relative total head) would circulate from the region exterior to the impeller discharge along the shrouds to the outer portions of the pressure side of the impeller blade. The flow picture would consist of loose spirals, part exterior and part interior to the impeller. The addition of a lower collecting ring substantially reduces the magnitude and extent of the negative losses. (This relatively small region occurs only for $\phi < 0.065$ and is not shown in Figs. 24.) Presumably, it would be completely eliminated by the addition of a top plate as well.

This matter is of some importance since impellers frequently run in volutes with considerable side clearance. According to these observations the velocity distributions and presumably also the head would be slightly different for such operation.
Velocity Profiles. Static-pressure measurements on the top shroud at the exit of the impeller were made and from these and the loss determinations, relative velocities were computed and are shown in Fig. 26. It was necessary to assume that the pressure was constant across the breadth of the impeller, but this should not introduce serious error into the results.

It can be seen from these figures that for $\phi \geq 0.10$ the velocity distributions are fairly flat between the blades except for a boundary-layer region on the bottom shroud.

Owing to the fact that the inlet portions of the impeller were strongly curved, the static pressure throughout the flow could not be measured. Thus it was not possible to present inlet relative-velocity plots.

Comparison of Two and Three-Dimensional Impellers. Several of the salient differences between the two and three-dimensional impellers have been mentioned already. Among the most important of these is the difference in the head and flow-rate characteristics. In fact, the flow rate for zero head of the 17-deg three-dimensional impeller is higher than any of the 23.5-deg two-dimensional impellers. Furthermore, the slope of the $\psi-\phi$ curve agrees much better with potential theory (as mentioned before) and also is less steep than the two-dimensional results.

The reasons for this behavior may be found in the inlet surveys for the two cases (Figs. 20 and 25). The abrupt turn of the two-dimensional impeller gives rise to the large inlet loss previously mentioned and a large boundary layer on the bottom shroud. This behavior occurs more or less throughout the entire region of good efficiency in the two-dimensional impellers, but for the three-dimensional impeller the inlet performance is seen to be good until the highest flow rate observed. A comparison of the two and three-dimensional exit-velocity profiles is shown in Figs. 26 and 27. It is seen that the two-dimensional runners do not have exit profiles as flat as the three-dimensional one. In view of these facts, the simplest over-all explanation would be that the influence of the boundary layer at the inlet and subsequent formation of a thick retarded zone on the low-pressure side of the vane lower the effective blade angle of the two-dimensional impellers and increase the radial velocity by the blockage of the passage. The direction of both of these effects is the same; i.e., to decrease the head at a given flow rate and to steepen the $\psi-\phi$ curve. These effects are larger for the 12.5-deg impeller than for the 20-deg impeller.

Thus, it is not surprising that steeper head-flow-rate curves
can be exhibited by the two-dimensional impellers. In fact, the influence of inlet angle on the torque characteristics of the two-dimensional impellers has already shown that their effects on internal-flow patterns are large. If, in addition, the head losses encountered at the inlet are considered, it is easy to see why the efficiency of the two-dimensional runners is not only lower but has a sharper peak as well.

In reference (2) experiments were done on two three-dimensional impellers that differed only slightly in the details of inlet construction, and it was found that there were significant differences in performance of the two runners. It was suggested there that large inlet losses were incurred as a result of the relatively minor inlet changes. That such a possibility can occur is borne out in the present paper. Not only can losses occur, but the resulting change in flow pattern alters the basic performance of the machine.

Effect of Volute. The present results are applicable only to impellers and not a complete pump. Because of the effect of the case or volute, there are numerous operational features which are decidedly different between the free impeller and complete pump. However, at the design point and somewhat on either side the influence of the case is not marked (13) and the results of free-impeller tests may be applied there. At flow rates much lower, and particularly much higher than the volute-design point, significant deviations from the free-impeller performance are found.

Conclusions
The principal experimental results are:

1. In the two-dimensional impeller series, the inlet angle affects the entire performance characteristic of the impeller by initiating different flow patterns within the impellers. The differing flow patterns are demonstrated by varying loss distributions and different torque requirements. Such major variations are not indicated by potential theory.

2. The two-dimensional and three-dimensional impeller types have important differences in performance as a result of inlet design. Roughly one half of the total losses of the two-dimensional impeller occur at the inlet, due probably to the sudden turning of the fluid from the axial to the radial direction. The more gradual fluid turning at the inlet of the Francis-type impeller is a more favorable condition.

As a consequence of these effects may be added the following observations:

(a) The performance of well-designed three-dimensional impellers can be predicted closely by potential theory, whereas this cannot be done for the two-dimensional impeller; (b) a higher and broader range of efficiency is found for the three-dimensional impellers; (c) the head flow-rate characteristic of the two-dimensional impellers is steeper than that for the three-dimensional impellers (even for vane angles exceeding the three-dimensional value); (d) with the two-dimensional impeller, as inlet angle is reduced, the flow rate for maximum efficiency decreases with the efficiency value remaining about the same, but the range of flow rates (in percentage) for high efficiency is reduced.

The present experiments, although fairly extensive, do not begin to explain many of the important problems that remain. However, it is hoped that the data and results given will prove to be of some use to designers and experimenters in this field.

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BIBLIOGRAPHY


Appendix I

Blade Design
It is assumed that the fluid is perfectly guided by the blades. The blade shape is then chosen to make the tangential or circumferential component of the absolute velocity increase linearly with radius. Thus, from the velocity triangle (Fig. 11) it can be seen that the equation of the streamlines or blade surface is

\[ \tan \beta = \frac{dr}{rd\theta} = C_m \frac{C_m}{U - C_m} \]  

For constant impeller breadth \( C_m = C_m r_2/r_1 \). The growth of \( C_m \) is now specified as

\[ C_m = K_1 (r - r_0) \omega \]

where \( K_1 \) and \( r_0 \) are constants. Equation [1] can be integrated to obtain

\[ \theta = \frac{U_2}{C_m} \left[ \frac{1 - K_1}{2} \left( \frac{r}{r_2} \right)^2 + K_1 \frac{r_0^2}{r_2^2} \right] \]  

The constant \( K_1 \) is evaluated at the impeller exit by stipulating the blade angle \( \beta_2 \) there; i.e.

\[ C_m = U_2 - \cot \beta_2 C_m = K_1 (r_2 - r_0) \]

or

\[ K_1 = \frac{1 - (C_m/U_2) \cot \beta_2}{1 - r_0/r_2} \]  

The blade-exit angle \( \beta_2 \) of all impellers was chosen arbitrarily as \( \beta_2 = 23.5^\circ \). The four impeller designs were then obtained by selecting \( C_m/U_2 = 0.110 \) with \( r_0/r_2 \) taking the values 0.55, 0.60, 0.65, 0.70, respectively. The inlet-blade angle \( \beta_1 \) is given by

\[ \beta_1 = \cot^{-1} \left[ \frac{1}{0.110} \left( \frac{r_1}{r_2} \right)^2 \left[ 1 - K_1 (1 - r_0^2/r_1^2) \right] \right] \]
The flow rate for "shockless" or smooth entry is designated as the design flow rate \( \phi_d \) and is computed as that value for which the relative flow angle is equal to the blade angle (blade thickness is accounted for in this computation).

A summary of the design constants is given in Table 1.

**Appendix 2**

**Measurement of Loss and Relative Velocity**

The Bernoulli equation in rotating co-ordinates for a frictionless, incompressible flow is

\[
p + \frac{\rho}{2} (W^2 - U^2) = \text{const} = p_T \quad \ldots [5]
\]

If the total pressure \( p_t \) and static pressure \( p_s \) are measured at the same point, then

\[
W = \left( \frac{p_t - p_s}{\rho/2} \right)^{1/2} \quad \ldots [6]
\]

The quantity \( p_t - p_s \) can be read directly on the rotating manometer, or \( p_t \) and \( p_s \) may be read individually as was done in the present experiments.

If the flow is not frictionless, then Equation [5] is modified by the loss in relative total head \( p_t \), i.e.

\[
p_t = p_T - p_t
\]

where the subscripts are defined in notation, thus

\[
p_t + \frac{\rho}{2} (W^2 - U^2) = p_T - p_t \quad \ldots [7]
\]

The quantity \( p_t \) is measured directly on the rotating manometer by comparing the total pressure \( p_t \) with the inlet total pressure \( p_T \) (both pressures being read at the same radius, i.e., the manometer radius).

The loss coefficient is defined as

\[
\tilde{\xi} = \frac{p_t}{\frac{1}{2} \rho U_t^2}
\]

and the static-pressure coefficient is defined as

\[
C_p = \frac{p_s - p_T}{\frac{1}{2} \rho U_t^2}
\]

Then the relative velocity, as a dimensionless quantity, can be calculated by solving Equation [7] with the foregoing substitution of dimensionless coefficients

\[
\left( \frac{W}{U_t} \right)^2 = \left( \frac{r}{r_2} \right)^2 - C_p - \tilde{\xi} \quad \ldots [8]
\]

**Efficiency and Weighted-Loss Coefficient**

It can be shown that the impeller efficiency is

\[
\eta = \frac{\tilde{\psi}_d}{\tilde{\psi}_d + \tilde{\xi}^{1/2}} = \frac{\tilde{\psi}_d}{\tilde{\psi}}
\]

where \( \tilde{\xi} \) is a weighted loss coefficient defined as

\[
\tilde{\xi}_w = \frac{\int \tilde{\xi}_w W \sin \beta \, dA}{\int W \sin \beta \, dA} \quad \ldots [9]
\]

both integrals being evaluated over the discharge area of the impeller. The angle \( \beta \) is the relative flow angle. Since this angle is difficult to measure, it is assumed constant over the passage cross section. This assumption can only be correct near the design or best efficiency point of the impeller. At other flow rates, and in particular low flow rates, the result must be low. In the figures of the report, the loss coefficients are usually expressed as fractions of the head.

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