Microresonator frequency comb optical clock

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Optical frequency combs serve as the clockwork of optical clocks, which are now the best time-keeping systems in existence. The use of precise optical time and frequency technology in various applications beyond the research lab remains a significant challenge, but one that integrated microresonator technology is poised to address. Here, we report a silicon-chip-based microresonator comb optical clock that converts an optical frequency reference to a microwave signal. A comb spectrum with a 25 THz span is generated with a 2 mm diameter silica disk and broadening in nonlinear fiber. This spectrum is stabilized to rubidium frequency references separated by 3.5 THz by controlling two teeth 108 modes apart. The optical clock’s output is the electronically countable 33 GHz microcomb line spacing, which features stability better than the rubidium transitions by the expected factor of 108. Our work demonstrates the comprehensive set of tools needed for interfacing microcombs to state-of-the-art optical clocks.

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1. INTRODUCTION

Optical frequency combs enable extraordinary measurement precision and accuracy entirely commensurate with their reference oscillator. A new direction in experiments is the creation of ultracompact combs via parametric nonlinear optics in microresonators [1,2]. We refer to these as microcombs, and here we report a silicon-chip-based microcomb optical clock that phase-coherently converts an optical reference to a microwave signal.

Optical clocks leverage the narrow, unvarying transitions of atoms to realize exceptionally stable laser frequencies measured at below the $10^{-17}$ level [3]. Optical frequency combs facilitate the measurement and use of these atomic references by providing a set of clock-referenced lines that span more than an octave [4]. Moreover, they have enabled advances in diverse fields from spectroscopy of atoms and molecules [5,6] to astronomy [7].

A new type of frequency comb has emerged based on optical microresonators [1,2]. Here, the comb generation relies on nonlinear parametric oscillation and cascaded four-wave mixing driven by a CW laser. Such microcombs offer revolutionary advantages over existing comb technology, including chip-based photonic integration, uniquely large comb-mode spacings in the tens of gigahertz range, and monolithic construction with small size and power consumption. Microcomb development has included frequency control of their spectra [8–11], characterization of their noise properties [12–14], a Rb-stabilized microcomb oscillator [15], and demonstration of phase-locked [12,16,17] and mode-locked states [18,19]. However, the milestone of all-optical frequency control of a microcomb to an atomic reference, including frequency division to the microwave domain, has not been achieved.

In this paper, we report the achievement of this goal by demonstrating a functional optical clock based on full stabilization of a microcomb to atomic Rb transitions. We generate a low-noise, continuously equidistant microcomb spectrum by use of an on-chip silica microresonator. The clock output is the 33 GHz microcomb line spacing, which is electronically measurable, and a traceable integer partition of the 3.5 THz frequency spacing of the Rb references. Here, we explore the basic features of this microcomb clock. Its $5 \times 10^{-9}$ Allan
deviation for 1 s averaging is completely dominated by the Rb reference, and the microcomb contribution is only $<2 \times 10^{-14}$ at 1 s, indicating that much more stable clocks could be supported. Our results highlight an architecture for the integration of microcombs with other high-performance and chip-scale atomic frequency references [20].

2. EXPERIMENTAL METHODS

Figure 1(a) shows a schematic of our microcomb optical clock. A 2 mm diameter disk resonator with a 10° wedge side profile provides parametric comb generation. The resonator, which has an unloaded quality factor of 63 million, is fabricated on a silicon chip using conventional semiconductor fabrication techniques [21]. Hence, the core of our system is scalable and could be integrated with other on-chip photonic elements, and eventually atomic systems [20,22]. In these experiments we use a tapered fiber for evanescent coupling [23]. We excite the disk resonator with light from a CW laser (optical frequency $v_p$) that is intensity modulated at frequency $f_{eo}$ and amplified to a maximum of 140 mW. The first-order sideband powers are approximately 3 dB lower than the pump, and the piece of highly nonlinear fiber (HNLF) before the disk resonator increases the second-order (third-order) sidebands to 12 (25) dB below the pump. The modulation implements our parametric seeding technique [11], which enables unmatched control of the microcomb line spacing. Here we further demonstrate that parametric seeding enables the complete suppression of undesirable, nonequidistant subcombs. Following generation in the disk resonator, the microcomb output is optically filtered to attenuate the pump laser and modulation sidebands; the resulting spectrum is shown by the top trace in Fig. 1(b). The microcomb bandwidth is approximately a factor of 10 higher than the seeding comb. By amplifying the microcomb spectrum and without any dispersion control, we broaden the initial 20 nm bandwidth an additional factor of 10 to 200 nm. The ~2 ps duration optical waveform obtained directly from the microresonator offers sufficient peak power for our experiments and is stable and repeatable even for different settings of pump frequency and power, intensity modulation, taper–resonator coupling, and pump polarization. The broadened spectrum [Fig. 1(b)] overlaps with the resonance frequencies of molecules such as HCN, C$_2$H$_2$, CO$_2$, CH$_4$, and atomic Rb and K after second-harmonic generation.

For frequency stabilization, we heterodyne the microcomb spectrum with telecom-grade semiconductor distributed feedback (DFB) lasers at 1560 and 1590 nm. These lasers are frequency doubled and stabilized to well-known Rb transitions [24–26]. Precise Rb spectroscopic data, especially near 780 nm, exist, and with attention to systematic effects a stability of $10^{-12}/\sqrt{\tau}$ has been demonstrated [24]. Therefore, we focus only on salient details for controlling the microcomb with these optical references. To operate an optical clock, we stabilize the microcomb’s two independent degrees of freedom to the Rb references by leveraging frequency control of its spectrum. The central line of the microcomb is phase locked to the 1560 nm DFB laser, which is separate from the pump laser. [9,15]. Additionally, the 108th comb line from the center, which we obtain via spectral broadening, is phase locked to the 1590 nm DFB laser by tuning the microcomb line spacing through control of $f_{eo}$.

3. RESULTS AND DISCUSSION

The output of our microcomb optical clock is obtained via photodetection of the $\Delta v = 32.9819213$ GHz line spacing, which reflects the frequency difference $\Delta f_{0}$ of the D2- and D1-stabilized lasers divided by 108, and a fixed 660/108 MHz offset for phase stabilization. This specific offset arises because the comb’s central mode is phase locked at a frequency 920 MHz higher than the 1560 nm laser, while mode 108 is phase locked 260 MHz higher than the 1590 nm laser. The offset could assume a range of predetermined values, including zero, and the microresonator free spectral range could be targeted to utilize a specific value. The data points in Fig. 1(c) are a continuous >12 h long record of the clock output. Here, the vertical axis shows the difference between the clock output and $\Delta f_{0} = 3, 561, 387, 470(180)$ kHz, whose uncertainty [24–26] is shown by the gray band. Although we have not systematically analyzed the accuracy of our clock, its output is in reasonable agreement with these previous data. The 271 Hz RMS fluctuation in a 20 s average of the clock output is significantly reduced from those of the D2 and D1 reference lasers, due to the principle of optical frequency division associated with
frequency combs \[4, 27, 28\]. The remainder of this paper presents an investigation of our clock, including the deterministic generation of an equidistant microcomb spectrum, a demonstration of the precise relationship between the clock output and Rb reference, and an analysis of the clock’s stability.

The essential aspect of a frequency comb is a uniform spacing of all its modes. However, microcomb spectra are often composed of overlapping subcombs with different offset frequencies \[29\]. Such a microcomb spectrum has a fundamentally reduced frequency measurement precision and is unusable for our optical clock experiment. Subcombs arise when parametric oscillation creates initial signal/idler fields in resonator modes \(\pm m_i\) away from the one excited by the pump laser. The green lines in Fig. 2(a) show a schematic of a subcomb with characteristic frequency offset from that of an equidistant comb given by \(\nu_0 = n_1(\Delta P - m_i\Delta\nu)\), where \(\Delta P \approx m_i\Delta\nu\) is the primary spacing with order \(n_i\). We use a coherent control technique, parametric seeding, to deterministically suppress subcombs and favor a continuous comb with a single offset frequency. The seeding comb, whose spectrum \(\nu_m = \nu_0 + m\nu_e\) is shown by the red lines in Fig. 2(a), experiences parametric gain in the microresonator, and it induces sidebands of the first signal/idler pair that fix \(\Delta\nu\) of all parametrically generated lines at \(\nu_e\). In this paper, we demonstrate for the first time (to our knowledge) that sufficient amplitude of the seeding comb \(\nu_{\pm m_i}\) modes can injection lock the subcomb, which completely nullifies its frequency offset \(\nu_0\).

To investigate subcomb injection-locking (Fig. 2), we monitor the amplitudes of subcomb and parametric seeding comb lines while we tune \(\nu_e\), and thus \(\nu_0\). Information about these amplitudes is obtained via photodetection of the entire microcomb spectrum, which yields a signal at frequency \(\Delta\nu\) of all its modes. However, microcomb spectra are often acknowledged to be of high degree of correlation. The frequencies are recorded in nearly continuous 1 s intervals by use of an auxiliary self-referenced repetition-rate-stabilized Er: fiber frequency comb \([30]\). In Fig. 3(a), the black points show the clock output, while the red open points are \(\Delta_{\text{Rb}}/108\). Since the difference of the DFB lasers is not calibrated, for clarity we subtract its mean value \(\Delta_{\text{Rb}}/108\) from all the points. The overlap of the two data sets suggests their correlation, which we analyze in more detail by subtracting them against each other; see Fig. 3(b). A linear fit of this correlation plot yields a slope of 108, 0002(59), and the horizontal intercept differs from zero by only \(\pm 2.4 \pm 1.5\) Hz, compared to the \(\sim 3.5\) THz frequency of the Rb reference. Knowledge of \(\Delta_{\text{Rb}}\) via the stabilized fiber comb enables us to compare the clock signal with its optical reference in real time. Figure 3(c) shows a frequency counter record of the clock output from the same dataset as in Fig. 1(c), but here at each point a correction for the noise of the Rb spectrometers is applied. This reduces the scale of clock fluctuations by a factor of \(\sim 1000\) to the hertz level and demonstrates that they are overwhelmingly determined by the Rb reference.

Our microcomb optical clock is designed to generate an electronically detectable microwave output at a precise integer subdivision of the Rb reference. In contrast to earlier work \[15\], the clock output is traceable to atomic structure without regard to the operating parameters or conditions of the microcomb. To test this principle, we simultaneously count the DFB lasers’ frequencies and the clock output and characterize their degree of correlation. The frequencies are recorded in nearly continuous 1 s intervals by use of an auxiliary self-referenced repetition-rate-stabilized Er: fiber frequency comb \([30]\).
central line is phase locked to the 1560 nm laser. For this experiment, the phase lock to the 1590 nm laser is switched off and a constant parametric seeding frequency, which is synthesized from a hydrogen maser, determines the microcomb line spacing. The open circles in Fig. 4 show the combined Allan deviation of the Rb references normalized to 33 GHz for six decades of integration time. For short measurement periods, the stability increases as approximately $1/\sqrt{\tau}$. However near 0.1 s the Allan deviation increases and only slowly improves for averaging periods up to 10,000 s. The impact of systematic drifts on the Rb transitions due to, for example, excitation laser power fluctuations, magnetic field noise, and the Rb vapor cell pressure has been discussed extensively in the literature [24]. Importantly, these effects, rather than any associated with the microcomb, explain the references’ stability.

With microcomb servo control via the Rb D1 reference restored, we analyze the clock output by way of its Allan deviation, which is obtained with respect to a synthesized 33 GHz frequency referenced to a hydrogen maser. Importantly, the clock’s stability (filled black points in Fig. 4) is improved by a factor of $\sim 100$ over that of the DFB lasers, whose noise is distributed among all the lines of the microcomb. Such optical frequency division is the key metrological feature of any comb. Fluctuations and inaccuracy of the Rb-referenced lasers are naturally reflected in the microcomb clock output, and this explains the slow averaging of the black filled points in Fig. 4 beyond $\sim 0.1$ s. On the other hand, the in-loop noise of the two servos that stabilize the microcomb, which are shown by the black and red traces in Fig. 4, indicate that our microcomb system as currently configured could support more stable frequency references, and hence produce a 33 GHz output with a 1 s fractional stability of $2 \times 10^{-14}$. Increasing the bandwidth of the servo loops, in particular by shortening the second HNLF, would improve residual noise. We demonstrate this potential for improvement by characterizing the clock output, including its real-time correction for Rb reference noise [Fig. 3(c)]. The green points in Fig. 4 show an upper limit for the corrected clock output’s Allan deviation, which monotonically decreases with averaging time to $10^{-12}$ at 10,000 s. Accordingly, we project that a microcomb utilizing compact, all-optical Rb frequency references in a controlled environment [24] could produce a 33 GHz output with $5 \times 10^{-11}/\sqrt{\tau}$ stability.

4. CONCLUSION

In conclusion, we have reported the all-optical stabilization of a chip-based microresonator frequency comb to atomic Rb transitions. The electronically detectable microwave output of our optical clock is stable, and it accurately subdivides the terahertz frequency difference of the Rb references. At present, the clock output stability is limited entirely by the Rb references. However, the microcomb frequency control architecture demonstrated here is sufficient to support references with orders-of-magnitude-higher performance. Future work will address this point, as well as focus on generation of higher-peak-power optical waveforms directly from the microcomb. Combined with nonlinear spectral broadening, this would enable the subdivision of even larger frequency gaps and ultimately the self-referencing of a microcomb.

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REFERENCES


