SEISMIC SOURCE FUNCTIONS AND ATTENUATION FROM LOCAL
AND TELESEISMIC OBSERVATIONS OF THE NTS EVENTS
JORUM AND HANDLEY

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ABSTRACT

Several strong-motion seismograms recorded at 8 km from a large nuclear
test at Pahute Mesa, Nevada Test Site, are modeled using the Cagniard-de Hoop
technique. The ratio of vertical to radial motions suggest that the peak values
are produced by ray paths that penetrated to a depth several kilometers below
the source. A homogeneous layered Earth model with velocity increasing with
depth was used in the modeling of the velocity time histories. The upper portion
of the velocity model was determined by averaging bore-hole data and the lower
portion was obtained from regional refraction measurements. Assuming a mod­
ified Haskell (1967) source representation,

$$\psi(t) = \psi_0[1 - e^{-Kt}(1 + Kt + (Kt)^2/2 - B(Kt)^3)]$$

we obtain a range of source descriptions with $\psi_0$ varying with $K$ and $B$, $\psi_0(K, B)$. The range of source models for Jorum are $\psi_0(5, 1) = 3.1$, $\psi_0(5, 2) = 1.7$, and $\psi_0(5, 3) = 1.2 \times 10^{11}$ cm$^3$, respectively. Given an explosion source descrip­
tion, it is a straightforward task to determine the teleseismic attenuation from
WWSSN observations. From both the short- and long-period observations from
these events, an average $t^*$ of 1.3 is obtained for compressional waves of a
dominant 1-sec period. This estimate is insensitive to the range of $K$ and $B$
obtained from the near-field modeling.

INTRODUCTION

In recent years, a number of authors have compared sources derived from local
strong motion data with teleseismic observations. In the case of explosions, investi­
gators have examined the frequency content of short-period $P$ waves to measure
attenuation (e.g., Frasier and Filson, 1972). They estimate $t_\alpha^*$ to be about 0.5 where

$$t_\alpha^* = \frac{T}{Q_\alpha}$$

with $T$ the travel time of compressional ($\alpha$) waves and $Q_\alpha$ the quality factor.

If $t^*$ is known along some ray path, then a convolution operator $A(r, t^*)$ can be
constructed to correct a seismic pulse for attenuation [Carpenter et al. (1967)].

In the case of earthquake data, occasionally both long- and short-period $P$ and $S$
waves at teleseismic distances and well-recorded local $S$ waves are available. The
long-period pulses are easily modeled synthetically. For example, the results of
Burdick and Mellman (1976) for the Borrego Mountain earthquake indicate that
the direct $P$ wave actually contains $P$, $pP$, and $sP$, with the latter phase dominating.
Modeling the phases $sP$ and $sS$ from the Borrego Mountain earthquake, Burdick
(1978) estimated $t_\beta^*$ to be 5.2 where the $\beta$ refers to shear waves. Heaton and
Helmburger (1977) modeled the strong-motion data and found that Burdick’s
teleseismic description of Borrego was compatible with the local observations.

In general, comparing seismic pulses at various locations produced by earthquakes
with the intent of determining $Q$ is particularly difficult because of source finiteness
and associated directivity effects. The complex radiation pattern associated with
earthquakes introduces large uncertainties in comparing waveforms from various
stations. With the goal of avoiding this problem, we have reworked some of the best data available for comparing observations made near large nuclear explosions with teleseismic measurements of short- and long-period P waves.

**Near-Field Studies**

The megaton events, Handley and Jorum, considered in this study were located on the Pahute Mesa of the Nevada Test Site (NTS), see Figure 1. The near-field data described by Peppin (1974) were recorded at several azimuths at a distance of 8 km. These data provide a reversed profile with Jorum shooting west and Handley toward the east. For this size event, recordings at 8 km probably better represent the source than would closer recordings. Near-source effects such as triggered movement on nearby joints should not dominate the observations and the recording site is less likely to be in the zone of nonlinear deformation. Seismograms recorded

![Diagram](image)

**FIG. 1.** Map of NTS showing accelerometer locations, \( \Delta_{1} \) (Jorum), \( \Delta_{2} \) (Handley), for the Jorum and Handley tests, modified from Peppin (1974).

from the Jorum experiment are shown in Figure 2; however, the reverse Handley experiment was not as successful. The records are similar to those in Figure 2, but are slightly clipped on the first downswing (Peppin, 1974). An amplitude plot of the first peak of the Handley data shows less variation than those of Figure 2, although the average acceleration is greater (Stump, 1979). Viewing the results of the two experiments as a whole, we see some variations with azimuth. However, given the uncertainty in the Earth model near the sites, the Jorum data appear to be representative of the observed motions.

The energy in the first arrivals at stations 4 to 6, (Figure 2) is concentrated on the vertical component but, as time progresses, shifts to the radial. Also, note that many of the later arrivals are not particularly coherent from site to site, as can be seen by comparing any individual trace with the average stack shown on the bottom of Figure 2. The initial features can be explained by an initial downgoing P wave, with
an incidence angle at the stations of about 30° yielding a radial to vertical ratio of about 0.4. The later arrivals probably contain abundant information about the source-surface interaction, slapdown, tectonic release, slippage along cracks, and other complex phenomena. This study will concentrate on the first cycle of motion

![Graph showing vertical and radial accelerations](image)

**Fig. 2.** Vertical and radial accelerograms at sites 6, 5, and 4 with peak amplitudes given above each trace. The *bottom traces* are the stacked averages of the vertical and radial components, respectively. The number above each trace indicates the peak amplitude in cm/sec².

which is interpreted as representative of the dominant outgoing signals. For modeling purposes, it is convenient to work with the integral of these acceleration measurements as displayed in Figure 3. The slight linear drift that results from integration of the record has not been removed because we will work with only the
first cycle. Furthermore, the instruments are sufficiently broadband that the initial velocity pulse can be treated as the true ground motion (McEvilly, personal communication). Thus, the first second of the average vertical velocity component of the local recordings along with the corresponding teleseismic observations (Figure 4) will be the prime data set for determining $t^*$. 

![Vertical and radial velocities obtained by integrating the accelerograms displayed in Figure 2](image)

**FIG. 3.** Vertical and radial velocities obtained by integrating the accelerograms displayed in Figure 2

**NEAR-FIELD MODELING TECHNIQUES**

The techniques for modeling teleseismic explosion waveforms have been discussed at length by numerous authors with one of the latest expositions being given by Burdick and Helmberger (1979). Assuming an elastic layered earth with $t^* = 1$, they find that large overshoots of at least 2 to 1 in the reduced displacement potential, RDP, will explain most of the short- and long-period observations of both the Soviet and United States explosions. The Burdick and Helmberger study used
the form of RDP proposed by von Seggern and Blandford (1972) expressed by

$$\psi(t) = \psi(\infty) \left[ 1 - e^{-Kt} (1 + Kt - B(Kt)^2) \right]$$

where $\psi(\infty)$ is the source strength, $K$ scales inversely as the cube root of the yield,

and $B$ is the overshoot constant. With $B > 2$ the data discussed by Burdick and Helmberger is well modeled without adding a slapdown phase or related phenomena. It should be noted that, in this study, the phase $pP$ is treated as a purely elastic interaction with the free surface. For the source depth of interest, this phase arrives during the latter half of the direct $P$ arrival. Hence, the overshoot behavior of the source and the phase $pP$ must add together to describe the observed phases. Because of the inherent trade-off, it is not possible to uniquely separate the real overshoot of the source from any nonlinear behavior of $pP$. 

Fig. 4. Station location and $P$ waves obtained from the WWSSN. Absolute amplitude data are listed in Table 1.
The displacement potential is given by
\[ \phi(R, t) = -\psi(t)/R \] (2)
and the displacement by
\[ D(R, t) = \psi(t)/R^2 + (1/R\alpha)d\psi(t)/dt, \] (3)
where \( R \) is the radial distance and \( \alpha \) is the velocity. In terms of generalized ray theory, the vertical displacement (positive upward) for a layered Earth becomes
\[ D(r, z, t) = (d\psi/dt * dS/dt) \] (4)
where the * signifies convolution. The step response of the model is given by
\[ S(t) = 2 \frac{1}{\pi} \left[ \frac{1}{\sqrt{t}} * \sum \text{rays} \right] \] (5)
see (Heimberger and Harkrider, 1972). The velocity component can be written as
\[ V(t) = \frac{d}{dt} (d\psi/dt * dS/dt) \] (6)
\[ = (d^2\psi/dt^2 * dS/dt) \] (7)
\[ = (d^3\psi/dt^3 * S) \] (8)
\[ = \frac{d}{dt} (d^2\psi/dt^2 * S). \] (9)

Mathematically, (6) through (9) are equivalents. However, each has a different physical significance. The derivative increases the high-frequency content of the operator by a factor of \( \omega \). At teleseismic distances, the delta response of the Earth, \( dS/dt \), is reasonably well known and thus, expression (6) is commonly used. For this reason, one does not worry about the fact that \( (d^2\psi/dt^2) \) of the expression (1) is ill behaved. In the present study, the local structure at Jorum is not particularly well known and consequently, the knowledge of \( S(t) \) at the short-periods is lacking and the operation \( (dS/dt) \) should be avoided. This can be accomplished by demanding more of \( \psi(t) \) or by adding another term in the von Seggern-Blandford (1972) description, as shown below
\[ \psi(t) = \psi_0 \left[ 1 - e^{-Kt} (1 + (Kt) + 1/2(Kt)^2 - B(Kt)^3) \right] \] (10)
and applying (9) in modeling the velocity pulses displayed in Figure 3. This source description is intermediate between Haskell (1967) and von Seggern and Blandford (1972). Haskell assumed a source function that resulted in continuous accelerations. His model has a far-field high-frequency behavior of \( \omega^{-4} \). Von Seggern and Blandford found that \( \omega^{-2} \) was a better description of the teleseismic data from Longshot, Milrow, and Cannikin. For this study, it is extremely useful to have velocity continuous. If we were attempting to model the high-frequency behavior of the teleseismic data, frequency \( \sim 3 \) to 4 Hz, this distinction would be significant. However, since the derived source description will be used for only the longer
periods, 1 to 2 sec, this difference is not particularly important. To compute \( S(t) \), we need to have an accurate layered model of the source region, which is considered next.

**Local Crustal Model**

A detailed velocity model of the Silent Canyon Caldera and Pahute Mesa would be rather complex. With increasing depth, the lithological units grade from bedded and ash flow tuffs to interbedded tuffs and lava flows to lavas and intrusives with intermediate composition (Orkild et al., 1969). We have attempted to represent this complex with a four-layer model, Figure 5. The surficial layer is an average velocity from an acoustic log obtained in a shallow borehole in the Oak-Spring tuff at the NTS (Keller, 1960). The bottom of this unit coincides with the position of the static water table (Springer and Kinnaman, 1971). The velocities of the next two units (3.4 and 3.8 km/sec) are consistent with a decrease in the tuff content with increasing depth and the report by Spence (1974) of an average caldera velocity of 3.6 km/sec. Finally, the velocity of the half-space is intermediate between the velocity of the pre-Cenozoic rocks that surround Pahute Mesa and the lavas and intrusions comprising the lower sections of the caldera (Spence, 1974; Diment et al., 1960). Depth to the top of this layer is approximately determined from geological sections constructed from borehole data (Orkild et al., 1969).

![Figure 5: Crustal models constructed for the Pahute Mesa test site. The hard top model referred to in the text assumes that \( \beta_1 = \beta_2 = 1.2 \text{ km/sec} \), i.e., no change in shear velocity above a depth of 1.5 km. The densities are from top to bottom, 2.6, 2.7, 2.8, and 2.82 gm/cm\(^3\), respectively.](image)

The S-wave velocity structures of the caldera region are not well constrained. The S-wave model shown in Figure 5 is a simple estimate based on the available P-wave data. The most important aspect of the S-wave model is the velocity of the topmost layer: a low S-wave velocity increases the strength of the phase, \( pP \). Synthetic seismograms for a modified velocity structure with a higher surface S-wave velocity are also discussed below. This model replaces the surface S-wave velocity with that of the second layer.
MODELING THE STRONG-MOTION RECORDS

Synthetic velocity waveforms based on the above model for a range of distances are presented in Figure 6. The transfer function, $dS/dt$, is included to display the roughness of the response caused by the layering. Note that in the synthetic velocity waveforms the phase $pP$, which becomes a strong feature beyond about 5 km, interacts with the overshoot feature of the source. Only generalized rays that arrive within the first second of motion have been included in these synthetics. Figure 7 shows a comparison of synthetic seismograms computed with various values of $K$ and $B$ with the observed vertical seismograms. Most of these fits could be considered adequate except, perhaps, for $(B = 2, K = 4)$, which is somewhat too broad. It should be noted that the ratio of radial to vertical motions shown in Figure 6 is about 0.45, whereas the average for the data is somewhat lower, with considerable variation for the individual recordings (Figure 3). Also, note that when the downswing is particularly large, as on station 6 on Figure 3, the ratio of radial to vertical motion is relatively low. Thus, to gain some insight several additional models were studied. The results are displayed in the left two columns of Figure 8. Since the radial shapes were quite similar to the verticals, only the vertical component and the amplitude

![Graph showing vertical and radial Green's functions and velocity responses assuming $(K = 5, B = 2)$ for the layered model given in Figure 5. The amplitudes are scaled to the top trace. Only P-mode generalized rays were included in these calculations. Numerical experimentation showed that rays containing S-wave legs contribute little to the early portion of the record. Rays encountering more than two internal reflections were neglected.](image-url)
ratios have been plotted. First, note that increasing the shear velocity in the surface layer (hard top) greatly affects the ratio as well as changes the strength of \( pP \). When the surface is soft (low-shear velocity), the phase \( pP \) is strong because of the weak conversion of \( pS \) and because a soft surface has a strong effect on the receiver function. Thus, a strong \( pP \) is compatible with a small ratio of radial to vertical and it appears that the waveforms shown on Figure 3 can be interpreted in this fashion. Another interesting feature that is common to the waveshapes in Figure 3 is a relatively broader upswing on the radial relative to vertical components. This feature is not particularly important to the objective of this study, but models that include

![Graph showing potential, displacement, and velocity for various assumed values of K and B.](image)

**Fig. 7.** The potential (cm³), displacement (cm), and velocity (cm/sec) for various assumed values of \( K \) and \( B \) are plotted in rows 1 and 3 where the numbers indicate peak values. The corresponding synthetic velocity and the average vertical observation (shown in Figure 3) are plotted in rows 2 and 4.
rays that convert from \( P \) to \( SV \) near the receiver in a thin soft layer at the surface produce this effect. The radial component is strongly affected by these types of conversions, whereas the vertical component is rather insensitive.

To test the sensitivity of the synthetics of the choice of model parameters, Green's functions for a second velocity model were also computed. The new model replaces the lower three layers with a linear gradient, Figure 5. The computed Green's functions are shown in the right side of Figure 8. Although the shapes of the new response functions are slightly different, the convolution of the longer period source function produces waveforms and amplitude ratios that are very comparable with the discrete model.

A problem that might affect these results would be the presence of thin high-velocity layers above the source. Such a structure could produce tunneling effects and strongly reduce the shorter period amplitudes. Fortunately, at \( \Delta = 8 \) km, the turning velocity at the depth of greatest penetration approaches 3.8 km/sec and this velocity should be sufficiently high to avoid that problem (see Mellman and Helmberger, 1974). If significant high-velocity layers are actually present above the source, then the source strength would be underestimated and the teleseismic \( t^* \) would be slightly overestimated.

In conclusion, the crustal model below the shot point down to about 4 km controls the amplitude of the synthetics. The delay time of \( pP \) is consistent with the model given in Figure 5. A smooth gradient model gives about the same results. Thus,
\[ \psi_0(K, B) \] can be determined by simply scaling the synthetic given in Figure 7 to the observed waveforms. Assuming \( K = 5 \), we obtain: \( \psi_0(5, 1) = 3.1; \psi_0(5, 2) = 1.7; \) and \( \psi_0(5, 3) = 1.2, \) all \( \times 10^{11} \) cm\(^3\). Next, the teleseismic waveshapes and amplitudes will be compared with these local field results.

**Teleseismic Results: \( t^* \)**

The amplitudes of the teleseismic observations are listed in Table 1. The right-hand column gives the amplitude corrected to 30°, i.e., removal of the geometrical spreading effects for the more distant stations. Thus the amplitude at SCP is left unchanged whereas the amplitude at HNR, the most distant station, is substantially increased. The geometrical correction used in these computations is based on the curve displayed in Figure 3 of Langston and Helmberger (1975). The overall average of the corrected amplitudes is 1024 \( \mu \), but there is considerable scatter with the more distant stations yielding the largest corrected amplitudes. The station geometry also imposes a strong correlation between azimuth and distance as can be seen from Table 1 and Figure 9. This observed amplitude pattern could be the result of one or all of three mechanisms: (1) strong azimuthal radiation pattern imposed by structure in the source region; (2) effective amplification by the receiver structure for the island stations in the west and northwest azimuths; and (3) lateral variations in \( t^* \).

The first mechanism is easily tested by comparing the amplitude behavior of several other events. Figure 9 shows the amplitude data for Jorum, Greeley, Boxcar, Benham, and Halfbeak. A constant scale factor has been applied to all observations.

<table>
<thead>
<tr>
<th>Station</th>
<th>Distance, ( \Delta (\degree) )</th>
<th>Azimuth ( \gamma (\degree) )</th>
<th>Amplitude ( (\mu )</th>
<th>Corrected Amplitude ( (\mu )</th>
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<td>868</td>
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<td>HNR</td>
<td>90.6</td>
<td>258.7</td>
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for each source in order to minimize the scatter that results from various source strengths. The scale factors were simultaneously adjusted such that the scatter in the data at all stations for all sources was minimized. These events were located throughout the Silent Canyon Caldera. All five events show a consistent azimuthal trend. Figure 10 shows the waveforms and amplitude ratios for Jorum and Handley. The Handley test was located a few kilometers outside of the boundary faults associated with the caldera. Note that the waveforms are very consistent between these two tests and that the amplitude ratio is stable. Also, note that stations BHP and QUI have very complicated waveforms which are presumably caused by receiver structure. For this reason, we have omitted these two stations in our amplitude

![Graph showing amplitude variations for five tests located throughout Pahute Mesa](image)

**Fig. 9.** Azimuthal variations in amplitudes as observed for five tests located throughout Pahute Mesa (NOR = 10°, COL = 336°). The absolute amplitudes for each event have been adjusted in order to minimize scatter that results from variations in source strength. The station azimuths are listed in Table 1.

considerations although their neglect does not change the overall average (1024 m/s) appreciably. We conclude from these data that near-source structure is not producing the amplitude pattern.

The question of systematic bias introduced by receiver structure is difficult to assess on a worldwide basis at this stage of study. Short-period records can show strong azimuthal patterns as discussed by Helberger and Wiggins (1971), Aki (1973), and others. Based on the geology of many of the island stations, significant waveform distortion would not be too surprising. This may in part explain the pattern in Figure 9. Fortunately, the stations in the United States have been well studied by Butler (1979) and the receiver functions for the Eastern U.S. stations appear remarkably simple. Some of the recordings from these stations for the Jorum and Handley events are displayed in Figure 11. The long-period observations are quite small on the actual records, whereas the short-period observations are nearly off-scale making both difficult to digitize. Included at the bottom of Figure 11 are the best-fitting short- and long-period synthetics produced by varying \( t^* \). In generating these responses, we used the crustal model at the source given in Figure 5 with the \( P \)-wave velocity below the 4.4-km/sec layer set at 5.0 km/sec. This is also the velocity assumed for the receiver half-space model. The amplitude of the synthetic can then be obtained from the theoretical curve given in Langston and Helberger (1975) which contains the appropriate corrections for propagation through the lower
crust and upper mantle. Variations in $K$ and $B$ were not particularly effective in changing the short-period amplitudes because changes in overshoot ($B$) effect the source strength ($\psi_0$) determination. That is, increasing the overshoot makes the short-period synthetics larger with constant $\psi_0$; but the source level is effectively

![Comparison of the observed teleseismic waveforms and amplitudes for the Handley and Jorum events.](image)

**Fig. 10.** Comparison of the observed teleseismic waveforms and amplitudes for the Handley and Jorum events.

smaller because of a compensating scale change required to fit the local amplitudes. Examples of these trade-offs are listed in Table 2 ($K = 5$, $B = 1, 2, 3$). These synthetic teleseismic amplitudes, listed for a range of $l^*$ values should be compared with the worldwide short-period average of 1024 m$\mu$ and the (SPZ/LPZ) ratio of 0.5. Thus, we find that the uniqueness problem associated with the source description
Fig 11 Comparison of the short-period (left) and long-period (right) waveforms from stations located in the Eastern United States with the synthetic seismograms, assuming \( t^* = 1.3 \).

does not seriously influence the estimate of \( t^* \) since the trade-off affects the local and teleseismic modeling in essentially the same manner.

**DISCUSSION**

The average corrected amplitude for all short-period observations is 1024 m\( \mu \). If the local data is sufficiently removed from the high stresses involved in the explosion to be considered linear, and if the simplified crustal model is appropriate, then the best estimate of \( t^* \) is 1.3. This value is significantly larger than previous determi-
nations, e.g., see Frasier and Filson (1972) and Der and McElfresh (1977). Those authors, working with digital data, find considerable amounts of high-frequency signal in some records. The observation of high-frequency energy in the teleseismic records requires a low estimate of $t^*$. One way to accommodate this apparent discrepancy is to adopt a more general form of the attenuation operator such as discussed in Minster (1978). If seismic attenuation is frequency-dependent, then the $t^*$ value discussed above is appropriate for only the periods $\sim 1$ to $2$ sec.

The $t^*$ derived in the present study is most appropriate for the frequency that dominates the $m_b$ measurement, i.e., $\sim 1$ Hz. The range of amplitudes observed in

<table>
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<th>TABLE 2</th>
<th>SYNTHETIC TELESEISMIC AMPLITUDES</th>
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</thead>
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<td>$K = 5$</td>
<td>$B = 1$  $B = 2$  $B = 3$  $B = 1$  $B = 2$  $B = 3$</td>
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<tr>
<td>$t^*$</td>
<td>0.8     3145  3162  3153  0.81  0.84  0.84</td>
</tr>
<tr>
<td></td>
<td>0.9     2520  2507  2529  0.73  0.76  0.76</td>
</tr>
<tr>
<td></td>
<td>1.0     2040  2028  2012  0.70  0.68  0.68</td>
</tr>
<tr>
<td></td>
<td>1.1     1640  1643  1658  0.62  0.62  0.63</td>
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<tr>
<td></td>
<td>1.2     1351  1350  1362  0.56  0.56  0.57</td>
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<td>1.3     1077  1084  1101  0.50  0.50  0.51</td>
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<tr>
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<td>1.4     898   902   913   0.45  0.46  0.47</td>
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<tr>
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<td>1.5     744   750   768   0.41  0.42  0.43</td>
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</table>

Fig 12 A gnomic projection (all great circles are straight lines) showing the NTS, WWSSN stations of the United States, and the Soviet Union test sites (modified from Butler, 1979). Butler (1979) has observed a large seismic attenuation at the stations GOL and ALQ, relative to other United States stations from sources in both the Soviet Union and the Kuriles (dotted azimuths). Worldwide stations in a northeast azimuth from NTS are significantly reduced in amplitudes relative to other azimuths.
Figure 9 could be interpreted as lateral variations in \( t^* \) with the range of 1.5 for the northeastern azimuths and 1.1 for the northwestern. However, with the present data set it is impossible to uniquely differentiate real lateral variation in \( t^* \) from apparent variations introduced by systematic bias in receiver structures. In a recent study by Butler (1979) of amplitudes at WWSSN stations in the United States from Soviet nuclear tests, it was found that stations in the Eastern United States do not show anomalously small amplitudes. However, the stations ALQ and GOL are depressed in amplitude by factors 2 to 3. The same study found a similar result from earthquake sources in the Kuriles. These observations suggest as a hypothesis that the upper mantle along the ray paths near the stations ALQ and GOL is typified by low \( Q \).

Figure 12 is a gnomic projection showing the Soviet test sites and the United States WWSSN stations. Dashed lines from stations ALQ and GOL show the ray paths that are attenuated (Butler, 1979). Also shown on this figure is the range of azimuths from NTS that have been characterized in this study by low amplitudes and large \( t^* \) (~1.5). It is very intriguing that the two studies are at least consistent with a low \( Q \) region in the upper mantle beneath the central Rocky Mountains. This model is clearly not unique and additional studies of the azimuthal receiver function characteristics of worldwide stations will be required to more fully understand the origin of the azimuthal amplitude anomalies associated with the NTS events.

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**References**


