Measurement of the muon charge asymmetry in inclusive $pp \rightarrow W + X$ production at $\sqrt{s} = 7$ TeV and an improved
determination of light parton distribution functions

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Measurements of the muon charge asymmetry in inclusive $pp \rightarrow W + X$ production at $\sqrt{s} = 7$ TeV are presented. The data sample corresponds to an integrated luminosity of 4.7 fb$^{-1}$ recorded with the CMS detector at the LHC. With a sample of more than 20 million $W \rightarrow \mu\nu$ events, the statistical precision is greatly improved in comparison to previous measurements. These new results provide additional constraints on the parton distribution functions of the proton in the range of the Bjorken scaling variable $x$ from $10^{-3}$ to $10^{-1}$. These measurements and the recent CMS measurement of associated $W + c$ charm production are used together with the cross sections for inclusive deep inelastic $e^+p$ scattering at HERA in a next-to-leading-order QCD analysis. The determination of the valence quark distributions is improved, and the strange-quark distribution is probed directly through the leading-order process $g + s \rightarrow W + c$ in proton-proton collisions at the LHC.

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I. INTRODUCTION

In the standard model (SM), the dominant processes for inclusive $W$-boson production in $pp$ collisions are annihilation processes: $ud \rightarrow W^+$ and $d\bar{u} \rightarrow W^-$ involving a valence quark from one proton and a sea antiquark from the other. Since there are two valence $u$ quarks and one valence $d$ quark in the proton, $W^+$ bosons are produced more often than $W^-$ bosons. The Compact Muon Solenoid (CMS) experiment at the Large Hadron Collider (LHC) has investigated this production asymmetry in inclusive $W$-boson production and measured the inclusive ratio of total cross sections for $W^+$ and $W^-$ boson production at $\sqrt{s} = 7$ TeV to be $1.421 \pm 0.006$(stat) $\pm 0.032$(syst) [1]. This result is in agreement with SM predictions based on various parton distribution functions (PDFs) such as the MSTW2008 and CT10 PDF sets [2,3]. Measurements of the production asymmetry between $W^+$ and $W^-$ bosons as a function of boson rapidity can provide additional constraints on the $d/u$ ratio and on the sea antiquark densities in the proton. For $pp$ collisions at $\sqrt{s} = 7$ TeV, these measurements explore the PDFs for the proton for Bjorken $x$ from $10^{-3}$ to $10^{-1}$ [4]. However, it is difficult to measure the boson rapidity production asymmetry because of the energy carried away by neutrinos in leptonic $W$-boson decays. A quantity more directly accessible experimentally is the lepton charge asymmetry, defined as

$$A(\eta) = \frac{d\sigma}{d\eta}(W^+ \rightarrow l^+\nu) - \frac{d\sigma}{d\eta}(W^- \rightarrow l^-\bar{\nu}) + \frac{d\sigma}{d\eta}(W^- \rightarrow l^-\bar{\nu}) - \frac{d\sigma}{d\eta}(W^+ \rightarrow l^+\nu),$$

where $d\sigma/d\eta$ is the differential cross section for $W$-boson production and subsequent leptonic decay and $\eta = -\ln(\tan(\theta/2))$ is the charged lepton pseudorapidity in the laboratory frame, with $\theta$ being the polar angle measured with respect to the beam axis.

High precision measurements of the $W$-boson lepton charge asymmetry can improve the determination of the PDFs. Both the $W$-boson lepton charge asymmetry and the $W$-boson production charge asymmetry were studied in $p\bar{p}$ collisions by the CDF and D0 experiments at the Tevatron collider [5–7]. The ATLAS, CMS, and LHCb experiments also reported measurements of the lepton charge asymmetry using data collected at the LHC in 2010 [8–11]. An earlier measurement of the $W$-boson electron charge asymmetry is based on 2011 CMS data corresponding to an integrated luminosity of 0.84 fb$^{-1}$ [12].

The impact of CMS measurements of the lepton charge asymmetry on the global PDF fits has been studied by several groups [13–17], who concluded that improvements in the PDF uncertainties for several quark flavors could be achieved with more precise data. In this paper, we report a measurement of the muon charge asymmetry using a data sample corresponding to an integrated luminosity of 4.7 fb$^{-1}$ collected with the CMS detector at the LHC in 2011. The number of $W \rightarrow \mu\nu$ events (more than 20 million) in this data sample is 2 orders of magnitude larger than for our previous measurement [10].

This precise measurement of the muon charge asymmetry and the recent CMS measurement of associated $W + c$ charm production [18] are combined with the cross sections

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for inclusive deep inelastic $e^+p$ scattering at HERA [19] in a quantum chromodynamics (QCD) analysis at next-to-leading order (NLO). The impact of these measurements of $W$-boson production at CMS on the determination of light-quark distributions in the proton is studied and the strange-quark density is determined.

This paper is organized as follows. A brief description of the CMS detector is given in Sec. II. The selection of $W \to \mu\nu$ candidates is described in Sec. III. The corrections for residual charge-specific bias in the measurement of the muon transverse momentum ($p_T$) and in the muon trigger, reconstruction, and selection efficiencies are discussed in Sec. IV. The extraction of the $W \to \mu\nu$ signal is described in detail in Sec. V. Systematic uncertainties and the full correlation matrix are given in Sec. VI. The final measurements are presented in Sec. VII, and the QCD analysis is discussed in detail in Sec. VIII. The summary and conclusion follow in Sec. IX.

II. THE CMS EXPERIMENT

The central feature of the CMS apparatus is a superconducting solenoid 6 m in diameter and 13 m long, which provides an axial field of 3.8 T. Within the field volume are a silicon pixel and strip tracker, a crystal electromagnetic calorimeter (ECAL), and a brass/scintillator hadron calorimeter. Muons are measured in gas-ionization detectors embedded in the steel flux return yoke. The ECAL consists of nearly 76000 lead tungstate crystals that provide coverage in pseudorapidity $|\eta| < 1.479$ in the barrel region and $1.479 < |\eta| < 3.0$ in the two end cap regions. A preshower detector consisting of two planes of silicon sensors interleaved with a total of three radiation lengths of lead is located in front of the ECAL end caps. Muons are selected in the pseudorapidity range $|\eta| < 2.4$, with detection planes constructed of drift tubes (DT), cathode strip chambers (CSC), and resistive plate chambers, and matched to the tracks measured in the silicon tracker resulting in an $\eta$-dependent $p_T$ resolution of about 1%–5% for muon $p_T$ up to 1 TeV. The inner tracker, consisting of 1440 silicon pixel and 15148 silicon strip detector modules, measures charged particles within the pseudorapidity range $|\eta| < 2.5$. It provides an impact parameter resolution of $\sim 15 \mu m$ and a $p_T$ resolution of about 1.5% for 100 GeV particles.

The CMS experiment uses a right-handed coordinate system, with the origin at the nominal interaction point, the $x$ axis pointing toward the center of the LHC, the $y$ axis pointing up (perpendicular to the LHC plane), and the $z$ axis along the counterclockwise-beam direction. The polar angle, $\theta$, is measured from the positive $z$ axis and the azimuthal angle, $\phi$, is measured in the $x$-$y$ plane.

A detailed description of the CMS experiment can be found in Ref. [20].

III. EVENT RECONSTRUCTION

The signature of a $W \to \mu\nu$ event is a high-$p_T$ muon accompanied by missing transverse momentum $\slashed{E}_T$ due to the escaping neutrino. The CMS experiment has utilized a particle-flow algorithm in event reconstruction, and the $\slashed{E}_T$ used by this analysis is determined as the negative vector sum of the transverse momenta of all particles reconstructed by this algorithm [21]. The $W \to \mu\nu$ candidates were collected with a set of isolated single-muon triggers with different $p_T$ thresholds, which is the major difference with respect to the previous CMS measurement where nonisolated single-muon triggers were used [10]. The isolated muon trigger requires that in the neighboring region of the muon trigger candidate both the transverse energy deposits in calorimeters and the scalar sum of the $p_T$ of the reconstructed tracks are small, and it reduces the trigger rate while maintaining a relatively low muon $p_T$ threshold. We use all the data-taking periods during which the isolated muon triggers were not prescaled (i.e. they were exposed to the full integrated luminosity).

Other physics processes can produce high-$p_T$ muons and mimic $W \to \mu\nu$ signal candidates. We consider the SM background contributions from multijet production (QCD background), Drell-Yan ($Z/\gamma^* \to \ell^+\ell^-$) production, $W \to \tau\nu$ production [electroweak (EW) background], and top-quark pair ($t\bar{t}$) production. In addition, cosmic-ray muons can penetrate through the center of the CMS detector and also mimic $W \to \mu\nu$ candidates.

Monte Carlo (MC) simulations are used to help evaluate the background contributions in the data sample and to study systematic uncertainties. Primarily, we use NLO MC simulations based on the POWHEG event generator [22] where the NLO CT10 PDF model [3] is used. The generated events are interfaced with the PYTHIA (v.6.422) event generator [23] for simulating the electromagnetic finite-state radiation (FSR) and the parton showering. The $\tau$ lepton decay in the $W \to \tau\nu$ process is simulated by the TAUOLA MC package [24]. We simulate the QCD background with the PYTHIA event generator where the CTEQ6L PDF model [25] is used. The CMS detector simulation is interfaced with GEANT4 [26]. All generated events are first passed through the detector simulation and then reconstructed in the same way as the collision data. Pileup is the presence of multiple interactions recorded in the same event. For the data used in this analysis, there are an average of about 7 reconstructed primary interaction vertices for each beam crossing. The MC simulation is generated with a different pileup distribution than we observe in the data. Therefore, the MC simulation is weighted such that the mean number of interactions per crossing matches that in data, using the inelastic $pp$ cross section measured by the CMS experiment [27].

The selection criteria for muon reconstruction and identification are described in detail in a previous report [28]. Therefore, only a brief summary is given here. A muon candidate is reconstructed using two different algorithms:

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one starts with a track measured by the silicon tracker and then requires a minimum number of matching hits in the muon detectors, and the other starts by finding a track in the muon system and then matching it to a track measured by the silicon tracker. Muons used in this measurement are required to be reconstructed by both algorithms. A global misalignment leads to a charge dependent bias in the reconstruction of muon momenta, which is removed by using a muon momentum correction. This misalignment leads to a charge dependent bias in the reconstruction of muon momenta, which is removed by using a muon momentum correction. The detailed description of the method for the extraction of the correction factors using $Z/\gamma^* \rightarrow \mu^+\mu^-$ events is given in Ref. [29]. Here we provide only a short summary of the method. First, corrections to muon momentum in bins of $\eta$ and $\phi$ are extracted separately for positively and negatively charged muons using the average of the $1/p_T$ spectra of muons in $Z/\gamma^* \rightarrow \mu^+\mu^-$ events. The mean values of the $1/p_T$ spectra at the MC generator level, varied by the reconstruction resolution, are used as a “reference.” The mean values of the reconstructed $1/p_T$ spectra in data or simulation are tuned to match the reference. Second, the correction factors derived in the previous step are tuned further by comparing the dimuon invariant mass in each bin of muon charge $Q$, $\eta$, and $\phi$ to the ones at the MC generator level varied by the reconstruction resolution. The same procedure is performed for both data and reconstructed MC events, and correction factors are determined separately. The correction factors are extracted using the same $\eta$ binning defined above in order to avoid correlations between different $\eta$ bins.

The data set used to derive the corrections was collected with a double-muon trigger with asymmetric $p_T$ thresholds of 17 and 8 GeV. Both muons are required to have $p_T > 25$ GeV, which exceeds significantly the trigger $p_T$ thresholds. The simulation has been corrected for the muon efficiency difference between data and MC simulation as discussed below. We illustrate the relative size of the derived corrections using a 40 GeV muon as an example. For muons within $|\eta| < 0.2$, the corrections derived using the $1/p_T$ spectra are less than 1.5% and 0.4% for data and MC simulation, respectively. A $\phi$ modulation of these corrections is observed. The maximum corrections are larger in high-$\eta$ region, and for muons with $|\eta| > 2.1$ these corrections can be as large as 3.5% and 1.4% for data and MC simulation, respectively. The additional corrections derived using the dimuon invariant mass are smaller. For muons within the complete detector acceptance, the additional corrections are less than 0.5% and 0.2% for data and simulation, respectively. These additional corrections show no evidence of $\eta$-$\phi$ dependence and fluctuate around zero within the statistical uncertainties of the final corrections. The statistical uncertainties of the corrections for various $\eta$-$\phi$ bins are uncorrelated. By comparing the correction factors for positively and negatively charged muons in each bin, we can determine the relative corrections from misalignment and from mismodeling of the magnetic field in the tracker system. The mismodeling corrections for muons with $|\eta| > 2.1$, where maximum deviations from zero are evident, are less than 0.3% and 0.4% for data and MC simulation, respectively. In contrast, in the same detector region, the corrections due to misalignment are about 4.4%
and 1.7\% for data and MC simulation, respectively. Hence, the bias comes predominantly from misalignment.

Figure 1 shows the average dimuon invariant mass (mass profile) as a function of muon $Q$ and $\eta$ before and after the correction, which includes both the contributions from tracker misalignment and mismodeling of the magnetic field. The dimuon mass profiles after the correction are compared to the reference mass profile for data and MC simulation. They agree well with the reference, so the muon momentum bias is largely removed. The reference mass profile is expected to be a function of $\eta$ because of the $p_T$ requirements for the two daughter muons in $Z/\gamma^* \rightarrow \mu^+\mu^-$ decays. Values of the dimuon mass profile as a function of muon $\eta$ are averaged over $\phi$, while the muon scale corrections correct for muon momentum bias in both $\eta$ and $\phi$.

The overall efficiency in the selection of muon candidates includes contributions from reconstruction, identification (including isolation), and trigger efficiencies. The muon reconstruction efficiency includes contributions from the reconstruction efficiency in the tracker system (“tracking”) and in the muon system. The muon “off-line” efficiency is the product of reconstruction and identification efficiencies. The contribution of each component to the overall efficiency (tracking, muon stand-alone reconstruction, identification, and trigger) is measured directly from the $Z/\gamma^* \rightarrow \mu^+\mu^-$ events using the tag-and-probe method [1,28]. In this method one of the daughter muons is used to tag the $Z/\gamma^* \rightarrow \mu^+\mu^-$ event and the other muon candidate is used as a probe to study the muon efficiencies as a function of $Q$, $\eta$, and $p_T$. For every event a positively charged muon can be selected as the tag and a negatively charged probe candidate is used to study the efficiencies for negatively charged muons. The same procedure is repeated by selecting a negatively charged muon.

![FIG. 1](image-url) (color online). The dimuon mass profile as a function of muon $\eta$ for $\mu^-$ (a), (c) and $\mu^+$ (b), (d), where (a) and (b) are before the correction and (c) and (d) are after the correction. The generated muon $p_T$ varied by reconstruction resolution in data is used to obtain the dimuon invariant mass of the reference.
muon as the tag to study efficiencies for positively charged muons. Each individual efficiency is determined in 22 bins of muon $\eta$, as defined above, and 7 bins of $p_T$ ($15-20, 20-25, 25-30, 30-35, 35-40, 40-45,$ and $> 45$ GeV) for both $\mu^+$ and $\mu^-$. The same procedure is applied to both data and MC simulation and scale factors are determined to match the simulation efficiencies to the data.

The measured average tracking efficiency in each $\eta$ bin varies from 99.6% to 99.9% with a slight inefficiency in the transition regions from the barrel to the end cap segments and at the edge of the tracker system. The ratio of tracking efficiencies for $\mu^+$ and $\mu^-$ is consistent with unity within statistical uncertainty. In the transition regions from the DT to the CSC, there is evidence that the muon off-line efficiency has a slight asymmetry between $\mu^+$ and $\mu^-$. The ratio of efficiencies for positively and negatively charged muons differs from unity by up to $1.0 \pm 0.3\%$. The trigger efficiency ratio is also found to differ from unity in some $\eta$ regions. The maximum deviation is at $\eta > 2.1$ where the efficiency for $\mu^+$ is about $2.0 \pm 0.5\%$ higher than that for $\mu^-$. Figure 2 shows the $\eta$ distribution for the leading $\mu^+$ and $\mu^-$ in the $Z/\gamma^* \rightarrow \mu^+\mu^-$ sample. The dimuon invariant mass is within $60 < m_{\mu\mu} < 120$ GeV. Here, the MC simulation is corrected for muon momentum bias, efficiency, and modeling of the $Z$-boson transverse momentum ($\vec{q}_T$) before normalizing to the measured data. The modeling of $Z$-boson $\vec{q}_T$ spectrum is discussed in detail in Sec. VI D 4. The $\eta$ dependence effect in data and MC simulation are in good agreement.

V. EXTRACTION OF THE ASYMMETRY

The asymmetry is calculated in bins of $|\eta|$ from the yields of $W^+$ and $W^-$. In this section, we explain how the yields are obtained from the $E_T$ distributions, and we discuss corrections to the $E_T$ needed in the accurate estimation of the yields. Finally, we explain how backgrounds are taken into account.

The raw charged asymmetry ($A_{raw}$) is defined in terms of the numbers $N^{W^+}$ and $N^{W^-}$ of $W^+$ and $W^-$ signal events,

$$A_{raw} = \frac{N^{W^+} - N^{W^-}}{N^{W^+} + N^{W^-}}. \quad (2)$$

The yields $N^{W^+}$ and $N^{W^-}$ are obtained from simultaneous binned maximum-likelihood fits of the $E_T$ distributions; the signal yields and the normalization of the QCD background are free parameters. The likelihood is constructed following the Barlow-Beeston method [30] to take into account the limited size of the MC signal event sample. The shapes of the $E_T$ distributions for the $W \rightarrow \mu\nu$ signal and the background contributions are taken from MC simulations after correcting for mismodeling of the detector response and the $\vec{q}_T$ distribution of the $W$ bosons, as discussed further in Sec. VI D 4 below. The pileup of each MC sample is matched to the data using an “accept-reject” technique based on the observed and simulated pileup distributions. This technique avoids a large spread of weights that would come from simply reweighting the MC events; the $E_T$ templates are constructed using the accepted MC events.

A total of 12.9 million $W^+ \rightarrow \mu^+\nu$ and 9.1 million $W^- \rightarrow \mu^-\bar{\nu}$ candidate events are selected. The expected backgrounds from QCD, EW, and $t\bar{t}$ events are about 8%, 8%, and 0.5%, respectively. The single top-quark and diboson ($WW/WZ/ZZ$) production is less than 0.1% and is neglected. The variation of the background composition as a function of $|\eta|$ is taken into account.

The estimate for the Drell-Yan background is based on the observed yields in a Drell-Yan control sample. The $W \rightarrow \tau\nu$ background scales with the $W \rightarrow \mu\nu$ signal using a factor determined from a MC simulation. The $t\bar{t}$
background is normalized to the NLO cross section obtained from MCFM [31–33]. Efficiency correction factors are applied to the simulation before determining the background normalization.

The level of the QCD background is determined by the fit. A constraint on the relative amount of QCD background in the $W^+$ and $W^-$ samples is obtained from a QCD-enriched control sample collected using a muon trigger with no isolation requirement. This constraint induces a correlation of $N_{W^+}$ and $N_{W^-}$, and the resulting covariance is taken into account when evaluating the statistical uncertainty on $A_{raw}$.

In the following sections, we discuss the corrections to the $E_T$ and then report the results of the fit to the $E_T$ distributions.

A. Corrections of the missing energy measurement

The analysis depends critically on the control of the $E_T$ distributions. Several corrections are needed to bring the simulation into agreement with the observed distributions. The $E_T$ depends on both the measured muon kinematics and the kinematics of the hadrons recoiling against the $W$ boson. The corrections for the calibration of the muon momentum, discussed in Sec. IV above, are applied by adding the $\tilde{p}_T$ correction to $E_T$ vectorially. The kinematic corrections for the so-called “hadronic recoil,” which are based on the control sample of $Z/\gamma^* \rightarrow \mu^+\mu^-$ events, are explained in detail here.

By definition, the hadronic recoil, $\tilde{u}$, is the vector sum of transverse momenta of all reconstructed particles except for the muon(s). For $Z/\gamma^* \rightarrow \mu^+\mu^-$ events,

$$\tilde{u} = -\hat{E}_T - \hat{q}_T,$$

(3)

where $\hat{q}_T$ is the transverse momentum of the dimuon system and $\hat{E}_T \approx 0$. The components of $\tilde{u}$ parallel and perpendicular to $q_T$ are $u_{||}$ and $u_{\perp}$, respectively. The mean of $u_{||}$, $\langle u_{||} \rangle$, is approximately zero, while the mean of $u_{\perp}$, $\langle u_{\perp} \rangle$, is close to the mean of the boson $q_T$. Differences in the distributions from data and MC are ascribed to detector effects, the simulation of jets, pileup and the underlying event, all of which should be nearly the same for $Z/\gamma^* \rightarrow \mu^+\mu^-$ and $W \rightarrow \mu\nu$ events. The distributions of $u_{||}$ and $u_{\perp}$ in $Z/\gamma^* \rightarrow \mu^+\mu^-$ events are used to derive corrections for the simulation that improve the modeling of $E_T$ for $W \rightarrow \mu\nu$ signal events as well as for backgrounds; this technique was employed previously by the Tevatron experiments and by CMS [34–36]. We correct both the scale and resolution of $E_T$.

A comparison of the $E_T$ distributions for $Z/\gamma^* \rightarrow \mu^+\mu^-$ events in data and MC shows that the agreement is not perfect. Both show a small $\phi$ modulation, but the phase and amplitude of the modulation are not the same. This modulation follows from the fact that collisions, including hard interactions that produce $W$ events as well as pileup events, do not occur exactly at the origin of the coordinate system. This modulation can be characterized by a cosine function, $C \cos(\phi - \phi_0)$. The dependence of the amplitude $C$ and phase term $\phi_0$ on the number of primary vertices is extracted from the $Z/\gamma^* \rightarrow \mu^+\mu^-$ event sample by fitting a $\phi$-dependent profile of $u_{||} - \langle u_{||} \rangle$. The amplitude $C$ is observed to depend linearly on the number of primary vertices, while the phase $\phi_0$ is almost independent of pileup. The $\phi$ modulation of $E_T$ can be removed by adding a vector in the transverse plane, $\Delta \hat{E}_T = C \cos \phi_0 \hat{x} + C \sin \phi_0 \hat{y}$ to $\hat{E}_T$ for each event.

The dependence of $\langle u_{||} \rangle$ with $Z$-boson $q_T$ should be approximately linear, and this behavior is indeed observed in both data and MC. This dependence is further studied according to the direction of the leading jet, namely, in four bins of jet $|\eta|$: [0.0–1.2], [1.2–2.4], [2.4–3.0], and [3.0–5.0]. The jets are formed by clustering particle-flow candidates using the anti-$k_T$ jet clustering algorithm [37] with a distance parameter of 0.5, and the muons are not included in the reconstruction of jets. The $(u_{||})$ behavior with $q_T$ for MC and data agrees very well when the leading jet is in the central region of the detector. When the leading jet is in the forward direction, a modest difference is observed, amounting to less than 10% in the highest $|\eta|$ bin.

The distributions of $u_{||} - \langle u_{||} \rangle$ and $u_{\perp}$ are fit to Gaussian functions whose widths are parametrized as functions of $q_T$. They depend strongly on the pileup, so they are also fit as functions of the number of vertices in the event. The weak dependence of $(u_{||})$ on the leading jet $|\eta|$ is neglected. The widths of the $u_{||} - \langle u_{||} \rangle$ and $u_{\perp}$ distributions are slightly larger in data than in MC. For example, when there are seven reconstructed vertices in the event (which corresponds to the mean number for this data set), the widths are 4%–10% larger.

A test of the hadronic recoil corrections is carried out with $Z/\gamma^* \rightarrow \mu^+\mu^-$ events. The hadronic recoil $\tilde{u}$ is calculated in each MC event, and the parallel component $u_{||}$ is rescaled by the ratio of $(u_{||})$ in data and in MC. Furthermore, the smearing of $u_{||}$ and $u_{\perp}$ is adjusted to match the resolutions measured with the data. The $\hat{E}_T$ is recalculated according to Eq. (3). Figure 3 shows $E_T$ and the $\phi$ of the $\hat{E}_T$ after applying the hadronic recoil corrections. The data and MC simulation are in excellent agreement, demonstrating that this empirical correction to $E_T$ works very well for $Z/\gamma^* \rightarrow \mu^+\mu^-$ events.

To apply the hadronic recoil correction determined in $Z/\gamma^* \rightarrow \mu^+\mu^-$ events to other MC simulations, such as $W \rightarrow \mu\nu$ events, requires defining a variable equivalent to the boson $\hat{q}_T$ in $Z/\gamma^* \rightarrow \mu^+\mu^-$ events. In $W \rightarrow \mu\nu$ events, the hadronic recoil is defined to be

$$\tilde{u} = -\hat{E}_T - \hat{p}_T,$$

(4)

where $\hat{p}_T$ is the muon transverse momentum. The hadronic recoil is decomposed into $u_{||}$ and $u_{\perp}$ components relative to
The hadronic recoil correction is applied in the manner above, and $q_T$ is recalculated. For the $W \rightarrow \mu \nu$ signal events, $q_T$ is the vector sum of the transverse momentum of the reconstructed muon and the generated neutrino. For $W \rightarrow \tau \nu$ events, the generated $W$-boson $q_T$ is used. For selected Drell-Yan background events, one muon is not reconstructed or not identified, so $q_T$ is calculated using the $p_T$ of the lost muon at the generator level. For the QCD background events, $q_T$ is identified with the $p_T$ of the reconstructed muon.

Figure 4 shows the $E_T$ distribution for the QCD control sample. We have selected only those events that pass a nonisolated muon trigger but that fail the isolated muon trigger. We also impose an anti-isolation selection cut: $\text{Iso}_{\text{track}}/p_T > 0.1$. With the application of the hadronic recoil corrections, the data and simulation are in very good agreement.
FIG. 5 (color online). Muon $p_T > 25$ GeV data sample. Examples of the extraction of the $W \to \mu\nu$ signal from fits to $E_T$ distributions of $W \to \mu\nu$ candidates in data: $0.0 \leq |\eta| < 0.2$ (a), (b), $1.0 \leq |\eta| < 1.2$ (c), (d), and $2.1 \leq |\eta| < 2.4$ (e), (f). The fits to $W^+ \to \mu^+\nu$ and $W^- \to \mu^-\bar{\nu}$ candidates are in panels (a), (c), (e) and (b), (d), (f), respectively. The ratios between the data points and the final fits are shown at the bottom of each panel. The dark shaded band in each ratio plot shows the statistical uncertainty in the shape of the MC $E_T$ distribution, and the light shaded band shows the total uncertainty, including all systematic uncertainties as discussed in Sec. VI.
B. Extraction of the asymmetry from fits to the missing transverse energy

The $W \rightarrow \mu \nu$ signal yields are obtained by fitting the $E_T$ distributions with all corrections applied. The events are selected with the default muon $p_T$ threshold of 25 GeV. The fits for $W^+$ and $W^-$ are shown in Fig. 5 for three ranges of $|\eta|$, namely, $0.0 \leq |\eta| < 0.2$, $1.0 \leq |\eta| < 1.2$, and $2.1 \leq |\eta| < 2.4$. The ratio of the data to the fit result is shown below each distribution, demonstrating good agreement of the fits with the data.

Table I summarizes the fitted yields $N^{W^+}$ and $N^{W^-}$, the correlation coefficient, the $\chi^2$ value for each fit, and the raw asymmetry $A_{\text{raw}}$. The $\chi^2$ values indicate that the fits are good. The uncertainty in $A_{\text{raw}}$ takes the covariance of $N^{W^+}$ and $N^{W^-}$ into account. Corrections to $A_{\text{raw}}$ for potential bias are discussed in the next section.

As an important cross-check, we repeat the analysis with a higher muon $p_T$ threshold of 35 GeV. The background compositions change significantly; the QCD background is reduced to about 1%. Furthermore, the predicted asymmetry differs from that predicted for the default analysis with the 25 GeV threshold. The results are summarized in Table I; they can be compared directly to the earlier measurement done with electrons [12].

| $|\eta|$ bin | $N^{W^+}$ (10^3) | $N^{W^-}$ (10^3) | $\rho(\eta)$ (\%) | $\chi^2$ (\nu_{doff} = 197) | $\mathcal{A}_{\text{raw}}$ (%) |
|-----------|----------------|----------------|-----------------|----------------|----------------|
| $p_T > 25$ GeV |
| 0.00–0.20 | 1033.0 ± 1.4 | 764.9 ± 1.2 | 14.5 | 255 | 14.912 ± 0.096 |
| 0.20–0.40 | 970.2 ± 1.3 | 713.9 ± 1.2 | 14.9 | 190 | 15.216 ± 0.098 |
| 0.40–0.60 | 1060.3 ± 1.4 | 771.5 ± 1.2 | 14.7 | 220 | 15.766 ± 0.094 |
| 0.60–0.80 | 1055.1 ± 1.4 | 752.4 ± 1.2 | 14.6 | 213 | 16.745 ± 0.093 |
| 0.80–1.00 | 935.8 ± 1.3 | 652.1 ± 1.1 | 14.5 | 245 | 17.866 ± 0.098 |
| 1.00–1.20 | 931.0 ± 1.3 | 625.4 ± 1.1 | 13.9 | 231 | 19.636 ± 0.099 |
| 1.20–1.40 | 949.0 ± 1.3 | 621.6 ± 1.1 | 14.2 | 209 | 20.848 ± 0.099 |
| 1.40–1.60 | 957.1 ± 1.3 | 607.3 ± 1.1 | 13.7 | 202 | 22.365 ± 0.099 |
| 1.60–1.85 | 1131.8 ± 1.4 | 687.6 ± 1.2 | 14.7 | 225 | 24.417 ± 0.093 |
| 1.85–2.10 | 1113.4 ± 1.4 | 656.8 ± 1.1 | 12.9 | 237 | 25.797 ± 0.094 |
| 2.10–2.40 | 843.6 ± 1.2 | 481.3 ± 1.0 | 11.8 | 244 | 27.341 ± 0.106 |
| $p_T > 35$ GeV |
| 0.00–0.20 | 574.3 ± 1.0 | 459.7 ± 0.9 | 18.9 | 203 | 11.083 ± 0.116 |
| 0.20–0.40 | 538.9 ± 0.9 | 428.9 ± 0.9 | 17.4 | 202 | 11.371 ± 0.119 |
| 0.40–0.60 | 588.3 ± 1.0 | 462.8 ± 0.9 | 18.5 | 187 | 11.935 ± 0.114 |
| 0.60–0.80 | 582.9 ± 1.0 | 453.7 ± 0.9 | 18.7 | 205 | 12.472 ± 0.114 |
| 0.80–1.00 | 513.7 ± 0.9 | 392.3 ± 0.8 | 18.7 | 218 | 13.406 ± 0.124 |
| 1.00–1.20 | 509.1 ± 0.9 | 379.2 ± 0.8 | 15.7 | 226 | 14.620 ± 0.121 |
| 1.20–1.40 | 520.2 ± 0.9 | 376.9 ± 0.8 | 16.2 | 191 | 15.970 ± 0.123 |
| 1.40–1.60 | 522.7 ± 0.9 | 370.2 ± 0.8 | 14.7 | 195 | 17.074 ± 0.123 |
| 1.60–1.85 | 614.6 ± 1.0 | 418.8 ± 0.9 | 17.5 | 239 | 18.945 ± 0.118 |
| 1.85–2.10 | 604.7 ± 1.0 | 395.8 ± 0.9 | 15.0 | 192 | 20.885 ± 0.123 |
| 2.10–2.40 | 464.3 ± 0.9 | 288.5 ± 0.8 | 14.7 | 234 | 23.357 ± 0.141 |

VI. SYSTEMATIC UNCERTAINTIES AND CORRECTIONS

The systematic uncertainties arise from many sources, including the measurement of the muon kinematics (efficiency, scale, and resolution), the modeling of the $E_T$ distributions, backgrounds, the boson $\tilde{q}_T$ distribution, and final-state radiation. In general, the total systematic uncertainty is 2–2.5 times larger than the statistical uncertainty (see Table II) and the main contributions come from the muon efficiency and from the QCD background. In the sections below, we discuss each source of systematic uncertainty, starting with muon-related quantities, followed by the $E_T$ measurement, backgrounds, and boson-related modeling issues.

We evaluate many of these uncertainties using a MC method, in which 400 sets of pseudodata are fitted to obtain the distribution of $A_{\text{raw}}$ values. This method allows us to propagate the uncertainties of the corrections to the measurement in a rigorous manner.

Several sources of potential bias are considered. To evaluate the bias, we defined a “true” muon charge asymmetry, $A_{\text{true}}$, calculated by taking the muon four-vectors and charge directly from the MC generator.

TABLE I. Summary of the fitted $N^{W^+}$, $N^{W^-}$, the correlation between the uncertainties in $N^{W^+}$ and $N^{W^-}$ ($\rho(\eta)$), the $\chi^2$ of the fit, and the extracted $A_{\text{raw}}$ for each $|\eta|$ bin. The number of degrees of freedom ($\nu_{doff}$) in each fit is 197. Here, $\rho(\eta)$ and $A_{\text{raw}}$ are expressed as percentages.
A. Muon kinematics

One source of potential bias for $A_{\text{raw}}$ is the charge of the muon. The rate of charge mismeasurement, $w$, is very small but not zero. The measured asymmetry will differ from the true asymmetry by a factor $(1 - 2w)$ assuming that the rate of mismeasurement is the same for positive and negative muons. The muon charge misidentification rate has been studied in detail and shown to have a negligible effect on the measured asymmetry [10].

The muon $p_T$ resolution can induce a spread of the measured asymmetry from $A_{\text{raw}}$, which varies from 1.5% to 5.0% [28] as a function of $|\eta|$. The resolution of $|\eta|$ is several orders of magnitude smaller than the bin widths used in this measurement; consequently, event migration around $p_T$ thresholds has a negligible effect on the measured asymmetry.

The muon momentum correction affects both the yields and the shapes of the $E_T$ distributions. To estimate the systematic uncertainty from this source, the muon $1/p_T$ correction parameters in each $\eta$-$(\phi$ bin and the muon scale global correction parameters are varied 400 times within their uncertainties. Each time the event yields can be slightly different in both data and MC simulation, and the extraction of the asymmetry is done for each of the 400 cases. The root
mean square (RMS) of the measured $A_{\text{raw}}$ variations in each muon $|\eta|$ bin is taken as the systematic uncertainty, and the bin-to-bin correlations are assumed to be zero.

The systematic uncertainties resulting from the muon momentum corrections are typically less than 40% of those from the uncertainties in the muon efficiencies (discussed below) for the $p_T > 25$ GeV sample. However, the two uncertainties are comparable for the $p_T > 35$ GeV sample for two reasons: first, the charge-dependent bias from the alignment increases with $p_T$; second, the Jacobian peak of the $W \rightarrow \mu\nu$ events is close to 35 GeV.

B. Muon efficiency ratio

A difference in the muon efficiencies for positively and negatively charged muons will cause the ratio of the selection efficiencies for $W^+$ and $W^-$ to differ from unity. This would bias the measured charge asymmetry, and we correct the $A_{\text{raw}}$ for this bias.

As discussed previously, the muon off-line and trigger efficiencies are measured in 7 bins in $p_T$ and 22 bins in $|\eta|$ for both $\mu^+$ and $\mu^-$. The off-line efficiency ratio between $\mu^+$ and $\mu^-$ is very close to unity in most of the detector regions. However, there is evidence that this ratio deviates from unity in the transition regions between the DT and CSC detectors.

We correct for this bias using efficiencies for $\mu^+$ and $\mu^-$ extracted from the $Z/\gamma^* \rightarrow \mu^+\mu^-$ data and MC samples. For each $|\eta|$ bin, an average $W$ selection efficiency $e(W^\pm)$ is obtained from the expression

$$e(W^\pm) = \frac{\Sigma (k e_{\text{data}}^\pm(p_T,\eta)/e_{\text{MC}}^\pm(p_T,\eta))}{\Sigma (k/e_{\text{MC}}^\pm(p_T,\eta))},$$

(5)

where $e_{\text{data}}^\pm(p_T,\eta), e_{\text{MC}}^\pm(p_T,\eta)$ are total muon efficiencies, $k$ are additional event-by-event weights introduced by $W$-boson $q_T$ weighting described below, and the sum is over the selected $W \rightarrow \mu\nu$ events. The efficiency ratio $\left(r^{W^+/W^-} = e^{+}/e^{-}\right)$ is used to correct the $A_{\text{raw}}$ for the efficiency bias using

$$A_{\text{true}} = A_{\text{raw}} - \frac{1}{2} (A_{\text{raw}})^2 (r^{W^+/W^-} - 1),$$

(6)

which is an expansion to leading order in $(r^{W^+/W^-} - 1)$. In addition, all MC samples are corrected for any data/MC efficiency difference.

To estimate the systematic uncertainty due to the muon efficiencies, the muon efficiency values in data and MC simulation are modified according to their errors in each $p_T$-$|\eta|$ bin independently and 400 pseudoefficiency tables are generated. In each pseudoexperiment the efficiency values are used to correct the MC simulation and $A_{\text{raw}}$. The raw asymmetry is further corrected for the efficiency ratio $r^{W^+/W^-}$ described above. The RMS of the resulting asymmetries in each $|\eta|$ bin is taken to be the systematic uncertainty originating from the determination of the ratio of the muon efficiencies. In this study, the variations for different $|\eta|$ bins are completely independent from each other, so the systematic uncertainties due to the efficiency ratio have zero correlation between different $|\eta|$ bins.

As a cross-check, Fig. 6 shows a comparison of the measured muon charge asymmetry ($A$) extracted for the positive pseudorapidity ($\eta > 0$) and negative pseudorapidity ($\eta < 0$) regions with muon $p_T > 25$ GeV (a) and muon $p_T > 35$ GeV (b) samples. The uncertainties include only the statistical uncertainty from the signal extraction and uncertainty in the determination of the efficiencies for positive and negative muons.

C. Backgrounds

The QCD background is estimated in part from the data. Nonetheless, a non-negligible systematic uncertainty
remains. We also discuss the uncertainty from the Drell-Yan background, and from the $t\bar{t}$ and $W \rightarrow \tau \nu$ backgrounds. The luminosity uncertainty enters in the estimation of these backgrounds, as discussed below.

1. QCD background

The total QCD background normalization is a parameter in the signal fit. The ratio of the QCD backgrounds in the $W^+$ and $W^-$ samples is fixed to the ratio observed in the QCD control region for each muon $\eta$ bin. The ratios are about 1.02 for the first ten $\eta$ bins and approximately 1.05 for the last $\eta$ bin, similar for both muon $p_T > 25$ and 35 GeV. There are two sources of the systematic uncertainties in the QCD background. The first is related to the ratio of the backgrounds in the $W^+$ and $W^-$ samples ("QCD $+/-$"), and the second is related to the modeling of the shape of the $E_T$ distribution in QCD events ("QCD shape").

To evaluate the systematic uncertainties QCD $+/−$, the QCD ratio is varied by ±5% and ±15% for muon $p_T$ thresholds of 25 and 35 GeV, respectively. The resulting shifts in the $A_{raw}$ are taken as the uncertainties. For the last $|\eta|$ bin, the variations are 10% (25 GeV ) and 20% (35 GeV). These variations of the QCD ratio span the maximum range indicated by the QCD MC simulation. As an additional cross-check, we fix the QCD shape to be the same for $\mu^+$ and $\mu^-$ and allow the two QCD normalizations to float in the extraction of the signal. We find that the fitted values for the ratio of the QCD backgrounds for $W^+$ and $W^-$ are within the uncertainties quoted above. The bin-to-bin correlation of these uncertainties in the asymmetries is assumed to be zero.

The second source of systematic uncertainties is a difference in the shape of the QCD background for $W^+$ and $W^-$. The QCD $E_T$ shape is taken from the MC simulation, and the recoil correction is applied as discussed in Sec. VA. Two types of variations in the shape of the QCD $E_T$ distribution are considered. First, the shape of the QCD $E_T$ distribution without the hadronic recoil correction is used in the extraction of the signal. This is done in a correlated way for the $W^+$ and $W^-$ samples. Second, the shape of the $E_T$ distribution for the QCD background is varied separately for the $W^+$ and $W^-$ samples (within the statistical uncertainties), and the resulting shapes are used in the signal extraction. These two contributions to the uncertainties from the QCD shape are then added in quadrature. The bin-to-bin correlation of the systematic uncertainties due to each shape variation is assumed to be 100%.

2. Drell-Yan background

The $Z/\gamma^* \rightarrow \mu^+\mu^-$ events in the Drell-Yan control region are used to check the Drell-Yan normalization. This is done in bins of dimuon invariant mass: 15–30, 30–40, 40–60, 60–120, 120–150, and $> 150$ GeV. The $Z/\gamma^* \rightarrow \mu^+\mu^-$ MC simulation in each bin is compared to the data yields after correcting the simulation for the data/simulation difference in pileup, $Z$-boson $q_T$, $E_T$ modeling, and efficiencies. After correcting for the detector bias and physics mismodeling, the MC simulation describes the data well, as shown in Fig. 2 for the dimuon invariant mass between 60 and 120 GeV. The data yield in this mass bin is about 3% higher than the predictions from the next-to-next-to-leading-order (NNLO) cross section as calculated with FEWZ 3.1 [38].

The ratios of data to MC simulation of the $Z/\gamma^* \rightarrow \mu^+\mu^-$ event yields as a function of the dimuon mass are used to rescale the MC prediction of the Drell-Yan background. We take the shift in the $A_{raw}$ with and without this rescaling as the systematic uncertainty. This and the PDF uncertainties in the $Z/\gamma^* \rightarrow \mu^+\mu^-$ yields are considered as systematic uncertainties due to “Drell-Yan background normalization.” This uncertainty is almost negligible at central $|\eta|$ bins and increases in the forward $|\eta|$ bins. The Drell-Yan background is larger in the forward region because of the lower efficiency of the “Drell-Yan veto” due to less detector coverage. The systematic uncertainties in the Drell-Yan background are assumed to have 100% correlation from bin to bin.

3. The $t\bar{t}$ and $W \rightarrow \tau \nu$ backgrounds

The $t\bar{t}$ and $Z/\gamma^* \rightarrow \tau^+\tau^-$ backgrounds are normalized to the integrated luminosity of the data sample after correcting for the muon efficiency difference between data and MC simulation. The uncertainty of the integrated luminosity is 2.2% [39]. The normalization of all the MC backgrounds is varied by ±2.2%, and the resulting maximum shift in $A_{raw}$ is taken as the systematic uncertainty in the determination of the luminosity. The bin-to-bin correlations are 100%.

The $t\bar{t}$ background estimate also depends on the theoretical prediction [31–33], to which we assign an additional 15%. The bin-to-bin correlation is 100%.

The $W \rightarrow \tau \nu$ background is normalized to the $W \rightarrow \mu\nu$ yields in data with a ratio obtained from a MC simulation. This ratio is largely determined by the branching fraction of $\tau$ decaying to $\mu$. A 2% uncertainty is assigned to the $W \rightarrow \tau \nu$ to $W \rightarrow \mu\nu$ ratio [40]. The correlation of this uncertainty is 100% bin to bin.

D. Modeling uncertainties

The remaining systematic uncertainties pertain to the modeling of the detector and the signal process $W \rightarrow \mu\nu$. We discuss first the issues concerning the $E_T$ distribution, then FSR, and finally the $q_T$ distribution.

1. Modeling of missing transverse momentum

To evaluate the systematic uncertainty due to the $\phi$ modulation of $E_T$, the correction for the $\phi$ modulation is removed and the shift in the $A_{raw}$ is taken as the systematic uncertainty.
The hadronic recoil correction changes the shape of the \( E_T \) distribution of all MC samples. To calculate the uncertainties resulting from this source, the average recoil and resolution parameters are varied within their uncertainties, taking into account the correlations between them. This is done 400 times, the RMS of the resulting \( A_{raw} \) variations is taken as systematic uncertainty, and bin-to-bin correlations are calculated.

Pileup can affect the \( E_T \) shapes. To estimate the effect of mismodeling the pileup in the simulation, the minimum-bias cross section is varied by \( \pm 5\% \) and the pileup distributions expected in data are regenerated. The MC simulation is then weighted to match to data, and the resulting shift in \( A_{raw} \) is treated as a systematic uncertainty due to the pileup. Pileup affects the \( E_T \) shapes for all muon \( \eta \) bins in the same direction with a correlation of 100%.

2. Final-state radiation

The emission of FSR photons in \( W \) decays reduces the muon \( p_T \) and can cause a difference in acceptance between \( W^+ \) and \( W^- \). We studied the impact of the FSR on the muon charge asymmetry using the POWHEG \( W \rightarrow \mu \nu \) MC sample. In this sample, FSR is implemented using a similar approach to parton showering and is approximate at the leading order (LO). We compare the muon charge asymmetry before and after FSR, and the difference is found to be within 0.07%–0.12% and 0.03%–0.11% for muon \( p_T \) selections of 25 and 35 GeV, respectively. The raw asymmetry values are not corrected for FSR. Instead, the full shift in the muon charge asymmetry predicted by the POWHEG MC is taken as an additional systematic uncertainty, and the bin-to-bin correlation is assumed to be 100%.

3. PDF uncertainty

The evaluation of PDF uncertainties follows the PDF4LHC recommendation [41]. The NLO MSTW2008 [2], CT10 [3], and NNPDF2.1 [42] PDF sets are used. All simulated events are weighted to a given PDF set, and the overall normalization is allowed to vary. In this way both the uncertainties in the total cross sections, as well as in the shape of the \( E_T \) distribution are considered. To estimate the systematic uncertainty resulting from the uncertainties in the CT10 and MSTW2008 PDFs, asymmetric master equations are used [2,3]. For the CT10, the 90% confidence level (C.L.) uncertainty is rescaled to 68% C.L. by dividing by a factor of 1.64485. For the NNPDF2.3 PDF set, the RMS of the \( A_{raw} \) distributions is taken. The half-width of the maximum deviation from combining all three PDF uncertainty bands is taken as the PDF uncertainty. The

| \(|\eta|\) bin | 0.0–0.2 | 0.2–0.4 | 0.4–0.6 | 0.6–0.8 | 0.8–1.0 | 1.0–1.2 | 1.2–1.4 | 1.4–1.6 | 1.6–1.85 | 1.85–2.1 | 2.1–2.4 |
|---------------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| \( p_T > 25 \text{ GeV} \) |        |        |        |        |        |        |        |        |        |        |        |
| 0.00–0.20     | 100.0  | 28.1   | 32.4   | 32.9   | 27.1   | 29.0   | 29.5   | 28.0   | 30.5   | 26.1   | 16.7   |
| 0.20–0.40     | 100.0  | 30.7   | 31.4   | 25.6   | 27.5   | 27.9   | 26.3   | 28.9   | 24.5   | 15.8   |        |
| 0.40–0.60     | 100.0  | 37.4   | 30.9   | 33.8   | 34.5   | 32.1   | 36.1   | 30.3   | 19.3   |        |        |
| 0.60–0.80     | 100.0  | 31.1   | 34.0   | 34.4   | 32.0   | 36.3   | 30.4   | 20.0   |        |        |        |
| 0.80–1.00     | 100.0  | 28.5   | 29.5   | 28.0   | 31.2   | 26.9   | 17.3   |        |        |        |        |
| 1.00–1.20     | 100.0  | 32.6   | 31.4   | 34.8   | 30.2   | 19.3   |        |        |        |        |        |
| 1.20–1.40     | 100.0  | 32.8   | 36.9   | 32.2   | 20.8   |        |        |        |        |        |        |
| 1.40–1.60     | 100.0  | 36.0   | 32.7   | 21.3   |        |        |        |        |        |        |        |
| 1.60–1.85     | 100.0  | 37.1   | 24.9   |        |        |        |        |        |        |        |        |
| 1.85–2.10     | 100.0  | 24.4   |        |        |        |        |        |        |        |        |        |
| 2.10–2.40     | 100.0  |        |        |        |        |        |        |        |        |        |        |

| \( p_T > 35 \text{ GeV} \) |        |        |        |        |        |        |        |        |        |        |        |
| 0.00–0.20     | 100.0  | 4.6    | 4.8    | 6.4    | 3.4    | 3.6    | 4.7    | 3.4    | 5.4    | 5.8    | 4.3    |
| 0.20–0.40     | 100.0  | 6.4    | 8.5    | 3.3    | 4.3    | 6.3    | 4.4    | 7.2    | 8.0    | 5.8    |        |
| 0.40–0.60     | 100.0  | 9.8    | 3.8    | 5.6    | 8.4    | 6.2    | 8.9    | 9.9    | 6.6    |        |        |
| 0.60–0.80     | 100.0  | 5.1    | 6.9    | 10.7   | 7.8    | 11.9   | 13.5   | 9.7    |        |        |        |
| 0.80–1.00     | 100.0  | 3.2    | 4.2    | 3.3    | 4.7    | 5.0    | 3.6    |        |        |        |        |
| 1.00–1.20     | 100.0  | 7.0    | 5.4    | 7.0    | 7.5    | 4.7    |        |        |        |        |        |
| 1.20–1.40     | 100.0  | 8.1    | 10.8   | 12.0   | 7.8    |        |        |        |        |        |        |
| 1.40–1.60     | 100.0  | 8.8    | 9.9    | 6.7    |        |        |        |        |        |        |        |
| 1.60–1.85     | 100.0  | 14.2   | 10.3   |        |        |        |        |        |        |        |        |
| 1.85–2.10     | 100.0  | 12.6   |        |        |        |        |        |        |        |        |        |
| 2.10–2.40     | 100.0  |        |        |        |        |        |        |        |        |        |        |

TABLE III. Correlation matrix of systematic uncertainties between different \(|\eta|\) bins. All systematic uncertainties are treated as additive. The values are expressed as percentages.
CT10 error set is used to estimate the bin-to-bin correlations. The PDF uncertainties are about 10% of the total experimental uncertainty.

4. W-boson $q_T$ modeling

To improve the agreement between data and simulation, the W-boson $q_T$ spectrum is weighted using weight factors determined by the ratios of the distribution of boson $q_T$ for $Z/\gamma^* \rightarrow \mu^+\mu^-$ events in data and MC simulation. We assume that the corrections are the same for W and Z events. This assumption is tested using two different sets of MC simulations: one from the POWHEG event generator and the other from MADGRAPH [43]. Here, the MADGRAPH simulation is treated as the “data,” and the ratio of Z-boson $q_T$ of the MADGRAPH and POWHEG simulations is compared to the same ratio in simulated W-boson events. This double ratio is parametrized using an empirical function to smooth the statistical fluctuations, and additional weights are obtained using the fitted function. We weight the POWHEG simulation to be close to the MADGRAPH simulation and measure the asymmetry again. The deviation of $A^\text{raw}$ is taken as the systematic uncertainty due to mis-modeling of W-boson $q_T$. The default boson $q_T$ weighting is based on the POWHEG simulation.

E. Total systematic uncertainty

Table II summarizes the systematic uncertainties in all $|\eta|$ bins. For comparison, the statistical uncertainty in each $|\eta|$ bin is also shown. The dominant systematic uncertainties come from muon efficiencies, QCD background, and the muon momentum correction. The correlation matrix of systematic uncertainty among $|\eta|$ bins is reported in Table III. The correlations among $|\eta|$ bins are small and do not exceed 37% and 14% for muon $p_T$ thresholds of 25 and 35 GeV, respectively. Much of the correlation is due to the systematic uncertainties in FSR and QCD background. The total covariance matrix, including both statistical and systematic uncertainties, is provided as Supplemental Material [44].

VII. RESULTS AND DISCUSSION

The measured asymmetries $A$, after all the corrections, are shown in Fig. 7 as a function of muon $|\eta|$ and summarized in Table IV. In Fig. 7 both statistical and systematic uncertainties are included in the error bars. These asymmetries are compared to predictions based on several PDF sets. The theoretical predictions are obtained using the FEWZ 3.1 [38] NLO MC calculation interfaced with the NLO CT10 [3], NNPDF2.3 [45], HERAPDF1.5 [46], MSTW2008 [2], and MSTW2008CPdeut [15] PDF sets. No EW corrections have been considered in these predictions. Results for muon $p_T > 25$ and $> 35$ GeV are shown in panels (a) and (b), respectively. The vertical error bars on data points include both statistical and systematic uncertainties. The data points are shown at the center of each $|\eta|$ bin. The theoretical predictions are calculated using the FEWZ 3.1 [38] MC tool. The PDF uncertainty for each PDF set is shown by the shaded (or hatched) band and corresponds to 68% C.L.

FIG. 7 (color online). Comparison of the measured muon charge asymmetries to the NLO predictions calculated using the FEWZ 3.1 [38] MC tool interfaced with the NLO CT10 [3], NNPDF2.3 [45], HERAPDF1.5 [46], MSTW2008 [2], and MSTW2008CPdeut [15] PDF sets. No EW corrections have been considered in these predictions. Results for muon $p_T > 25$ and $> 35$ GeV are shown in panels (a) and (b), respectively. The vertical error bars on data points include both statistical and systematic uncertainties. The data points are shown at the center of each $|\eta|$ bin. The theoretical predictions are calculated using the FEWZ 3.1 [38] MC tool. The PDF uncertainty for each PDF set is shown by the shaded (or hatched) band and corresponds to 68% C.L.

between the FEWZ 3.1 and DYNNLO 1.0 is within 1%. The predictions using the CT10 and HERAPDF1.5 PDF sets are in good agreement with the data. The predictions using the NNPDF2.3 PDF set (which include the previous CMS electron charge asymmetry result and other LHC experimental measurements [45]) are also in good agreement with the data. The predictions using the MSTW2008 PDF set are not in agreement with the data, as seen in our previous analyses [10,12]. The more recent
MSTW2008CPdeut PDF set is a variant of the MSTW2008 PDF set with a more flexible input parametrization and deuteron corrections [15]. This modification has significantly improved the agreement with the CMS data even though they have not included LHC data, as shown in Fig. 7.

Since the per-bin total experimental uncertainties are significantly smaller than the uncertainty in the current PDF parametrizations, this measurement can be used to constrain PDFs in the next generation of PDF sets.

Figure 8 shows a comparison of the measured muon charge asymmetries to the NNLO predictions. The NNLO HERAPDF1.5 PDF is used. The calculations are performed using the FEWZ 3.1 and DYNNLO 1.0 MC tools. Both MC simulations give consistent results with agreement at the 1% level. With a \( p_T \) threshold of 25 GeV, the NLO and NNLO predictions are very similar. The NNLO predictions are slightly higher in high-\(|\eta|\) regions. In the same high-\(|\eta|\) region at a \( p_T \) threshold of 35 GeV, the NNLO predictions are significantly lower than the NLO prediction. However, they agree well within the quoted PDF uncertainty in the HERAPDF1.5 PDFs.

Figure 9 shows a comparison of this result to the previous CMS electron charge asymmetry measurement extracted from part of the 2011 CMS data [12]. The electron charge asymmetry has been measured with a slightly different \( \eta \) binning because of the different subdetector geometry in the calorimeter and the muon system.
We have calculated the bin-by-bin differences between these two measurements using the first seven \( \eta \) bins, where identical bin definitions are used, and the differences are fitted with a constant. The fitted constant is larger than zero by about 1.7 sigma, and the muon channel exhibits slightly higher asymmetry in these seven \( \eta \) bins than the electron one. The electron charge asymmetry uses a statistically independent data sample. A combination of both results can be used to improve the global PDF fits. The correlation between the electron charge asymmetry and this result is expected to be small. The completely correlated systematic sources of uncertainty include the luminosity measurement, \( t \bar{t} \) background, \( W \rightarrow \tau \nu \) background, and PDF uncertainty.

The theoretical predictions for the lepton charge asymmetry are given for the kinematic region specified by the lepton \( p_T \) threshold. The \( p_T \) distribution of the \( W \) boson affects the acceptance, and hence, the predicted charge asymmetry. However, the effect on \( W^+ \) and \( W^- \) is largely correlated. Therefore, the impact on the lepton charge asymmetry measurement mostly cancels. Figure 10 shows the comparison of these results to the NLO CT10 PDF predictions based on the FEWZ 3.1 and RESBOS [49–52]. RESBOS does a resummation in boson \( q_T \) at NLO (and approximate NNLO) plus approximate next-to-next-to-leading logarithm, which yields a more realistic description of boson \( q_T \) than a fixed-order calculation such as the FEWZ 3.1. The difference between the FEWZ 3.1 and RESBOS predictions is negligible and our measurement, however precise, is not sensitive to the difference.

### VIII. THE QCD ANALYSIS OF HERA AND CMS RESULTS OF W-BOSON PRODUCTION

The main objective of the QCD analysis presented in this section is to exploit the constraining power and the interplay of the muon charge asymmetry measurements, presented in this paper, and the recent measurements of \( W + \) charm production at CMS [18] to determine the PDFs of the proton. These two data sets, together with the combined HERA inclusive cross section measurements [19], are used in an NLO perturbative QCD (pQCD) analysis.

Renormalization group equations, formulated in terms of DGLAP evolution equations [53–58], predict the dependence of the PDFs on the energy scale \( Q \) of the process in pQCD. The dependence on the partonic fraction \( x \) of the proton momentum cannot be derived from first principles and must be constrained by experimental measurements.
Deep inelastic lepton-proton scattering (DIS) experiments cover a broad range of the \((x, Q^2)\) kinematic plane. The region of small and intermediate \(x\) is probed primarily by the precise data of HERA, which impose the tightest constraints on the existing PDFs. However, some details of flavor composition, in particular the light-sea-quark content and the strange-quark distribution of the proton, are still poorly known. Measurements of the \(W^+\) and \(Z\)-boson production cross sections in proton-(anti)proton collisions are sensitive to the light-quark distributions, and the constraining power of the \(W\)-boson measurements is applied in this analysis.

The muon charge asymmetry measurements probe the valence-quark distribution in the kinematic range \(10^{-3} \leq x \leq 10^{-1}\) and have indirect sensitivity to the strange-quark distribution. The measurements of the total and differential cross sections of \(W^+\) charm production have the potential to access the strange-quark distribution directly through the LO process \(g + s \rightarrow W^+ + c\). This reaction was proposed as a way to determine the strange-quark and antiquark distributions \([59–61]\).

Before the LHC era, constraints on the strange-quark distribution were obtained from semi-inclusive charged-current scattering at the NuTeV \([62,63]\) and CCFR \([64]\) experiments. Dimuon production in neutrino-nucleus reactions is sensitive to strangeness at LO in QCD in reactions such as \(W^+ + s \rightarrow c\). These measurements probe the (anti) strange-quark density at \(x \approx 10^{-1}\) and \(Q^2\) of approximately 10 GeV\(^2\), but their interpretation is complicated by nuclear corrections and uncertainties in the charm-quark fragmentation function. The NOMAD Collaboration reported a recent determination of the strange-quark suppression factor

\[
\kappa_s(Q^2) = \frac{\int_0^1 x[\bar{s}(x, Q^2) + s(x, Q^2)]dx}{\int_0^1 x[\bar{u}(x, Q^2) + d(x, Q^2)]dx},
\]

where the value \(\kappa_s(Q^2 = 20 \text{ GeV}^2) = 0.591 \pm 0.019\) is determined at NNLO by using dimuon production \([65]\). The measurements of semi-inclusive hadron production on a deuteron target at HERMES \([66]\) have been recently reevaluated \([67]\) to obtain the \(x\) dependence of the strange-quark distribution at LO at an average \(Q^2 = 2.5 \text{ GeV}^2\). In that analysis the strange-quark distribution is found to vanish above \(x = 0.1\), but this result depends strongly on the assumptions of the kaon fragmentation function.

In a recent analysis by the ATLAS Collaboration \([68]\), the inclusive cross section measurements of \(W^\pm\) and \(Z\)-boson production were used in conjunction with DIS inclusive data from HERA. The result supports the hypothesis of a symmetric composition of the light-quark sea in the kinematic region probed, i.e., \(\bar{s} = \bar{d}\).

The LHC measurements of associated production of \(W\) bosons and charm quarks probe the strange-quark distribution in the kinematic region of \(x \approx 0.012\) at the scale \(Q^2 = m_W^2\). The cross sections for this process were recently measured by the CMS Collaboration \([18]\) at a center-of-mass energy \(\sqrt{s} = 7 \text{ TeV}\) with a total integrated luminosity of 5 fb\(^{-1}\). The results of the QCD analysis presented here use the absolute differential cross sections of \(W + \text{charm}\) production, measured in bins of the pseudorapidity of the lepton from the \(W\) decay, for transverse momenta larger than 35 GeV.

### A. Details of the QCD analysis

The NLO QCD analysis is based on the inclusive DIS data \([19]\) from HERA, measurements of the muon charge asymmetry in \(W\) production for \(p_T > 25\) GeV, and measurements of associated \(W + \text{charm}\) production \([18]\). The treatment of experimental uncertainties for the HERA data
follows the prescription of HERAPDF1.0 [19]. The correlations of the experimental uncertainties for the muon charge asymmetry and W + charm data are taken into account.

The theory predictions for the muon charge asymmetry and W + charm production are calculated at NLO by using the MCFM program [31,32], which is interfaced to APPLGRID [69].

The open source QCD fit framework for PDF determination HERAFITTER [19,70,71] is used and the partons are evolved by using the QCDFNUM program [72]. The TR’ [2,73] general mass variable flavor number scheme is used for the treatment of heavy-quark contributions with the following conditions: (i) heavy-quark masses are chosen as $m_c = 1.4$ GeV and $m_b = 4.75$ GeV, (ii) renormalization and factorization scales are set to $\mu_r = \mu_f = Q$, and (iii) the strong coupling constant is set to $\alpha_s(m_Z) = 0.1176$.

The $Q^2$ range of HERA data is restricted to $Q^2 \geq Q^2_{\text{min}} = 3.5$ GeV$^2$ to assure the applicability of pQCD over the kinematic range of the fit. The procedure for the determination of the PDFs follows the approach used in the MSTW group [2,73].

The second analysis is denoted as “free-s fit,” in which the interplay between the muon charge asymmetry measurements and W + charm production data is analyzed. The strange-quark distribution is determined by fitting 15 parameters in Eqs. (8)–(12). Here, instead of Eq. (11) $d$ and $\bar{s}$ are fitted separately by using the functional forms

$$x\bar{d}(x) = A_{\bar{d}}x^{B_{\bar{d}}}(1-x)^{C_{\bar{d}}}, \quad (13)$$

$$x\bar{s}(x) = A_{\bar{s}}x^{B_{\bar{s}}}(1-x)^{C_{\bar{s}}}. \quad (14)$$

Additional constraints $A_{\bar{d}} = A_{\bar{d}}$ and $B_{\bar{d}} = B_{\bar{d}}$ are applied to ensure the same normalization for $\bar{u}$ and $\bar{d}$ densities at $x \to 0$. The strange-antiquark parameter $B_{\bar{d}}$ is set equal to $B_{\bar{d}}$, while $A_{\bar{d}}$ and $C_{\bar{d}}$ are treated as free parameters of the fit, assuming $xs = x\bar{s}$. This parametrization cannot be applied to HERA DIS data alone, because those data do not have sufficient sensitivity to the strange-quark distribution.

### B. The PDF uncertainties

The PDF uncertainties are estimated according to the general approach of HERAPDF1.0 [19] in which experimental, model, and parametrization uncertainties are taken into account. A tolerance criterion of $\Delta \chi^2 = 1$ is adopted for defining the experimental uncertainties that originate from the measurements included in the analysis. Model uncertainties arise from the variations in the values assumed for the heavy-quark masses $m_b$, $m_c$ with $4.3 \leq m_b \leq 5$ GeV, $1.35 \leq m_c \leq 1.65$ GeV, and the value of $Q^2_{\text{min}}$ imposed on the HERA data, which is varied in the interval $2.5 \leq Q^2_{\text{min}} \leq 5.0$ GeV$^2$. The parametrization uncertainty is estimated similarly to the HERAPDF1.0 procedure: for all parton densities, additional parameters are added one by one in the functional form of the parametrizations such that Eqs. (8)–(11) are generalized to $Ax^B(1-x)^C(1+Dx)$ or $Ax^B(1-x)^C(1+Dx+E x^2)$. In the free-s fit, in addition, the parameters $B_{\bar{d}}$ and $B_{\bar{d}}$ are decoupled. Furthermore, the starting scale is varied within $1.5 \leq Q^2_{0} \leq 2.5$ GeV$^2$. The parametrization uncertainty is constructed as an envelope built from the maximal differences between the PDFs resulting from all the parametrization variations and the central fit at each $x$ value. The total PDF uncertainty is obtained by adding experimental, model, and parametrization uncertainties in quadrature. In the following, the quoted uncertainties correspond to 68% C.L.

### C. Results of the QCD analysis

The muon charge asymmetry measurements, together with HERA DIS cross section data, improve the precision of the valence quarks over the entire $x$ range in the fixed-$s$ fit. This is illustrated in Fig. 11, where the $u$ and $d$
The change in the shapes of the light-quark distributions in supplemental material. valence, relevant for the W-boson production, $Q^2 = m_W^2$. The results at $Q^2 = 1.9$ GeV$^2$ can be found in supplemental material. A change in the shapes of the light-quark distributions within the total uncertainties is observed. The details of the effect on the experimental PDF uncertainty of $u$ valence, $d$ valence, and $d/u$ distributions are also given in supplemental material.

In the next step of the analysis, the CMS $W + c$ charm measurements are used together with the HERA DIS data and the CMS muon charge asymmetry. Since both CMS $W$-boson production measurements are sensitive to the strange-quark distribution, a free-$s$ fit can be performed. The advantage of including these two CMS data sets in the 15-parameter fit occurs because the $d$-quark distribution is significantly constrained by the muon charge asymmetry data, while the strange-quark distribution is directly probed by the associated $W + $charm production measurements. In the free-$s$ fit, the strange-quark distribution $s(x, Q^2)$ and the strange-quark fraction $R_s(x, Q^2) = (s + \bar{s})/(u + \bar{d})$ are determined. The global and partial $\chi^2$ values for each data set are listed in Table V, where the $\chi^2$ values illustrate a general agreement among all the data sets.

In Fig. 12, the resulting NLO parton distributions are presented at $Q^2_0 = 1.9$ GeV$^2$ and $Q^2 = m_W^2$. The strange quark distribution $s(x, Q^2)$ and the ratio $R_s(x, Q^2)$ are illustrated in Fig. 13 at the same values of $Q$ as in Fig. 12. The total uncertainty in Fig. 12 is dominated by the parametrization uncertainty in which most of the expansion in the envelope is caused by the decoupling parameter choice $B_s \neq B_d$. The strange-quark fraction rises with energy and reaches a value comparable to that of $u$ and $d$ antiquarks at intermediate to low $x$. Also, a suppression of $R_s$ at large $x$ is observed, which scales differently with the energy. This result is consistent with the prediction provided by the ATLAS Collaboration [68], where inclusive $W$- and $Z$-boson production measurements were used to determine $r_s = 0.5(s + \bar{s})/\bar{d}$. In Ref. [68], the NLO value of $r_s = 1.03$ with the experimental uncertainty $\pm 0.19_{\text{exp}}$ is quoted at $x = 0.023$ and $Q^2 = 1.9$ GeV$^2$. In the framework used, the two definitions of the strange-quark fraction are very similar at the starting scale $Q^2_0$ and the values $R_s$ and $r_s$ can be directly compared.

![FIG. 11 (color online). Distributions of $u$ valence (top) and $d$ valence (bottom) quarks as functions of $x$ at the scale $Q^2 = m_W^2$. The results of the 13-parameter fixed-$s$ fit to the HERA data and muon asymmetry measurements (light shaded band), and to HERA only (dark hatched band) are compared. The total PDF uncertainties are shown. In the bottom panels the distributions are normalized to one for a direct comparison of the uncertainties. The change of the PDFs with respect to the HERA-only fit is represented by a solid line.](image-url)
In the free-s fit, the strangeness suppression factor is determined at $Q^2 = 20 \text{ GeV}^2$ to be $\kappa_s = 0.5_{-0.10}^{+0.12} (\text{exp})^{+0.05}_{-0.06} (\text{model})^{+0.13}_{-0.10} (\text{parametrization})$, which is in agreement with the value [65] obtained by the NOMAD experiment at NNLO.

The impact of the measurement of differential cross sections of $W$+charm production on the strange-quark distribution and strangeness fraction $R_s$ is also examined by using the Bayesian reweighting [13,14] technique. The results qualitatively support the main conclusions of the current NLO QCD analysis. Details can be found in supplemental material.

**IX. SUMMARY**

The $W \to \mu \nu$ lepton charge asymmetry is measured in $pp$ collisions at $\sqrt{s} = 7 \text{ TeV}$ using a data sample corresponding to an integrated luminosity of 4.7 fb$^{-1}$ collected with the CMS detector at the LHC (a sample of more than 20 million $W \to \mu \nu$ events). The asymmetry is measured in 11 bins in absolute muon pseudorapidity, $|\eta|$, for two different muon $p_T$ thresholds, 25 and 35 GeV. Compared to the previous CMS measurement, this measurement
significantly reduces both the statistical and the systematic uncertainties. The total uncertainty per bin is 0.2%–0.4%. The data are in good agreement with the theoretical predictions using CT10, NNPDF2.3, and HERAPDF1.5 PDF sets. The data are in poor agreement with the prediction based on the MSTW2008 PDF set, although the agreement is significantly improved when using the MSTW2008/CPdeut PDF set. The experimental uncertainties are smaller than the current PDF uncertainties in the present QCD calculations. Therefore, this measurement can be used to significantly improve the determination of PDFs in future fits.

This precise measurement of the $W \to \mu\nu$ lepton charge asymmetry and the recent CMS measurement of associated $W +$ charm production are used together with the cross sections for inclusive deep inelastic scattering at HERA in an NLO QCD analysis of the proton structure. The muon charge asymmetry in $W$-boson production imposes strong constraints on the valence-quark distributions, while the $W +$ charm process is directly sensitive to the strange-quark distribution.

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