Revisiting the AMBA AHB bus case study

Ioannis Filippidis Richard M. Murray

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Abstract

This report describes a number of changes to the ARM AMBA bus case study from that lead to significant reduction in synthesis time. In addition, it identifies the reason of blowup for the synthesized strategies in earlier studies as lack of binary decision diagram (BDD) reordering during strategy construction. Enabling dynamic BDD reordering with the group sifting algorithm, we synthesized strategies for as many as 18 masters, with both the original and revised specifications. This conclusion is based on detailed experimental measurements that show the changes of BDD sizes over time for the fixpoint and other variables during the nested fixed point computation, including the cumulative time spent on BDD reordering and the total number of BDD nodes. The measurements were obtained for eight different cases, allowing to compare the original with the revised specifications, with strategy reordering enabled or not, and conjoining the weak fairness guarantees or merging them into a single Büchi automaton. The revised specification proposed here is expressed using the open Promela language.

Contents

1 Introduction

2 Revising the formal specification

2.1 A1 vs ARM standard

2.2 Weakening A1

2.3 Proof of weakening

2.4 Undating G2

2.5 A3 becomes trivially true

2.6 Coupling between A1 and G2

2.6.1 Coupling

2.6.2 Modifying A1 to remove the coupling

2.7 Reducing the number of variables modeling the environment

2.7.1 Substitutions

2.7.2 Removing array HLOCK

2.8 Merging progress guarantees

2.9 Changes to variables
3 Experimental results

3.1 Experimental configurations

3.1.1 Enabling reordering during strategy construction
3.1.2 Reordering using group sifting
3.1.3 Number of variables

3.2 Instrumentation of the GR(1) synthesis algorithm

3.2.1 The different configurations
3.2.2 Measurements for each phase

3.3 Observations

3.3.1 General
3.3.2 Comparison of variants

3.4 Trade-off of counter in state space

3.4.1 The two alternatives
3.4.2 Effect of reordering and memoization

4 Relevant work

A Note on determinism of automata
B Revised AMBA AHB specification
C Original AMBA AHB specification

List of Figures

1 Revising assumption A1
2 Automaton for guarantee G2
3 Abstraction of interest from the product of Fig. 1a and Fig. 2
4 The form of a single Büchi automaton with one accepting state that is equivalent to N weak fairness goals
5 Total run time vs number of masters for synthesizing an arbiter using the revised specification, with fairness as a Büchi automaton, and reordering enabled during strategy construction. These repeated experiments are different runs than those from which the detailed tracing plots were generated.
6 Peak memory consumption for the experiments of Fig. 5
7 Revised spec with BA and strategy reordering
8 Revised spec with BA but no strategy reordering
9 Original spec with BA and strategy reordering
10 Original spec with BA but no strategy reordering
11 Revised spec with conjunction and strategy reordering
12 Revised spec with conjunction but no strategy reordering
13 Original spec with conjunction and strategy reordering
14 Original spec with conjunction but no strategy reordering (last runs with memory upgrade)
15 Revised with BA, w/o divided by w/ reordering
16 Original with BA, w/o divided by w/ reordering
Revised spec with conjunction and strategy reordering: 5 masters.

Revised spec with conjunction and strategy reordering: 6 masters.

Revised spec with conjunction and strategy reordering: 7 masters.

Revised spec with conjunction and strategy reordering: 8 masters.

Revised spec with conjunction and strategy reordering: 9 masters.

Revised spec with conjunction and strategy reordering: 10 masters.

Revised spec with conjunction and strategy reordering: 11 masters.

Revised spec with conjunction and strategy reordering: 12 masters.

Revised spec with conjunction and strategy reordering: 13 masters.

Revised spec with conjunction and strategy reordering: 14 masters.

Revised spec with conjunction and strategy reordering: 15 masters.

Revised spec with conjunction and strategy reordering: 16 masters.

Revised spec with conjunction and strategy reordering: 17 masters.

Revised spec with conjunction and strategy reordering: 18 masters.

Revised spec with conjunction and strategy reordering: 19 masters.

Revised spec with conjunction and strategy reordering: 20 masters.

Revised spec with conjunction but no strategy reordering: 2 masters.

Revised spec with conjunction but no strategy reordering: 3 masters.

Revised spec with conjunction but no strategy reordering: 4 masters.

Revised spec with conjunction but no strategy reordering: 5 masters.

Revised spec with conjunction but no strategy reordering: 6 masters.

Revised spec with conjunction but no strategy reordering: 7 masters.

Revised spec with conjunction but no strategy reordering: 8 masters.

Revised spec with conjunction but no strategy reordering: 9 masters.

Revised spec with conjunction but no strategy reordering: 10 masters.

Revised spec with conjunction but no strategy reordering: 11 masters.

Original spec with BA and strategy reordering: 2 masters.

Original spec with BA and strategy reordering: 3 masters.

Original spec with BA and strategy reordering: 4 masters.

Original spec with BA and strategy reordering: 5 masters.

Original spec with BA but no strategy reordering: 2 masters.

Original spec with BA but no strategy reordering: 3 masters.

Original spec with BA but no strategy reordering: 4 masters.

Original spec with BA but no strategy reordering: 5 masters.

Original spec with BA but no strategy reordering: 6 masters.

Original spec with BA but no strategy reordering: 7 masters.

Original spec with BA but no strategy reordering: 8 masters.

Original spec with BA but no strategy reordering: 9 masters.

Original spec with BA but no strategy reordering: 10 masters.
<table>
<thead>
<tr>
<th>Original spec with conjunction and strategy reordering</th>
<th>masters</th>
</tr>
</thead>
<tbody>
<tr>
<td>10 masters</td>
<td>109</td>
</tr>
<tr>
<td>11 masters</td>
<td>110</td>
</tr>
<tr>
<td>12 masters</td>
<td>111</td>
</tr>
<tr>
<td>13 masters</td>
<td>112</td>
</tr>
<tr>
<td>14 masters</td>
<td>113</td>
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<td>15 masters</td>
<td>114</td>
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<td>16 masters</td>
<td>115</td>
</tr>
<tr>
<td>17 masters</td>
<td>116</td>
</tr>
<tr>
<td>18 masters</td>
<td>117</td>
</tr>
<tr>
<td>2 masters</td>
<td>118</td>
</tr>
<tr>
<td>3 masters</td>
<td>119</td>
</tr>
<tr>
<td>4 masters</td>
<td>120</td>
</tr>
<tr>
<td>5 masters</td>
<td>121</td>
</tr>
<tr>
<td>6 masters</td>
<td>122</td>
</tr>
<tr>
<td>7 masters</td>
<td>123</td>
</tr>
<tr>
<td>8 masters</td>
<td>124</td>
</tr>
<tr>
<td>Comparison with [1]</td>
<td>125</td>
</tr>
<tr>
<td>Synthesis time for the revised specification using a BA (w/o strategy reordering)</td>
<td>126</td>
</tr>
<tr>
<td>Fig. 45 to Fig. 59, and conjoining liveness goals (using strategy reordering), Fig. 60 to Fig. 78, compared to results from [1, 2]</td>
<td>126</td>
</tr>
<tr>
<td>Listing corresponding to formula in text</td>
<td>127</td>
</tr>
</tbody>
</table>

References:
1. [1]
2. [2]


1 Introduction

The ARM processor Advanced Microcontroller Bus Architecture (AMBA) [8] specifies a number of different bus protocols. Among them, the Advanced High-performance (AHB) architecture has been studied extensively in the reactive synthesis [4, 5, 6, 7, 1, 2, 9, 10] and verification [11, 12, 13, 14, 15, 16, 17] literature.

The AHB bus comprises of masters that need to communicate with slaves, and an arbiter that controls the bus and decides which master is given access to the bus. The arbiter receives requests from the masters that desire to access the bus, and must respond in a weakly fair way. In other words, every master that keeps uninterruptedly requesting the bus must eventually be granted access to it. Note that the AMBA technical manual does not specify any requirement on fairness, but instead leaves that decision to the designer. For automated synthesis, weak fairness is one possible formalization that ensures servicing of all the masters.

In addition, a master can request that the access be locked. However, the arbiter makes no promises as to whether a request for the lock will be granted. If the arbiter does lock the access, then it guarantees to maintain the lock until the request for locking is withdrawn by the master that currently owns the bus.

A specification for the arbiter appeared in [4] and is presented in detail in [1]. In [2], the authors formalize also the specifications for masters and slaves connected to the bus. Here, we revise the specification of [1], and express it in the open PROMELA language.

The original specification includes some properties that are not in the GR(1) fragment. In [1], these properties are translated to deterministic Büchi automata, by introducing auxiliary variables for representing the nodes of the automaton. These variables are added to the problem’s alphabet. The resulting formulae are much less readable, and not easy to modify and experiment with.

Here, we specify these properties directly as processes (transition systems), with progress states where needed.

During expression of the specification in the PROMELA language, there are two possible representations of the fairness requirements. In the original specification, fairness is required by a conjunction of recurrence formulae

\[ \bigwedge_{i=0}^{N-1} \Box \Diamond (\text{request}[i] \rightarrow \text{master} = i) \]

It is possible to rewrite this conjunction as a Büchi automaton (BA) with a single accepting state, which checks each fairness condition, one after the other. The property described by the BA is equivalent to that described by the conjunction. This change reduces the number of recurrence goals from \( N \) to 1. In the GR(1) synthesis algorithm [18], this reduces the number of fixed point computations.

An initial motivation for this modification was to obtain a specification parameterized by the domain of a counter variable (local to the BA process), which avoids the need to regenerate the specification from an auxiliary script (as has been typically the case in similar studies).

Another motivation was to explore the design space, and the sensitivity of the specification, by varying the amount of detail that was specified. In particular, we were interested in observing whether the runtimes improve significantly in case that the order of goals was given and fixed. Note that the Büchi automaton above does not fix the order that goals have to be satisfied. This variant was an initial attempt that placed more constraints on the design, to see whether those “hints” to the synthesizer had a significant effect, or not.
This experimentation revealed a notable difference between the two alternatives. When using a Büchi automaton, there is a single liveness goal. So a single sub-strategy is synthesized for this goal, and it need not be combined with other sub-strategies, as there are none. In contrast, when there are multiple liveness goals, the individual sub-strategies need to be combined into a single one. The process of combining the sub-strategies is disruptive to the BDD variable ordering. As a result, it is impossible to scale synthesis using a conjunction of liveness guarantees, without enabling dynamic reordering during the synthesis of the final, monolithic strategy. Reordering during strategy construction is not necessary, and in fact, if the liveness goals are represented as BA, then reordering during that final phase of synthesis has a negative effect on runtime. The trade-off is introducing auxiliary variables (a counter) in the state space that are used to represent the nodes of the BA. Together with the sequencing of goals that the BA represents, this leads to longer runtimes, but scales without difficulty to a larger number of masters, without any need for reordering during strategy construction.

The revised specification is given in Listing 1, where some additional changes involve weakening the assumptions, and modifying assumption A1. An instance of the original specification is given in Listing 2. In 1, assumption A1 requires that for locked undefined-length bursts, masters eventually withdraw their request to access the bus. This assumption is not explicit in the ARM standard, so we modify it, by requiring that masters withdraw only their request for the lock, not for bus access. Weakening the assumptions also allowed abstracting the array HLOCK of N lock requests by the two bits that are only referenced in it. Another difference is that a Mealy game is solved here, and a Moore in 2.

In Section 2, we describe how the specification was revised, referring to the technical ARM specification. In Section 3, we present the experiments, measurements, observations, and conclusions based on the measurements and the GR(1) synthesis algorithm.

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2 Revising the formal specification

Declarative specifications for this case study were presented in [4, 5, 1, 2]. These papers do not mention the processors used as hardware, so the difference in processor clock speed is unknown, so the speedups are compared only as absolute time intervals.

We base our specifications on those of [1]. In that case study, each requirement was obtained either:

- by formalizing the AMBA AHB standard, or
- by adding some desired (e.g., fair arbiter) or auxiliary properties (e.g., auxiliary scheduling variables start, decide) that are left unspecified in the standard.

When initially formalized in LTL, some of the requirements yield formulae that are not in the GR(1) fragment. Nonetheless, there do exist deterministic Büchi automata for these particular properties (the notion of determinism is discussed in Appendix A). The next step in [1] is to translate these properties to (symbolic) deterministic Büchi automata, whose states are represented by auxiliary variables that become part of the problem’s alphabet. This translation is not always trivial.

The translation step can be done either manually or automatically. However, with automatic translation the user has little control over the form of the determined automaton. The ability to modify the automaton itself proves important during development and, especially, while debugging the specification. By changing directly the automaton, one can observe what effects selected modifications have on realizability, and understand better the problem’s structure.

Another aspect of writing LTL formulae, instead of attempting to express the design intent as an automaton, is that the former may require nesting of operators, which quickly becomes unmanageable. Writing imperatively a Büchi automaton for the same property can prove easier. Moreover, as the reduction of progress conditions in the AMBA example demonstrates, the availability of imperative elements can encourage modifications that significantly reduce the problem’s complexity, while preserving the required property. For these reasons, describing directly automata can benefit the synthesis process.

The properties from [1] have been either:

- changed, because they did not correspond to the ARM standard, or
- expressed directly as automata, in case they do not belong to GR(1) (similarly to what was done in [1] by defining the automata directly in LTL), or
- equivalently expressed as automata, because this allows significant reduction in synthesis time, or
- reformulated to an equivalent, but syntactically simpler formula, in several cases due to the availability of array arithmetic, or
- remained unchanged.

The correspondence is noted inline, for example, “G 5” is the guarantee with index 5 in [1]. In what follows, we consider each specification in incremental order, using the numbering in [1].
2.1 A1 vs ARM standard

Consider assumption A1, stating that for locked indefinite duration bursts, the master that controls the bus must eventually withdraw its request for access to the bus. This property is expressed in temporal logic as:

$$\Box \left( (HMASTLOCK \land (HBURST = INCR)) \rightarrow \bigcirc \bigcirc \neg HBUSREQ[HMASTER] \right)$$

The ARM standard states that:

- Sec.3.11.2, paragraph 2, p.3-29 and Sec. 3.11.4, p.3-33: A master can lose ownership of the bus early, because the arbiter decides to limit their access time.
- Sec.3.11.2, paragraph 3, p.3-29 and Sec. 3.11.5, p.3-34: If a master requests both:
  1. bus access (by setting HIGH the signal $HBUSREQ[i]$), and
  2. locking of its access (by setting HIGH the signal $HLOCK[i]$)

then: if the arbiter decides to give the bus to the master, and lock the access, then the arbiter guarantees that it will maintain the lock,

“until the locked sequence has completed”.

The question becomes what “completion” of a locked sequence means. If a sequence has predefined length (determined by $HBURST$ and some other signals), then the arbiter knows how long the request will last (G3 addresses this for length-4 locked bursts).

However, for indefinite length bursts, the arbiter does not know a priori when the locked sequence will terminate. In [1], the “locked sequence” is interpreted as the time interval until the master who was granted locked access stops requesting bus access. The master withdraws its request for access by setting $HBUSREQ[HMASTER]$ to false. As a consequence, the progress assumption A1 requires that a master who requested indefinite locked access, eventually withdraw its request to communicate.

However, it is not clear from the standard whether this behavior is intended. In Table 2-2, entry $HLOCK$, p.2-5, it is stated that

“When HIGH, this signal indicates that the master requires locked access to the bus, and no other master should be granted the bus until this signal is LOW.”

The “until” above suggests that the arbiter can grant the bus to another master, after master $j$ deasserts the signal $HLOCK[j]$. This implies that deassertion of $HLOCK[j]$ by the current master suffices to allow the arbiter to reassign the bus. It does not refer to the signal $HBUSREQ[j]$.

2.2 Weakening A1

Based on the previous note, we can arrive at a weaker assumption, that decouples the:

1. lock requests $HLOCK$, from the
2. bus access requests $HBUSREQ$.
As soon as a master withdraws its request for locking its access, the arbiter is allowed to assign the bus to another master. This does not oblige the current master to withdraw its request for bus access. So the master is free to keep requesting bus access ($HBUSREQ$), but is obliged to stop requesting the lock ($HLOCK$). In other words, a master is not allowed to lock the bus forever (but may keep forever requesting access to the bus, without ever lowering $HBUSREQ[j]$, in agreement with Sec. 3.11.2, paragraph 1, p.3-29 “A bus master ...may request the bus during any cycle”).

The modified assumption $A1$ is

$$\Box((HMASTLOCK \land (HBURST = INCR)) \rightarrow \bigcirc\Box\neg HLOCK[HMASTER])$$

(2)

Later, we will remove the conjunct $(HBURST = INCR)$, for reasons explained then.

Note that, up to here, this allows the master to stop requesting bus access (LOW $HBUSREQ$), but keep requesting the lock (during an indefinite length burst). Sec 3.11.2, paragraph 6, p.3-29 assumes that the master never does this. It is formulated as assumption $A3$ (Eq. (5)). As commented later, we remove assumption $A3$, because it is not necessary for realizability (and simplifying it has no adverse effect – weakening of assumptions is desirable [19]).

### 2.3 Proof of weakening

We now prove that the previous change to $A1$ from Eq. (1) to Eq. (2) weakens the assumptions. In other words, the modified assumption Eq. (2) is implied by the assumptions in the original specification. The original assumptions contain the conjuncts

$$\bigwedge_{i=0}^{N-1}((HMASTER = i) \rightarrow (BUSREQ \leftrightarrow HBUSREQ[i]))$$

(3)

$$= \Box(\Box BUSREQ \leftrightarrow HBUSREQ[HMASTER])$$

$$\Box((HMASTLOCK \land (HBURST = INCR)) \rightarrow \bigcirc\Box\neg BUSREQ)$$

(4)

$$\Box \bigwedge_{i=0}^{N-1} (HLOCK[i] \rightarrow HBUSREQ[i]).$$

(5)

Eqs. (3) and (5) imply that

$$\Box(\Box BUSREQ \leftrightarrow HBUSREQ[HMASTER]) \implies$$

$$\Box(\Box \neg BUSREQ \rightarrow \neg HBUSREQ[HMASTER]) \overset{\text{Eq. (5)}}{\implies}$$

$$\Box(\Box \neg BUSREQ \rightarrow \neg HLOCK[HMASTER]).$$

By this and Eq. (3), it follows that

$$\Box((HMASTLOCK \land (HBURST = INCR)) \rightarrow \bigcirc\Box\neg HLOCK[HMASTER])$$

(7)

This proves that Eq. (2) is implied by the original specification of [19].

### 2.4 Updating G2

The replacement of $HBUSREQ[HMASTER]$ by $HLOCK[HMASTER]$ in $A1$ implies that the same replacement applies to $G2$ also.
2.5 A3 becomes trivially true

The replacement of $\text{HBUSREQ[HMASTER]}$ by $\text{HLOCK[HMASTER]}$ in A1 allows each master $i$ to keep $\text{HBUSREQ}[i]$ always HIGH. As a result, assumption A3 does not constrain the environment in a way essential for realizability (since the environment can set HIGH all the elements of array $\text{HBUSREQ}$ forever). Therefore, we drop assumption A3.

2.6 Coupling between A1 and G2

2.6.1 Coupling

In this section, we analyze the dependence of G2 on A1. The conclusion motivates simplifying A1. An initial (wrong) attempt to express the LTL property A1 in Promela (without using Fig.9(a) [1]) resulted in the code

```c
assume env proctype withdraw_lock(){
    progress:
    do
        :: lock && (burst == INCR);
        do
            :: ! master_lockreq; break
            :: true /* wait */
            od
        :: else
        od
    od
}
```

We have used $\text{master_lockreq}$ in place of $\text{HMASTLOCK[HMASTER]}$, for reasons explained later. This automaton is shown in Fig. 1a.

The correct automaton for property A1 is Fig.9(a), and is expressed by the code

```c
assume env proctype withdraw_lock(){
    progress0:
    do
        :: lock && (burst == INCR); goto S1;
        :: else
        od;
    S1:
    do
        :: (! master_lockreq) && ! (lock && (burst == INCR));
        goto progress0
        :: (! master_lockreq) && (lock && (burst == INCR));
        goto progress1
        :: else
        od;
    progress1:
    do
        :: master_lockreq; goto S1;
}
```
(a) Initial attempt to represent Eq. (2) as an automaton.

(b) Revised assumption A1 as an automaton.

Figure 1: Revising assumption A1.

:: (! master_lockreq) && (lock && (burst == INCR));
:: else;
    goto progress0
od
}

The specification with the first automaton as A1 is unrealizable. Using the second automaton, the specification is realizable.

Consider the first automaton and the automaton for G2, shown in Fig. 2:

assert sys proctype maintain_lock(){
    do
        :: lock && start && (burst == INCR);
        do
            :: ! start && ! master_lockreq; break
            :: ! start
            od
        :: else
        od
    }

Each of them has two states: an “initial” one (outer do), and a “waiting” one (inner do). The product of the two automata has 4 states, and an abstraction is shown in Fig. 3.

State 0: both automata at the initial states. The system has not yet lost at this state.

State 1: both automata at the “waiting” states. As soon as the environment sets master_lockreq, the system returns to the initial state and is released, so that it can start a new bus access later.
(The environment also returns to its initial state).

State 2: the environment at the initial state, and the system at the waiting state. The system has lost, because the initial A1 state is a progress state, and the environment can keep $HBURST$ different from $INCR$, to remain at its initial state. So the environment is not obliged to withdraw the lock request $master\_lockreq$, leaving the system indefinitely trapped at its waiting state.

State 3: the system at the initial state, and the environment at its waiting state. Note that state 3 is reachable, because the environment can reach its waiting state as soon as $lock \land (burst == INCR)$, whereas the system has to wait until $start$, and $start$ can be delayed arbitrarily long by the environment keeping $ready\_LOW$ (G1).

If the system transitions to its waiting state, but the environment remains at its waiting state, then state 1 is reached. If the environment transitions to its initial state, but the system remains at its initial state, then state 0 is reached. These two transitions cause no problems.

The transition that makes the system lose is if the environment returns to its initial state, and the system transitions to its waiting state, both at the same time. If this happens, then state 2 is reached, and the system has lost. This transition is possible, only if $burst == INCR$ can hold when $! master\_lockreq$.

This execution is not possible with the automaton of Fig.9(a), because in order for the environment to return to $progress0$ there, it must set both $burst \neq INCR$ and $! master\_lockreq$ at the same time. This implies that the environment will return to its initial state, without letting the system transition from its initial, to its waiting state. So it prevents the transition from state 3 to the losing state 1.

### 2.6.2 Modifying A1 to remove the coupling

The coupling analyzed previously requires that the original automaton be used for assumption A1 (which can be rewritten, using structured programming constructs). The resulting specification is more fragile (for example, the initial attempt at manually writing an automaton contained the error above). Moreover, it results in longer synthesis time.
For these reasons, we simplify assumption A1 to

\[ \square (\text{HMASTLOCK} \rightarrow \lozenge \lozenge \neg \text{HLOCK}[\text{HMASTER}]) \]  

Using the replacement bit variable ! master_req, this is equivalent to the (much simpler) automaton

```plaintext
assume env proctype withdraw_lock(){
    progress:
    do
        :: lock;
        do
            :: ! master_lockreq; break
            :: true /* wait */
        od
        :: else
    od
}
```

This automaton is shown in Fig. 1b. Note that the only modification from the erroneous initial attempt is to remove the conjunct burst == INCR from the guard lock && (burst == INCR). The modified assumption A1 states that if the current master is granted the lock, then next it must eventually withdraw the locking request. This assumption is reasonable, because no master that has been granted locked bus access is entitled to continue requesting the lock indefinitely. Moreover, it decouples the type of burst from the lock requests.
2.7 Reducing the number of variables modeling the environment

2.7.1 Substitutions

Earlier, we used \texttt{master\_lockreq} in place of \texttt{HLOCK[HMASTER]}. The reason is that assumption A3 does not constrain \texttt{HLOCK} any more (and was dropped, as explained earlier), so each bit in the array \texttt{HLOCK} can take any value in its domain (no constraint). Therefore, it is not significant which bit this is, so \texttt{HMASTER} can be removed, abstracting the value \texttt{HLOCK[HMASTER]} by a single environment bit \texttt{master\_lockreq}.

This implies the same replacement, of \texttt{HLOCK[HMASTER]} by the bit \texttt{master\_lockreq}, also in G2.

The only remaining use of array \texttt{HLOCK} is in G7. Using arrays, the guarantee G7 can be expressed as

\[ \langle \text{decide} \rightarrow (\text{lockmem}' \leftrightarrow \text{HLOCK[grant']}) \rangle \]

We observe that \texttt{HLOCK[grant']} above is again an element of the array \texttt{HLOCK}. Before replacement with bit \texttt{master\_lockreq}, the only constraint on \texttt{HLOCK} was A1. A1 required that \texttt{HLOCK[HMASTER]} eventually become LOW, if locked access is granted.

In general, \texttt{grant'} will be a master different than the current (so as to serve all masters), therefore \texttt{HLOCK[grant']} takes values independently of \texttt{HLOCK[HMASTER]}. So we abstract \texttt{HLOCK[grant']} by a single environment bit \texttt{grantee\_lockreq}. The bit \texttt{grantee\_lockreq} represents the lock request of that master that is selected as the next grantee. The values of \texttt{grantee\_lockreq} are not constrained in any way.

The initial condition assumption A4 implies that \texttt{master\_lockreq} and \texttt{grantee\_lockreq} must be false initially.

2.7.2 Removing array HLOCK

The replacements:

1. \texttt{HLOCK[HMASTER]} by the single bit \texttt{master\_lockreq}, and of

2. \texttt{HLOCK[HGRANT[i]']} by the single bit \texttt{grantee\_lockreq}

weaken the assumptions. Therefore, they are desirable.

After these replacements, the array \texttt{HLOCK} does not appear in any guarantee or assumption (except the initial condition A4). Therefore, the array \texttt{HLOCK} can now be removed.

In the best case (\(N = 16\) masters), the replacement of the bit array \texttt{HLOCK} by the 2 bits \texttt{master\_lockreq} and \texttt{grantee\_lockreq} resulting in a reduction by 16 - 2 = 14 bits. So it reduces by 28 (14 unprimed and 14 primed copies) the number of environment variables in the binary decision diagram (BDD). This reduction is significant, because environment variables are universally quantified, leading to an exponential increase in the number of possible next inputs. This reduction reduced synthesis time.

Instead of 32 possible next environment valuations for \texttt{HLOCK}, this replacement reduces them to 4, so a reduction of universal branching by a factor of 8.
2.8 Merging progress guarantees

The second significant change was the merging of the $N$ weak fairness guarantees in G9:

$$\bigwedge_{i=0}^{N-1} \Box \Diamond (\text{HBUSREQ}[i] \rightarrow (\text{HMASTER} = i))$$

into an equivalent Büchi automaton with a single progress state. This reduces the $N$ inner fixed point computations in the GR(1) synthesis algorithm, to only a single fixed point computation. As a result, the number of masters $N$ does not increase any more the number of progress goals that the system must satisfy.

The Büchi automaton used is

```cpp
/* G9: weak fairness */
assert active proctype fairness(){
  int(0, N) count;
  do
    :: ! request[count] || (master == count);
    if
      :: (count < N) && (count' == count + 1)
      :: (count == N) && (count' == 0);
      progress: skip
    fi
    :: else
  od
}
```

This automaton is equivalent with the conjunction of weak fairness guarantees, because it
• “looks” at each one of them in turn,
• waits until that progress requirement is satisfied (! request[count] || (master == count))
• then increments the counter count and waits for the next fairness guarantee to be satisfied,
until it reaches the last fairness guarantee. At this point it has completed a round of each fairness
guarantee being satisfied, so it visits the progress state, and starts a new round. The structure of
the automaton (after unfolding of the program graph) is shown in Fig. 4.

The automaton is equivalent to the LTL property
\[
\square \left( \diamond \left( \left( \text{HBUSREQ}[0] \rightarrow (\text{HMASTER} = 0) \right) \land 
\bigcirc \left( \left( \text{HBUSREQ}[1] \rightarrow (\text{HMASTER} = 1) \right) \land \ldots \right) \right) \right)
\]

This demonstrates the merits of using a language that allows directly writing sequential com-
position. Note that this automaton does not constrain in any way the order in which the arbiter
chooses masters to grant the bus. In other words, it does not restrict the master to using a particular
priority for choosing masters.

Note that, after all these changes, the result is a fully parameterized program, where one need
only change a single preprocessor definition (#define N 15), in order to define a different number
of masters in the bus.

2.9 Changes to variables

Note that we use an integer variable to model the HGRANT signal. This conforms to the standard,
because the standard requires that exactly one HGRANT_i bit be true at a time. So we reduce
the number of BDD variables by a factor exponential in the number of masters. The synthesized
integer values of HGRANT_i can readily be mapped to patterns of 7 bits, where only a single one
is true.
3 Experimental results

3.1 Experimental configurations

The experiments were performed with the open PROMELA compiler \cite{20} and the SLUGS GR(1) synthesizer as back-end \cite{21}. The hardware used has:

1. Intel(R) Xeon® X5550 processing core
2. runs Ubuntu 14.04.1
3. 11 GB RAM (3 experiments in the last batch were run after an upgrade to 27GB RAM).

The modifiable parameters are listed in the table below. The parameters that are fixed are assigned values in the table. The remaining parameters vary over the experiments. The number of variables varies by the size of the masters, and is given for the different specifications in Fig. 7 to Fig. 14.

In addition, there are two versions of the specification: the original from \cite{1}, and the revised one proposed here. The original specification is obtained by translating to PYTHON the Perl generator script for AMBA specifications that is distributed on the Anzu homepage. The new generator produces the same specifications, but in open PROMELA syntax (as ltl blocks for assumptions and assertions). For each specification, there are two equivalent variants that we evaluate: conjoining the fairness formulae, or merging them into a single Büchi automaton.

In the experiments, we are interested in the effect of the following parameters: strategy reordering, machine (memory, CPU frequency), conjunction vs BA, original vs revised AMBA specification, initial variable ordering.

3.1.1 Enabling reordering during strategy construction

In all experiments, reordering is enabled during realizability. Checking realizability without reordering causes a memory blowup very fast, going from 309K BDD nodes in the strategy for 2 masters, to 1.8M BDD nodes for 3 masters. For comparison, when dynamic reordering during realizability is enabled, in the worst case, the strategy BDD for 2 masters has about 20K nodes, and about 200K nodes for 3 masters.

In SLUGS, reordering during strategy construction is disabled by default. Enabling reordering during this second phase proved the enabling factor for scalable synthesis of the AMBA case study when the (weak) fairness guarantees are conjoined. In contrast, the revised specification with the fairness requirements represented as a single Büchi automaton does not require that reordering be enabled during construction of the strategy.

The price is longer runtimes. Nonetheless, when strategy reordering is deactivated, the runtimes using a BA do not scale as quickly as memory does when using a conjunction of fairness formulae. Without reordering during strategy construction, the shared BDD quickly blows up, for both the original and revised specifications, as shown in Fig. 123 and Fig. 84, respectively.

Note that in experiments with the same specification, the realizability phase has the same parameters, independently of whether the strategy is constructed with reordering enabled or not. Typically, realizability terminates, whereas construction of a strategy can cause a memory blowup.

\textsuperscript{1}The worst case in terms of strategy size blowup is the original spec with reordering disabled during strategy construction.
Table 1: Parameters of the experiments (both those constant and variable).

<table>
<thead>
<tr>
<th>parameter</th>
<th>value</th>
</tr>
</thead>
<tbody>
<tr>
<td>mem</td>
<td>10GB</td>
</tr>
<tr>
<td>cache</td>
<td>uint-1</td>
</tr>
<tr>
<td>min hit</td>
<td>1</td>
</tr>
<tr>
<td>blowup</td>
<td>1.2</td>
</tr>
<tr>
<td>reorder</td>
<td>group sifting</td>
</tr>
<tr>
<td>reorder during strategy construction</td>
<td>varies</td>
</tr>
<tr>
<td>number of variables</td>
<td>varies</td>
</tr>
<tr>
<td>universal branching (number of env vars)</td>
<td>varies</td>
</tr>
<tr>
<td>initial var order</td>
<td>natural order (1, 2, 10, ...)</td>
</tr>
</tbody>
</table>

or time out, limiting the number of masters for which we could synthesize an arbiter, for certain combinations of specification with parameters.

3.1.2 Reordering using group sifting

Rudell’s sifting \( 22 \) is the reordering algorithm used by SLUGS. After experiments with different reordering algorithms, group sifting \( 23 \) was found as the algorithm that produces the best results for this case study. Group sifting is an extension of sifting that automatically detects affinity between variables, and creates temporary groups. Grouped variables are shifted together during swaps of levels. This can improve the results by avoiding a situation where shifting one of the two tightly coupled variables finds no better place, because the other variable is “pulling it back” (known as rubber-band effect), and the same happening to the second variable results in no overall change. In contrast, moving both variables together enables finding a better position for both of them.

3.1.3 Number of variables

Original vs revised specification The number of variables differs between the original and revised specifications. It also differs for each variant of these specifications. In the original specification, the number of variables grows faster with the number of masters, than it does in the revised one. The reasons are:

- The use of one lock request bit for each master. The lock requests have been abstracted by using two bits, without any conflict with the requirements described in the AMBA technical manual \( 3 \). This change leads to \( N - 2 \) fewer environment variables, where \( N \) is the number of masters. It is a significant gain, because not only does it reduce the state space size, but also the degree of universal branching (at each state, the environment has fewer “next moves”).

- The one-hot encoding of the system variables “master” and “grantee” in the original specification. In the revised specification, these variables are encoded as bitvectors. The two formulations are equivalent. As a result, in the revised specification, the number of system variables increases only when the number of masters reaches boundaries of powers of 2. The effect is reduction of state space size.
Table 2: Overview of results.

<table>
<thead>
<tr>
<th></th>
<th>Strategy reordering</th>
<th>Specification</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>with</td>
<td>original</td>
</tr>
<tr>
<td>Conjunction of fairness</td>
<td>w/o</td>
<td>slow</td>
</tr>
<tr>
<td></td>
<td></td>
<td>memory blowup</td>
</tr>
<tr>
<td>Büchi automaton</td>
<td>with</td>
<td>very slow</td>
</tr>
<tr>
<td></td>
<td>w/o</td>
<td>slow</td>
</tr>
<tr>
<td></td>
<td></td>
<td>ok (slower)</td>
</tr>
<tr>
<td></td>
<td></td>
<td>memory blowup</td>
</tr>
</tbody>
</table>

Fig. 7 to Fig. 14 show how the number of variables scales for the original and revised specification variants considered.

**Conjunction vs Büchi automaton** The number of variables also between a specification that includes fairness in the form of conjoined recurrence formulae, and as a Büchi automaton. The representation of a Büchi automaton requires introducing an auxiliary bitvector for representing the current node of the automaton. This is also discussed later, in the section Section 3.4 analyzing the trade-off of using a BA, instead of handling weak fairness at the level of the strategy construction algorithm.

Note that when using a BA in the original specification, there is one extra fairness guarantee from one of the automata (Eq.G2.4 in [1]). This results in one extra point in the “combined strategy” plots. The number of points in a “combined strategy” plot is equal to the number of recurrence goals in the game, plus one (the initial point). This guarantee is not present in the revised specification, because it describes a safety property that can be represented by a process without progress states.

**Optimizing away unused auxiliary variables** Note that if the processes of a player do not include any atomic blocks, then no auxiliary variables are added for requesting and granting atomic execution of processes. In the specification of the AMBA arbiter used here, no atomic blocks are necessary, so the auxiliary variables $ex_s$ and $pm_s$ are not used, thus the compiler does not define them. This avoids unnecessarily increasing the number of states.

### 3.2 Instrumentation of the GR(1) synthesis algorithm

#### 3.2.1 The different configurations

The experiments were performed for 8 different combinations: original and revised specification, using conjunction or a BA, and with strategy reordering enabled and disabled. An overview of the results is shown in Table 2, and in detail in Fig. 26 to Fig. 124.

#### 3.2.2 Measurements for each phase

The measurements were obtained by inserting in SLUGS statements that print the information and dumping this output to a log file. The most relevant set of changes can be found in a fork of SLUGS on github. There are three distinct phases of computation:

1. Fixed-point iteration that decides realizability and stores the interant sets $X, Y, Z$. 

2. Construction of individual strategies, one for each recurrence goal.

3. Combination of the individual strategies into a single one that iterates through them.

Each phase involves different quantities to be measured, so it is instrumented slightly differently.

The realizability phase involves three nested iterations, each one computing a fixed point. The three variables are $X, Y, Z$, and at a high level, the iteration has the structure of the following $\mu$-calculus formula $\nu Z. \mu Y. \nu X$. So $X, Z$ are greatest fixed points and $Y$ is a least fixed point. Moreover, $X$ is in the innermost loop, so it is the most frequently updated variable, with variable $Y$ less frequently updated, and variable $Z$ the least frequently updated one.

Each one of the variables $X, Y, Z$ represents a set symbolically, by reference to a BDD in the shared BDD managed by Cudd. Therefore, the size of these variables can be quantified as the number of BDD nodes in the referenced BDD. This number is obtained by calling the function Cudd_DagSize.

In addition, the total number of nodes in the shared BDD is recorded with Cudd_ReadNodeCount. The total size of the shared BDD corresponds to the current memory use of Cudd (though they are not identical entities). Reordering is triggered based on growth of the shared BDD, as measured by its number of nodes. The total number of nodes also quantifies the randomness with which new nodes have been added \cite{24}, and so how inefficiently representable the intermediate results of the fixed point computation are, compared to the final result (that is typically much smaller, as has been observed in the literature \cite{25}).

Plotting the sizes of the variables $X, Y, Z$ provides a view into the fixed-point iteration. However, it is difficult or impossible to tell when a loop starts or ends, by only inspecting how $X, Y$ and $Z$ change. For this reason, the indices of the:

1. current recurrence assumption, and
2. current recurrence guarantee

are also recorded. Finally, the total runtime is measured with the function gettimeofday from sys/time.h, and the time spent reordering so far is measured with the function Cudd_ReadReorderingTime.

The remaining measurements are taken during construction of the strategy. During construction of the individual strategies, the quantities recorded are the total time, reordering time so far, goal pursued by the strategy under construction, the total number of nodes in the shared BDD, the number of nodes in the BDD of the current strategy, as well as the number of BDD nodes in the sets of new and accumulated states.

The final phase combines the individual strategies into a single one. Besides the total and reordering time, the goal whose strategy is currently combined in the overall strategy, the total BDD nodes, and the nodes in the combined strategy (so far) are recorded.

### 3.3 Observations

#### 3.3.1 General

The figures can be understood as follows. There are two sets of figures:

1. the top four figures extend through the whole computation, whereas
2. the bottom three figures contain more details for each of the individual phases.
In most runs, reordering takes a high, to very high, percentage of the total runtime. A sense of this ratio can be obtained visually by comparing the bisector in Fig. 26(i) (dotted) to the cumulative reordering time (solid line). The final values of each run are collected in Fig. 7 to Fig. 14.

The periods of constancy of the reordering curve correspond to BDD computations. The highlighted period corresponds to the construction of individual strategies.

Fig. 26(ii) shows the goal that is currently pursued during realizability, and the goal whose strategy is currently being constructed during the individual strategy construction phase. For the revised specification, there is only a single recurrence goal, so this curve is constant. For the original specification, the successive goals appear as increments.

Fig. 26(iii) shows the recurrence assumption that is currently being considered during the fixed-point computation of $Y$. For every iteration of the middle fixed-point $Y$, the computation takes a disjunction over all assumption, which results in fast cycling in the plot.

The total number of nodes in the shared BDD is shown in Fig. 26(iv). We can identify the following features that correspond to the computation. Initially, the total number of nodes grows slowly, and several reorderings occur (flat or slightly decreasing periods). These are triggered by the initial exploration of the state space. The new states added to the BDD trigger changes to the variable ordering, which tends to “adapt” to the sets that need to be represented.

After the first outer fixed point is completed, the stored iterants ($X, Y$ over the inner iterations, to be used for constructing the strategies in the final fixed-point iteration) are deleted, if a fixed-point was not reached in the current iteration. This dereferencing appears as abrupt reductions of the number of nodes to almost zero (forming “teeth”). So each such reduction corresponds to one iteration of the $Z$ greatest fixed-point.

During construction of the strategy, the number of nodes increases monotonically, if no reordering is enabled. If reordering is enabled in the strategy construction phase, then the number of nodes may be observed to decrease, and in those cases, its rate of growth is always limited (with the trade-off of long interruptions for reordering). Note that the allocated memory never decreases, because Cudd does not release memory, even when nodes are deleted.

In some total node count plots, a dashed line is visible, starting from the end of the highlighted period. This corresponds to the time between the completion of individual strategy construction, and the first iteration of combining strategies. It is included, because reordering during that period can defer the initial iteration of constructing the combined strategy.

In the second set of figures, Fig. 26(v) shows the sizes of the fixed-point variables $X, Y, Z$. We can observe that $X, Y$ are quite similar in size. This is expected, because $Y$ is assigned the union of $X$ over the recurrence assumptions (and there are only two recurrence assumptions). The variable $Z$ exhibits more interesting behavior. In the initial iteration, $Z$ is always 1 ($\top$), by definition. Its size changes in the following iterations, remaining constant in each one of those iterations. As a result, the curve of variable $Z$ indicates the successive loops of the outer fixed-point iteration. We can also observe “humps” of $X, Y$ during the intermediate results of each outer iteration. Note that these humps of $X, Y$, and steps of $Z$ correspond to the teeth in Fig. 26(vi).

Fig. 26(vi) shows the BDD size of the strategies for the individual goals, as they are being constructed. It also shows the number of accumulated and new states. It is interesting that these curves are typically close to constant. Another observation is that, in most cases, this phase is brief, unless reordering is triggered. When strategy reordering is disabled, this phase is always of short duration.

---

2 Counting over the graphics within each subfigure proceeds from top to bottom.
Finally, the size of the cumulative strategy as the individual ones are being combined is shown in Fig. 26(vii). Note that in the revised specification, when using a BA, there is only one recurrence goal, so only a single point in this plot (there is only a single sub-strategy, so not multiple ones to be combined). In cases without reordering and with conjunction, the rapid growth of the combined strategy can be observed in this plot. Another observed feature is the triggering of reordering during this last phase, and that if triggered, reordering takes most of the time in this phase.

Fig. 7 to Fig. 14 summarize the previous measurements over the number of masters, per experimental configuration. The top plot shows how the numbers of variables change. The number of variables determines the size of the state space, and this is a difference between specification variants. The number of environment variables gives an upper bound on the amount of universal branching in a problem.

The second plot summarizes the total number of nodes in the shared BDD, and the size of the synthesized strategies. This is a measure of how larger the intermediate BDDs are from the desired result.

The third and fourth plots show how total, realizability, and reordering times scale with the number of masters, and how they compare to each other.

Fig. 15 to Fig. 25 are the most interesting, and compactly represent the conclusions from the all the experiments. The show ratios of quantities between different selected pairs of configurations, those that we think are the most interesting and useful.

### 3.3.2 Comparison of variants

From the measurements, we observe that

- The revised specification is orders of magnitude better than the original, as seen in Figs. 24 and 25.
- Using a Büchi automaton, reordering during strategy construction is not needed, and undesired, as seen in Figs. 15 and 16.
- Using conjunction of fairness goals, reordering is necessary, as seen in Figs. 17 and 18.
- Conjunction with reordering is clearly better than the BA, by about an order of magnitude, as seen in Figs. 19 to 21.
- Using a Büchi automaton is clearly better than conjunction without reordering, by several orders of magnitude, as seen in Figs. 22 and 23. In absence of strategy reordering, only the BA scales.

### 3.4 Trade-off of counter in state space

In the following, by realizability phase, we refer to the fixed-point computation that stratifies the set of states to produce the layers that comprise the attractors 18, 20. This phase stores these sets in memory as an array of BDD nodes. By construction phase, we refer to the construction of a strategy that satisfies the original specification, using the layers produced by the realizability phase. So the realizability phase precedes the construction phase.
3.4.1 The two alternatives

In this section, we evaluate the two (equivalent) alternatives for representing liveness goals:

1. as a conjunction of the form $\Box\Diamond p_0 \land \Box\Diamond p_1 \land \cdots \land \Box\Diamond p_{N-1}$

2. as a single Büchi automaton with the structure shown in Fig. 4.

Representing the Büchi automaton augments the system state by the integer counter that describes the current node. This counter is linear in the number of fairness guarantees.

Conjoining multiple fairness goals leads to the construction of a sub-strategy for each goal. In order to obtain the overall strategy, these sub-strategies are combined, using a counter to keep track of the currently active sub-strategy. This other counter comprises the transducer’s memory.

Note that both counters have the same range. In the final strategy, both counters appear as BDD variables. The difference is that the first counter is present during the attractor computations (realizability phase), whereas the second is introduced only at the end (strategy construction phase).

This means that using a Büchi automaton shifts the transducer memory from the construction, to the realizability phase. As a result, the state space of the game is multiplied by a factor of $k$, the number of fairness goals. In the experiments presented here, the default implementation of the synthesis algorithm in SLUGS was used. In the worst case, the time complexity increases by a factor $O(k^3)$, measured in number of symbolic controllable preimage computations. An improved implementation employing fixpoint memoization is available as a SLUGS option, but was not used. The improved implementation would be affected by a factor of $O(k^2)$.

Nonetheless, an improvement is observed, because synthesis remains scalable, even without reordering during the construction phase. This can be understood by considering three effects.

Including the counter in the state space encodes the problem symbolically, instead of explicitly. It avoids the combination of individual strategies later, which is an enumerated procedure that iterates over the transducer’s memory (the counter introduced during the construction phase). The number of sub-strategies to disjoin increases linearly with the number of liveness goals. This can affect the suitability of the variable order significantly, and it does. The measurements indicate an exponential growth of the total number of nodes in the shared BDD, as the number of masters grows.

The second effect is the reduction of intermediate results of BDD computations. As has been observed in the literature, unstructured breadth-first search of the state space creates intermediate sets that have “a lot of ad hoc detail”. For a fixed variable ordering, this semi-random detail decreases the likelihood of these intermediate sets being efficiently representable as BDDs. As described in, an interesting analog is the entropy of random strings in information theory. The Büchi automaton introduces structure in the state space that is relevant to the fairness constraints.

The third effect is the abruptness of changes to how far from optimal the current order is. The experimental results suggest that disjoining individual strategies at the end is disruptive to the variable ordering, necessitating reordering to avoid BDD blowup. In contrast, shifting the counter to the state space allows the order to adapt over a longer number of iterations, while the BDD is changing less abruptly (i.e., during the attractor computations).

Another effect is the reduction of size of the goal set. This can lead to a simpler BDD for the $Z$ variable in the fixed-point computation. It is observed as small BDD size for $Z$ for a specification that uses a Büchi automaton. For example, in Fig. 25 to Fig. 57, $Z$ is much smaller than $X$ and $Y$. In contrast, a conjunction of recurrence formulae leads to large $Z$ values, much larger in many cases than the variables $X, Y$. This difference can be seen in Fig. 80 to Fig. 88.
3.4.2 Effect of reordering and memoization

In most cases, 65% or more, of the total runtime is spent reordering the shared BDD. A similar observation has been made in [1]. Therefore, reordering is a controlling factor of overall runtime. Reordering by sifting considers all BDDs in a “neighborhood” of the BDD being reordered. This allows it to cross boundaries between basins of attraction associated with different local minima.

However, it also makes sifting (and reordering in general) quite sensitive to the details of intermediate results during the fixed-point computation. In turn, these intermediate results can depend on the order that individual goals are visited, as well as variations in the encoding, e.g., of a program graph by integers. Overall, these variations can cause reordering to “touch” expensive neighborhoods, resulting in significant runtime outliers being observed. The sensitivity of BDD computations is a common observation in the symbolic model checking literature [25].

This effect can be further amplified by the cache, where results are memoized (mapping arguments to results of the operation being performed). As more memory is required, results are overwritten, causing regeneration, thus deviating from the practically bilinear cost of BDD operations, to the worst-case exponential [28], Programmer’s Guide.

Configuring Cudd memory limit Initially, fragile behavior was observed with Cudd. This was due to the maximum memory limit of Cudd that by default is set to 3GB in Slugs. Increasing this limit to that available on the machine resulted in improved performance, and very significantly reduced fragile behavior. This limit can be set with the function Cudd_SetMaxCacheHard. A relevant suggestion can be found in the Cudd Programmer’s manual, Sec. “Modifiable parameters”.

Effect of initial order Another factor that introduced significant variability and adversely affected runtime was the initial order of variables. In the initial implementation, the initial order of variables was not controlled. The result was semi-random, because the enumeration of items in PYTHON sets and dictionaries can vary arbitrarily.

Later, the BDD variables were initially sorted in natural order by their bitblasted “flat” name (i.e., after translation to logic and bitblasting). The flat name of a variable includes scope information in the form of a prefix. This brings together in ordering variables that are defined in the same namespace, bits in the same bitvector, and variables with similar names (with respect to natural ordering). Initial sorting by natural order improved the results.

Using a natural lexical ordering to obtain the initial variable order brings together variables in the same scope. The revised specification contains more information in the form of variable scopes, because local variables in the same process have the same prefix in the logic formulae (for example, a local variable x will become pid0_x). The original specification is flat (no processes in the syntactic description), so it contains less scoping information.

---

3 In BFCuddManager.h as of f9eef21813e7e6d23c0bd63563b587cc1cee95c6 (line 30).
Figure 5: Total run time vs number of masters for synthesizing an arbiter using the revised specification, with fairness as a Büchi automaton, and reordering enabled during strategy construction. These repeated experiments are different runs than those from which the detailed tracing plots were generated.
Figure 6: Peak memory consumption for the experiments of Fig. 5.

Table 3: Index of measurements for each experiment.

<table>
<thead>
<tr>
<th>Revised</th>
<th>Y</th>
<th>Y</th>
<th>Y</th>
<th>Y</th>
</tr>
</thead>
<tbody>
<tr>
<td>BA</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Reorder</td>
<td>Y</td>
<td>Y</td>
<td>Y</td>
<td>Y</td>
</tr>
<tr>
<td>masters</td>
<td></td>
<td></td>
<td></td>
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<table>
<thead>
<tr>
<th></th>
<th>Experiments</th>
</tr>
</thead>
<tbody>
<tr>
<td>2</td>
<td>Fig. 60</td>
</tr>
<tr>
<td>3</td>
<td>Fig. 61</td>
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<tr>
<td>4</td>
<td>Fig. 62</td>
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<td>Fig. 63</td>
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<td>Fig. 76</td>
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<td>19</td>
<td>Fig. 77</td>
</tr>
<tr>
<td>20</td>
<td>Fig. 78</td>
</tr>
</tbody>
</table>
Figure 7: Revised spec with BA and strategy reordering.
Figure 8: Revised spec with BA but no strategy reordering.
Figure 9: Original spec with BA and strategy reordering.
Figure 10: Original spec with BA but no strategy reordering.
Figure 11: Revised spec with conjunction and strategy reordering.
Figure 12: Revised spec with conjunction but no strategy reordering.
Figure 13: Original spec with conjunction and strategy reordering.
Figure 14: Original spec with conjunction but no strategy reordering (last runs with memory upgrade).
Figure 15: Revised with BA, w/o divided by w/ reordering.
Figure 16: Original with BA, w/o divided by w/ reordering.
Figure 17: Revised with conjunction, w/o divided by w/ reordering.
Figure 18: Original with conjunction, w/o divided by w/ reordering.
Figure 19: Original with conjunction and with reordering, divided by original BA w/o reordering.
Figure 20: Revised conjunction divided by BA (both with reordering).
Figure 21: Revised conjunction with reordering, divided by BA w/o reordering.
Figure 22: Revised conjunction divided by BA (both w/o reordering).
Figure 23: Revised conjunction w/o reordering, divided by BA with reordering.
Figure 24: Original with BA divided by revised with BA (both w/o reordering).
Figure 25: Original with conjunction divided by revised with conjunction (both with reordering).
Figure 26: Revised spec with BA and strategy reordering: 2 masters.
Figure 27: Revised spec with BA and strategy reordering: 3 masters.
Figure 28: Revised spec with BA and strategy reordering: 4 masters.
Figure 29: Revised spec with BA and strategy reordering: 5 masters.
Figure 30: Revised spec with BA and strategy reordering: 6 masters.
Figure 31: Revised spec with BA and strategy reordering: 7 masters.
Figure 32: Revised spec with BA and strategy reordering: 8 masters.
Figure 33: Revised spec with BA and strategy reordering: 9 masters.
Figure 34: Revised spec with BA and strategy reordering: 10 masters.
Figure 35: Revised spec with BA and strategy reordering: 11 masters.
Figure 36: Revised spec with BA and strategy reordering: 12 masters.
Figure 37: Revised spec with BA and strategy reordering: 13 masters.
Figure 38: Revised spec with BA and strategy reordering: 14 masters.
Figure 39: Revised spec with BA and strategy reordering: 15 masters.
Figure 40: Revised spec with BA and strategy reordering: 16 masters.
Figure 41: Revised spec with BA and strategy reordering: 17 masters.
Figure 42: Revised spec with BA and strategy reordering: 18 masters.
Figure 43: Revised spec with BA and strategy reordering: 19 masters.

64
Figure 44: Revised spec with BA and strategy reordering: 20 masters.
Figure 45: Revised spec with BA but no strategy reordering: 2 masters.
Figure 46: Revised spec with BA but no strategy reordering: 3 masters.
Figure 47: Revised spec with BA but no strategy reordering: 4 masters.
Figure 48: Revised spec with BA but no strategy reordering: 5 masters.
Figure 49: Revised spec with BA but no strategy reordering: 6 masters.
Figure 50: Revised spec with BA but no strategy reordering: 7 masters.
Figure 51: Revised spec with BA but no strategy reordering: 8 masters.
Figure 52: Revised spec with BA but no strategy reordering: 9 masters.
Figure 53: Revised spec with BA but no strategy reordering: 10 masters.
Figure 54: Revised spec with BA but no strategy reordering: 11 masters.
Figure 55: Revised spec with BA but no strategy reordering: 12 masters.
Figure 56: Revised spec with BA but no strategy reordering: 13 masters.
Figure 57: Revised spec with BA but no strategy reordering: 14 masters.
Figure 58: Revised spec with BA but no strategy reordering: 15 masters.
Figure 59: Revised spec with BA but no strategy reordering: 16 masters.
Figure 60: Revised spec with conjunction and strategy reordering: 2 masters.
Figure 61: Revised spec with conjunction and strategy reordering: 3 masters.
Figure 62: Revised spec with conjunction and strategy reordering: 4 masters.
Figure 63: Revised spec with conjunction and strategy reordering: 5 masters.
Figure 64: Revised spec with conjunction and strategy reordering: 6 masters.
Figure 65: Revised spec with conjunction and strategy reordering: 7 masters.
Figure 66: Revised spec with conjunction and strategy reordering: 8 masters.
Figure 67: Revised spec with conjunction and strategy reordering: 9 masters.
Figure 68: Revised spec with conjunction and strategy reordering: 10 masters.
Figure 69: Revised spec with conjunction and strategy reordering: 11 masters.
Figure 70: Revised spec with conjunction and strategy reordering: 12 masters.
Figure 71: Revised spec with conjunction and strategy reordering: 13 masters.
Figure 72: Revised spec with conjunction and strategy reordering: 14 masters.
Figure 73: Revised spec with conjunction and strategy reordering: 15 masters.
Figure 74: Revised spec with conjunction and strategy reordering: 16 masters.
Figure 75: Revised spec with conjunction and strategy reordering: 17 masters.

96
Figure 76: Revised spec with conjunction and strategy reordering: 18 masters.
Figure 77: Revised spec with conjunction and strategy reordering: 19 masters.
Figure 78: Revised spec with conjunction and strategy reordering: 20 masters.
Figure 79: Revised spec with conjunction but no strategy reordering: 2 masters.
Figure 80: Revised spec with conjunction but no strategy reordering: 3 masters.
Figure 81: Revised spec with conjunction but no strategy reordering: 4 masters.
Figure 82: Revised spec with conjunction but no strategy reordering: 5 masters.
Figure 83: Revised spec with conjunction but no strategy reordering: 6 masters.
Figure 84: Revised spec with conjunction but no strategy reordering: 7 masters.
Figure 85: Revised spec with conjunction but no strategy reordering: 8 masters.
Figure 86: Revised spec with conjunction but no strategy reordering: 9 masters.
Figure 87: Revised spec with conjunction but no strategy reordering: 10 masters.
Figure 88: Revised spec with conjunction but no strategy reordering: 11 masters.
Figure 89: Original spec with BA and strategy reordering: 2 masters.
Figure 90: Original spec with BA and strategy reordering: 3 masters.
Figure 91: Original spec with BA and strategy reordering: 4 masters.
Figure 92: Original spec with BA and strategy reordering: 5 masters.
Figure 93: Original spec with BA and strategy reordering: 6 masters.
Figure 94: Original spec with BA but no strategy reordering: 2 masters.
Figure 95: Original spec with BA but no strategy reordering: 3 masters.
Figure 96: Original spec with BA but no strategy reordering: 4 masters.
Figure 97: Original spec with BA but no strategy reordering: 5 masters.
Figure 98: Original spec with BA but no strategy reordering: 6 masters.
Figure 99: Original spec with BA but no strategy reordering: 7 masters.
Figure 100: Original spec with BA but no strategy reordering: 8 masters.
Figure 101: Original spec with conjunction and strategy reordering: 2 masters.
Figure 102: Original spec with conjunction and strategy reordering: 3 masters.
Figure 103: Original spec with conjunction and strategy reordering: 4 masters.
Figure 104: Original spec with conjunction and strategy reordering: 5 masters.
Figure 105: Original spec with conjunction and strategy reordering: 6 masters.
Figure 106: Original spec with conjunction and strategy reordering: 7 masters.
Figure 107: Original spec with conjunction and strategy reordering: 8 masters.
Figure 108: Original spec with conjunction and strategy reordering: 9 masters.
Figure 109: Original spec with conjunction and strategy reordering: 10 masters.
Figure 110: Original spec with conjunction and strategy reordering: 11 masters.
Figure 111: Original spec with conjunction and strategy reordering: 12 masters.
Figure 112: Original spec with conjunction and strategy reordering: 13 masters.
Figure 113: Original spec with conjunction and strategy reordering: 14 masters.
Figure 114: Original spec with conjunction and strategy reordering: 15 masters.
Figure 115: Original spec with conjunction and strategy reordering: 16 masters.
Figure 116: Original spec with conjunction and strategy reordering: 17 masters.
Figure 117: Original spec with conjunction and strategy reordering: 18 masters.
Figure 118: Original spec with conjunction but no strategy reordering (last runs with memory upgrade): 2 masters.
Figure 119: Original spec with conjunction but no strategy reordering (last runs with memory upgrade): 3 masters.
Figure 120: Original spec with conjunction but no strategy reordering (last runs with memory upgrade): 4 masters.
Figure 121: Original spec with conjunction but no strategy reordering (last runs with memory upgrade): 5 masters.
Figure 122: Original spec with conjunction but no strategy reordering (last runs with memory upgrade): 6 masters.
Figure 123: Original spec with conjunction but no strategy reordering (last runs with memory upgrade): 7 masters.
Figure 124: Original spec with conjunction but no strategy reordering (last runs with memory upgrade): 8 masters.
4 Relevant work

The specification that we considered was proposed in [5, 4, 1]. The time reported there for 12 masters is in the order of 20 hours, using the synthesizer Anzu [29]. Both Anzu (Perl) and Slugs (C++) use Cudd [28] as BDD library.

In [2], a more complete specification was presented for the AHB arbiter, by extending the specification of [1], but without revisions of the form proposed here. In particular, [2] refines the specification, adding more detail, whereas we abstract it, weakening and modifying assumptions. The times reported there are much improved compared to [1], but still scale to above an hour for 16 masters. In contrast, the revised specification with conjunction synthesizes in the order of minutes (with strategy reordering enabled).

In [8], a different algorithm is proposed for constructing the winning strategy from the intermediate sets produced by the fixed point iteration that decides realizability. The resulting strategy is eager to progress in reaching multiple goals, when the opportunity exists, cycling faster through liveness goals. The times reported there are in the order of 6 and 10 hours (for the various strategy construction algorithms) for 15 masters.
A Note on determinism of automata

Note that the (symbolic) automaton is deterministic, because it commits to the choices it makes, i.e., its existential branching is visible to the property (the variables that represent the state are letters in the alphabet). (For automated determinization of LTL properties to either parity or Büchi automata, prior to solving a parity game, see [30]).

For example, an automaton with four nodes can be represented by introducing an auxiliary integer variable \( u \in \{0, 1, 2, 3\} \). Suppose that it has the transitions \( (u = 0) \rightarrow ((\varphi_1 \land O(u = 1)) \lor (\neg \varphi_1 \land O(u = 0))) \land ((u = 1) \rightarrow ((\varphi_2 \land O(u = 2)) \lor (\varphi_3 \land O(u = 2))) \land ((u = 2) \rightarrow ((\varphi_4 \land O(u = 3)) \lor (\varphi_5 \land O(u = 2)) \lor (\neg \varphi_4 \land \neg \varphi_5 \land O(u = 2))) \land ((u = 3) \rightarrow (\varphi_6 \land O(u = 0))) \). It can be argued that this formula is much less readable and editable than the listing of Fig. 127.

Note that the above automaton can have more than a single enabled transition. Nonetheless, it represents a deterministic Büchi automaton, because the program counter \( u \) is visible to the environment. This forces the system to commit to its future strategy during GR(1) synthesis, when it selects a valuation of its variables as reaction. In other words, the non-determinism is visible, because \( u \) is part of the alphabet and so of the moves that the synthesis algorithm takes in the game. For the above symbolic automaton to be non-deterministic, the variable \( u \) must not be part of the alphabet, so not a visible output. This is not the case in GR(1) synthesis. Strictly speaking, the previous can be regarded as a symbolic representation of an automaton, but not as a Büchi automaton. If each edge label is conjoined with a formula of the form \( O(u = j) \), then the resulting representation will indeed be a deterministic Büchi automaton.
B Revised AMBA AHB specification

Listing 1: The revised AMBA AHB specification.

```c
#define N 2  /* N + 1 masters */
#define SINGLE 0
#define BURST4 1
#define INCR 2

/* variables of masters and slaves */
/* A4: initial condition */
free env bool ready = false;
free env int(0, 2) burst;
free env bool request[N + 1] = false;
free env bool grantee_lockreq = false;
free env bool master_lockreq = false;

/* arbiter variables */
/* G11: sys initial condition */
free bool start = true;
free bool decide = true;
free bool lock = false;
free bool lockmemo;
free int(0, N) master = 0;
free int(0, N) grant;

/* A2: slaves must progress with receiving data */
assume ltl { []<> ready }

/* A3: dropped, weakening the assumptions */
/* A1: if current master is granted locked access,
* then it must progress by withdrawing the lock request. */
assume env proctype withdraw_lock(){
    progress:
    do
        :: lock;
        do
            :: ! master_lockreq; break
            :: true /* wait */
        od
        :: else
        od
}
```
assert ltl {  
  []{  
    /* G1: new access starts only when slave is ready */  
    (start' -> ready)  
    /* G4,5: current master and lock updated */  
    * only when communicating slave signals  
    * that it completed receiving data.  
    */  
    && (ready -> ((master' == grant) && (lock' <-> lockmemo)))  
    /* G6: current master and locking may change only */  
    * when an access starts, and remain invariant otherwise  
    */  
    && (! start' -> (  
        (master' == master) &&  
        (lock' <-> lock)))  
    /* G7: when deciding, remember if the requestor requested also locking. */  
    * when implementing the circuit, route:  
    * grantee_lockreq = lockreq[grant']  
    */  
    && (decide -> (lockmemo' <-> grantee_lockreq))  
    /* G8: current grantee and locking memo */  
    * remain invariant while not deciding. */  
    */  
    && (! decide -> (  
        (grant' == grant) &&  
        (lockmemo' <-> lockmemo)))  
    /* G10: only a requestor can become grantee */  
    && ((grant' == grant) || (grant' == 0) || request[grant'])  
  }  
}  
/* all properties must hold synchronously */  
sync{  
  /* G9: weak fairness */  
  assert sys proctype fairness(){  
    int(0, N) count;  
    do  
      :: (! request[count] || (master == count));  
  }
}
if  
:: (count < N) && (count' == count + 1)  
:: (count == N) && (count' == 0);  
    progress: skip  
    :: else  
    od  
}  
/* G2: if locked access of unspecified length starts,  
* then locking shall be withdrawn before starting  
* another access.  
*/  
assert sys proctype maintain_lock(){  
    do  
        :: (lock && start && (burst == INCR));  
        do  
            :: (! start && ! master_lockreq); break  
            :: ! start  
            od  
        :: else  
        od  
    }  
/* G3: for a BURST4 access,  
* count the "ready" time steps.  
*/  
assert sys proctype count_burst(){  
    int(0, 3) count;  
    do  
        :: (start && lock &&  
            (burst == BURST4) &&  
            (!ready || (count' == 1)) &&  
            (ready || (count' == 0)) );  
        do  
            :: (! start && ! ready)  
            :: (! start && ready && (count < 3) &&  
                (count' == count + 1))  
            :: (! start && ready && (count >= 3)); break  
        od  
        :: else  
        od  
    }  
}
C  Original AMBA AHB specification

The following specification was created by a translator based on the original one from the Anzu website [29].

Listing 2: The original AMBA AHB specification from [1], for the case of 2 masters.

```plaintext
free env bit hready, hburst0, hburst1, hbusreq0, hlock0, hbusreq1, hlock1;
free sys bit hmaster0, hmastlock, start, locked, decide, hgrant0, busreq, stateA1_0, stateA1_1, stateG2, stateG3_0, stateG3_1, stateG3_2, hgrant1, stateG10_1;
assume ltl { free env bit hready, hburst0, hburst1, hbusreq0, hlock0, hbusreq1, hlock1;
free sys bit hmaster0, hmastlock, start, locked, decide, hgrant0, busreq, stateA1_0, stateA1_1, stateG2, stateG3_0, stateG3_1, stateG3_2, hgrant1, stateG10_1;
assume ltl {

hready == 0 && hbusreq0 == 0 && hlock0 == 0 && hbusreq1 == 0 && hlock1 == 0 && hburst0 == 0 && hburst1 == 0

[]( hlock0 == 1 > hbusreq0 == 1 ) &&
[]( hlock1 == 1 > hbusreq1 == 1 ) &&
[](<>(stateA1_1 == 0)) &&
[](<>(hready == 1))
}

assert ltl {

hmaster0 == 0 && hmastlock == 0 && start == 1 && decide == 1 && locked == 0 && hgrant0 == 0 && hgrant1 == 0 && busreq==0 && stateA1_0 == 0 && stateA1_1 == 0 && stateG2 == 0 && stateG3_0 == 0 && stateG3_1 == 0 && stateG3_2 == 0 && stateG10_1 == 0

[](hmaster0 == 0) -> (hbusreq0 == 0 <-> busreq==0)) &&
[](hmaster0 == 1) -> (hbusreq1 == 0 <-> busreq==0)) &&
```
[[]((stateA1_1 == 0) && (stateA1_0 == 0) && (hmastlock == 0) || (hburst0 == 1)) || (hburst1 == 1))) ->
X((stateA1_1 == 0) && (stateA1_0 == 0)) &&
[](((stateA1_1 == 0) && (stateA1_0 == 0) && (hmastlock == 1) && (hburst0 == 0) && (hburst1 == 0))) ->
X((stateA1_1 == 1) && (stateA1_0 == 0))) &&
[](((stateA1_1 == 1) && (stateA1_0 == 0) && (busreq == 0) && ((hmastlock == 0) || (hburst0 == 1) || (hburst1 == 1))) ->
X((stateA1_1 == 0) && (stateA1_0 == 0)) &&
[](((stateA1_1 == 0) && (stateA1_0 == 0) && (busreq == 0) && (hmastlock == 1) && (hburst0 == 0) && (hburst1 == 0))) ->
X((stateA1_1 == 1) && (stateA1_0 == 0))) &&
[](((stateA1_1 == 0) && (stateA1_0 == 0) && (busreq == 0) && (hmastlock == 1) && (hburst0 == 0) && (hburst1 == 0))) ->
X((stateA1_1 == 0) && (stateA1_0 == 0))) &&
[]((hready == 0) -> X(start == 0)) &&
[](((stateG2 == 0) && ((hmastlock == 0) || (start == 0) || (hburst0 == 1) || (hburst1 == 1))) -> X(stateG2 == 0)) &&
[](((stateG2 == 0) && (hmastlock == 1) && (start == 1) && (hburst0 == 0) && (hburst1 == 0))) -> X(stateG2 == 1)) &&
[](((stateG2 == 1) && (start == 0) && (busreq == 1)) -> X(stateG2 == 1)) &&
[](((stateG2 == 1) && (start == 1)) -> false) &&
[](((stateG2 == 1) && (start == 0) && (busreq == 0)) -> X(stateG2 == 0)) &&
[](((stateG3_0 == 0) && (stateG3_1 == 0) && (stateG3_2 == 0) && ((hmastlock == 0) || (start == 0) || ((hburst0 == 1) || (hburst1 == 0)))) ->
X(stateG3_0 == 0) && X(stateG3_1 == 0) && X(stateG3_2 == 0)) &&
[](((stateG3_0 == 0) && (stateG3_1 == 0) && (stateG3_2 == 0) && ((hmastlock == 1) && (start == 1) && ((hburst0 == 0) && (hburst1 == 1)) && (hready == 0))) ->
X(stateG3_0 == 1) && X(stateG3_1 == 0) && X(stateG3_2 == 0)) &&
[](((stateG3_0 == 0) && (stateG3_1 == 0) && (stateG3_2 == 0) && ((hmastlock == 1) && (start == 1) && ((hburst0 == 0) && (hburst1 == 1)) && (hready == 1))) ->
X(stateG3_0 == 0) && X(stateG3_1 == 1) && X(stateG3_2 == 0)))

152
[]((stateG3_0 == 1) && (stateG3_1 == 0) && (stateG3_2 == 0) && ((
  start == 0) && (hready == 0)))) ->
(X(stateG3_0 == 1) && X(stateG3_1 == 0) && X(stateG3_2 == 0))
&&
[]((stateG3_0 == 1) && (stateG3_1 == 0) && (stateG3_2 == 0) && ((
  start == 0) && (hready == 1)))) ->
(X(stateG3_0 == 0) && X(stateG3_1 == 1) && X(stateG3_2 == 0))
&&
[]((stateG3_0 == 1) && (stateG3_1 == 0) && (stateG3_2 == 0) && ((
  start == 1))) -> false) &&
[]((stateG3_0 == 0) && (stateG3_1 == 1) && (stateG3_2 == 0) && ((
  start == 0) && (hready == 0)))) ->
(X(stateG3_0 == 0) && X(stateG3_1 == 1) && X(stateG3_2 == 0))
&&
[]((stateG3_0 == 0) && (stateG3_1 == 1) && (stateG3_2 == 0) && ((
  start == 0) && (hready == 1)))) ->
(X(stateG3_0 == 0) && X(stateG3_1 == 0) && X(stateG3_2 == 1))
&&
[]((stateG3_0 == 1) && (stateG3_1 == 1) && (stateG3_2 == 0) && ((
  start == 1))) -> false) &&
[]((stateG3_0 == 0) && (stateG3_1 == 0) && (stateG3_2 == 1) && ((
  start == 0) && (hready == 0)))) ->
(X(stateG3_0 == 0) && X(stateG3_1 == 0) && X(stateG3_2 == 1))
&&
[]((stateG3_0 == 0) && (stateG3_1 == 0) && (stateG3_2 == 1) && ((
  start == 0) && (hready == 1)))) ->
(X(stateG3_0 == 0) && X(stateG3_1 == 0) && X(stateG3_2 == 0)))
&&
[[((stateG3_0 == 0) && (stateG3_1 == 0) && (stateG3_2 == 1) && ((start == 1))) → false] &&
[[((hready == 1) → ((hgrant0 == 1) <-> (X(hmaster0 == 0))))] &&
[[((hready == 1) → ((hgrant1 == 1) <-> (X(hmaster0 == 1))))] &&
[[X(start == 0) → (((hmaster0 == 0)) <-> (X(hmaster0 == 0))))] &&
[[X(start == 0) → (((hmaster0 == 1)) <-> (X(hmaster0 == 1))))] &&
[[((X(start == 0))) → ((hmastlock == 1) <-> X(hmastlock == 1))]
&&
[[((decide == 1 && hlock0 == 1 && X(hgrant0 == 1)) → X(locked == 1)]
&&
[[((decide == 1 && hlock0 == 0 && X(hgrant0 == 1)) → X(locked == 0)]
&&
[[((decide == 1 && hlock1 == 1 && X(hgrant1 == 1)) → X(locked == 1)]
&&
[[((decide == 1 && hlock1 == 0 && X(hgrant1 == 1)) → X(locked == 0)]
) &&
[[((decide == 0) → (((hgrant0 == 0)<-> X(hgrant0 == 0))))] &&
[[((decide == 0) → (((hgrant1 == 0)<-> X(hgrant1 == 0))))] &&
[[((decide == 0)→(locked == 0 <-> X(locked == 0)))] &&
[[((stateG10_1 == 0) && (((hgrant1 == 1) || (hbusreq1 == 1)))) → X(stateG10_1 == 0)]
&&
[[((stateG10_1 == 0) && ((hgrant1 == 0) && (hbusreq1 == 0))) → X(stateG10_1 == 1)]
&&
[[((stateG10_1 == 1) && ((hgrant1 == 1) && (hbusreq1 == 0)))→ X(stateG10_1 == 1)]
&&
[[((stateG10_1 == 1) && (hbusreq1 == 1)) → X(stateG10_1 == 1)]
&&
[[((decide==1 && hbusreq0 == 0 && hbusreq1 == 0) → X(hgrant0==1)]
) &&
[[<>(stateG2 == 0)] &&
[[<>(stateG3_0 == 0) && (stateG3_1 == 0) && (stateG3_2 == 0)]
))
&& []<>(((hmaster0 == 0)) || hbusreq0 == 0)) &&
[[<>(((hmaster0 == 1)) || hbusreq1 == 0))]
}
References


