HARD X-RAY MORPHOLOGICAL AND SPECTRAL STUDIES OF THE GALACTIC CENTER MOLECULAR CLOUD SGR B2: CONSTRAINING PAST SGR A* FLARING ACTIVITY

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Abstract

Galactic Center (GC) molecular cloud Sgr B2 is the best manifestation of an X-ray reflection nebula (XRN) reprocessing a past giant outburst from the supermassive black hole Sgr A*. Alternatively, Sgr B2 could be illuminated by low-energy cosmic ray electrons (LECRe) or protons (LECRp). In 2013, NuSTAR for the first time resolved Sgr B2 hard X-ray emission on sub-arcminute scales. Two prominent features are detected above 10 keV – a newly emerging cloud G0.66 and a decreasing Fe K\(\alpha\) emission consistent with the same Sgr A* outburst. In the LECRp scenario, we derived the required CR ion power \(dW/dt = (1 - 4) \times 10^{39}\) erg s\(^{-1}\) and the CR ionization rate \(\zeta_H = (6 - 10) \times 10^{-15}\) H\(^{-1}\) s\(^{-1}\). The Sgr B2 background level X-ray emission will be a powerful tool to constrain GC CR population.

Subject headings: Galaxy: center — X-rays: individual (Sgr B2) — X-rays: ISM — Molecular Clouds

1. INTRODUCTION

The Galactic center (GC) supermassive black hole Sagittarius A* (Sgr A*) is the closest such object and is thus an ideal target for investigation of galactic nuclei and their activity cycles (Morris et al. 1999, Ponti et al. 2013). Sgr A* is an underluminous black hole with a bolometric luminosity about 10\(^{-9}\) times the Eddington luminosity for a 4 \times 10\(^6\) M\(_\odot\) black hole (Ghez et al. 2008, Gillessen et al. 2009). Its current X-ray quiescent state, with a luminosity of \(L_X \sim 10^{33}\) erg s\(^{-1}\) (Baganoff et al. 2003), is punctuated by flares up to a few times \(10^{34}\) erg s\(^{-1}\) (e.g. Baganoff et al. 2001, Porquet et al. 2008, Nowak et al. 2012), during which the bolometric luminosity is still orders of magnitude lower than its Eddington luminosity. Hard X-rays up to ~ 79 keV have also been detected from the flares by NuSTAR (Barrière et al. 2014). Whether it has ever experienced more substantial increases in activity as observed in low-luminosity Active Galactic Nuclei (AGN) is still under discussion.

Indication of such past activity of Sgr A* has come from Galactic center molecular clouds (GCMCs). In the populous Central Molecular Zone (CMZ, Morris & Serabyn 1996), Sgr B2 is the densest and most massive molecular cloud. It has complicated substructures including compact star-forming cores like Sgr B2(M), Sgr B2(N) and Sgr B2(S) (Etxaluze et al. 2013 and references therein). In an extremely simplified picture, its density distribution can be described as a dense core with a radius of 0.15–0.3 pc (2\(\prime\)–4\(\prime\)), surrounded by an envelope extended to ~ 5 pc (2.2\(\prime\)) with a density of 10\(^{-5}\) cm\(^{-3}\) and a larger diffuse component reaching ~ 22.5 pc with a roughly constant density of ~ 10\(^3\) cm\(^{-3}\) (Lis & Goldsmith 1990, de Vicente et al. 1997).

Sgr B2 is the first GCMC from which a strong 6.4 keV Fe K\(\alpha\) line was discovered (Koyama et al. 1996). ASCA detected this significant line feature with an equivalent width of about 1 keV, which was later confirmed by
Chandra, Suzaku and XMM-Newton observations [Murakami et al. 2001; Koyama et al. 2007; Terrier et al. 2010]. Time variability of the Sgr B2 Fe Kα line was revealed by years of monitoring by different instruments. The 6.4 keV line flux began declining in 2001 and decreased by a factor of $\sim 0.4$ by 2005 [Inui et al. 2009], and further decreased by a factor of $0.39 \pm 0.04$ from 2005 to 2009 [Nobukawa et al. 2011]. The flux and morphology change of the X-ray emission is also observed from other GC molecular clouds. Interestingly, the clouds exhibit Fe Kα line variability in different ways, some rising, others are decreasing and an emission peak is detected in the “Bridge” structure with a time scale as short as two years [Muno et al. 2007; Ponti et al. 2010; Capelli et al. 2012; Clavel et al. 2013].

Reflection of incoming X-rays by cold molecular material is a natural explanation of the observed X-ray emission. In the X-ray reflection nebula (XRN) model, K-shell photo-ionization and the subsequent fluorescence produce a strong Fe Kα line with an equivalent width EW $\geq 1$ keV, while a competition between Compton scattering of high energy photons and photoelectric absorption of low energy photons gives rise to a Compton reflection hump around 20–30 keV [Sunyaev et al. 1993; Sunyaev & Churazov 1998; Koyama et al. 1998]. An embedded or nearby transient X-ray source was ruled out to be an illuminating source, since no transient source has been sufficiently bright ($L \geq 10^{37}$ erg s$^{-1}$) for several years since 1993 within or close to Sgr B2 (e.g. Revnivtsev et al. 2004; Terrier et al. 2010). Sgr A* was proposed to be the likely source illuminating Sgr B2. A major outburst from Sgr A*, with a luminosity of a few $10^{39}$ erg s$^{-1}$ lasting more than 10 years and ending a few hundred years ago would explain the Sgr B2 emission [Koyama et al. 1996; Terrier et al. 2010]. This hypothesis is reinforced by the discovery of a superluminal Fe K echo from the “Bridge”, which points to propagation of an event far away from the clouds [Ponti et al. 2010]. However, the story gets complicated by different Fe Kα line variability detected from GCMCs, which cannot be explained with a single outburst from Sgr A*. The strong and fast variation of the Fe Kα line flux in the “Bridge” region requires a two-year peaked outburst with luminosity of at least $10^{39}$ erg s$^{-1}$, while the slower Fe Kα line behavior detected in other clouds suggests a second flare with a longer duration [Clavel et al. 2013].

The propagation of cosmic-ray (CR) particles within the molecular clouds is an alternative explanation. Low-energy cosmic ray electrons (LECRe) and protons (LECRp) can both produce hard X-rays and Fe Kα emission [Valinia et al. 2000; Dogiel et al. 2009]. The Sgr B2 Fe Kα flux variation time scale of $\sim 10$ years is too short compared to the Coulomb cooling time of $\sim 100$ MeV protons invoked in the LECRp scenario, thus rules it out as a major contributor to the fast changing Fe Kα emission of Sgr B2 [Terrier et al. 2010]. However, LECRe could be a major contributor to the constant background level of the Sgr B2 Fe Kα emission, which could be detectable once the reflected X-ray emission completely fades [Dogiel et al. 2009; Dogiel et al. 2009].

2. OBSERVATION AND DATA REDUCTION

2.1. NuSTAR Data

The NuSTAR observatory operates in the broad X-ray energy band from 3 to 79 keV [Harrison et al. 2013]. Sgr B2 was observed by NuSTAR in October 2013 in two 25% overlapping pointings, with a total exposure time of 293.7 ks (See Table 1).

In both observations, the Sgr B2 region was imaged with the two co-aligned X-ray telescopes, with corresponding focal plane modules FPMA and FPMB, providing an angular resolution of $58''$ Half Power Diameter (HPD) and $18''$ Full Width Half Maximum (FWHM) over the 3–79 keV X-ray band, with a characteristic spectral resolution of 400 eV (FWHM) at 10 keV. The nominal reconstructed NuSTAR astrometry is accurate to $8''$ (90% confidence level [Harrison et al. 2013]. The
data were reduced and analyzed using the NuSTAR Data Analysis Software NuSTARDAS v. 1.3.1. and HEASOFT v. 6.13, then filtered for periods of high instrumental background due to South Atlantic Anomaly (SAA) passages and known bad/noisy detector pixels. The NuSTAR detectors are not completely shielded from incident X-rays that do not go through the optics, which is referred to as stray light. Bright X-ray sources within ~1–5 degrees of the NuSTAR field of view can significantly contaminate one or both of the detector planes. The contaminated detector pixels can be removed based on a numerical model that fully takes into account the telescope geometry [Krivonos et al. 2014]. Thus, to make a stray-light-free mosaic, we used this model to remove stray-light patterns from both FPMA and FPMB detectors by flagging the contaminated detector pixels as bad, when processing with the NuSTAR-DAS pipeline. As a result, stray-light from the the X-ray sources SLX 1744–299 and 1E 1740.7–2942 were removed from FPMA detectors, and that from GX 3+1 and SLX 1735–269 were removed from FPMB detectors. We then registered these stray-light-free images with the brightest point sources available in individual observations. As a result, the astrometry is improved to ~4″. Lastly we combined the exposure-corrected images in different energy bands (Figure 1).

On the other hand, removing the stray-light patterns is not necessary for spectral extraction. The stray-light background does not significantly change from one sky pointing to another, provided that they are separated by no more than 10′–20′ [Krivonos et al. 2014]. Therefore, for the Sgr B2 core region detected in one observation, we extracted the background from the same detector region in the other observation. This was our motivation for using two 25% overlapping sky pointings. This background subtraction method has been applied to many sources detected by NuSTAR suffering from stray-light (e.g. [Zhang et al. 2014] [Krivonos et al. 2014], and is proven to subtract mild stray-light contamination properly.

Due to the extremely bright stray-light contamination within 90″ of Sgr B2 on FPMB, we used FPMA data only for the Sgr B2 core spectrum. From the selected data sets, we extracted source spectra from a circular region of 90″ radius centered on Sgr B2 (R.A.=17h47m20.4s, Decl.=-28°29′07.0″, J2000). In this way, we had two source-background pairs with the Sgr B2 core detected on FPMA in observation 40012018002 and 40012019001. We combined the two FPMA source spectra and their associated response files and background spectra. The resultant spectrum was grouped such that the detection significance in each data bin is at least 3σ. The confidence level for all the error bars reported in this paper are 90%.

Another cloud feature, G0.66–0.13 (R.A.=17h47m41.5″, Decl.=-28°26′23.0″, J2000) [Ponti et al. 2014], is only captured in the second observation (obsID 40012019001) and avoids the stray light from GX 3+1 on FPMB. We thus used both FPMA and FPMB from the second observation for its spectral analysis. The spectra were combined and grouped with the same method as for the central 90″ region.

2.2. XMM-Newton Data

We collected and analyzed all the XMM-Newton data available in the archive covering the Sgr B2 and G0.66–0.13 regions. This includes observations performed in 2000, 2001, 2002, 2004 and 2012. The 2000 data were excluded due to low effective exposure and poor statistics, while for the other years we used all the available observations. The list of XMM-Newton observations is presented in Table 1, along with the total EPIC pn-equivalent exposure times (i.e., computed assuming a 0.4 ratio between the effective areas of the MOS and pn detectors). For each selected observation we extracted the spectra from all available EPIC instruments using the XMM-Newton Extended Source Analysis Software (ESAS; Snowden et al. 2008) distributed with version 12.0.1 of the XMM-Newton Science Analysis Software. For each exposure, calibrated event files were produced with the tasks emchain and emchain and filtered with pn-filter and mos-filter in order to exclude the time intervals affected by soft proton contamination. The spectra were then extracted with the ESAS mos-spectra and pn-spectra scripts and rebinned to have at least 30 counts in each bin to apply chi-square statistics. The quiescent component of the EPIC internal particle background (QPB) was estimated using archival observations provided within the ESAS database and taken with the filter wheel closed.

3. SPATIAL DISTRIBUTION OF THE HARD X-RAY EMISSION AND THE Fe Kα LINE EMISSION

Figure 1 shows the resultant 17′ × 11′ NuSTAR sky mosaics of the Sgr B2 region in the 3–40 keV, 3–10 keV, 6.2–6.6 keV and 10–40 keV bands. The 3–40 keV image shows that two features are significantly detected: the central 90″ of Sgr B2 and a newly discovered cloud feature G0.66–0.13, whose 6.4 keV Fe Kα emission turned bright in 2012 as revealed by the XMM-Newton data (Terrier et al. in prep.). The green circle of 90″ radius outlines the central region of Sgr B2, corresponding to 3.4±0.3 pc with the cloud distance of 7.9±0.8 kpc [Reid et al. 2009]. The green ellipse outlines the cloud feature G0.66–0.13, with a semi-major axis of 130″ (4.9±0.5 pc) and a semi-minor axis of 76″ (2.9±0.3 pc). G0.66–0.13 is ~14 pc away from the center of Sgr B2 in the projected plane. Sgr B2 and G0.66–0.13 are both about 100 pc away from Sgr A* in the projected plane. The lower energy 3–10 keV image is also shown to compare with previous observations of Sgr B2 by Chandra, XMM-Newton, and other imaging observatories. The 6.2–6.6 keV band

<table>
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<th>Observation ID</th>
<th>Start Time (UTC)</th>
<th>Exposure (ks)</th>
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<td>2012-09-30T19:39:50</td>
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The image with continuum emission subtracted shows the Fe Kα line emission morphology of the Sgr B2 region. The 10–40 keV band image provides the line-free continuum emission morphology. All the images are scaled individually to illustrate the morphology of major features. The images are overlaid with 6.4 keV line emission contours. The contours are made from the 2012 image of the XMM-Newton CMZ scan in the 6.28–6.53 keV band, from which the continuum emission (estimated assuming a power law model between two adjacent bands) has been subtracted (Ponti et al. 2014, 2015 in press).

The 10–40 keV image demonstrates that the high energy X-ray (≥ 10 keV) morphology of Sgr B2 is resolved at sub-arcminute scales for the first time. It clearly reveals substructures of Sgr B2 and proves that the X-ray emission in this energy band is extended (Figure 1). Both the central 90″ of Sgr B2 and G0.66−0.13 are significantly detected above 10 keV. G0.66−0.13 shows two bright cores separated by about 100″, well correlated with its 6.4 keV line contour. The size of each peak is ~ 20″. The 10–40 keV surface brightness of the whole G0.66−0.13 region is (3.5 ± 0.8) × 10^{-6} ph cm^{-2} s^{-1} arcmin^{-2}. Within the central 90″ region of Sgr B2, the 10–40 keV emission peaks at the center, coinciding with the compact star-forming core Sgr B2(M), with a surface brightness of (1.6 ± 0.1) × 10^{-5} ph cm^{-2} s^{-1} arcmin^{-2} for the central 25″ radius region. It is detected at the ~ 17σ level and likely to be the hard X-ray counterpart of Sgr B2(M). The right panel of Figure 2 shows the zoomed-in 7″ × 5″ image of the central region in 10–40 keV. Besides Sgr B2(M), X-ray emission around the additional compact core Sgr B2(N), about 50″ north of Sgr B2(M), is also detected (~ 5σ). The zoomed-in images in Figure 2 are overlaid with the source regions of Sgr B2(M) (RA= 17h47m20.30s, Dec= −28°23′04.01″, J2000) and Sgr B2(N) (RA= 17h47m20.30s, Dec= −28°23′04.01″, J2000) defined from submm band observations by Herschel (Etxaluze et al. 2013). X-ray emission from a third compact core Sgr B2(S), south of Sgr B2(M), is not detected in 10–40 keV. The surrounding regions show lower surface brightness, with the western half of the annulus from 25″ to 90″ brighter than the eastern half. The 10–40 keV morphology strongly resembles the optical depth map at 250 μm, which indicates the local column density, derived from submm continuum emission (Etxaluze et al. 2013). In the 250 μm optical depth map, Sgr B2(M) and Sgr B2(N) have highest optical depth at 250 μm (τ_{250μm} > 1), while the surrounding areas have gradually lower τ_{250μm} with the western region higher than the eastern. It suggests that the hard X-ray continuum emission traces the local column density of the cloud material.

In 6.2–6.6 keV, only the main compact core Sgr B2(M) is significantly detected. Sgr B2(N) is not detected at 6.4 keV, nor in the 3–10 keV range (left panel of Figure 2). This could be due to higher local absorption. G0.66−0.13 is also not detected by NuSTAR at 6.4 keV. This is a dramatic change from its 2012 Fe Kα line morphology represented by the cyan contours, where G0.66−0.13 was brighter than the Sgr B2 core region. This indicates that the G0.66−0.13 Fe Kα emission has a short life time (e-folding decay time) of about 1 year.

Finally, we note that the small white circle with 16″ radius illustrates a bright point source CXOUGC J174652.9−282607, which is registered in the Chandra point source catalogue (Muno et al. 2009). The source is detected up to ~ 40 keV by NuSTAR (R.A.= 17h47m52.96s, Decl.= −28°26′07.37″, J2000), and will be reported in another work (Hong et al. in prep.).

4. TIME-VARIABILITY OF CENTRAL Sgr B2 AND G0.66−0.13

With the XMM-Newton data in 2001, 2002, 2004 and 2012 and the most recent 2013 NuSTAR observation of Sgr B2, we obtained the observed 6.4 keV line flux for the central 90″ radius region of Sgr B2 using a simple model wabs(apec:wabs+pougauss:gauss) (see Section 5.1.1) as the observed line flux is model independent. All the model parameters are fixed to be the same for all the years, while the normalizations for the power-law and Gaussian components are left free. The fit is satisfactory with χ^2_n = 1.0 for d.o.f. = 517. The resultant absorbed flux change of the central 90″ of Sgr B2 over time is shown in Figure 3 with square data points. The 6.4 keV line flux shows a clear decreasing trend from 2001 to 2013, which can be fit with a linear decay model with a slope of s = −0.25 × 10^{-5} ph cm^{-2} s^{-1} yr^{-1}. The varying flux is preferred at a ~ 1σ level over a flat light curve. In 2013 the observed 6.4 keV line flux is down to (0.83 ± 0.21) × 10^{-5} ph cm^{-2} s^{-1}, which corresponds to about 20% of the 2001 observed flux. The 6.4 keV line flux decrease rate is compatible with previous works showing that the 6.4 keV line emission of a more extended Sgr B2 region in 2005 is about 60% of that of 2000 (Imi et al. 2009). The life time of the X-ray photons is t ~ 11 years, which agrees well with the ~ 11-year light crossing time for the central 90″, with a distance of 7.9 kpc (Reid et al. 2009). Although the 2001–2013 lightcurve shows a decreasing trend, we note that the 2013 Fe Kα emission is at the same level as that of 2012. With limited statistics, it is not conclusive whether the Sgr B2 Fe Kα emission was still decreasing in 2013 or it had reached a constant background emission level. Future observation of the Sgr B2 region will constrain its timing variability.

Seven-year monitoring of Sgr B2 by INTEGRAL/IBIS reveals that the hard X-ray continuum emission flux decreases with a similar trend to the 6.4 keV emission, both decaying up to 40% from 2003 to 2009 (Ferrier et al. 2010). This decay profile predicts that the hard X-ray emission in 2013 reaches ~ 30% that of 2001. The 10–40 keV flux of the central 90″ of Sgr B2 measured by NuSTAR in 2013 is F_{10–40 keV} = (1.9 ± 0.2) × 10^{-12} erg cm^{-2} s^{-1}. Therefore, the extrapolated 10–40 keV flux of the central Sgr B2 region in 2001 is F_{10–40 keV} ~ 6.3 × 10^{-12} erg cm^{-2} s^{-1} based on the hard X-ray decay profile. To verify the estimated flux in 2001, we extrapolated the 2001 XMM-Newton spectrum into higher energies and derived the 10–40 keV flux of the central 90″ in 2001 to be F_{10–40 keV} = (6 ± 2) × 10^{-12} erg cm^{-2} s^{-1}, which matches with the 2001 flux value extrapolated based on NuSTAR measurements. This will be used to derive the luminosity of the primary source in Section 6.1.

The newly discovered cloud feature G0.66−0.13, 6′ (14 pc) from the central Sgr B2 region in the projected
Figure 1. Upper left panel: 17'×11' NuSTAR 3–40 keV mosaic image of the Sgr B2 region overlaid with 6.4 keV line emission contours (cyan dashed) made from 2012 XMM-Newton observations of the same region. The green circle is the central 90'' of Sgr B2 and the green ellipse shows the new cloud feature G0.66−0.13. Both the Sgr B2 core and G0.66−0.13 are detected in 3–40 keV. Upper right panel: NuSTAR 3–10 keV mosaic image of the Sgr B2 region. The small white circle shows a bright point source CXOUGC J174652.9−282607. Lower left panel: NuSTAR 6.2–6.6 keV mosaic image of the Sgr B2 core region from which the continuum emission is subtracted. The inner 90'' of Sgr B2 correlates well with its 2012 emission. While G0.66−0.13 was brighter than the inner 90'' of Sgr B2 in 2012, it is not detected in the 6.2–6.6 keV energy band by NuSTAR in 2013. Lower right panel: NuSTAR 10–40 keV mosaic image. The central 90'' of Sgr B2 and G0.66−0.13 are both detected in 10–40 keV. All the images are in cts s$^{-1}$ and overlaid with the Galactic coordinates with a grid of 0.1°. Sgr A* is outside of the field of view to the bottom right. The dark regions with irregular shapes are those of no exposure, which are cut out due to contamination of stray-light from bright point sources outside the field-of-view.

Figure 2. Zoomed-in 6'× 4' NuSTAR mosaic image of the central Sgr B2 region in 6.2–6.6 keV with continuum emission subtracted (left panel) and 10–40 keV (right panel). Both images are in cts s$^{-1}$ and overlaid with 6.4 keV line emission contours (cyan dashed). The two main compact cores Sgr B2(N) and Sgr B2(M) are outlined with 15'' radius region and 20'' radius region, respectively. The region for the central 90'' of Sgr B2 is overlaid for comparison. Sgr B2(M) is detected in both energy bands, while Sgr B2(N) is only detected above 10 keV.
Figure 3. Time variability of the Fe Kα line for the central 90′′ of Sgr B2 and the additional cloud feature G0.66−0.13. The Sgr B2 absorbed 6.4 keV line flux was measured in 2001, 2002, 2004 and 2012 by XMM-Newton (red squares), and in 2013 by NuSTAR (orange square). The Fe Kα line flux shows a clear decay of up to 80% of the measured Sgr B2 flux from 2001 to 2013. A chi-square analysis method leaves mainly the molecular cloud emission and previously detected X-ray point sources, thus we first checked the flux contribution from known point sources in the source and background regions. The background regions we use do not contain any point sources above the Chandra detection threshold. In the source region, there are four point sources detected by Chandra within 90′′ of Sgr B2: CXOUGC J174723.0−282231, CXOUGC J174720.1−282305, CXOUGC J174718.2−282348 and CXOUGC J174713.7−282337. We checked each source using the stacked spectrum made from all archived Chandra data between 1999-09-21 and 2012-10-31 available for Sgr B2. Their summed observed flux corresponds to ∼7% of the total observed flux of the central 90′′ region below 10 keV. By extrapolating their spectra into a higher energy band, we estimate their flux contribution above 10 keV is only ∼4%. Therefore the flux contribution from point sources is not significant for our study. None of the four sources exhibits a 6.4 keV line feature, while the brightest one among the four point sources exhibits a significant 6.7 keV line feature in its spectrum. It can be best fit with a collisionally ionized plasma model apec with a temperature of ∼3 keV. We thus used this model to represent unresolved point X-ray sources and any possible residual GC diffuse X-ray background within the source region.

5.1. Ad hoc XRN Model

To examine the XRN scenario, we first applied a popular XRN model, with the wabs absorption model for a direct comparison with previous work. The model is composed of a power-law and two Gaussians representing the Fe Kα emission line at 6.40 keV and the Kβ line at 7.06 keV, modified by intrinsic absorption column density. All the model components are subject to the foreground absorption, resulting in the XSPEC model wabs*(apec+wabs*powerlaw+gauss+gauss). We fixed the line energies of the two Gaussians to be 6.40 keV (best-fit centroid energy of the Fe Kα line of ∼6.44 keV) and 7.06 keV, with the normalization ratio of Kβ/Kα set to 15% [Murakami et al. 2001].

The 3–79 keV spectrum is well-fit with this simple model ($χ^2=0.97$ for d.o.f. = 91). The best-fit model parameters are listed in Table 2. The temperature of the thermal component is $T = 2 \pm 1$ keV with an unabsorbed 2–10 keV flux of $F_{2-10} = (6 \pm 4) \times 10^{-13}$ erg cm$^{-2}$ s$^{-1}$, consistent with the spectra of the point sources within 90′′ of Sgr B2. The 6.4 keV Fe Kα line has an observed flux of $F_{6.4} = (8.3 \pm 2.1) \times 10^{-6}$ ph cm$^{-2}$ s$^{-1}$. We calculated its equivalent width (EW) based on the power-law as the only continuum component, resulting in EW = $1.2^{+0.3}_{-0.4}$ keV. The best-fit power-law photon index is $Γ = 1.9 \pm 0.5$, consistent with previous measurements of $Γ \approx 2$ [Terrier et al. 2010]. The observed 10–40 keV flux is $F_{10-40} = (1.9 \pm 0.2) \times 10^{-12}$ erg cm$^{-2}$ s$^{-1}$. The intrinsic absorption column density is found to be $N_H = (5.0 \pm 1.3) \times 10^{23}$ cm$^{-2}$, on the lower end of, but still consistent with, the previous result of $(6.8 \pm 0.5) \times 10^{23}$ cm$^{-2}$ derived using the combined 2003 XMM-Newton and 2003–2004 INTEGRAL/IBIS data [Terrier et al. 2010]. All components are subject to a foreground interstellar column density of $N_H(j) = (1.1 \pm 0.4) \times 10^{22}$ cm$^{-2}$. The foreground column density value is consistent with our analysis of accumu-
lated 2001-2012 XMM-Newton data of the inner 90° of Sgr B2, which gives \( N_H(i) = (1.0 \pm 0.2) \times 10^{23} \text{ cm}^{-2} \).

Although this ad hoc model can fit well to the data, it is not self-consistent, with the continuum emission and fluorescence lines decoupled. A power-law can only measure the spectral slope of the observed scattered continuum, but not the illuminating source spectrum. The model is valid for measuring the illuminating source spectrum only when a molecular cloud is optically thin \((N_H < 10^{24} \text{ cm}^{-2})\) and the Compton scattering is negligible. Interpretation of the resultant best-fit value for the intrinsic column density \( N_H(i) \) calls for caution. As this ad hoc model does not take cloud geometry into account, the \( N_H(i) \) measured by this model represents a characteristic column density of the cloud, while in reality illuminating X-ray photons are absorbed and scattered in various locations of the cloud.

5.1.2. Self-consistent XRN Model MYTorus

In the XRN scenario, to consistently measure the illuminating X-ray spectrum and to properly determine the intrinsic column density, a self-consistent XRN model based on Monte-Carlo simulations is required. Murakami et al. (2001), Revnivtsev et al. (2004), Terrer et al. (2010) and Odaka et al. (2011) have applied Monte-Carlo based XRN models to Sgr B2 data in order to study its morphology and spectrum. The MYTorus model is the only XRN model available in XSPEC to self-consistently measure the illuminating source spectrum and the intrinsic column density (Murphy & Yaqoob 2009). MYTorus was originally developed for Compton-thick Active Galactic Nuclei (AGN) assuming a toroidal reflector with neutral materials and uniform density. The default Fe abundance in the MYTorus model is one solar and does not allow variation. There are three components offered in the model: the transmitted continuum (MYTZ), the scattered continuum (MYTS) and the iron fluorescence lines (MYTL). In the case of GCMCs, the observed spectrum only contains the last two components, because we are seeing only the reflected X-ray photons off the cloud. We thus use the combination of MYTS and MYTL. Both components depend on the intrinsic equatorial hydrogen column density \( N_H(i) \), the illuminating source spectrum photon index \( \Gamma \), the inclination angle \( \theta_{\text{obs}} \) between the line-of-sight and the torus symmetry axis, and the model normalization \( N_{MT} \). To self-consistently measure the illuminating source spectrum, all the parameters are linked between MYTS and MYTL as a coupled mode where the same incident X-ray spectrum is input into both components. We select a termination energy of the incident power-law as 500 keV. As the best-fit energy centroid for the Fe Kα line is \( \sim 6.44 \text{ keV} \), we select an energy offset of \( +10 \text{ eV} \) for the MYTL component to allow freedom for the centroid energy. The resultant model is \texttt{wabs*(apec+MYTS+MYTL)}, where the two \texttt{MYTorus} components are implemented as table models in Xspec: \texttt{atable{mytormus_scatteredH500_v00.fits}+atable{mytlv000010pEe04H500_v00.fits}}.

The coupled mode of the \texttt{MYTorus} model can be applied to the GCMC X-ray reflection spectra with some restrictions, by treating a quasi-spherical cloud as part of a virtual torus and rescaling incident X-ray flux properly (see Figure A6 for geometry). Due to the toroidal geometry and the uniform density profile \texttt{MYTorus} assumes, for GCMCs we restrict the applicability of the model to the inclination angle range of \( \theta_{\text{obs}} \lesssim 60° \) and the equatorial column density range of \( N_H \lesssim 10^{24} \text{ cm}^{-2} \), in order to be insensitive to the torus geometry (see Appendix for more details). When \( N_H(i) \) reaches \( \sim 10^{24} \text{ cm}^{-2} \), we derive the systematic error based on the \texttt{MYTorus} model to be 25% for \( N_H \), 3% for \( \Gamma \) and 10% for the model normalization (Mori et al. submitted). We note that the \( N_H(i) \) measured by the \texttt{MYTorus} model is an averaged value over the torus.

This self-consistent model can fit to the Sgr B2 spectrum well, yielding \( \chi^2 = 1.09 \) for \( \text{d.o.f.} = 92 \) (left panel of Figure 4). Both the best-fit temperature and the flux of the \texttt{apec} component are consistent with the fitting results of the ad-hoc power-law model (Table 2). The foreground column density is \( N_H(f) = (1.2 \pm 0.1) \times 10^{23} \text{ cm}^{-2} \), consistent with that derived from the ad hoc model and better constrained. However, the intrinsic equatorial column density is \( N_H(i) = (1.01 \pm 0.16_{\text{stat}} \pm 0.25_{\text{sys}}) \times 10^{24} \text{ cm}^{-2} \), which is twice the \( N_H(i) \) value measured with the ad hoc model. The \( N_H(i) \) value derived with the two models cannot be directly compared due to the lack of geometry definition for \( N_H(i) \) in the ad hoc model. \( N_H(i) \) in the \texttt{MYTorus} model corresponds to the minor diameter of the torus (or diameter of the quasi-spherical cloud), while \( N_H(i) \) in the ad hoc model roughly corresponds to the cloud radius as it “measures” an averaged effect, which might explain the difference by a factor of 2 (see the Appendix). For the central 90° of Sgr B2, the cloud radial optical depth due to Thomson scattering derived by the \texttt{MYTorus} model is \( \tau_T = 0.67 \pm 0.27 \), consistent with previous measurements of \( \tau_T = 0.4 \pm 0.1 \) derived from a self-developed Monte-Carlo simulation with combined ASCA/GIS, GRANAT/ART-P and INTEGRAL/IBIS data when Sgr B2 was much brighter (Revnivtsev et al. 2004). As a result, the central 90° of Sgr B2 is marginally optically thin. The illuminating source spectrum photon index is constrained to be \( \Gamma = 2.2 \pm 0.4 \) with the systematic error negligible, compatible with the observed spectrum slope of \( \Gamma = 1.9 \pm 0.5 \) measured by the power-law model which does not consider Compton scattering. With the hard upper limit on the inclination angle \( \theta_{\text{obs}} = 60° \) chosen for this study, the \texttt{MYTorus} model is not sensitive to the parameter \( \theta_{\text{obs}} \). Therefore, this parameter could not be constrained by our work.

Though with limitations, \texttt{MYTorus} is currently the best self-consistent XRN model available. The systematic errors could be underestimated since they are estimated solely based on the \texttt{MYTorus} model (see the Appendix). A modified XRN model based on \texttt{MYTorus} with a spherical reflector and variable Fe abundance is under development for the specific case of GCMCs, which will remove the uncertainties induced by the toroidal reflector and the fixed Fe abundance (T. Yaqoob, private communication). The more sophisticated XRN model will also implement the specific density profile of Sgr B2 to remove uncertainties induced by non-uniform density and better constrain \( N_H(i) \) (Walls et al. in prep.).

5.1.3. Self-consistent Cosmic Ray Electron Model LECRe
To determine whether CR electrons can be a major contributor to the remaining Sgr B2 X-ray emission in 2013, we tested the LECRe model (Tatischeff et al. 2012). The LECRe model has four free parameters: the power-law index of the accelerated particle source spectrum, $s$, the path length of cosmic rays in the non-thermal X-ray production region, $\Lambda$, the minimum electron energy, $E_{\text{min}}$, and the model normalization, $N_{\text{LECR}}$, which provides the power injection in the interaction region by primary cosmic-ray electrons of kinetic energies between $E_{\text{min}}$ and $E_{\text{max}} = 1$ GeV: $dW/dt = 4\pi D^2 N_{\text{LECR}}$ erg s$^{-1}$, where $D$ is the source distance. Since the fit cannot constrain the path length of LECRe, we fix it to $\Lambda = 5 \times 10^{22}$ H – atoms cm$^{-2}$ as was used in Tatischeff et al. (2012). As shown in the middle panel of Figure 4, it results in an acceptable fit to the data with $\chi^2 = 1.18$ for d.o.f. = 92 (Table 2). The electron spectral index is found to be $s = 2.8 \pm 0.5$ with a normalization of $N_{\text{LECR}} = (2.8 \pm 0.2) \times 10^{-7}$ erg cm$^{-2}$ s$^{-1}$. Previous analysis with XMN-Newton and INTEGRAL/JBIS data found that $s \sim 1.5$, but with an unconstrained error bar (Terrier et al. 2010). The best-fit minimum electron energy is as low as 3 keV, with an upper bound of 50 keV. Electrons with such low energy cannot leave their acceleration site, nor penetrate the cloud. The best-fit molecular cloud metallicity is $Z/Z_\odot = 4.0^{+2.9}_{-0.6}$ higher than $Z/Z_\odot = 3.1 \pm 0.2$ derived by Terrier et al. (2010). Such a metallicity value is too high compared to current measurements of the GC interstellar medium metallicity which ranges from slightly higher than solar to twice solar. Furthermore, compared to the XRN models, the LECRe model results in a poorer fit above 10 keV as it cannot fit to the spectrum curvature equally well. The LECRe model results in a poorer fit above 10 keV as it cannot fit to the spectrum curvature equally well. The LECRe model results in a poorer fit above 10 keV as it cannot fit to the spectrum curvature equally well.

5.1.4. Self-consistent Cosmic Ray Proton Model LECRp

While CR electrons can be safely excluded as a major contributor to the 2013 Sgr B2 X-ray emission, low energy CR proton/ion bombardment could be a major process if the Sgr B2 X-ray emission obtained in 2013 has already reached the constant background level. The LECRp model has the same model parameters as the LECRe model, with four free parameters $s$, $\Lambda$, $E_{\text{min}}$, and $N_{\text{LECR}}$. As the path length cannot be constrained by the fit, we fix it to $\Lambda = 5 \times 10^{22}$ H – atoms cm$^{-2}$, a typical value for nonrelativistic particles propagating in massive molecular clouds of the GC environment (Tatischeff et al. 2012). The right panel in Figure 4 shows that it results in an overall good fit with $\chi^2 = 1.17$ for d.o.f. = 92 (Table 2). The best-fit Fe abundance is $Z/Z_\odot = 2.5^{+1.5}_{-1.0}$, which is consistent with the GC metallicity. The CR proton spectral index is $s = 1.9^{+0.8}_{-0.7}$. This agrees with the CR proton spectral index derived with the LECRp model for the arches region using the XMM-Newton spectrum ($s = 1.9^{+0.5}_{-0.6}$ Tatischeff et al. 2012) or the NuSTAR spectrum ($s = 1.7 \pm 0.6$, Krivonos et al. 2014). CR iron bombardment was proposed by these authors to explain the X-ray emission from the Arches before a significant variability of the X-ray emission was detected (Clavel et al. 2014). As discussed in Tatischeff et al. (2012), with such a relatively hard CR spectrum, the X-ray emission produced by CR protons depends weakly on the minimum ion energy $E_{\text{min}}$. Therefore, we fix it to $E_{\text{min}} = 10$ MeV nucleon$^{-1}$. The total power required by CR protons in the cloud can be derived from the best-fit model normalization $N_{\text{LECR}} = (1.4 \pm 0.4) \times 10^{-7}$ erg cm$^{-2}$ s$^{-1}$. The power injected by primary protons of energies between $E_{\text{min}} = 10$ MeV and $E_{\text{min}} = 1$ GeV is $dW/dt = (1.0 \pm 0.3) \times 10^{39}$ erg s$^{-1}$ for $D = 7.9$ keV. However, the power injected into the cloud by the CR protons depends on the minimum energy $E_{\text{min}}$. For $E_{\text{min}} = 1$ MeV and $E_{\text{min}} = 100$ MeV, the best-fit model normalizations are $N_{\text{LECR}} = 2.0^{+1.1}_{-0.5} \times 10^{-7}$ erg cm$^{-2}$ s$^{-1}$ and $N_{\text{LECR}} = 0.7^{+0.3}_{-0.1} \times 10^{-7}$ erg cm$^{-2}$ s$^{-1}$, respectively. The corresponding power injected by CR protons is in the range of $dW/dt = (0.4 - 2.3) \times 10^{39}$ erg s$^{-1}$. Therefore, the LECRp scenario could explain the current level Sgr B2 X-ray emission and can only be excluded by further variability.

5.2. Main Compact Cores Sgr B2(M) and Sgr B2(N)

Herschel observations have shown that the local 250μm optical depth at Sgr B2(M) and Sgr B2(N) ($\tau_{250\mu m} \sim 1$) is higher than that of the surrounding region within 90″ roughly by a factor of 2–5 (Etxaluze et al. 2013). Specifically, the Sgr B2(M) 250μm optical depth is $\tau_{250\mu m} \sim 0.9$. Etxaluze et al. (2013) converted it to a local column density of $N_H \sim 1 \times 10^{24}$ cm$^{-2}$ based on the correspondence $\tau_{250\mu m}/N_H = 8.8 \times 10^{-26}$ cm$^2$ for optically thin clouds. This conversion factor is increased to $5 \times 10^{-25}$ cm$^2$ for the Sagittarius region (Bernard et al. 2010), thus reducing the Sgr B2(M) column density to $N_H \sim 1.8 \times 10^{24}$ cm$^{-2}$. We extracted a spectrum from a 20″ radius region (Figure 2) centered on Sgr B2(M) to measure the local optical depth independently using the X-ray data. The Sgr B2(M) spectrum is fit with the MYTorus model using the same model settings for the central 90″ region. The model yields a good fit with $\chi^2 = 1.00$ for d.o.f. = 39. While all the other key parameters are consistent with those derived from the central 90″ region, the intrinsic equatorial column density is $N_H(i) = (2.0^{+3.2}_{-1.0,stat} \times 10^{24}) \times 10^{24}$ cm$^{-2}$, twice that of the whole 90″ region but compatible within error bars. The LECRp model can also fit well to the Sgr B2(M) spectrum ($\chi^2 = 1.02$ for d.o.f. = 39), giving consistent $N_H(i)$ value. It agrees well with the Herschel measurements of local column densities. The corresponding radial optical depth in the direction of Sgr B2(M) is $\tau r = 1.3^{+2.3}_{-1.5}$. The NuSTAR observations confirm the Herschel measurements that the Sgr B2(M) region is not optically thin, though with large error bars. The 10–40 keV flux of Sgr B2(M) and Sgr B2(N) falling into the central 90″ region is $F_{10-40 \text{ keV}} = (6.1 \pm 0.2) \times 10^{-13}$ erg cm$^{-2}$ s$^{-1}$, contributing to about one third of the total flux of the central 90″. The surrounding regions within the 90″ radius region contribute to the remaining two thirds of the total flux. The second core, Sgr B2(N), does not have
sufficient statistics to perform a similar analysis.

5.3. The new feature G0.66−0.13

Since neither focal plane modules are severely contaminated by stray light, we were able to use the combined FPMA and FPMB NuSTAR data for G0.66−0.13. Furthermore, the G0.66−0.13 region does not contain sources registered in the Chandra point source catalogue (Muno et al. 2009). The background-subtracted NuSTAR spectrum for G0.66−0.13 does not show any significant line features. To compare with the significant Fe Kα lines detected by XMM-Newton in 2012, we fit the NuSTAR 2013 spectrum together with the XMM-Newton 2012 spectrum. Since the sharply decreasing Fe Kα emission cannot be explained by the LECRp scenario, we examine the G0.66−0.13 spectrum only with the MyTorus model. Because of different background subtraction methods, the thermal component in the XMM-Newton data represents the GC diffuse emission while the thermal component in the NuSTAR data represents undetected point source and residual diffuse emission. Therefore we use the model $\text{apec}+\text{MyTorus}+\text{MYTL}$ for the joint fitting, with all the model parameters linked except for $kT$ and the model normalizations of apec, MyTorus and MYTL. The model gives a good fit ($\chi^2/\text{d.o.f.} = 55$), with a best-fit photon index of $\Gamma = 1.4 \pm 0.5$, a foreground column density of $N_H(f) = (8.2^{+3.3}_{-4.5}) \times 10^{22} \text{ cm}^{-2}$ and an intrinsic equatorial column density of $N_H(i) = 3.0^{+3.9}_{-1.9} \times 10^{23} \text{ cm}^{-2}$ (Figure 5). The intrinsic density $N_H(i)$ is lower than that of the central 90′′ radius region, indicating that G0.66−0.13 is optically thin. However, in case that G0.66−0.13 is partially illuminated, the measured $N_H(i)$, which is the illuminated column density, would be smaller than the cloud intrinsic column density. The 10−40 keV flux for the NuSTAR 2013 data is $F_{10-40 \text{ keV}} = (9.0 \pm 1.2) \times 10^{-13} \text{ erg cm}^{-2} \text{ s}^{-1}$ in 10−40 keV. The observed 6.4 keV flux in 2012 measured by XMM-Newton is $F_{6.4 \text{ keV}} = (1.5 \pm 0.2) \times 10^{-5} \text{ ph cm}^{-2} \text{ s}^{-1}$, while the 2013 NuSTAR spectrum does not require a 6.4 keV line, with 6.4 keV flux upper limit of $5 \times 10^{-6} \text{ ph cm}^{-2} \text{ s}^{-1}$ (90% confidence level). The 8−12 keV non-thermal continuum emission measured by NuSTAR in 2013 dropped to ≈ 50% of that measured by XMM-Newton in 2012. Both the fluorescence emission and the hard X-ray emission show fast variability (or short life time), which could be due to a partial illumination of G0.66−0.13.

6. DISCUSSION

6.1. X-ray Reflection of Past Sgr A* Outbursts

The broadband spectrum obtained by NuSTAR supports the XRN scenario where Sgr B2 reflects incoming X-rays from an illuminating source, which is most likely a past X-ray outburst from Sgr A*. The illuminating source photon index measured with the broadband NuSTAR spectrum in 2013 using the MyTorus model is constrained to $\Gamma = 2.2 \pm 0.4$, compatible with the illuminating source photon index of $\Gamma = 2.0 \pm 0.2$ derived with combined XMM-Newton and INTEGRAL/IBIS spectra obtained in 2003-2004 when Sgr B2 was much more brighter (Terrier et al. 2010). Such a past Sgr A* outburst spectrum is consistent with the current bright Sgr A* X-ray flares spectra with $\Gamma \approx 2−3$ (e.g. Baganoff et al. 2001, Nowak et al. 2012, Barriere et al. 2014), although the mechanisms of both the past giant X-ray outbursts and the current relatively mild X-ray flares remain unclear. The outburst spectrum is also compatible with, though at the extreme end of, the average AGN photon index of $1 \leq \Gamma \leq 2$ with cut-off energies between 30 keV to 300 keV (Molina et al. 2013), which is also expected for the Sgr A* spectrum if it became active.

The Sgr B2 cloud as a whole has been discussed as an optically thin cloud (e.g. Koyama et al. 1996, Sunyaev & Churazov 1998, Revnivtsev et al. 2004, Terrier et al. 2010). In 2013, NuSTAR found the hard X-ray emission is concentrated in the central 90′′ radius region of Sgr B2, but it is unknown whether the hard X-ray emission in 2003-2009 was similarly concentrated within 90′′ or more extended due to the mild angular resolution of INTEGRAL/IBIS. While in the direction of the compact core Sgr B2(M) the optical depth is as high as $\tau_T \gtrsim 1$, the majority of the central 90′′ radius region is optically thin with $\tau_T < 1$. Besides, the 10−40 keV image shows that the X-ray continuum emission traces the local column density, also suggesting the majority of the central 90′′ of Sgr B2 is optically thin. Therefore, although there are complicated substructures with higher local column densities, the central 90′′ can be considered as optically thin for a simplified calculation of Sgr A* outburst luminosity.

For an optically thin cloud, the luminosity of the primary source can be derived via two independent analytical methods: the Fe Kα fluorescence process using the 6.4 keV line flux we measured, and the Compton scattering process with the measured hard X-ray continuum. In most previous works, the primary source luminosity has been calculated via the fluorescence process, due to good measurements of the 6.4 keV line but poorly constrained continuum emission. The 6.4 keV line emission flux for continuum radiation is expressed by Sunyaev & Churazov (1998) as

$$ F_{6.4} = \phi \frac{\Omega}{4\pi D^2} Z_{Fe} \tau_T I(8) \text{ ph cm}^{-2} \text{ s}^{-1} $$

(1)

where $\Omega$ is the cloud solid angle subtended to the illuminating source, $D$ is the distance to the observer, $Z_{Fe}$ is the iron abundance relative to solar, $\tau_T$ is optical depth due to Thomson scattering, and $I(8)$ is the illuminating source flux at 8 keV. $\phi$ is a factor of the order of unity, which depends on the source spectrum. Sunyaev & Churazov (1998) assumed the source spectrum to be bremsstrahlung with a temperature from 5 to 150 keV, corresponding to $\phi \sim 1.0 - 1.3$. Now, with a better knowledge of the primary source spectrum, we know it can be well described with a power-law with $\Gamma \approx 2$. $\Gamma$ ranges from 1.8 to 2.6, as measured with the MyTorus model, corresponding to $\phi \sim 1.1 - 1.3$. In the calculation hereafter we will adopt $\Gamma \approx 2$ and its corresponding $\phi \approx 1.18$.

Using the Sunyaev & Churazov (1998) approach, we express $I(8)$ with illuminating source luminosity at 8 keV in the 8 keV wide energy band as $L_8 = I(8) \times 8 \times 1.6 \times 10^{-5} \text{ erg s}^{-1}$. For the central region of Sgr B2 we adopted $r = 90''$ assuming it was entirely illuminated, so the luminosity of the source required to produce the observed 6.4 keV line is:
sponding to a 3–79 keV luminosity of \( L \) is \( L \). This is comparable to the \( L \) and averaged optical depth \( \tau \) and \( T \) et al. 2010). With the maximum central 90\'s Sgr B2 flux \( F_{6.4} = (4.3 \pm 0.6) \times 10^{-5} \) ph cm\(^{-2}\) s\(^{-1}\) obtained in 2001 and averaged optical depth \( \tau_{P} = 0.67 \pm 0.27 \) measured with \( \text{NuSTAR} \), the resultant primary source luminosity is \( L_{S} = (1.5 \pm 0.7) \times 10^{39} \) erg s\(^{-1}\), corresponding to a 3–79 keV luminosity of \( L_{3–79} \text{ keV} = (5.0 \pm 2.3) \times 10^{38} \) erg s\(^{-1}\) or 1–100 keV luminosity of \( L_{1–100} \text{ keV} = (0.7 \pm 0.3) \times 10^{39} \) erg s\(^{-1}\). This is comparable to the \( L_{1–100} \text{ keV} \sim 1.1 \times 10^{39} \) erg s\(^{-1}\) derived from \( \text{XMM-Newton} \) and \( \text{INTEGRAL/IBIS} \) data obtained in 2003-2004 (Terrier et al. 2010). The uncertainty of the primary source luminosity mainly comes from the measurement uncertainty of \( \tau_{P} \) and the distance between Sgr B2 and the primary source, \( d \). The solid angle \( \Omega \) could also be lower in the case of partial illumination, which would result in an underestimation of the primary source luminosity.

Since this was the first time the Sgr B2 10–40 keV continuum emission has been resolved, we can also derive the primary source continuum luminosity from the Compton scattered continuum. As discussed in Capelli et al. (2012), the observed scattered continuum at an angle \( \theta \) with respect to the incident radiation direction is:

\[
S_{I}(E) = \frac{\Omega}{D^{2}} \frac{3 \tau_{P} (1 + \cos^{2} \theta)}{8 \pi} I(E) \text{ ph cm}^{-2} \text{ s}^{-1} \text{ keV}^{-1}
\]

where \( I(E) \) is the photon flux from the source in units of \( \text{ph s}^{-1} \text{ keV}^{-1} \). This relationship is based on Thomson scattering, which is a good approximation for incident photons with energies of a few keV. However, when the photon energy is higher, electron quantum mechanical effects become important. As a result, we need to consider the Compton scattering process. Starting with the Compton scattering cross section formula, we derived a correction factor from Thomson scattering to Compton scattering as \( f_{TC} = (1 + \frac{E}{\hbar c} (1 - \cos \theta))^{-4} \) assuming a power-law spectrum with \( \Gamma \approx 2 \). The correction holds as long as \( \hbar \omega \ll mc^{2} \) for the electrons, which is true for

\[
\Omega = \left( \frac{1}{2} \pi \sin \theta \cos \theta \right)
\]

\[
\frac{3 \tau_{P} (1 + \cos^{2} \theta)}{8 \pi}
\]

\[
D^{2}
\]

\[
I(E)
\]

\[
\text{ph cm}^{-2} \text{ s}^{-1} \text{ keV}^{-1}
\]
The relationship between integrating both sides of equation (4) gives us the relation angle 10–40 keV Compton scattered continuum measured at higher order terms. As a result, the source luminosity can be expressed as:

\[ F_{\text{S}} \text{~tered continuum} \text{ can be expressed as:} \]

The observed 10–40 keV scattered continuum flux is \( F_{10-40} = \int_{10}^{40} S(E) \text{~ph cm}^{-2} \text{~s}^{-1} \text{~keV}^{-1} \). Thus, integrating both sides of equation (4) gives us the relation between \( F_{10-40} \) and \( L_8 \). We keep the first order correction term of the integrated form and neglect higher order terms. As a result, the source luminosity in the 8 keV wide band can be expressed with observed 10–40 keV Compton scattered continuum measured at angle \( \theta \) as:

\[ L_8 = 4 \times 10^{39} \left( \frac{F_{10-40}}{10^{-11} \text{erg cm}^{-2} \text{~s}^{-1}} \right) \left( \frac{0.1}{\tau_T} \right) \left( \frac{1}{1 + \cos^2 \theta} \right) \times (0.72 + 0.12(1 - \cos \theta)) \text{~erg s}^{-1} \]  

We use the maximum value of the hard X-ray continuum flux in 2012 from the lightcurve obtained by XMM-Newton. In Section 5 we estimated the 10–40 keV flux of the central 90° in 2001. The resultant source luminosity is \( L_8 = (3.6 \pm 1.8) \times 10^{38} \text{~erg s}^{-1} \), where \( f(\theta) = \frac{1}{1 + \cos^2 \theta} \). Thus, \( L_8 \) is approximately equal to 0.36–0.84 corresponding to \( \theta \sim 0° - 180° \). As the scattering angle range cannot be derived from the XRN model fitting in our study, we adopt \( \cos \theta \sim 0.8 \) based on VLBI observation results [Reid et al. 2009] to derive a nominal value for \( f(\theta) \). The error of \( f(\theta) \) is calculated corresponding the full allowed range of the scattering an-

\[ \chi^2 \text{~d.o.f.} \]

\[ N_\text{H}(f) \]

\[ N_\text{H}(i) \]

\[ Z/Z_\odot \]

\[ kT \]

\[ F_{\text{apec}}(2-10 \text{~keV}) \]

\[ F_\text{obs}(10-40 \text{~keV}) \]

\[ \text{EW}_{6.4 \text{~keV}} \]

\[ \Gamma_{\text{p.l.}} \]

\[ \Gamma_{\text{MT}} \]

\[ N_{\text{MT}} \]

\[ \Lambda \]

\[ s \]

\[ E_{\text{min}} \]

\[ N_{\text{LECR}} \]

\[ \chi^2 \text{~d.o.f.} \]

\[ N_\text{H}(f) \]

\[ N_\text{H}(i) \]

\[ Z/Z_\odot \]

\[ kT \]

\[ F_{\text{apec}}(2-10 \text{~keV}) \]

\[ F_\text{obs}(10-40 \text{~keV}) \]

\[ \text{EW}_{6.4 \text{~keV}} \]

\[ \Gamma_{\text{p.l.}} \]

\[ \Gamma_{\text{MT}} \]

\[ N_{\text{MT}} \]

\[ \Lambda \]

\[ s \]

\[ E_{\text{min}} \]

\[ N_{\text{LECR}} \]

\[ \chi^2 \text{~d.o.f.} \]

\[ N_\text{H}(f) \]

\[ N_\text{H}(i) \]

\[ Z/Z_\odot \]

\[ kT \]

\[ F_{\text{apec}}(2-10 \text{~keV}) \]

\[ F_\text{obs}(10-40 \text{~keV}) \]

\[ \text{EW}_{6.4 \text{~keV}} \]

\[ \Gamma_{\text{p.l.}} \]

\[ \Gamma_{\text{MT}} \]

\[ N_{\text{MT}} \]

\[ \Lambda \]

\[ s \]

\[ E_{\text{min}} \]

\[ N_{\text{LECR}} \]

\[ \chi^2 \text{~d.o.f.} \]

\[ N_\text{H}(f) \]

\[ N_\text{H}(i) \]

\[ Z/Z_\odot \]

\[ kT \]

\[ F_{\text{apec}}(2-10 \text{~keV}) \]

\[ F_\text{obs}(10-40 \text{~keV}) \]

\[ \text{EW}_{6.4 \text{~keV}} \]

\[ \Gamma_{\text{p.l.}} \]

\[ \Gamma_{\text{MT}} \]

\[ N_{\text{MT}} \]

\[ \Lambda \]

\[ s \]

\[ E_{\text{min}} \]

\[ N_{\text{LECR}} \]

\[ \chi^2 \text{~d.o.f.} \]
gle $\theta = 0^\circ - 180^\circ$, resulting in $f(\theta) = 0.46^{+0.38}_{-0.10}$. Thus, $L_8 = (1.7^{+1.6}_{-0.9}) \times 10^{38} \left(\frac{d}{100 \text{ pc}}\right)^2 \text{erg s}^{-1}$, corresponding to a 3–79 keV luminosity of $L_{3-79} = (5.6^{+5.2}_{-2.9}) \times 10^{38} \left(\frac{d}{100 \text{ pc}}\right)^2 \text{erg s}^{-1}$ or a 1–100 keV luminosity of $L_{1-100} = (0.8^{+0.7}_{-0.4}) \times 10^{39} \left(\frac{d}{100 \text{ pc}}\right)^2 \text{erg s}^{-1}$.

This result is consistent with $L_8$ calculated via the photoelectric absorption process. Indeed, comparing equation (2) and (5), we have

$$\frac{L_8^{(abs)}}{L_8^{(scat)}} = 3 \left(\frac{\theta_{\text{abs}}}{\theta_{\text{scat}}}ight) \left(\frac{\phi_{\text{abs}}}{\phi_{\text{scat}}} \right)^{-1} \left(\frac{Z_{\text{Fe}}}{Z_{\text{X}}}ight)^{-1} = 0.8^{+0.4}_{-0.6}$$  

which is a factor of the order of unity. The primary source luminosity independently calculated via the Compton scattering is remarkably consistent with that calculated via photoelectric absorption. The consistency strongly supports the X-ray reflection scenario. With Equation (4), the primary source luminosity in any energy band can be directly derived given the measurement of the molecular cloud flux in the same energy band. This continuum-flux-based method has also been applied to other GC molecular clouds in the future for testing the XRN model and constrain the Sgr A* outburst history (Mori et al. 2015).

The MYTorus model can also give the illuminating source spectrum, although it assumes fixed solar abundance and that the observation angle cannot be constrained with the data. By rescaling the incoming X-ray flux by the solid angle ratio of the torus ($\Omega/4\pi = 0.5$) and Sgr B2 ($\Omega/4\pi = 2.89 \times 10^{-1}$), we derive the primary source luminosity to be $L_8 = (1.4^{+0.5}_{-0.4}) \times 10^{38} \left(\frac{d}{100 \text{ pc}}\right)^2 \text{erg s}^{-1}$ (see the Appendix for details). As the 2013 X-ray emission from Sgr B2 is 30% that of its maximum flux (Section 5), the primary source luminosity with the peak Sgr B2 flux is $L_8 = (4.6^{+1.6}_{-1.3}) \times 10^{38} \left(\frac{d}{100 \text{ pc}}\right)^2 \text{erg s}^{-1}$, or $L_{3-79} = (1.5^{+0.5}_{-0.4}) \times 10^{39} \left(\frac{d}{100 \text{ pc}}\right)^2 \text{erg s}^{-1}$ with the 2001 Sgr B2 X-ray flux. With large error bars, the primary source luminosity derived by the MYTorus model overlaps with that derived with the analytical calculations, though the best-fit luminosity value is higher. For the other GC molecular clouds, the MYTorus model also gives a primary source luminosity higher than that derived from the analytical calculation roughly by a factor of 2 (Mori et al. 2015).

We note that the analytical calculations above are valid for an optically thin ($\tau_T \ll 1$) cloud where the fluorescence photons are not scattered and the continuum emission photons are scattered once inside the cloud. Sgr B2 has very complicated density profile, including three main compact cores (Sgr B2(N), Sgr B2(M) and Sgr B2(S) from north to south) and numerous clumpy regions. Overall its density decreases as radius becomes larger. Without a model fully considering the density distribution within Sgr B2, the measured $\tau_T$ for a specific region is an averaged value. For the 90$^\circ$ radius region we adopt, and larger regions previous works adopt (e.g., 4.5$'$ radius region in Terrier et al. 2010), the averaged optical depth for such large regions is $\tau_T \ll 1$, thus have been treated as optically thin as a whole. However, for the compact cores at the center of Sgr B2, which have higher local density, the local optical depths are higher than 1 as indicated by Herschel and NuSTAR measurements, though with large error bars. For these regions, multi-scattering could take place during the decay stage. The X-ray emission life time of optically thick material is longer than its light crossing time ($t = \tau_T c$ when $\tau_T \gg 1$) due to decay caused by multi-scattering. The reflected X-ray emission follows an exponential decay for optically thick materials and a parabolic decrease for optically thin materials. Therefore, the optically thicker material flux decreases much slower at late stages. If the compact core regions are confirmed to be optically thick, X-ray emission from the central compact cores Sgr B2(M) and Sgr B2(N) could still be bright enough to be detected when the surrounding optically-thin regions completely fades. However, if the optical depth in the direction of the compact cores can be more tightly constrained to $\tau_T = 1$, the multi-scattering effect would be negligible. Future observation of Sgr B2 can test this prediction and better constrain the local optical depth in the direction of the compact cores.

### 6.2. Cosmic Ray Electron Bombardment

LECRe cannot be the major contribution to the bright Fe Kα line emission from Sgr B2, as both the required iron abundance and the electron power are too high to be physical (e.g., Revnivtsev et al. 2004) [Terrier et al. 2010]. After a decade of decreasing in the Fe Kα line flux, we tested whether the the constraints on the LECRe parameters by the remaining emission level in 2013 are still excluding this scenario. Generating the bremsstrahlung emission with the observed slope of $\Gamma = 1.9$ in 3-79 keV requires a relatively soft electron spectra with $s \sim 2.8$ and a minimum CR electron energy far below 100 keV as we measured, which is illustrated in Tatischeff et al. 2012]. For such a soft CR spectrum, the neutral Fe Kα line is predicted to be relatively weak, with $E_W < 0.4 \times (Z/Z_\odot)$ keV (Fig. 3 in Tatischeff et al. 2012]. Therefore, to fit the observed Fe Kα line EW of $\sim 1$ keV as measured by NuSTAR, the required Fe abundance is found to be $Z_{Fe} = 4.0^{+2.0}_{-1.0}$, still significantly exceeding the current measurement of GC metallicity of solar to twice solar. This is due to the relatively inefficient production of 6.4 keV photons by LECRe interactions, for which the iron fluorescence yield $R_{6.4\text{ keV}} = L_X/(dW_e/dt)$ is always lower than $1 \times 10^{-6} (Z/Z_\odot)$ for $s > 2.3$ and $E_{min} < 100$ keV (Tatischeff et al. 2012]. Besides the unphysical Fe abundance required by the Fe Kα emission, the LECRe model also results in an overall poorer fitting to the broadband 3–79 keV spectrum compared to the XRN model. Especially, the hard X-ray part of the spectrum has more residuals for the LECRe model, thus providing a more exclusive constraint which does not depend on local metallicity.

Another difficulty in explaining all the 6.4 keV emission with LECRe is the lack of an obvious particle acceleration site. Yusuf-Zadeh et al. (2002) suggested that the interaction of non-thermal radio filaments and the cloud could locally accelerate CR electrons. Yet until now no such filaments have been observed around Sgr B2. Even if there exists a local CR acceleration site, the non-thermal electrons with energies below 100 keV are not
able to escape the acceleration region and penetrate the whole dense cloud (Yusef-Zadeh et al. 2007). Therefore, we conclude that LECRe scenario cannot be a major contributor to the remaining X-ray emission from Sgr B2 in 2013.

6.3. Cosmic Ray Ion Bombardment

Although it is clear that the Sgr B2 Fe Kα emission decreases since 2001, the same level of the Fe Kα emission in 2012 and 2013, and the lacking of measurements between 2005 and 2011 do not allow us to determine whether the Fe Kα emission was still decreasing in 2013 or it has reached the constant background emission level. Future observations of Sgr B2 can distinguish between the two cases. Dogiel et al. (2009) estimated that CR protons could contribute to about 15% of the observed maximum Fe Kα flux obtained around 2000, although this prediction is highly model dependent. In 2012 and 2013, the Sgr B2 Fe Kα emission reached 20% of that measured in 2001 (Section 4), therefore the 2012 and 2013 Fe Kα emission could be mainly due to CR proton bombardment.

The 2013 NuSTAR Sgr B2 spectrum can be fit well with the self-consistent LECRp model. The required metallicity of $Z/Z_\odot = 2.5^{+1.5}_{-1.9}$ overlaps with the GC environment metallicity of one solar to twice solar. Assuming all the X-ray emission from the central 90″ Sgr B2 in 2013 is due to CR proton bombardment, the required total power of the CR proton of energies between $E_{\text{min}} = 10$ MeV and $E_{\text{max}} = 1$ GeV in the cloud region is $dW/dt = (1.0 \pm 0.3) \times 10^{39}$ erg s$^{-1}$. Taking the uncertainty of $E_{\text{min}}$ into account, the required CR proton energy ranges in $dW/dt = (0.4 - 2.3) \times 10^{39}$ erg s$^{-1}$ (Section 5.1.4). According to Tatischeff et al. (2012), there is an additional 40% power comes from α-particles with $\zeta_\alpha/C_p = 0.1$, the final required total kinetic CR ion power is (0.6 - 3.2) $\times 10^{39}$ erg s$^{-1}$, which is roughly 10% of the steady state mechanical power supplied by supernovae in the inner ~200 pc of the Galaxy (Tatischeff et al. 2012). The required power injection is quite significant and probably difficult to fully be accounted with typical sources.

The power deposited into the cloud is lower than the incident CR ion power, because CR ions with energies lower than $E_{\text{min}}$ cannot penetrate the cloud and that with a path length of $\Lambda = 5 \times 10^{23}$ cm$^{-2}$ those ions with energies higher than 180 MeV can escape from the cloud without depositing energy in it (Tatischeff et al. 2012). Therefore, the power deposited by CR ions into central Sgr B2 is $W_d \sim 8 \times 10^{38}$ erg s$^{-1}$. With the central 90″ of Sgr B2 mass of $M \sim (0.5 - 2) \times 10^6 M_\odot$ estimated based on the simplified Sgr B2 density profile (Section 1) and a total mass of $M = 6 \times 10^6 M_\odot$ (Lis & Goldsmith 1990), the corresponding ionization rate can be estimated to be $\zeta_H \sim (6 - 10) \times 10^{-15}$ H$^{-1}$ s$^{-1}$ using Equation (11) in Tatischeff et al. (2012). This CR ionization for the dense materials in Sgr B2 is comparable to the GC CR ionization rate of $\zeta_H \sim (1 - 3) \times 10^{-15}$ s$^{-1}$, which is found to be uniform throughout the GC on scales of 200 pc (e.g. Goto et al. 2011).

In the following we compare the application of LECRp model on Sgr B2 and the Arches region and discuss possible LECR ion sources. The X-ray emission from the Arches region was interpreted as CR ion bombardment before a significant decrease in Fe Kα was revealed (Clavel et al. 2014). In the LECR scenario, the CR spectral index is constrained by the broadband NuSTAR Arches region spectrum to $s = 1.65^{+0.05}_{-0.05}$ (Krivonos et al. 2014), which agrees with that derived from Sgr B2 spectrum ($s = 1.9^{+0.8}_{-0.7}$). The GC LECR ion source is suggested to be Galactic supernovae or star accretion onto Sgr A* (Dogiel et al. 2013 and the references therein). The arches spectrum requires an ionization rate ($\zeta_H \sim 10^{-13}$ H$^{-1}$ s$^{-1}$) (Tatischeff et al. 2012) higher than that of Sgr B2 by a factor of $\sim 10 - 20$, significantly exceeding the CR ionization rate in the GC environment. Recently, Clavel et al. (2014) found a 30% flux drop from the Arches cluster in 2012, which indicates that a large fraction of the non-thermal emission of the Arches is likely due to the past activity of Sgr A*. This could explain the high ionization required by the Arches spectrum, assuming all the X-ray emission is due to LECRp. If the CR ionization rate of the Arches cluster is comparable to the GC CR ionization rate, LECR bombardment should contributes to only a few percent of the total X-ray emission. However, there could be local LECR ion sources within the Arches cluster (Dogiel et al. 2009), which would increase the local CR ionization rate and therefore the LECR contribution to the X-ray emission. While it is uncertain when the Arches cluster X-ray emission will reach the constant background level, it is likely that Sgr B2 has reached or will soon reach the background X-ray emission level. Therefore, the remaining emission from Sgr B2 will be a unique powerful tool to probe the CR population in the GC in the X-ray energy bands. The LECRp scenario will stay valid as long as no further decrease is observed in the coming years.

6.4. The Nature of G0.66−0.13

G0.66−0.13 is an elliptical feature with a major radius of ~5 pc and a minor radius of ~3 pc. The illuminating source photon index ($\Gamma = 1.4 \pm 0.5$) is compatible with that of the central region of Sgr B2 ($\Gamma = 2.2 \pm 0.4$). The intrinsic column density of $N_H (i) = 3.0^{+3.8}_{-1.9} \times 10^{23}$ cm$^{-2}$ is lower than the column density of the central part of Sgr B2. The primary source luminosity based on its 2012 peak Fe Kα emission is $L_\alpha = (1.3 \pm 0.5) \times 10^{38} (R/100$ pc)$^2 (Z_{Fe})^{-1}$ erg s$^{-1}$, or $L_\alpha = (4.3 \pm 1.6) \times 10^{38} (R/100$ pc)$^2 (Z_{Fe})^{-1}$ erg s$^{-1}$. It is consistent with the primary source luminosity required by the central region of Sgr B2. The Fe Kα line intensity of G0.66−0.13 exhibits fast decay at 6.4 keV. The linear fitting shows that the G0.66−0.13 Fe Kα emission demonstrates an increasing trend prior to 2013 (Figure 5). However, the increase could be much sharper than what is shown in Figure 5. We do not have good enough statistics to distinguish between a linear increasing from 2000 to 2012 and a sharp peak in 2012 on top of a baseline Fe Kα emission. In 2012, the peak Fe Kα emission from G0.66−0.13 was brighter than the Sgr B2 core Sgr B2(M). The non-detection of its Fe Kα emission in 2013 suggests a fast decrease in Fe Kα line flux. The fast flux decrease with a lifetime of $t \sim 1$ year roughly matches the light crossing time of the peak within G0.66−0.13 ($r/c \sim 2$ years).
Both Sgr B2 and G.66–0.13 are about 100 pc away from Sgr A*, while the G.66–0.13 X-ray flux reached the peak 12-18 years after Sgr B2. If G.66–0.13 was illuminated by the same Sgr A* outburst that illuminated Sgr B2, it should be 16-23 pc behind the Sgr B2 center in the line-of-sight assuming Sgr B2 is 130 pc in front of the projection plane [Reid et al. 2009]. Therefore, G.66–0.13 could be a molecular clump, with a higher local density than its surrounding environment, located in the Sgr B2 envelope which extends to about 22.5 pc.

7. CONCLUSIONS

We studied the X-ray emission of the central 90° of Sgr B2 and a newly discovered cloud feature G.066–0.13 with NuSTAR. We present their broadband spectra, morphology and time variability and discuss two possible origins of the observed X-ray emission in 2013: X-ray reflection nebula and cosmic ray bombardment.

• Central 90° of Sgr B2. The substructures of Sgr B2 are resolved at sub-arcminute scales at hard X-ray energy (> 10 keV). The hard X-ray continuum emission in 10–40 keV reveals two compact star-forming cores Sgr B2(M) and Sgr B2(N) surrounded by diffuse emission with the western side brighter than the eastern side. The central 90° region is marginally optically thin on average.

• Main Compact Cores Sgr B2(M) and Sgr B2(N): Compact cores Sgr B2(M) and Sgr B2(N) are resolved above 10 keV for the first time. Both the 6.4 keV line emission and the 10–40 keV continuum emission peak at the location of the main compact core Sgr B2(M). While Sgr B2(N) is significant in 10–40 keV continuum emission, it is not detected at 6.4 keV in 2013 perhaps due to higher local absorption. The Sgr B2(M) spectrum requires a high optical depth of \( \tau_T = 1.3^{+2.5}_{-1.0} \), consistent with the Herschel measurement, suggesting it is not optically thin.

• XRN vs. LECR: After a decade of decreasing, the 2012–2013 Fe Kα emission reached 20% of that in 2001, but remained at the same level during 2012–2013. The lack of data between 2005 and 2011 does not allow us to determine whether the 2013 Fe Kα emission kept decreasing (which could be explained by the XRN or the LECR model) or had reached the constant background level (for which the LECR model is favored). We first excluded the LECR scenario based on unphysical best-fit parameters, no matter whether the Fe Kα emission is decreasing or not. The significant 6.4 keV line of Sgr B2 in 2013 requires the Fe abundance to be at least 3.4 solar, significantly exceeding the current measurements of the GC metallicity. The best-fit minimum electron energy is far below 100 keV. With such low energies, the non-thermal electrons are not able to penetrate Sgr B2 even if there is a local CR particle acceleration site. Therefore, we conclude that the LECR scenario cannot be a major contributor to the remaining level of the X-ray emission from Sgr B2 in 2013.

The 2013 Sgr B2 X-ray emission can be best explained by the XRN scenario if the X-ray emission is still decreasing. We examine the XRN scenario with an ad hoc XRN model and a self-consistent XRN model. Due to lack of geometrical information in this ad hoc model, interpretation of the intrinsic column density of \( N_H(i) = (5.0 \pm 1.2) \times 10^{23} \) cm\(^{-2}\) calls for caution. With the self-consistent XRN model MYTorus, we derive the intrinsic equatorial column density to be \( N_H(i) = (1.0 \pm 0.4) \times 10^{24} \) cm\(^{-2}\), twice that derived from the ad hoc model. This corresponds to \( \tau_T = 0.67 \pm 0.27 \), confirming that the central 90° region is marginally optically thin on average. In the XRN scenario, we develop an analytical method to calculate the primary source luminosity via Compton scattering with the 10–40 keV scattered continuum (Equation 5). With this approach the primary source luminosity in any X-ray energy band can be derived with the observed continuum emission. The resulting primary source luminosity is \( L_{3-79 \text{ keV}}^{\text{abs}} = (5.6^{+2.2}_{-1.0}) \times 10^{38} (d/100 \text{ pc})^2 \text{ erg s}^{-1} \). This is remarkably consistent with the primary source luminosity calculated via the photoelectric absorption process based on the updated source spectral shape, resulting in \( L_{3-79 \text{ keV}}^{\text{abs}} = (5.0 \pm 2.3) \times 10^{38} (d/100 \text{ pc})^2 \text{ erg s}^{-1} \). We find that \( L_{3-79 \text{ keV}}^{\text{scat}} \) is of order of unity, confirming the self-consistency of the XRN model.

In case the Fe Kα emission has reached the background level in 2013, the reflected X-rays could have completely faded and the LECRp process could be a major contributor. The required total CR ion power is \( \frac{dW}{dt} = (6.0 - 3.2) \times 10^{39} \) erg s\(^{-1}\), about 10% of the mechanical power supplied by supernovae in the inner \( \sim 200 \) pc of the Galaxy. The CR ionization rate is found to be \( \zeta_H \sim (6 - 10) \times 10^{-15} \) H\(^{-1}\) s\(^{-1}\), consistent with the CR ionization rate in the GC environment. If the Sgr B2 X-ray emission has indeed reached the background level, it would be a powerful tool to constrain the CR ion population in the GC.

• The new cloud feature G.066–0.13: The Fe Kα line flux of G.066–0.13 reached its peak in 2012 and quickly diminished within \( \sim 1 \) year. The fast variability is best explained by the XRN scenario. The required primary source luminosity \( L_{3-79 \text{ keV}}^{\text{abs}} = (4.3 \pm 1.6) \times 10^{38} (d/100 \text{ pc})^2 Z_{\text{Fe}}^{-1} \) erg s\(^{-1}\) is consistent with that derived from central Sgr B2. Assuming G.66–0.13 is illuminated by the same Sgr A* outburst that illuminates Sgr B2, it should be 16-23 pc behind the Sgr B2 center along the line-of-sight, which is still within the Sgr B2 region. G.66–0.13 could be a molecular clump with a local column density higher than surroundings located in the Sgr B2 envelope.

• Other Galactic center molecular clouds and Sgr A* outburst history: In the NuSTAR Galactic plane survey, other Galactic center giant molecular clouds were also detected well above 10 keV, including the “Bridge” and G.013–0.13. The same methodology to derive the primary source luminosity is applied to each cloud and reconstruct the Sgr A* outburst history (Mori et al. submitted).

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Figure 6. A spherical cloud (red circle) in a virtual torus (grey area) shows how the MyTorus model geometry is related to the GCMC geometry. The illuminating source (Sgr A* for GCMC) is shown by the yellow star. In the MyTorus model, the incident angle $\theta_{\text{obs}}$ is defined as the angle between the symmetry axis of the torus (dotted grey line) and the LOS (black vertical line). The equatorial column density $N_H$ is defined over the minor diameter of the torus. When applying to the GCMC case, the quasi-spherical cloud can be considered as part of the torus. Incoming X-ray photons from the illuminating source are scattered by the cloud at an angle $\theta$ to the direction of the observer. The green lines show the travel paths of the X-ray photons. $d_{\text{proj}}$ is the projected distance between the cloud and the illuminating source as seen by the observer, and $d_{\text{los}}$ is the LOS distance between the cloud and the projected plane. A face-on view of the torus ($\theta_{\text{obs}} = 0^\circ$) corresponds to the case where the cloud locates in the projected plane noted by a dashed black horizontal line ($\theta = 90^\circ$, $d_{\text{los}} = 0$). The figure is from Appendix B1 in Mori et al. (submitted).

APPENDIX

APPLICABILITY OF MYTORUS MODEL TO SGR B2 SPECTROSCOPY

The MyTorus model was originally developed to study X-ray spectra of Compton-thick AGNs. The assumed geometry is a torus with a uniform distribution of neutral material reflecting incoming X-rays from an illuminating source at the center. Three model components are offered: the transmitted continuum (MYTZ), the scattered continuum (MYTS) and Fe fluorescence lines (MYTL). The model allows a range of values for three key model parameters: the illuminating source photon index $\Gamma = 1.4 - 2.6$, the equatorial hydrogen column density (corresponding to the minor diameter of the torus) $N_H = 10^{22} - 10^{25}$ cm$^{-2}$ and the inclination angle $\theta_{\text{obs}} = 0^\circ - 90^\circ$. Considering a spherical molecular cloud as part of a virtual torus, the MyTorus model can be applied to molecular cloud spectra with some limitations. Figure A6 shows the geometry of a molecular cloud and a virtual torus. In the MyTorus model, the observation angle $\theta_{\text{obs}}$ is defined as the angle between the light-of-sight (LOS) and the symmetry axis of the torus. In contrast, most GC molecular cloud publications use the scattering angle $\theta$. A face-on case in the MyTorus model ($\theta_{\text{obs}} = 0^\circ$) corresponds to a cloud in the same projected plane as the illuminating source, where the scattering angle is $\theta = 90^\circ$. For three key assumptions of the MyTorus model, we discuss the valid parameter space where the model is applicable to the molecular cloud X-ray reflection spectra in the following.

Toroidal Reflector

In the face-on case ($\theta_{\text{obs}} = 0^\circ$), MyTorus gives an accurate solution for a fully illuminated quasi-spherical molecular cloud, as different azimuthal parts of the torus all scatter at the same angle $\theta = 90^\circ$. To derive the incoming X-ray flux that illuminates the cloud (red circle in Figure A6, which is part of the grey virtual torus), we simply need to rescale it by the solid angle ratio of the torus (fixed to $\Omega/2\pi = 0.5$) and the cloud. For Sgr B2, its solid angle respect to Sgr A*
is $\sim 2.89 \times 10^{-4}$. When the inclination angle deviates from $\theta_{\text{obs}} = 0^\circ$, i.e. the face-on case, different azimuthal parts of the torus scatter incoming X-rays at different angles. The reflected spectrum thus shows variation and becomes inaccurate for a quasi-spherical molecular cloud. However, the scattered component MYTS does not vary strongly with $\theta_{\text{obs}}$ as long as $\theta_{\text{obs}} \lesssim 60^\circ$ and $N_H \lesssim 10^{24}$ cm$^{-2}$ (See Figure 17 in Mori et al. 2015). When $\theta_{\text{obs}} > 60^\circ$, the spectral variation starts to become significant, for the following two reasons. Firstly, as the inclination angle increases, the X-ray photons back-scattered by the side of the torus hit the closer side of the torus before reaching the observer, thus are subject to further absorption. Secondly, multi-scattering can become important and cause angular-dependent X-ray flux, although it is negligible at $N_H \lesssim 10^{24}$ cm$^{-2}$.

Next we determine the systematic error of measuring $N_H$, $\Gamma$, and model normalization based on the MYTorus model. We simulated MYTS spectra for $\theta = 60^\circ$ and $N_H = 10^{23} - 10^{24}$ cm$^{-2}$ and fit with the MYTS model with $\theta_{\text{obs}}$ set to 0$^\circ$. The deviations of the best-fit value of these model parameters from their input value are adopted as the systematic errors. At $N_H = 10^{23}$ cm$^{-2}$, the deviation of $N_H$, $\Gamma$, and model normalization from their input are 10%, 1% and 7%, while at $N_H = 10^{24}$ cm$^{-2}$, the deviations increase to 25%, 3% and 10%. Therefore we conclude that the reflected X-ray spectrum model MYTorus is not sensitive to the reflector geometry in the NuSTAR energy band as long as $\theta_{\text{obs}} \lesssim 60^\circ$ and $N_H \lesssim 10^{24}$ cm$^{-2}$. Similar to the face-on case, the incident X-ray flux can be derived by rescaling it with the solid angle ratio of the torus $\Omega/4\pi = 0.5$ and central 90$^\circ$ of Sgr B2 cloud $\Omega/4\pi = 2.89 \times 10^{-4} \times (100 \text{ pc}/R)^2$ with systematic error $< 10\%$. However, the conversion from the incident angle in the MYTorus model to the position of the cloud cannot be well established. We note that the $N_H$ measured by the MYTorus model is an averaged value over the torus: it does not take into account the specific geometry of the studied cloud and its possible partial illumination (see e.g. Odaka et al. [2011]). The systematic errors are estimated solely based on the MYTorus model and might therefore be underestimated. The more sophisticated model under development will better constrain the $N_H$ (Walls et al. in prep).

Fe Abundance Fixed to Solar

The Fe abundance is important in determining the incoming X-ray flux solely from measurements of Fe fluorescent lines, while the 3–79 keV broadband spectrum of NuSTAR also provides the energy range where Compton scattering dominates (> 10 keV) over Fe fluorescence. The incoming X-ray flux is determined consistently from both the Compton scattering process with the MYTS component and the Fe fluorescence process via the MYTL component. The best-fit model parameters ($N_H$, $\Gamma$ and normalization) of MYTS do not vary significantly when the MYTS model is fit to the cloud X-ray spectra with or without the 6–10 keV energy range which covers the 6.4 keV Fe K$\beta$ line and the 7.1 keV Fe K edge. Data tables for different Fe abundances in the range of $Z_{Fe} = 0.5 − 3.0$ will be implemented to the modified XRN model for molecular clouds.

Uniform Density

The incoming X-ray flux from the illuminating source will not be significantly affected by non-uniform density profiles as long as $N_H \lesssim 10^{24}$ cm$^{-2}$, where multi-scattering is negligible. If the density is not uniform, large clouds can include very dense clumps where multi-scattering effects can be significant. For Sgr B2, the largest optical depth is $\tau_T \sim 1$ in the direction of the densest cores Sgr B2(M), in which case the multi-scattering effects are negligible. The current XRN model does not address the complicated density profile of Sgr B2, which contains compact cores, clumps and an overall decreasing density profile. A more sophisticated XRN model with a reasonable density profile of Sgr B2 implemented is under development (Walls et al. in prep) and will reduce the uncertainties caused by non-uniformity of Sgr B2.

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