Multiplet-specific shape resonance and autoionization effects in (2+1) resonance enhanced multiphoton ionization of O₂ via the d 1Π g state

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Multiplet-specific shape resonance and autoionization effects in (2+1) resonance enhanced multiphoton ionization of \( \text{O}_2 \) via the \( \sigma^2 \Pi_g \) state

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In this paper we discuss the single-photon ionization dynamics of the \( \sigma^1 \Pi_g \) Rydberg state of \( \text{O}_2 \). Comparison is made with vibrationally resolved measurements of photoelectron spectra which employ \( (2+1) \) resonance enhanced multiphoton ionization (REMPI) through the \( \sigma^1 \Pi_g \) state. A \( \sigma^1 \) shape resonance near the ionization threshold leads to non-Franck-Condon vibrational branching ratios and a substantial dependence of photoelectron angular distributions on the vibrational state of the \( X^2 \Pi_g \) ion. Significant differences exist between our one-electron predictions and experiment. These are mainly attributed to electronic autoionization of repulsive \( \Sigma_u^+ \), \( \Sigma_u^- \), and \( \Delta_u \) states associated with the \( 1\pi_u^2 \) configuration. A proposed singlet \( K \) \( \Pi_u \) Rydberg state converging to the \( A^2 \Pi_u \) ion probably also contributes to autoionization in the \( \sigma^1 \Pi_g \) state spectrum. We also show that autoionizing \( \Pi \) and \( \Pi \) Rydberg states of \( \text{O}_2 \) converging to the \( \sigma^1 \Pi_g \) and \( A^2 \Pi_u \) ionic thresholds, respectively, may play a previously unsuspected role in the \( C^3 \Pi_g \) state one-color REMPI spectra. We discuss multiplet-specific (spin-dependent) effects via comparison of these results with recent experimental and theoretical studies of \( \text{O}_2 \) \( \sigma^1 \Pi_g \) photoionization.

I. INTRODUCTION

The photoionization dynamics of the \( C^3 \Pi_u \) \( (1\pi_u 3\sigma_u^0) \) Rydberg state of \( \text{O}_2 \) have recently been studied experimentally and theoretically by \( (2+1) \) resonance enhanced multiphoton ionization spectroscopy (REMPI).\(^1\text{-}^5\) These studies have shown that a \( \sigma_u \) shape resonance leads to strong non-Franck-Condon ionic vibrational distributions and photoelectron angular distributions. Presently there is significant interest in using REMPI to prepare molecular ions in vibrationally (and rotationally) state-selected states. Since the shape resonance in \( \text{O}_2 \) was shown to effectively inhibit efficient vibrational state-specific production of ions via the \( C^3 \Pi_u \) state, additional experimental studies have probed the higher-lying \( '4s-3d' \) Rydberg states.\(^6\) Due to the symmetry of the excited orbital, some of these levels may not access the \( \sigma_u \) ionization continuum, thus permitting \( \text{O}_2^+ \) state preparation to better than \( \sim 80\% \) for several vibrational levels.

In this paper, we present studies of photoionization dynamics of the \( d^1 \Pi_g \) \( (1\pi_u 3\sigma_u^0) \) Rydberg state of \( \text{O}_2 \), the singlet analog of the \( C^3 \Pi_u \) state. The \( d^1 \Pi_g \) state of \( \text{O}_2 \) has been detected, and partially characterized, by several electron impact and REMPI studies.\(^6\text{-}^{11}\) The singlet coupling of the \( 3\sigma_u^0 \) Rydberg electron to the \( X^2 \Pi_u \) ion core results in a small, positive energy shift of the potential energy curve, relative to the triplet state (\( -0.1 \) eV). In contrast, the \( \sigma_u \) shape resonance with its localized character, as well as the energetically accessible valence autoionizing states, exhibit large (\( \sim 1-3 \) eV) energy shifts relative to their triplet analogs. Due to these considerations, the REMPI photoelectron dynamics may significantly depend on which spin state of the neutral Rydberg level is accessed in the two-photon absorption step. In particular, the photoelectron spectra observed by Miller et al.\(^14\) for the \( d^1 \Pi_g \) Rydberg state display greater non-Franck-Condon behavior than that observed for the \( C^3 \Pi_u \) spectra. As discussed below, we attribute this mainly to autoionization of repulsive valence states and Rydberg states converging to excited states of the ion and not to the \( \sigma_u \) shape resonance. Such multiplet-specific shape resonance and autoionization effects are generally energy dependent. They could be further probed to great advantage via two-color REMPI experiments.

Although we believe that autoionization is the major source of disagreement between present theory and available experiments, another class of electronic interactions relevant to excited-state photoionization dynamics are avoided crossings between the resonantly prepared Rydberg state and repulsive valence states of the same electronic symmetry. Van der Zande et al.\(^15\) have recently studied the \( C^3 \Pi_u \) and \( d^1 \Pi_g \) Rydberg states of \( \text{O}_2 \) using charge-exchange translational spectroscopy. Specifically they investigated and deduced details of the Rydberg-valence interactions and associated predissociation processes. These interactions may influence ion vibrational distributions through electronic correlations and perturbations of vibrational levels of the neutral Rydberg in the vicinity of the curve crossing.

In Sec. II we give a brief discussion of numerical details of the calculations. In Sec. III we present vibrational branching ratios and discuss the shape-resonance and electron correlation effects relevant to ion vibrational distributions for photoionization of the \( d^1 \Pi_g \) Rydberg state. A qualitative discussion of the correlation effects in terms of Franck-Condon factors, survival factors, and SCF calculations is given. Rigorous incorporation of these states in the photoionization calculations remains a major goal of our studies. Also presented in Sec. III are two-color (energy-dependent)}
branching ratios and vibrationally resolved photoelectron angular distributions. Section IV gives a brief conclusion.

II. CALCULATIONAL DETAILS

In the frozen-core Hartree–Fock approximation there are four dipole-allowed channels for ionization of the \( ^1\Pi_g \) state corresponding to photoionization of the singly occupied \( 3\sigma_g \) Rydberg orbital. The electronic continuum wave functions are

\[
\Psi( ^1\Pi_u ) = \frac{1}{\sqrt{2}} \{ |[\text{core}] \, 1\pi^+_g \, k\sigma_u | - |[\text{core}] \, 1\pi^+_g \, k\sigma_u | \},
\]

(1a)

\[
\Psi( ^1\Sigma_u^+ ) = \frac{1}{2} \{ |[\text{core}] \, 1\pi^+_g \, k\pi_u^- | + |[\text{core}] \, 1\pi^-_g \, k\pi_u^- | - |[\text{core}] \, 1\pi^+_g \, k\pi_u^- | - |[\text{core}] \, 1\pi^-_g \, k\pi_u^- | \},
\]

(1b)

\[
\Psi( ^1\Sigma_u^- ) = \frac{1}{2} \{ |[\text{core}] \, 1\pi^+_g \, k\pi_u^- | - |[\text{core}] \, 1\pi^-_g \, k\pi_u^- | - |[\text{core}] \, 1\pi^+_g \, k\pi_u^- | + |[\text{core}] \, 1\pi^-_g \, k\pi_u^- | \},
\]

(1c)

\[
\Psi( ^1\Delta_u ) = \frac{1}{\sqrt{2}} \{ |[\text{core}] \, 1\pi^+_g \, k\pi_u^- | - |[\text{core}] \, 1\pi^-_g \, k\pi_u^- | \},
\]

(1d)

where \([\text{core}] = 1\sigma_g^2 \, 2\sigma_g^2 \, 2\sigma_g^2 \, 3\sigma_g^2 \, 1\pi_u^2\). The associated one-particle Schrödinger equations for the continuum orbitals can be derived straightforwardly\(^{17,18}\) and have been presented in detail in Eq. (2) of Ref. 5 for the case of triplet coupling. The singlet-coupled equations can be obtained simply by changing the signs preceding the exchange operators for the \( 1\pi_g \) electron, and the nonlocal \( S' \) terms.

The Gaussian basis sets, internuclear distances, partial-wave expansions, and radial grids used to evaluate the \( R \)-dependent transition moments for the \( k\sigma_u \) and \( k\pi_u \) channels are identical to those for the \( C^3\Pi_g \) calculations.\(^3,5\) The initial state \( ^1\Pi_g \) SCF wave functions were calculated using a \( (9s5p2d) / (4s3p2d) \) Gaussian basis set with diffuse functions on the center of mass with exponents identical to those in Ref. 5. The total SCF energy of the \( ^1\Pi_g \) state at \( R = 2.282 \text{ao} \) with this basis is \(-149.285 87 \text{a.u.} \), resulting in an energy splitting of 0.073 eV compared to the \( C^3\Pi_g \)

![FIG. 1. \( O_2 \) potential energy curves for the ground state, the first ionic state, and singlet and triplet valence states deriving from the electronic configuration \( 1\pi^+_g \). The potential curves are taken from Refs. 29 and 30.](http://scitation.aip.org/termsconditions)
state. The $d' \Pi_g$ state vibrational wave functions and those for the $X^2 \Pi_g$ ion were calculated using the RKR potentials discussed in Refs. 3 and 5. For later discussion, in Fig. 1 we summarize potential energy curves for the $O_2$ neutral and ionic ground states and several singlet and triplet Rydberg and repulsive valence states relevant to this discussion.

III. DISCUSSION OF RESULTS

A. Shape resonance effects

In Fig. 2 we show the calculated photoionization cross section for the singlet and triplet-coupled $3s\sigma_u \rightarrow k\sigma_u$ channel at the internuclear distance $R = 2.088 \, a_0$. The $\sigma_u$ shape resonance in the singlet-coupled channel is shifted $\sim 2.5$ eV higher in kinetic energy than the triplet-coupled channel, similar to singlet-triplet energy shifts typically observed for excited valence states. This shift is due to the greater (repulsive) exchange interaction of the ionized electron with the ion core in the singlet-coupled final state. In Fig. 2 the large difference between the length and velocity cross sections at low energy is due to our neglect of electron correlations beyond the Hartree–Fock level in the $13 \Pi_g$ ionization channels. These differences largely cancel upon forming the vibrational branching ratios (see Fig. 3). Residual discrepancies with experiment are attributed mainly to autoionization of repulsive valence states (discussed below).

For ground state photoionization of $O_2$, the $\sigma_u$ shape resonance has been discussed by Raseev et al.\cite{19} for the $3\sigma_u$ level, and by Gerwer et al.,\cite{20} Dittman et al.,\cite{21} and Braunstein and McKoy\cite{22,23} for both the $3\sigma_u$ and $1\sigma_g$ levels. Particularly for the $3\sigma_u$ level, it was shown\cite{24} that it is essential to include multiplet-specific aspects of this problem to account for observed one-electron features of the photoionization spectra. In these ground and the present excited-state studies, the $R$ dependence of the transition moment induced by the shape resonance results in non-Franck–Condor effects observable in both vibrational branching ratios and photoelectron angular distributions.\cite{25-26}

For the present REMPI studies, the shift of the resonance to higher kinetic energy will result in some decrease in the calculated non-Franck–Condor effect, but not as much as Fig. 2 may suggest. Note that the shift in the $\sigma_u$ resonance position is much larger than the difference in ionization thresholds (3.84 and 3.93 eV for the $v' = 0$ levels, respectively). The photoelectron energies for the $d' \Pi_g$ and $C^3 \Pi_g$ (2 + 1) spectra range from $\sim 0.25$–1.3 eV, which is a small portion of the abscissa scale in Fig. 2. The $\sigma_u$ cross section still depends strongly on $R$, causing only a weak detuning effect when compared against the triplet results.\cite{5} Branching ratios and angular distributions which illustrate the energy dependence over a broad energy range are discussed below.

![TABLE I. Summary of vibrationally resolved cross sections and branching ratios.](image)

*From Ref. 14.

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure2.png}
\caption{Calculated photoionization cross sections for the $3s\sigma_g \rightarrow k\sigma_u$ channel of the $O_2$ $d' \Pi_g$ and $C^3 \Pi_g$ states. Solid curves: length form; dash curve: velocity form.}
\end{figure}

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure3.png}
\caption{Calculated vibrational branching ratios for photoionization of the $\nu' = 0$–3 levels of the $O_2$ $d' \Pi_g$ state. Length form (crossed bar); velocity form (crosshatched bar). The calculations are compared with the measurements of Miller et al. (Ref. 14, solid bar).}
\end{figure}
B. Branching ratios and correlation effects

Figure 3 shows our calculated vibrational branching ratios compared with the photoelectron intensities measured by Miller et al.\textsuperscript{14} for the $\nu' = 0$–3 levels of the $1^1\Pi_g$ state. Table I gives a summary of the calculated and measured branching ratios. These distributions have been normalized so that the sum over $\nu^+$ for each intermediate level equals unity. Inclusion of the $R$ dependence of the transition moment arising from the shape resonance accounts for some of the observed $\Delta\nu \neq 0$ intensity, e.g., the $\nu^+ = 3$–5 states accessed via the $\nu' = 2$ and intermediate states. The Franck-Condon approximation predicts essentially zero intensity for these off-diagonal transitions. However, major discrepancies between theory and experiment are more apparent for the singlet spectra than for the triplet.\textsuperscript{2,3,5} We attribute these discrepancies mainly to autoionizing repulsive valence states and Rydberg states converging to excited ionic states. Perturbations of the resonant intermediate levels by repulsive valence states cannot be ignored; however, as discussed below, we expect this interaction to be of lesser consequence in the present REMPI problem.

1. Autoionization of repulsive valence states

Prior studies\textsuperscript{2-5} of the photoionization of the O$_2$ C $^3\Pi_g$ Rydberg state have suggested the importance of autoionizing $3^\Delta_a$, $3^\Sigma_u^+$, and $3^\Sigma_u^-$ valence states derived from the $1\pi_2 1\pi_2$ electronic configuration. These repulsive states intersect the lower portion and rise above the potential energy curve of the $X^2\Pi_g$ ion, and may thus autoionize into the $3^\Delta_a$, $3^\Sigma_u^+$, and $3^\Sigma_u^-$ channels deriving from $3\sigma_g \rightarrow k\pi_u$ ionization. To qualitatively discuss the importance of autoionization of these repulsive states, we introduce dimensionless autoionization probabilities $\xi_{\nu^+}$ and the “survival factor” $S$ ($S < 1$). The survival factor is the ratio between the dissociative recombination cross section and the capture cross section for a positive ion plus electron. Its departure from unity indicates the importance of autoionization compared with dissociation.\textsuperscript{23} Following Giusti,\textsuperscript{27} we define the quantities

\[
\xi_{\nu^+} = \pi \langle \chi_{\nu^+} | \mathbf{V}(R) | \chi_{\nu} \rangle, \tag{2a}
\]

\[
\mathbf{V}(R) = \langle \Phi_k | H | \Phi_d \rangle, \tag{2b}
\]

\[
S = \left[ 1 + \sum_{\nu^+} \xi_{\nu^+}^2 \right]^{-1}, \tag{2c}
\]

where $\chi_{\nu^+}$ and $\chi_d$ are vibrational wave functions of the ion and neutral dissociating state $\Phi_d$, respectively, and $H$ is the fixed-nuclei electronic Hamiltonian. Here $\Phi_k$ is the continuum wave function for $3\sigma_g \rightarrow k\pi_u$ photoionization. We made Franck-Condon approximations to these quantities, i.e., $\xi_{\nu^+} = \pi \mathbf{V}(R) \langle \chi_{\nu^+} | \chi_{\nu} \rangle$, where $\mathbf{R}$ is the centroid\textsuperscript{28} $\mathbf{R} = \langle \chi_{\nu^+} | \mathbf{R} | \chi_{\nu} \rangle / \langle \chi_{\nu^+} | \chi_{\nu} \rangle$. The differential Franck-Condon factors $\langle \chi_{\nu^+} | \mathbf{R} | \chi_{\nu} \rangle$ were calculated using the $X^2\Pi_g$ curve of Krupenie\textsuperscript{30} and the valence $1^3\Sigma_u^-$, $1^3\Sigma_u^+$, and $1^3\Delta_u$ potential energy curves of Saxon and Liu\textsuperscript{31} (shown in Fig. 1). The widths for the $1^3\Sigma_u^-$, $1^3\Delta_u$, and $1^3\Sigma_u^+$ states calculated by Guberian\textsuperscript{31} were employed, and we have assumed the triplet and singlet widths for states of the same spatial symmetry to be identical. The $R$-centroid procedure was employed only for the $1^3\Sigma_u^-$ valence states, since widths for the other symmetries are essentially $R$ independent.\textsuperscript{31} In Tables II and III we give our calculated $\xi_{\nu^+}$ matrix elements and survival factors for singlet and triplet valence states.

Focusing on the $\nu' = 0$ level in Fig. 3, most of the observed intensity is concentrated in the $\Delta\nu = 0$ peak. The $\sim 10\%$ intensity in the $\nu^+ = 1$ peak likely derives from

\[\text{TABLE II. Autoionization probabilities and survival factors for singlet valence states.}\]

<table>
<thead>
<tr>
<th>$\nu^*$</th>
<th>$\nu^+$</th>
<th>$c^1\Sigma_u^-$</th>
<th>$1^1\Sigma_u^+$</th>
<th>$1^1\Delta_u$</th>
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<tr>
<td>0</td>
<td>0</td>
<td>5.0x10^{-3}</td>
<td>1.1x10^{-4}</td>
<td>6.7x10^{-2}</td>
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<tr>
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<td>3.3x10^{-2}</td>
<td>2.1x10^{-3}</td>
<td>0.21</td>
<td>0.95</td>
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<tr>
<td>1</td>
<td>2.8x10^{-3}</td>
<td>5.8x10^{-4}</td>
<td>0.11</td>
<td>0.09</td>
</tr>
<tr>
<td>2</td>
<td>6.7x10^{-2}</td>
<td>4.6x10^{-2}</td>
<td>2.6x10^{-2}</td>
<td>0.84</td>
</tr>
<tr>
<td>3</td>
<td>9.5x10^{-2}</td>
<td>0.15</td>
<td>0.12</td>
<td>0.12</td>
</tr>
<tr>
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<td>0.12</td>
<td>6.8x10^{-2}</td>
<td>1.7x10^{-3}</td>
<td>0.62</td>
</tr>
<tr>
<td>5</td>
<td>0.57</td>
<td>0.48</td>
<td>0.43</td>
<td>-</td>
</tr>
</tbody>
</table>

\[\text{The single photon energy used in the (2 + 1) REMPI experiments of Ref. 14 for the \nu' = 0–3 levels are 4.118, 4.230, 4.349, and 4.450 eV, respectively. The continuum vibrational energies for each repulsive state were obtained from the relation } E_c = E_{\infty} - |E(\infty) - \hbar \omega_{\nu IU}|, \text{ where } E(\infty) \text{ is the asymptotic energy with respect to the minimum of the } X^2\Sigma_g^- \text{ potential curve (Ref. 29), and } \omega_{\nu IU} \text{ is the ground-state vibrational frequency.}\]

\[\text{Survival factors (see explanation in text).}\]

\[\text{TABLE III. Autoionization probabilities and survival factors for triplet valence states.}\]

<table>
<thead>
<tr>
<th>$\nu^*$</th>
<th>$\nu^+$</th>
<th>$B^3\Sigma_u^-$</th>
<th>$A^3\Sigma_u^+$</th>
<th>$C^3\Delta_u$</th>
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<tr>
<td>1</td>
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<td>0.27</td>
<td>3.5x10^{-3}</td>
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<td>0.96</td>
</tr>
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<tr>
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<td>2.2x10^{-2}</td>
<td>0.96</td>
</tr>
<tr>
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<td>1.3x10^{-2}</td>
<td>1.5x10^{-2}</td>
<td>0.96</td>
</tr>
<tr>
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<td>3.7x10^{-2}</td>
<td>4.7x10^{-2}</td>
<td>0.42</td>
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<td>7.9x10^{-2}</td>
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<td>1.2x10^{-2}</td>
<td>1.2x10^{-2}</td>
<td>0.96</td>
</tr>
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<td>9.6x10^{-3}</td>
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<td>6.8x10^{-2}</td>
<td>2.7x10^{-2}</td>
<td>3.3x10^{-2}</td>
<td>0.96</td>
</tr>
<tr>
<td>3</td>
<td>2.5x10^{-1}</td>
<td>4.8x10^{-2}</td>
<td>6.6x10^{-2}</td>
<td>0.96</td>
</tr>
<tr>
<td>4</td>
<td>0.14</td>
<td>4.9x10^{-2}</td>
<td>7.7x10^{-2}</td>
<td>0.96</td>
</tr>
<tr>
<td>5</td>
<td>4.5x10^{-2}</td>
<td>2.3x10^{-2}</td>
<td>4.8x10^{-2}</td>
<td>0.96</td>
</tr>
</tbody>
</table>

\[\text{The single photon energy used in the (2 + 1) REMPI experiments of Ref. 2 for the \nu' = 1–3 levels are 4.192, 4.306, and 4.418 eV, respectively.}\]

\[\text{Survival factors (see explanation in text).}\]
autoionization of the 1\Delta_u valence state since its survival factor (Table II) deviates considerably from unity. Autoionization of the 1\Delta_u state should remain prevalent for the \nu' = 1 intermediate state.

Comparison with theory suggests that the \nu' = 2 off-diagonal transitions have little contribution from direct ionization. At this level of excitation, the survival factor is about equal for all autoionizing states. Interestingly, there appears to be an effective partitioning of autoionization strength according to whether \Delta \nu < 0 or \Delta \nu > 0. Particularly for \Delta \nu < 0 autoionization of the 1\Delta_u state is strongest, while for \Delta \nu > 0 1\Sigma_u^- and 1\Sigma_u^+ autoionization dominates.

For the \nu' = 3 level again each symmetry makes a substantial contribution to autoionization. In Fig. 3 the apparent agreement between theory and experiment for the \nu' = 4 ionic level may be fortuitous since a theoretical treatment incorporating these autoionizing states will redistribute the photoelectron intensity. The increase of the parameter \xi_{\nu+}^+ for the \nu' = 5 ionic level relative to \nu' = 4 for 1\Sigma_u^- and 1\Delta_u symmetries may qualitatively account for the observed increase in photoelectron intensity.

It is interesting to compare the survival factors of the singlet autoionizing valence states with their triplet counterparts of Table III. With the exception of the 3\Sigma_u^- state, autoionization of the singlet states appears more significant than in the triplet case. This circumstance supports the apparent poor level of agreement between present theory and experiment for the d 1\Pi_u state. The large shift of the singlet valence states (compared to the triplets) results in overall more favorable Franck-Condon overlaps between the repulsive and ion potential curves.

The above qualitative analysis in terms of survival factors neglects interference with direct ionization. In fact, full theoretical consideration requires simultaneous treatment of the competing processes of direct ionization, autoionization, and dissociation. Such calculations have recently been achieved in REMPI studies\textsuperscript{12,13} of the C 3\Pi_g state of H\textsubscript{2}. MQDT studies\textsuperscript{34,35} of H\textsubscript{2} and NO have earlier considered a unified treatment of these competing processes in single-photon absorption. We are currently attempting to include these interactions in further studies of O\textsubscript{2}.

### 2. Autoionization of Rydberg states converging to the a 4\Pi_u and A 2\Pi_u ionic states

Autoionizing states converging to the a 4\Pi_u and A 2\Pi_u states of O\textsuperscript{2+} have been investigated by many workers since the early work of Price and Collins,\textsuperscript{36} and have recently been discussed and reviewed by Wu.\textsuperscript{37} A high-resolution synchrotron study of autoionizing states converging to the a 4\Pi_u ion has recently been reported,\textsuperscript{38} as well as studies which prepare these states by charge-exchange translational spectroscopy.\textsuperscript{39} The earlier discussions\textsuperscript{1-5} of the C 3\Pi_g REMPI-PES spectra neglected the possible role of these states. Their singlet analogs may influence the d 2\Pi_g REMPI spectra as well. In Fig. 4 we show the relevant potential energy curves, and discuss qualitatively in the following section the role of these states in the C 3\Pi_g and d 2\Pi_g (2 + 1) REMPI problems.

![Potential energy curves](image)

**FIG. 4.** Potential energy curves for the first ionic state, the H'\Pi_u (1\pi_u^+ 1\sigma_g 3\sigma_u^-) Rydberg state converging to the a 4\Pi_u ionic state (IP = 16.10 eV), and the J'\Pi_u and K'\Pi_u Rydberg states which converge to the A'\Pi_u ionic state (IP = 17.05 eV). The potentials for the H and J states are Morse curves constructed from constants given in Refs. 37 and 40. The K state (dashed curve) is shifted upward from the J state by 0.15 eV, as discussed in the text.

a. 3\Pi_g autoionizing states. For triplet states, Nishitani \textit{et al.}\textsuperscript{40} have unambiguously assigned the vibrational progression in the 900–1010 Å region as all belonging to a single H 23\Pi_g (1\pi_u^+ 1\pi_g 3\sigma_u^-) Rydberg state converging to the a 4\Pi_u ion. This state is energetically accessible in the \nu' = 1–3 levels of the C 3\Pi_g one-color REMPI studies. Due to the large displacement of the potential curves, Franck-Condon factors become appreciable mainly for higher vibrational levels of the X 2\Sigma_g^- ion. Calculated Franck-Condon factors between the H 3\Pi_g state and the X 2\Sigma_g^- ion are given in Table IV, which agree with the corresponding distributions plotted in Fig. 5 of Ref. 40. For one-color (2 + 1) REMPI via the \nu' = 1,2 levels of the C 3\Pi_g state, the total photon energy nearly coincides with the \nu = 2 (T_0 = 12.61 eV) and \nu = 5 (T_0 = 12.98 eV) levels of the H 3\Pi_u state, respectively. Qualitatively, as follows from the theoretical analysis of

<table>
<thead>
<tr>
<th>\nu'</th>
<th>0</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
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<td>\nu'</td>
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*Franck-Condon factors were obtained using a Morse potential with spectroscopic constants from Ref. 40 for the O\textsubscript{2+} 3\Pi_g state, and with the RKR potential of Ref. 29 for the O\textsubscript{2+} 2\Sigma_g^- state.
Smith and Mies, we would expect autoionization to be favored in the \( \Delta \nu > 0 \) transitions, i.e., the \( \nu^+ = 2 \) and 3 levels. These states could influence the vibrational distribution for the \( \nu = 3 \) level of the \( C^1\Pi_g \) state as well. Note that, although the Franck–Condon factors in Table IV are small, autoionization of the \( H^1\Pi_u \) state is prominent in single-photon ionization spectra leading to the \( X^2\Pi_g \) ion. 38, 34

The \( J^3\Pi_u \left( 1\pi_u^0 1\pi_u^0 3\sigma_g^0 \right) \) state, which is the first member of a Rydberg series converging to the \( A^2\Pi_u \) ion, lies 0.8 eV above the \( H^1\Pi_u \) state and is energetically accessible in the \( \nu = 3 \) REMPI spectra of the \( C^1\Pi_g \) state. The total photon energy for \( \nu = 3 \) (13.254 eV) lies slightly below the \( \nu = 1 \) level (\( T_o = 13.27 \) eV) of the \( J^3\Pi_u \) state. This level would preferentially autoionize into the \( \nu^+ = 3–5 \) levels of the ion, as qualitatively indicated by examining the \( \nu = 1 \) Franck–Condon distribution in Table IV, which should be nearly identical for the \( J^3\Pi_u \) and \( H^1\Pi_u \) states.

b. \( 1^3\Pi_u \) autoionizing states. Singlet Rydberg states with the \( 1\pi_u^0 1\pi_u^0 3\sigma_g^0 \) configuration, which have not yet been observed, are likely relevant to one-color REMPI of the \( d^1\Pi_g \) state. Such a singlet Rydberg state with the above configuration, which we denote \( K^1\Pi_u \), may be associated with the \( A^2\Pi_u \) ion core, i.e., the singlet analog of the \( J^3\Pi_u \) state (see Fig. 4). The predicted term value of \( T_o = 13.30 \) eV (derived below) makes this state energetically accessible for the \( \nu = 3 \) REMPI spectra of the \( d^1\Pi_g \) state (Fig. 3). In particular, the total photon energy for the \( \nu = 3 \) \( d^1\Pi_g \) state REMPI spectra (13.380 eV) nearly coincides with the \( \nu = 0 \) level of the \( K^1\Pi_u \) state. Therefore, from Table IV (which should remain essentially valid for the \( K^1\Pi_u \) state) we expect preferential autoionization into \( \nu^+ = 3–5 \) levels of the ion.

c. SCF calculations. To support the above qualitative discussion and previous assignments of the \( H \) and \( J^3\Pi_u \) states, 37, 40 we have performed single-configuration SCF calculations on the \( J, H \), and the \( K^1\Pi_u \) state of \( O_2 \). The open-shell wave functions for these states have the form

\[
\Psi(H^3\Pi_u) = \frac{1}{\sqrt{12}} \{ 3 |1\pi_u^+ 1\pi_u^+ 3\sigma_g^- 1\pi_u^- 1\pi_g^- | - |1\pi_u^+ 1\pi_u^- 3\sigma_g^- 1\pi_u^+ 1\pi_g^+ | \}
\]

\[
\Psi(J^3\Pi_u) = \frac{1}{\sqrt{6}} \{ 2 |1\pi_u^+ 1\pi_u^+ 1\pi_u^- 3\sigma_g^- 1\pi_g^+ 1\pi_g^- | - |1\pi_u^+ 1\pi_u^- 1\pi_u^- 3\sigma_g^- 1\pi_g^+ 1\pi_g^- | \}
\]

\[
\Psi(K^1\Pi_u) = \frac{1}{\sqrt{12}} \{ 2 |1\pi_u^+ 1\pi_u^- 1\pi_u^- 3\sigma_g^- 1\pi_g^+ 1\pi_g^- | - |1\pi_u^+ 1\pi_u^- 1\pi_u^- 3\sigma_g^- 1\pi_g^+ 1\pi_g^- | \}
\]

With a basis identical to that of the \( C^1\Pi_u \) and \( d^1\Pi_g \) state SCF calculations, we find total energies of \(-149.240 \pm 43\), \(-148.875 \pm 84\), and \(-148.870 \pm 34\) a.u., at \( R = 2.282 \) \( \alpha_0 \), respectively, for these states. For the \( H^1\Pi_u \) state, we calculate the \( 3\sigma_g^- \) orbital eigenvalue to be \(-3.52 \) eV. Using the experimental ionization potential of 16.10 eV, 37, 40 we calculate a term value and quantum defect of \( T_o = 12.58 \) eV and \( \delta = 1.034 \), which compare reasonably well with the experimental values of 12.35 eV and 1.095, respectively. The \( J^3\Pi_u \) and \( K^1\Pi_u \) states each consist of a mixture between three components, corresponding to the three parentages \( \Sigma^- \), \( \Delta \), and \( \Sigma^- \) associated with the \( 2\Pi_u \left( 1\pi_u^0 1\pi_g^0 \right) \) states of the ion core. 45, 46 Instead of solving a term secular problem, we invoke a simplification by initially calculating the \( J^3\Pi_u \) and \( K^1\Pi_u \) SCF states corresponding to pure \( \Sigma^- \)-parentage. The wave functions given in Eqs. (3b) and (3c) above assume this single parentage. We then calculated an empirically corrected term value for the \( J^3\Pi_u \) state by employing the \( 3\sigma_g^- \) orbital eigenvalue, \(-3.67 \) eV, and the observed \( A^2\Pi_u \) ionization potential, 17.05 eV. 37, 40 For the \( J^3\Pi_u \) state our calculation gives \( T_o = 13.38 \) eV and \( \delta = 1.075 \), compared to the experimental values of 13.15 eV and 1.133, respectively. Using the singlet–triplet splitting obtained by subtracting total \( J^3\Pi_u \) and \( K^1\Pi_u \) SCF energies (0.15 eV), and the experimental term value of the \( J^3\Pi_u \) state, the predicted term value of the \( K^1\Pi_u \) state is \( T_o = 13.30 \) eV, with a singlet quantum defect of \( \delta = 1.095 \).

The \( 1^3\Pi_u \) Rydberg states may be incorporated into ab initio photoionization calculations using the Smith–Mies–Fano 41–43 procedure or an appropriate MQDT treatment. However since the \( 1^3\Pi_u \) ionization channels contain the \( \sigma_g \) shape resonance, the associated non-Franck–Condon effect must be incorporated explicitly, as done here at the one-electron level for direct photoionization.

3. Initial-state perturbations

Another mechanism leading to non-Franck–Condon effects in vibrational distributions is perturbation of the initial Rydberg state by the valence–Rydberg interaction, i.e., an avoided crossing. The \( C^1\Pi_u \) and \( d^1\Pi_g \) Rydberg states of \( O_2 \) are intersected by \( 1^3\Pi_u \) and \( 1^1\Pi_u \) valence potential energy curves, which are derived from the electronic configuration \( 3\sigma_g^- 1\pi_u^0 \). Cartwright et al. 8 first postulated the weak electronic interaction leading to the interpretation of two crossing diabatic states near the minimum of the \( C^1\Pi_u \) Rydberg potential curve. For the \( d^1\Pi_g \) state, Van der Zande et al. 16 have recently deduced the coupling matrix element \( H_{0v} \) of 55 meV from their kinetic-energy-release spectra, and accounted for the decrease in rotational constant \( B_{\nu} \) going from \( \nu = 0 \)–3, and its return to that of the ion for \( \nu > 3 \). To estimate the effect of this perturbation on the \( d^1\Pi_g \) REMPI spectra, we calculated the \( \nu = 0 \)–3 vibrational wave functions for the lower adiabatic potential \( (\nu' = 1,4,8,12 \) for the double well 16) without nonadiabatic coupling, and directly incorporated them in the calculation of the vibrational.
branching ratios. Since a dipole transition between the $3\sigma_g^1\pi_g^-$ state and the $3\sigma_g^1 \rightarrow \kappa \pi_u^-$ continuum is very weak, and nonadiabatic corrections to the vibrational wave functions are small, we expect this procedure to be a good approximation. We found almost negligible changes in the branching ratios, due to the preservation of nodal structure of the vibrational wave functions in the inner region of the double-well potential curve. This further indicates that the (final-state) autoionization effects discussed above are likely dominant. For situations where there is a strong avoided crossing, e.g., the $B^3 \Sigma_g^+ \rightarrow E^3 \Sigma_u^-$ system of $O_3$, one must solve the coupled Schrödinger equations for a full treatment.

C. Photoelectron angular distributions

Figure 5 shows calculated vibrationally resolved photoelectron angular distributions for the $\nu' = 0$ and 1 levels of the $d^1 \Pi_g$ Rydberg state. In these figures we have plotted the angular distribution

$$\frac{d\sigma}{d\Omega} \propto 1 + \beta P_2(\cos \theta), \quad (4)$$

where $\beta$ is the asymmetry parameter for an unaligned molecular target, $\theta$ is the angle between the direction of the light polarization and the photoelectron momentum, and $P_2$ is a Legendre polynomial. The numerical values of the $\beta$ parameters and those for other $\nu'$ levels are given in Table V. No experimental values are available for the $d^1 \Pi_g$ state, although a comparison between theory and experimental results for the $C^3 \Pi_g$ state has been made, with satisfying results. Note that we have neglected any effects due to state alignment arising from the two-photon excitation. This will be of interest in future experimental studies of specific rotational branches.

The difference between $\Delta \nu = 0$ and $\Delta \nu \neq 0$ distributions is very large, due to the non-Franck–Condon effect associated with the $\sigma_g$ resonance. This is similar to that discussed for the $C^3 \Pi_g$ state. However, there is also considerable difference between the $\Delta \nu \neq 0$ angular distributions for the singlet state compared to the triplet. For example, for the $\nu' = 1 \rightarrow \nu^+ = 2$ transition, the calculated $d^1 \Pi_g$ state is 0.55, and $\beta = -0.027$ for the singlet (Table V), at nearly the same total photon energy of ~12.5 eV.

It would be interesting to experimentally measure these photoelectron angular distributions to confirm this large multiplet-specific effect, which is not too apparent when comparing the singlet and triplet branching ratios. Additionally, it would be useful to measure changes in the higher-order terms in the REMPI angular distributions and compare them with their triplet counterparts so as to ascertain the role of spin coupling in the alignment induced by the two-photon absorption step.

D. Energy-dependent branching ratios and angular distributions

$(2 + 1')$ two-color REMPI studies of the $d^1 \Pi_g$ state may provide useful insight into the role of autoionization on these ion vibrational distributions. To illustrate what the present one-electron theory predicts for the energy dependence of such distributions, Fig. 6 shows calculated vibrationally resolved branching ratios and photoelectron angular distributions for photoionization of the $\nu' = 3$ level over a range of photon energies. For the branching ratios, all curves begin at 4.32 eV photon energy above the $\nu' = 3$ level of the $d^1 \Pi_g$ state and the $\nu^+ = 0\rightarrow 5$ channels are hence energeti-

![FIG. 5. Calculated photoelectron angular distributions for the $\nu' = 0$ and 1 levels of the $O_3$ $d^1 \Pi_g$ state. Solid curve: length form; dash curve: velocity form. In this figure $\theta = 0$ is vertical.](image-url)
The non-Franck–Condon effects induced by the $\sigma_v$ shape resonance accounts for some of the observed deviations from the expected $\Delta \nu = 0$ propensity rule for ionization of molecular Rydberg states. However, the vibrational branching ratios calculated with the Hartree–Fock model, which include the effects of the shape resonance, differ significantly from the observed values. There are no measurements of the photoelectron angular distributions for the $d$ $^{1} \Pi_u$ state. It would be interesting to compare these photoelectron angular distributions with those for the $C$ $^{1} \Pi_u$ state, since the present calculations predict significant differences due to the particular spin couplings in the resonant intermediate and final states.

In the present $d$ $^{1} \Pi_u$ REMPI problem, multichannel interactions involving both repulsive and Rydberg autoionizing states likely result in the major departures from the simple Franck–Condon prediction. We have tentatively identified these interactions as arising from autoionization of singlet valence states derived from the $1 \pi_u^0 1 \pi_u^1$ electronic configuration, analogous to earlier assessments for the $C^{1} \Pi_u$ state. Evidence has also been presented which indicates that Rydberg states which converge to the $a$ $^{2} \Pi_u$ and $A$ $^{2} \Pi_u$ ion states may be responsible for a portion of the observed $\Delta \nu \neq 0$ intensity, in both $C^{3} \Pi_u$ and $d$ $^{3} \Pi_u$ state REMPI spectra. Since the singlet states associated with the $A$ $^{2} \Pi_u$ ion core have not been observed, it may be of interest to probe them directly by inducing single-photon transitions from, e.g., the $O_2$ $X^{1} \Sigma_g^+$ or $I \Delta_g$ states, or by charge-exchange translational spectroscopy.

**ACKNOWLEDGMENTS**

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**IV. CONCLUSION**

We have presented ionic vibrational branching ratios and vibrationally resolved photoelectron angular distributions for photoionization of the $d$ $^{1} \Pi_u$ Rydberg state of $O_2$. The non-Franck–Condon effects induced by the $\sigma_v$ shape resonance accounts for some of the observed deviations from the expected $\Delta \nu = 0$ propensity rule for ionization of molecular Rydberg states. However, the vibrational branching ratios calculated with the Hartree–Fock model, which include the effects of the shape resonance, differ significantly from the observed values. There are no measurements of the photoelectron angular distributions for the $d$ $^{1} \Pi_u$ state. It would be interesting to compare these photoelectron angular distributions with those for the $C$ $^{1} \Pi_u$ state, since the present calculations predict significant differences due to the particular spin couplings in the resonant intermediate and final states.

In the present $d$ $^{1} \Pi_u$ REMPI problem, multichannel interactions involving both repulsive and Rydberg autoionizing states likely result in the major departures from the simple Franck–Condon prediction. We have tentatively identified these interactions as arising from autoionization of singlet valence states derived from the $1 \pi_u^0 1 \pi_u^1$ electronic configuration, analogous to earlier assessments for the $C$ $^{1} \Pi_u$ state. Evidence has also been presented which indicates that Rydberg states which converge to the $a$ $^{2} \Pi_u$ and $A$ $^{2} \Pi_u$ ion states may be responsible for a portion of the observed $\Delta \nu \neq 0$ intensity, in both $C$ $^{3} \Pi_u$ and $d$ $^{3} \Pi_u$ state REMPI spectra. Since the singlet states associated with the $A$ $^{2} \Pi_u$ ion core have not been observed, it may be of interest to probe them directly by inducing single-photon transitions from, e.g., the $O_2$ $X^{1} \Sigma_g^+$ or $I \Delta_g$ states, or by charge-exchange translational spectroscopy.

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