Diversity in extinction laws of Type Ia supernovae measured between 0.2 and 2 μm

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ABSTRACT
We present ultraviolet (UV) observations of six nearby Type Ia supernovae (SNe Ia) obtained with the Hubble Space Telescope, three of which were also observed in the near-IR (NIR) with Wide-Field Camera 3. UV observations with the Swift satellite, as well as ground-based optical and NIR data provide complementary information. The combined data set covers the wavelength range 0.2–2 μm. By also including archival data of SN 2014J, we analyse a sample spanning observed colour excesses up to $E(B-V) = 1.4$ mag. We study the wavelength-dependent extinction of each individual SN and find a diversity of reddening laws when characterized by the total-to-selective extinction $RV$. In particular, we note that for the two SNe with $E(B-V) \gtrsim 1$ mag, for which the colour excess is dominated by dust extinction, we find $RV = 1.4 \pm 0.1$ and $RV = 2.8 \pm 0.1$. Adding UV photometry reduces the uncertainty of fitted $RV$ by ~50 per cent allowing us to also measure $RV$ of individual low-extinction objects which point to a similar diversity, currently not accounted for in the analyses when SNe Ia are used for studying the expansion history of the Universe.


1 INTRODUCTION
Studies of the cosmological expansion history using Type Ia supernovae (SNe Ia) have greatly improved our understanding of the Universe. While pioneering work lead to the discovery of the accelerated expansion from a few dozen SNe Ia (Riess et al. 1998; Perlmutter et al. 1999), the present samples of several hundred SNe Ia out to $z \sim 1.5$ show to high-precision that Einstein’s Cosmological Constant provides an excellent fit for this phenomenon (e.g. Amanullah et al. 2010; Conley et al. 2011; Sullivan et al. 2011; Suzuki et al. 2012; Betoule et al. 2014). These findings have been possible due to the great accuracy of SNe Ia as distance indicators when observed in two or more broadband filters over several weeks, starting before light curve peak (see Goobar & Leibundgut 2011, for a recent review). The distance to each individual supernovae (SN) is obtained by fitting an SN Ia template to the photometric data (see e.g. Riess, Press & Kirshner 1996; Nugent, Kim & Perlmutter 2002; Guy et al. 2007a; Jha, Riess, & Kirshner 2007; Conley et al. 2008; Burns et al. 2011, and references therein) in order to obtain the brightness and colour at maximum together with the light-curve shape. The fitted properties are then typically combined using empirical linear relations to form a distance-dependent quantity (Phillips 1993; Tripp 1998).

The colour correction is based on the observation that red SNe are fainter than bluer ones, which could originate from a combination of an intrinsic SN Ia colour law, and extinction by dust in the host galaxy. The colour-brightness relation is commonly determined by minimizing the scatter around the best-fitting cosmological model,
but there is no a priori reason why the two effects should follow the same colour–luminosity relation, nor can it be expected that host galaxy dust should have the same properties in different SN environments. In fact, even in the Milky Way, a range of extinction properties have been observed for different lines of sight.

When SNe Ia are used to measure distances, these uncertainties are handled by introducing a systematic error on the colour–luminosity relation, which makes an important contribution to the error budget when propagated to the derived cosmological parameters. Addressing the colour–brightness relation, and in particular breaking the degeneracy between the intrinsic colour component and dust extinction, is important for future SN Ia surveys to improve beyond the current cosmological constraints.

The properties and wavelength-dependent extinction of dust in the Milky Way has been carefully studied and is commonly characterized by the total, $A_V$, to selective, $E(B - V) = A_B - A_V$, extinction ratio as $R_V = A_V/(A_B - A_V)$. Lower values of $R_V$ correspond to steeper extinction laws, since, for a given total extinction, $A_V$, these imply a larger reddening, $E(B - V)$.

The reddening of SNe Ia can be studied by comparing observed colours between reddened and similar un-reddened objects. Several such studies of individual SNe Ia (e.g. Elias-Rosa et al. 2006, 2008; Krisciunas et al. 2007; Folatelli et al. 2010; Amanullah et al. 2014, from hereon A14) in nearby galaxies, point to significantly lower values of $R_V$ than has been observed in the Milky Way. Since the reddening of several of these SNe Ia is significantly higher than what can be expected from the Milky Way extinction along the line of sight, the observed colour excesses are likely dominated by extinction in the SN host galaxies. For low-reddening SNe this may not be the case, but it is by nature difficult to measure $R_V$ to high precision for individual SNe Ia with low $E(B - V)$. However, the global reddening law for a sample of SNe Ia can be measured, and several studies have obtained low-$R_V$ values (e.g. Astier et al. 2006; Nobili & Goobar 2008; Burns et al. 2014, from hereon B14) using this approach.

Chotard et al. (2011) and Scolnic et al. (2014) noted that globally derived reddening laws will be biased if the intrinsic SN Ia colour dispersions are not accounted for correctly, and Chotard et al. (2011) find $R_V = 2.8 \pm 0.3$, consistent with the Milky Way average, for their sample of 76 SNe Ia of which 73 had $E(B - V) < 0.3$ mag. B14 also obtain $R_V \approx 3$ when they constrain their analysis to only include low-extinction SNe Ia, while highly reddened objects appear to prefer lower values ($R_V \approx 1.7$) which is in agreement with previous studies (Folatelli et al. 2010). This suggests that a single, global, reddening law derived from a set of SNe Ia could depend on the colour distribution of the sample.

The degeneracy between intrinsic SNe Ia colour variations and dust extinction, can also be approached by studying the relation between SN colours and spectroscopic properties. Wang et al. (2009) found $R_V = 1.6$ for SNe Ia with ‘high’ photospheric velocities (HV, $>11800$ km s$^{-1}$) within 5 d of maximum, while they obtained $R_V = 2.4$ for objects with ‘normal’ velocity (NV, $<11800$ km s$^{-1}$). The expansion velocities were quantified by measuring the velocity of the Si II 6355 Å absorption feature. Foley & Kasen (2011) confirmed their findings but also conclude that when SNe with $E(B - V) > 0.35$ mag are omitted, they obtain $R_V \approx 2.5$ for the two separate subsamples, which also have different intrinsic colours. In other words, these findings also suggest that low-$R_V$ values are primarily associated with high-extinction, and these could dominate when a single global reddening law is derived from a sample of SNe Ia.

One natural explanation for low-$R_V$ values arises if SNe Ia are surrounded by circumstellar (CS) dust (Wang 2005; Goobar 2008). In this scenario, photons can scatter back into the line of sight which reduces the total extinction. Photons that scatter on the CS dust will also arrive later than photons that do not interact which will give rise to time-dependent reddening (Wang 2005; Amanullah & Goobar 2011; Brown et al. 2015). An observation will be a superposition of the SN spectrum at the given epoch and SN light from earlier epochs, but the scattering cross-section is wavelength-dependent so the fraction of delayed photons will also vary with wavelength. Further, depending on the geometry, scattered photons could give rise to a plateau for the late-time tail of the light curve and indications of such tails have been observed in $B - V$ (Fürster et al. 2013).

CS dust could also be heated by the SN, where the temperature will depend on the dust properties and the distance from the explosion. Heated dust has been detected in mid- to far-infrared for a subset of peculiar SNe Ia (Fox et al. 2011; Taddei et al. 2012; Fox & Filippenko 2013; Silverman et al. 2013a), but Herschel and Spitzer observations (Johansson, Amanullah & Goobar 2013; Johansson et al. 2014) of a handful of normal SNe Ia show no signs of heated CS dust (see also Maeda, Nozawa & Motohara 2014, for limits from near-IR observations). For two of these SNe, 2006X and 2007le, together with SNe 1999cl and the SN 2002ic-like PTF11kx, time-varying Na I D absorption features have been observed in their spectra on time-scales comparable to the SN lifetime which is consistent with the presence for CS material (Patat et al. 2007; Blondin et al. 2009; Simon et al. 2009; Dilday et al. 2012). Absorption from Na I has been used as a proxy for dust extinction (see e.g. Poznanski, Prochaska & Bloom 2012), although high-resolution spectra are required (Poznanski et al. 2011) and its validity for extinction along lines-of-sight of SNe Ia has been challenged (Phillips et al. 2013). Time-varying Na I D can be explained by photo-ionization of neutral sodium (e.g. Borkowski, Blondin & Reynolds 2009) and subsequent recombination by the SN. In a recent study by Soker (2014) this explanation has been questioned and an alternative model of photon-induced desorption of sodium from dust in planetary nebulae remnants was proposed. It has also been suggested that time-variations may originate from patchy interstellar material along the line of sight (Patat et al. 2010). More recently, Graham et al. (2015b) claimed a detection of a time-varying K I absorption feature in 2014J, while the corresponding Na I D feature remained unchanged, which they argue is consistent with the presence of CS material at a radius of $r_{min} \sim 10^{19}$ cm due to the different ionization cross-sections.

An extensive study with multi-epoch high-resolution spectra of 14 SNe (Sternberg et al. 2014) have failed to reveal further examples of time varying Na I D. Nevertheless, a statistically significant preponderance of Na I D features which are blue shifted with respect to the local velocity have been observed in high- and mid-resolution spectra (Sternberg et al. 2011; Maguire et al. 2013, respectively), suggesting that there is outflowing material from the SN progenitor system.

In this work, we seek to expand our knowledge of extragalactic extinction in the line of sight and SN Ia reddening by making the widest wavelength study of a sample of SNe Ia to date. We present UV-to-NIR light curves for six SNe Ia based on data mainly obtained from The Nordic Optical Telescope (NOT) and the Hubble Space Telescope (HST). The observations and data reduction is presented in Section 2 while the light curves and colours are presented in Section 3. The method for deriving individual reddening laws for each SN is described in Section 4, and after adding SN 2014J from A14 to the sample we present the results in Section 4.3. We search for CS dust in Section 5 and all the
Table 1. SN coordinates are quoted from the discovery telegrams. All host galaxy data were obtained from the Nasa Extragalactic Database (NED), unless otherwise specified, where $v_h$ is the measured recession velocity, and the Milky Way extinctions are from the Schlafly & Finkbeiner (2011) calibration of the Schlegel, Finkbeiner & Davis (1998) infrared-based dust maps. The projected distances from the host galaxy nuclei, $r_\perp$, were calculated based on the host galaxy distances and the SN offsets specified in Appendix A.

<table>
<thead>
<tr>
<th>SN</th>
<th>$\alpha_{SN}$</th>
<th>$\delta_{SN}$</th>
<th>$r_\perp$ (kpc)</th>
<th>Host galaxy</th>
<th>$\alpha_h$</th>
<th>$\delta_h$</th>
<th>$v_h$ (km s$^{-1}$)</th>
<th>Distance (Mpc)</th>
<th>MW $A_V$ (mag)</th>
</tr>
</thead>
<tbody>
<tr>
<td>2012bl</td>
<td>20:23:55.28</td>
<td>-48:21:17.3</td>
<td>15.6(0.2)</td>
<td>ESO 234-19</td>
<td>20:23:51.0</td>
<td>-48:21:32</td>
<td>5608</td>
<td>71(1)$^a$</td>
<td>0.098</td>
</tr>
<tr>
<td>2012bm</td>
<td>13:05:45.66</td>
<td>+46:27:52.9</td>
<td>7.5(0.3)</td>
<td>UGC 8189</td>
<td>13:05:46.6</td>
<td>+46:27:42</td>
<td>7436</td>
<td>103(8)$^b$</td>
<td>0.033</td>
</tr>
<tr>
<td>2012cg</td>
<td>12:27:12.83</td>
<td>+09:25:13.2</td>
<td>1.3(0.2)</td>
<td>NGC 4424</td>
<td>12:27:11.6</td>
<td>+09:25:14</td>
<td>437</td>
<td>15(2)$^c$</td>
<td>0.057</td>
</tr>
<tr>
<td>2012cp</td>
<td>13:47:01.79</td>
<td>+33:53:35.0</td>
<td>1.9(0.1)</td>
<td>UGC 8713</td>
<td>13:47:01.2</td>
<td>+33:53:37</td>
<td>4956</td>
<td>57(3)$^d$</td>
<td>0.058</td>
</tr>
<tr>
<td>2012cu</td>
<td>12:53:29.35</td>
<td>+02:09:39.0</td>
<td>5.4(1.2)</td>
<td>NGC 4772</td>
<td>12:53:29.1</td>
<td>+02:10:06</td>
<td>1040</td>
<td>41(9)$^e$</td>
<td>0.074</td>
</tr>
<tr>
<td>2012et</td>
<td>23:42:38.82</td>
<td>+27:05:31.5</td>
<td>2.7(0.2)</td>
<td>MCG +04-55-47</td>
<td>23:42:38.4</td>
<td>+27:05:31</td>
<td>7483</td>
<td>105(7)$^f$</td>
<td>0.221</td>
</tr>
<tr>
<td>2014J</td>
<td>09:55:42.11</td>
<td>+69:40:25.9</td>
<td>1.0(0.3)</td>
<td>M82</td>
<td>09:55:52.7</td>
<td>+69:40:46</td>
<td>203</td>
<td>3.5(0.3)$^g$</td>
<td>0.189$^g$</td>
</tr>
</tbody>
</table>

Notes: $^a$Parnovsky & Parnowski (2010); $^b$Calculated based on the redshift with $H_0 = 73 \pm 5$ km s$^{-1}$/Mpc; $^c$Cortés, Kenney & Hardy (2008); $^d$Springob et al. (2009); $^e$Tully et al. (2009); $^f$Dalcanton et al. (2009).

Figure 1. The seven SNe analysed in this work. The patches for SNe 2012bm, 2012cg, 2012cp, 2012cu and 2012et were obtained from BVR images from NOT, while the images for SNe 2012bl and 2014J are obtained from the Swope telescope and HST/WFC3 (Program DD-13621; PI Goobar) images, respectively.

results are discussed in Section 6. We conclude and summarize in Section 7.

All seven SNe$^1$ are listed in Table 1 and shown together with their host galaxies in Fig. 1. They are also briefly summarized in Appendix A.

2 OBSERVATIONS AND DATA REDUCTION

2.1 Hubble Space Telescope

All previously unpublished HST observations discussed in this work are listed in Table 2. Each SN was observed at two different epochs (four for SN 2012et) with the Wide-Field Camera 3 (WFC3) during the HST Cycle 19 under programme GO-12582 (PI: Goobar). All SNe were imaged with the WFC3/UVIS channel through the passbands $F225W$, $F275W$ and $F336W$. In addition to this, NIR imaging in the HST passbands $F125W$ and $F160W$ was obtained for the SNe 2012cg, 2012cu and 2012et with the WFC3/IR channel. Examples of both the WFC3/UVIS and WFC3/IR observations are shown in Fig. 2.

WFC3/UVIS consists of two $4096 \times 2051$ e2V CCD detectors with a plate scale of 0.04 arcsec pixel$^{-1}$, while the Teledyne HgCdTe infrared detector used in the WFC3/IR channel has a pixel scale of 0.13"/pixel. For each observation, only the sub-arrays (apertures), listed in Table 2, of the detectors were read-out. All WFC3 data were reduced using the standard STScI reduction pipeline and calibrated using CALWF3.

The WFC3/UVIS CCDs, like all HST CCDs, are plagued with charge transfer inefficiencies (CTI), i.e. degradations of the detector.
with the UVIS2-M1K1C-SUB sub-array. For this aperture, we in-

mic rays. The CTI can be reverse corrected at the pixel level using

performance over time due to damage in the silicon lattice from cos-

2010). The patch sizes are 10 arcsec \times 10 arcsec and in the upper row the first

epochs obtained through the F275W filter is shown for each of the three

SNe 2012bl, 2012bm and 2012cp. In the two lower rows, the corresponding

patches are shown for the SNe 2012cg, 2012cu and 2012et, together with

the NIR observations in the F160W filter that also were obtained for these

objects. The marked (red) region in the lower right panel show the isophot

from which the host galaxy background of SN 2012et was estimated as

explained in the text.

zero-points$^3$ for WFC3. Since there were no bright stars present

in the fields, we used the general enclosed energy tables provided

by STScI for this purpose. To account for the time and wavelength

dependence of the WFC3/UVIS aperture corrections, we adopt an

additional uncertainty of 0.05 mag for all measurements using the

4 pixel radius, which was derived by comparing the enclosed en-

ergy tables with photometry from different aperture radii of the high

signal-to-noise data.

Only the SN 2012et NIR measurements suffered from host galaxy

contamination. The host contribution was estimated by placing aper-

tures of the same radius used for the SN photometry along the

isophot of the galaxy that intersects with the position of SN 2012et

as illustrated in the lower right panel of Fig. 2. The background was

then estimated as the median of these measurements, and the root-

mean-square (RMS) of the measurements was added in quadrature

to the photometric uncertainty. All the WFC3 photometry is pres-

ented in Table 3 and shown in Fig. 3. Here, we also present updated

photometry of SN 2014J using the method described here which is

consistent with the results presented in A14.

For most HST visits, we also obtained long-slit spectroscopy with

the Space Telescope Imaging Spectrograph (STIS) where the

G230LB grating covering the wavelength range 1600–3100 Å, and for two

SNe (2012cg, 2012et) G430L, 2900–5700 Å. The data were reduced using

the calstis pipeline which is part of the STSDas package. The

pipeline was run for all the spectra up to the point where the

calibrated 2D spectra were created. Only the spectra of SN 2012cg

and the red G430L spectrum of SN 2012et contained any significant


\begin{table}
\centering
\caption{Wide-Field Camera-3 and STIS observations together with the used apertures, where UVIS1 and UVIS2 are the two chips of the WFC3/UVIS channel. The observations with the WFC3/IR and WFC3/UVIS channels were obtained through the F125W, F160W and F225W, F275W, F336W broad-band passbands, respectively.} 
\begin{tabular}{cccc}
\hline
Civil date & MJD & Aperture & SN \\
\hline
2012-04-09 & 56026.4 & UVIS1-2K2A-SUB & 2012bl \\
2012-04-09 & 56026.5 & STIS 52X0.2 G230L & 2012bm \\
2012-04-13 & 56030.6 & UVIS1-2K2A-SUB & 2012bm \\
2012-04-13 & 56030.7 & STIS 52X0.2 G230L & 2012bm \\
2012-04-16 & 56033.1 & STIS 52X0.2 G230L & 2012bl \\
2012-04-16 & 56038.2 & UVIS1-2K2A-SUB & 2012bl \\
2012-04-20 & 56037.4 & STIS 52X0.2 G230L & 2012bl \\
2012-04-21 & 56038.2 & UVIS1-2K2A-SUB & 2012bl \\
2012-06-04 & 56082.4 & UVIS2-M1K1C-SUB & 2012cg \\
2012-06-04 & 56082.4 & IRSUB64 & 2012cg \\
2012-06-04 & 56082.5 & STIS 52X0.2 G230L & 2012cg \\
2012-06-18 & 56096.4 & STIS 52X0.2 G230L & 2012cg \\
2012-06-18 & 56096.4 & STIS 52X0.1 G430L & 2012cg \\
2012-06-19 & 56097.5 & UVIS2-M1K1C-SUB & 2012cg \\
2012-06-19 & 56097.5 & IRSUB64 & 2012cg \\
2012-06-04 & 56082.6 & UVIS1-2K2A-SUB & 2012cp \\
2012-06-04 & 56082.7 & STIS 52X0.2 G230L & 2012cp \\
2012-06-16 & 56094.6 & UVIS1-2K2A-SUB & 2012cp \\
2012-06-17 & 56095.6 & STIS 52X0.2 G230L & 2012cp \\
2012-07-02 & 56110.8 & UVIS2-M1K1C-SUB & 2012cu \\
2012-07-02 & 56110.8 & IRSUB512 & 2012cu \\
2012-07-07 & 56115.8 & UVIS2-M1K1C-SUB & 2012cu \\
2012-07-07 & 56115.8 & IRSUB512 & 2012cu \\
2012-10-01 & 56201.5 & UVIS2-M1K1C-SUB & 2012et \\
2012-10-01 & 56201.5 & IR & 2012et \\
2012-10-01 & 56201.8 & STIS 52X0.2 G230L & 2012et \\
2012-10-01 & 56201.8 & STIS 52X0.2 G430L & 2012et \\
2012-10-05 & 56205.6 & UVIS2-M1K1C-SUB & 2012et \\
2012-10-05 & 56205.6 & IR & 2012et \\
2012-10-09 & 56209.8 & UVIS2-M1K1C-SUB & 2012et \\
2012-10-09 & 56209.8 & IR & 2012et \\
2012-10-13 & 56213.9 & UVIS2-M1K1C-SUB & 2012et \\
2012-10-13 & 56213.9 & IR & 2012et \\
\hline
\end{tabular}
\end{table}

\footnote{2 http://www.stsci.edu/hst/wfc3/tools/cte_tools}

\footnote{3 We used the zero-points from 2012 March 06.}
Table 3. The photometry of all SNe. All magnitudes are in the natural Vega system. The rest-frame magnitude and colour can be obtained from Columns 4 to 6 using equation (1). Columns 5 and 9 are the Galactic extinctions and Columns 6 and 10 are $K_X$ and $K_V$ corrections for the two bands, respectively. All corrections were calculated after the SN 2011fe template had been reddened with the best fitted F99 law, shown in Table 5, for each SN. The $V$ magnitude is only shown for data points used in the colour analysis, i.e. with phases between $-10$ and $+35$ d. Column 2 show the effective light-curve-width-corrected phase, while Column 7 specifies whether the $V$ magnitude was measured for the same epoch (D) or if it was calculated using the SNOOPY model (M).

The corresponding intrinsic colour for the SN 2011fe template is shown when available in Column 11. The Swift magnitudes of SN 2014J are from Brown et al. (2015). (This table is available in its entirety in a machine-readable form in the online journal. A portion is shown here for guidance regarding its form and content.)

MJD Phase $X$ $A^{MW}_X$ $K_X$ Match $V$ $A^{MW}_V$ $K_V$ $(V - X)_0$
---
56082.4 0.2 WFC3 F336W 11.74(0.06) 0.09 0.01 M 12.04(0.04) 0.06 0.00 0.61
56097.5 14.0 WFC3 F336W 13.75(0.01) 0.09 0.02 M 12.53(0.07) 0.06 0.00 $-0.90$
56082.4 0.2 WFC3 F125W 12.37(0.01) 0.01 0.05 M 12.53(0.04) 0.06 0.00 $-0.55$
56097.5 14.1 WFC3 F125W 13.88(0.03) 0.02 $-0.07$ M 12.53(0.07) 0.06 0.00 $-1.91$
56082.4 0.2 WFC3 F225W 16.38(0.05) 0.13 0.02 M 12.53(0.04) 0.06 0.00 $-2.55$
56097.5 14.0 WFC3 F225W 17.60(0.08) 0.13 0.02 M 12.53(0.07) 0.06 0.00 $-0.68$
56082.4 0.2 WFC3 F160W 12.67(0.03) 0.01 0.01 M 12.53(0.04) 0.06 0.00 $-0.88$
56097.5 14.1 WFC3 F160W 13.24(0.03) 0.01 0.55 M 12.53(0.07) 0.06 0.00 $-0.69$

Figure 3. Observed light curves for the SN sample. Our analysis is based on optical $UBVRI$ and NIR $JHK$ photometry from ground-based observatories (circles), UV ($F_{225W}, F_{275W}, F_{336W}$) and NIR ($F_{125W}, F_{160W}$) photometry from the HST (squares). For the SNe 2012bl and 2012cg we also use Swift/UVOT photometry (triangles). The data are shown in their instrumental system but have been shifted using the distance moduli based on the distances in Table 1 and offset for clarity. The thick, solid, lines show the SNOOPY $V$-models used to calculate colours as described in the text, while the dashed lines show synthesized light curves of SN 2011fe to guide the eye. When an SN has observations in a similar filter from multiple instruments only one of the light curves is shown. The epoch is the observed date with respect to the fitted day of maximum in the $B$ band from Table 5.
signal and were extracted using the calstis xid routine with a 4 pixel aperture.

2.2 Swift/UVOT

UV photometry was also obtained with the Ultra-Violet/Optical Telescope (UVOT; Roming et al. 2005) on the Swift spacecraft (Gehrels et al. 2004) for the SNe 2012bl, 2012cg, 2012cp and 2012cu in the \( uvw_1 \), \( uvw_2 \) and \( uvw_3 \) filters. However, the \( uvw_1 \) and \( uvw_2 \) filters are not well suited for extinction studies due to the significant ‘red-tails’ of these filters. Milne et al. (2010) used the UV spectra of SN 1992A (Kirshner et al. 1993) and estimated that 52 per cent and 44 per cent of the light in \( uvw_1 \) and \( uvw_2 \), respectively, originate from wavelengths redder than 3000 Å. Brown et al. (2015) show how the observed photons and the corresponding effective wavelengths shift dramatically as reddening increases.

The \( uvw_2 \) filter, on the other hand, is much better constrained (1 per cent of the light comes from >3000 Å) and is used for the extinction studies in this work. The \( uvw_2 \) magnitudes were measured using the pipeline from the Swift Optical/Uninovieto Supernova Archive (SOUA; Brown et al. 2014), including correction for the time-dependent sensitivity and revised zero-points from Breeveld et al. (2011). The result is presented in Table 3 and shown in Fig. 3. Only the SNe 2012bl and 2012cg showed a significant SN flux in the \( uvw_2 \) band after subtraction of the underlying host galaxy flux. The flux measured for SN 2012cp was consistent with the host galaxy brightness and no signal was measured for SN 2012cu.

2.3 Ground-based observations

The ground-based spectroscopic observations are listed in Table 4 while the photometric observations are summarized together with the measured magnitudes in Table 3 and shown in Fig. 3. All SNe except for SN 2012bl were observed with the 2.56 metre NOT under programmes 45-009 and 46-018 (PI: Amanullah). Imaging and spectroscopy was obtained with the 6.4 arcmin × 6.4 arcmin Andalusia Faint Object Spectrograph and Camera (ALFOSC) using the filter set \( U \) (#7), \( B \) (#74), \( V \) (#75), \( R \) (#76), \( i \) (#12) and the \( R = 360 \) grism (#4). The data were reduced using standard IRAF routines and the QUBA pipeline (Valenti et al. 2011). The photometry was measured by first fitting the point spread function (PSF) using DAOPHOT (Stetson 1987) to stars in the fields. The calibrated magnitudes were obtained either from Landolt fields (Landolt 1992) observed during the night, or, when these were not available, by comparing the fluxes to stars in the fields that were then calibrated against Landolt fields for the photometric nights.

With the NOT, we also obtained high-resolution spectroscopy of SN 2012cg using the Fibre-fed Echelle Spectrograph (FIES; Telting et al. 2014) in its high-resolution mode, \( R = 67000 \). Simultaneous wavelength reference (Thorium-Argon) spectra were obtained and the data were reduced using the software FITSFORM which is provided by the observatory.

NIR observations were carried out for SNe 2012bm, 2012cg and 2012cp with the 4 arcmin × 4 arcmin NOTCam instrument in the \( J \), \( H \) and \( K_s \) bands under the programmes 45-007 (PI: Kankare) and 46-020 (PI: Mattila). We used the wide field imaging option of the 4 arcmin \( \times \) 4 arcmin HgCdTe NOTCam detector with a plate scale of 0.234 arcsec pixel\(^{-1}\). The observations were carried out using either 5 or 9-point dithering patterns. For the SNe with extended host galaxies, beam-switching was used to guarantee a successful sky subtraction. We used the NOTCam Quick-Look reduction package based on IRAF. Bad pixels (which includes two dead columns) were
masked and we used master differential skyflats which were obtained from bright and faint skyflats. Further, the images were corrected for geometric distortions\(^6\) before the individual images were aligned and co-added.

SN 2012cg was also observed in \(JHK_s\) with the 4.3 arcmin \(\times\) 4.3 arcmin CAIN instrument on the 1.52 metre Carlos Sanchez Telescope at Observatorio del Teide on Tenerife. CAIN III is a 256 \(\times\) 256 pixel HgCdTe NIR detector, where we used the wide field option with a plate scale of 1.0 arcsec pixel\(^{-1}\). The data were reduced using a dedicated IRAF package provided by J. Pullido and A. Barrena.

The two SNe 2012bm and 2012cp were also observed by the Palomar Transient Factory with the Palomar 48-inch telescope (Rau et al. 2009) in the Mould \(R\). We use their photometry which was obtained by first determining the PSF prior to subtractions, and then carrying out PSF photometry on the subtracted frames (Firth et al. 2015). The calibration of this data has been described in Ofek et al. (2012).

Photometric follow-up of SN 2012bl was carried out by the Carnegie Supernova Project using the Swope telescope for the optical and the du Pont telescope for the NIR. The reduction and photometry have been described in detail in Hamuy et al. (2006) and Contreras et al. (2010). PSF photometry was performed with respect to a local sequence of standard stars calibrated to the Landolt (1992) and Smith et al. (2002) standard fields for the optical observations and the Persson et al. (1998) for the NIR.

Further, we here also present spectroscopic observations of SNe 2011fe, 2012cg and 2014J obtained using the Intermediate dispersion Spectrograph and Imaging System (ISIS) instrument at the William Herschel Telescope, the Low Resolution Imaging Spectrometer (LRIS) instrument at Keck and the Dual Imaging Spectrograph (DIS) instrument at the Apache Point Observatory. These data were reduced in a standard manner.

### 3 SN SPECTRA AND COLOURS

The spectra for the seven SNe around maximum are shown in Fig. 4, where we also added the classification spectrum of SNe 2012bm and 2012et (Tomasella et al. 2014) to the set of spectroscopic observations already described above. For SN 2012cg, both the \(HST/STIS\) G250LB and G430L spectra, and the ALFOSC spectrum, that was obtained the same day, are shown. We used SNID (Blondin & Tonry 2007) to type the spectra and all SNe could be classified as ‘normal’, although SN 2012et also provided acceptable matches to the normal SN 2011fe for the matching epoch (Mazzali et al. 2014) for comparison.

All photometric data are shown in Fig. 3 and for each measurement in each filter, \(X\), where \(X \in \{uvm2, F225W, \ldots, K_s\}\), we calculated the colour \(X - V\). When \(X\) and \(V\)-band measurements are not available for the same dates, and the colour could not be obtained directly, a \(V\)-band model was used to calculate the colours. When applicable, we used a smoothed spline model but for the SNe 2012bm and 2012cp the \(V\)-band data were too sparsely sampled to allow reliable spline fits. For these objects we instead fitted the SN Ia template from Hsiao et al. (2007, H07 from hereon) to the observed data. Both the spline and template-based models were obtained using the SNOOPY light-curve fitter (Burns et al. 2011) and are shown as thick lines in Fig. 3. Further, for all model-based colours we add 0.05 mag in quadrature to uncertainties in order to account for the inaccuracy of the models.

All colours were corrected for Galactic extinction, \(A_{MW}\), using the extinction law by Cardelli, Clayton & Mathis (1989, CCM from hereon) with \(R_V = 3.1\) and the \(A_{MW}\) values shown in the last column of Table 1. The values are from the Schlafly & Finkbeiner (2011) recalibration of the Schlegel et al. (1998) dust maps, except for SN 2014J where we use a value obtained from studying neighbouring regions (Dalcanton et al. 2009).

The colours were also \(K\)-corrected (e.g. Nugent et al. 2002) and \(S\)-corrected (e.g. Suntzeff 2000; Stritzinger et al. 2002; Krisciunas et al. 2003) to a common rest-frame filter system that will be used for the remaining analysis throughout the paper. The analysis was carried out using the WFC3/UVIS and \(Swift/UVOT\) filters for the UV, the ALFOSC filter set for the optical and the NOTCam filters for the NIR, since the bulk of the data were obtained using these filters. The combined \(K\)- and \(S\)-corrections (\(K_X\) from now on) are calculated synthetically using the spectral energy distribution (SED) of SN 2011fe as described in Section 4.1 and the filter transmissions provided by the different observatories.

To summarize, all colours were obtained as

\[
X - V = (m_X - A_{MW} - K_X) - (m_V - A_{MW} - K_V),
\]

where \(m_X\) are the measured instrumental magnitudes in filter \(X\) and \(m_V\) is the \(V\) magnitude for the same date either measured directly, or obtained from a spline or template model. All values are presented in Table 3 where we have also added the \(Swift\) photometry of SN 2014J from Brown et al. (2015) to the measurements described in Section 2. As will be further discussed in Section 4, not only the observed colours, but also, \(A_{MW}\) and \(K_X\) depend on the reddening of each SN and were therefore obtained iteratively during the extinction law fitting. The values shown in Table 3 were obtained after the SN 2011fe SED had been reddened with the Fitzpatrick

\(^6\) Gàlffalk, (private communication).
Filter is commonly used to measure SN Ia distances. SN Ia light curves show diversity in extinction laws for SNe Ia. Diversity in extinction laws for SNe Ia (1999, hereafter F99) law using the parameters shown in Table 5 for each SN.

A subset of the colours are also shown in Fig. 5 where the colours obtained using measurements and the V-band model are shown with filled and open symbols, respectively.

SNe Ia are intrinsically bright in the rest-frame B-band and this filter is commonly used to measure SN Ia distances. SN Ia light curves are typically quantified by a few parameters such as the brightness and time of maximum, \( t^\text{max}_B \), for example the B-band, and the light-curve shape. The light-curve shape can be quantified using different methods, where perhaps the most straightforward is to measure the brightness decline for the first 15 d past \( t^\text{max}_B \). Phillips (1993) showed that fast declining SNe Ia are typically intrinsically fainter than slow declining objects, a discovery that lay the foundation for using SNe Ia as distance indicators for precision cosmology. An alternative approach to quantify the light-curve shape is to introduce a stretch parameter (Perlmutter et al. 1997), \( s_B \), which can be defined as the value needed to match the time-evolution of an observed light curve to a standard SN Ia template.

The time-evolution of SN Ia X–V colours also depends on light-curve shape. For example, Nobili & Goobar (2008, from hereon N08) present colour–light-curve shape relations in the optical while Nobili & Goobar (2008, from hereon N08) present colour–light-curve shape relations in the optical while B14 show that the SNe Ia colours can be standardized over a wide range of decline rates by introducing colour-stretch, \( s_{BV} = t_{BV}/30\, \text{d} \), where \( t_{BV} \) is the time between \( t^\text{max}_B \) and the maximum of the B–V colour. However, this approach requires \( B \rightarrow V \) coverage up to \( t \approx t^\text{max}_B + 40 \) in order to accurately determine \( s_{BV} \).

We here standardize the measured colours using \( s_B \). All colours will be studied and compared as a function of phase, \( p \), defined as \( p = (t - t^\text{max}_B)/s_B \), where \( t \) are the observing dates. The phases for the colours shown in Fig. 5 have been determined by using the values of \( t^\text{max}_B \) and \( s_B \) from Table 5, which are fitted simultaneously with the reddening law as described in Section 4.4.

### Table 5: The best fitted parameters to all measured colours between phases −10 and +35 d for the reddening laws investigated in this work. For the power law, we have fixed \( a \) to a value of 1 to break the degeneracy between this parameter and \( A_V \). For each value, we quote the 68 per cent level fitted uncertainty when the parameters are considered individually. The degrees of freedoms were calculated under assumptions that the colours are independent measurements, which is not the case.

<table>
<thead>
<tr>
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<tbody>
<tr>
<td>F99</td>
<td></td>
<td></td>
<td></td>
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<td></td>
</tr>
<tr>
<td>( E(B - V) )</td>
<td>0.15(0.02)</td>
<td>0.17(0.03)</td>
<td>0.35(0.03)</td>
<td>0.46(0.04)</td>
<td>0.99(0.03)</td>
<td>1.36(0.02)</td>
</tr>
<tr>
<td>( R_V )</td>
<td>2.7(0.07)</td>
<td>1.7(0.05)</td>
<td>3.0(0.04)</td>
<td>3.0(0.5)</td>
<td>2.8(0.1)</td>
<td>1.4(0.1)</td>
</tr>
<tr>
<td>( t^\text{max}_B )</td>
<td>56 080.6(0.3)</td>
<td>56 191.0(0.5)</td>
<td>56 081.0(0.3)</td>
<td>56 018.0(1.9)</td>
<td>56 104.5(0.4)</td>
<td>56 687.9(0.2)</td>
</tr>
<tr>
<td>( s_B )</td>
<td>1.12(0.02)</td>
<td>1.01(0.03)</td>
<td>1.18(0.02)</td>
<td>1.24(0.12)</td>
<td>1.04(0.03)</td>
<td>1.14(0.01)</td>
</tr>
<tr>
<td>( \chi^2/\nu )</td>
<td>1.67</td>
<td>1.50</td>
<td>1.60</td>
<td>2.83</td>
<td>0.63</td>
<td>2.38</td>
</tr>
<tr>
<td>CCM+O</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>( A_V )</td>
<td>0.44(0.19)</td>
<td>0.30(0.13)</td>
<td>1.51(0.40)</td>
<td>1.47(0.43)</td>
<td>3.59(0.29)</td>
<td>1.97(0.10)</td>
</tr>
<tr>
<td>( \beta )</td>
<td>−1.2(0.4)</td>
<td>−1.7(0.5)</td>
<td>−0.8(0.2)</td>
<td>−1.2(0.4)</td>
<td>−1.0(0.1)</td>
<td>−2.0(0.1)</td>
</tr>
<tr>
<td>( t^\text{max}_B )</td>
<td>56 080.6(0.3)</td>
<td>56 191.0(0.5)</td>
<td>56 081.0(0.3)</td>
<td>56 020.4(2.7)</td>
<td>56 104.8(0.4)</td>
<td>56 688.1(0.2)</td>
</tr>
<tr>
<td>( s_B )</td>
<td>1.12(0.02)</td>
<td>1.00(0.03)</td>
<td>1.18(0.02)</td>
<td>1.16(0.15)</td>
<td>1.02(0.03)</td>
<td>1.13(0.01)</td>
</tr>
<tr>
<td>( \chi^2/\nu )</td>
<td>1.79</td>
<td>1.17</td>
<td>1.95</td>
<td>2.13</td>
<td>1.78</td>
<td>1.65</td>
</tr>
</tbody>
</table>

where \( (X - V)_0 \) is the assumed \( X - V \) colour for the unreddened objects.

In this work, we will study different extinction laws and how well they describe the observed SN Ia reddening. Each extinction law, \( A(\lambda; \alpha) \), depends on a set of parameters \( \alpha \) (e.g. \( E(B - V) \) and \( R_V \)), that will be fitted to the observed colour excesses, \( E(X - V)_\lambda \), by minimizing

\[
\chi^2 = \sum_X \sum_p \left[ \frac{E(X - V)_\lambda - (A_X - A_{X\lambda})}{\sigma_{X\lambda}^2} \right]^2 .
\]

Here \( A_X \) and \( A_{X\lambda} \) are the predicted extinctions in the \( X \) and \( \lambda \) filters for phase \( p \) and can be calculated as

\[
A_X = -2.5 \log_{10} \left( \frac{\int T_X(\lambda) \times 10^{-0.4(\lambda; \alpha) S_0(\lambda; p) \lambda \, d\lambda}}{\int T(\lambda) S_0(\lambda; p) \lambda \, d\lambda} \right) ,
\]

if the effective filter transmission, \( T_X(\lambda) \), and theSED, \( S_0(\lambda; p) \), of the unreddened source are assumed to be known. Further, \( \sigma_{X\lambda}^2 \) are the uncertainties added in quadrature. This includes the measurement errors, but will in most cases be dominated by the intrinsic colour uncertainties discussed in Section 4.1.

In addition to the extinction law parameters \( \alpha \), we will also minimize equation (3) with respect to the parameters \( t^\text{max}_B \) and \( s_B \) that together determine the phase, \( p \). The observed values of these parameters are extinction dependent (see e.g. Leibundgut 1988; Phillips 1993; Nugent et al. 2002; A14) since broad-band measurement of an object suffering from extinction will effectively probe redder wavelengths than the observation of the same unreddened object would have. The SN Ia light curve decline rate varies with wavelength, and slower decline rates are in general expected to be observed for reddened objects.

Similarly, the Galactic extinction, \( A_X^{\text{MW}} \), as well as the \( K_S \) corrections, are also properties measured through broad-band filters and therefore also depend on the SED of the source, as seen from e.g. equation (4). Since the observed SED in the Milky Way is affected by the extinction in the SN host galaxy, these properties will also depend on the reddening law. The effect will be particularly significant in the UV, where the wavelength dependence for the extinction laws is steep. For example, the Galactic extinction in the SwiftUV2.
Figure 5. A selection of measured colours from UV to NIR together with literature SNe 2011by and 2011fe. The phases, \( p = (t - t_{\text{max}})/s_B \), were obtained using the values of \( t_{\text{max}} \) and \( s_B \) from Table 5. The colours from the H07 spectral template (dashed red) and Nobili & Goobar (2008, N08, solid blue with dispersion region) are also shown together with the derived colour model of SN 2011fe (solid grey) with the adopted dispersions (grey region). Filled symbols show colours where a V-band measurement was obtained for the same date, while a V-band model was used to obtain the measurements that are shown with open symbols. Error bars are only plotted for data points where the uncertainty exceeds 0.1 mag. See text for details.

We take this effect into account by fitting each reddening law, \( A(\lambda; \tilde{a}) \), iteratively and update \( A^\text{MW}_V \) and \( K_X \) using the fit \( \tilde{a} \) values in each iteration. That is, after each iteration, we re-calculate the observed colour and colour excesses using equations (1) and (2) before re-fitting the reddening law using equation (3). The procedure is repeated until the change in the fitted parameters is less than 1 per cent between iterations.

As mentioned above we use the average value of \( R_V = 3.1 \) when correcting for the Galactic extinction. For the majority of the SNe the Galactic extinction is negligible compared to the host reddening, with the exception of SN 2012et. For this SN we also tried carrying out the fits using the extreme values of \( R_V = 2.2 \) and \( R_V = 5.8 \).
observed in the Milky Way (e.g. CCM; F99) and concluded that this could impact the fit values with up to one statistical standard deviation.

4.1 SN Ia intrinsic colours and SED

In order to minimize equation (3), we need to make assumptions of the intrinsic colours, \((X - V)_0\), and SED, \(S_0(\lambda; \rho)\) of the unreddened objects. The reddening laws for SNe Ia are typically derived by either comparing them to individual objects that show similarities in light-curve properties and spectral evolution (Krisciunas et al. 2006; A14), or to SN Ia colour and SED templates.

In Fig. 5, the H07 template is plotted (dashed red) for the optical colours. Although the H07 template does extend from the UV to NIR, the data it is based on are sparse at the endpoints of this range. N08 studied the intrinsic optical colours between \(-10\) and \(+50\) d from \(B\)-band maximum. Two of their colour laws are shown (in blue) for normal, \(s_B = 1\), SNe Ia in Fig. 5 together with the colour dispersions they derive. Although these templates provide excellent coverage at optical wavelengths none of them cover, to high accuracy, the full wavelength range required for the UV–NIR analysis in this work.

The best studied unreddened SN Ia to date is SN 2011fe, discovered by the Palomar Transient Factory in the nearby spiral galaxy M101 (PTF11kly; Nugent et al. 2011). Its close proximity allowed detailed spectroscopic and photometric observations over a broad wavelength range from the UV (Brown et al. 2012; Mazzali et al. 2014), through the optical (e.g. Munari et al. 2013) to the near- (Matheson et al. 2012; Hsiao et al. 2013), and mid-infrared (McClelland et al. 2013). The SN was also targeted in the far-IR (Johansson et al. 2013) and radio (Chomiuk et al. 2012a), but was not detected at these wavelengths.

SN 2011fe is a normal SN Ia in both the optical and the NIR (Matheson et al. 2012; Munari et al. 2013) and does not show any spectroscopic peculiarities (Pereira et al. 2013). Further, the low Galactic and host galaxy reddening along the line-of-sight, \(E(B - V)_{\text{host}} = 0.011 \pm 0.002\) mag and \(E(B - V)_{\text{host}} = 0.014 \pm 0.002\) mag (deduced from the integrated equivalent widths of the Na D lines; Patat et al. 2013), makes it an excellent comparison object for studying reddening of SNe Ia. The colours of SN 2011fe shown in Fig. 5 (solid black lines) have been obtained by combining the available UV–NIR data, as described in Appendix B based on the measurements (black triangles). We have also combined the spectroscopic data to create a daily sampled SED, shown in Fig. B1. From the excellent \(B - V\) match between SN 2011fe and H07, we can also conclude that any potential discrepancies introduced by using the SNOOPY model for the \(V\)-band is not likely to have any significant effect on the derived reddening laws when the colours are compared to the corresponding SN 2011fe colours.

In order to properly compare the colours of reddened SNe Ia to SN 2011fe, and fit reddening laws, we also need accurate estimates of the expected intrinsic colour dispersions. It is desirable to take into account how these vary in time, and how they are correlated both in time and with different colours. However, since we lack this information for all colours involved in the analysis, we adopt a simplified approach where all colours are treated equally with phase-independent dispersions for each colour. We further follow the procedure from A14 and assume that the colour uncertainties between SN phases are completely correlated and that there is no correlation between different colours.

Milne et al. (2013, M13 from hereon) following the work of Brown et al. (2010) and Milne et al. (2010), studied the UV–optical colours of 23 SNe Ia observed by Swift. They reported a dispersion of \(\sim 0.3\) mag in UV–\(V\) for their \(E(B - V) < 0.2\) mag sample after correcting the data for extinction and the result does not seem to be affected significantly by the choice of \(R_V\). We adopt this dispersion, shown as grey bands around the SN 2011fe colour template in Fig. 5, for the \(uvm2 - V\), \(F225W - V\), and \(F275W - V\) colours. For the \(F336W - V\) and \(U - V\), we adopt a dispersion of 0.1 mag based on the \(U - V\) dispersion from N08. Note that since these dispersions were derived for unreddened objects, and the dispersion of SNe Ia colours decrease with wavelength, they can be considered as conservative for highly reddened SNe. When reddened SNe Ia are studied using the WFC3/UVIS filters, the observations will effectively probe redder wavelengths compared to similar studies of unreddened objects as illustrated in e.g. Fig. D1, and as a consequence the intrinsic dispersion of the former observations can be expected to be lower than the latter. On the other hand, even larger dispersions have been also observed in the UV, and we will use these intrinsic uncertainties under the assumption that all the SNe we study are similar to the reference SN 2011fe, which we will discuss further in Section 6.1.

B14 derive a dispersion for the pseudo-colour \(B_{\text{max}} - V_{\text{max}}\) of 0.06 mag using a Cauchy Prior for the colour distribution of their SNe Ia observed with the Carnegie Supernova Project. This is consistent with the phase-dependent results of N08 who derive a \(B - V\) dispersion of \(\lesssim 0.1\) mag, which we use here, within the range \(-10\) to \(+35\) d. For the \(V - R\) and \(V - i\) colours we adopt the N08 dispersions of 0.08 mag.

The NIR colours of SNe Ia typically show low dispersion (see e.g. Meikle 2000) and for the NIR-optical \(V - J\) and \(V - H\) colours we can estimate the dispersion in our phase range by using all SNe with \(E(B - V) < 0.2\) mag from the ‘Gold Sample’ in Stanishev et al. (2015) and find 0.12 mag and 0.13 mag, respectively. For \(V - K_s\), we conservatively adopt 0.2 mag based on the studies carried out at maximum (B14) and the dispersion of the \(K_s\)-band (Friedman 2012; Friedman et al. 2014).

The observed colour excesses, \(E(X - V)\), for each reddened SN, together with the adopted colour dispersions, shown as background regions, are plotted in Fig. 6. SN 2012bl has not been plotted in the figure. It will be omitted from the extinction analysis due to its lack of reddening.

If the colour excess is observed at single wavelengths, i.e. \(E(\lambda_i - \lambda_j) = A_{\lambda_i} - A_{\lambda_j}\), it will be time-independent for interstellar dust extinction. However, for broadband photometry, we can expect \(E(X - V)\) to vary with time which is illustrated by e.g. the UV colours in Fig. 6. As the intrinsic colour of the source varies with time, the effective wavelengths of all broadband filters will change as well. Further, since the first term on the right-hand side in equation (2) is also affected by a reddening law, any change in the effective wavelength of the filters \(X\) and \(V\) will affect this term more than the second term, which will induce a time-variability for \(E(X - V)\). For most filters, the time-variability will be negligible except in the UV (where the extinction has a steep wavelength dependence), and in particular for filters with red tails, e.g. \(F225W\) (see Appendix D), the effect is significant. This is illustrated by the bottom panel of Fig. D1 where the effective wavelength of three WFC3/UVIS UV filters have been plotted for an SN Ia at maximum for different extinctions.

4.2 Reddening laws

We test three different extinction law parametrizations. In addition to the widely used CCM law modified by O’Donnell (1994,
Figure 6. The observed colour excess, $E(X - V)$, against phase for all SNe and filters. The predicted colour excess from the SN 2011fe template and the fitted F99 law, presented in Table 5, is shown with solid lines and the regions surrounding them mark the adopted intrinsic colour uncertainties. The uncertainties are also indicated by open brackets for the three SNe with the least reddening. The phase, $p = (t - t_{\text{max}})/s_B$, was calculated based on the fitted $t_{\text{max}}$ and $s_B$ values from Table 5. The apparent $E(X - V)$ time-dependence of the F225W filter for e.g. SN 2014J originates from the red tails of these filters which causes the observed colour excess to vary with the intrinsic colour of the source.

We also test a simple power-law model (Goobar 2008),

$$A(\lambda; A_V, a, \beta) = A_V \left[ 1 - a + a \left( \frac{\lambda}{\lambda_V} \right)^\beta \right],$$

where the reference wavelength, $\lambda_V$, will be chosen as $\lambda_V = 0.55 \, \mu m$. The CCM+O and F99 laws can be approximated by a power law in the optical and NIR range, and Goobar (2008) showed that the observed reddening law of an object embedded in CS dust

hereafter CCM+O), which has been derived from studying different lines of sight in the Milky Way, we also fit the parametrization from F99 that has been derived in a similar manner. For each of these we fit both the colour excess $E(B - V)$, which relates to the optical depth, and the ratio of the total-to-selective extinction, $R_V$. In the Milky Way the value of $R_V$ typically varies between $R_V = 2.2$–5.8, for different lines of sight (e.g. CCM; F99), despite this we allow extrapolations of $R_V$ within the range $R_V = 0.5$–8 when we fit the laws to the SN colours.
Figure 7. The normalized extinction, $A_X/A_V$ for the four SNe with $E(B-V) > 0.2$ mag. Here, $A_X/A_V = 1 + E(X-V)/A_V$ where $E(X-V)$ is calculated as the weighted (with the measurement uncertainties) averages for all epochs, and $A_V$ is obtained from the fitted F99 parameters in Table 5. Following A14, each data point has been plotted at the wavelength where the residual to the extinction law is matching the corresponding residual between $E(X-V)$ and the fitted reddening law in Fig. 6. Note that all fitted parameters described in this work were obtained by minimizing equation (3), and not by fitting the extinction laws to the data points in this plot. The filter passbands for the filters used for the minimization are shown at the top.

4.3 Results

The fitted parameters for the three extinction laws are presented in Table 5 for each individual SN. The extinction laws were fitted to all available colours between phases $-10$ and $+35$ d and the predicted colour excesses using the best fitted F99 laws are also shown in Fig. 6. The revised photometry of SN 2014J and updated intrinsic colour model with respect to A14 only had a minor impact on the fitted results for this highly reddened SN, and the values presented here are consistent with A14.

Further, all three reddening laws capture the general wavelength dependence of the observed colour excesses with the possible exception of SN 2012cg which will be discussed below. This shows that the observed SN colours from UV to NIR can indeed be described by the colours of SN 2011fe, with the adopted intrinsic dispersions, together with an extinction law with only two free parameters.

The six SNe span a broad range both in reddening, $E(B-V) = 0.2–1.4$ mag, and in $R_V = 1.4–3.0$ which confirms the findings from previous optical and NIR studies (e.g. B14), that point to a diversity of observed reddening laws of SNe Ia. The significant difference in the derived extinction laws is also illustrated in Fig. 7 where the relative extinction, $A_X/A_V$, for the F99 law has been plotted for two different values of $R_V$. The diversity is particularly striking bluewards of the $U$ band ($\lambda < 3600$ Å), emphasizing the power of using UV data to study diversity in extinction.

In Fig. 7 we also show the relative extinction, $A_X/A_V = 1 + E(X-V)/A_V$, for the four SNe with $E(B-V) > 0.2$ mag against inverse wavelength. Here, $E(X-V)$ is calculated as the weighted average for all phases and $A_V$ was obtained from the fitted F99 parameters...
responding to wavelengths, it is non-trivial to derive a specific wavelength cor-
sources, and the measurements correspond to different effective

could be the case for SN 2014J, where the F99 law with


Table 6. Fitted F99 parameters using only data between −5
to +5 and +10 to +20 d from maximum, respectively. While
SNe 2012cg and 2014J both have UV–NIR observations for
both intervals, the fits to SN 2012cp are only based on UV–
optical data. The parameters \( \alpha_{\beta} \) and \( \delta \) were fixed to the
values given in Table 5.

<table>
<thead>
<tr>
<th>SN</th>
<th>Phase</th>
<th>( E(B - V) )</th>
<th>( R_V )</th>
<th>( \chi^2/\nu )</th>
</tr>
</thead>
<tbody>
<tr>
<td>SN2012cg</td>
<td>[−5, +5]</td>
<td>0.16(0.02)</td>
<td>1.7^{+0.8}_{-0.6}</td>
<td>1.51</td>
</tr>
<tr>
<td></td>
<td>[+10, +20]</td>
<td>0.13(0.03)</td>
<td>3.6^{+1.5}_{-1.0}</td>
<td>1.34</td>
</tr>
<tr>
<td>SN2012cp</td>
<td>[−5, +5]</td>
<td>0.33(0.03)</td>
<td>1.8^{+0.6}_{-0.5}</td>
<td>1.63</td>
</tr>
<tr>
<td></td>
<td>[+10, +20]</td>
<td>0.34(0.03)</td>
<td>2.2^{+0.8}_{-0.6}</td>
<td>0.55</td>
</tr>
<tr>
<td>SN2014J</td>
<td>[−5, +5]</td>
<td>1.35(0.03)</td>
<td>1.5^{+0.1}_{-0.1}</td>
<td>1.81</td>
</tr>
<tr>
<td></td>
<td>[+10, +20]</td>
<td>1.32(0.03)</td>
<td>1.6^{+0.1}_{-0.1}</td>
<td>1.56</td>
</tr>
</tbody>
</table>

5 SEARCHING FOR CS DUST

All the SNe studied here show a colour excess evolution that is
within the adopted dispersion with the exception of SN 2012cg.

This SN reveals a minimum in its NIR colour evolution around
two weeks past max which is possibly accounted to the diversity
observed in NIR SN Ia light curves between the first and second
peaks. This is within the assumed intrinsic uncertainty although the
assumption that these are fully correlated between epochs does not
hold in this case. What is perhaps even more striking are the ~2σ
variations of the \( uvm2 - V \) evolution which suggests that this colour
evolve slower than the corresponding 2011fe colour, resulting in an
apparent decrease with time of the colour excesses.

The fact that the observed colour evolution of SN 2012cg is not
consistent with a single extinction law is also illustrated by Table 6
where the F99 law has been fitted for two phase intervals: around
maximum and between 10 and 20 d past \( t_{\text{max}}^{\text{NIR}} \). The fits were carried
out for the three SNe that had UV data in both these intervals while
keeping the fitted values of \( \alpha_{\beta} \) and \( \delta \) fixed to the values given in Table 5. The fitted parameters of SNe 2012cp and 2014J are
within errors between the two epochs while this is not the case for
SN 2012cg.

Evolving colour excesses, or a reddening law that changes with
time, is predicted if CS dust is present in the SN environment.

Amanullah & Goobar (2011) studied this effect at optical wave-
lengths and we can extend that analysis, using the same tools, to
also cover UV and NIR in order to test the observed colour evolution
of SN 2012cg against the expectations for a CS scenario.

In Fig. 9 the same colour excesses of SN 2012cg that are plotted in
the upper-left panel of Fig. 6 are shown. The solid lines represent the
result when we fit a combined F99 and CS dust law to the bluest
colours, \( uvm2 - V \) and \( F225W - V \), while keeping \( t_{\text{max}}^{\text{NIR}} \) and \( \delta \) fixed to the values from Table 5. The best-fitting values for the F99
law are \( E(B - V) \approx 0.2 \) mag and \( R_V \approx 3.0 \). The CS dust in this case
consists of dust modelled to match the average extinction properties
in the Milky Way (Draine 2003) and distributed in a thin spherical
Although adding Milky Way-like CS dust to the picture can give an explanation for the time-evolution of the bluest colours, it does not provide an improvement beyond a single F99 law when all colours are considered simultaneously, which is shown by the dashed lines in Fig. 9. Here, the best fit is obtained for $A_V \approx 0.2$. The explanation for this is that the specific CS dust model we test also predicts evolution of the redder colours which in this case is not supported by the data. If CS dust is present, the total extinction, $A_V$, can only decrease with time due to late-arriving scattered photons. From the results in Table 6, we see that this is not the case for $A_V$, although the value of $A_V$ is in this case model dependent.

It is also possible to detect CS dust by studying the time-evolution of multi-epoch high-resolution spectroscopy. This was mentioned in Section 1 and is the observational signature that has been used to claim detections of CS dust around SNe Ia.

For SN 2012cg, we obtained high-resolution FIES spectra for three epochs which are listed in Table 4 and correspond to phases $-7$, $1$ and $13$ d with respect to $t_B^{\text{max}}$. All spectra contain well-resolved unsaturated Na I features (Fig. 4), which are shown in Fig. 10. The bulk of the distinguishable features are likely part of the visible interstellar medium (ISM), but it cannot be excluded that Na I associated with CS medium could contribute to the observed profile. A full description of the Na I profile and summary of other interstellar absorption features is presented in Section 6.4.

The FIES spectra were normalized by fitting third-order polynomials to the continua bracketing Na I. No telluric corrections were performed on the spectra, due to the lack of standard star observations on some of the epochs. We fitted Gaussian profiles to the weighted average of the three epochs, and find that the Na I line ratios (D1/D2) range from 2 to 1.2 for individual features. The deepest features have low ratios, indicating that they are not optically thin. Based on a standard star spectrum taken on the second epoch, we identify telluric features overlapping with Na ID, whereas Na ID appears to be located at a less affected part of the spectrum. We therefore focus most of the time-variation analysis on Na ID, because it is less contaminated by telluric features and it is more likely to be optically thin due to the lower absorption cross-section of this transition. We measure the total equivalent width of Na ID at the respective epochs to be, $702 \pm 9, 711 \pm 32$ and $685 \pm 20$ mÅ.

Since no significant time-variations of Na ID absorption between different epochs could be detected beyond the noise level, we attempt to use the non-detections to constrain possible CS dust models assuming a thin sphere of CS material shell distribution around the SN. Using the Na I photo-ionization model described by Borkowski et al. (2009) and recently applied to SN 2014J in Graham et al. (2015b), we can exclude CS material, and thus also CS dust, at certain radii from the SN. If the Na I is optically thin, a change in equivalent width of Na ID is directly proportional to a decrease in column density. We can thus compute the fractional decrease in equivalent width of Na ID expected due to photoionization of CS material at a given radius from an SN. In this model, CS Na I can be excluded which is far enough away from the SN to not have been fully ionized by the first epoch and close enough to see changes by the following epochs. The diversity of SNe Ia

![Figure 9](http://mnras.oxfordjournals.org/)

Figure 9. The measured colour excesses for different phases for SN 2012cg are taken from Fig. 6. Overplotted are the best fits of a combined CS and F99 dust law, where the dust has been adopted from Amanullah & Goobar (2011) where the dust is distributed in a thin spherical shell. The solid lines show the best fit when only the $uvw2 - V$ and $F225W - V$ colours are considered, while the dashed lines show the fit to all colours. The former is extinction, $A_V$, not the case for $A_V$. From the results in Table 6, we see that this is the observational signature that has been used to claim detections of CS dust around SNe Ia.

![Figure 10](http://mnras.oxfordjournals.org/)

Figure 10. Na ID absorption doublet of SN 2012cg. The rest-frame wavelength of Na ID in NGC 4424 (solid lines) and for the approximate stellar velocity along the line of sight (dashed) are indicated. The dotted vertical line indicates a sky emission line. In Section 5 the profile of Na ID is discussed in detail.
the profile. We therefore also consider how much a single feature must change to be detected given the signal to noise of the spectra. The limits obtained by the absence of change beyond three times the RMS noise are comparable to those set by the fractional change of the total equivalent width. Lastly, we note that the limits are not valid if there is CS material that is not optically thin, since the equivalent width then does not change linearly with column density.

In summary, although the existence of Milky Way-like CS dust at \( r_{\text{dust}} \approx 3 \times 10^{19} \) cm is consistent with the observed time-evolution of \( E(uvw2 - V) \) and non-detection of time-varying Na I absorption for SN 2012cg, the minimal \( E(X - V) \) evolution of the redder wavelengths favours this explanation. This suggests that CS dust can only be present either in very small amounts, \( A_{\text{CSMW3}}^{\text{SN}} < 0.05 \) or if it is located at larger radii \( r_{\text{dust}} \approx 10^{20} \) cm for which the time-delays are much larger than the time-scales studied here and are not expected to affect the observed colours (Amanullah & Goobar 2011). Further, non-detections in radio (Chomiuk et al. 2012b) and far-IR (Johansson et al. 2013) are other observational signatures suggesting that SN 2012cg exploded in an environment free from CS material. Here, the far-IR observations are sensitive to pre-existing CS dust that would be heated by the explosion.

6 DISCUSSION

6.1 Using SN 2011fe as a colour template

One possible explanation for the time-evolution of the SN 2012cg UV – V colour excess could be that it is intrinsically different from SN 2011fe. We have already argued that all the SNe in our sample, are normal SNe Ia by comparing their overall spectra (see Fig. 4) and their SNID classification, but we can also study individual features which has proven to be a useful approach for sub-classifying normal SNe Ia.

The properties of individual features can be quantified by e.g. measuring their velocities and pseudo-equivalent widths (pW), where pseudo refers to the fact that the equivalent widths are obtained using a pseudo-continuum since proper continua are absent in SN Ia spectra. The pseudo-continuum can be defined with a straight line between the two flux peaks surrounding an absorption feature and the pW is then calculated as the integral of the spectrum flux relative to the continuum. Using this method, the error of the measurement will typically be dominated by the systematic uncertainty introduced by the determination of the pseudo-continuum.

Branch et al. (2006) suggested a classification scheme based on pseudo-equivalent width measurements of the absorption features near 5750 Å and 6100 Å (following the naming convention from Garavini et al. 2007, we refer to these as pW6 and pW7, respectively), that can be associated with Si ii 5972 Å and Si ii 6355 Å as shown in Fig. 4. They identify four different groups when considering pW6 and pW7 for their sample where in particular the ‘core normal’ (CN) SNe, to which SN 2011fe belongs, are tightly clustered and show a high degree of general spectral homogeneity.

In Table 7, we show measurements of pW6 and pW7 for spectra close to maximum after correcting our spectra for host galaxy reddening (although this is not expected to have any major impact on the results as discussed in Nordin et al. 2011) using the fitted reddening laws from Section 4.3. We also present the pW for Ca ii H&K (pW1 following Garavini et al. 2007) and note that all SNe have pW1 < 150 Å. It has been shown that pW1 correlates with the intrinsic U – B colour (Folatelli et al. 2013; B14), where SNe with pW1 > 150 Å are intrinsically redder than the bulk of normal SN Ia.
Using the classification criteria from Blondin et al. (2012), we can classify all SNe as CN except for SN 2012et which lands in range that Branch et al. (2006) defines as the ‘broad-line’ (BL) group. These SNe Ia have broader and deeper 6100 Å absorption but are in most aspects not very different from CN SNe. When the observed spectra from the two groups are compared with synthetic spectra generated with SYNOW (Branch et al. 2003) similar photospheric velocities and excitation temperatures can be used to describe both the CN and BL groups (Branch et al. 2006).

Given these results, there is no evidence for any significant discrepancy between the optical properties of our SNe and SN 2011fe, with the exception for the additional source of luminosity observed in the very early optical light curve of SN 2014J (Goobar et al. 2015). However, several studies have shown that normal SNe in the optical still show dispersion in the UV and M13 argued that their grey region is marking the average SN Ia velocity range (Folatelli et al. 2012, 2013). The dashed line marks the difference used to separate high- and low-velocity objects by Wang et al. (2009) at maximum.

On the other hand, exceptions from these findings is, SN 2011de, the brightest SN Ia observed (Brown 2014), and the results by Wang et al. (2012), showing, using the HST Advanced Camera for Surveys, that the UV-optical colours of the HV object SN 2004dt are significantly bluer than the NV SN 2005cf.

We have measured the Si II velocities, which are presented in Fig. 12, for all spectra we have obtained of the SNe at $t < +25$ d from $\lambda_{\text{min}}^{\text{meas}}$ by fitting Gaussian profiles. From the figure we conclude that SN 2011fe, 2012bm, 2012eg and 2012cp show similar velocity evolutions, and the single measurement we have of SN 2012cu is also consistent with SN 2011fe. The SNe 2012bl, 2012et and 2014f, on the other hand, are classified as HV. Note however that the velocity range for the full sample is still small enough for the scatter induced by the optical colour–velocity relation to land within the adopted uncertainty of 0.1 mag for $B - V$ (Mandel et al. 2014).

Mandel et al. (2014) further find no evidence for such a relation for the $V - R$ and $V - i$.

SN 2012et is both classified as BL (although the $pW6$ and $pW7$ values put its close to the border of the BL and CN groups) and HV, and such objects have been shown to be redder than the bulk of normal SNe Ia (Folatelli et al. 2013; B14). However, the value of $pW1$ for SN 2012et at $-8$ d is $pW1 = 82 \pm 7$ Å, which is well below $pW1 = 150$ Å where the BL HV start to deviate in colour (see fig. 17 in B14).

M13 also determine that NUV-blue SNe show evidence of unburned C II in their optical spectra while the remaining groups consist of objects both with and without unburned C II detections. These results are also consistent with optical spectroscopic studies where SNe Ia with signatures of unburned carbon are bluer in their optical colours (e.g. Thomas et al. 2011; Folatelli et al. 2012; Silverman & Filippenko 2012). Unburned carbon can be detected through absorption attributed to the most prominent line in the optical, C II...
In conclusion, based on the optical spectroscopy available both around maximum light and in the nebular phase, there are no observational signatures that would disfavour comparing the colours of the SNe to SN 2011fe for studying reddening together with the adopted uncertainties. In particular, while SNe 2011fe and 2012cg have slightly different light-curve shapes, they show remarkable similarities in spectroscopical features and evolution. However, the SNe 2011by and 2011fe have also been found to be almost identical in their optical properties and have slightly different light-curve shapes, they show remarkable similarities in spectroscopical features and evolution. However, the uncertainty in the fitted reddening laws if we instead compare the measured colours to SN 2011fe.

In Appendix C, we describe this procedure and construct a model SED of SN 2011by as a colour template to model the flux ratio between SNe 2011by and 2011fe as described in Appendix C.

6.2 SN 2011by as colour template

SN 2011by was discovered (Jin & Gao 2011) in NGC 3972 and found to be a spectroscopically normal SN Ia (Silverman, Ganshalingam & Filippenko 2013b) with minimal reddening (Maguire et al. 2012). HST/STIS UV observations were obtained at maximum (Programme GO-12298; PI: Ellis) and using these data Foley & Kirshner (2013) and Graham et al. (2015a) have shown that while SN 2011by is almost identical to SN 2011fe in its optical properties it is intrinsically fainter in the UV. The two SNe are compared at maximum in Fig. 14, where the ratio between the spectra are plotted. Comparing this to the ratio between SNe 2012cg and 2011fe at maximum, also shown in the figure, suggests that SN 2011by may be an even better reference SN than SN 2011fe in the UV.

Both SNe 2011by and 2012cg are fainter than SN 2011fe in the UV, which could explain why SN 2012cg is marginally redder in its UV colours than predicted by the fitted reddening laws. Two other SNe in the sample, 2012bm and 2012cp, show a similar behaviour for the bluest colour $F_{225W}$. HST/STIS spectroscopy of SN 2011by was obtained at phases $-10$ and $-1$ d, which unfortunately does not allow us to construct an SED covering the full range of our observations as we did for SN 2011fe. However, we can use the available spectrum at maximum and the Swift observations of this SN to model the difference between SNe 2011by and 2011fe in the UV. In Appendix C, we describe this procedure and construct a model SED of SN 2011by under the assumption that it is identical to SN 2011fe at wavelengths $\lambda > 3000$ Å.

Using this as the comparison SN, we can refit the reddening laws for the SNe 2012cg, 2012cp and 2012bm for which we have reason to believe that SN 2011by may provide a better comparison object. The fitted F99 parameters at maximum are presented in Table 8. The fitted parameters for SNe 2012cp and 2012bm change marginally...
Table 8. Best fitted parameters of the F99 law using the colour and SED model that has been adapted to match SN 2011by in the UV as described in Section C. The quoted uncertainties are the statistical $1\sigma$ errors from the $\chi^2$ fit.

<table>
<thead>
<tr>
<th></th>
<th>2012cg</th>
<th>2012cp</th>
<th>2012bm</th>
</tr>
</thead>
<tbody>
<tr>
<td>$E(B - V)$</td>
<td>0.12(0.02)</td>
<td>0.34(0.03)</td>
<td>0.45(0.04)</td>
</tr>
<tr>
<td>$R_V$</td>
<td>$3.7_{-1.0}^{+1.4}$</td>
<td>$3.2_{-0.4}^{+0.5}$</td>
<td>$3.0_{-0.4}^{+0.4}$</td>
</tr>
<tr>
<td>$s_B^{\text{max}}$</td>
<td>56 080.5(0.3)</td>
<td>56 081.1(0.3)</td>
<td>56 018.3(1.1)</td>
</tr>
<tr>
<td>$s_B$</td>
<td>1.13(0.02)</td>
<td>1.19(0.02)</td>
<td>1.24(0.08)</td>
</tr>
<tr>
<td>$\chi^2/\nu$</td>
<td>0.88</td>
<td>1.09</td>
<td>2.13</td>
</tr>
</tbody>
</table>

Figure 15. The colour excess for SN 2012cg, similar to the upper-left panel of Fig. 6, with the exception that the measured and predicted colour excesses are based on the SED model described in Section C, which has been derived to mimic SN 2011by in the UV. The solid lines represent the best fitted F99 law with the parameters given in Table 8.

compared to Table 5 but we do note that reduced $\chi^2$ has decreased. However, the most interesting result here is for SN 2012cg. Not only the fitted reddening law parameters change, but also the time-evolution of $E(uvm 2 - V)$ becomes less significant, which can be seen in Fig. 15. This can be explained from Fig. C1, where the colour excesses of SN 2011by are shown with respect to SN 2011fe, and a similar time-evolution for $E(uvm 2 - V)$ is shown. We note that there is still a tension between the bluest colours and the fitted reddening law which may suggest that the spectrum of SN 2012cg drops faster than SN 2011by at $\lambda < 2500$ Å.

From the spectroscopic similarities between SNe 2011by and 2012cg as shown in Fig. 14 and the similar UV-optical colours we find that SN 2011by appears to be a better comparison SN for SN 2012cg than SN 2011fe. This study also show how studying the UV-colour evolution of SNe Ia provides a powerful tool for comparing predictions of CS dust scenarios with intrinsic colour variations.

6.3 The impact of the UV data

Another approach for testing the robustness of the reddening laws is to study how the fitted parameters are affected by the data at different wavelengths. We do this by comparing the fitted F99 parameter values for two different cases, where we use all measured colours (UV–NIR) and where we omit the UV data (OPT-NIR). A tension between the two cases could be a sign of either assuming an incorrect reddening law or colour reference SN. We keep $t_{\text{max}}^{\text{opt}}$ and $s_B$ fixed for this study and use SN 2011by as reference for the SNe with red UV colours. The results are presented in Table 9.

The results are consistent for all SNe except for SN 2014J, where the addition of the UV data shifts the fitted values by $\sim 2\sigma - 3\sigma$. We fit a low value of $R_V$ for this SN and, as shown in Fig. 8, a power law appears to provide a better fit in this case. In Table 10, we present the results on the two colour sets when using a power-law relation for the two low-$R_V$ SNe. While there is a slight, $\sim 1\sigma$, tension for SN 2012et, the results are fully consistent between the two cases for SN 2014J.

The major impact of adding the UV-colours is, however, on the uncertainties of the fitted values, in particular for low-reddening SNe. This is illustrated in Fig. 16 where the grey contour shows the 68 per cent confidence region for $E(B - V)$ and $R_V$ when the F99 law is fitted to the optical–NIR data of SN 2012cg, while the blue contour shows the uncertainties from the full UV–NIR fit. From the figure, we conclude that extending the wavelength range significantly improves the constraints on $R_V$ despite the high intrinsic dispersion adopted for the $Swift$ and $HST$ colours.
Figure 16. Contours showing the joint 68 per cent uncertainty region for the fitted parameters $R_V$ and $E(B-V)$ for a F99 extinction laws for SN 2012cg in comparison to SN 2011by. The two contours show the fit results when the full data set (UV–NIR) is used (dark blue contour region) and when the colours based on HST and Swift UV observations are omitted (light grey contour region). All data between phases $-10$ and $+35$ d with respect to $t_{max}$ were used, and the best-fitting values for the two cases have been marked by black and blue dots, respectively.

6.4 Extinction from interstellar absorption features

In Section 5, we discussed the constraints on the existence of CS dust that can be derived from non-detection of time-varying Na ID absorption lines. Na ID lines in high-resolution spectra are also commonly used as a proxy for reddening (Poznanski et al. 2011) and the equivalent width of the lines have been shown to correlate well with extinction in the Milky Way (see Munari & Zwitter 1997; Poznanski et al. 2012). However, Phillips et al. (2013) found that of their sample of SNe Ia $\sim 25$ per cent, of which most have blue shifted Na ID features, have unusually high Na I column densities compared to the values expected from the Poznanski et al. (2012) relation. It is currently unclear whether the high abundance of sodium is intrinsic to the environment of some SN Ia or if the Milky Way reference value is anomalous compared to other galaxies. Other species, such as diffuse interstellar bands, have been shown to be useful for studying the ISM in SNe Ia host galaxies (Sollerman et al. 2005) and in particular the diffuse interstellar band (DIB) feature at 5780 Å may provide a better proxy for reddening of SNe Ia than Na ID (Phillips et al. 2013). In Table 11, we present equivalent width values of Na ID and the DIB at 5780 Å with corresponding reddening estimated by the empirical relations (Poznanski et al. 2012) and (Phillips et al. 2013), respectively, for the SNe of which we have obtained spectra or published data exists. Further empirical reddening relations exist for ISM features Ca II H&K (Murga et al. 2015) and Mg II (Ménard et al. 2008). These relations have so far not been extensively studied for their validity in estimating the reddening of SNe.

Besides Na ID, narrow Ca II H&K features, with respective equivalent widths of $770 \pm 30$ and $579 \pm 35$ mÅ could only be measured from the first FIES epoch of SN 2012cg. These values are well above the range in which the relations in (Murga et al. 2015) are valid. Phillips et al. (2013) also quote the detection of the DIB 5780 Å which is consistent with the non-detection in the individual FIES epochs within the signal to noise. The most prominent absorption features in Na ID, shown in Fig. 10 roughly agree with $v_0$ from Table 1 and are slightly blueshifted with respect to the apparent stellar velocity of $\sim 448$ km s$^{-1}$ along the line of sight of SN 2012cg (see Cortés, Kenney & Hardy 2006). Additional features of the Na ID and Ca II H&K profiles span a range from $\sim 370$–$530$ km s$^{-1}$, whereby a number of features are blended on the redshifted side of the profile. SN 2012cg is included in the analysis of Phillips et al. (2013) and is not counted in the group of SNe with anomalously high Na I column densities. However, the best fit $E(B-V)$ in Table 9 for 2012cg highly disagrees with the value computed from the Poznanski et al. (2012) relation.

Four epochs of high-resolution spectra of SN 2012cu have been described in Sternberg et al. (2014). No time-variability is detected in the deep Na ID absorption features, which likely consist of several blended components. The velocity of the Na ID lines of $\sim 1130$ km s$^{-1}$ are in agreement with the H I velocity along the line of sight of SN 2012cu in NGC 4772 (Haynes et al. 2000). We perform the photoionization analysis described in Section 5 on the Na ID doublet of 2012cu. The non-variation of Na ID1 indicates that there is no Na I between $6 \times 10^{18} – 2 \times 10^{19}$ cm. However, these constraints are weak since the absorption lines are close to saturation and not optically thin. The $E(B-V)$ computed from the Poznanski et al. (2012) relation is $\sim 2$σ greater than the photometric value. Furthermore, this value must be considered a lower limit since the Na ID doublet of SN 2012cu appears to be close to saturation.

SN 2012et is included in the sample of Maguire et al. (2013) in which an Na ID2 equivalent width is quoted from a mid-resolution spectrum. The corresponding Poznanski et al. (2012) relation $E(B-V) \sim 1$σ greater than expected.

Table 11. Equivalent width values of Na ID, the DIB feature at $\lambda 5780$ Å and Mg II at $\lambda 2796$ Å for which reddening parameters can be inferred from Poznanski et al. (2012), Phillips et al. (2013) and Ménard et al. (2008), respectively. Upper limits are determined for Mg II measurements, since the doublet is blended in the STIS spectra. In the case of SN 2014J, the Na ID equivalent width extrapolates the relation by Poznanski et al. (2012) beyond any reasonable value for $E(B-V)$. Best photometric $E(B-V)$ values have been taken from Table 9 for comparison and the $E(B-V)$ for 2011fe and 2011by is assumed to be negligible.

<table>
<thead>
<tr>
<th>SN</th>
<th>Na ID1 (mÅ)</th>
<th>Na ID2 (mÅ)</th>
<th>$E(B-V)$ (Na ID)</th>
<th>DB 5780 (mÅ)</th>
<th>$A_V$ (mag)</th>
<th>Mg II 2796 (Å)</th>
<th>$E(B-V)$ (Phot.)</th>
</tr>
</thead>
<tbody>
<tr>
<td>2014J</td>
<td>2558 (6)</td>
<td>2831 (9)</td>
<td>–</td>
<td>344 (4)</td>
<td>1.8 (0.9)</td>
<td>$\leq 1.4$ (0.8)</td>
<td>$3.5 (0.2)$</td>
</tr>
<tr>
<td>2012cg</td>
<td>700 (9)</td>
<td>1018 (8)</td>
<td>1.6$^{+0.4}_{-0.3}$</td>
<td>85 (5)$^a$</td>
<td>0.4 (0.2)</td>
<td>$\leq 3.5$ (0.2)</td>
<td>$0.11 (0.02)$</td>
</tr>
<tr>
<td>2012cu</td>
<td>849 (3)$^b$</td>
<td>925 (3)$^b$</td>
<td>1.7$^{+0.4}_{-0.3}$</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>0.99 (0.03)</td>
</tr>
<tr>
<td>2012et</td>
<td>–</td>
<td>650 (40)$^c$</td>
<td>0.3$^{+0.3}_{-0.1}$</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>0.16 (0.02)</td>
</tr>
<tr>
<td>2011Fe</td>
<td>27.4 (1.1)$^d$</td>
<td>47.1 (0.8)$^d$</td>
<td>0.017$^{+0.004}_{-0.003}$</td>
<td>–</td>
<td>2.9 (0.2)</td>
<td>0.06$^{+0.03}_{-0.02}$</td>
<td>–</td>
</tr>
<tr>
<td>2011by</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>$\leq 2.3$ (0.2)</td>
<td>$\leq 0.04$ (0.02)</td>
<td>–</td>
<td>–</td>
</tr>
</tbody>
</table>

Note. Equivalent width values retrieved from $^a$Phillips et al. (2013), $^b$Sternberg et al. (2014), $^c$Maguire et al. (2013) and $^d$Patat et al. (2013).
It is clear from Phillips et al. (2013) that Na I D do not serve as good reddening proxies for SNe Ia and that the scatter in the Poznanski et al. (2012) relation is underestimated. This appears to be the case for SNe with high reddening, such as 2014J, as well as low reddening such as 2012cg. Furthermore, many of the Na I D profiles do not appear to be optically thin, implying that the column densities are rather underestimated, which would further increase the discrepancy between the Poznanski et al. (2012) relation and observations. There is thus motivation to investigate other ISM species, such as e.g. Mg II, which are more difficult to observe and have not been studied in large samples so far.

STIS spectra of SNe 2014J (from Foley et al. 2014), 2012cg, 2011fe and 2011by\(^7\) around the Mg II doublet at \(\lambda 2796, 2803 \text{ Å}\) are shown in Fig. 17. The absorption features can be used to test the relation

$$E(B - V) = (0.008 \pm 0.001) W(1.88 \pm 0.17)$$

of Ménard et al. (2008), where \(W\) is the equivalent width of Mg II at \(\lambda 2796 \text{ Å}\). The STIS spectra of SNe 2012bl, 2012bm, 2012cp and 2012et are not included in the sample due to the low signal to noise around the Mg II doublet. Upon visual inspection of Fig. 17, one can see that the Mg II lines are deep for all four SNe and the line ratios obtained from fitting a double Gaussian profile further indicate that the lines are not optically thin. In all STIS spectra, except those of 2011fe, the Mg II doublet is strongly blended. Further, it cannot be excluded that the entire absorption is attributed to the Milky Way. We therefore measure the total equivalent width of the observed features and consider 2/3 of the value to be the upper limit of the component at \(\lambda 2796 \text{ Å}\). The fraction is chosen from the line ratio of the Mg II doublet, if it is optically thin. The limits we obtain along with the corresponding \(E(B - V)\) computed from the relation above are shown in Table 11. The Mg II doublet is resolved better in the 2011fe STIS spectra and the equivalent width can be determined from the Gaussian fits more accurately. The value presented in Table 11 is the average equivalent width computed from all available 2011fe STIS spectra. In comparison to the photometric \(E(B - V)\), the Ménard et al. (2008) relation clearly underestimates the reddening of 2014J, whereas no firm conclusions can be drawn for the other SNe due to the large errors and since blending with Milky Way features cannot be excluded.

### 6.5 The origin of SN reddening

While it can be expected that the observed SN Ia colour arise from a mixture of extinction by dust and intrinsic SN Ia colour diversity, the latter is typically of order \(|\Delta(B - V)| \lesssim 0.1\) (e.g. N08). Thus, we can assume that the impact of dimming by dust will dominate with increased observed reddening and that the fitted extinction laws will be less susceptible to intrinsic SN Ia variations. It is therefore particularly interesting to compare the fits for SNe 2012cu and 2014J. They are the reddest objects in our sample, and at the same time, show very different total-to-selective extinction, \(R_V = 2.8 \pm 0.1\) and \(R_V = 1.4 \pm 0.1\) for SNe 2012cu and 2014J, respectively.

The evidence for material in the line of sight is strengthened by the fact that both SNe show deep Na I D absorption lines in their spectra (e.g. Sternberg et al. 2014; Goobar et al. 2014, for 2012cu and 2014J, respectively). Since CS dust is expected to give rise to steep extinction laws, such a scenario may offer an explanation for the low \(R_V\) of SN 2014J. However, no time-variability has been found for the Na I D absorption lines for any of the SNe we studied, although Graham et al. (2015b) report a detection of time-varying K I absorption for SN 2014J. When combined with the non-varying Na I D, these findings point to CS dust at radii of \(r_{\text{dust}} \gtrsim 10^{19} \text{ cm}\) due to the difference in ionization energies. The detection of light echoes (Crots 2015) also points to the existence of dust at a comparable distance from the site of the explosion, 11 pc, i.e. \(r_{\text{dust}} \sim 3 \times 10^{19} \text{ cm}\).

Further, we have studied the PSF shape of SN 2014J in the HST A14 photometry to search for signs of dust at smaller radii but none could be detected, which is consistent with the lack of time-evolution of the SN 2014J colours with respect to SN 2011fe. For CS dust at \(r_{\text{dust}} \gtrsim 10^{19} \text{ cm}\) the photon time-delay exceeds the typical time-scale of the SN Ia light curve and no colour time-evolution is expected as discussed in Amanullah & Goobar (2011).

Other observations suggesting that the nature of the extinction of SN 2014J is primarily interstellar, is that the polarization angle of the SN light is well aligned with the spiral structure of the host galaxy (Patat et al. 2015), the lack of thermal emission from the SN environment in near and mid-IR (Johansson et al. 2014), and that the velocities of the observed multiple Na I D lines are consistent with measured H I velocities along the line of sight in the host galaxy (Ritchey et al. 2015). The latter is also the case for SNe 2012cu (Haynes et al. 2000). Even if dust does exist at \(r_{\text{dust}} \sim 10^{19} \text{ cm}\) this is not expected to have any major impact on the measured \(R_V\) for such large distances (Wang 2005).

If the reddening of both SNe 2012cu and 2014J are dominated by interstellar extinction, the dust properties along the two lines of sight must be significantly different, and the dust in M82 must be of a nature that has not been observed in the Milky Way (although see Brown et al. 2015, for a possible explanation). M82 is a starburst galaxy, and the dust properties have been studied by Hutton et al. (2014). They find that a steep Milky Way-like law is preferred over the Calzetti (2001) law, used for starburst galaxies and they derive a wavelength dependence of the scattering within a central projected radius of \(<3 \text{ kpc}\) that suggests that ‘only small grains are entrained in the inner SN-driven wind’, which is consistent with both the location (see Table 1) and the characteristic of the observed reddening of SN 2014J.

\(^7\) STIS spectra of SNe 2011fe and 2011by were taken as part of Programme GO-12298; PI: Ellis.
Table 12. Surface brightness (mag/arcsec) measured using a 2 kpc radius centred on the SN position in the GALEX FUV and NUV filters.

<table>
<thead>
<tr>
<th>SN</th>
<th>FUV</th>
<th>NUV</th>
</tr>
</thead>
<tbody>
<tr>
<td>2014J</td>
<td>26.5 (0.2)</td>
<td>24.9 (0.1)</td>
</tr>
<tr>
<td>2012bm</td>
<td>26.7 (6.1)</td>
<td>25.9 (2.4)</td>
</tr>
<tr>
<td>2012cg</td>
<td>25.1 (0.4)</td>
<td>24.4 (0.2)</td>
</tr>
<tr>
<td>2012cp</td>
<td>24.7 (1.3)</td>
<td>24.6 (0.7)</td>
</tr>
<tr>
<td>2012cu</td>
<td>26.6 (1.0)</td>
<td>24.9 (0.2)</td>
</tr>
<tr>
<td>2012et</td>
<td>24.9 (2.6)</td>
<td>24.4 (1.2)</td>
</tr>
<tr>
<td>2012bl</td>
<td>26.1 (3.3)</td>
<td>26.2 (2.1)</td>
</tr>
</tbody>
</table>

For SNe Ia, Rigault et al. (2013) found that when using Hα emission as a tracer for ongoing star formation, SNe with local Hα emission is on average redder and more homogeneous, resulting in a lower brightness dispersion. These results have been confirmed by Kelly et al. (2015) and Rigault et al. (2015) using UV data from the Galaxy Evolution Explorer (GALEX). If the low RV originates from small dust grains in regions undergoing intense star formation, we can expect to observe different local properties between SNe 2012cu and 2014J. In Table 12, we present the surface brightness at the position of the SNe using an aperture with a 2 kpc radius. From this we cannot draw any firm conclusion based on the local UV surface brightness of the host galaxies. Even after we attempt to correct for host galaxy dust, following the recipe used in Rigault et al. (2015), we see no correlation with UV surface brightness and measured RV.

In Fig. 18, we show the fitted F99 parameters from Table 5 for all SNe together with similar measurements from the literature. Low values of RV are not unique for SNe Ia, and has also been observed in the line of sight of other light sources such as gamma-ray burst afterglows (Fynbo et al. 2014) and quasi-stellar objects (QSO; e.g. Fynbo et al. 2013; Leighty et al. 2014). From the figure, it is apparent that there are several observations with low-RV values for high-extinction SNe Ia, while SN 2012cu is both showing high extinction and a relatively high RV. For low-extinction SNe it is by nature difficult to measure RV for individual objects, but there are several statistical studies that obtain higher (RV ≤ 3) average values of RV compared to what is observed for high-extinction SNe Ia (e.g. Chotard et al. 2011; Mandel, Narayan & Kirshner 2011).

The UV observations allow us to improve the sensitivity on RV for individual low-reddened SNe, and it is interesting to note that we measure RV discrepancies similar to what we saw for high-extinction objects. The colours of SNe 2012cg and 2012et are however a mixture of intrinsic variation as was shown by the comparison of SN 2012cg with SNe 2011by and 2011fe in particular. For these objects, we therefore cannot draw any firm conclusions to what extent the measured RV is solely a dust property. Note though that there are strong indications of dust along the line of sight for these SNe from Na ID absorption (as we have seen for SN 2012cu and for SN 2012et in Maguire et al. 2013). Independent of the origin of the reddening we conclude that our sample of reddened SNe Ia with well observed colours, although limited, suggests that a range of RV values can be expected for both low and high-reddened SNe Ia.

Given the findings of M13 that all ‘NUV-blue’ SNe belong to the photospheric NV class while the ‘NUV-red’ consists of both NV and HV SNe and the colour–velocity relation for B − V (Wang et al. 2009), we can also compare the derived extinction parameters with the measured Si II λ6355 Å velocities. From Figs 12 and 18, we conclude that both SNe for which we measure a low RV (2014J and 2012et) are classified as HV SNe while the remaining belong to the NV class. This is consistent with the statistical study of samples of SNe Ia by Wang et al. (2009), although our sample size does not allow us to draw firm conclusions. However, the fact that we present SNe with both high and low values of RV in both high- and low-extinction environments argues against that the origin of the discrepancy in observed reddening laws is solely due to intrinsic SN properties.

One possible explanation to both of these findings could be that HV SNe primarily explode in environments with low RV dust. Wang et al. (2013) and Pan et al. (2015) have shown that HV SNe are, on average, both located in more luminous hosts, and in brighter regions, closer to their host nuclei, compared to the corresponding NV samples. Further, the results from Hutton et al. (2014) showed that a steep Milky Way law is preferred for the central region of M82, and similarly the extinction towards the Galactic bulge also follows a steeper extinction curve (RV ≃ 2.5 Nataf et al. 2013) compared to the Milky Way average. Both the dust and SN Ia properties are likely to be affected by the environment where they are produced and if HV SNe Ia originate from younger and more metal-rich progenitors than NV SNe Ia (Wang et al. 2013), it is possible that the average dust properties in the two environments are different as well.

Studies of high-redshift SNe for cosmological applications are unlikely to include highly reddened SNe like 2012cu and 2014J, but objects with similar reddening to SNe 2012cg and 2012et are common. In Fig. 19, we show the normalized colour excesses, E(X − V)/E(B − V), for the three least reddened SNe, where we have used the approach from Fig. 7 to obtain the plotted wavelengths. Fig. 19 also shows the average reddening F99 law and the SALT2 colour law (Guy et al. 2007b) which has been empirically derived without attempting to discriminate between the different sources of SN reddening. Plotted here is the version used in the cosmology analysis from Betoule et al. (2014). Although the reddening laws are
consistent at wavelengths covered by the $B$–$R$ bands, the SALT2 law starts to diverge from the data in the UV, wavelengths that becomes increasingly important when SNe Ia at high redshifts are studied. The lack of understanding SN reddening is one of the dominating astrophysical systematic uncertainties when SNe Ia are used for cosmology (see e.g. Amanullah et al. 2010; Sullivan et al. 2011; Suzuki et al. 2012; Betoule et al. 2014) and further UV studies are needed in order to discriminate between different sources of reddening.

7 SUMMARY AND CONCLUSIONS

In this work, we have presented and analysed broad-band photometry of seven SNe Ia covering the wavelength range 0.2–2 $\mu$m, obtained mainly from HST, Swift and the NOT.

All SNe are found to be normal with respect to their light curves and optical spectroscopic properties. The SNe have colour excesses in the range $E(B-V)=0.0$–1.4 mag and we have studied the reddening properties by comparing them to the normal pristine SNe Ia, 2011fe and 2011by. In particular, we have explored three different extinction laws: O'Donnell (1994), F99, and Goobar (2008).

We have further studied the time-evolution of the fitted reddening laws and tested the consistency over a broad wavelength range. For the one SN, 2012cg, we do find indications of time-evolution of the bluest colours and we have investigated if this could be explained by CS dust. Further, we have also searched for time-varying absorption features, in particular Na I D, for SN 2012cg in multi-epoch high-resolution spectroscopy. The high-resolution spectra were also used to estimate the extinction along the line of sight using the absorption of Na I D and Mg II as dust proxies. The validity of using SN 2011fe as a colour template was discussed and compared to the resulting reddening parameters when using SN 2011by.

We summarize the main findings as follows.

(i) We observe a diversity in extinction properties characterized by a total-to-selective extinction, $R_V$, ranging from $R_V \approx 1.4$ to $R_V \approx 3$.

(ii) The diversity between the fitted reddening laws for different SNe is significantly greater than the discrepancy between the laws for a single SN. Although, we do find that the empirical F99 law provides a better fit for SNe with $R_V \sim 3$ while a power law is preferred for the low-$R_V$ SN 2014J.

(iii) For the two reddest SNe, both with $E(B-V)>1$ mag, we observe significantly different values of $R_V$ with $R_V = 2.8 \pm 0.1$ and $R_V = 1.4 \pm 0.1$, for SN 2012cu and 2014J, respectively. Based on their Na I D profiles being consistent with the observed H I velocity fields in their host galaxies, the lack of thermal emission and the observed polarization being aligned with the host galaxy plane for SN 2014J, we conclude that the reddening is likely dominated by extinction in the ISM of the host galaxy. Further, pre-existing CS dust at radii $r_{\text{dust}} < 10^{19}$ cm is expected to give rise to evolution of the colour excesses, $E(X-V)$, but this is not observed for either SN 2012cu nor SN 2014J.

(iv) We compare nebular spectra of SNe 2011fe, 2012cg and 2014J and conclude that all three are very similar at epochs $>280$ d from maximum, with SNe 2011fe and 2012cg being remarkably similar.

(v) We compare the STIS spectra at maximum of SNe 2011by, 2011fe and 2012cg and conclude that while SN 2012cg is well matched to both SNe at $\lambda > 3800$ Å it is better matched to SN 2011by at shorter wavelengths.

(vi) For SN 2012cg we observe time-evolution in $E(uvw2-V)$ with respect to SN 2011fe, but when the object is compared to SN 2011by the evolution is less significant. CS dust at $r_{\text{dust}} \sim 10^{17}$ cm is consistent with $E(uvw2-V)$ but disfavoured by the lack of evolution of the redder colours. However, this example illustrates that observations over a wide wavelength range provides a powerful tool for separating the origin of colour excess evolution of SNe Ia.

(vii) For low-reddening SNe such as SN 2012cg, adding UV data to optical and near-IR can decrease the statistical uncertainty of $R_V$ by $>50$ per cent.

(viii) The two SNe with low $R_V$ are found to have the highest Si II velocities at maximum which is consistent with previous studies (Wang et al. 2009).

(ix) By measuring the equivalent width from absorption of Na I, we confirm the results of Phillips et al. (2013), and find that the extinction derived for SNe 2012cg, 2012cu and 2012et using the Poznanski et al. (2012) relation is higher than what we observe directly for these objects.

Future studies, including a larger sample of low-reddening objects covering a wide range in host galaxy morphologies, will be necessary to robustly estimate the impact of the diversity in the wavelength dependence of reddening on the estimates of cosmological parameters from SNe Ia. The current work, clearly showing that there is significant range in the extinction parameters, and possibly also extinction laws, should motivate further multiwavelength studies of SNe Ia, also including the UV.

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APPENDIX A: SUMMARY OF SNe STUDIED IN THIS WORK

The seven SNe Ia that we study in this work are briefly summarized below.

(i) SN 2012bl was discovered by the Chilean Automatic Supernova Search 42.9 arcsec east and 14.6 arcsec north of the centre of the galaxy ES0 234-19 on March 26.38 UT from an unfiltered image (Pignata et al. 2012). A spectrum (Prieto et al. 2012) was obtained with the 2.5 m du Pont telescope at the Las Campanas Observatory on March 27.28 UT and object was classified as an SN Ia using SNID (Blondin & Tonry 2007).

(ii) SN 2012bm, located 10.95 arcsec west and 10.4 arcsec north of the centre of the galaxy UGC 8189, was discovered on March 27 by Puckett et al. (2012). A spectrum was obtained on Mar. 28.05 UT and it was classified (Cappellaro et al. 2012) as an SN Ia using GELATO (Harutyunyan et al. 2008).

(iii) SN 2012cg was discovered (Kandrashoff et al. 2012) by the Lick Observatory Supernova Search (Filippenko et al. 2001) on May 17.220 UT. The redder than normal SN was located 17.3 arcsec east and 1.5 arcsec south (Cenko et al. 2012) of the centre of the Virgo Cluster member NGC 4424 in a region with many blue stars and disturbed dust lanes. Graur & Maoz (2012) used pre-explosion HST images of this well-studied galaxy to rule-out most supergiants as possible binary companions for the progenitor scenario.

(iv) SN 2012cp was discovered 6.7 arcsec east and 1.2 arcsec south of the centre of UGC 8713 on May 23.2 UT by the Puckett Observatory Supernova Search (Cox et al. 2012). Milisavljevic (2012) and Zhang, Wu & Wang (2012) obtained spectroscopy of the object on May 25.3 and 25.7 UT, respectively, and reported that it was consistent with an SN Ia before maximum.

(v) SN 2012cu was discovered on June 14.6 UT by Itagaki et al. (2012) 3.1 arcsec east and 27.1 arcsec south of the nucleus of the galaxy NGC 4772 and later classified as an SN Ia by Marion et al. (2012). Pre-explosion Chandra observations are available of the host galaxy and were used by Nielsen, Voss & Nelemans (2013) to constrain the X-ray emission from the progenitor scenario.

(vi) SN 2012et, located 5.3 arcsec east and 0.8 arcsec north of the centre of MCG +04-55-47, was discovered by Rich et al. (2012) on September 12.057 UT, and later classified on September 13.80 UT as a high-velocity SNe Ia (Dennefeld et al. 2012).

(vii) SN 2014J was discovered by Fossey et al. (2014) in the nearby galaxy M82 on January 21.805 UT, and later classified by Cao, Kasliwal & McKay (2014). The SN was located 4 arcsec west and 21 arcsec south of the ill-defined nucleus of the host galaxy.

APPENDIX B: A SPECTRAL AND COLOUR MODEL FROM SN 2011fe

SN 2011fe is a normal SN Ia with excellent temporal and wavelength coverage with negligible extinction along the line of sight and is therefore a suitable object for reddening studies. In A14, we used the available UV–NIR spectroscopic time series (Pereira et al. 2013; Mazzali et al. 2014) and the NIR light curves (Matheson et al. 2012) to derive the extinction law of SN 2014I. In this work, we extend this template with UV photometry (Brown et al. 2012) and optical photometry at 25 to 40 d past B-maximum.

The light curves in the UV F225W, F275W, F336W and the optical BVRi bands are first constructed by synthesizing the spectra from Mazzali et al. (2014) and Pereira et al. (2013). A light curve for each filter is then obtained by fitting smoothed splines using SNOOPY (Burns et al. 2011). For the redder optical R and i bands, the sparse temporal coverage after 20 d past B-maximum does not allow an accurate spline fit of the second bump. We therefore also use the data from Munari et al. (2013) to constrain the spline fit at >25 d past B-max. For the Swift/UVOT uvw2 filter and the NIR JHKs we fit spline models to the measured light curves from Brown et al. (2012) and Matheson et al. (2012), respectively. The light curves are then used to calculate the (X − V)0 colours shown in Fig. 5.

As explained in Section 4, we also need a template of the spectral energy density of the unreddened object in order to be able to calculate the expected extinction for each passband for a given extinction model. In A14 the extinction for a given set of reddening law parameters was first calculated for all available spectra of SN 2011fe and the extinction for any given epoch was then obtained using spline interpolations. Similar to the light-curve spline model, this approach is adequate for the UV, but due to the sparse spectral coverage, it will cause the model to deviate from the light curve for the redder optical bands and NIR at >25 d past maximum. In A14 this did not affect the final results due to the high extinction of SN 2014J and the conservative intrinsic colour dispersions adopted in the analysis.

In this work, we have developed a more accurate SED template by first resampling the spectral time series used in A14 to a resolution of 10 Å, which are shown as the red spectra in Fig. B1. These were then used to calculate the missing wavelength and temporal elements through linear interpolation (shown in grey in Fig. B1), and finally the full matrix is mangled to match the light curves described above. The mangling was carried out by first calculating the ratio between the light-curve fluxes and the corresponding synthetic SED fluxes. A function was then setup for each phase where the calculated ratios were adopted for the effective wavelengths of the filters. For all wavelengths shorter (longer) than the bluest (reddest) point, the function was assumed to take the same value as in the extreme points, while we interpolate the function value for all intermediate wavelengths, using the calculated ratios. The SED for the given phase was then multiplied by the function.

The difference between the synthetic colours calculated from the mangled SED and the spline colour model was always found to be within <0.05 mag for all epochs, and often even smaller. In Fig. B2 these differences are shown for six different colours. Since these differences are within the adopted intrinsic colour uncertainties they will not have any significant impact on the fitted reddening laws.
APPENDIX C: A MODEL FOR THE UV OF SN 2011by

The SNe 2011by and 2011fe have been found to be remarkably similar in the optical, both around maximum and at nebular phases, while showing significant discrepancies in the UV (Foley & Kirshner 2013; Graham et al. 2015a). In Fig. 14, the ratio between the spectra are shown at maximum to illustrate this. Unfortunately, SN 2011by does not have the wavelength and temporal coverage that SN 2011fe has, but we can create a crude template for SN 2011by based on the assumption that it is indeed identical to SN 2011fe with the exception of the UV wavelengths.

In Fig. 14 the solid green line is showing the function

$$f(x') = c \left( \frac{x'}{(x'^4 + 1)^{1/4}} - 1 \right) + 1 \text{ with } x' = \frac{x - x_0}{\alpha}, \quad (C1)$$

where $x$ is the wavelength given in microns. In the figure, the function is plotted for the parameters $x_0 = 0.2495$, $\alpha = 0.0360$ and $c = 0.3359$.

SN 2011by was observed by Swift in the UV (M13) and in the optical (Silverman et al. 2013b), and the colour excesses of these measurements with respect to SN 2011fe are shown in Fig. C1. Here, we note that $E(uvm2 - V)$ is showing a similar time-evolution as was seen for SN 2012cg in the upper-left panel of Fig. 6.

Under the assumption that SNe 2011by and 2011fe are twins at wavelengths $\lambda > 3000 \text{ Å}$ we can create an approximate template for SN 2011by by multiplying the SED of SN 2011fe, presented in Appendix B and shown in Fig. B1, by equation (C1). Further, if we fix the parameters $x_0$ and $\alpha$ to the values given above, we can fit $c$ for each epoch with $uvm2$ observations by forcing the synthetically calculated $A_{uvm2}$, based on the SED to match the observed $E(uvm2 - V)$ in Fig. C1 (again, assuming that $V^{2011fe} = V^{2011by}$).

The fitted values of $c$ are shown in Fig. C2 and the synthetic values of $A_{uvm2}$ that these values correspond to are been plotted as black dots in Fig. C1.

Further, we parametrize $c(p)$ with a Gaussian,

$$c(p) = \frac{a}{\sqrt{2\pi}\sigma} \exp \left[ -\frac{1}{2} \left( \frac{p - p_0}{\sigma} \right)^2 \right] + b,$$

where $p$ is the phase in days, $p_0$ is the maximum light, and $a$, $\sigma$, and $b$ are parameters to be determined.

Figure B2. Examples of the difference between synthetic colours calculated from the SED template, and the corresponding colours from the light-curve spline templates.
The time-dependent $c$ of SN 2011by by using the template of SN 2011fe from Section B photometry. The solid line is showing a Gaussian fit.

Figure C1. The difference in colour between SNe 2011by and 2011fe, where the ground-based photometry has been adopted from Silverman et al. (2013b). Observations for which the colour was obtained from measured $V$-band data are shown with filled symbols, while values obtained from a $V$-band template are shown with open symbols. The colour difference between the SNe can also be calculated synthetically based on equation (C1) under the assumption that this function describes the flux ratio of the two objects, for all epochs, after adjusting for the difference in distance. This is motivated by the observation that these SNe appear to be twins at all wavelengths except for the UV. The parameter $c$ in the equation was fitted by matching the synthetic and measured $uvm2 - V$ for each epoch, where the former is shown by the black points for the best fitted values.

Figure C2. The fitted values of parameter $c$ in after the SED of SN 2011fe has been fitted together with equation (C1) to match SN 2011by $uvm2$ photometry. The solid line is showing a Gaussian fit.

as shown by the solid line in Fig. C2, with $p_0 = -0.939$, $a = 1.406$, $b = 0.211$ and $\sigma = 4.992$.

To summarize, we create a crude light curve and SED template of SN 2011by by using the template of SN 2011fe from Section B and multiply it with equation (C1), where the parameters, including the time-dependent $c$, are given above.

APPENDIX D: RED TAILS OF THE HST FILTERS

The HST filter transmission used in this work, shown in the upper panel of Fig. D1, suffer from red tails. That is, part of the flux observed for an object in these filters originates from wavelengths that are redder than the range where most of the transmission lies. As mentioned in A14, the red tails are relatively small for the WFC3/UVIS filters, e.g. the transmission of $F225W$ is roughly one part in 100,000 at 5000 Å compared to the peak transmission at $\sim 2250$ Å. Despite this, the red tails will have implications when reddened SNe Ia are studied. For example, from spectrophotometry of SN 2011fe at maximum (thin blue line in the middle panel of Fig. D1), we conclude that $\sim 0.5$ per cent of the flux (dashed blue line) in the $F225W$ filter will originate from wavelengths $> 4000$ Å. However, extinction will suppress the UV-flux significantly and after applying an F99 reddening law with $E(B-V) = 1.4, R_V = 1.4$, $\sim 60$ per cent of the $F225W$ flux (thick blue line) comes from photons with $\lambda > 4000$ Å.

Another way to illustrate the effect of the red tails is shown in the lower panel of Fig. D1, where the solid lines show the effective median wavelengths for an observation of SN 2011fe at maximum through the HST filters with various amounts of reddening applied. The effective median wavelength is defined such that 50 per cent of the light originates from redder and bluer wavelengths, respectively. Further, the wavelength range defined by the points where 10 per cent and 90 per cent of the light comes from bluer wavelengths (i.e. the region that includes 80 per cent of the light) is shown for increasing reddening. From the figure we conclude that, $F275W$ and $F336W$ are less plagued by red tails than $F225W$, where the latter, in fact, will be probing redder effective wavelengths of the SN spectrum than the two former filters for $E(B-V) \gtrsim 1$ mag.

The fact that we are comparing different effective wavelengths when calculating the colour excess between a reddened and unreddened source is true for all broad-band observations. However, fitting extinction properties based on filters with red tails that span a wavelength range where the SED drops rapidly, also puts demands on knowing the passband throughput accurately even when the transmission drops several orders of magnitude as for the filters in Fig. D1.

The expected WFC3/UVIS passband red tails were tested (Brown 2011) in the final round of thermal vacuum tests of WFC3 prior to launch. They studied the filter throughputs in four wavelength bins centred on 450, 600, 750 and 900 nm and found deviations of up to $\sim 40$ per cent between the measured and expected transmission. If the deviations are taken as an estimate of the throughput uncertainty at these wavelengths, we can evaluate its impact on the extinction analysis.

We carried out this test by first applying an F99 reddening law with $E(B-V) = 1.4, R_V = 1.4$ to the SED of SN 2011fe described in Section 4.1. The impact on the calculated extinction for the two bands $F225W$ and $F275W$ (the test of $F336W$ was not carried out due to limitations in the setup as described in Brown 2011) can then be calculated. We do this by comparing synthetic magnitudes from the original SYNPHOT throughputs, to magnitudes obtained after the filters have been multiplied by a spline function derived from the deviations for the four wavelength bins mentioned above. The impact on the calculated extinction was found to always be $< 0.05$ mag.

Further, the worst case scenario can be estimated by letting all the measured deviations from Brown (2011) maximize the amount of red light entering the filter. The result on the extinction from this was $< 0.10$ mag for $t < 20$ d with respect to $B$ max and 0.15–0.20 mag
Diversity in extinction laws for SNe Ia

Figure D1. The upper panel shows the filter transmissions, $T_{x}(\lambda)$, of the WFC3/UVIS passbands, multiplied with an arbitrary normalization, $C$. The thin blue line in the middle panel shows the spectrum of SN 2011fe at $B$ band maximum, while the dashed blue line shows the same spectrum after it has been multiplied by the $F225W$ throughput. The thick blue line shows the same spectrum after it has been reddened with an F99 extinction law with $E(B-V) = 1.4$ mag and $R_V = 1.4$, similar to what we observe for SN 2014J. All three spectra have arbitrary normalization, $C$. In the plot, we have also marked the wavelength region from which 80 per cent of the light originates from, defined such that 10 per cent of light comes from bluer wavelengths, and 10 per cent comes from redder wavelengths. The lower panel shows the median wavelength, i.e. where 50 per cent of the light originates from redder and bluer wavelengths, for three passbands for SN 2011fe at $B$ maximum, reddened with an F99 extinction law ($R_V = 1.4$) with increasing extinction. The 80 per cent region is shown in the same manner as for the middle panel.

for $t = 20–40$ d, which is still within the dispersion that we have adopted for the intrinsic UV colours.

It is also possible to investigate the accuracy of the full HST/WFC3/UVIS SYNPHOT throughput by comparing spectrophotometry of objects, with known spectra, to WFC3/UVIS photometry. This is in fact the most direct test we can carry out of our method for fitting extinction laws since this is using the very same procedure. In Fig. D2, we have plotted stars from CALSPEC,\footnote{http://www.stsci.edu/hst/observatory/crds/calspec.html} with the corresponding UVIS-photometry using the same analysis path as in Section 2.1 with a 0.4 arcsec radius. The agreement is in general more than sufficient for the purpose of this analysis, but it is unfortunate that data are not available for redder stars for which the impact of the red tail can be expected to be more significant. The star P330E should be discarded from the comparison since this star has been used for calibrating the WFC3/UVIS system.

However, we can carry out the same test for the reddened SNe Ia that have been observed with both STIS and WFC3/UVIS. In Table D1, we present spectrophotometry at maximum for SNe 2012cg and 2014J, using the transmissions of the WFC3/UVIS filters, compared to the corresponding WFC3/UVIS photometry.

Table D1. Spectrophotometry of STIS spectra at maximum of SNe 2012cg and 2014J at maximum using the filter transmissions shown in Fig. D1 compared to WFC3/UVIS photometry of the same objects. For SN 2012cg the observations were obtained in consecutive HST orbits, while the data for SN 2014J was taken 1 d apart. For this SN, we have calculated the magnitude difference synthetically from the SN 2011fe spectra described in Section 2.1 with a 0.4 arcsec radius. The agreement is in general more than sufficient for the purpose of this analysis, but it is unfortunate that data are not available for redder stars for which the impact of the red tail can be expected to be more significant. The star P330E should be discarded from the comparison since this star has been used for calibrating the WFC3/UVIS system.

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2014J, the spectrum and photometry were obtained on consecutive
days, and the magnitudes based on the former were correct to cor-
respond to the WFC3/UVIS epoch using the SN 2011fe template.
These corrections are < 0.1 mag.

For these two SNe, the discrepancies between two instruments
are within 0.1 mag, including F225W. This is the filter with the
most significant red tails, and the photon wavelength distribution
for F225W is significantly different for two SNe. The consistency
between spectrophotometry and WFC3/UVIS photometry for two
SNe that define the end points of the reddening range in our study
is showing that any errors of the filter transmissions will not affect
the conclusions drawn in the paper.

Further, the fact that we also observe a discrepancy of ∼0.1 mag
for the F336W filter, which has minor red tails, suggests that the
discrepancies we observe for F225W may not necessarily originate
from uncertainties of these.

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