Dust formation in Milky Way-like galaxies

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ABSTRACT
We introduce a dust model for cosmological simulations implemented in the moving-mesh code AREPO and present a suite of cosmological hydrodynamical zoom-in simulations to study dust formation within galactic haloes. Our model accounts for the stellar production of dust, accretion of gas-phase metals on to existing grains, destruction of dust through local supernova activity, and dust driven by winds from star-forming regions. We find that accurate stellar and active galactic nuclei feedback is needed to reproduce the observed dust–metallicity relation and that dust growth largely dominates dust destruction. Our simulations predict a dust content of the interstellar medium which is consistent with observed scaling relations at $z = 0$, including scalings between dust-to-gas ratio and metallicity, dust mass and gas mass, dust-to-gas ratio and stellar mass, and dust-to-stellar mass ratio and gas fraction. We find that roughly two-thirds of dust at $z = 0$ originated from Type II supernovae, with the contribution from asymptotic giant branch stars below 20 per cent for $z \gtrsim 5$. While our suite of Milky Way-sized galaxies forms dust in good agreement with a number of key observables, it predicts a high dust-to-metal ratio in the circumgalactic medium, which motivates a more realistic treatment of thermal sputtering of grains and dust cooling channels.

Key words: dust, extinction – galaxies: evolution.

1 INTRODUCTION
Dust in the interstellar medium (ISM) exists alongside gas-phase metals and alters the dynamic and spectroscopic properties of galaxies (Calzetti, Kinney & Storchi-Bergmann 1994; Silva et al. 1998; Dey et al. 1999; Calzetti et al. 2000; Netzer et al. 2007; Spoon et al. 2007; Melbourne et al. 2012). The surfaces of dust grains play host to a range of chemical reactions that subsequently influence the behaviour of the ISM and impact star formation (Hollenbach & Salpeter 1971; Mathis 1990; Li & Draine 2001; Draine 2003). Additionally, observations suggest that dust is a significant contributor of metals in the circumgalactic medium (CGM; Bouché et al. 2007; Peeples et al. 2014; Peek, Ménard & Corrales 2015). Understanding the life cycle of dust grains, including their production in asymptotic giant branch (AGB) stars and supernovae (SNe; Gehrz 1989; Todini & Ferrara 2001; Nozawa et al. 2003; Ferrarotti & Gail 2006; Nozawa et al. 2007; Zhukovska, Gail & Trieloff 2008; Nanni et al. 2013; Schneider et al. 2014), growth via accretion of gas particles in the ISM and coagulation with other dust particles (Draine 1990; Dominik & Tielens 1997; Dwek 1998; Hirashita & Kuo 2011), destruction via thermal sputtering, collisions with other dust grains, and SN shocks (Draine & Salpeter 1979a,b; McKee 1989; Jones, Tielens & Hollenbach 1996; Bianchi & Ferrara 2005; Yamasawa et al. 2011), and other physical processes, is important in accurately modelling dust evolution.

Even at high redshift, galaxies can form substantial masses of dust. Far-infrared and submillimetre observations show that some dust-rich galaxies and quasars out to $z \sim 7$ have dust masses greater than $10^7 M_\odot$ (Hughes, Dunlop & Rawlings 1997; Bertoldi et al. 2003; Fan et al. 2003; Venemans et al. 2012; Casey, Narayanan & Cooray 2014; Riechers et al. 2014; Watson et al. 2015). Two notable examples are SDSS J1148+5251, a $z = 6.4$ quasar with an inferred dust mass of $(3.4^{+1.38}_{-1.24}) \times 10^8 M_\odot$ (Valiante et al. 2009, 2011), and A1689-zD1, a $z = 7.5 \pm 0.2$ galaxy with a dust mass of $4 \times 10^7 M_\odot$ and a dust-to-gas ratio comparable to the Milky Way value (Watson et al. 2015). To produce such large dust masses at high redshift, average SNe must yield roughly $1 M_\odot$ of dust, a quantity larger than the amount of dust SNe have been observed to condense (Todini & Ferrara 2001; Sugerman et al. 2006; Dwek, Galliano & Jones 2007; Lau et al. 2015). However, these dusty examples may not be representative of typical high-redshift galaxies. There is recent evidence of actively star-forming galaxies at $z > 6.5$ with little dust obscuration (Walter et al. 2012; Kanekar et al. 2013; Ouchi et al. 2013), and observations suggest that dust extinction is generally decreased in low luminosity and high-redshift systems (Bouwens et al. 2012). Our current understanding of dust formation at high redshift is therefore still quite incomplete.

Significant variation in dust properties also exists at low redshift. The Galactic dust-to-gas ratio is roughly $10^{-2}$ (Gilmore, Wyse &
Kuijken 1989; Sodroski et al. 1997; Zubko, Dwek & Arendt 2004) and several times larger than the values observed for the Large and Small Magellanic Clouds (Pei 1992; Gordon et al. 2014; Roman-Duval et al. 2014; Tchernevshyov et al. 2015). In contrast, the metal-poor local dwarf galaxy I Zwicky 18 has been estimated to have a dust mass of no more than 1800 M⊙, and a corresponding dust-to-gas ratio in the range of (3.2–13) × 10^−6, several orders of magnitude below the typical values expected for larger systems (Fisher et al. 2014). Additionally, observations and models of the ISM indicate that the nature of dust can differ among individual chemical species (Wilms, Allen & McCray 2000; Kimura, Mann & Jessberger 2003; Jenkins 2009).

The current sample of galaxies with reliable dust estimates has grown in recent years, driven by programmes like SINGS (Kennicutt et al. 2003; Draine et al. 2007), the Herschel Reference Survey (Boselli et al. 2010), the Herschel ATLAS (Eales et al. 2010), KINGFISH (Kennicutt et al. 2011), and the Dwarf Galaxy Survey (Madden et al. 2013). Various trends and scaling relations involving dust and host galaxy properties have been observed from this data. There is a positive correlation between dust-to-gas ratio and metallicity (Vladilo 1998; Draine et al. 2007; Galametz et al. 2011; Rémy-Ruyer et al. 2014; Zahid et al. 2014). However, the detailed behaviour of the dust–metallicity relation is unclear. Observations indicate that the dust-to-gas ratio is reduced at low metallicity, possibly due to effects in the interstellar radiation field that limit dust growth and enhance destruction processes (Rémy-Ruyer et al. 2014). Even over small metallicity ranges, there is pronounced scatter in the dust-to-gas ratio.

The observed dust–metallicity relation implies a dust-to-metal ratio that is fairly constant across a range of galaxy morphologies and histories. However, the nature of the dust-to-metal ratio at high redshift and low metallicity is uncertain. Recent work using gamma-ray bursts has yielded dust-to-metal ratios fairly consistent with the Local Group, even in low-metallicity systems (Zafar & Watson 2013; Sparre et al. 2014). This would require SNe to be efficient producers of dust or grains to grow rapidly in the ISM (Mattsson et al. 2014). Separate analysis of gamma-ray burst damped Lyman α absorbers suggests a non-universal dust-to-metal ratio, with low-metallicity environments producing dust less efficiently than spiral galaxies (De Cia et al. 2013). Even in the Milky Way, observations of strong gas-phase depletion (Roche & Aitken 1985; Sembach & Savage 1996; Jenkins 2004, 2009) contrast the expectation that dust destruction outpaces stellar injection of dust (Barlow 1978; Draine & Salpeter 1979b; Dwek & Scalo 1980; McKee 1989; Jones et al. 1994, 1996). Understanding the balance between gas-phase metals and dust in Milky Way-sized systems requires more work.

A number of other empirical scaling relations have emerged, tying observed dust masses to various galactic properties. These include relations between dust-to-stellar mass ratio and gas fraction (Cortese et al. 2012), dust-to-stellar mass ratio and redshift (Dunne et al. 2011), dust extinction and stellar mass (Zahid et al. 2014), dust mass and gas mass (Corbelli et al. 2012), dust mass and star formation rate (SFR; da Cunha et al. 2010), and dust surface density and radial distance (Ménard et al. 2010; Pappalardo et al. 2012). Observational data have also yielded initial estimates of the dust mass function for low and high redshift (Dunne et al. 2000, 2011). These scaling relations provide constraints on galaxy formation models that include a treatment of dust.

A variety of numerical models have been used in previous work to better understand how dust evolves in a galaxy. These include one- and two-zone models (Dwek 1998; Lisenfeld & Ferrara 1998; Hirashita & Ferrara 2002; Inoue 2003; Morgan & Edmunds 2003; Calura, Pipino & Matteucci 2008; Valiante et al. 2009; Gall, Andersen & Hjorth 2011b; Yamasawa et al. 2011; Asano et al. 2013a; Zhukovskya 2014; Feldmann 2015), semi-analytic methods (Somerville et al. 2012; Mancini et al. 2015), and more recently first smoothed-particle hydrodynamical simulations resolving local dust variations (Bekki 2013, 2015b). These models include processes like the formation of dust during stellar evolution, dust growth and destruction in the ISM, radiation field effects, and dust-enhanced molecular formation. Many of these one-zone models have addressed the formation of dusty high-redshift quasars and have indicated that if dust is unable to condense efficiently in SNe, a high star formation or accretion efficiency is needed to produce large dust masses at z > 5 (Morgan & Edmunds 2003; Michalowski et al. 2010; Gall, Hjorth & Andersen 2011a; Gall, Andersen & Hjorth 2011c; Michalowski 2015).

Numerical dust models have also focused on the evolution of the dust-to-gas and dust-to-metal ratios, often used in observations to characterize galaxies. The dust–metallicity relation is reproduced in many one-zone models (Issa, MacLaren & Wolfendale 1990; Lisenfeld & Ferrara 1998). These models predict a dust-to-metal ratio that is independent of metallicity in galaxies where SNe are the primary producers of dust (Morgan & Edmunds 2003), and whose radial gradient in galactic discs can be used to estimate interstellar dust growth (Mattsson, Andersen & Munkhammar 2012). The evolution of the dust-to-metal ratio may vary significantly with time, with the dust-to-metal ratio at z ≳ 2 possibly just 20 per cent of the present value (Inoue 2003). Interestingly, galaxies are predicted to switch from low to high dust-to-metal ratio when crossing a critical metallicity threshold that enables efficient ISM dust growth (Zhukovskya et al. 2008; Inoue 2011; Asano et al. 2013a; Feldmann 2015). Previous one-zone dust models applied to the formation of a single galaxy show present day dust-to-metal ratios of roughly 0.5 (Dwek 1998) and 0.9 (Calura et al. 2008), with results significantly dependent on the strength of dust growth and destruction mechanisms in the ISM. These models also find depletion roughly constant across all chemical species. However, the biggest weakness of these one-zone models is their lack of spatial resolution, limiting their ability to make predictions about the distribution of dust within a galaxy.

Cosmological simulations provide a better means to understand how dusty systems can form at high redshift and how their dust content, both in the ISM and CGM, evolves in time. Additionally, simulations of full cosmological volumes can provide the sample size of galaxies needed to corroborate observed scaling relations involving dust. Recent cosmological hydrodynamical simulations have suggested that heavily dust-attenuated galaxies can form even at z ∼ 7, with ultraviolet and optical colours consistent with a model having a dust-to-metal ratio of 0.4 (Kimm & Cen 2013). Motivated by the observed reddening of background quasars by foreground galaxies in Sloan Digital Sky Survey (SDSS) data (Ménard et al. 2010), smoothed-particle hydrodynamical simulations found that half of this reddening signal is attributable to dust more than 100 h^−1 kpc from the closest massive galaxy (Zu et al. 2011). Radial gradients of the dust-to-gas ratio in galactic discs appear to be steeper for larger galaxies (Bekki 2015b). Even in simulations where dust is not directly treated, radiative transfer post-processing can be used to infer dust extinction (Jonsson 2006; Narayanan et al. 2010; Hayward et al. 2013; Yajima et al. 2014). The dynamics of grain sputtering in SN shocks can also be studied using tracer particles (Silvia, Smith & Shull 2010). While some studies have investigated the impact of feedback mechanisms, such as winds driven by SNe, on the cosmological evolution of dust (Zu et al. 2011; Bekki 2015b), much work still remains.
In this work, we incorporate essential dust physics into a moving-mesh simulation code and, for the first time in studies of dust, use a large sample of zoom-in cosmological initial conditions. Compared to previous dust models using one-zone methods and idealized initial conditions, our approach has the ability to resolve the structure of dust within a galaxy and the impact that local feedback processes have on dust evolution. While some smoothed-particle hydrodynamical simulations have treated dust without using zoom-in cosmological initial conditions, our highest resolution cosmological run offers improved mass resolution.

This paper is structured as follows. In Section 2, we discuss the theory and numerical implementation of our dust model in the context of a larger galaxy formation framework. Details of the cosmological initial conditions for our simulations are provided in Section 3. We analyse the importance of physical feedback processes, individual dust model components, and variations in simulation initial conditions in Section 4. Finally, in Section 5, we summarize our results and discuss the implications of our findings on future observations.

2 METHODS

We employ cosmological simulations to track the evolution of dust and its effect on galaxy dynamics. We briefly review the core components of the galaxy formation model currently implemented in the moving-mesh code AREPO (Springel 2010), which have been detailed in prior work (Vogelsberger et al. 2013) and used for various cosmological studies (Vogelsberger et al. 2012, 2014a,b; Genel et al. 2014; Torrey et al. 2014), and then describe the new dust physics we have added. AREPO uses a dynamic Voronoi tessellation to solve the equations of ideal hydrodynamics with a finite-volume method. A second-order Godunov scheme is used in conjunction with an exact Riemann solver to compute fluxes between cells. Additionally, gravitational and collisionless physics have been implemented using methods similar to the TREEPM scheme in the smoothed-particle hydrodynamics code GADGET (Springel 2005).

2.1 Galaxy formation and feedback mechanisms

The current galaxy model in AREPO accounts for a number of physical processes, including primordial and metal-line gas cooling, stellar evolution and subsequent chemical enrichment of the ISM, black hole formation, and stellar and active galactic nuclei (AGN) feedback, which together yield a galaxy stellar mass function in good agreement with observations over 0 < z < 3 (Genel et al. 2014; Torrey et al. 2014). The star formation prescription stochastically creates star particles in dense regions of ISM gas, with masses distributed according to a Chabrier (2003) initial mass function (IMF). As stars evolve off of the main sequence, mass is recycled to the neighbouring ISM. This chemical enrichment routine follows nine elements (H, He, C, N, O, Ne, Mg, Si, and Fe). We adopt elemental mass yields and recycling fractions for AGB stars from Karakas (2010), SNe II from Portinari, Chiosi & Bressan (1998), and SNe Ia from Thielemann et al. (2003). We employ a stellar lifetime function from Portinari et al. (1998). Galactic outflows are modelled using wind particles launched from star-forming ISM gas and temporarily decoupled from hydrodynamics to emulate a galactic fountain driven by stellar feedback (Springel & Hernquist 2003). We include the minor feedback modifications detailed in Marinacci, Pakmor & Springel (2014), which alter radio-mode AGN feedback and adopt warm galactic winds.

2.2 Dust evolution

A wide variety of dust models have been used in recent galaxy formation simulations, though essentially all models track both the formation of dust during stellar evolution and its subsequent evolution in the ISM. The most simplistic of these models take a one-zone approach, solving a set of coupled ordinary differential equations for the time evolution of the total mass of gas, metals, and dust within a galaxy (Hirashita & Ferrara 2002; Inoue 2003; Morgan & Edmunds 2003; Calura et al. 2008; Valiante et al. 2009; Gall et al. 2011b; Yamasawa et al. 2011; Asano et al. 2013a; Zhukovska 2014; Feldmann 2015). Other work assumes a two-component galaxy model, consisting of a bulge and disc region and allowing for local dust properties to be studied as a function of radial distance from the galactic centre (Dwek 1998). More recently, Bekki (2013, 2015b) has performed smoothed-particle hydrodynamical simulations that treat dust locally and offer improved spatial resolution.

In this work, we focus on the dominant dust production and evolution mechanisms. We leave additional processes, such as the catalysis of molecular hydrogen on dust grains and the effect of interstellar radiation fields, to future efforts. We track the mass of dust in each chemical species within individual gas cells. Dust is passively advected between gas cells when solving the hydrodynamic equations in each time step, in essence adopting a two-fluid approach with dust fully coupled to gas. However, dust is not implemented as a strictly passive tracer: as shown below, dust impacts metal-line cooling and in turn star formation and gas dynamics. Alternative treatments, including ‘live’ dust particles decoupled from gas and subject to frictional or radiative forces (Kwok 1975; Draine & Salpeter 1979a; Barsella et al. 1989; Theis & Orlov 2004; Bekki 2015a), may be pursued in future work.

2.2.1 Dust production via stellar evolution

During the stellar evolution process described in Section 2.1, a certain amount of the mass $\Delta M_i$ of species $i$ evolved by stars and returned to neighbouring gas cells in some time step is assumed to condense into dust, with the exception of H, He, N, and Ne. The remaining metal mass exists in the gas phase. In the framework below, we follow the approach used by Dwek (1998) and other subsequent works that track individual chemical elements. Most notably, we adopt a different functional form for the amount of dust produced during mass return from AGB stars than from SNe. Additionally, we make a distinction between AGB stars with $C/O > 1$ in their stellar envelope, which are expected to produce carbonaceous solids (e.g. graphite or amorphous carbon), and those with $C/O < 1$, which are thought to form primarily silicate dust (Draine 1990). In essence, the equations below describe elemental mass yields for dust, computed as a function of the yields for overall metals returned by stars.

For AGB stars with a carbon-to-oxygen ratio of $C/O > 1$ in their returned mass, the amount of species $i$ dust produced is given by

$$\Delta M_{i,dust} = \begin{cases} \delta_{C}^{AGB,C/O>1} (\Delta M_C - 0.75 \Delta M_0) & \text{if } i = C \\ 0 & \text{else,} \end{cases}$$

where $\delta_{C}^{AGB,C/O>1}$ is the carbon condensation efficiency for AGB stars with $C/O > 1$, discussed below in more detail. Similarly, for
AGB mass return with C/O < 1, the mass of species i dust formed is

$$\Delta M_{i,dust} = \begin{cases} 
0 & \text{if } i = C \\
10 \sum_{j=M,Fe} \delta_{i,j} \Delta M_j / \mu_j & \text{if } i = O \\
\delta_{i,j} \Delta M_j & \text{else},
\end{cases}$$

(2)

where $\mu_i$ is the mass in amu and $\delta_{i,j}$ is the condensation efficiency for species i in AGB stars with C/O < 1. Finally, the mass of dust for element i produced via SNe ejecta is

$$\Delta M_{i,dust} = \begin{cases} 
\delta_{SN} \Delta M_C & \text{if } i = C \\
10 \sum_{j=M,Fe} \delta_{SN,j} \Delta M_j / \mu_j & \text{if } i = O \\
\delta_{SN,j} \Delta M_j & \text{else},
\end{cases}$$

(3)

where the dust condensation efficiency of element i for SNe is $\delta_{SN}$, which may differ from the corresponding efficiency for AGB stars. Equation (3) and its condensation efficiencies are used for both SNe Ia and II, consistent with all aforementioned models. Additionally, we note that the numerical prefactor for the calculation of $\Delta M_{i,dust}$ in equations (2) and (3) is slightly reduced from that given in Dwek (1998). We have found that this minor modification is necessary for oxygen, whose dust production is tied to the ejecta of heavier elements, in order to avoid the formation of more oxygen dust than total oxygen mass returned. We use different stellar nucleosynthesis yields than in Dwek (1998), and even though there is considerable uncertainty in the condensation efficiencies, we demonstrate in Section 4.3 that our results are insensitive to moderate changes in these prefactors. The range of condensation efficiencies that we explore is described in Section 3.2.

Within each gas cell, we separately track the mass of dust produced by AGB stars, SNe Ia, and SNe II, motivated by a desire to understand the dominant channels of dust production at high redshift. Additionally, we refer to carbon grains as graphite dust, and the dust in remaining species as silicate dust. While a simplification that fails to distinguish the full diversity of compounds that comprise dust grains, including polycyclic aromatic hydrocarbons, this division has been adopted in similar studies and is a step towards analysing the underlying ISM chemistry (Tielens & Allamandola 1987; Dwek 1998; Weingartner & Draine 2001).

### 2.2.2 Interstellar dust growth

The mass of dust in the ISM may increase over time, as gas-phase elements collide with existing grains (Draine 1990). To model the accretion of dust grains in the ISM, we follow the prescription of Dwek (1998) and Hirashita (1999) and in every time step compute each cell’s instantaneous dust growth rate

$$\left( \frac{dM_{i,dust}}{dt} \right)_i = \left( 1 - \frac{M_{i,dust}}{M_{i,metal}} \right) \left( \frac{M_{i,dust}}{\tau_g} \right),$$

(4)

where $M_{i,dust}$ is the cell’s mass of species i dust, summed over components originating from AGB stars, SNe Ia, and SNe II, $M_{i,metal}$ is the corresponding species i metal mass, and $\tau_g$ is a characteristic growth time-scale. Note that the first factor in parentheses induces a growth rate that depends on the local dust-to-metal ratio and slows the accretion rate as gas-phase metals are condensed into dust (Dwek & Scalo 1980; McKee 1989).

Previous studies have explored accretion time-scales dependent upon local gas density and temperature (Yoza & Bekki 2014; Zhitkovskaya 2014; Bekki 2015b) as well as metallicity (Inoue 2003; Asano et al. 2013a) in an attempt to better match the observed dust–metallicity relation. Following these prescriptions, for each gas cell, we compute the local dust growth time-scale

$$\tau_g = \tau_g^\text{ref} \left( \frac{\rho^\text{ref}}{\rho} \right) \left( \frac{T^\text{ref}}{T} \right)^{1/2},$$

(5)

where $\rho$ and $T$ are the density and temperature of the gas cell, $\rho^\text{ref}$ and $T^\text{ref}$ are reference values for density and temperature in molecular clouds, and $\tau_g^\text{ref}$ is an overall normalization influenced by factors like atom–grain collision sticking efficiency and grain cross-section (see section 2.2. of Hirashita 2000 for a detailed derivation). We take $\rho^\text{ref}$ to be 1 H atom cm$^{-3}$ and $T^\text{ref} = 20$ K. This growth time-scale is shortest in dense gas where collisions are more frequent than in the diffuse halo. Future efforts will need to more accurately model atom–grain collisions, taking into account a possibly temperature-dependent collision sticking efficiency and a realistic grain size distribution (Li & Draine 2001; Weingartner & Draine 2001).

### 2.2.3 Grain destruction

Dust grains that have formed in the ISM can subsequently be destroyed through a number of processes, including shocks from SN remnants (Seab & Shull 1983; Seab 1987; Jones et al. 1994), thermal and non-thermal sputtering (Draine & Salpeter 1979a; Tielens et al. 1994; Caselli, Hurtquist & Haves 1997), and grain–gas collisions (Draine & Salpeter 1979b; Jones et al. 1996). In particular, shocks reduce the net efficiency of dust formation in SNe, expected to be the primary producers of dust at high redshift. The mass of grains destroyed in such a manner is thought to be proportional to the energy of the shocks (McKee 1989).

Paralleling equation (4), for every active cell we can estimate the local dust destruction rate for species i as

$$\left( \frac{dM_{i,dust}}{dt} \right)_d = - \frac{M_{i,dust}}{\tau_d},$$

(6)

where $\tau_d$ is a characteristic destruction time-scale (McKee 1989; Draine 1990; Jones & Nuth 2011) and again the dust mass is computed by summing its components originating from AGB stars, SNe Ia, and SNe II. While we could tie $\tau_d$ to the galaxy-wide SN rate (Hirashita & Ferrara 2002) or the radially dependent gas surface density and SN rate (Calura et al. 2008), we instead estimate a dust destruction time-scale on a cell-by-cell basis, given by

$$\tau_d = \frac{M_g}{\epsilon \gamma M(100)},$$

(7)

where $M_g$ is the gas mass within a cell, $\epsilon$ denotes the efficiency with which grains are destroyed in SN shocks, $\gamma$ is the local Type II SN rate, and $M(100)$ is the mass of gas shocked to at least 100 km s$^{-1}$ (Dwek & Scalo 1980; Seab & Shull 1983; McKee 1989). We take $\epsilon = 0.3$, though there is a range of physically plausible values used in previous work. Applying the Sedov–Taylor solution to a homogeneous environment yields

$$M(100) = 6800 E_{SNII}^{51} \left( \frac{v_s}{100 \text{ km} \text{s}^{-1}} \right)^{-2} M_\odot,$$

(8)

where $E_{SNII}^{51}$ is the energy released by a Type II SN in units of 10$^{51}$ erg, and $v_s \sim 100 \text{ km} \text{s}^{-1}$ is the shock velocity (McKee 1989). Equation (8) implicitly assumes SN shock expansion into...
a homogeneous medium of \( n = 0.13 \text{ cm}^{-3} \), corresponding to the star formation density threshold in our model. We employ a fixed ISM density when calculating \( M_\text{f}(100) \) because the detailed ISM multiphase structure and, in particular, the ambient gas density around each SN are not resolved in our simulations. In any case, we caution that this destruction prescription neglects thermal sputtering and grain–grain collisions in the CGM and thus may overdeplete gas-phase metals in the diffuse halo.

During every time step, the net dust growth rate in every active gas cell is computed by combining equations (4) and (6), and this rate is used to update the local dust mass. When performing this update, we keep the relative proportions of dust mass originating from AGB stars, SNe Ia, and SNe II constant.

Additionally, the amount of dust in the ISM is reduced when star particles are created. We assume that dust and gas-phase metals are distributed uniformly within each gas cell, so that each star particle’s metals come from gas-phase and dust sources in the same proportion as in the ISM. For example, if a star particle is created from a cell in which 25 per cent of oxygen exists as dust and 75 per cent exists in the gas phase, then the amount of gas-phase oxygen lost by the cell is three times greater than the amount of oxygen dust lost. Other schemes to consume dust during star formation may be possible but more challenging to implement.

### 2.2.4 Dust effects on cooling

The galaxy formation model highlighted in Section 2.1 calculates gas cooling rates using contributions from primordial species, metals and Compton cooling. In particular, the metal-line cooling rate is assumed to scale linearly with the gas-phase metallicity (see equation 12 in Vogelsberger et al. 2013). The depletion of metals on to dust grains will decrease the gas-phase metallicity of the ISM and therefore reduce metal-line cooling.

Observations suggest that dust cooling channels can explain the formation of very metal-poor stars (Caffau et al. 2011; Klessen, Glover & Clark 2012), and modelling finds that cooling-induced fragmentation of dust impacts low-metallicity star formation (Schneider et al. 2006; Tsuribe & Omukai 2006; Dopcke et al. 2013). In numerical work, the temperature of dust grains can be computed via thermal equilibrium calculations accounting for atomic line emission, grain photoelectric effect heating, heating of dust through external radiation fields, and dust cooling through thermal emission (Krumholz, Leroy & McKee 2011). Dust may affect cooling rates computed in cosmological simulations using local ionizing radiation (Cantalupo 2010; Gnedin & Hollon 2012; Kannan et al. 2014). In hot gas with temperatures above \( 10^7 \text{ K} \), cooling from ion–grain collisions is expected to be strong (Ostriker & Silk 1973). For simplicity of our model, we neglect dust cooling channels in this first study.

While our model does not currently implement any specific dust cooling processes, metal-line cooling will be reduced in comparison with previous simulations involving AREPO’s galaxy formation physics. Decreased cooling will in turn have a dynamical effect on galaxy formation, lowering the SFR. Future inclusion of dust cooling channels may weaken some of the dynamical effects seen in this work.

### 2.2.5 Winds from stellar feedback

We employ the non-local stellar feedback implementation from Vogelsberger et al. (2013) with some modification for dust. In this feedback prescription, gas cells in star-forming regions of the ISM are stochastically converted into wind particles, given a velocity

\[
v_w = \kappa_w \sigma_{1D} \Omega_0 \]

where \( \kappa_w \) is a dimensionless scale and \( \sigma_{1D} \) is the local one-dimensional dark matter velocity dispersion, and allowed to move without hydrodynamic constraints.

When wind particles recouple to the gas, they deposit their metals, both gas-phase and dust, in the same proportion as the ISM from which they were launched. Thus, these stellar winds help carry metals and drive outflows away from dense regions of the ISM. In Section 4.2, we investigate the importance of these winds and their strength in distributing dust throughout a galaxy.

### 3 COSMOLOGICAL RUNS

#### 3.1 Initial conditions

The initial conditions for our runs consist of the Aquarius suite of haloes, previously used for high-resolution cosmological studies of Milky Way-sized structure (Springel et al. 2008). All runs adopt the \( \Lambda \text{CDM} \) cosmological parameters \( \Omega_m = \Omega_{\text{dm}} + \Omega_b = 0.25 \), \( \Omega_b = 0.04 \), \( \Omega_{\Lambda} = 0.75 \), \( \sigma_8 = 0.9 \), \( n_s = 1 \), and Hubble constant \( H_0 = 100 h \text{ km s}^{-1} \text{ Mpc}^{-1} = 73 \text{ km s}^{-1} \text{ Mpc}^{-1} \), which were employed in the Millennium and Millennium-II suites of simulations (Springel et al. 2005; Boylan-Kolchin et al. 2009). Though recent results from the Wilkinson Microwave Anisotropy Probe (Hinshaw et al. 2013) and Planck satellite (Planck Collaboration XVI 2014) suggest, for example, a value of \( h < 0.73 \), we choose to adopt these parameters in part to remain consistent with recent hydrodynamical simulations also utilizing the Aquarius suite of haloes in AREPO (Marinacci et al. 2014).

The Aquarius haloes are labelled with the letters A through H, and each is simulated in a periodic box of side length 100 \( h^{-1} \text{ Mpc} \). In Aquarius nomenclature, our main simulations were performed using level 5 initial conditions. In addition, we simulated the Aquarius C halo using higher and lower resolution initial conditions, levels 4 and 6, respectively, in order to study the convergence properties of the fiducial dust model. We have found our dust model to be well converged and use the highest resolution initial conditions for some visualizations in this work. The Aquarius C halo, which we also use to study variations in dust and feedback physics, was adopted in the Aquila comparison project (Scannapieco et al. 2012) to analyse the results of a wide range of cosmological hydrodynamical codes. This halo has a fairly quiescent merger history, especially at low redshift (Wang et al. 2011). We also note that Marinacci et al. (2014) applied this galaxy formation model without dust to the Aquarius haloes and found robust convergence over these same resolution levels.

The same gravitational softening length was used for gas, dark matter, and stars, and it was kept constant in comoving units until \( z = 1 \), with a maximum value in physical units of 680 pc for the high-resolution region using level 5 initial conditions. The maximum values for levels 4 and 6 initial conditions were factors of 2 lower and higher, respectively. The \( z = 1 \) softening length was then used down to \( z = 0 \). We employ the SUBFIND algorithm (Springel et al. 2001) for determining gravitationally bound structure and substructure.

In Table 1, we provide basic statistics on these haloes, computed at \( z = 0 \) using the fiducial model described below. We provide two computations of the gas and dust masses: \( M_{\text{gas}} \) and \( M_{\text{dust}} \), which are summed over all cells in the halo, and \( M_{\text{gas, disc}} \) and \( M_{\text{dust, disc}} \), which include contributions only from dense ISM gas cells and estimate
the gas and dust content of the galactic disc. We isolate ISM gas by filtering cells according to temperature $T$ and density $\rho$ using the relation
\[
\log \left( \frac{T}{[K]} \right) < 6 + 0.25 \log \left( \frac{\rho}{10^{10} [M_\odot h^{-2} \text{kpc}^{-3}]} \right),
\]
which has been shown to remove cells in the hot halo (see equation 1 in Torrey et al. 2012). Additionally, Table 1 indicates the number and mass resolution of gas and dark matter cells in each halo.

### 3.2 Fiducial parameters

In Table 2, we present the set of parameter values that comprise our fiducial dust model. The fiducial feedback parameters are similar to those used in Vogelsberger et al. (2013), with $E_{\text{SNII}} = 1.09$ and $\delta_m = 3.0$, and we did not retune the feedback model after including dust. Given that dust depletion will affect cooling rates and star formation, future feedback modifications may be required. This highlights the need to include dust in detailed galaxy formation models.

The fiducial dust condensation efficiencies follow those from Dwek (1998) and assume that a certain fraction of ejecta from an AGB star or SN exists as dust, with the remainder occupying the gas phase. These efficiencies are allowed to vary among species, since AGB stars and SNe are thought to produce dust of differing compositions (Ferrarotti & Gail 2006; Zhukovska et al. 2008). For example, the high and low values of $\delta_{\text{C}}$ and $\delta_{\text{SN}}$, respectively, are motivated by the idea that carbon-rich AGB stars are the dominant producers of carbonaceous grains. We caution that the condensation efficiencies used for SNe Ia are high given recent observations and modelling work that suggest dust forms inefficiently in SNe Ia (Nozawa et al. 2011; Gomez et al. 2012). However, as shown in Section 4, SNe Ia produce only about 10 per cent of the dust in a galaxy, and so our results are not very sensitive to the condensation efficiencies for SNe Ia.

While condensation efficiencies of the form described in Section 2.2.1 have also been adopted in more recent simulations (Calura et al. 2008; Bekki 2013), stellar models have begun to analyse the composition of ejected dust as a function of a star’s mass and metallicity (Ferrarotti & Gail 2006; Bianchi & Schneider 2007; Zhukovska et al. 2008; Nanni et al. 2013; Schneider et al. 2014). For example, low-metallicity AGB stars are thought to produce very low amounts of silicate grains (Ferrarotti & Gail 2006). Also, some of these recent models track dust grains for SiC, Al$_2$O$_3$, or other compounds that do not map neatly on to our chemical evolution model. While we do not adopt condensation efficiencies that vary with mass or metallicity, we can still compare the dust masses predicted by our stellar yield tables and condensation efficiencies with...

### Table 1. Basic data on all eight Aquarius haloes simulated using level 5 initial conditions and the fiducial dust model detailed in Section 3.2. Additionally, we show the same statistics for the Aquarius C halo simulated at levels 4 and 6. To keep consistent with the naming convention adopted later in this work, runs are referred to by their halo letter (A through H), resolution levels (4, 5, or 6), and the suffix ‘FI’ to denote that the fiducial dust physics were used. Here, the virial radius $R_{200}$ is the radius about the halo’s potential minimum enclosing a density 200 times greater than the critical density. We list the gas, dark matter, and dust masses using all cells within the halo, denoted $M_{\text{gas}}$, $M_{\text{dm}}$, and $M_{\text{dust}}$, respectively. Here, $M_{\text{gas, disc}}$ and $M_{\text{dust, disc}}$ are the estimated gas and dust masses in the galactic disc, computed using only dense ISM gas cells as determined by the temperature–density phase space cut in equation (10). Finally, we indicate the number of gas and dark matter cells in the halo and their respective mass resolutions.

<table>
<thead>
<tr>
<th>Run</th>
<th>$R_{200}$ (kpc)</th>
<th>$M_{\text{gas}}$ ($10^8 M_\odot$)</th>
<th>$M_{\text{dm}}$ ($10^8 M_\odot$)</th>
<th>$M_{\text{dust}}$ ($10^6 M_\odot$)</th>
<th>$M_{\text{gas, disc}}$ ($10^8 M_\odot$)</th>
<th>$M_{\text{dust, disc}}$ ($10^6 M_\odot$)</th>
<th>$N_{\text{gas}}$</th>
<th>$N_{\text{dm}}$</th>
<th>$m_{\text{gas}}$ ($10^9 M_\odot$)</th>
<th>$m_{\text{dm}}$ ($10^9 M_\odot$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>A5:FI</td>
<td>237.5</td>
<td>11.62</td>
<td>182.29</td>
<td>5.61</td>
<td>4.52</td>
<td>3.79</td>
<td>211 527</td>
<td>690 478</td>
<td>5.03</td>
<td>26.40</td>
</tr>
<tr>
<td>B5:FI</td>
<td>183.0</td>
<td>4.22</td>
<td>78.18</td>
<td>3.48</td>
<td>1.37</td>
<td>1.82</td>
<td>119 386</td>
<td>518 981</td>
<td>3.35</td>
<td>17.59</td>
</tr>
<tr>
<td>C5:FI</td>
<td>233.5</td>
<td>11.11</td>
<td>175.93</td>
<td>5.98</td>
<td>3.47</td>
<td>3.47</td>
<td>253 836</td>
<td>814 834</td>
<td>4.11</td>
<td>21.59</td>
</tr>
<tr>
<td>D5:FI</td>
<td>240.7</td>
<td>15.18</td>
<td>195.56</td>
<td>12.20</td>
<td>6.12</td>
<td>7.66</td>
<td>319 074</td>
<td>846 419</td>
<td>4.40</td>
<td>23.10</td>
</tr>
<tr>
<td>E5:FI</td>
<td>206.7</td>
<td>6.14</td>
<td>114.16</td>
<td>5.35</td>
<td>1.09</td>
<td>1.00</td>
<td>179 039</td>
<td>652 270</td>
<td>3.33</td>
<td>17.50</td>
</tr>
<tr>
<td>F5:FI</td>
<td>208.0</td>
<td>9.26</td>
<td>113.67</td>
<td>9.48</td>
<td>3.58</td>
<td>5.55</td>
<td>375 068</td>
<td>942 365</td>
<td>2.30</td>
<td>12.06</td>
</tr>
<tr>
<td>G5:FI</td>
<td>201.9</td>
<td>9.94</td>
<td>95.99</td>
<td>7.78</td>
<td>5.20</td>
<td>5.74</td>
<td>317 798</td>
<td>769 854</td>
<td>2.83</td>
<td>14.88</td>
</tr>
<tr>
<td>H5:FI</td>
<td>180.1</td>
<td>2.61</td>
<td>76.24</td>
<td>1.60</td>
<td>0.20</td>
<td>0.34</td>
<td>87 369</td>
<td>588 050</td>
<td>2.96</td>
<td>15.56</td>
</tr>
<tr>
<td>C4:FI</td>
<td>232.5</td>
<td>6.82</td>
<td>159.19</td>
<td>3.89</td>
<td>1.44</td>
<td>1.76</td>
<td>1265 814</td>
<td>589 234</td>
<td>0.51</td>
<td>2.70</td>
</tr>
<tr>
<td>C6:FI</td>
<td>235.6</td>
<td>13.92</td>
<td>179.84</td>
<td>6.91</td>
<td>4.97</td>
<td>4.54</td>
<td>39 592</td>
<td>104 118</td>
<td>32.90</td>
<td>172.73</td>
</tr>
</tbody>
</table>

### Table 2. Fiducial dust model parameters. The dust condensation efficiencies regulate the fraction of metal ejecta for a chemical species that condenses into dust, as outlined in Section 2.2.1. The reference growth time-scale $\tau_{\text{ref}}$ influences the rate at which gas-phase metals deplete on to dust grains, and $E_{\text{SNII}}$ controls the energy per SN II, which in turn affects grain destruction in SN shocks.

<table>
<thead>
<tr>
<th>Variable</th>
<th>Fiducial value</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\delta_{\text{AGB,C/O}=1}$</td>
<td>0.0 for $i = H$, He, N, O, Ne, Mg, Si, Fe, 1.0 for $i = C$</td>
<td>Dust condensation efficiency for species $i$ in AGB stars with C/O &gt; 1 in ejecta.</td>
</tr>
<tr>
<td>$\delta_{\text{AGB,C/O}&lt;1}$</td>
<td>0.0 for $i = H$, He, N, C, Ne, 0.8 for $i = O$, Mg, Si, Fe</td>
<td>Dust condensation efficiency for species $i$ in AGB stars with C/O &lt; 1 in ejecta.</td>
</tr>
<tr>
<td>$\delta_{\text{SN}}$</td>
<td>0.0 for $i = H$, He, Ne, N, 0.5 for $i = C$, 0.8 for $i = O$, Mg, Si, Fe</td>
<td>Dust condensation efficiency for species $i$ in SNe.</td>
</tr>
<tr>
<td>$\tau_{\text{ref}}$</td>
<td>0.2</td>
<td>Reference dust growth time-scale, in units of [Gyr].</td>
</tr>
<tr>
<td>$E_{\text{SNII}}$</td>
<td>1.09</td>
<td>Available energy per SN II, in units of [$10^{51}$ erg].</td>
</tr>
</tbody>
</table>
those from more detailed stellar models. In Table 3, we calculate the total dust masses condensed in our model for various choices of stellar mass and metallicity. We note that AGB stars produce total dust masses around $10^{-2}$–$10^{-3} \, M_\odot$ with no strong metallicity dependence, fairly consistent with stellar models (Zhukovska et al. 2008; Nanni et al. 2013).

We can also compare the results of Table 3 to predictions of dust masses condensed in SNe II, although we caution that this subject is debated in the literature. For SNe II with masses of 12 and $20 \, M_\odot$, we calculate condensed dust masses of roughly 0.4 and 0.8 $M_\odot$, respectively. In comparison, Todini & Ferrara (2001) predicted about 0.3 and 0.5 $M_\odot$ of dust for these choices of stellar mass. Our results are consistent with the estimate that between 2 and 5 per cent of a progenitor’s mass becomes dust in SNe II in the range $13 \, M_\odot \leq M \leq 40 \, M_\odot$ (Nozawa et al. 2003). However, there is some tension with observations: SN 2003gd, for example, was determined to have no more than 0.02 $M_\odot$ of dust (Sugerman et al. 2006; Meikle et al. 2007), and other SNe have failed to produce the amount of dust expected from models (Rho et al. 2008, 2009). As stellar models begin to implement more complex chemical reaction networks (e.g. Cherchneff 2010) and more observations are gathered, better constraints can be placed on the dust masses condensed in core-collapse SNe.

In the ISM, refractory grains are estimated to have destruction time-scales of $10^8$–$10^9$ yr, lower than the typical injection time of dust from stellar sources (Barlow 1978; Draine & Salpeter 1979b; Dwek & Scalo 1980; McKee 1989). Mechanisms that allow metals to recondense in the ISM and counter the destruction-injection imbalance are needed to regulate gas-phase abundances. The growth time-scale $\tau_g$ characterises dust growth in molecular clouds and the associated probability that a gas-phase metal atom will collide and stick to an existing grain (Draike 1990; Hirashita 2000). Just as we tie the dust destruction time-scale in each cell to its local SN rate, we adopt a growth time-scale dependent on local gas density and temperature that enables dust to grow more quickly in dense ISM gas. There is evidence that dust growth is particularly dominant over stellar dust production in galaxies above a certain critical metallicity (Inoue 2011; Asano et al. 2013a; Mancini et al. 2015), and other models have begun to explore the effect of density, temperature, and metallicity variations on local growth time-scales (Inoue 2003; Bekki 2015b). While models that employ variable growth time-scales sometimes assume a characteristic grain size, grain density, and atom collision sticking efficiency, increasing the number of estimated parameters, in this work we fixed such parameters at typical Galactic values in a manner similar to equation 12 in Hirashita (2000) in order to capture the essential density and temperature dependence in the growth time-scale. The resulting estimated reference time-scale $\tau_g^{\text{ref}}$ is shown in Table 2.

Table 4 lists the range of model variations that we consider in addition to the fiducial setting. These variations are divided into

### Table 4

<table>
<thead>
<tr>
<th>Name</th>
<th>Abbreviation</th>
<th>Physics</th>
</tr>
</thead>
<tbody>
<tr>
<td>Fiducial</td>
<td>FI</td>
<td>Fiducial dust parameters from Table 2, $\kappa_w = 3.0$, includes AGN feedback.</td>
</tr>
<tr>
<td>No feedback</td>
<td>NF</td>
<td>No stellar or AGN feedback.</td>
</tr>
<tr>
<td>AGN feedback</td>
<td>AF</td>
<td>Only AGN feedback.</td>
</tr>
<tr>
<td>Slow winds</td>
<td>SW</td>
<td>$\kappa_w = 1.85$.</td>
</tr>
<tr>
<td>Fast winds</td>
<td>FW</td>
<td>$\kappa_w = 7.4$.</td>
</tr>
<tr>
<td>Constant growth time-scale</td>
<td>CG</td>
<td>Uses growth time-scale of $\tau_g = 0.2 , \text{Gyr}$, ignores local density and temperature.</td>
</tr>
<tr>
<td>Constant destruction time-scale</td>
<td>CD</td>
<td>Uses destruction time-scale of $\tau_d = 0.5 , \text{Gyr}$, ignores local SN rate.</td>
</tr>
<tr>
<td>Low production</td>
<td>LP</td>
<td>All condensation efficiencies from Table 2 halved.</td>
</tr>
<tr>
<td>No growth</td>
<td>NG</td>
<td>No growth mechanism.</td>
</tr>
<tr>
<td>No destruction</td>
<td>ND</td>
<td>No destruction mechanism.</td>
</tr>
<tr>
<td>Production only</td>
<td>PO</td>
<td>No growth or destruction mechanisms.</td>
</tr>
<tr>
<td>Without dust</td>
<td>WD</td>
<td>No dust tracking, all metals exist in gas phase.</td>
</tr>
</tbody>
</table>

Dust formation in Milky Way-like galaxies

two categories: those that apply the fiducial dust model and vary the underlying feedback mechanisms, and those that adopt the fiducial feedback settings and explore the impact of the various dust processes. We also explore the fiducial feedback model without dust tracking. In this last model, all metals are assumed to exist in the gas phase and contribute to metal-line cooling. This model without dust is expected to produce larger SFRs and gas-phase metallicities.

These feedback and dust model variations, together with the range of Aquarius haloes used as initial conditions, provide a suitable starting point for understanding the impact of dust on cosmological galaxy formation simulations.

In the remainder of this paper, we refer to our runs using four-character identifiers: the first refers to the Aquarius halo chosen (i.e. one of A through H), the second denotes the resolution level of the initial conditions (i.e. 4, 5, or 6), and the last two indicate the underlying physical model using the abbreviations in Table 4. For example, C5:ND is shorthand for the simulation of the Aquarius C halo using level 5 initial conditions with no dust destruction mechanism.

4 RESULTS

4.1 Distribution of dust in the fiducial model

We first use our highest resolution simulation of the Aquarius C halo with fiducial dust and feedback physics to analyse the distribution of gas-phase metals and dust within the central halo and surrounding CGM. This is motivated by observations of significant amounts of dust in the CGM (Ménard et al. 2010; Peeples et al. 2014; Peek et al. 2015) and the fact that gas-phase metals may condense into dust in regions of low star formation. In Fig. 1, we show surface densities of baryons (Σ), gas-phase metals (Σgas-phase metal), and dust (Σdust) for face-on and edge-on views of the galactic disc at z = 2, 1, and 0. We also display the projected dust-to-metal ratio (Zdust/Z) at these redshifts, where Zdust denotes the mass fraction of dust and Z is the usual metallicity, including gas-phase metals and dust. This halo does not undergo any major mergers below z = 6 (Wang et al. 2011), and so these images capture the quiescent formation of a disc of diameter roughly 15 kpc.

At z = 2, dust is most concentrated in the galactic centre, with a surface density roughly an order of magnitude larger than that outside the disc. The surface densities of gas-phase metals and dust evolve in a similar fashion from z = 2 to 1 and largely trace the distribution of baryons. By z = 1, Σdust > 10⁻² M⊙pc⁻² extends out to around 25 kpc as dust grows on the edges of the galactic disc. The surface density of gas-phase metals in the CGM is largely unchanged from z = 2 to 1, with a dust-to-metal ratio below 0.1. The dust-to-metal ratio is largest near the galactic centre and several times higher than the typical value away from the disc. By z = 0, there is less variation between gas-phase metals and dust. The central disc, roughly 15 kpc across, has Σdust > 10⁻¹ M⊙pc⁻², and the dust-to-metal ratio remains highest in the star-forming central core where dust is produced. We caution that the absence of thermal sputtering in the diffuse halo may artificially cause dust-to-metal ratios to rise in the CGM.

These results indicate that dust depletion can affect the distribution of gas-phase metals, especially in regions where high star formation activity produces the most dust. To highlight the dust evolution in the inner galactic disc, in Fig. 2 we display zoomed-in projections of the dust-to-metal ratio for the face-on images from Fig. 1. At each of z = 2, 1, and 0, the dust-to-metal ratio is largest near the galactic centre. However, by z = 0, the spatial variation in dust-to-metal ratio that is prominent at z = 1 diminishes, although there are small pockets of low dust-to-metal ratio in the outer disc. In conjunction with Fig. 1, this suggests that observations of galaxies should see dust-to-metal ratios that are highest near galactic cores and vary with redshift.

4.2 Impact of feedback

While some previous cosmological simulations treating dust have investigated the effect of galactic winds (Zh et al. 2011) and SN feedback (Bekki 2015b), there has been no comprehensive analysis of feedback physics on dust evolution. In Fig. 3, we show the total dust, metal, gas, and stellar masses as a function of redshift for each of the feedback variations detailed in Table 4 applied to the Aquarius C galaxy. We also plot the SFR and gas-phase metallicity, two dynamical quantities that will be impacted by the presence of dust.

Until z ≈ 4, the no feedback and AGN-only feedback models are very similar, producing stellar masses several times larger than those seen in the fiducial, slow winds, and fast winds models with stellar feedback enabled. This is consistent with the SFR plot, which shows that the no feedback and AGN-only feedback runs have similar behaviour at high redshift. All runs yielded dust masses at high redshift more than an order of magnitude smaller than the several 10⁷ M⊙ and above of dust observed for SDSS J1148+5251 and A1689-zD1 at z = 6.4 and higher (Valiante et al. 2009, 2011; Watson et al. 2015). This is not too surprising since simulations of haloes larger than those in the Aquarius suite seem to be required to produce such dusty systems at high redshift.

At low redshift, AGN feedback strongly suppresses the SFR in the Aquarius C galaxy. The reduction in SFR provides more opportunity for gas-phase metals in the ISM to condense into dust, leading to a decline in gas-phase metallicity relative to the no feedback model. The runs with stellar feedback see a similar suppression of gas-phase metallicity below z ≈ 1. This effect is most pronounced for the fast winds model, which is most efficient at driving gas-phase metals away from star-forming regions and has the lowest stellar mass. In the absence of SN activity, these gas-phase metals can accrete on to dust grains more rapidly. The fast winds run sees a drop in gas-phase metallicity of roughly 0.7 dex from z = 1 to 0. We note that the gas-phase metallicities shown in Fig. 3 correspond to the dense galactic disc and that the hot halo sees less metal enrichment. The fiducial and slow winds models do not experience such severe declines in gas-phase metallicity and are more similar to the AGN-only feedback run at z = 0 than the extreme no feedback model.

Fig. 4 shows the evolution of the dust-to-gas ratio D and dust-to-metal ratio Zdust/Z for the same feedback variations. The fiducial model for this Milky Way-sized galaxy yields D ≈ 10⁻², consistent with estimates of the Galactic value (Gilmore et al. 1989; Sodroski et al. 1997; Zubko et al. 2004). The feedback variations also yield dust-to-gas ratios within a factor of several of the fiducial value. The dust-to-gas ratio increases by roughly 1 dex from z = 2 to 0 for the fiducial, slow winds, and fast winds runs. Above, we noted that the fast winds model promotes gas-phase depletion of metals, and so one might expect a high dust-to-gas ratio. However, because star formation is so strongly suppressed in this model, the total amount of dust is roughly half that of the fiducial run. As a result, the fast winds model has a dust-to-gas ratio comparable to the fiducial value. On the other hand, the fast winds model is the largest of all models, at nearly 0.75. This is slightly below the fiducial model’s z = 0 dust-to-metal ratio of near 0.65, which is still
Figure 1. Surface densities of baryons, gas-phase metals, and dust (first, second, and third columns, respectively) as well as corresponding dust-to-metal ratio (fourth column) for the Aquarius C halo at $z = 2$, $1$, and $0$ using level 4 initial conditions with fiducial feedback and dust physics. The two images in each column at fixed redshift represent face-on (top) and edge-on (bottom) projections. All distances are given in physical units. The scale bar in the first row indicates $25$ kpc. Projections were performed in a cube of side length $150h^{-1}\text{kpc}$ centred on the potential minimum. Movies of this simulation are available through http://www.mit.edu/~ryanmck/#research.
consistent with the growth in dust mass from Fig. 3. All feedback

These surface densities display moderate increases from

$z$ be 50, 30, and 20 per cent of the

zological simulations of larger galaxy populations will be needed

that are fairly consistent with SDSS observations. However, cos-

malizations and shapes in broad agreement with M31 data. These

runs experience a drop in dust surface density of roughly one order

of magnitude or more when leaving the galactic disc, with nor-

mizations and shapes in broad agreement with M31 data. These

models also all predict $\Sigma_{\text{dust}}$ scalings out to more than 100 kpc

that are fairly consistent with SDSS observations. However, cos-

mological simulations of larger galaxy populations will be needed
to confirm this trend on the scales detailed in Ménard et al. (2010).

Such simulations will also be able to investigate predictions about
the dust content of the intergalactic medium (Aguirre 1999; Inoue

& Kamaya 2003; Petric et al. 2006; Dijkstra & Loeb 2009; Corrales

& Paerels 2012).

Fig. 6 displays the dust–metallicity relation for these feedback

runs, plotting dust-to-gas ratio versus gas-phase metallicity at $z = 2,

1, and 0. We also display observations from Kennicutt et al. (2011)

and Galametz et al. (2011), which cover roughly a 1.5 dex range

in oxygen abundance. To facilitate comparison with these data, we

compute the dust-to-gas ratio and gas-phase metallicity using only
dense gas in the galactic disc, as determined by the temperature–
density phase space cut in equation (10). We use this temperature–
density cut in all subsequent plots involving comparison to obser-

vational data.

Variations in feedback affect both the gas-phase metallicity and

the dust-to-gas ratio, particularly at low redshift. All models except

the no feedback model see a decline in gas-phase metallicity from

$z = 1$ to 0, with the effect most pronounced for the fast winds
run. The fiducial model is most similar to the runs with fast and
slow winds, consistent with the results in previous figures. Although
these stellar feedback models lie above the dust–metallicity relation
at $z = 0$, the fits at $z = 1$ and 2 are much more reasonable. The no
feedback model has a high gas-phase metallicity at all redshifts and
thus lies slightly below the dust–metallicity observations. These
results indicate that the inclusion of feedback in our dust model
can affect the dust–metallicity evolution of galaxies and help limit
high-redshift metallicities.

Because heavy elements trapped in dust grains do not contribute
to metal-line cooling in our model, we expect star formation to
decrease as gas-phase metals accrete on to dust. This qualitative
effect is shown in Fig. 7, which compares the projected baryon and
gas-phase metal densities for our fiducial model as well as a model

![Figure 2. Zoomed-in projections of the dust-to-metal ratio using the face-on (top) and edge-on (bottom) views of the Aquarius C halo at $z = 2$, 1, and 0 presented in Fig. 1. These plots capture the inner disc region, with the scale bar in the upper right indicating 10 kpc in physical units. A cube of side length $50 h^{-1}$ kpc was used for the projection volume.](image-url)
Figure 3. Clockwise from top left, a comparison of dust mass, metal mass, stellar mass, gas-phase metallicity, SFR, and gas mass as a function of redshift for the Aquarius C galaxy using various feedback parameters. These quantities include contributions only from the dense galactic disc and not the hot halo. In each plot, the top panel shows results on an absolute scale, while the ratio of quantities relative to the fiducial run (denoted $f_{FI}$) is shown in the bottom panel. This convention is also adopted in subsequent figures. The metal mass includes both gas-phase and dust contributions. The fast winds (FW) and no feedback (NF) runs produce dust masses at $z = 0$ roughly half that produced in the fiducial (FI) model. The fast winds run sees the strongest decline in SFR and gas-phase metallicity towards $z = 0$. 

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with all dust physics disabled. In this latter model, all metals outside of stars are considered to be in the gas phase. The run without dust produces a slightly larger galactic disc at \( z = 0 \), while the run with dust slightly reduces the density of gas-phase metals in the CGM. While we caution that our fiducial dust model ignores dust sputtering and may overdeplete gas-phase metals in the halo, these results suggest that the presence of dust affects how galaxies evolve in simulations, even if feedback settings are unaltered.

To analyse this effect quantitatively, in Fig. 8 we plot the SFR and gas-phase metallicity versus redshift for our fiducial model as well as our model without dust. Differences in these models are most noticeable beginning at \( \approx 1 \). While both models produce similar SFRs, the deviation in gas-phase metallicity from \( \approx 1 \) to 0 is more pronounced. Without dust, the gas-phase metallicity increases and plateaus, whereas the model with dust sees a decline of roughly 0.5 dex. At low redshift, even the fiducial feedback settings are sensitive to whether dust is included or not.

In the analysis above, the fiducial feedback model produced dust-to-gas and dust-to-metal ratios in rough agreement with the Galactic values. While its location on the observed dust–metallicity relation was in tension with observations at \( z = 0 \), the fiducial run at higher redshift yielded more accurate results. The no feedback model, already known to overproduce high stellar mass galaxies (Vogelsberger et al. 2013), has the highest SFR and lowest dust-to-metal ratio of the various models. Fast winds strongly suppress star formation and dust production, carrying metals to galactic regions where dust destruction is less effective. This resulted in a poor \( z = 0 \) dust–metallicity fit, owing to low redshift gas-phase depletion. While the models with slow winds and AGN-only feedback do not suffer such extreme problems, they offer no advantage over the fiducial feedback model. Previous studies have shown that in the absence of winds, the dust-to-metal ratio required to match observed intergalactic reddening is unphysical (Zu et al. 2011). We note that variations in stellar wind feedback affect our dust–metallicity relation more strongly than in Bekki (2015b), though in both cases stronger feedback suppresses the dust-to-gas ratio and gas-phase metallicity. In the remainder of this paper, we adopt the fiducial feedback parameters.

4.3 Variations of the dust model

Motivated by observations of high-redshift dusty galaxies, previous one-zone dust models have studied the importance of dust growth in the ISM relative to contributions from stellar sources. Dust growth appears to be dominant in galaxies above a critical metallicity, and galaxies with a shorter star formation time-scale reach this critical metallicity more quickly (Inoue 2011; Asano et al. 2013a). The carbon-to-silicate dust mass ratio changes significantly as dust growth overtakes stellar injection, and dust growth in the ISM can be important even in dwarf galaxies (Zhukovska 2014). While we do not investigate it in this paper, we acknowledge that variations in the IMF can affect dust model results, particularly in low-mass galaxies (Gall et al. 2011b). Top-heavy IMFs may also strengthen dust production from SNe, despite leading to increased grain destruction (Dunne et al. 2011). It is therefore natural to consider how the various components of our dust model impact galaxy evolution. This will help to determine which aspects of dust physics are most important and worthy of more detailed modelling in future work.

In Fig. 9, we plot the redshift evolution of dust mass in the Aquarius C galaxy for each of the dust model variations listed in Table 4. We also show how each variation compares to the fiducial result. Because dust was shown to have a dynamical effect on star formation in Section 4.2, the total metal masses for each run show minor differences. The dust mass evolution of the fiducial model was most similar to that of the model with decreased dust condensation efficiencies, enabling more mass to be ejected in the gas phase.
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Figure 5. Surface density of dust ($\Sigma_{\text{dust}}$) as a function of radial distance from the Aquarius C halo’s spin axis at $z = 0$ for our set of feedback variations. The radial range extends to $R_{200}$, as defined in Table 1, and the bottom subpanel shows surface density relative to the fiducial result. The grey dashed line indicates the $\Sigma_{\text{dust}} \propto r^{-0.8}$ scaling observed in SDSS data over cosmological distances (Ménard et al. 2010). The amplitude of this scaling has been chosen to align with simulated data from 25 kpc out to roughly 100 kpc. Squares indicate measurements of M31’s projected dust profile (Draine et al. 2014). Triangles denote the M31 data scaled by a factor of 2 to model a Milky Way dust mass that may be higher than that of M31.

Figure 6. Dust-to-gas ratio ($D$) versus gas-phase metallicity for varying feedback runs involving the Aquarius C halo, plotted at $z = 2$, 1, and 0. Smaller circles denote higher redshift. The dust-to-gas ratio and gas-phase metallicity have been computed using only dense gas cells in the galactic disc. For comparison, observational data from Kennicutt et al. (2011) and Galametz et al. (2011) (as compiled in Rémy-Ruyer et al. 2014) are provided. All runs except that with no feedback experience a drop in gas-phase metallicity from $z = 1$ to 0.

Figure 7. Face-on and edge-on projections of total surface density (left-hand column) and gas-phase metal surface density (right-hand column) at $z = 0$ for simulations of the Aquarius C halo with fiducial dust (FI; top half) and without dust (WD; bottom half). The scale bar in the first row marks 25 kpc, and the projection volume is the same as that used in Fig. 1. Not shown are metals occupied by dust, which exist only in the fiducial simulation. Compared to the simulation without dust, the fiducial dust run results in a smaller disc and a decreased gas-phase metal surface density beyond 15 kpc from the galactic centre.

In fact, their $z = 0$ dust masses were almost identical, while at $z \approx 2.5$ the fiducial model produced about twice as much dust. This perhaps reduces the effect of large uncertainties in dust condensation efficiencies, especially for results at low redshift. For modelling at high redshift, metallicity-dependent condensation efficiencies (as in the one-zone model of Zhukovska et al. 2008) may have more of an impact.

In contrast, the model without dust growth deviated significantly from the fiducial run, and the dust mass increased by only a factor of 4 from $z \approx 4$ to 0. The fiducial model and other models with growth enabled saw an increase in dust mass closer to one order of magnitude. This corroborates findings from earlier one-zone models and highlights the importance of dust growth at low redshift. We caution that more detailed growth mechanisms following one-zone models that take into account variations in dust grain sizes (Hirashita
A comparison of SFR (top) and gas-phase metallicity (bottom) computed for the Aquarius C galaxy as a function of redshift in the fiducial (FI) and without dust (WD) models. The FI run has decreased metal-line cooling, as gas-phase metals deplete onto dust grains. The SFRs largely agree, but at $z = 0$, the difference in gas-phase metallicities between the FI and WD runs is roughly 0.5 dex.

Figure 9. Dust mass as a function of redshift for a variety of dust models applied to the Aquarius C galaxy. This only includes contributions from the inner disc and not the hot halo. The no feedback (NF) run is shown for comparison. At $z = 0$, the dust model without a growth mechanism (NG) yields a final dust mass more than an order of magnitude below those obtained by models with growth enabled. The difference between a destruction mechanism based on local SNe (FI) and a uniform time-scale (CD) is minor at $z = 0$, but at high redshift the CD run is more similar to the run without any destruction (ND). The model without any growth or destruction (PO) sees a dust mass at low redshift reduced by roughly a factor of 2 compared to the ND run with growth. The fiducial model was most similar to the low production (LP) model with smaller condensation efficiencies.

Figure 10 shows the dust-to-gas and dust-to-metal ratios for these dust model runs, using contributions from cells within the disc of the Aquarius C galaxy. Nearly all dust variations yield a $z = 0$ dust-to-gas ratio within a factor of 2 of the fiducial value of $D \approx 10^{-2}$. At high redshift, models without dust destruction display an increased dust-to-gas ratio. A dust model without growth results in a late time dust-to-gas ratio suppressed by over 1 dex relative to the fiducial run. Without growth, the dust-to-gas ratio shows little evolution from its value at $z = 5$. The effect of limiting dust growth is much more severe than that of limiting grain destruction. Modelling work motivated by observations of SINGS galaxies and high redshift quasars has similarly predicted that dust growth and non-stellar dust production can have a pronounced impact on a galaxy’s dust content, while dust destruction is less influential (Draine 2009; & Kuo 2011; Asano et al. 2013b; Nozawa et al. 2015) and their impact on grain collision rates will offer a better assessment of the role dust growth plays in the ISM. Before $z \approx 5$, the difference between a model employing only stellar dust production and a model with both stellar production and ISM dust growth is minor, while both models yield more dust than in the fiducial run with destruction. However, by $z = 0$, the model lacking growth and destruction sees a final dust mass approximately two times smaller than that obtained by the model with growth but without destruction. Grain growth becomes increasingly important towards low redshift.

This is consistent with the hypothesis that galaxies pass through a critical metallicity at which dust growth in the ISM dominates stellar production.

The run adopting a constant destruction time-scale of $\tau_d = 0.5$ Gyr for dust destruction, rather than the fiducial time-scale computed locally using SN activity, behaves more like the model lacking any destruction whatsoever and overproduces dust at high redshift relative to the fiducial model. By $z = 0$, the constant destruction time-scale run agrees well with the fiducial run. Dust models that globally adopt $\tau_d = 0.5$ Gyr (e.g. the fiducial runs in Bekki 2015b) may be overestimating a galaxy’s dust content by a factor of several at high redshift.
Figure 10. Comparison of dust-to-gas ratio ($D$; left) and dust-to-metal ratio ($Z_{\text{dust}}/Z$; right) for the range of dust models in Fig. 9 run on the Aquarius C galaxy. These ratios are computed using total masses within the dense galactic disc. The no feedback (NF) model is also shown for comparison. In both plots, the model lacking a dust destruction mechanism (ND) yielded the highest dust-to-gas and dust-to-metal ratios at essentially all redshifts. Conversely, the model with only dust production enabled (PO) results in dust-to-gas and dust-to-metal ratios at $z = 0$ roughly half those obtained by the fiducial model. The run without dust growth but with destruction (NG) more strongly suppresses both ratios. The NG and PO runs display very flat dust-to-metal ratio evolutions.


Models without growth and without destruction produced the lowest and highest dust-to-metal ratios for $z < 2$, respectively. While the dust-to-metal ratio predicted by only allowing stellar production of dust is roughly 0.3 and physically acceptable, it is nearly constant and displays little evolution. In contrast, both growth and destruction mechanisms are needed to capture the increase in dust-to-metal ratio expected at low redshift (Inoue 2003), as in our fiducial model and the run with low dust condensation efficiencies. The extent to which the dust-to-metal ratio varies within a galaxy and among different galaxies is unclear (Mattsson et al. 2012), so it is difficult to assess whether our fiducial dust model yields a typical dust-to-metal ratio. In any case, from Fig. 10 we can conclude that varying dust condensation efficiencies makes little difference to the dust-to-metal ratio evolution, and while adopting a constant destruction time-scale instead of using local SNe-driven destruction leads to a higher dust-to-metal ratio at high redshift, the effect is nowhere near as severe as limiting dust growth or destruction.

In comparison, the models lacking growth and destruction mechanisms see less diversity among gas cells. The no growth model has $Z_{\text{dust}}/Z < 0.5$ for essentially every cell, with the typical dust-to-metal ratio decreasing towards $z = 0$. Conversely, the no destruction model sees $Z_{\text{dust}}/Z > 0.4$ for nearly all gas cells at $z = 1$ and 0. Additionally, by $z = 0$, the model without destruction witnesses a peak dust-to-gas ratio roughly 2 dex above that obtained in the no growth model. These results suggest that the presence of both growth and destruction mechanisms leads to more variation in the simulated dust content of galaxies.

4.4 Variations in the initial conditions

In the remainder of this work, we use the fiducial feedback and dust models to investigate the evolution of dust within our sample of eight Aquarius galaxies. Fig. 12 shows the dust mass, stellar mass, SFR, and gas-phase metallicity for each of these galaxies as a function of redshift. These quantities exclude contributions from cells in the hot halo. The variation in galactic dust mass is largest...
at low redshift, with galaxies D and H producing dust masses of $8 \times 10^8 M_\odot$ and $3 \times 10^7 M_\odot$, respectively, at $z = 0$. Changes in the dust content largely trace changes in the overall metal mass. We note that two of the galaxies with the largest dust and metal masses at high redshift, A and C, are known to have progenitors that assemble their mass more rapidly than the others (Wang et al. 2011). The SFRs for these galaxies cover the range $0.4$–$7 M_\odot \text{yr}^{-1}$ at $z = 0$, and the galaxy that experiences the largest drop in SFR from $z = 1$ to $0$, galaxy E, also sees the largest decline in gas-phase metallicity. While decreased star formation produces fewer dust grains in the ISM, it also weakens SN-based grain destruction, ultimately enabling gas-phase depletion.

To further contrast these haloes, in Fig. 13 we display face-on and edge-on dust surface density projections for the Aquarius sample at $z = 0$. These haloes are at various stages of galactic disc formation. In some cases, as for halo C, a quiescent disc of dust has formed with an abrupt drop in dust surface density when moving to the CGM. Other haloes, including D, F, and G, display much more spatial variation, especially off the disc plane. In particular, halo G is perturbed by a satellite galaxy at $z = 0$ (Marinacci et al. 2014). A dusty disc of comparable size was found in recent smoothed-particle hydrodynamical simulations of a $10^{12} M_\odot$ halo (Bekki 2015b), resembling our results for halo C. Furthermore, the diversity of dust surface densities that we see could impact the creation of synthetic galaxy images and spectra using spectral energy distribution modelling (Silva et al. 1998; Jonsson 2006; Bernyk et al. 2014; Snyder et al. 2015; Torrey et al. 2015).

Fig. 14 shows the projected dust-to-metal ratio of these haloes at $z = 0$ and indicates that the dust-to-metal ratio exhibits fluctuations within the galactic disc. Analytical arguments suggest that dust-to-metal gradients can be used to estimate the relative strength of dust growth and destruction in the ISM, with flat dust-to-metal profiles expected in the absence of dust growth and destruction (Mattsson et al. 2012). Rather compact galaxies, as in haloes E and H, see less spatial variation in the dust-to-metal ratio than the larger galactic discs in Fig. 13, which tend to have more pockets of low and high dust-to-metal ratio. Stellar density projections for the Aquarius suite have previously been made using the same physical model without dust (Marinacci et al. 2014) and show that depressions in dust-to-metal ratio are similar in size to regions of high stellar density. In
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Figure 12. Clockwise from top left, a comparison of dust mass, stellar mass, gas-phase metallicity, and SFR for the Aquarius sample of galaxies with standard dust model parameters. These quantities include contributions only from the dense galactic disc and not the hot halo.

particular, haloes A, C, F, and G have some of the largest stellar discs and also some of the most variation in dust-to-metal ratio. While our dust model does not properly account for thermal sputtering and grain–grain collisions in hot regions of the CGM, Fig. 14 suggests the presence of noticeable dust-to-metal ratio fluctuations in Milky Way-mass galactic discs that trace stellar structure.

To investigate the dust-to-metal ratio evolution more quantitatively, in Fig. 15 we plot the dust-to-gas and dust-to-metal ratios as a function of redshift for these galaxies. The dust-to-gas ratios tend to evolve in similar fashion, reaching Milky Way-like values of \((0.8–1.8) \times 10^{-2}\) by \(z = 0\). At \(z = 7.5\), where A1689-zD1 has been observed to have a near-Galactic dust-to-gas ratio (Watson et al. 2015), the Aquarius suite of galaxies sees dust-to-gas ratios slightly under \(10^{-4}\). Our results suggest that A1689-zD1 and other dusty high-redshift galaxies do not arise from Milky Way-like progenitors and motivate further study of the dust-to-gas ratio over a range of halo masses. Recent models predict that larger haloes see more dramatic growth in the dust-to-gas ratio towards low redshift and that smaller systems have less dynamic dust-to-gas ratios (Bekki 2015b). A larger statistical sample of galaxies would also enable comparison to observed dust mass functions (Dunne et al. 2000, 2011).

The dust-to-metal ratios in Fig. 15 display more diversity, with \(z = 0\) values ranging from roughly 0.6 to 0.7. While high depletion has been observed for some elements, including Si, Mg, and Fe, in the local interstellar cloud (Kimura et al. 2003), this would not greatly change the overall dust-to-metal ratio. Estimates of the dust-to-metal ratio for typical galaxies, including the Milky Way and Magellanic Clouds, lie closer to 0.5 (Aguirre 1999; De Cia et al. 2013). All show an increase in dust-to-metal ratio from \(z = 2\) to 0, expected of galaxies (Inoue 2003). Before \(z \approx 3\), about half of galaxies display a flat dust-to-metal ratio near 0.1. However, there is some variation in when the Aquarius galaxies see the most growth in dust-to-metal ratio. Galaxies A and C, which assemble the majority of their mass more quickly than the others (Wang et al. 2011), show some of the earliest growth in dust-to-metal ratio, suggesting that accretion history may influence dust-to-metal ratio evolution.

In Fig. 16, we construct temperature–density phase diagrams for all gas cells within halo C at \(z = 2, 1,\) and 0. We analyse gas cells in three different ways: by total dust mass, by mass-weighted dust-to-gas ratio, and by mass-weighted dust-to-metal ratio. We note that from \(z = 2\) to 0 dust mass becomes increasingly concentrated in hot, diffuse halo gas with \(T \sim 10^6\) K and dense, star-forming ISM gas with \(T \sim 10^4\) K near the equation of state transition. By contrast, the
phase diagram region with $T \sim 10^5$ K has a total dust mass largely unchanged with redshift. While SDSS data do suggest that the dust masses of galactic haloes are similar to those found in galactic discs (Ménard et al. 2010), the results in Fig. 16 also motivate better modelling of dust evolution in the diffuse halo where grains may travel at higher velocities, have lower sticking efficiencies when impacting gas-phase metals, and undergo grain–grain collisions. Thus, it is likely that the halo dust mass is overstated, especially at $z = 0$, but we still expect the presence of dust beyond the galactic disc.

Dust-to-gas ratios tend to increase from $z = 2$ to 0 most rapidly in high-density regions. Gas density correlates more strongly with average dust-to-gas ratio than does temperature. We see a similar trend in dust-to-metal ratio, as dense gas above the equation of state transition sees its dust-to-metal ratio increase from roughly 0.2 to 0.6 over this redshift range. In contrast, low-density gas with $\rho \sim 10^{-20}$ g cm$^{-3}$ barely changes in dust-to-metal ratio. This result is physically justified, since the dust growth time-scale is shortest in high-density gas, and agrees with observations of elemental depletions increasing with gas density (Jenkins 2009).

In Fig. 17, we display the radial dust surface density profiles for each of the Aquarius haloes at $z = 0$. There is fairly little evolution from $z = 1$ to 0, although the growth in virial radius causes $\Sigma_{\text{dust}} \sim 10^{-3} M_{\odot}$ pc$^{-2}$ out to $r \approx 200$ kpc by $z = 0$. These Milky Way-sized haloes have dust profiles fairly consistent with observations of M31, with higher normalizations in the inner disc. The Aquarius haloes tend to show rather sharp drops in dust surface density when moving outside of the galactic disc: for example, halo C witnesses a decline of almost an order of magnitude in $\Sigma_{\text{dust}}$ near $r \approx 20$ kpc, although it is not as sharp as the drop seen for M31. The Aquarius haloes have dust profiles that decay from $r \approx 20$ to $\approx 100$ kpc in rough agreement with the observed scaling $\Sigma_{\text{dust}} \propto r^{-0.8}$ seen in SDSS data (Ménard et al. 2010).

In Fig. 18, we compare the cumulative dust mass distributions for the Aquarius galaxies with the observed distribution for M31 (Draine et al. 2014), normalizing to the total dust mass within a radial distance of 25 kpc from galactic centre. We do not necessarily expect the Aquarius suite to have cumulative dust mass distributions identical to that of M31 but use these observational data for guiding purposes. The Aquarius haloes witness a slightly steeper enclosed dust mass distribution for $r < 10$ kpc than is observed for M31, but
Figure 14. Projected dust-to-metal ratio in the inner disc region for the haloes shown in Fig. 13. Face-on (top) and edge-on (bottom) projections are displayed for each halo column. The projection volume was a cube of side length $50 h^{-1}$ kpc. Fig. 2 displayed higher resolution images for the Aquarius C halo at $z = 2, 1,$ and $0$.

the simulated and observed distributions are in rough agreement. In particular, we find in the Aquarius sample that the dust masses enclosed within 10 kpc are between 9 and 54 per cent of the total dust mass within 25 kpc. For comparison, the observed value for M31 is about 25 per cent (Draine et al. 2014) and recent smoothed-particle hydrodynamical simulations using a Milky Way-sized halo with dust growth mechanism similar to ours found that roughly 18 per cent of the dust mass inside of 25 kpc is contained within the innermost 10 kpc (Bekki 2015b).

4.5 Scaling relations

To better understand how realistically our sample of eight Aquarius galaxies produce dust, we compare against a number of empirical scaling relations seen in recent observations (Draine et al. 2007; Galametz et al. 2011; Kennicutt et al. 2011; Corbelli et al. 2012; Cortese et al. 2012; Rémy-Ruyer et al. 2014). These scalings enable valuable predictions about the dust content in very metal-poor galaxies (Fisher et al. 2014) and high-redshift, dusty quasars (Bertoldi et al. 2003; Fan et al. 2003; Valiante et al. 2009). Also, these relations help determine the quantities that most effectively trace the presence of dust in galaxies. One of the most prominent of these scalings is the dust–metallicity relation, which finds a dust-to-gas ratio that scales fairly linearly with metallicity (Draine et al. 2007; Galametz et al. 2011; Kennicutt et al. 2011; Rémy-Ruyer et al. 2014) and is often used to estimate the dust mass within a galaxy. It is therefore interesting to consider such scaling relations and to investigate any variations in our Aquarius sample. In the observational comparisons below, we compute all quantities using dense ISM gas, as determined by the cut in temperature–density phase space of all gas cells belonging to the main halo group given by equation (10). This cut isolates the galactic disc and thus ignores the effect of dust growth in the CGM that is possibly too strong.

We first show the dust–metallicity relation for the Aquarius galaxies in Fig. 19, plotting dust-to-gas ratio versus gas-phase metallicity at $z = 2, 1,$ and $0$, with the gas-phase metallicity calculated from oxygen and hydrogen abundances. As in Fig. 6, we compare against observational data from Kennicutt et al. (2011) and Galametz et al. (2011). Previous models have been fairly successful at reproducing the dust–metallicity relation (Dwek 1998; Lisenfeld & Ferrara 1998; Calura et al. 2008; Bekki 2015b; Feldmann 2015) and have investigated the nature and scatter of this relation at low metallicity (Rémy-Ruyer et al. 2014). In comparison to several models that see a strictly monotonic increase in dust-to-gas ratio and gas-phase
metallicity towards low redshift (Lisenfeld & Ferrara 1998; Bekki 2015b; Feldmann 2015), the Aquarius haloes display more diverse redshift evolution while remaining in agreement with the observed dust–metallicity relation at $z = 2$ and 1. While the data for $z = 0$ capture the positive correlation between dust-to-gas ratio and gas-phase metallicity, they tend to lie above the observed relation, as in Fig. 6.

While some haloes, like A and B, display small drops in gas-phase metallicity from $z = 1$ to 0, others show much more pronounced behaviour. In particular, haloes C and E have some of the largest declines in SFR from $z = 1$ to 0 in our sample, weakening grain destruction and enhancing depletion of gas-phase metals. Given that the temperature–density cut used to isolate dense gas in the galactic disc will minimize the influence of dust in the CGM, Fig. 19 suggests that the dust–metallicity relation can evolve in a non-monotonic fashion even near the galactic centre. However, the behaviour at $z = 0$ together with fairly high dust-to-metal ratios in Fig. 15 indicate that gas-phase metals may be too heavily depleted at low redshift. Additionally, while there is evidence for a dust–metallicity relation that is less steep for metallicities below 8.0 (Rémy-Ruyer et al. 2014), suggesting that the global dust–metallicity trend cannot be fit by a single power law, the Aquarius galactic disc gas-phase metallicities lie above this region. Future simulations of full cosmological volumes will allow us to explore the dust–metallicity scaling at low metallicity.

In Fig. 20, we compare the dust mass–gas mass scaling seen for our Aquarius suite with observations of metal-rich galaxies from the Herschel Virgo Cluster Survey (Cortese et al. 2012). These observational data found the best fit scaling $M_{\text{gas}} \propto M_{\text{dust}}^{0.25}$, suggesting that the dust-to-gas ratio increases weakly with gas mass. That is, the presence of additional gas leads to increased star formation, which in turn produces enough dust to cause the dust-to-gas ratio to rise. We find that the Aquarius data obey a slightly steeper scaling of gas mass with dust mass, consistent with the results in Fig. 15 showing fairly little variation in the dust-to-gas ratio in our sample. However, the Aquarius haloes tend to be more gas- and dust-rich than those from the Herschel Virgo Cluster Survey, and future work should investigate whether our observed scaling holds for lower mass systems.

The Herschel Virgo Cluster Survey also investigated the relationship between dust-to-gas ratio and stellar mass, observing the weak scaling $D \propto M_{\ast}^{0.26}$. This scaling is possibly weak because increased star formation injects more dust into the ISM through stellar production but also leads to SNe destroying dust more rapidly. In Fig. 21, we compare the $D - M_{\ast}$ data from the Aquarius suite with the Herschel scaling and find the Aquarius data to lie close to the observed best fit. While the Aquarius haloes show a scatter in dust-to-gas ratio that roughly matches that seen in the Herschel data, our haloes do not cover the full range of stellar masses observed by Herschel.

In Fig. 22, we compare the observed scaling between dust-to-stellar mass ratio and gas fraction ($M_{\text{gas}}/(M_{\ast} + M_{\text{gas}})) seen in Herschel Reference Survey data (Cortese et al. 2012) with results from our Aquarius sample. The dust-to-stellar mass ratio is expected to anticorrelate with stellar mass and decrease from late- to early-type galaxies (Cortese et al. 2012). Late-type galaxies with high gas fraction see more efficient stellar injection of dust, while early-type galaxies are more influenced by grain destruction. The Aquarius suite is in good agreement with the observed dust-to-stellar mass ratio scaling, covering a range of gas fractions from less than 0.1 to 0.5.

While the Aquarius haloes compare favourably to these dust scaling relations at $z = 0$, in the future we would like to perform similar analyses for multiple epochs. There are estimates of the dust mass function for $z < 0.5$ (Dunne et al. 2011) and for high-redshift submillimetre sources (Dunne, Eales & Edmunds 2003). The relation between dust mass, SFR, and stellar mass has also been studied out to $z = 2.5$ (Santini et al. 2014). These scalings...
would be interesting in part because our Aquarius haloes displayed more diversity at high redshift than at $z = 0$.

Especially at high redshift, it is important to understand the relative dust production strengths of SNe and AGB stars, since this helps determine whether dusty galaxies and quasars could have dust content driven by stellar sources as opposed to interstellar dust growth. Chemical evolution models suggest that AGB stars played an important role in forming the large dust mass of SDSS J1148+5251 at $z = 6.4$, possibly contributing over half of the observed dust (Valiante et al. 2009). Observations of dust in the ejecta of SNe fall short of the 1 M$_\odot$ or more an SN needs to produce in order to explain the dust content of SDSS J1148+5251 (Todini & Ferrara 2001; Sugerman et al. 2006; Dwek et al. 2007; Lau et al. 2015), and if SNe are not dominant producers of dust, high SFRs might be needed to form dusty $z \gtrsim 5$ galaxies (Morgan & Edmunds 2003; Santini et al. 2014). Given that the progenitors of AGB stars take longer to evolve off of the main sequence than SNe, it is unclear whether AGB stars can have a large impact at high redshift. In Fig. 23, we compare the dust mass contributions of SNe Ia, SNe II, and AGB stars for the Aquarius C galaxy as a function of redshift. We see that 80 per cent or more of dust originated in SNe II for $z \gtrsim 5$, with the contribution from AGB stars peaking at roughly 40 per cent for $z \approx 2$. Recent investigation of the Small Magellanic Cloud suggests that even at low redshift AGB stars are not dominant producers of dust (Boyer et al. 2012). In this Aquarius galaxy, we see that by $z = 0$ about 20 per cent of dust has its origins in AGB stars. While future work is needed to investigate how these stellar contributions vary with galaxy stellar mass and metallicity, in our sample of Milky Way-sized galaxies we find SNe to be the dominant producers of dust.

5 DISCUSSION AND CONCLUSIONS

We have implemented a first very basic dust model in the moving-mesh code AREPO, adding to the existing galaxy formation physics. Our dust model accounts for local stellar production of dust, growth in the ISM due to accretion of gas-phase metals, destruction via SN shocks, and dust driven by stellar feedback winds. Dust is also passively advected between gas cells. We track dust in individual chemical species as well as follow contributions from AGB stars, SNe Ia, and SNe II.
Figure 17. Radial profiles of dust surface density ($\Sigma_{\text{dust}}$) in the disc plane for all simulated haloes, plotted at $z = 0$. The radial profiles extend out to the virial radius of each halo as defined in Table 1. We compare with the observed dust profile for M31 (grey squares; Draine et al. 2014) and an M31 profile scaled by a factor of 2 (grey triangles), given that the Galactic dust content may vary from that of M31. The grey dashed line shows the $\Sigma_{\text{dust}} \propto r^{-0.8}$ scaling observed in SDSS data (Ménard et al. 2010), with normalization adjusted to the Aquarius data.

Figure 18. Enclosed dust mass as a function of radial distance for all haloes at $z = 0$, normalized to $M(r < 25 \text{ kpc})$, the mass within 25 kpc of the disc centre. The normalized cumulative dust mass distribution observed for M31 is given by the grey dashed line (Draine et al. 2014). While there is some scatter in the Aquarius haloes, the enclosed dust mass profiles are similar to that of M31.

Figure 19. Dust-to-gas ratio ($D$) versus gas-phase metallicity for the Aquarius haloes plotted at $z = 2, 1$, and 0, with smaller circles denoting higher redshift. The same observational data of local galaxies from Kennicutt et al. (2011) and Galametz et al. (2011) as in Fig. 6 are shown in grey. These galaxies all show decreases in gas-phase metallicity from $z = 1$ to 0 but fall close to the observed scatter at $z = 2$ and 1.

Figure 20. Scaling relation between dust mass ($M_{\text{dust}}$) and gas mass ($M_{\text{gas}}$) for the eight Aquarius haloes, with observational data from the Herschel Virgo Cluster Survey (Corbelli et al. 2012). The dashed line represents the best fit scaling for the sample of 35 metal-rich galaxies in Virgo at $z = 0.003$, with $M_{\text{gas}} \propto M_{\text{dust}}^{0.75}$. Uncertainties in the regression parameters yield scaling fits given by the dotted lines. The Aquarius haloes are more massive than those in this observational sample and display a slightly steeper gas-dust scaling.
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Using this dust model, we performed cosmological zoom-in simulations of the Aquarius suite of eight haloes with the goal of understanding how dust forms in Milky Way-sized systems. After investigating the effect of feedback and the strength of various dust model components, we used the full sample of Aquarius haloes to compare to a range of dust observations at low redshift. We summarize our main findings as follows.

(i) Variations in stellar and AGN feedback impact the predictions made by our dust model. The absence of any feedback led to a $z = 0$ dust-to-metal ratio of 0.2 for one Aquarius galaxy, roughly a factor of 3 lower than the value predicted by our fiducial feedback model. Excluding feedback led to high star formation and more efficient SN-based dust destruction. On the other hand, a model with fast stellar feedback-driven winds helped sweep dust away from the galactic centre and enhance depletion of gas-phase metals due to weakened star formation, raising the halo-wide dust-to-metal ratio to over 0.7.

(ii) Allowing gas-phase metals to deplete on to dust grains and not contribute to metal-line cooling has the potential to affect gas-phase metallicity. We see a difference in halo gas-phase metallicity between runs with and without dust of roughly 0.5 dex at $z = 0$. This result also motivates the future inclusion of dust cooling channels.

(iii) In the absence of dust growth, dust-to-gas and dust-to-metal ratios are suppressed by more than an order of magnitude at $z = 0$ from the values predicted by our fiducial model with dust growth and destruction mechanisms. Without growth, we obtain a dust-to-gas ratio of $3 \times 10^{-4}$ for one Milky Way-like galaxy, below the Galactic value of roughly $10^{-2}$, and a dust-to-metal ratio $Z_{\text{dust}}/Z \lesssim 0.05$. The differences between the fiducial model and no dust growth model are noticeable for $z \lesssim 5$.

(iv) For $z \gtrsim 5$, the dust mass and dust-to-gas ratio produced by a model adopting a constant dust destruction time-scale of $\tau_d = 0.5$ Gyr are largely indistinguishable from those produced by a model with no dust destruction. By $z = 0$, the constant destruction time-scale model yields results similar to those from the

Figure 23. Evolution of dust mass contributions from different stellar types for the Aquarius C galaxy using the fiducial dust model. The bottom subpanel shows the fraction of total dust mass ($f_{\text{tot}}$) contributed by each component. As noted in Section 2.2.3, the relative proportions of dust produced by AGB stars and SNe are kept constant during changes in dust mass from dust growth or destruction. Type II SNe are responsible for roughly 80 per cent of dust formed in the first Gyr and two-thirds of dust at $z = 0$. This figure captures the delayed production of dust by AGB stars owing to their long lifetimes.

Figure 22. Relation between dust-to-stellar mass ratio ($M_{\text{dust}}/M_*$) and gas fraction ($M_{\text{gas}}/(M_* + M_{\text{gas}})$) for all simulated Aquarius haloes, shown as coloured circles, with observational data from the Herschel Reference Survey at $z \leq 0.006$ provided as grey squares (Cortese et al. 2012). The observational data include both galaxies classified as H$_\text{I}$-normal and H$_\text{I}$-deficient and omit upper limits. Both simulation and observation predict that galaxies with larger gas fraction have higher dust-to-stellar mass ratio.

Figure 21. Dust-to-gas ratio ($D$) plotted as a function of stellar mass ($M_*$) for our sample of Aquarius haloes, with the same Herschel Virgo Cluster Survey data as in Fig. 20 given in grey (Corbelli et al. 2012). The observed weak scaling with $D \propto M_*^{0.26}$ is indicated by the dashed line. The scatter of Aquarius haloes is similar to that in these observations.
fiducial model with local SNe-based dust destruction. At $z = 0$, the model with constant destruction time-scale produces a dust mass $M_{\text{dust}} = 3 \times 10^8 M_\odot$ in the galactic disc with a dust-to-gas ratio $D = 10^{-2}$.

(v) The Aquarius haloes form dusty galactic discs with typical surface densities $\Sigma_{\text{dust}} \sim 10^{-1} M_\odot \text{pc}^{-2}$. The inclusion of thermal sputtering and grain–grain collisions would likely reduce the dust-to-metal ratios seen in the CGM. Dust-to-gas ratios for these Milky Way-like galaxies increase by roughly an order of magnitude from $z = 3$ to 0 and cover the range $(0.8–1.8) \times 10^{-2}$ at $z = 0$.

(vi) The predicted ISM dust content of the Aquarius haloes is consistent with a number of observed scaling relations at $z = 0$, including scalings between dust mass and gas mass, dust-to-gas ratio and stellar mass, and dust-to-stellar mass ratio and gas fraction. While the overall trend of the dust–metallicity relation is reproduced over $8.1 < 12 + \log (O/H) < 9.0$ at $z = 2$ and 1, the Aquarius galaxies do not evolve along strictly monotonic tracks from $z = 2$ to 0.

(vii) Our dust model tracks contributions from individual chemical species, but additional physics is needed to capture differences between silicate and graphite grain types. As shown in Fig. 24, currently silicate and graphite grains are distributed in essentially the same manner. While we may expect slight variations, given that AGB stars and SNe produce dust of different compositions and the dust originating from SNe may be more readily destroyed in SN shocks, future work should include starlight-driven radiation pressure on dust grains. Given that the dust composition will impact the grain size distribution (Mathis, Rumpl & Nordsieck 1977; Kim, Martin & Hendry 1994) and radiation pressure is suggested to be important in simulations treating dust (Murray, Quataert & Thompson 2005; Bekki 2015a), this physics may help differentiate between silicate and graphite grains.

While our current dust model is fairly passive and simplistic, it reproduces a number of observed dust scaling relations surprisingly well at low redshift and is a step towards a more complete treatment of dust in cosmological galaxy formation simulations. In the future, we can explore a live dust model that includes dust–gas interactions more directly, enables dust cooling channels, and allows for radiative forces to affect the motion of grains. Together with simulations of full cosmological volumes, this work will lead to a better understanding of the full diversity of dust seen in the Universe.

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