Evaluation of reactor neutrino flux: issues and uncertainties

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Evaluation of the reactor $\nu_e$ flux and spectrum is an essential ingredient of their application in the neutrino oscillation studies. Two anomalies, i.e. discrepancies between the observed and expected count rates, are widely discussed at the recent time. The total rate is $\sim 6\%$ lower than the expectation at all distances $>10$ m from the reactor. And there is a shoulder (often referred to as “bump”) at neutrino energies 5-7 MeV, not predicted in the calculated spectrum. I review the ways the flux and spectrum is evaluated and concentrate on the error budget. I argue that far reaching conclusions based on these anomalies should await a thorough understanding of the uncertainties of the spectrum, and point out possible standard physics sources of the anomalies.

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1 Introduction

Nuclear reactor are pure and powerful sources of low-energy electron antineutrinos that have been successfully used in the study of neutrino oscillations. In the past neutrino flux and spectrum was determined in a large number of experiments at distances 10-100 m from the reactor core (see the review [1]). Recent experiments, with considerably larger and more accurate detectors, Daya-Bay [2], RENO [3], and Double-Chooz [4] at ~ 1 km were not only able to determine the mixing angle $\theta_{13}$, but were also able to observe and confirm the anomalies mentioned in the abstract.

![Figure 1](image-url)

Figure 1: The measured reactor rate, normalized to the prediction of [5] plotted as a function of the distance from the reactor core. The rate is corrected for the 3-flavor neutrino oscillation at each baseline. Reproduced from [2].

The experimentally determined reactor antineutrino capture rate is shown in Fig. 1 as a function of the distance from the reactor. It is normalized to the prediction of refs. [5] [6]; the global fit that includes all past measurements and is corrected for the known three-flavor neutrino oscillations results in the ratio $R = 0.942 \pm 0.009(\text{exp}) \pm 0.025(\text{model})$. Thus the average $R$ is experimentally determined with ~1% accuracy, and suggests that 5-6% of the $\nu_e$ flux is missing already at $L \leq 10$ m. Such disappearance at short distances cannot be explained within the three-flavor mixing scenario with commonly accepted and experimentally well determined parameters, and hence it is referred to as the “reactor anomaly”.

If one would insist on explaining it using the neutrino oscillation phenomenon, it would require that the corresponding $L(\text{m})/E_{\nu_e}(\text{MeV})$ is of the order of unity, i.e. it would imply the existence of one or more additional and necessarily sterile neutrinos with $\Delta m^2 \sim 1 \text{ eV}^2$. That hypothesis was raised, e.g., in [7]. In that sense the reactor anomaly is in accord with other indications of the $\nu_e$ non-standard disappearance (or mixing) such as LSND [8], MiniBooNE [9], GALLEX [10] or SAGE [11]. However, the significance of the reactor
anomaly obviously critically depends on the value and the uncertainty of the predicted reactor $\nu_e$ spectrum.

Figure 2: The shoulder (bump) observed in the near detector \cite{12} at RENO. The predictions are from the Huber-Mueller model \cite{6, 5} model, normalized to the same number of events.

In addition all three recent large reactor experiments, Daya-Bay, RENO, and Double Chooz observed a feature (or shoulder) in the experimental spectrum at 4-6 MeV of the prompt positron energy, $E_{\text{prompt}} \approx E_\nu + (M_p - M_n) + m_e$, relative to the predicted theoretical evaluation in the refs. \cite{5, 6}. An example of the data, from the RENO experiment, is shown in Fig. 2. The spectral shape of the shoulder cannot be produced by the standard $L/E_\nu$ neutrino oscillations dependence; it is almost certainly caused by the reactor fuel $\nu_e$ emission. Note, however, that the shoulder was not observed in previous experiments. We have to ask, therefore, whether its existence implies a significant problem of expected/predicted reactor spectra in general?

In the following I discuss first how the expected/predicted reactor spectrum is evaluated. That discussion then leads to the consideration of the origin (or explanation) of these two observed anomalies. More detailed discussion of these issues can be found in the forthcoming review \cite{13}.

2 Nuclear reactors as $\nu_e$ sources

Nuclear reactors derive their power from the fission and from the radioactive decay of the corresponding fission fragments. In power reactors 99.9% of the power comes from the fission of $^{235}$U, $^{239}$Pu, $^{241}$Pu and $^{238}$U, while research reactors use usually highly enriched
\[ S(E_\nu) = \frac{W_{th}}{\sum_i (f_i/F)} \sum_i f_i \frac{dN_i}{dE_\nu} (E_\nu) \]  

Here \( W_{th} \) is the reactor total thermal energy, \( f_i/F \) is the fraction of fissions from actinide \( i \), \( e_i \) is the effective thermal energy per fission, and \( dN_i/dE_\nu \) is the cumulative \( \nu_e \) spectrum of \( i \) normalized per fission. \( W_{th} \) and \( f_i/F \), which are changing with time, are usually supplied by the reactor operators, and \( e_i \) are known with negligible error. It is usually assumed that the individual neutrino spectra \( dN_i/dE_\nu \) depend only on the nuclear properties of the isotope \( i \). Their determination is the main topic of this section.

In the ‘ab initio’ approach the aggregate fission antineutrino spectrum is determined by summing the contributions of all \( \beta \)-decay branches of all fission fragments

\[ \frac{dN_i}{dE_\nu} = \sum_n Y_n(Z, A, t) \sum_j b_{n,j}(E_0^j) P_\nu(E_\nu, E_0^j, Z) \]  

where \( Y_n(Z, A, t) \) is the number of \( \beta \) decays of the fragment \( Z, A \) at time \( t \), and the label \( n \) characterizes each fragment. The quantity \( Y_n \) converges to the cumulative fission yield. The beta-decay branching ratios \( b_{n,j}(E_0^j) \) are characterized by the endpoint energies \( E_0^j \) and are normalized to unity, \( \Sigma_j b_{n,j}(E_0^j) = 1 \). The function \( P_\nu(E_\nu, E_0^j, Z) \) is the normalized \( \nu_e \) spectrum shape for the branch \( n, j \). For the corresponding aggregate fission electron spectrum, the \( E_\nu \) in the individual spectra \( P \) must be replaced by \( E_e = E_0^j - E_\nu \).

In applying the summation technique several sources of uncertainty arise. The fission yields \( Y_n \) for many important fragments involve large uncertainties. The branching ratios \( b_{n,i} \) are also not known for all fragments, and nor are the quantum numbers (spins and parity) of all of the initial and final states. The shape of the \( \beta \) decay spectrum \( P \) is simple for Gamow-Teller allowed transitions (\( \Delta I \leq 1, \pi_i \pi_f = 1 \)) transitions. However, \( \sim 30\% \) of the transitions making up the aggregate spectra are known to be so-called first forbidden transitions, (\( \Delta I \leq 2, \pi_i \pi_f = -1 \)), and involve nuclear structure dependent combinations of several operators. Finally, there are important, albeit small, corrections to the beta-decay spectra arising from radiative, nuclear finite size, and weak magnetism effects, and these can also depend on the details of the transitions.

The alternative method of determining the spectra \( dN_i/dE_\nu \) begins with the experimentally measured aggregate electron spectrum associated with the fission of each individual actinide \( i \). The electron spectrum for thermal neutron fission of \( ^{235}\text{U} \), \( ^{239}\text{Pu} \) and \( ^{241}\text{Pu} \) were measured at ILL, Grenoble, France in 1980’s [14]. \( ^{238}\text{U} \) fissions only with fast neutrons; its electron spectrum was measured much later [15] with larger error bars. These experimentally determined electron spectra are automatically summed over all fission fragments and the corresponding \( \beta \)-decay branches, so no information on the fission yields and branching ratios is needed. It is necessary, however, to convert them into the \( \nu_e \) spectra.

To convert a measured aggregate electron spectrum into an antineutrino spectrum, the spectrum is binned over an energy grid. The spectrum in each bin is fitted to a fictitious \( \beta \) decay, and therefore the aggregate spectrum is described by a sum of virtual \( \beta \)-decay
branches of assumed spectral shapes. The conversion to the antineutrino spectrum is then simply accomplished by replacing the energy $E_e$ in each branch by $E_0 - E_\nu$. The procedure guaranties that the experimental electron spectrum is well reproduced. However, the converted $\nu_e$ depends to some degree on the assumptions made about the spectrum shapes $P_i$, whether they correspond to allowed or forbidden transitions, their $Z$ dependence, and the form of the corrections arising from nuclear finite size and weak magnetism. To avoid sizable systematic errors when converting the electron spectrum, it is necessary to use the data bases and evaluate the dependence of the average nuclear charge $Z$ on the endpoint energy discussed, e.g. in [6, 16].

3 Electron and $\nu_e$ spectra of individual $\beta$ decays

The $\beta$-decay spectrum shape of each $\beta$ branch can be expressed as

$$P_\beta(E_\nu, E_0, Z) = K p_e E_e (E_0 - E_e)^2 F(Z, E_e) C(Z, E_e) (1 + \delta(Z, A, E_e)),$$

where $K$ is the normalization factor, $p_e E_e (E_0 - E_e)^2$ is the phase space factor, $F(Z, E_e)$ is the Fermi function that takes into account the effect of the Coulomb field of the daughter nucleus on the outgoing electron, and the shape factor $C(Z, E_e)$ accounts for the energy or momentum dependence of the nuclear matrix elements. For the allowed decays, $C(Z, E_e) = 1$. Finally, the function $\delta(Z, A, E_e)$ describes the subdominant corrections to the spectrum shape.

For the allowed $\beta$ decays the corrections $\delta(Z, A, E_e) = \delta_{QED} + \delta_{FS} + \delta_{WM}$ represent the few % deviations from the standard spectrum shape related to the radiative, finite nuclear size and weak magnetism. The latter two depend to some extent on the details of each transition. In practice they are replaced by the estimate of their average values; thus they must be assigned a sizable uncertainty. The evaluation in refs. [5, 6] takes this source of error presumably correctly into account. In fact, the treatment of these corrections in [5, 6] is responsible for a substantial part of the revision of the predicted flux compared with the more approximate way it was treated previously.

The treatment of the first forbidden $\beta$ decays represents even more significant source of uncertainty, which is difficult to quantify. The shape factors corresponding to different operators are listed in ref. [17]. That reference also lists the corresponding weak magnetism corrections that are rather different from those for the allowed decays. The corresponding finite size corrections have not been consistently evaluated as yet. The main difficulty, though, is that in most first forbidden decay, unlike the allowed ones, more than one operator contributes, and interference among their contributions is expected. Even though, as many textbooks claim, the shape of the first forbidden $\beta$ decays is similar to the shape of the allowed decays, deviations at few % level are expected and common. The fact that the quantum numbers of many short lived fission fragments are not known makes the quantitative analysis even more difficult.
4 The “bump” in reactor spectrum

The shoulder or so-called “bump” mentioned earlier was not observed in previous experiment. In particular, it is not present in the experimental electron spectra [14]. The shoulder could have its origin in several effects that are not included, or not included accurately, in the reactor spectrum predictions [5, 6]. The contribution of $^{238}\text{U}$, that is only weakly constrained by the observed electron spectrum might not be accurate. The harder neutron spectrum in power reactors may lead to different fission fragment distributions than in the very thermal ILL reactor used for the electron fission spectra measurements. Alternatively, the measured electron spectra themselves [14], which represent the basis for the antineutrino evaluations [5, 6], might be incorrect.

Several possible origins of the bump have been identified and investigated by different authors [18, 19], but it was generally concluded that, without further experimental investigation, it is impossible to determine which, if any or several, of the explanations are correct. In the ab initio summation method the necessary input are the fission yields, and two standard fission-yields libraries, JEFF-3.1.1 and ENDF/B-VII.1 differ [19] significantly in the predicted yields of several nuclei dominating the shoulder region. When the problems in the ENDF/B-VII.1 library were corrected, the predictions of the two databases are considerably closer, and agree within 6% at all energies. Most significantly, neither database (corrected ENDF or JEFF) now predict a bump relative to the measured $^{235}\text{U}$ aggregate electron fission spectrum.

At present, the two most likely sources of the bump seem to be $^{238}\text{U}$ or the hardness of the neutron spectrum. The $^{238}\text{U}$ spectrum is considerably harder in energy than that of the other actinides, and the ENDF/B-VII.1 and JEFF-3.1.1 libraries predict a bump relative to the $^{238}\text{U}$ antineutrino spectrum of [5] and [15]. Thus, without experiments designed to isolate the contributions from each actinide to the shoulder, $^{238}\text{U}$ cannot be ruled out as a significant source of the bump. The effect of the hardness of reactor neutron spectrum on the antineutrino spectrum has never been tested directly. The PWR reactors used by Daya Bay, RENO and Double Chooz are harder in energy than the thermal spectrum of the ILL reactor, and involve considerably larger epithermal components.

The existence of the “bump” has little effect on the extraction of the neutrino oscillation parameters from the reactor experiments and it could be entirely uncorrelated with the “reactor anomaly”. However, it raises the very serious question of how well the antineutrino spectra are known, and suggests that estimated uncertainties at the 1-2% level are too optimistic.

5 Reactor anomaly

The reactor anomaly, mentioned in the introduction, is one of several experimental results that contradicts the standard three-flavor neutrino oscillation paradigm. Clearly, this is an issue of fundamental importance, potentially a source of the long sought after “physics beyond the standard model”. In the case of the reactor $\nu_e$ capture rate the experimental data are quite firm, but the expectations depend on an assumed reactor spectrum, involving
uncertainties that are difficult to determine reliably.

The summation method requires knowledge of both the decay spectra and fission yields for all of the fragments determining the spectra, and both inputs involve uncertainties. For the decay of individual nuclei, the databases are incomplete because about 5% of the nuclei are sufficiently far from the line of stability that no measurements of the spectra are available, and thus modeling is necessary. The spectrum shape corrections involve sizable uncertainties. For the weak magnetism correction they are typically estimated to be ~20% for the allowed decays and perhaps 30% for the forbidden ones. The finite size corrections involve both the weak transition density $\rho_W$ and the charge density $\rho_{ch}$. Several density or radius approximations have been made in the literature and these differ from one another by about 50%, the tentative uncertainty. For forbidden decays that correction is even more uncertain. The database fission yields are also uncertain for many important nuclei. While it is difficult to estimate the uncertainty in the database fission yields, the tentative place uncertainty arising from their contribution to the summation method is ~10%.

Though many of the uncertainties also apply when converting a measured electron spectrum to an antineutrino spectrum, the situation is somewhat different since the fit must reproduce the electron spectrum. Nevertheless, when in ref. [19] different assumptions were made about which weak magnetism and shape factors should be applied to the non-uniquely forbidden component of the spectrum and with fits to the electron spectrum of equal statistical accuracy, the antineutrino spectrum was found to vary by as much as 4%. To determine the full effect of the uncertainties that apply to a conversion from a measured electron spectrum to an antineutrino spectrum, requires a detailed multi-parameter sensitivity study. In the absence of such a study, 5% uncertainty on the conversion method is tentatively assigned.

In general, conversion of measured aggregate electron fission spectra provide more accurate determinations of the antineutrino spectra than do predictions from the databases. The database calculations do, however, provide means of estimating the relative importance of theoretical corrections to the spectra and their uncertainties. Improving on the theoretical inputs to the spectra will be challenging. Thus, there is a clear need for new experiments. Ideally, these should involve more than one reactor design and fuel enrichment, because the remaining issues will require a better understanding of the role of the hardness of the reactor neutron spectrum and of the four individual actinides that make up total spectra. For the bump energy region, better measurements of the $^{238}$U spectrum would be particularly valuable.

This brief discussion suggests that it is possible, perhaps even likely, that both anomalies have their origin in standard physics. Decisive experiments are planned, and some of them will have results soon. Until then a diligent work on reducing the systematic uncertainties is clearly indicated.

References


