

1 **Assessment of Regional Methane Emissions Inventories through Airborne Quantification**
2 **in the San Francisco Bay Area**

3

4 **SUPPLEMENTARY INFORMATION**

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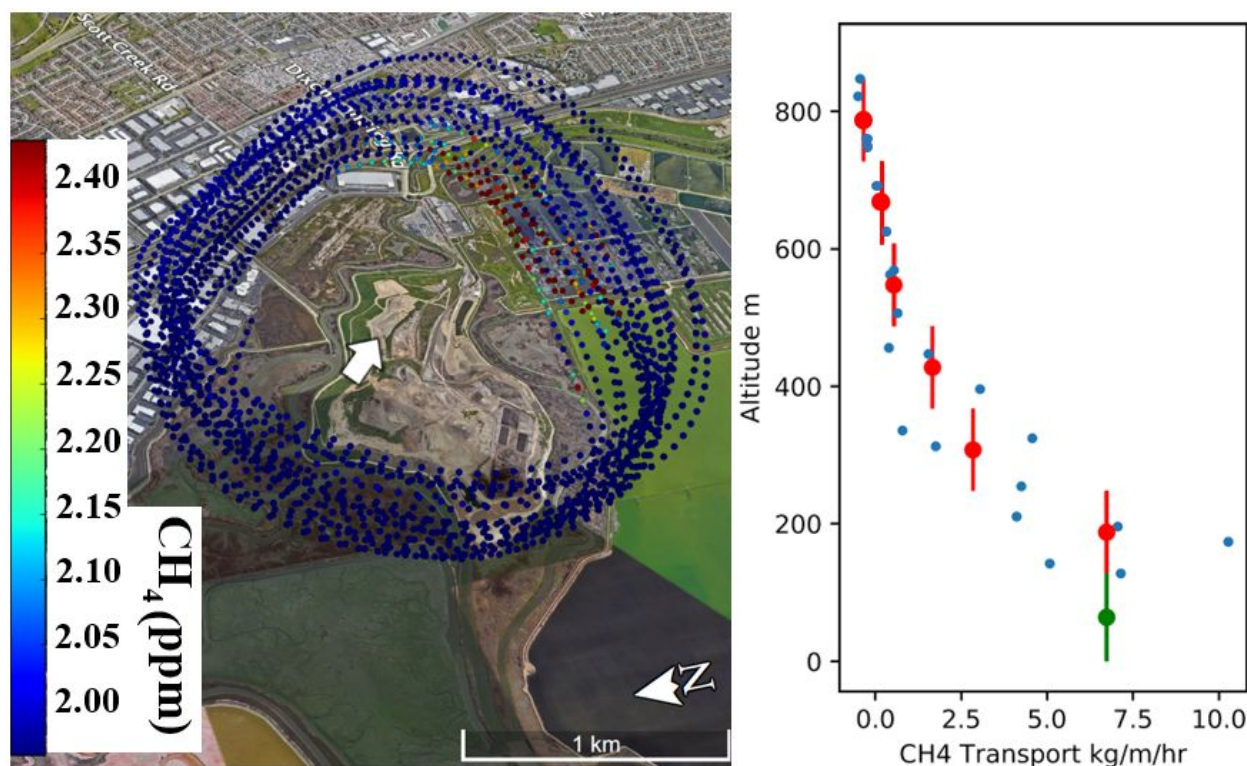
39 **APPENDIX 1 – AIRBORNE FLUX ESTIMATION METHOD**

40 **Airborne Mass Fluxes**

41 In this study, emission rates are measured using an airborne mass balance technique that
42 combines trace gas concentrations of methane, carbon dioxide and/or ethane with coincident
43 meteorological measurements. This project deployed an instrumented Mooney aircraft owned
44 and operated by Scientific Aviation to conduct emissions measurements from target sources. The
45 aircraft is outfitted with a data system that measures and records real-time aircraft speed,
46 position, altitude, and horizontal winds (accuracy < 0.5 m s⁻¹), as well as ambient temperature,
47 pressure, and relative humidity. A flight-optimized Picarro (Santa Clara, CA) cavity ringdown
48 spectrometer and an on-board data system provide fast-response, in-situ concentration
49 measurements of CH₄, CO₂, and water vapor. Many of the flights also included instrumentation
50 to measure ethane (C₂H₆) concentrations to provide a reliable source marker for fossil-fuel
51 derived CH₄ sources, since decomposition-induced biological sources of CH₄ such as landfills,
52 wastewater treatment and composting do not emit C₂H₆. We use the C₂H₆ data qualitatively to
53 confirm the source / origin of the observed CH₄ emissions.

54 The method used by Scientific Aviation and its application to quantify emissions from
55 facilities and sources have been described previously in greater detail.^{25,26} In brief, the
56 measurement approach is based on mass balance principles and Gauss's Law as described in

57 Conley et al.²⁵ For each target site, the aircraft flies a closed loop pattern around a facility,
58 beginning at the minimum safe altitude (often ~60m above ground level) and climbing
59 progressively higher, until real-time data indicate the aircraft is above the plume (Figure S1).
60 Additional loops are flown above the plume to confirm the extent of vertical mixing. The flight
61 path traces a cylinder around the target site and using the observed horizontal wind and trace gas
62 concentration enhancements (upwind-minus-downwind concentrations over background),
63 Gauss's Law is applied to estimate the flux divergence through the cylinder. Details of the
64 calculations to estimate the average emission rate for each sampled site using mass-balance
65 horizontal flux divergences are presented elsewhere.^{25,26}



66
67 **Figure S1.** Example aircraft data (A) Flight path colored by methane concentrations over Newby
68 Island landfill, showing the enhancements in CH₄ are downwind of the landfill (white arrow
69 indicates wind direction at the time of the flight); and, (B) Vertical profile of horizontal methane
70 flux divergences for the flight path where blue circles represent each horizontal loop's flux
71 divergences, red bars and circles represent the altitude bins and binned averages, respectively,
72 and the green circle is the assumed flux divergence for the layer between the lowest flight
73 altitude and the surface representing the - "ground contribution term".

74 The flux contribution of the emission plume flowing underneath the lowest aircraft sampling
75 altitude and the ground surface is estimated by investigating the Large Eddy Simulation (LES)
76 flux divergence profiles in the lowest layer and evaluating the accuracy of the approach against
77 coordinated controlled release and real-time power plant CO₂ emissions releases.²⁵

78 **Uncertainty Estimation**

79 Controlled release tests have been applied before to verify the accuracy of the cylindrical
80 mass balance method and have generated accuracies within 15% or better with an average
81 accuracy of 6%.²⁵ Since field-measurement flights often take place in less than optimal
82 conditions as compared to the controlled release tests, the Scientific Aviation method estimates
83 uncertainties for each target measurement. The main uncertainty term arises from the prediction
84 of flux below the lowest flight altitude, and this is minimized by prior LES studies that have been
85 used to determine a downward distance that provides very little change in the plume flux
86 divergence from the lowest loop to the ground.²⁵ The uncertainty in the final emission rate
87 produced by the Scientific Aviation method is determined by summing in quadrature terms
88 representing a binning error from the standard deviations of the horizontal flux divergences for
89 the individual closed-path loops within each altitude bin (assumed to provide an estimate of
90 variability from turbulence), error due to the number of loops flown around a facility, uncertainty
91 term due to not capturing the horizontal efflux below the lowest leg of the aircraft profile, and
92 the uncertainty due to the lack of consistency of the wind velocity during the observations over a
93 target facility.^{25,26} The uncertainty in horizontal flux for each closed-loop path is estimated from
94 the uncertainty in the wind measurement and the uncertainty in the chemical species
95 measurement, summed in quadrature.²⁵

96 The successful application of the Scientific Aviation method for quantifying emissions
97 relies upon favorable wind conditions and adequate vertical mixing. Ideal wind conditions are
98 moderate and steady in both speed and direction. Completely calm conditions, very high wind
99 speeds, or rapidly varying wind directions are not ideal for this method and introduce large
100 errors. The highest degree of confidence in the results require sampling most of the plume at and
101 above the lowest flight altitude and below the top of the boundary layer to ensure complete
102 sampling of the entire plume. Under ideal conditions, emissions uncertainties $\leq 10\%$ can be
103 achieved. Conditions that are less than ideal increase the uncertainty in the resulting flux. For
104 this study, the mean of the individual emissions uncertainties across all site-assessments was
105 25% with a range of 9-76%.

106

107 **APPENDIX 2 – ESTIMATION OF ACTUAL DAY-TO-DAY VARIATION**

108 Although not shown, there was no appreciable trend or seasonality. The data were
109 clustered in time, specifically during the 2nd and 4th quarters of the calendar year; there were only
110 two observations in the 1st quarter and none in the 3rd. There was significant day-to-day
111 variation, however, on the order of four times the measurement error variance. This analysis
112 addresses the question of whether there is evidence of day-to-day variation in refinery emissions
113 evident above measurement error. We note that as long as this variation is “random” in the sense
114 that the choice of days the airplane flights occurs is independent of the actual emissions, then the
115 above estimates should be valid.

116 There are several approaches. We can analyze the data on the original, linear scale or the
117 log scale, and we can consider the uncertainties as fixed and known or themselves only estimates
118 of the true measurement errors.

119 **Approach 1 – Original scale**

120 Each of the 41 measurements came with a corresponding uncertainty estimate. Let
121 observations from a particular refinery be Y_1, Y_2, \dots, Y_n , and let u_1, u_2, \dots, u_n be the
122 corresponding uncertainties. Assume the Y_j have the same mean, μ , but different variances, σ_j^2 ,
123 $j=1, \dots, n$. let $S = \sum_{j=1}^n (Y_j - \bar{Y})^2$. Then, after some algebra, the uncertainty, $E(S)$, is given by E
124 $(S) = \frac{n-1}{n} \sum \sigma_j^2$ or $\frac{E(S)}{n-1} = \overline{\sigma^2}$. If all the σ_j^2 were equal ($\sigma_j^2 \equiv \sigma^2$), and σ^2 were known, then S/σ^2
125 would have an approximately chisquare distribution. If we instead divide S by the mean of the
126 σ_j^2 , then $S/\overline{\sigma^2}$ would likely be longer-tailed, but perhaps a chisquare distribution would be a
127 good first approximation, an upper bound, at least. Alternatively, to roughly account for the fact
128 that the u_j are also estimates of σ_j , we could assume that $F = \frac{S}{(n-1)u^2}$ has an F distribution, with

129 n-1 df in the numerator, and n df in the denominator. The table below shows the results by
 130 refinery, and also where the refineries are pooled.

131 **Table S1.** Summary of statistical tests run on the refinery emissions data.

Tests for actual variation					p-values	
Refinery	# obs	S/(n-1)	$\overline{u^2}$	F	Chisquare	F
Marathon	7	29,244	8,182	3.6	0.002	0.073
Chevron	7	28,938	28,233	1.0	0.407	0.488
Phillips	10	29,977	15,158	2.0	0.038	0.162
Shell	6	343,928	19,519	17.6	<0.001	0.003
Valero	11	23,618	11,324	2.1	0.022	0.131
Combined	41	75,760	15,809	5.1	<0.001	<0.001

132
 133 Individual tests are clearly significant only for the Shell refinery, though borderline
 134 significant for Marathon and Valero. However, combining all five refineries does produces a
 135 highly significant result and an F-statistic of roughly 5. But note that the numerator of Approach
 136 1 incorporates the uncertainty variance plus the true day-to-day variance. This suggests that the
 137 day-to-day variance is roughly $5 - 1 = 4$ times the measurement error.

138 **Approach 2 – Log scale**

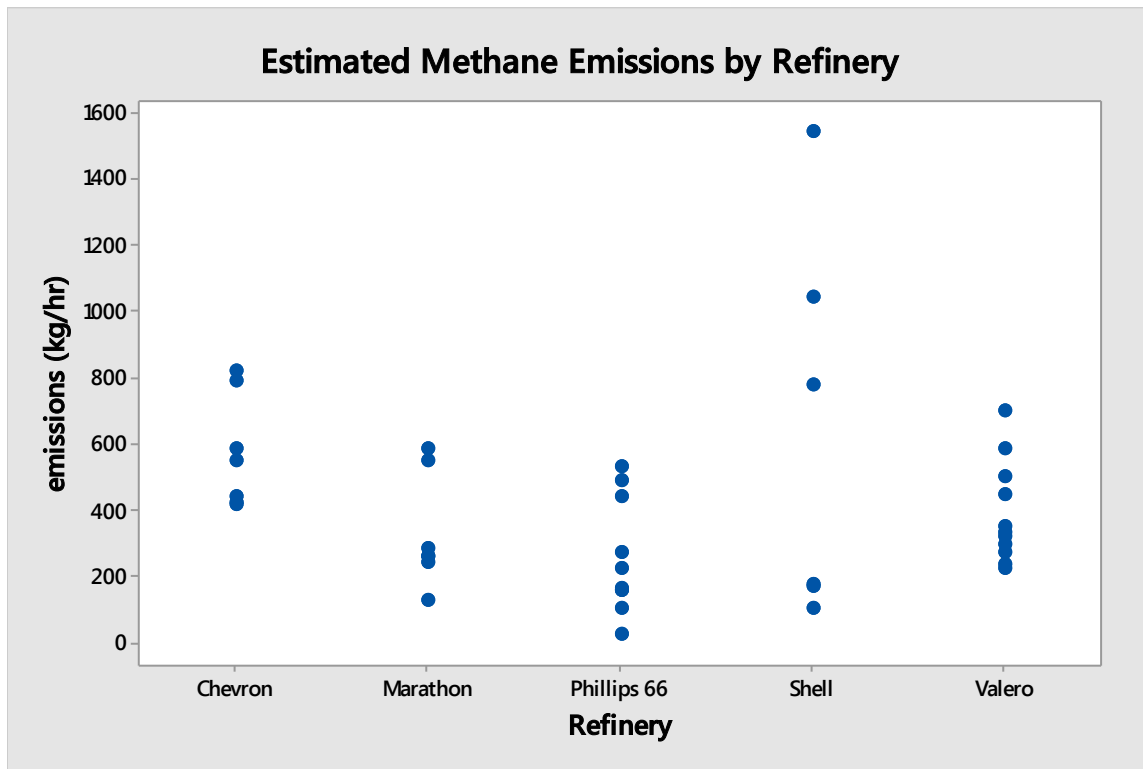
139 As demonstrated in Appendix 3, the data appear to fit a log-normal model reasonably well. The
 140 model incorporates both measurement error, $\text{Var}(U)$, and the actual day-to-day variance,
 141 $\text{Var}(W)$. The fitted model estimated a true variance of $\hat{\sigma}^2 = 0.347$. This compares with an
 142 estimated mean of the log uncertainties = 0.09. The estimated ratio of $\text{Var}(W)$ to $\text{Var}(U)$ is thus
 143 $0.347/0.09 = 3.8$. This ratio is similar to that found in Approach 1.

144 **APPENDIX 3 – ANALYSIS OF REFINERY METHANE EMISSIONS DATA**

145 There are 41 aircraft measurements from the 5 Bay Area refineries from which to
146 develop estimates of their total hourly average methane (CH₄) emissions and the uncertainty of
147 these estimates. Two statistical methods yield essentially the same estimates, and simulations
148 also show a similar range of values as traditional confidence intervals. We estimate total CH₄
149 emissions from the five refineries at 19,000 mt/yr, with a 95% confidence interval of 15,500
150 mt/yr to 22,800 mt/yr.

151 **Data**

152 A total of 41 measurements were made between 2015 and 2018. Figure S2 shows a dot
153 plot by refinery.

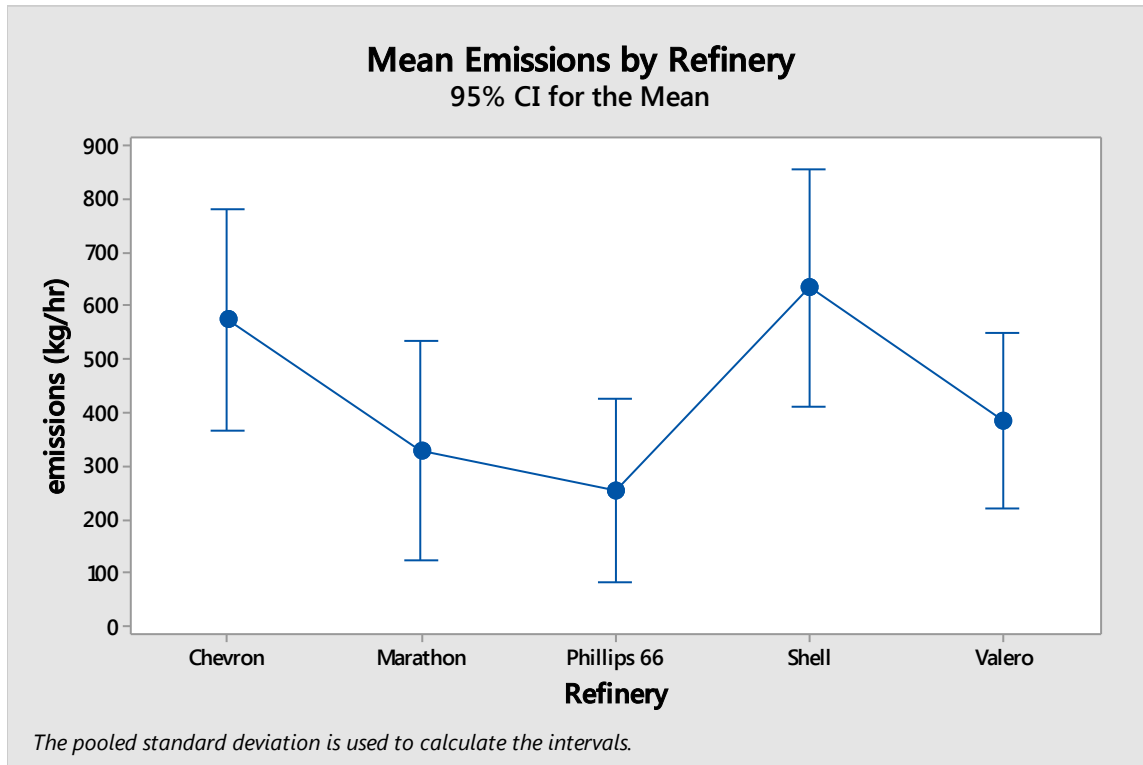


154 **Figure S2.** Estimated Methane Emissions by Refinery.

156 **Estimation Methods**

157 The goal was to estimate total emissions, T, from the 5 refineries, or $T = m_1 + m_2 + m_3 +$
158 $m_4 + m_5$, where m_i = estimated mean hourly CH₄ emissions from the *i*th refinery. The simplest

159 estimate would assume that the emissions rates from the refineries were equal: $m_i \equiv m$, and
 160 estimate the total emissions as $T = 5m$, where m is the arithmetic mean of the 41 measurements.
 161 However, a 1-way analysis of variance found statistical differences among the refineries
 162 ($p=0.044$). Figure S3 shows the refinery means and 95% confidence intervals. Thus, from this
 163 point, we do the analysis estimating separate means for each refinery.



164
 165 **Figure S3.** Means and 95% confidence intervals by refinery.

166 Because the measurement uncertainties differ, we considered using mean estimates with
 167 inverse variance weighting, which can produce more efficient estimators. But, as shown later in
 168 Figure S5, the uncertainties are correlated with the individual values. Thus, a weighted average
 169 would produce biased results. So, here we use simple arithmetic means.

170 Let \bar{y}_i be the arithmetic mean of the n_i measurements from refinery i , and estimate $T = \bar{y}_1$
 171 $+ \bar{y}_2 + \dots + \bar{y}_5$. Assuming that the variances are equal, we can compute a pooled variance

172 estimate: $s^2 = \frac{\sum_{i=1}^5 \sum_{j=1}^{n_i} (y_{ij} - \bar{y}_i)^2}{41 - 5}$, where y_{ij} is the j th observation from refinery i . The estimated

173 standard error of T is the square root of $\tau^2 = s^2 \sum_{i=1}^5 \frac{1}{n_i}$. This method provides an unbiased
174 estimator as long as the observations can be considered to be collected at random. A 100*(1-
175 α)% confidence intervals based on the t-distribution is:

$$176 \quad T \pm t_{41, \alpha/2} * \tau \quad (1)$$

177 **Bootstrap estimate of uncertainty**

178 We simulate T by sampling from each refinery's observations with replacement.
179 Specifically, we can randomly select y_{ij}^* from $\{y_{i1}, y_{i2}, \dots, y_{ini}\}$, with replacement, $j=1, \dots, n_i$, for i
180 $= 1, \dots, 5$, (in other words, generating new random samples of size 41 from the original data) and
181 compute $T^* = \bar{y}_1^* + \dots + \bar{y}_5^*$, where $\bar{y}_i^* = \frac{1}{n_i} \sum_{j=1}^{n_i} y_{ij}^*$. This yields the same estimated mean
182 and variance but provides different (and probably more realistic) lower and upper confidence
183 interval bounds due to the skewness of the underlying data.

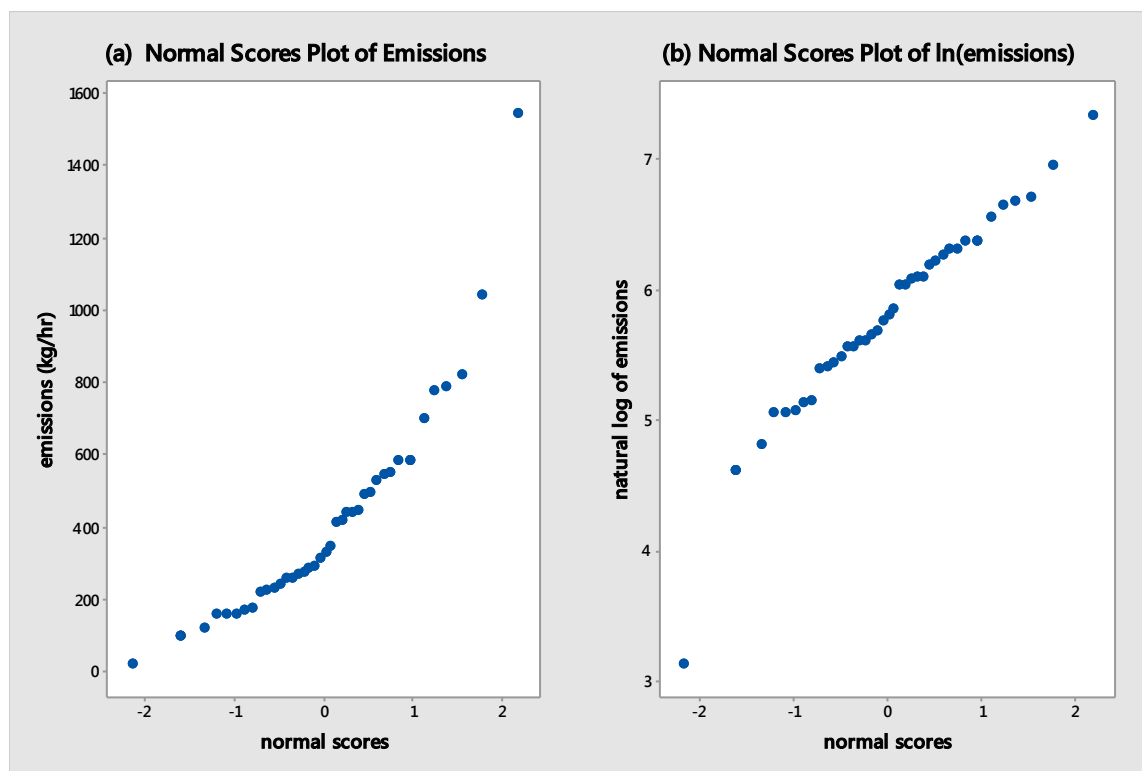
184 **Parametric approach**

185 Generally, we can get more efficient estimators (that is, having less uncertainty) if we
186 know the approximate distribution of the data and we use a parametric approach tailored to that
187 distribution. Also, for these data the individual measurements have different uncertainties, so it
188 would be preferable if these could be incorporated into the analysis.

189 The simplest situation would be if the data were normally distributed. A normal scores
190 plot¹ suggests the data are right-skewed, i.e., non-normal (Figure S4). Because the data are a
191 mixture of distributions with different means, a simple test of normality such as the Shapiro-
192 Wilk test can't be applied. Instead we constructed a test using the mean of Shapiro-Wilk
193 statistics for each refinery, i.e., $S = \sum_{i=1}^5 W_i/5$, where W_i is the Shapiro-Wilk statistic for

¹ A normal scores plot shows the data versus the expected values of the order statistics from a sample of the same size of standard normal random variables. If the data were normal, the points should lie close to a straight line. If the points are concave as in Figure S4a, this indicates the data are right-skewed.

194 refinery $i, i=1, \dots, 5$. We simulated the value of S 100,000 times, using pseudo-random normal
195 variates. The observed value of S was 0.87, with a p-value of 0.037, based on the simulation.

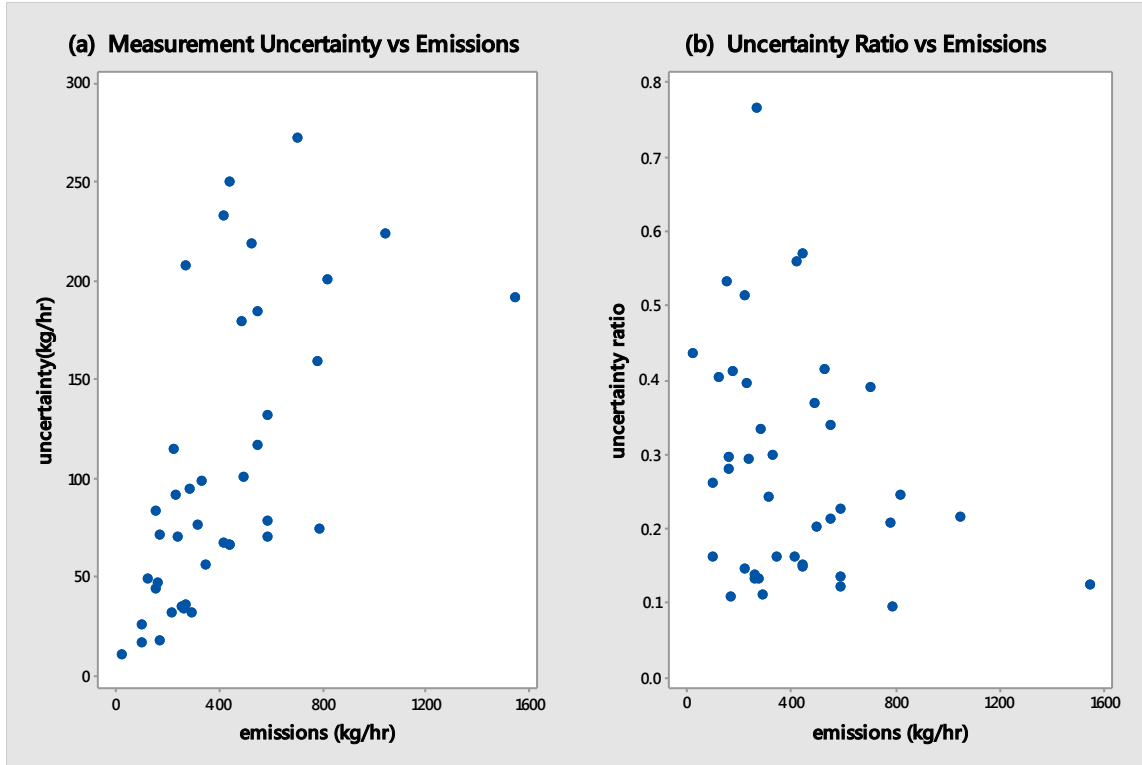


196
197 **Figure S4.** Normal scores plots of the (a) estimated emissions, and, (b) their log values.

198 For the natural logs of the data (Figure S4b), the figure doesn't suggest non-normality.

199 The value of S for the logs of the data was 0.90, with a p-value of 0.17. Here, normality can't be
200 rejected, so we assume the data are log-normally distributed.

201 A second issue is how to deal with the uncertainties. Figure S5a shows that uncertainties
202 increase as emissions increase. Figure S5b shows the ratios of uncertainty to emissions. Here
203 there is no significant correlation, so that the percent uncertainty appears independent of the
204 magnitude of the emissions.



205
 206 **Figure S5.** Estimated refinery emissions plotted against (a) absolute value of uncertainties, and,
 207 (b) uncertainties as percentage of magnitude of emissions.

208 Given the results of Figure S5, it is reasonable to model the measurement error as
 209 multiplicative, that is, that a measured value is the product of the true emissions times
 210 measurement error. This dovetails with the assumption that the data are log-normally
 211 distributed, since the error becomes additive on the log scale. We model the data on the original
 212 scale as $Y = WU$, where U = measurement error and W = true (but unobserved) actual emissions.
 213 Assume that both W and U are log-normally distributed and that they are statistically
 214 independent. Also assume that $E(U) = 1$, so that the measurement provides an unbiased
 215 estimator of W , that is, $E(Y|W) = W$. The goal will be to estimate $E(W)$.

216 Since U is lognormally distributed, $E(U) = e^{\vartheta + \frac{\sigma^2}{2}} = 1$ by assumption. Or, taking logs,
 217 $\vartheta + \frac{\sigma^2}{2} = 0$, so that we need $\vartheta = -\frac{\sigma^2}{2}$. With this constraint, we have $Var(U) = (e^{\sigma^2} - 1)e^{2\vartheta + \sigma^2}$
 218 $= e^{\sigma^2} - 1$. We've been given the measurement error of Y , say σ_Y , which suggests that the

219 measurement error (sd) of U given Y would be σ_Y/Y . Combining this with $\text{Var}(U)$, we get *Var*

220 $(U|Y) = e^{\sigma^2} - 1 = \frac{\sigma_Y^2}{Y^2}$, or $\sigma^2 = \ln\left(1 + \frac{\sigma_Y^2}{Y^2}\right)$. Let's first consider an individual refinery with n

221 observations. Let $\ln(W_j) \sim \text{Normal}(\mu, \sigma^2)$, $j = 1, 2, \dots, n$. Based on the assumptions above,

222 $\ln(U_j) \sim \text{Normal}(-\frac{\sigma_j^2}{2}, \sigma_j^2)$, where $\sigma_j^2 = \ln\left(1 + \frac{\sigma_{Y_j}^2}{Y_j^2}\right)$, for the jth observation. We take σ_j^2 as known.

223 Then $X = \ln(Y) = \ln(W) + \ln(U)$ is the sum of two independent normal random variables so its

224 distribution is also normal, with mean $\mu - \frac{\sigma_j^2}{2}$, and variance $\sigma^2 + \sigma_j^2$. We can write the joint

225 likelihood of the X_j as: $L = \prod_{j=1}^n \frac{1}{\sqrt{2\pi(\sigma^2 + \sigma_j^2)}} e^{-\frac{(x_j - \mu + \frac{\sigma_j^2}{2})^2}{2(\sigma^2 + \sigma_j^2)}}$. Taking logs:

$$226 \quad l = \ln(L) = -\frac{n}{2} \ln(2\pi) - \sum_{j=1}^n \ln(\sigma^2 + \sigma_j^2) - \sum_{j=1}^n \frac{(x_j - \mu + \frac{\sigma_j^2}{2})^2}{2(\sigma^2 + \sigma_j^2)}.$$

227

228 Taking the derivative of the log likelihood with respect to μ and setting it equal to 0, we can find

229 its maximum likelihood estimator (mle): $\hat{\mu} = \sum_{j=1}^n u_j (x_j + \frac{\sigma_j^2}{2})$, where $u_j = \frac{1}{\hat{\sigma}^2 + \sigma_j^2} [\sum_{k=1}^n \frac{1}{1\hat{\sigma}^2 + \sigma_k^2}]^{-1}$

230 , and $\hat{\sigma}^2$ is the mle of σ^2 . Since $E(W) = e^{\mu + \frac{\sigma^2}{2}}$, the mle of $E(W)$ is just $e^{\hat{\mu} + \frac{\hat{\sigma}^2}{2}}$.

231 This approach could be applied, computing each mean separately although this involves

232 estimating 10 parameters with only 41 observations. Another approach is to estimate μ

233 separately by refinery but assume that σ^2 is the same. This requires estimating 6 parameters –

234 still a lot, but not unreasonable. We call this estimate T_2 . An R script was written to compute

235 the estimates of the μ_i and σ^2 by maximizing the log likelihood. Calculating the uncertainty of

236 this estimator is difficult. Instead we derived a confidence interval by simulating the
237 distributions of W and U.

238 **Results**

239 **Estimate 1. Using separate arithmetic means for the 5 refineries.** Here the estimated $T_1 =$
240 2,171, with a pooled standard deviation estimate of 267. The estimated se is: 214. Using
241 equation (1), a 95% confidence interval for T_1 is 1,720 kg/hr to 2,600 kg/hr.

242 **Bootstrap simulation of Estimate 1.** Based on a simulation of 10,000 bootstrap samples T_b has
243 a 95% confidence interval of 1,720 kg/hr to 2,670 kg/hr.

244 **Estimate 2. Assuming observations log-normally distributed with different μ and same σ^2**
245 **across refineries.** The estimated μ_i were 5.72, 6.39, 5.33, 6.02, and 5.90 for Marathon,

246 Chevron, Phillips, Shell, and Valero, respectively, and $\hat{\sigma}^2 = 0.347$. So $T_2 = \sum_{i=1}^5 e^{\hat{\mu}_i + \frac{\hat{\sigma}^2}{2}}$
247 = 2,240 kg/yr. A simulation was performed here also, yielding a 95% confidence interval of
248 1,770 kg/yr to 2,840 kg/yr.

249 **Discussion**

250 Estimates using the log-normal yielded somewhat higher totals than arithmetic means.
251 But the two estimates were well within the 95% confidence interval of the other. The
252 uncertainty ranges were similarly wide. There was no appreciable benefit in terms of reduced
253 variability to using a parametric approach. Thus, we use the simpler Estimate 1 for the point
254 estimate 2,194 kg/hr, or $24 \cdot 365 / 1000 \cdot 2171 = 19,000$ mt/year, rounded to the nearest hundred,
255 and the 95% confidence interval 1,680 to 2,720 kg/hr, or 15,500 to 22,800 mt/year based on the
256 bootstrap simulation.

257

258 **APPENDIX 4 – ESTIMATION OF UNCERTAINTY IN SECTOR-WIDE EMISSIONS**

259 For landfills and POTWs, we estimate total emissions, T , as $T_S + T_U$, where T_S and T_U represent
 260 the total emissions for sampled and unsampled facilities, respectively. For the uncertainty of T , it
 261 is noted that T_S and T_U are not statistically independent because they are both linear functions of

262 the \bar{y}_i : $T_S = \sum_{i \in S} a_i \bar{y}_i$, where $a_i = 1$, and $T_U = \sum_{i \in S} b_i \bar{y}_i$, where $b_i = \frac{x_i}{(\sum_{j \in U} x_j) \sum_{j \in S} x_j^2}$

263 = *constant* * x_i . Using the general formula for the variance of two random variables yields

264 $\text{Var}(T) = \text{Var}(T_S) + 2*\text{Cov}(T_S, T_U) + \text{Var}(T_U)$. The general formula for the covariance of two

265 linear combinations of random variables, $U =$

266 $\sum a_i X_i$ and $V = \sum b_i X_i$, is $\text{Cov}(U, V) = \sum_i \sum_j a_i b_j \text{Cov}(X_i, X_j)$. In the present case, we assume the

267 \bar{y}_i are mutually independent and have the same variance, σ^2 , say. So $\text{Cov}(T_S, T_U) = \sum_{i \in S} a_i b_i \sigma^2$

268 = $\sigma^2 \sum_{i \in S} a_i b_i$.

269 Letting $\mathbf{a}' = (a_1, a_2, \dots, a_k)$ and $\mathbf{b}' = (b_1, b_2, \dots, b_k)$, where $k =$ number of elements in S , Cov

270 $(T_S, T_U) = \sigma^2 \mathbf{a}' \mathbf{b}$. Also $\text{Var}(T_S) = \text{Cov}(T_S, T_S) = \sigma^2 \mathbf{a}' \mathbf{a}$, and similarly, $\text{Var}(T_U) = \text{Cov}$

271 $(T_U, T_U) = \sigma^2 \mathbf{b}' \mathbf{b}$. Thus, the correlation between T_S and T_U is $\rho = \frac{\sigma^2 \mathbf{a}' \mathbf{b}}{\sqrt{\sigma^2 \mathbf{a}' \mathbf{a} * \sigma^2 \mathbf{b}' \mathbf{b}}} = \frac{\mathbf{a}' \mathbf{b}}{\sqrt{\mathbf{a}' \mathbf{a} * \mathbf{b}' \mathbf{b}}}$, which

272 is just the cosine of the angle between \mathbf{a} and \mathbf{b} . Since $\mathbf{a} =$ the $\mathbf{1}$ vector, and $\mathbf{b} =$ constant * x_i , the

273 correlation is the cosine of the angle between $\mathbf{1}$ and \mathbf{x} , where $\mathbf{x}' = (x_1, x_2, \dots, x_k)$. Then

274 $\text{Cov}(T_S, T_U) = \rho \text{Var}(T_S) \text{Var}(T_U)$. Using the general formula for the standard deviation of the

275 sum of two variables, we estimate $\sigma_T = \sqrt{\sigma_{T_S}^2 + 2\rho\sigma_{T_S}\sigma_{T_U} + \sigma_{T_U}^2}$.

276

277 **APPENDIX 5 – ALTERNATE ANALYSIS OF COMPOSTING SECTOR EMISSIONS**
278 **USING EMISSION-TO-THROUGHPUT RATIOS (MIDPOINT METHOD)**

279 With observations from only 2 compost facilities, we can only get a rough idea of the
280 total CH₄ emissions from compost facilities and an even rougher estimate of uncertainty. One
281 way or the other, we want to scale up the estimated emissions from these 2 to all of the facilities
282 using throughput as a surrogate. One approach is a regression through the origin. Since only the
283 slope is fit, that leaves 1 degree of freedom to estimate uncertainty.

284 An alternative, shown here, is to ignore any correlation between these 2 facilities and
285 their corresponding throughput estimates, and scale up based on the ratio of total throughput (T)
286 to the throughput from these 2 facilities ($T_0 = T_1 + T_2$, where T_1 and T_2 are the throughputs from
287 the 2 facilities), and estimating $C = \text{total CH}_4 \text{ emissions}$ from $C_0 = C_1 + C_2$ by $C = T/T_0 * C_0$. Let
288 C_1 and C_2 be the mean of the CH₄ measurements from the 2 facilities. If we consider them as
289 randomly selected from the set of all compost facilities, then they are independent with mean $\mu =$
290 mean emissions from the facilities and variance σ^2 .

291 To estimate uncertainty, we use the usual sample standard deviation, s , where $S^2 =$
292 $\frac{\sum_1^2 (c_i - \bar{c})^2}{2 - 1}$. This works out to $S^2 = (c_1 - c_2)^2 / 2$, so $s = |c_1 - c_2| / \sqrt{2}$. $C_0 = C_1 + C_2$, so variance
293 of $C_0 = \sigma^2 + \sigma^2 = 2\sigma^2$, and its standard deviation is $\sqrt{2} * \sigma$. So we estimate the standard
294 deviation of C_0 as $\sqrt{2} * s = |c_1 - c_2|$. Then the standard error of C is just $T/T_0 * s$.

295 **Results**

296 $x_1 = 328 \text{ kg/hr} = 2.88 \text{ Gg CH}_4/\text{yr}$

297 $x_2 = 175 \text{ kg/hr} = 1.54 \text{ Gg CH}_4/\text{yr}$

298 $T_1 = 533 \text{ thousand metric tons/yr}$

299 $T_2 = 80 \text{ thousand metric tons/yr}$

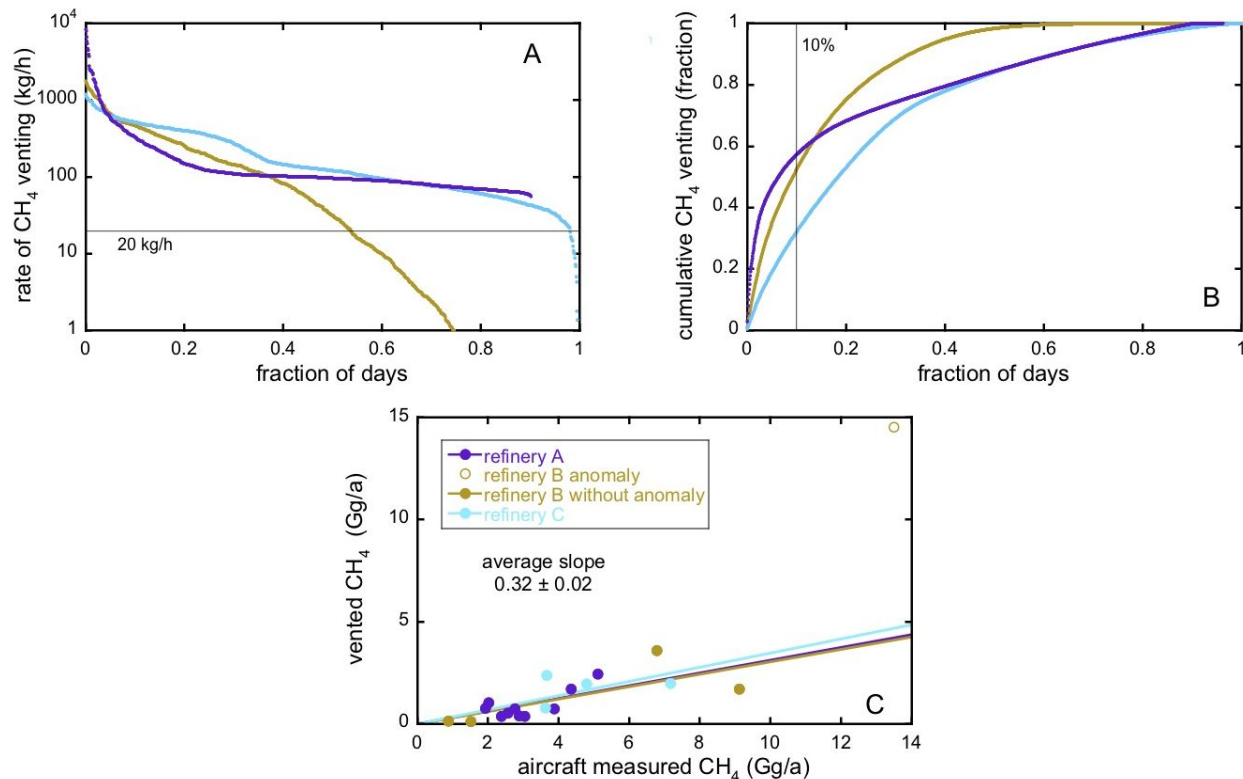
300 $T_0 = 1546 \text{ thousand metric tons/yr}$

301 → Estimated total CH₄ emissions = C = 1546/(533+80)*(2.88+1.54) = 11.1 Gg CH₄/yr.

302

303 → Standard error of C = 1546/613*|2.88-1.54| = 3.4 Gg CH₄/yr.

304



305
 306 **Figure S6** – CH₄ emissions derived from refinery reported H₂ venting data at three SFBA
 307 refineries not equipped with Pressure Swing Adsorption technology and with atmospheric vents
 308 at H₂ plants. The panels plot the averaged vented daily CH₄ emission rates (Figure S6A) and
 309 cumulative fractional total of CH₄ emissions released into the atmosphere (Figure S6B) against
 310 the fraction of total days that CH₄ is vented in a ~3-4 year period (2015-18). Figure S6C shows
 311 the correlation between aircraft-measured facility-scale CH₄ emissions and the corresponding
 312 daily vented CH₄ emission rate derived from H₂ plant data. The total number of days for which
 313 H₂ venting data is available is 1387 (Refinery A), 1096 (Refinery B) and 1124 (Refinery C) days.

314

315 **Table S2:** List of airplane-measured facility-scale CH₄ and CO₂ emissions rate over five SFBA
316 refineries between 2015-18. The “Campaign” column indicates the agency (CEC – California
317 Energy Commission, ARB – California Air Resources Board, BAAQMD – Bay Area Air
318 Quality Management District) that funded the corresponding measurement flight.

Facility name	Campaign	Date	Methane	Measurement	Carbon Dioxide	Measurement
			Mass Rate	Uncertainty	Mass Rate	Uncertainty
(kg/h)						
Phillips Rodeo	CEC	2/16/2015	271	207	179416	48152
	CEC	5/12/2015	488	179	407069	33287
	CEC	5/15/2015	222	114	262140	53836
	CEC	6/16/2015	527	218	151568	16948
	CEC	5/23/2016	23	10	176504	11204
	BAAQMD	10/10/2016	159	47	299541	73368
	BAAQMD	12/19/2016	157	44	404220	42517
	ARB	10/5/2017	156	83	208256	120456
	BAAQMD	5/9/2018	100	26	257660	35230
	ARB	10/6/2018	439	66	301174	40438
Tesoro Martinez	CEC	5/13/2015	283	94	155080	59413
	CEC	5/15/2015	239	70	240533	16313
	CEC	5/23/2016	258	35	274634	13303
	BAAQMD	10/10/2016	259	34	313391	91139
	BAAQMD	12/20/2016	585	70	467486	55990
	ARB	10/6/2017	546	184	497760	87407
	BAAQMD	4/11/2018	122	49	156154	56323
	CEC	2/16/2015	700	272	417444	20589
Valero Benicia	CEC	5/13/2015	315	76	445250	34918
	CEC	5/15/2015	220	32	218778	28701
	CEC	6/16/2015	231	91	395421	21012
	CEC	5/20/2016	584	78	306688	15534
	CEC	5/23/2016	293	32	213983	7079
	CEC	6/10/2016	329	98	NA	NA
	BAAQMD	10/5/2016	347	56	369182	67994
	BAAQMD	10/10/2016	272	36	308881	32478
	BAAQMD	4/11/2018	497	100	485409	65732
	ARB	10/6/2018	443	66	302806	40508
Shell Martinez	BAAQMD	10/5/2016	100	16	564717	112847
	BAAQMD	11/9/2016	1540	191	777818	100606
	BAAQMD	11/11/2016	173	71	198460	58674
	BAAQMD	4/11/2018	1041	223	342567	57897
	BAAQMD	6/21/2018	774	159	534424	74239
	ARB	10/7/2018	168	18	618500	44940

Facility name	Campaign	Date	Methane	Measurement	Carbon Dioxide	Measurement
			Mass Rate	Uncertainty	Mass Rate	Uncertainty
			(kg/h)			
	BAAQMD	10/10/2016	585	132	428456	147778
	BAAQMD	11/9/2016	787	74	472533	74238
Chevron Richmond	ARB	10/5/2017	440	250	351743	137663
	BAAQMD	4/21/2018	418	233	527907	213887
	BAAQMD	5/9/2018	414	67	675761	79344
	ARB	10/5/2018	819	200	596532	138009
	ARB	10/6/2018	548	116	429953	59157

319

320

321 **Table S3:** List of SFBA’s landfill facilities with permit-based prior CH₄ inventory emission
 322 estimates. Facilities sampled using airplane approach are highlighted in orange.

Facility	City	Methane emissions		
		2016	2017	2018
		(metric tons)		
Waste Management of Alameda County (Altamont)	Livermore	8768	8340	7957
Keller Canyon Landfill Company	Pittsburg	6426	3936	3936
International Disposal Corp of CA (Newby Island)	Milpitas	6075	7725	8442
Browning-Ferris Industries of CA, Inc (Ox Mountain)	Half Moon Bay	5651	6012	6012
Redwood Landfill Inc	Novato	3899	4201	4304
Guadalupe Rubbish Disposal	San Jose	3279	3010	2231
Kirby Canyon Recycling and Disposal Facility	San Jose	3062	3332	4164
Republic Services Vasco Road, LLC	Livermore	2703	2678	2845
Potrero Hills Landfill, Inc	Suisun City	2472	4201	4033
Republic Services of Sonoma County, Inc	Petaluma	2363	4596	4710
Waste Management of Alameda County	Fremont	2215	2236	2168
West Contra Costa County Landfill	Richmond	2146	2146	2146
Cypress Amloc Land Co , Inc	Colma	998	790	695
City of Mountain View (Shoreline Landfill)	Mountain View	992	1129	1164
Waste Management Inc	San Leandro	646	603	615
Acme Fill Corporation	Martinez	547	547	483
Recology Pacheco Pass	Gilroy	544	484	475
Clover Flat Resource & Recovery Park	Calistoga	415	415	446
Napa-Vallejo Waste Management Authority	Napa	406	383	413
City of Santa Clara	Santa Clara	398	350	12
Zanker Road Resource Management,Ltd	San Jose	361	361	361
TRC	Antioch	314	296	291
Turk Island Solid Waste Disposal Site	Union City	305	252	229
Cal-Pox, Inc	San Rafael	234	234	234
Sunquest Properties Inc	Brisbane	223	223	223
City of Berkeley/Engr Div/Public Works	Berkeley	166	196	23
Zanker Road Material Processing Facility	San Jose	166	168	168
Shoreline Amphitheatre	Mountain View	130	130	93
City of Alameda, Maint Serv Center	Alameda	110	110	0
City of San Jose (Singleton Road Landfill)	San Jose	103	83	66
Bayview Business Park Owner's Association	San Rafael	66	66	66
Pleasanton Garbage Service, Inc	Pleasanton	50	55	18
Spirit HD Colma CA, LP	Colma	37	21	13
City of Palo Alto Landfill	Palo Alto	19	19	20
City of Burlingame, Waste Water Treatment Plant	Burlingame	9	9	7
County of Santa Clara	San Jose	7	14	36
City of Menlo Park	Menlo Park	4	4	4
City of Sunnyvale/Public Works Dept	Sunnyvale	4	4	4
	Total	56313	59359	59107

323 **Table S4:** Summary of airplane-measured facility-scale emissions rate over ten SFBA landfills
 324 from year 2015-19. The “Campaign” column indicates the agency (ARB – California Air
 325 Resources Board, CalRecycle – California Department of Resource Recycling and Recovery,
 326 BAAQMD – Bay Area Air Quality Management District) that funded the corresponding
 327 measurement flight.

Facility	Campaign	Date	Methane	Measurement	BAAQMD	EPA	
			Mass Rate	Uncertainty	Inventory	GHGRP	
(kg/h)							
Altamont	BAAQMD	11/09/2016	2132	424	1001	812	
	BAAQMD	12/19/2016	1983	295	1001	812	
	ARB	10/06/2017	2977	653	952	778	
	ARB & CalRecycle	12/07/2017	1358	547	952	778	
	BAAQMD	05/11/2018	2010	267	908	778	
	ARB & CalRecycle	08/27/2018	2077	240	908	778	
	Vasco	BAAQMD	12/20/2016	536	121	309	144
BAAQMD		05/11/2018	807	157	325	160	
BAAQMD		10/12/2016	931	211	734	700	
Keller Canyon	ARB	10/06/2017	640	209	449	605	
	BAAQMD	03/26/2018	1339	277	449	605	
	BAAQMD	3/28/2018	1130	355	449	605	
	BAAQMD	6/21/2018	396	145	449	605	
	BAAQMD	8/23/2018	1127	171	449	605	
	ARB	10/5/2018	1361	209	449	605	
	BAAQMD	6/27/2019	1115	156	449	605	
Newby Island	BAAQMD	11/11/2016	2893	1173	693	640	
	ARB	10/05/2017	2075	587	882	769	
	BAAQMD	04/20/2018	2214	402	964	769	
	BAAQMD	08/25/2018	2442	387	964	769	
	ARB	10/05/2018	3287	487	964	769	
Potrero Hills	ARB	10/06/2017	2292	385	480	394	
	ARB & CalRecycle	12/07/2017	2004	417	480	394	
	BAAQMD	04/20/2018	1799	532	460	394	
	ARB & CalRecycle	08/23/2018	1718	252	460	394	
	ARB	10/05/2018	919	286	460	394	
	Redwood	BAAQMD	12/20/2016	660	166	445	507
		ARB & CalRecycle	11/17/2017	140	42	480	618
BAAQMD		04/11/2018	505	102	491	618	
BAAQMD		05/09/2018	422	52	491	618	

Sonoma County	BAAQMD	07/17/2018	796	122	538	314
Kirby Canyon	BAAQMD	07/18/2018	383	166	475	439
Guadalupe	BAAQMD	07/18/2018	187	63	255	468
Half Moon Bay (Ox Mountain)	ARB	10/06/2018	2939	574	686	533

328

329 **Table S5:** List of SFBA’s publicly owned treatment works (POTWs) with their annual
 330 throughput of waste effluent processed. Facilities sampled by the airplane for this study are
 331 highlighted in orange.

Facility	City	Effluent Throughput		
		2016	2017	2018
million liters of wastewater				
San Jose-Santa Clara Regional Wastewater Facility	San Jose	127777	141361	146827
San Francisco South East Treatment Plant	San Francisco	94673	94673	96649
East Bay Municipal Utility District	Oakland	82798	91505	91505
Central Contra Costa Sanitary District	Martinez	48885	48885	60790
Union Sanitary District	Union City	30866	32237	33679
City of Santa Rosa Wastewater Treatment	Santa Rosa	23996	23996	29189
San Francisco, City & County, PUC	San Francisco	20082	22818	24420
Palo Alto Regional Water Quality Control Plant	Palo Alto	25987	28440	23988
Silicon Valley Clean Water	Redwood City	20646	23106	19169
Fairfield-Suisun Sewer District	Fairfield	17863	22451	18272
City of Sunnyvale Water Pollution Control	Sunnyvale	16497	18060	18060
Delta Diablo Sanitation District	Antioch	17114	18321	17455
Hayward Waste Water Treatment Plant	Hayward	14497	14407	17099
Oro Loma Sanitary District	San Lorenzo	17231	20754	16913
Vallejo Sanitation & Flood Control District	Vallejo	13336	16736	16814
San Mateo Water Quality Control Plant	San Mateo	15348	18008	15307
Dublin San Ramon Services District - Wastewater TP	Pleasanton	14388	14388	14617
Central Marin Sanitation Agency	San Rafael	11430	19800	14126
Napa Sanitation District - Soscol	Napa	11534	13953	13953
South San Francisco-San Bruno Water Quality Plant	South San Francisco	11659	11848	11848
West County Wastewater District	Richmond	10573	13805	11318
City of Livermore Sewage Treatment Plant	Livermore	7640	8070	8070
City of Richmond Water Pollution Control District	Richmond	6905	10251	8014
North San Mateo County Sanitation Dist	Daly City	72453	6560	7858
Novato Sanitary District	Novato	5290	6534	7813
City of Petaluma, Dept of Water Resources & Convs	Petaluma	7283	8521	7037

San Leandro Water Pollution Control Plant	San Leandro	6449	7173	6727
Sonoma County Water Agency	Sonoma	3865	5194	5663
City of Brentwood	Brentwood	4690	4980	4820
Sewerage Agency of South Marin	Mill Valley	4141	4296	4296
City of Burlingame, Waste Water Treatment Plant	Burlingame	4153	4823	3734
City of Pacifica Calera Creek Water Recycling	Pacifica	3372	3676	3459
Pinole-Hercules Wastewater Treatment Plant	Pinole	3431	4079	3426
North Point Wet Weather Facility, SFPUC	San Francisco	4318	6592	3409
Las Gallinas Valley Sanitary District	San Rafael	3361	4517	3305
City of Benicia	Benicia	409	3355	2724
Town of Windsor	Windsor	2261	2562	2628
City of Millbrae Wastewater Treatment Plant	Millbrae	2227	2486	2486
	American			
City of American Canyon	Canyon	2230	1904	1904
Town of Discovery Bay	Discovery Bay	1031	1605	1817
Mt View Sanitary District	Martinez	1707	2041	1813
Sausalito-Marin City Sanitary District	Sausalito	1803	2246	1595
Marin County Sanitary Distr No 5	Tiburon	958	1039	1039
City of Calistoga	Calistoga	643	897	1034
San Francisco International Airport	San Francisco	852	852	943
Rodeo Sanitary District	Rodeo	741	999	818
Town of Yountville	Yountville	649	667	667
City of St Helena	Saint Helena	647	717	569
Treasure Island - US Navy BRAC PMO-W	San Francisco	382	428	496
Pacific Union College	Angwin	na	na	142
USCG Training Center	Petaluma	124	131	100
Adventist Health St Helena	Saint Helena	na	na	46
U S Veterans Administration Medical Center	Livermore	14324	9	9
Discovery Bay Community Services District	Discovery Bay	38	na	na
	Total	815555	816759	810461

332

333 **Table S6:** Summary of airplane-measured facility-scale CH₄ emissions rate over four SFBA
334 wastewater treatment plants (POTWs) from 2016-18. The “campaign” column indicates the
335 agency (ARB – California Air Resources Board, BAAQMD – Bay Area Air Quality
336 Management District) that funded the corresponding measurement flight.

Facility	Campaign	Date	Methane	Measurement
			Mass Rate	Uncertainty
			kg/h	
San Jose Santa Clara	BAAQMD	04/19/2018	204	54
	BAAQMD	04/20/2018	290	69
	ARB	10/05/2018	427	80
EBMUD Oakland	BAAQMD	11/11/2016	82	314
	BAAQMD	12/19/2016	91	26
	BAAQMD	04/19/2018	130	24
	BAAQMD	05/10/2018	83	21
San Francisco Southeast	BAAQMD	12/20/2016	229	56
	BAAQMD	04/19/2018	62	10
	BAAQMD	05/10/2018	80	16
Central Contra Costa	BAAQMD	04/20/2018	120	22

337

338 **Table S7:** List of SFBA’s composting operations with their annual throughput of green and food
339 waste accepted (or maximum permitted). Facilities sampled by the airplane for this study are
340 highlighted in orange.

Facility	City	2018 throughput (thousand metric tons)
Z-Best Composting Facility	Gilroy	533
Newby Island Compost Facility	San Jose	146
Composting Facility (Altamont Landfill)	Livermore	140
Redwood Landfill	Novato	128
WM Earthcare of Marin	Novato	121
Zanker Road Class III Landfill	San Jose	87
WCCSLF Organic Materials Processing	Richmond	80
South Valley Organic Composting Facility (Recology Pacheco Pass)	Gilroy	37
City of Napa Material Diversion Facility	Napa	35
East Bay Municipal Utility District	Oakland	33
Monterey Mushrooms - Morgan Hill	Morgan Hill	30
Potrero Hills Compost Facility	Suisun City	18
West Marin Compost	Nicasio	18

Grab N` Grow (Soiland Co.)	Santa Rosa	15
Upper Valley Disposal Service (Napa Recycling and Waste Services)	Saint Helena	14
Vision Recycling Green Waste Composting	Livermore	13
Dolcini Brothers Composting Operation Ag	Petaluma	13
Goodyear Road Compost Facility	Benicia	10
Laguna Subregional Compost Facility	Santa Rosa	10
Carneros River Ranch	Petaluma	8
West Marin Compost Project- Drop Off	Nicasio	7
Blue Line Transfer	South SF	6
Oliveira Enterprises, Inc.	Byron	5
PSSI Ag. Material Storage / Handling Op.	Stanford	4
Poncia Fertilizer	Santa Rosa	3
Altamont Resource + Recovery Facility	Livermore	3
Countryside Mushrooms, Inc.	Gilroy	3
Upper Valley Research Composting Op. #2	Saint Helena	3
B and D Mushrooms, Inc.	San Martin	3
	Point Reyes	
Point Reyes Compost Co. LLC	Station	2
Reichert Duck Farm	Petaluma	2
Royal Oaks Mushrooms	Morgan Hill	2
Bolinas-Stinson Resource Rcvry. Project	Bolinas	2
South Valley Organic Composting Facility	Gilroy	2
Global Mushrooms Farm	Gilroy	2
South Valley Mushroom Farm	Morgan Hill	2
Buchli Station	Napa	2
Oso Vineyard	Pope Valley	1
Clover Flat Resource Recovery Park	Calistoga	1
Joseph Phelps Vineyards	Saint Helena	1
Yount Mill Composting	Oakville	0
Mont Emei Vineyards, LLC	Napa	0
Opus One	Oakville	0
Tierra Vegetables	Santa Rosa	0
Graton Waste Water Treatment Plant	Graton	0
Thermopile Research Composting Operation	Nicasio	0
Central Compost Site2	Petaluma	0
Zero Waste to Energy Development Co. AD	San Jose	0

	Total	1546
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341

342 **Table S8:** Summary of airplane-measured facility-scale CH₄ emissions rate over two large SFBA
 343 composting operations.

Facility	Date	Methane Mass Rate	Measurement Uncertainty
		kg/h	
ZBEST Composting	05/10/2018	374	75
	07/18/2018	251	46
	08/25/2018	360	31
West Contra Costa Composting	05/11/2018	175	37

344

345 **Table S9:** Summary of airplane-measured facility-scale CH₄ emissions rate over two SFBA
 346 dairy facilities.

Facility	Date	Methane Mass Rate	Measurement Uncertainty
		kg/h	
Tresch dairy farm	10/12/2016	10	4
McClelland dairy	10/12/2016	38	7

347

348