

## The TESS-Keck Survey III: A Stellar Obliquity Measurement of TOI-1726 c

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### ABSTRACT

We report the measurement of a spectroscopic transit of TOI-1726 c, one of two planets transiting a G-type star with  $V = 6.9$  in the Ursa Major Moving Group ( $\sim 400$  Myr). With a precise age constraint

from cluster membership, TOI-1726 provides a great opportunity to test various obliquity excitation scenarios that operate on different timescales. By modeling the Rossiter-McLaughlin (RM) effect, we derived a sky-projected obliquity of  $-1_{-32}^{+35}$  °. This result rules out a polar/retrograde orbit; and is consistent with an aligned orbit for planet c. Considering the previously reported, similarly prograde RM measurement of planet b and the transiting nature of both planets, TOI-1726 tentatively conforms to the overall picture that compact multi-transiting planetary systems tend to have coplanar, likely aligned orbits. TOI-1726 is also a great atmospheric target for understanding differential atmospheric loss of sub-Neptune planets (planet b  $2.2 R_{\oplus}$  and c  $2.7 R_{\oplus}$  both likely underwent photoevaporation). The coplanar geometry points to a dynamically cold history of the system that simplifies any future modeling of atmospheric escape.

*Keywords:* planets and satellites: formation;

## 1. INTRODUCTION

The stellar obliquity is the angle between the rotation axis of the host star and the normal of the orbital plane of its planet. While the planets in the Solar System are well-aligned with the Sun (obliquity  $\lesssim 7^\circ$ ), many of the known exoplanets have polar or even retrograde orbits (e.g. Sanchis-Ojeda et al. 2013; Dalal et al. 2019). These spin-orbit misalignments are often interpreted as signposts of a dynamically hot formation or evolution history. Various mechanisms have been proposed to be responsible for tilting the orbits of planets. Many of these mechanisms operate on different timescales: primordial disk misalignment during the disk-hosting stage ( $\lesssim 3$  Myr, e.g. Lai et al. 2011; Batygin 2012); nodal precession induced by an inclined companion ( $\sim 3.5$  Myr for HAT-P-11b, Yee et al. 2018); the Kozai-Lidov mechanism operates on a wide range of timescales  $10^4$  to  $10^8$  yr depending on the system configuration (e.g. Fabrycky & Tremaine 2007); and secular chaos between longer-period giant planets can happen in  $10^7$  to  $10^8$  yr (e.g. Wu & Lithwick 2011). A sample of obliquity measurements spanning a range of precise host star ages will help us distinguish these orbit-tilting mechanisms.

Precise stellar ages for main sequence stars are hard to come by, particularly for later-type stars which barely evolve over a Hubble time. Our best age constraints come from establishing cluster membership of a planet host so that the ensemble study of kinematics, stellar activity, Li abundance, gyrochronology and isochronal fitting of other stars in the same cluster can firmly pin down the stellar age. So far, there are about a dozen planet hosts found in young clusters (e.g. David et al. 2016; Mann et al. 2016). They are crucial for our understanding of various aspects of planet formation and evolution. TOI-1726 is a G-type star in the Ursa Ma-

jor Moving Group ( $414 \pm 23$  Myr, Jones et al. 2015) that hosts two transiting sub-Neptune planets with 2.2 and  $2.7 R_{\oplus}$  on 7 and 20-day orbits (Mann et al. 2020). With a V-band magnitude of 6.9 and a projected rotational velocity  $v \sin i$  of  $\sim 7$  km/s, TOI-1726 provides a rare opportunity to measure the stellar obliquity of a young sub-Neptune planet. In this work, we discuss a new measurement of the stellar obliquity of planet c.

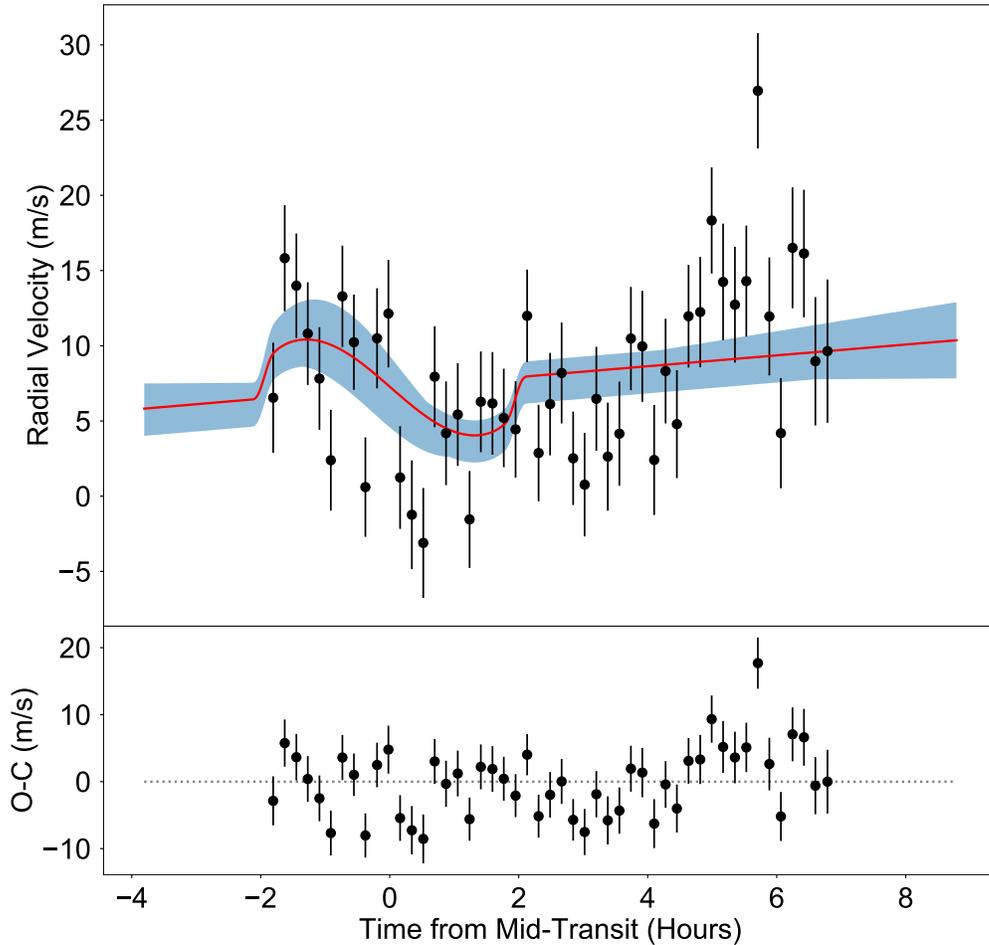
This letter is structured as follows. In Section 2 we present the spectroscopic measurements of the TOI-1726. Section 3 describes the constraints on the stellar parameters using both spectroscopy and Gaia information. In Section 4, we present a joint analysis of the *TESS* light curve and the Rossiter-McLaughlin (RM) effect to measure the stellar obliquity of TOI-1726 c. Section 5 discusses the implication of our finding.

## 2. SPECTROSCOPIC MEASUREMENT

We obtained 49 spectra of TOI-1726 on the night of UTC 2020 Feb 26, spanning a transit of TOI-1726 c. We used the Automated Planet Finder (APF, Vogt et al. 2014a) at the Lick Observatory. The spectra were obtained with an iodine cell whose dense forest of molecular lines provide both the wavelength solution and a means of determining the line spread function. The spectral resolution was  $\sim 100,000$ . We obtained consecutive 10-min exposures that enabled a median SNR of 145 per reduced pixel near  $5500 \text{ \AA}$ . The iodine method for determining precise radial velocities requires a template spectrum of the star with a high signal-noise-ratio. A template spectrum should have been obtained with APF. However, due to weather conditions and scheduling constraints, we had to secure a high SNR template of TOI-1726 on the High Resolution Echelle Spectrometer on the 10m Keck I telescope on the night of UT 2020 Mar 10. APF and HIRES have similar instrumental designs (Vogt et al. 1994, 2014b). Moreover, we explicitly deconvolved the different instrumental profiles from the template spectra in our Doppler pipeline (Howard

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**Figure 1.** The measured radial velocities during the transit of TOI-1726 c. The red line is the best-fit model; the blue shaded region represent the 68% confidence region from the posterior distribution. The data suggest a stellar obliquity of  $-1_{-32}^{+35}$  ° that favors a prograde, and likely aligned orbit for TOI-1726 c . Visually, there are also hints of a red noise component towards the end of observation. We investigated the source of this red noise component with line profile analysis and its effect on obliquity measurement with a Prayer’s Beads analysis in Section 4.

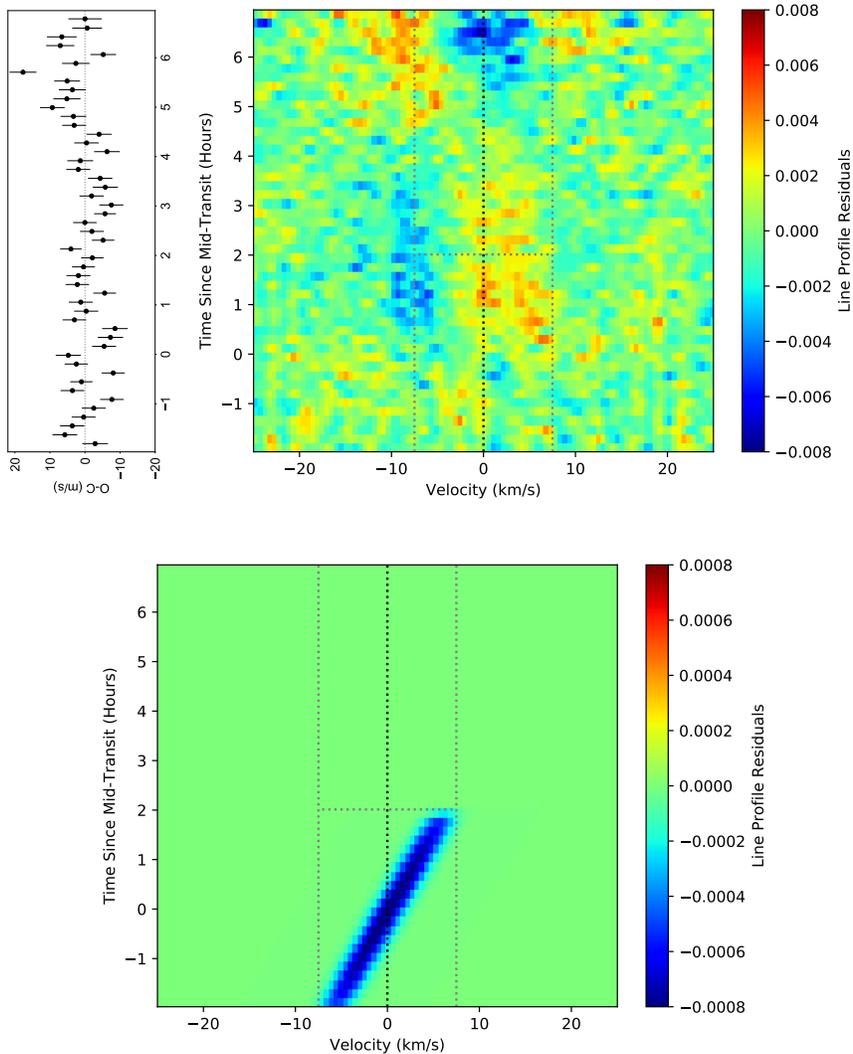
et al. 2010), therefore the high SNR, iodine-free HIRES spectrum should serve adequately as the template spectrum for reducing the APF dataset. More details of our forward-modeling Doppler pipeline are described in Howard et al. (2010). The radial velocities and uncertainties are plotted in Fig. 1 and reported in Table 1.

### 3. STELLAR PARAMETERS

We constrained the spectroscopic parameters ( $T_{\text{eff}}$ ,  $\log g$  and  $[\text{Fe}/\text{H}]$ ) of TOI-1726 using the iodine-free spectra

from Keck/HIRES and the SpecMatch pipeline<sup>1</sup> (Petigura et al. 2017). In short, SpecMatch models observed optical spectra with interpolated model spectra from the precomputed grid (Coelho et al. 2005) of discrete  $T_{\text{eff}}$ ,  $[\text{Fe}/\text{H}]$ ,  $\log g$  and  $v \sin i$  values. Line broadening effects from both rotation and macroturbulence are included by convolving the model spectra with the kernel described by Hirano et al. (2011). Instrumen-

<sup>1</sup> <https://github.com/petigura/specmatch-syn>

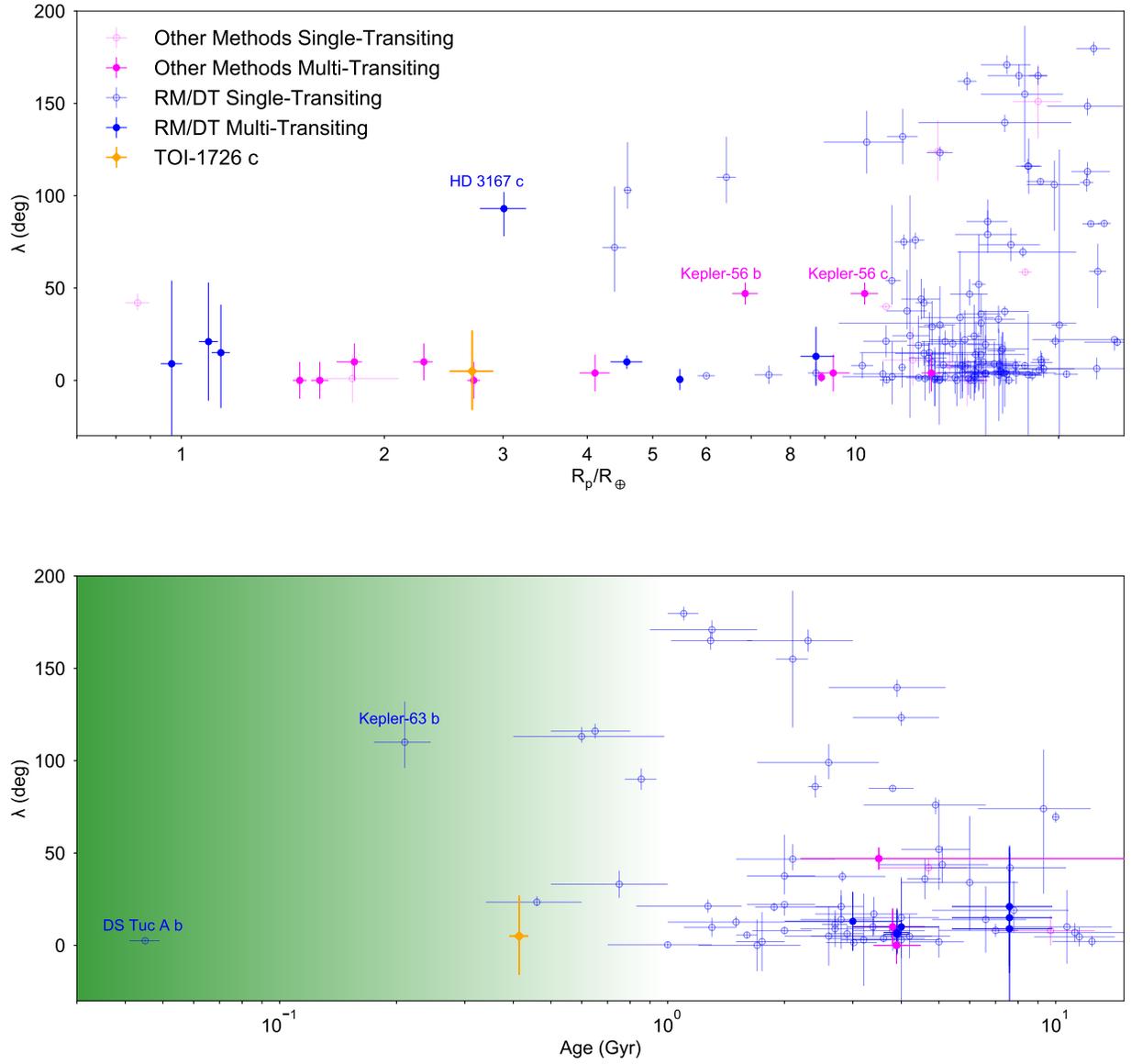


**Figure 2.** **Top Left:** The residuals of the RM time series same as Figure 1. **Top Right:** The measured line profile residuals as a function of time and velocity. The vertical gray lines indicate the  $v \sin i$  of the host star. The horizontal gray line indicate the end of the transit  $t_{IV}$ . Some localized patterns can be seen which are likely due to a combination of stellar activity and instrumental drifts. **Bottom:** The simulated planetary shadow of TOI-1726c on a well-aligned orbit. The signal is about one order of magnitude lower than the uncertainties seen in the measurements (note the different color coding in these two panels); and remains undetected with the current measurement.

tal broadening is modeled as a Gaussian function with a FWHM of 3.8 pixels, a value that provides a good match to the widths of telluric lines. We calculate the weighted average of spectroscopic parameters of five  $\sim 400 \text{ \AA}$  spectral segments. The final output spectroscopic parameters are corrected for known systematic effects from previous comparison with standard stars. Particularly, SpecMatch systematically yields higher ( $\sim 0.1$  dex) surface gravity  $\log g$  for earlier-type stars when compared with asteroseismic results of standard stars (Huber et al. 2013a). This effect is empirically corrected for with a

scaling relation  $\log g(T_{\text{eff}}, [\text{Fe}/\text{H}])$ . See Petigura (2015a) for detail.

To derive the stellar parameters, we further make use of Gaia parallax information (Gaia Collaboration et al. 2018). We followed the procedure described in detail by Fulton & Petigura (2018). To summarize, we link the stellar effective temperature, the parallax measurement from Gaia and the  $K$ -band magnitude (which is less affected by extinction) together with Stefan-Boltzmann Law for an independent constraint on the radius of the star. In practice, we put in the priors on spectroscopic parameters and the parallaxes into the *Isoclas-*



**Figure 3.** The projected stellar obliquity  $\lambda$  plotted against the planetary radius (Upper) and stellar age (Lower). The majority of stellar obliquity measurements are performed for single-transiting planets which are believed to have a dynamically hot history. We highlighted measurements of relatively unexplored multi-transiting systems with filled symbols. TOI-1726 is a unique opportunity for obliquity measurement for multi-transiting sub-Neptune planetary systems with a well-determined young age. The green shading in the lower panel qualitatively captures the magnitude of the high-energy radiation from the host star that is responsible for driving photoevaporation. These high-energy radiation dwindles with the first few hundred Myr: a timescale future observations of TOI-1726 are poised to probe.

*sify* package of Huber et al. (2017) which then compares these parameters with the MESA Isochrones & Stellar Tracks (MIST, Choi et al. 2016) to determine the posterior distribution of various stellar parameters. The results are summarized in Table 2.

#### 4. JOINT LIGHT CURVE AND RM ANALYSIS

TOI-1726 was observed by *TESS* (Ricker et al. 2014) in Sector 20 from UT 2019 Dec 24 to 2020 Jan 20. We downloaded the reduced light curve from the Mikulski Archive for Space Telescopes website<sup>2</sup>. We only kept data points with a Quality Flag of 0, i.e., those with no known problems.

We started from the transit ephemerides reported by the *TESS* team. We first removed the data spanning the transits of both planet b and c from the light curve. This enabled us to measure the stellar rotation period of TOI-1726 by applying the Lomb-Scargle periodogram. We detected a strong rotational modulation at a period of  $6.36^{+0.75}_{-0.25}$  days where the uncertainties are derived from the full width half maximum of the peak. As a consistency check, we calculated  $v = 2\pi R_{\star}/P_{\text{rot}}$ , the rotation period of  $6.36^{+0.75}_{-0.25}$  days and the stellar radius of  $0.92 \pm -0.10 R_{\odot}$  together give a rotational velocity  $v$  of  $7.3^{+0.7}_{-1.0}$  km/s which is consistent with the  $v \sin i$  of  $6.56 \pm 1.0$  km/s determined from the spectroscopic analysis alone. Using the procedure described in Masuda & Winn (2020), the orbital inclination of the host star is  $>45^{\circ}$  at 95% confidence level. This agreement of  $v \sin i$  and  $v$  is supporting evidence for a prograde and perhaps well-aligned orbit of TOI-1726 c, in addition to the analysis of the RM effect described later in the paper.

We then analyzed the in-transit light curve simultaneously with the Rossiter-McLaughlin effect. We isolated data taken within one transit duration of the transit midpoint. We used the *Batman* package (Kreidberg 2015) to model the transit light curves. We adopted a quadratic limb-darkening law, imposing Gaussian priors on the coefficients with medians taken from pre-computed limb darkening coefficients from EXOFAST<sup>3</sup> (Eastman et al. 2013) and with widths of 0.3. We put a prior on the mean stellar density based on the analysis in Section 3. We sampled  $P_{\text{orb}}$ ,  $R_p/R_{\star}$  and  $a/R_{\star}$  uniformly in logarithmic space. We put a uniform prior on the impact parameter  $b$  [-1,1] and on the midtransit time ( $T_c$ ). We assumed that both planets are on circular orbits. The current RV dataset (Hirsch et al. in prep) only provide weak constraints on the orbital eccentricities and are consistent with being circular for both planets.

To model the RM effect, we followed the prescription of Hirano et al. (2011). The additional parameters are the sky-projected obliquity  $\lambda$ , the projected rotational velocity  $v \sin i$  the radial velocity offset  $\gamma$  and the local gradient of the offset  $\dot{\gamma}$ . We also included a jitter parameter to account for any additional astrophysical or instrumental noise. The likelihood function of the RM model was combined with the likelihood function of the transit model.

We sampled the posterior distribution using the Markov Chain Monte Carlo technique implemented in the *emcee* code (Foreman-Mackey et al. 2013). We used 128 walkers and ran until the Gelman-Rubin convergence statistics dropped below 1.03. We first included a prior on the rotational modulation  $v \sin i$  of  $6.56 \pm 1.0$  km/s from spectroscopic analysis in Section 3. The sky-projected obliquity has a posterior distribution of  $-6^{+28}_{-25}$  ° i.e. favor a prograde and possibly aligned orbit for planet c. The posterior distribution also favors a slightly higher  $v \sin i$  of  $7.0 \pm 1.0$  km/s. When we removed the prior on  $v \sin i$  altogether, the data are consistent with a broader range of  $v \sin i$  of  $9.9^{+4.3}_{-3.4}$  km/s; while the posterior distribution of stellar obliquity also widened  $\lambda$   $-5^{+33}_{-26}$  °. Table 2 reports the summary of the posterior distribution for the key parameters.

#### 5. DOPPLER TOMOGRAPHY AND RED NOISE MITIGATION

We tried to look for the Doppler shadow of planet c in the subtle variation of the line profiles using the non-Iodine part of the spectra (4000–5000 Å). Our analysis is similar to that of Albrecht et al. (2013). In short, we cleaned the spectrum from outliers with 5-sigma clipping. We removed the continuum and blaze function with a polynomial fit to the 95% percentile flux level in each Echelle order. We cross-correlated the individual spectrum with the bestfit SpecMatch spectrum before rotational/instrumental broadening is applied. We then subtracted the globally averaged line profile from the individual line profiles to extract the subtle variations that may be caused by the shadow of the transiting planet (Figure 2). However, given the small transit depth of the planet ( $\sim 0.08\%$ ), we could not convincingly detect the shadow of the planet in the line profile residuals. Instead, the line profile residuals are dominated by patterns that are almost one order of magnitude larger in amplitude; roughly constant in velocity and extend well beyond the transit duration. We suspect that these pattern most likely produced by the change of the point spread function due to instrumental effects or the emergence of stellar activity on TOI-1726. How-

<sup>2</sup> <https://archive.stsci.edu>

<sup>3</sup> [astroutils.astronomy.ohio-state.edu/exofast/limbdark.shtml](http://astroutils.astronomy.ohio-state.edu/exofast/limbdark.shtml).

ever, we do not have a physically-motivated model to eliminate these effects.

Visual inspection of the residuals of the RM time series hint at the presence of a correlated noise component more noticeably starting at 4 hours after the mid-transit of planet c (Figure 1). This coincided the onset of correlated noises in the radial velocity residuals (Figure 2) as well as an increase of the S index (Table 1). To assess how the presence of a correlated noise component might have affected the constraint on stellar obliquity, we performed a Prayer’s Beads analysis. This is perhaps more worrisome as some of the line profile residual patterns happened during the transit of planet c (Figure 2). Our analysis is as follows. We first found the maximum likelihood model with the Levenberg-Marquardt method as implemented in PYTHON package LMFIT. We recorded the corresponding residuals and cyclically permuted the residuals before adding them back to the best-fit model. This generated a series of mock datasets that contains the same correlated noise component as the original dataset. We found the maximum likelihood model for each mock dataset. Focusing on the stellar obliquity, the resultant distribution of obliquity is  $\lambda = -1_{-32}^{+35}$  °. This is a broader distribution compared to that from the white-noise-only model in Section 4; but qualitatively these two models both favor a prograde, possibly aligned orbit for TOI-1726c.

## 6. DISCUSSION

### 6.1. Obliquity of Multi-Transiting Systems

It has been noted in several previous works that the underlying orbital architectures of *Kepler* single-transiting (here we refer to the observed multiplicity, to be distinguished from planets that only transited host stars once during the time span of observation) and multi-transiting systems may be different. Specifically, single-transiting systems seem to have a broader distribution of orbital eccentricities whereas multi-transiting systems mostly favor circular orbits (Van Eylen & Albrecht 2015; Xie et al. 2016; Mills et al. 2019). In addition, Fang & Margot (2012) and Zhu et al. (2018) suggested that the mutual inclination dispersion is larger when the observed multiplicity of a planetary system is smaller. A plausible explanation of this architectural difference is the dynamical interaction between the sub-Neptune planets or that with a more distant giant planets. Zhu & Wu (2018) and Bryan et al. (2019) independently arrived at the conclusion that *Kepler*-like sub-Neptune planets are much more likely to have a cold Jupiter companion ( $>1\text{AU}$ ) than randomly chosen stars (Cumming et al. 2008; Clanton & Gaudi 2014). Masuda et al. (2020) further showed that when the inner

planetary system only has one transiting planet, its cold Jupiter is likely inclined by tens of degrees relative to the inner planetary system. The interpretation is that the dynamical interaction of an inclined cold Jupiter can stir up the initially co-planar planetary systems while exciting larger mutual inclinations and eccentricities. The single-transiting systems represent the dynamically hot sub-sample while the multi-transiting systems are dynamically colder.

It will be interesting to see if the same architectural difference carries over to the stellar obliquity distribution. So far, there are about 150 obliquity measurements in the literature. Traditional RM effect is more easily detected for planets with larger radii and more frequent transits. As a result, the vast majority of existing measurements were performed for hot Jupiters or hot Neptunes. Intriguingly, it is often the case that these hot Jupiters and hot Neptunes are single-transiting planets with spin-orbit misalignments both of which hint at a dynamically hot past (Dong et al. 2018). On the other hand, multi transiting systems tend to display low obliquities (Albrecht et al. 2013). Unfortunately there are only  $\sim 11$  obliquity measurements obtained for multi-transiting systems to date (see Fig. 3). We note the most complete census of spin-orbit angle of multi-transiting systems was done by Winn et al. (2017). They compared the projected rotational velocity  $v \sin i$  and the rotational velocity  $v = 2\pi R_{\star}/P_{\text{rot}}$ . If a system is grossly misaligned,  $v \sin i$  would be much smaller than  $v$ . Winn et al. (2017) found that the majority of *Kepler*-like systems (systems with several sub-Neptune planets within 1AU) are well-aligned with their host star. The six high-obliquity suspects Winn et al. (2017) identified were dominated by hot Jupiters. This result revealed a picture that planets in multi-planet systems are generally well-aligned as one would expect from a cold dynamical history. Coming back to the multi-transiting systems that have their stellar obliquities explicitly measured, most of these measurements were often obtained with alternative methods, rather than the RM effect, such as asteroseismology (e.g. Huber et al. 2013b) or spot-crossing anomalies (e.g. Sanchis-Ojeda et al. 2012). The results mostly yield well-aligned orbits. We note that the only exceptions are the polar orbit of HD 3167 c (Dalal et al. 2019) and  $50^{\circ}$  inclined orbit of Kepler-56 b and c (Huber et al. 2013b). What kind of formation channel gave rise to misaligned multi-planet systems have been a topic of interests for the theorists (e.g. Li et al. 2014; Spalding & Batygin 2015). It will be interesting to see if these two systems are indeed rare occurrences. Our result on TOI-1726 c is one crucial step towards enlarging that sample of multi-transiting

planetary system. Although the obliquity constraints on planet b and planet c individually are weak:  $1_{-43}^{+41}$  ° (Mann et al. 2020) versus  $-1_{-32}^{+35}$  °, the fact that both planets transit and posterior distribution of obliquity both center at 0 seems to favor a coplanar, likely aligned, dynamically quiet architecture for TOI-1726.

### 6.2. *Obliquity in Time*

As we mentioned briefly in the introduction, many different theories have been offered to explain the observed diversity of stellar obliquities (e.g. Fabrycky & Tremaine 2007; Wu & Lithwick 2011; Lai et al. 2011; Batygin 2012; Yee et al. 2018). Since these theories operate on very different timescales, a potential way to test some of them is to obtain obliquity measurements for a sample of planets with well-determined ages. For example, if young planetary systems rarely display spin-orbit misalignment, it is reasonable to say that the orbit-tilting mechanisms that only operate during the disk-hosting stage (e.g. Lai et al. 2011; Batygin 2012) cannot be the dominant channel to generate spin-orbit misalignment. The cluster membership of TOI-1726 (Mann et al. 2020) provides a firm and precise age estimate for the host star. In Fig. 3, we plotted all obliquity measurements for systems with better than 20% age estimates. TOI-1726 c is the third youngest planet with obliquity measurement. Moreover TOI-1726 c is a sub-Neptune which is the predominant product of planet formation in the Galaxy (Petigura et al. 2013), whereas a group of planets for which obliquity measurements have been lacking (Fig. 3).

### 6.3. *A great system for studying atmospheric losses*

The bimodal radius distribution and the presence of the so-called "Hot Neptune Desert" both suggest that atmospheric loss from sub-Neptune planets is a common if not ubiquitous phenomena (Fulton et al. 2017). TOI-1726 is a great system for a study of atmospheric loss. The star is 400 Myr old which is comparable to the timescale where high-energy radiation from the host star begins to diminish (Ribas et al. 2005) and the photoevaporation starts to come to a conclusion (see Fig. 3). Moreover, the system contains two sub-Neptune planets whose low surface gravity make them the planets most amenable to photoevaporation (Wang & Dai 2018). The two planets are suited to comparative study since they orbit around the same host star. In other words, the planets are bathed in the same high-energy radiation environment except for a difference in orbital distance. Any difference in the outcome of atmospheric loss has to come from the different planetary parameters e.g. orbital period and planetary mass etc. The

prograde and coplanar orbits of both planet b (Mann et al. 2020) and planet c together disfavor a violent event such as high-eccentricity migration or giant impact collision that would have disrupted the planets' coplanarity and complicated the evolution of the atmospheres. We also note that there is no compelling evidence for a cold Jupiter that may generate dynamical instability of the inner planetary system ( $\sim 8000$ -day baseline, Hirsch et al. in prep).

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*Facilities:* Automated Planet Finder (Levy), *TESS*

*Software:* Batman (Kreidberg 2015), Emcee (Foreman-Mackey et al. 2013), EXOFAST (Eastman et al. 2013),

Isoclassify (Huber 2017), lmfit(Newville et al. 2014)  
SpecMatch (Petigura 2015b; Yee et al. 2017),

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**Table 1.** Lick/APF Radial Velocities

Time (BJD)	RV (m/s)	RV Unc. (m/s)	S index	S Unc.
2458905.618603	6.54	3.66	0.374	0.002
2458905.626056	15.82	3.52	0.381	0.002
2458905.633579	13.99	3.47	0.373	0.002
2458905.640951	10.81	3.41	0.372	0.002
2458905.648485	7.82	3.41	0.375	0.002
2458905.655846	2.39	3.35	0.377	0.002
2458905.663311	13.29	3.37	0.382	0.002
2458905.670752	10.23	3.17	0.385	0.002
2458905.678159	0.61	3.31	0.375	0.002
2458905.685705	10.49	3.33	0.384	0.002
2458905.693031	12.14	3.57	0.386	0.002
2458905.700588	1.24	3.41	0.389	0.002
2458905.708180	-1.23	3.61	0.381	0.002
2458905.715564	-3.11	3.65	0.382	0.002
2458905.722925	7.94	3.36	0.380	0.002
2458905.730262	4.18	3.45	0.383	0.002
2458905.737843	5.43	3.42	0.381	0.002
2458905.745470	-1.55	3.22	0.379	0.002
2458905.752749	6.28	3.35	0.385	0.002
2458905.760260	6.17	3.41	0.381	0.002
2458905.767575	5.20	3.28	0.381	0.002
2458905.775190	4.44	3.20	0.391	0.002
2458905.782655	11.99	3.08	0.380	0.002
2458905.790061	2.87	3.21	0.384	0.002
2458905.797492	6.12	3.40	0.384	0.002
2458905.804945	8.19	3.35	0.381	0.002
2458905.812386	2.52	3.11	0.379	0.002
2458905.819793	0.77	3.44	0.367	0.002
2458905.827362	6.47	3.46	0.391	0.002
2458905.834758	2.63	3.59	0.382	0.002
2458905.842257	4.15	3.46	0.378	0.002
2458905.849699	10.48	3.43	0.379	0.002
2458905.857059	9.96	3.69	0.381	0.002
2458905.864721	2.41	3.66	0.375	0.002
2458905.872093	8.32	3.48	0.380	0.002
2458905.879396	4.79	3.59	0.374	0.002
2458905.886930	11.96	3.41	0.380	0.002
2458905.894476	12.24	3.67	0.376	0.002
2458905.901883	18.33	3.53	0.384	0.002
2458905.909255	14.24	3.88	0.385	0.002
2458905.916893	12.73	3.85	0.382	0.002
2458905.924254	14.29	3.69	0.383	0.002
2458905.931707	26.95	3.83	0.387	0.002
2458905.939126	11.95	3.92	0.386	0.002
2458905.946590	4.19	3.66	0.394	0.002
2458905.954113	16.51	4.02	0.383	0.002
2458905.961497	16.13	4.24	0.388	0.002
2458905.968869	8.97	4.26	0.383	0.002
2458905.976681	9.64	4.76	0.391	0.002

**Table 2.** Stellar and Transit Parameters of planet c

Parameter	Symbol	Posterior Distribution
Sky-projected Obliquity (deg)	$\lambda$	$-1^{+35}_{-32}$
Projected Stellar Rotation (km/s)	$v \sin i$	$7.0 \pm 1.0$
Radial Velocity Offset (m/s)	$\gamma$	$4.69^{+1.95}_{-1.98}$
Radial Velocity Trend (m/s/day)	$\dot{\gamma}$	$19.4^{+8.5}_{-8.8}$
Planet/Star Radius Ratio	$R_p/R_*$	$0.02660^{+0.00082}_{-0.00074}$
Planetary Radius ( $R_\oplus$ )	$R_p$	$2.71 \pm 0.14$
Time of Conjunction (BJD-2457000)	$t_0$	$1844.0577 \pm 0.0011$
Impact Parameter	$b$	$0.50 \pm 0.07$
Scaled Semi-major Axis	$a/R_*$	$38.0^{+1.7}_{-4.6}$
Orbital Period (days)	$P_{\text{orb}}$	$20.5456^{+0.0016}_{-0.0019}$
Jitter (m/s)	$\sigma$	$3.66^{+0.80}_{-0.75}$
Effective Temperature ( $T_{\text{eff}}$ )	$K$	$5710 \pm 100$
Surface Gravity (dex)	$\log g$	$4.6 \pm 0.1$
Metallicity (dex)	[Fe/H]	$0.05 \pm 0.05$
Projected Stellar Rotation from Spectroscopy (km/s)	$v \sin i$	$6.56 \pm 1.0$
Stellar Mass ( $M_\odot$ )	$M_*$	$0.994 \pm 0.036$
Stellar Radius ( $R_\odot$ )	$R_*$	$0.934 \pm 0.019$
Stellar Density ( $\text{g/cm}^3$ )	$\rho_*$	$1.72 \pm 0.17$
Rotation Period (days)	$P_{\text{rot}}$	$6.36^{+0.75}_{-0.25}$