White Dwarf Subsystems in Core-Collapsed Globular Clusters

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Abstract

Numerical and observational evidence suggests that massive white dwarfs dominate the innermost regions of core-collapsed globular clusters by both number and total mass. Using NGC 6397 as a test case, we constrain the features of white dwarf populations in core-collapsed clusters, both at present day and throughout their lifetimes. The dynamics of these white dwarf subsystems have a number of astrophysical implications. We demonstrate that the collapse of globular cluster cores is ultimately halted by the dynamical burning of white dwarf binaries. We predict that core-collapsed clusters in the local universe yield a white dwarf merger rate of $\mathcal{O}(10) \text{ Gpc}^{-3} \text{ yr}^{-1}$, roughly 0.1%–1% of the observed Type Ia supernova rate. We show that prior to merger, inspiraling white dwarf binaries will be observable as gravitational-wave sources at millihertz and decihertz frequencies. Over 90% of these mergers have a total mass greater than the Chandrasekhar limit. We argue that the merger/collision remnants, if not destroyed completely in an explosive transient, may be observed in core-collapsed clusters either as young neutron stars/pulsars/magnetars (in the event of accretion-induced collapse) or as young massive white dwarfs offset from the standard white dwarf cooling sequence. Finally, we show that collisions between white dwarfs and main-sequence stars, which may be detectable as bright transients, occur at a rate of $\mathcal{O}(100) \text{ Gpc}^{-3} \text{ yr}^{-1}$ in the local universe. We find that these collisions lead to depletion of blue straggler stars and main-sequence star binaries in the centers of core-collapsed clusters.

Unified Astronomy Thesaurus concepts: White dwarf stars (1799); Globular star clusters (656); Type Ia supernovae (1728); Stellar dynamics (1596); Gravitational wave astronomy (675)

1. Introduction

For a standard initial mass function, present-day globular clusters are expected to harbour tens of thousands of white dwarfs (WDs) formed from the evolution of stars with initial masses in the range $\approx 1\text{--}8 M_{\odot}$ (e.g., Salpeter 1955; Kroupa 2001). Despite their high abundances, the observational study of WDs in globular clusters has progressed rather slowly, with a number of early searches impeded simply by the low luminosities of these objects (e.g., Richer 1978; Ortolani & Rosino 1987; Elson et al. 1995). In the mid-1990s, large populations of WDs and clear evidence of the WD cooling sequence were observed for the first time in several nearby globular clusters: M4 (Richer et al. 1995, 1997), NGC 6752 (Renzini et al. 1996), and NGC 6397 (Cool et al. 1996). More recently, several studies have taken further strides forward, using measurements of WD cooling sequences to constrain the ages of several Galactic globular clusters (e.g., Hansen et al. 2002, 2007, 2013).

The presence of WDs in globular clusters (GCs) has a number of implications across astronomy. If accreting material from a binary companion, WDs may be observed as cataclysmic variables (e.g., Grindlay et al. 1995; Ivanova et al. 2006; Belloni et al. 2016; Kremer et al. 2020b), which are well observed in GCs (e.g., Knigge 2012). WDs may be a critical ingredient in the formation of pulsars (also well observed in GCs; Ransom 2008) through accretion-induced

collapse (e.g., Bailyn & Grindlay 1990; Tauris et al. 2013; Ye et al. 2019). Additionally, WD mergers facilitated by dynamical interactions in the dense cores of GCs may provide an avenue for Type Ia supernovae (SNe) or other transients (e.g., Shara & Hurley 2002; Shen et al. 2019; Kremer et al. 2020b).

Recent studies have shown that in the central regions of core-collapsed GCs, massive WDs are likely the dominant stellar population (e.g., Kremer et al. 2020b; Rui et al. 2021b). The process of cluster core-collapse, in turn, is expected to be facilitated primarily by stellar-mass black holes (BHs; e.g., Kremer et al. 2020a). Thus, the dynamical evolution of massive WDs is intimately related to the dynamics governing stellar-mass BHs, and a discussion of WDs in GCs merits a discussion of their more massive remnant relatives.

The evidence for stellar-mass BHs in dense star systems like GCs is mounting. Over the past decade, eight stellar BH candidate binaries have been identified in Milky Way GCs through radio/X-ray observations (five candidates; Strader et al. 2012; Chomiuk et al. 2013; Miller-Jones et al. 2015; Shishkovsky et al. 2018) and radial-velocity measurements (three candidates; Giesers et al. 2018, 2019). On the computational side, a number of recent studies have shown that populations of BHs play an important role in the dynamical evolution of their host clusters. Once BHs mass-segregate to their host cluster’s core, energy generated through series of binary-mediated BH encounters effectively heats the core of the cluster, delaying the onset of cluster core collapse until the BH population is sufficiently depleted (e.g., Merritt et al. 2004;

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Mackey et al. 2007; Breen & Heggie 2013; Wang et al. 2016; Arca Sedda et al. 2018; Kremer et al. 2018b, 2019a; Antonini & Gieles 2020). In some scenarios, this “BH burning” may be prominent enough to accelerate the dissolution of a cluster through its tidal boundary (e.g., Chatterjee et al. 2017; Giersz et al. 2019; Gieles et al. 2021; Weatherford et al. 2021). Broadly speaking, by leveraging this understanding of the interplay of BHs with their host clusters’ structure, it is possible to constrain BH populations indirectly through analysis of observed cluster properties (e.g., Weatherford et al. 2018, 2020; Arca Sedda et al. 2018; Askar et al. 2018).

Recently, Vitral & Mamon (2021) demonstrated that the nearby core-collapsed NGC 6397 contains a diffuse dark inner subcluster of unresolved objects with a total mass of roughly $1000 M_{\odot}$ concentrated within the innermost $6''$. NGC 6397 has long been associated with similar claims; a number of analyses have argued that this cluster hosts an intermediate-mass BH (IMBH; e.g., Kamann et al. 2016). However, claims of IMBHs in core-collapsed clusters are controversial (e.g., Heggie et al. 2007; McNamara et al. 2003; Kirsten & Vlemmings 2012; Gieles et al. 2018; Tremou et al. 2018). While allowing for the possibility of WDs and neutron stars (NSs), Vitral & Mamon (2021) suggest that stellar-mass BHs likely dominate the mass of this central dark population. However, this is inconsistent with the current consensus understanding of BH dynamics in dense star clusters (Rui et al. 2021). To this point, several recent papers have shown specifically that, on the basis of observed features, NGC 6397 likely harbours at most a handful of stellar BHs at present day (Weatherford et al. 2020; Rui et al. 2021b).

In this paper, we follow up on the initial results presented in Rui et al. (2021b) and demonstrate that the observations presented in Vitral & Mamon (2021) can be explained by a diffuse subcluster of massive WDs. As the population of stellar BHs is slowly depleted over the lifetime of a cluster, massive WDs become the most massive population of stars.⁷ Once nearly all BHs have been ejected and the energy produced through BH dynamics is no longer able to delay collapse of the cluster core, these massive WDs are expected to dominate (by number and mass) the inner regions of their host cluster (e.g., Kremer et al. 2020b). To demonstrate these processes, we present a large set of N -body models representative of NGC 6397. These models build upon the analysis of Rui et al. (2021a), which presented best-fit models for NGC 6397 and other clusters (on the basis of matches to the observed surface brightness and velocity dispersion profiles) from an extensive suite of models covering the parameter space of Milky Way GCs (the CMC Cluster Catalog; Kremer et al. 2020b). We go on to examine broadly populations of WDs in clusters and discuss various physical processes made possible by the high WD densities expected in core-collapsed clusters like NGC 6397.

This paper is organized as follows. In Section 2, we describe the N -body models used in this study and discuss the specific application to observations of NGC 6397. In Section 3, we discuss the results from our models and argue that NGC 6397 hosts a dense population of WDs at present. If indeed dense

populations of WDs are common in core-collapsed clusters, this implies an amplified rate of WD mergers, which, in turn, has important implications for Type Ia supernovae and other possible transients and also the formation of millihertz and decahertz gravitational-wave (GW) sources. In Section 4, we discuss the dynamics of WD subsystems and estimate the rate of WD mergers and the detection prospects for GW detectors. In Section 5, we explore possible outcomes of WD mergers/collisions and discuss a few observational tests of these outcomes. In Section 6, we discuss interactions of WDs with main-sequence (MS) stars in core-collapsed clusters. Finally, in Section 7, we summarize our results and discuss several avenues for future study.

2. Computational Methods

2.1. Prescriptions for White Dwarf Physics

To create our N -body cluster models, we use our cluster dynamics code `Cluster Monte Carlo` (CMC). For a recent review of CMC, including a discussion of the most current prescriptions for compact object formation, see Kremer et al. (2020b). We summarize here the treatments for WD formation and evolution implemented in CMC. Unless otherwise noted, this treatment follows exactly that implemented in SSE (Hurley et al. 2000) and BSE (Hurley et al. 2002). We specify three distinct types of WDs.

1. He WDs: Helium (He) WDs (BSE type $k=10$) are formed following envelope loss of giant branch stars with zero-age main-sequence mass (M_{ZAMS}) less than the maximum initial stellar mass such that He ignites degenerately in a helium flash (see Equation (2) of Hurley et al. 2000). Note that the envelope stripping required to produce He WDs can only occur through binary evolution. We assume dynamical stellar collisions are all “sticky sphere,” meaning that giant envelopes are not ejected (for further detail, see Kremer et al. 2020c).
2. CO WDs: WDs composed primarily of carbon (C) and oxygen (O) (BSE type $k=11$) are formed by envelope loss of a thermally pulsing asymptotic giant branch (AGB) star with mass below the minimum mass required to undergo nondegenerate C ignition in the core (denoted as M_{up} in Pols et al. 1998; Hurley et al. 2000). Note that M_{up} depends on metallicity (see Table 2 of Pols et al. 1998). By default in CMC, we set $M_{\text{up}} = 1.4 M_{\odot}$ (see Breivik et al. 2020). At the metallicity of NGC 6397 ($Z \approx 0.0002$), the most massive CO WD that will form through the evolution of a single star is roughly $1.1 M_{\odot}$.
3. ONe WDs: WDs composed primarily of O and neon (Ne) (BSE type $k=12$) form by envelope loss of a thermally pulsing AGB star with mass in the range M_{up} to M_{ec} , where M_{ec} (by default, $M_{\text{ec}} = 2.5 M_{\odot}$ in our models; see Breivik et al. 2020) is the minimum mass of a star that avoids electron capture onto Ne and Mg in the core (also metallicity-dependent; see Pols et al. 1998). For NGC 6397-like metallicity, ONe WDs formed through stellar evolution will have masses $>1.1 M_{\odot}$.

In Figure 1 we show the relation between WD mass and zero-age main sequence (ZAMS) mass for three different metallicities. The vertical dashed lines indicate the ZAMS mass corresponding to the transition from CO to ONe WD formation

⁷ Of course, neutron stars are of comparable mass to the most massive WDs. However, the majority of neutron stars are expected to be ejected at early times from clusters due to natal kicks (in a typical cluster, only 1000 NSs are retained at late times compared to roughly 10^4 WDs; e.g., Ye et al. 2019). Thus, WDs are the dominant population for the purposes of this study.

Figure 1. WD–ZAMS mass relation for three different metallicities: $Z = 0.0002$ (corresponding to NGC 6397) in black, 0.002 in blue, and 0.02 in green. We show as vertical dashed lines the ZAMS mass corresponding to the transition from CO to ONe WD formation (with colors corresponding to the given metallicity).

as described above (with colors corresponding to the given metallicity).

We compute white dwarf radii as in Tout et al. (1997) and Hurley et al. (2000):

$$R_{\text{WD}} = \max \left[R_{\text{NS}}, 0.0115 \sqrt{\left(\frac{M_{\text{Ch}}}{M_{\text{WD}}} \right)^{2/3} - \left(\frac{M_{\text{WD}}}{M_{\text{Ch}}} \right)^{2/3}} \right] \quad (1)$$

(in units of $R_{\odot}$), where $R_{\text{NS}} = 10$ km is the assumed neutron star radius and $M_{\text{Ch}} = 1.44 M_{\odot}$ is the Chandrasekhar mass.

We model WD luminosity evolution using standard cooling theory (Mestel 1952; Hurley et al. 2000):

$$L_{\text{WD}} = 133 \left(\frac{M_{\text{WD}}}{M_{\odot}} \right) \left(\frac{Z}{Z_{\odot}} \right)^{0.4} \left(A \left[\frac{t}{\text{Myr}} + 0.1 \right] \right)^{-1.4} L_{\odot}, \quad (2)$$

where Z is the metallicity, t is the age of the WD since formation, and A is the effective baryon number, which is dependent on WD composition. We use $A = 4$ for He WDs, $A = 15$ for CO WDs, and $A = 17$ for ONe WDs. If a new WD is formed through a WD–WD merger, we assume the age is reset to zero (see Section 5).

Of particular relevance to this study are the outcomes of dynamically mediated collisions between WDs and dynamical mass transfer onto WDs (i.e., when a WD binary is driven to Roche lobe overflow, and ultimately merger, through GW-driven inspiral). We describe below our methods to compute the masses and types of remnants resulting from these interactions.

Mass transfer occurs in a double WD binary when it has inspiralled sufficiently through GW emission that one of the WDs fills its Roche lobe. Upon Roche lobe overflow, we assume dynamically unstable mass transfer occurs (leading to a merger) when the mass ratio of the system $q > 0.628$ (Tout et al. 1997). Stable mass transfer ensues for $q < 0.628$, possibly leading to a long-lived accreting binary (for a description of the treatments implemented in BSE for stable mass transfer from one WD onto another, see Section 2.6.6 of Hurley et al. 2002).

The outcome of dynamically unstable mass transfer depends on the types of WDs involved. We assume that when two He WDs merge, the triple- α reaction ignites and releases sufficient energy to completely unbind the merger product, leaving behind no remnant (Hurley et al. 2002). When a He WD accretes dynamically onto a CO/ONe WD, we assume the accreted material swells to form an envelope around the CO/ONe core and forms an He giant branch star (following Iben et al. 1996). The most relevant case for the purposes of this study is dynamical accretion of material from one CO/ONe WD onto another. In this case, the more massive WD is assumed to accrete total mass $\Delta M = \dot{M}_{\text{Edd}} \tau_{\text{M}}$ from the donor star, where $\dot{M}_{\text{Edd}}$ is the Eddington limit and $\tau_{\text{M}} = \sqrt{\tau_{\text{KH}} \tau_{\text{dyn}}}$ is the characteristic mass-transfer timescale (here, τ_{KH} and τ_{dyn} are the Kelvin–Helmholtz and dynamical timescales of the donor, respectively). For typical WDs of mass roughly $1 M_{\odot}$, $\dot{M}_{\text{Edd}} \approx 10^{-5} M_{\odot} \text{ yr}^{-1}$ and $\tau_{\text{M}} \approx 2000$ yr, giving a typical $\Delta M \approx 10^{-3} M_{\odot}$. Following Saio & Nomoto (1998) and Belczynski et al. (2002), if $M_1 + \Delta M > M_{\text{Ch}}$, we assume that electron capture leads to an accretion-induced collapse of the primary, leaving behind a neutron star of mass $M = 1.24 M_{\odot}$. If $M_1 + \Delta M < M_{\text{Ch}}$ (the more common case), we assume an ONe/CO WD primary remains (depending on the accretor’s composition). In both cases, the secondary (donor) is destroyed.

A dynamically mediated collision occurs when two WDs pass one another such that the pericenter distance $r_p < R_1 + R_2$, the summed radii of the two components. When this occurs, we adopt the “sticky sphere” approximation that the mass of the collision product $M_3 = M_1 + M_2$, the summed component masses. The stellar type of the collision product depends on the types of the two colliding objects (for further detail, see Section 2.7 of Hurley et al. 2002). For collisions between two He WDs, we assume the triple- α reaction is ignited so that the collision remnant is destroyed completely. For collisions between an He WD and a CO/ONe WD, we assume the He material forms an envelope around the CO/ONe core such that a giant branch He star forms (BSE stellar type $k = 8$ or 9) with core mass equal to the original CO/ONe WD mass. For collisions between two CO and/or ONe WDs, we assume a new CO/ONe WD is formed unless $M_3 > M_{\text{Ch}}$, in which case we assume an NS forms through accretion-induced collapse.

Of course, these treatments of merger/collision products are highly simplified, and general outcomes of WD mergers are likely more complex and diverse than considered here (e.g., Iben & Tutukov 1984; Webbink 1984; Nomoto & Kondo 1991; Hillebrandt & Niemeyer 2000; Woosley & Kasen 2011; Shen et al. 2012; Schwab et al. 2016; Schwab 2021). However, we stress that from the perspective of cluster dynamics, the specific outcome is largely irrelevant. Only a few dozen WD mergers/collisions are expected to occur in a typical core-collapsed cluster (see Table 1), so merger/collision products (or lack thereof for an explosive transient outcome) will constitute at most a few percent of the total population of $\sim 10^3$ WDs in the innermost region and $\sim 0.1\%$ of the total population of $\gtrsim 10^4$ WDs in the entire cluster. However, if detectable, the outcomes of these few dozen WD mergers may potentially provide powerful observational tests of the WD dynamics described in this paper. We return to this topic in more detail in Section 5.

Finally, when an MS star of mass M_1 merges with a WD of mass M_2 , we assume the MS star is accreted dynamically and swells up to form an envelope around the WD, which becomes

Table 1
List of N -body Models

(1)	$N (\times 10^5)$ (2)	r_v (pc) (3)	R_{gc} (kpc) (4)	N_{BH} (5)	Number of White Dwarfs				Number of WD + WD mergers		
					N_{tot} (6)	N_{He} (7)	N_{CO} (7)	N_{ONe} (8)	N_{ej} (10)	$N_{in-cluster}$ (11)	N_{coll} (12)
1	3.9	0.95	6	0	36,243	293	34,690	1260	10	26	31
2	3.9	0.95	8	0	38,297	355	36,586	1356	9	18	22
3	3.9	1.0	6	0	37,364	297	35,828	1239	11	17	35
4	3.9	1.0	8	1	37,325	306	35,738	1281	13	20	21
5	3.9	1.05	6	1	33,984	313	32,313	1358	7	8	14
6	3.9	1.05	8	0	39,302	412	37,471	1419	3	11	26
7	4.0	0.95	6	1	37,148	306	35,603	1239	21	19	30
8	4.0	0.95	8	0	37,755	244	36,286	1225	15	16	25
9	4.0	1.0	6	1	36,067	289	34,404	1374	1	9	16
10	4.0	1.0	8	1	37,196	263	35,640	1293	10	23	28
11	4.0	1.05	6	0	39,292	359	37,478	1455	4	10	11
12	4.0	1.05	8	0	38,223	349	36,443	1431	2	16	16
13	4.1	0.95	6	0	39,501	377	37,746	1378	9	23	26
14	4.1	0.95	8	0	40,955	410	39,115	1430	7	12	20
15	4.1	1.0	6	1	39,257	368	37,515	1374	11	25	20
16	4.1	1.0	8	0	40,062	391	38,310	1361	12	27	28
17	4.1	1.05	6	0	38,774	394	37,043	1337	13	15	22
18	4.1	1.05	8	2	40,439	418	38,529	1492	3	10	12
19	4	2	8	9	41,776	499	40,340	937	0	0	0
20	4	4	8	44	40,700	1054	38,717	929	0	0	0
21 ^{α}	3.2	1	6	2	27,260	2516	23,730	1014	23	17	33

Note. Complete list of models used in this study. Models 1–18 all have similar properties to NGC 6397 at present day (see Figure 2). Unlike the other models, models 19–20 still retain BHs at present and thus have yet to undergo core collapse (see Figure 4). Model 21 (denoted by α) has a primordial binary fraction of 50%, while all other models assume 5% (see discussion in Section 7.3).

the core of a new giant star with total mass $M_3 = M_1 + M_2$ and core mass $M_{3,c} = M_2$. For an He WD + MS merger, the product will be a star on the first giant branch (BSE stellar type $k = 3$). For a CO/ONe WD + MS merger, the product is a thermally pulsating AGB star (BSE stellar type $k = 6$). A new age appropriate to its core mass is then computed for this new star as described in Section 2.7.4 of Hurley et al. (2002). This treatment is also simplified in nature. In reality, a collision between an MS star and a WD may lead to complete destruction of the star and detonation of the WD (e.g., Shara & Shaviv 1977). We return to this topic in Section 6.

2.2. Cluster Models

In Rui et al. (2021a), we presented a framework for comparing CMC models to observed clusters based on surface brightness and velocity dispersion profiles. As an application of this framework, we analyzed the CMC Cluster Catalog and identified best-fit models for dozens of GCs observed in the Milky Way (MW), including NGC 6397, which was examined in detail in this earlier study. We direct the reader to Rui et al. (2021a) for a more detailed discussion of our scheme for identifying best-fit models for a given observed system.

In this analysis, we start with the CMC simulation identified by Rui et al. (2021a) as an effective match to present-day NGC 6397. The initial conditions for this simulation are shown as row 10 in Table 1. In order to increase our sample of NGC 6397-like models, we run 17 additional simulations that explore the parameter space near our original best-fit model. Specifically, we adopt a grid of values with initial particle number $N/10^5 = (3.9, 4, 4.1)$, initial virial radius $r_v/\text{pc} = (0.95, 1, 1.05)$, and Galactocentric distances $R_{gc}/\text{kpc} = (6, 8)$. We

also include two additional simulations with $r_v = 2$ and 4 pc to demonstrate the differences between an NGC 6397-like cluster and BH-rich clusters with large cores at present day.

In all models, we adopt a metallicity of $Z = 0.0002$ (the observed metallicity of NGC 6397; Harris 1996). We assume all models are initially fit by a King model (King 1962) with concentration parameter $W_0 = 5$. We adopt a Kroupa initial mass function in the range $0.08\text{--}150 M_\odot$ (Kroupa 2001). For primordial binaries, we assume orbital separations drawn from a log-uniform distribution in orbital period from near contact to the hard-soft boundary, mass ratios drawn from a uniform distribution from 0.1 to 1, and eccentricities drawn from a thermal distribution. For our fiducial set of models (1–20 in the table), we adopt a primordial binary fraction of 5%. We also examine a simulation with a primordial binary fraction of 50% to explore its effect on our results (see Section 7.3).

In Figure 2, we show surface brightness and velocity dispersion profiles for all models in this study overlaid on observed profiles of NGC 6397 from Trager et al. (1995), Watkins et al. (2015), Baumgardt & Hilker (2018), and Baumgardt et al. (2019). For further discussion of how models are compared to observations, see Rui et al. (2021a). In bold red, we show the model identified as the best fit to NGC 6397 (via the method in Rui et al. 2021a), corresponding to simulation 17 from Table 1 at the final cluster snapshot. In dashed blue, we show simulation 20 at the final cluster snapshot. Although nearly identical in total mass to our NGC 6397-like models, model 20, which contains 44 BHs, clearly does not resemble the overall structure of NGC 6397 at present, as its core is influenced significantly by its BH population. In light red, we show all remaining NGC 6397-like models from Table 1 (models 1–18).

Figure 2. Surface brightness (top) and velocity dispersion (bottom) profiles for all models in this study compared to observed profiles for NGC 6397. In red, we show data from simulations 1–18, with the bold red curves indicating our best-fit model for NGC 6397. In blue we show results from simulation 20, which, unlike the other models, contains a BH subsystem throughout its entire lifetime.

3. White Dwarf Populations in Core-collapsed Clusters

In Figure 3, we show the enclosed mass of various stellar populations as a function of (2D-projected) distance from the cluster center for two representative clusters: in the top panel we show our best-fit model to NGC 6397 (model 17 in Table 1) and in the bottom panel we show the BH-rich counterpart model 20 that has yet to undergo core collapse by the present day. In both panels, the blue curves denote the WD population: all WDs (solid), CO WDs (dashed), He WDs (dotted), and ONe WDs (dashed-dotted). The remaining colors denote other stellar populations, as shown in the figure legend.

We denote with a vertical dashed line a distance of 0.07 pc (6") from the cluster center, within which Vitral & Mamon (2021) argue a diffuse cluster of dark objects of mass $1000\text{--}2000 M_\odot$ is enclosed in NGC 6397. As shown, roughly $10^3 M_\odot$ ($30 M_\odot$) of WDs (NSs) are enclosed within this distance in our NGC 6397-like model. This model contains zero BHs. Thus, as in Rui et al. (2021b), we argue that a central population of massive WDs—roughly two-thirds CO and one-third ONe WDs—is the most plausible explanation for the dark diffuse component identified in Vitral & Mamon (2021).

The model shown in the bottom panel of Figure 3 contains roughly $1000 M_\odot$ worth of stellar BHs ($N_{\text{BH}} = 44$) at late times. A BH population this massive dominates the core dynamics, and mass segregation forces lower-mass luminous stellar

populations outward. As a result, this BH-rich counterpart exhibits a large observed core radius (roughly 3 pc; see Figure 4) at present. The key point is that a large BH population is inconsistent with an observed core-collapsed structure.

In Figure 4, we show the time evolution of these same two cluster models (blue curves denote our best-fit simulation for NGC 6397 while gray curves show the BH-rich simulation 20). We also include simulation 19 as an intermediary ($r_v = 2$ pc) between these two extremes. The top panel shows the number of BHs retained as the cluster evolves. In all three clusters, roughly 500 BHs (out of 800 in total) are retained in the cluster at early times after taking into account natal kicks. The number of BHs subsequently declines as BHs are ejected due to dynamical processes as described in Section 1. The number of BHs retained at late times is determined by the ejection rate, which in turn is determined by the initial cluster density; the NGC 6397-like model (initial $r_v = 1$ pc) is initially the most dense of the three and ultimately ejects all of its BHs.

A frequently used parameter that reflects the dynamical age of a GC is the ratio between the core radius, r_c , and the half-light radius, r_h (e.g., Fregeau & Rasio 2007; Chatterjee et al. 2013). In a self-gravitating system like a GC, energy flows naturally from the core to the halo, leading to core contraction and halo expansion (e.g., Heggie & Hut 2003). As a cluster ages, r_c/r_h decreases (at a rate determined primarily by “BH burning” in the cluster core; Kremer et al. 2020a). This core contraction halts when quasi-equilibrium is achieved through the energy generated by dynamical burning of stellar binaries (e.g., Heggie & Hut 2003). In the middle panel of Figure 4, we show r_c/r_h versus time. Here the core radius is defined as the theoretical density-weighted core radius typically used in N -body simulations (e.g., Casertano & Hut 1985). In all three simulations, the core expands at early times due to mass loss from high-mass stellar evolution. In the $r_v = 4$ pc model, which retains the most BHs at the end of the simulation, the core is heated by BH dynamics and r_c/r_h remains roughly constant over the complete lifetime. For $r_v = 2$ pc, the core is still contracting by the end of the simulation—binary burning equilibrium has yet to be achieved. In the NGC 6397-like cluster, which ejects all of its BHs after roughly 10 Gyr, the core contracts significantly, ultimately undergoing collapse and attaining quasi-equilibrium once binary burning (primarily of WDs, as shown in Figure 3) begins.

Finally, in the bottom panel, we show the number density of WDs within the cluster core radius (here defined in the observational sense; see Morscher et al. 2015) versus time. The number of retained WDs is determined primarily by the initial mass function and subsequent stellar evolution, which are assumed to be identical for these three clusters. Thus, the total number of WDs is roughly comparable in these three clusters (see also Table 1). In this case, the differences in the evolution of WD density are attributed primarily to the evolution of core radius. We see that, in the absence of BHs, a core-collapsed cluster like NGC 6397 features a central WD density roughly three orders of magnitude higher than a cluster in the BH burning phase.

The connection between WD and BH subsystems suggested by Figures 3 and 4 in the context of clusters with NGC 6397-like masses and properties is indeed a general trend across all cluster types. To demonstrate this point, we use the set of cluster models published in the CMC Cluster Catalog.

Figure 3. Enclosed mass vs. radius for various stellar populations for our best-fit model for NGC 6397 (simulation 17; top panel) and for our representative BH-rich cluster (simulation 20; bottom panel). The vertical dashed black line denotes the cluster-centric distance within which Vitral & Mamon (2021) constrained a diffuse subsystem of roughly $1000 M_{\odot}$ in NGC 6397. We argue that, in NGC 6397, WDs are the most plausible explanation for this massive dark population.

This catalog contains roughly 150 cluster simulations (evolved for a Hubble time or until dissolution) that collectively span the range in observed properties (such as cluster mass, metallicity, radii, and Galactocentric distances) of the Milky Way GCs at present day. To focus specifically on old low-metallicity clusters,⁸ we exclude here the 50 solar-metallicity simulations in the catalog. In Figure 5, we show the number density of WDs within the cluster core radius versus total number of retained BHs (top panel) and versus the core radius (bottom panel) for all models in this catalog with ages in the range 10–14 Gyr. The different colors indicate the five distinct values of initial N (initial cluster mass) assumed. As illustrated in the figure, for constant initial cluster mass, clusters with larger BH subsystems (and thus larger core radii due to the influence of BH burning) feature relatively lower-density WD populations in their cores. Once its BH subsystem has been depleted, a cluster develops a dense WD subsystem.

Motivated by these results, we argue that a dense central population of WDs is a common feature of all dynamically old

⁸ While in principle WD subsystems will develop in high-metallicity (e.g., near $Z_{\odot}$) clusters, high-metallicity clusters born relatively recently are unlikely to be sufficiently old at present day to have reached core-collapse (although of course this depends on cluster masses and other properties). We reserve for future work a study of the possibility of WD subsystems in high-metallicity young clusters.

Figure 4. The evolution in time of various cluster properties for an NGC 6397-like model (blue; $r_v = 1$ pc) and two non-core-collapsed BH-rich clusters of identical initial mass: black ($r_v = 2$ pc) and gray ($r_v = 4$ pc). In the top panel we show the total number of retained BHs vs. time, in the middle we show the ratio of core radius to half-light radius, r_c/r_h , and in the bottom panel we show the number density of WDs within the core radius. In our NGC 6397-like model, core contraction is halted at $t \approx 10$ Gyr when quasi-equilibrium is attained through energy generated by dynamical “burning” of WD binaries.

core-collapsed clusters. Indeed, the presence of high-density WD subsystems in core-collapsed clusters has been hinted at previously, specifically in the context of M15 (Murphy et al. 2011). Given that core-collapsed clusters are common (in the Milky Way, roughly 20% of GCs are core-collapsed; Harris 1996), this has important implications for various astrophysical phenomena that may be influenced by WD dynamics. We go on to explore several such applications in the following sections.

4. White Dwarf Mergers

We expect WD binaries to merge through two primary mechanisms:

1. *Gravitational wave-driven inspirals* that occur after a binary has hardened to Roche lobe overflow through series of binary-mediated encounters. If $q > 0.628$ (see Section 2), we assume a merger ensues. These GW inspiral-driven mergers may occur either inside or outside the cluster, depending on whether a binary has attained sufficiently high recoil to have been ejected from its host.

Figure 5. Number density of WDs within the cluster core radius vs. total number of BHs retained (top panel) and vs. core radius (bottom panel) for all low-metallicity cluster models in the CMC Cluster Catalog (Kremer et al. 2020b). Black, blue, green, orange, and yellow points indicate models with initial N of $[2, 4, 8, 16, 32] \times 10^5$, respectively.

2. *Direct physical collisions* that occur when the pericenter distance of a pair of WDs is less than the sum of the WD radii, $r_p < R_1 + R_2$. These collisions may occur through single–single encounters or during binary–resonant encounters.⁹

To develop a sense of the typical timescales at play and to build physical intuition, we analytically explore these merger processes in Section 4.1. In Section 4.2, we compare the results from our N -body models to our analytic estimates. In Section 4.3, we estimate the overall WD merger rate and discuss the potential detectability of these binaries as GW sources.

⁹ The direct collision channel is analogous to the “GW capture” channel for binary BH mergers (e.g., Samsing 2018; Rodriguez et al. 2018). For WDs, the cross section for GW capture lies within the WD’s physical radius, thus in this limit a head-on collision (i.e., with no inspiral) occurs.

4.1. Analytic Estimates

Within a core-collapsed cluster, WD binaries will undergo series of binary-mediated encounters that gradually harden the binaries (e.g., Heggie & Hut 2003). Conservation of energy requires that, when a binary hardens, energy be transferred to the center-of-mass velocity of the interacting stars. Thus, the recoil velocity of the binary increases with each encounter. This process continues either until the binary receives a recoil velocity sufficient to eject it from the host cluster or until the binary’s GW inspiral time becomes small enough that the binary merges inside the cluster.

The characteristic orbital separation at which a binary will be dynamically ejected is given by

$$a_{ej} \approx \alpha \frac{Gm}{v_{esc}^2} \approx 0.02 \text{ au} \left(\frac{m}{M_\odot} \right) \left(\frac{v_{esc}}{40 \text{ km s}^{-1}} \right)^{-2} \quad (3)$$

(e.g., Rodriguez et al. 2016; Samsing 2018), where we have adopted $v_{esc} \approx 40 \text{ km s}^{-1}$ as the escape velocity from the core of a host cluster representative of NGC 6397 and assumed $\alpha \approx 1/6 \times [1/\delta - 1]$, where $\delta \approx 7/9$ is a constant that reflects the amount by which the semimajor axis of a binary changes with each encounter (for detail, see Samsing 2018). To determine whether or not a binary with orbital separation a_{ej} is more likely to be ejected (and potentially merge after ejection) or to merge inside its host cluster, we compare the characteristic timescales for GW inspiral and binary–single encounters that may lead to ejection.

For a binary near a_{ej} , the characteristic timescale to undergo a binary–single encounter and be ejected is given by

$$t_{ej} \approx \frac{1}{n_{WD} \Sigma \sigma_v}, \quad (4)$$

where n_{WD} is the number density of single WDs in the WD subsystem, σ_v is the velocity dispersion, and Σ is the cross section of the binary. Including gravitational focusing, this cross section can be expressed as

$$\Sigma = \pi a_{ej}^2 \left(1 + \frac{6Gm}{a_{ej} \sigma_v^2} \right), \quad (5)$$

where $m \approx 1 M_\odot$ is a typical WD mass. Assuming the gravitational focusing term dominates (typical for velocity dispersions found in GCs), we obtain

$$t_{ej} \approx 900 \text{ Myr} \left(\frac{\sigma_v}{10 \text{ km s}^{-1}} \right) \times \left(\frac{v_{esc}}{40 \text{ km s}^{-1}} \right)^2 \left(\frac{n_{WD}}{10^6 \text{ pc}^{-3}} \right)^{-1} \left(\frac{m}{M_\odot} \right)^{-2} \quad (6)$$

for binaries near a_{ej} .

For highly eccentric binaries (representative of dynamically formed binaries; e.g., Heggie & Hut 2003), the GW inspiral time for a WD binary at this separation can be estimated (as in Peters 1964) as

$$t_{insp} \approx 100 \text{ Myr} \left(\frac{a}{0.02 \text{ au}} \right)^4 \left(\frac{m}{M_\odot} \right)^{-3} (1 - e^2)^{7/2}, \quad (7)$$

where we have adopted a fiducial eccentricity of $e = 0.9$.

With these two timescales in mind, we can draw two immediate conclusions. First, given that both t_{ej} and t_{insp} are small compared to the typical time by which we expect an NGC 6397-like cluster to have reached a core-collapsed configuration with high central WD density (≈ 4 Gyr; see Figure 4), we conclude that GW inspirals of WDs will certainly occur in these environments. Second, since $t_{\text{insp}} < t_{\text{ej}}$, we expect that once a binary is hardened to a_{ej} , an in-cluster merger is more likely than an ejection.

Note that this is different from the case of binary BHs. Since $a_{\text{ej}} \propto m$ and since $m_{\text{BH}} \sim 10 M_{\odot}$ is an order of magnitude larger than the typical WD mass, the characteristic orbital separation for BH binaries to be ejected is relatively wide compared to that for WD binaries. In this contrasting case for BHs, $t_{\text{ej}} \propto m^{-2} \approx 9$ Myr (Equation (6)), a factor of 100 times shorter than the characteristic ejection time for WD binaries. Meanwhile, the GW inspiral time of a binary of separation a_{ej} scales as $t_{\text{insp}} \propto a_{\text{ej}}^4 m^{-3} \propto m$. Thus for BH binaries, t_{insp} is an order of magnitude or more larger than t_{ej} , indicating that most BH binaries will be ejected prior to merger. Indeed, in the models considered in this study, roughly two-thirds of all BH mergers occur after the binary has been ejected, with the other third occurring through in-cluster inspirals and GW captures combined. Of course, the ratio of in-cluster to ejected mergers depends upon the host cluster’s escape velocity; more massive and compact clusters will always feature a higher ratio of in-cluster to ejected mergers, regardless of the binary component masses. We have focused here simply on escape velocities representative of NGC 6397.

Next, we estimate the rate of WD mergers occurring through direct collisions. For single–single encounters, this rate is given by

$$\Gamma_{\text{coll}}^{\text{ss}} \approx n_{\text{WD}} \Sigma_{\text{coll}} \sigma_v N_{\text{WD}}, \quad (8)$$

where Σ_{coll} is the cross section for collisions (Equation (5) with a replaced by the WD’s physical radius). This produces the following scaling:

$$\Gamma_{\text{coll}}^{\text{ss}} \approx 0.2 \text{ Gyr}^{-1} \left(\frac{m}{M_{\odot}} \right) \left(\frac{R_{\text{WD}}}{10^8 \text{ cm}} \right) \times \left(\frac{n_{\text{WD}}}{10^6 \text{ pc}^{-3}} \right) \left(\frac{\sigma_v}{10 \text{ km s}^{-1}} \right)^{-1} \left(\frac{N_{\text{WD}}}{1000} \right). \quad (9)$$

For a cluster spending roughly 4 Gyr in a core-collapsed configuration (as in the NGC 6397-like model shown in Figures 3 and 4), we can expect $\mathcal{O}(1)$ WD–WD collisions through single–single encounters.

For collisions occurring during binary–single resonant encounters, the collision rate can be expressed as

$$\Gamma_{\text{coll}}^{\text{bs}} \approx n_{\text{WD}} \Sigma \sigma_v N_{\text{bin}} P_{\text{coll}}, \quad (10)$$

where Σ is the cross section for binary–single encounters given by Equation (5), N_{bin} is the number of WD binaries (assuming a 10% binary fraction in the core, $N_{\text{bin}} \approx 0.1 N_{\text{WD}}$), and P_{coll} is the probability that a given binary–resonant encounter leads to a collision. For resonant encounters with roughly equal component masses, $P_{\text{coll}} \propto R/a$ (e.g., Heggie & Hut 2003). For example, Samsing et al. (2017) showed that for binary–single encounters with three WDs and semimajor axis values of 10^{-3} – 0.1 au, $P_{\text{coll}} \sim 100(R/a)$. Adopting this relation and assuming, as before, that gravitational focusing dominates,

we write the binary–single collision rate as

$$\Gamma_{\text{coll}}^{\text{bs}} \approx 3 \text{ Gyr}^{-1} \left(\frac{m}{M_{\odot}} \right) \left(\frac{R_{\text{WD}}}{10^8 \text{ cm}} \right) \times \left(\frac{n_{\text{WD}}}{10^6 \text{ pc}^{-3}} \right) \left(\frac{\sigma_v}{10 \text{ km s}^{-1}} \right)^{-1} \left(\frac{N_{\text{WD}}}{1000} \right). \quad (11)$$

Therefore, we expect collisions through binary–single encounters to be roughly a factor of 10 more common than those occurring through single–single interactions. For NGC 6397-like clusters, we can expect $\mathcal{O}(12)$ binary-mediated collisions per cluster. Since the characteristic timescale for collisions $t_{\text{coll}} \approx (\Gamma_{\text{coll}}^{\text{bs}})^{-1} \approx 300$ Myr is comparable to the timescale for in-cluster inspirals (Equation (7)) we can expect these two channels to contribute roughly comparable rates in NGC 6397-like clusters.

4.2. Results from N-body Models

Having motivated the topic analytically, we now discuss the WD mergers identified in our N -body models. In total, from our 18 models representative of NGC 6397 (see columns 10, 11, and 12 of Table 1), we identify 161, 305, and 403 mergers from the ejected inspiral, in-cluster inspiral, and head-on collision channels, respectively. As predicted from the analytic estimates, in-cluster inspirals and collisions produce comparable rates in our models, while the rate from ejected inspirals is lower by a small factor. Of the 403 total direct collisions, 15 occur through single–single encounters and 196 (192) occur through binary–single (binary–binary) resonant encounters; as predicted from the analytic estimates, binary-mediated encounters dominate the direct collision rate by an order of magnitude or more.

In Figure 6, we illustrate the sequence of dynamical encounters leading to merger for three representative mergers, one from each channel. All three of these sequences come from simulation 17. As demonstrated by these three examples, WD binaries in general undergo extended series of encounters with other WDs and MS stars in their host clusters, hardening the binaries until GW inspiral leads to merger. En route to a sufficiently compact orbital separation, WDs will occasionally collide with other WDs (and MS stars; see Section 6).

In the left panel of Figure 7, we show the component masses for all WD mergers and collisions identified in our models. More than 90% of the mergers/collisions feature a total mass in excess of the Chandrasekhar limit (shown as the dashed black line in the figure). As a dashed gray line, we show the $q > 0.628$ boundary, above which WD binaries driven to Roche lobe overflow through GW inspiral are assumed to be dynamically unstable, leading to merger (see Section 2). In the right panel of Figure 7, we show the semimajor axis and eccentricity at the time of the last dynamical encounter for all WD binaries that merge through GW inspiral. For in-cluster (ejected) mergers, the median semimajor axis is 0.13 au (0.03 au) and the median eccentricity is 0.99 (0.94). As expected for reasons described in Section 4.1, in-cluster mergers typically form at higher eccentricity and larger semimajor axis than ejected mergers.

Ejected inspiral

In-cluster inspiral

Direct collision

Binary—single resonant encounter + collision
 $M_1 = 1.3 M_\odot$
 $M_2 = 1.0 M_\odot$

Figure 6. Illustration of the dynamical encounter histories for representative WD mergers from each of the three merger channels described in Section 4. These mergers are each taken from simulation 17 in Table 1.

Figure 7. Left panel: component masses for all WD–WD mergers/collisions occurring at late times ($t > 9$ Gyr) in our simulations. Blue and red circles denote ejected and in-cluster inspirals, respectively, and black open circles denote collisions. The dashed black line marks systems with a total mass equal to the Chandrasekhar limit ($1.44 M_\odot$), and the dashed gray curve marks the $q > 0.628$ boundary, above which Roche lobe overflow is assumed to lead to merger (see Section 2). Right panel: eccentricity vs. semimajor axis at time of last dynamical encounter for all inspirals, with colors the same as in the left panel.

4.3. Estimating the Merger Rate and Prospects for GW Detection

Assuming a typical core-collapsed cluster underwent core collapse and formed a WD subsystem roughly 4 Gyr ago (as motivated by the NGC 6397–like models; see Figure 4), we estimate from our models a total rate of roughly 10^{-8} WD mergers per year for a single NGC 6397–like cluster. In the Milky Way, roughly 20% of observed GCs are core-collapsed. Assuming a population of roughly 200 GCs in the Milky Way

(150 observed plus an additional ~ 50 that may be hidden behind the bulge), we assume roughly 40 core-collapsed clusters populate our Galaxy at present. Accounting for the fact that NGC 6397 is a factor of roughly two times less massive than the average Milky Way GC, and assuming that the WD merger rate scales roughly linearly with cluster mass (as is the case for binary BH mergers; e.g., Rodriguez et al. 2016), we estimate a total WD merger rate of roughly 10^{-6} yr^{-1} in a Milky Way–like galaxy. For a giant elliptical galaxy like M87, expected to host $\gtrsim 10^4$ GCs (e.g., Tamura et al. 2006), the rate

Figure 8. Characteristic strain vs. peak GW frequency for all WD–WD inspirals identified in our models. Red (blue) curves mark systems that merge inside (outside) their host cluster. For reference, the dashed black curve denotes a representative $1 M_{\odot} + 1 M_{\odot}$ system and the vertical dashed lines mark inspiral times for this representative binary as it evolves. The solid black and gray curves show the sensitivity curves for LISA and DECIGO, respectively.

may be as high as 10^{-4} yr^{-1} . Assuming the average number density of GCs in the local universe is roughly 3 Mpc^{-3} (e.g., Rodriguez et al. 2016) and assuming a fraction f of these clusters are core-collapsed, we estimate an overall WD merger rate of roughly $f \times 50 \text{ Gpc}^{-3} \text{ yr}^{-1}$ in the local universe from GCs.

In analogy with the proposed connection of BH subsystems in GCs and gravitational-wave sources detected by LIGO/Virgo (e.g., Rodriguez et al. 2016; Askar et al. 2017; Fragione & Kocsis 2018; Rodriguez & Loeb 2018; Antonini & Gieles 2020; Kremer et al. 2020b), an obvious application to explore is GW astronomy. Unlike stellar BH and NS binaries, which merge within the LIGO/Virgo frequency band ($f_{\text{GW}} > 10 \text{ Hz}$), WD binaries merge at decihertz frequencies, as limited by the physical sizes of WDs. In this case, millihertz detectors such as LISA (e.g., Amaro-Seoane et al. 2017) and decihertz detectors like DECIGO (e.g., Kawamura et al. 2011; Arca Sedda et al. 2020) are necessary to observe the inspiral and merger of these systems.

In Figure 8, we show the characteristic GW strain (calculated as in Kremer et al. 2019b, assuming a LISA observation time of 5 yr) and peak frequency of GW emission (calculated as in Wen 2003) from formation (marked as the filled circles) to merger for all inspiraling systems identified in our models. In red (blue), we show the WD binaries that merge inside (outside) their host cluster, depending on whether or not a given system was dynamically ejected. For reference, the dashed black curve denotes the inspiral of a characteristic $1 M_{\odot} + 1 M_{\odot}$ circular WD binary. For this characteristic system, we show a number of representative inspiral times as vertical dashed lines. For all systems in this plot, we assume a source distance of 9 kpc from Earth, the average heliocentric distance of GCs in the MW.

The solid black and gray curves denote the sensitivity curves for LISA (Robson et al. 2019) and DECIGO. For “stationary” sources (i.e., sources whose frequency evolves negligibly over the 5 yr LISA observation window), the signal-to-noise ratio can be read roughly by eye from this figure as the height of the characteristic strain above the sensitivity curve. For instance, at $f_{\text{GW}} \approx 1.5 \times 10^{-3} \text{ Hz}$ ($t_{\text{insp}} \approx 1 \text{ Myr}$), the characteristic strain of the characteristic $1 M_{\odot} + 1 M_{\odot}$ binary (dashed black curve) is roughly a factor of 10 above the LISA sensitivity curve at this frequency, indicating a signal-to-noise ratio of roughly 10 at the assumed distance of 9 kpc.

The characteristic strain of a source is inversely proportional to the distance. Thus, WD–WD inspirals are unlikely to be resolved by LISA at distances far beyond the Milky Way. Combined with the small estimated WD merger rate from Galactic GCs ($\approx 10^{-6} \text{ yr}^{-1}$), this suggests it is highly unlikely that LISA would observe a merging WD binary formed in a GC. However, LISA may resolve these inspiraling binaries as stationary sources at lower frequencies (roughly millihertz) when their inspiral times are still long (e.g., Willems et al. 2007; Kremer et al. 2018a). We can estimate the number of detectable stationary sources as $N_{\text{stat}} \approx \Gamma_{\text{merger}} \times t_{\text{insp}}$, where Γ_{merger} is the total merger rate (roughly 10^{-8} yr^{-1} per typical core-collapsed GC) and t_{insp} is the inspiral time when the source becomes resolvable by LISA. From Figure 8, we see $t_{\text{insp}} \approx 10 \text{ Myr}$ for a $1 M_{\odot} + 1 M_{\odot}$ binary when its strain exceeds the LISA sensitivity. Thus, we estimate roughly 10^{-1} sources per core-collapsed cluster. NGC 6397, roughly a factor of five times nearer to Earth than the average MW GC, may contain up to order unity resolvable sources. Assuming 40 core-collapsed clusters in the MW, we estimate roughly four resolvable sources from GCs in our Galaxy. To within a factor of a few, this estimate is satisfyingly consistent with the roughly 20 resolvable WD–WD sources previously estimated

in Kremer et al. (2018a) using CMC models that neither included relativistic effects nor focused specifically on core-collapsed clusters.

Although LISA will not be able to observed extragalactic WD sources in large numbers, third-generation decihertz detectors (which propose to probe higher GW frequencies at greater sensitivity) may observe many extragalactic WD binaries. For instance, Maselli et al. (2020) demonstrated that mergers of roughly $1 M_{\odot}$ WDs can be resolved by DECIGO with signal-to-noise ratios of roughly 20 out to a distance of 1 Gpc, potentially enabling GW detection of roughly dozens of WD mergers formed in GCs per year.

5. White Dwarf Merger Outcomes

In this section, we discuss potential outcomes of the WD mergers/collisions identified in our models and examine a few potential observational tests.

In the top panel of Figure 9, we show in black the normalized distribution of component masses for all WD mergers (here combining the ejected and in-cluster inspirals and the collisions). In blue, we show the normalized mass distribution for all WDs formed through standard stellar evolution. The peak at roughly $0.6 M_{\odot}$ arises simply from the initial mass function; these WDs come from stars with $M_{\text{ZAMS}} \approx 1 M_{\odot}$, which in old ($t \gtrsim 10$ Gyr) clusters are the least massive objects that have yet to form WDs. Meanwhile, the peak in the WD mass distribution at roughly $1 M_{\odot}$ arises from the “bump” in the $M_{\text{WD}}-M_{\text{ZAMS}}$ relation at ZAMS masses in the range $\approx 2.5-3.5 M_{\odot}$ at low metallicities (see Figure 1). This bump is caused by the growth (or lack thereof) of the progenitor stars’ cores while on the giant branch (see Hurley et al. 2000). As shown, the population of WDs that go on to merge are preferentially more massive than the overall WD population. In a core-collapsed cluster, the most massive WDs mass-segregate to the dense central regions, where, due to increased dynamical activity, they are more likely to merge.

In the bottom panel of Figure 9, we show the normalized distribution of total mass, $M_1 + M_2$, for all merging/colliding WD pairs of various types identified in our models. Of the roughly 1000 mergers/collisions identified in our models, 44% feature two CO WDs (dark blue histogram), 13% two ONe WDs (green histogram), 38% a CO and ONe WD pair (light blue histogram), and only 5% an He WD paired with a CO or ONe WD (black histogram). The dashed vertical line marks the Chandrasekhar limit. 91% of all mergers/collisions in our models have a total mass greater than M_{Ch} .

The outcomes of WD mergers/collisions are highly uncertain and various scenarios have been proposed depending on the masses and compositions of the two WDs involved. These outcomes fall broadly into two main camps: the nondestructive case (similar to what is implemented in CMC) that forms a massive single WD (e.g., Schwab 2021) or NS/pulsar (e.g., Nomoto & Iben 1985; Schwab et al. 2016) and the destructive case where an explosive transient results with no remnant left behind. As described in Section 2, we assume in CMC that all WD mergers/collisions avoid complete detonation and instead result in an ONe WD (in the event of dynamically unstable binary mass transfer) or an accretion-induced-collapse NS (in the event of a “sticky sphere” dynamical collision).

In Figure 10, we show a Hertzsprung–Russell (H-R) diagram for all single WDs found in our best-fit model for NGC 6397. Luminosities are calculated as in Equation (2) and temperatures

are computed using the radii obtained from Equation (1) and assuming blackbody emission. Filled circles denote WDs formed through standard evolution of a single star. The blue band reproduces the well-known cooling track produced by CO WDs of various ages (e.g., Hansen et al. 2007; Richer et al. 2013). ONe WDs result from a relatively narrow range in ZAMS mass ($\approx 4.5-6 M_{\odot}$ for $Z = 0.0002$; see Section 2). So, unlike the CO WDs that form over a wide range of times, ONe WDs all form at $t \sim 100$ Myr. This relatively narrow range in ONe WD age manifests itself as the horizontal green band seen in the figure.

Open circles show remnant WDs formed through recent in-cluster WD mergers identified in the model (13 in total). For these WDs, we reset the age following merger and use the new WD mass to recalculate the luminosity and temperature using Equations (1) and (2). Of course, the true luminosities and temperatures of WD merger remnants are uncertain. However, we note that WD J0551+4135 (Gentile Fusillo et al. 2019), identified as a potential high-mass, $\approx 1.15 M_{\odot}$, WD candidate based on its position in the Gaia H-R diagram (Gaia Collaboration et al. 2018), occupies a similar location in the H-R diagram to our proposed WD merger remnants (i.e., to the upper left of the standard WD cooling sequence). Hollands et al. (2020) argue that the properties of this object are consistent with it having formed from an earlier WD merger. Although WD J0551+4135 is not itself identified in a star cluster, its observed features may provide a clue to the properties of WD merger remnants that may potentially be observed in clusters. For reference, we show the properties of WD J0551+4135 derived from Hollands et al. (2020) as a red star in Figure 10. If indeed a fraction of WD mergers result in young, massive WD remnants, we predict core-collapsed clusters like NGC 6397 may host up to $\mathcal{O}(10-20)$ such objects, which may be observationally identified by their unique position on the H-R diagram.

Another possible outcome of WD mergers/collisions is NS/pulsar formation. This outcome is expected if electron capture onto ^{20}Ne and ^{24}Mg is triggered, leading to collapse of the O/Ne/Mg core (e.g., Miyaji et al. 1980; Nomoto 1984). In our models, we assume this process occurs when the total mass of a WD + WD dynamical collision exceeds the Chandrasekhar limit. This is almost certainly an oversimplification; the precise details of WD mergers/collisions leading to NS formation are far more complex (e.g., Schwab 2021). However, our current implementation can at least roughly quantify the number of NSs/pulsars that may be formed through this process.

Pulsars are observably abundant in GCs (e.g., Ransom 2008). Most pulsars in Galactic GCs have millisecond periods—unsurprising since millisecond pulsars have low spin-down rates and thus long lifetimes ($\gtrsim 10^{10}$ yr). Meanwhile, young pulsars with periods $\gtrsim 30$ ms have relatively short lifetimes ($\approx 10^7$ yr). Thus young pulsars formed through standard stellar evolution at early times in GCs are no longer observed at present day. However, young pulsars may form at late times through dynamical interactions, including WD mergers, NS/WD–MS star collisions, and/or partial NS recycling via accretion in binaries (e.g., Verbunt & Freire 2014; Ye et al. 2019). In this case, observations of young pulsars in clusters may indicate prior WD mergers in clusters.

Figure 9. Top panel: normalized mass distribution for all WDs formed through standard evolution of a single/binary star (light blue) and mass distribution for all WD components that undergo mergers/collisions with other WDs (black). Bottom panel: normalized distribution of total mass, $M_1 + M_2$, for all WD mergers/collisions in our models. Different colors denote different combinations of WD types; 44% of all mergers are CO + CO WDs (dark blue histogram), 38% are CO + ONe (light blue), 13% are ONe + ONe (green), and 5% are He + CO/ONe (black).

In total, 17 young pulsars (spin period ≥ 30 ms) are currently observed in Galactic GCs: eight in core-collapsed GCs and nine in non-core-collapsed GCs.¹⁰ Given that about 20% of Galactic GCs are core-collapsed (Trager et al. 1995), this nearly even split tentatively suggests that young pulsars are overabundant in core-collapsed clusters. This may be due to the amplified WD merger rate in core-collapsed clusters at late times.

In CMC, we follow the prescriptions in Ye et al. (2019) to model pulsar magnetic fields and spin periods. When an NS

Figure 10. Hertzsprung–Russell diagram for all single WDs in the best-fit model identified for NGC 6397. Gray, blue, and green filled circles denote He, CO, and ONe WDs, respectively. Open circles denote young massive WDs formed through recent WD–WD mergers. The red star shows the inferred properties of WD J0551+4135, a high-mass WD candidate in the Galactic field proposed to have formed from a previous WD merger similar to those studied here.

forms through a WD–WD collision, we assume a new young pulsar forms. Once formed, these pulsars typically survive for $\sim 10^7$ – 10^8 yr before their magnetic fields and spin periods evolve sufficiently to fall below the pulsar “death” line. In our best-fit models for NGC 6397, we identify 1–2 young pulsars (defined here simply as pulsars with spin periods ≥ 30 ms) per snapshot. If WD binary mergers were assumed to produce pulsars in *all* cases, the number of young pulsars per model would likely increase by a small factor.

Some studies have argued that conservation of angular momentum during accretion-induced collapse may potentially lead to NSs with spin periods of a few milliseconds (e.g., King et al. 2001; Dessart et al. 2006). In this case, WD mergers may be progenitors of some fraction of the young millisecond pulsars observed in GCs. Additionally, if at least one of the merging WDs is highly magnetic (e.g., Ferrario et al. 2015), conservation of magnetic flux during accretion-induced collapse may produce NS magnetic fields of $\gtrsim 10^{14}$ G (e.g., King et al. 2001; Levan et al. 2006; Dessart et al. 2007; Schwab 2021), comparable to field strengths expected for magnetars (e.g., Woods & Thompson 2006; Olausen & Kaspi 2014). Although a magnetar has yet to be observed in an old GC, WD–WD mergers may provide a possible pathway to form such objects.

Alternatively, several studies argue that the most likely outcome of a massive WD merger/collision is an explosive transient with no remnant left behind. Possible transients include standard Type Ia SNe arising from carbon detonation (e.g., Webbink 1984; Woosley & Weaver 1994; Pakmor et al. 2010; Shen et al. 2018; Sato et al. 2016; Perets et al. 2019), subluminal transients such as SNe Iax (e.g., Foley et al. 2013) that may result from failed detonation (e.g., Kromer et al. 2015), or Ca-rich gap transients (e.g., Kasliwal et al. 2012).

¹⁰ <http://www.naic.edu/pfreire/GCpsr.html>

potentially formed from He shell ignition (e.g., Dessart & Hillier 2015; Polin et al. 2021). As shown in Section 4.2, we estimate an overall WD merger rate of up to roughly $50 \text{ Gpc}^{-3} \text{ yr}^{-1}$ in the local universe from core-collapsed GCs. The volumetric rate of Type Ia SNe observed in the local universe is $(2.5 \pm 0.5) \times 10^4 \text{ Gpc}^{-3} \text{ yr}^{-1}$ (Li et al. 2011; Cappellaro et al. 2015). Note that SNe Iax and Ca-rich gap transient rates are comparable to the Type Ia rate, within a factor of a few (e.g., Kasliwal et al. 2012; Foley et al. 2013). So, even in the scenario where *all* WD mergers in clusters lead to explosive transients, they are unlikely to constitute more than 0.1%–1% of the observed rate for these events in the local universe. Nonetheless, if a Type Ia SN or other transient were observed in association with a host cluster (either within the cluster or slightly offset from it if the WD binary merged after dynamical ejection), this would provide clear evidence for the dynamical processes described above.

We have suggested several possible outcomes of WD mergers/collisions and proposed some observational tests. In general, more detailed studies are required to determine more precisely the expected outcome of WD mergers/collisions and the properties of their potential remnants (if any). Some recent studies on this topic include Guerrero et al. (2004), Lorén-Aguilar et al. (2009), Rosswog et al. (2009), Dan et al. (2011), Woosley & Kasen (2011), García-Berro et al. (2012), Shen et al. (2012), Aznar-Siguán et al. (2013), Piro et al. (2014), Kromer et al. (2015), Schwab et al. (2016), Perets et al. (2019), Polin et al. (2019), and Schwab (2021).

6. Collisions between White Dwarfs and Main-sequence Stars

As shown in Figure 3, near the centers of core-collapsed clusters, a subdominant population of MS stars will mix with the massive WDs; in the case of our NGC 6397-like model, the ratio of WDs to MS stars is roughly 5:1 within the core defined at 0.07 pc. Due to mass segregation, the MS population in the central regions consists preferentially of stars near the turnoff mass (roughly $0.9 M_{\odot}$ for a cluster of this age), massive stars that formed via stellar collisions (which would be potentially observed as blue stragglers; e.g., Bailyn 1995), and MS binaries. Indeed, in the NGC 6397-like model shown in Figure 3, the median mass of MS stars in the central region is roughly $0.6 M_{\odot}$ compared to $0.2 M_{\odot}$ in the entire cluster. In addition to the role of MS stars in WD binary hardening (see Figure 6), interactions between these two populations will cause WD–MS collisions and WD–MS binary formation, which we discuss further in Section 7.

In the gravitational focusing limit, the cross section for WD–MS collisions is proportional to the MS star’s radius, and is therefore roughly 100 times larger than the WD–WD collision cross section (see Equations (9)–(11)). In this case, although MS stars are outnumbered by WDs in a core-collapsed cluster’s inner region, MS–WD collisions are expected to occur more than an order of magnitude more frequently than WD–WD collisions.

In total, 4750 WD–MS collisions occur at late times ($t > 9 \text{ Gyr}$) in our NGC 6397-like models (on average 263 per model). Of these, roughly 8% and 92% occur through single–single and binary-mediated resonant encounters, respectively. Performing rate calculations analogous to those in Section 4.2, we estimate a WD–MS collision rate of roughly 10^{-7} yr^{-1} per core-collapsed cluster, roughly $f \times 10^{-5} \text{ yr}^{-1}$ in

the Milky Way (as before, f is the fraction of clusters that are core-collapsed), and roughly $f \times 10^3 \text{ Gpc}^{-3} \text{ yr}^{-1}$ in the local universe.

In our CMC models, we assume a WD–MS merger produces a giant-branch star with core mass equal to the initial WD (see Section 2). In reality, this treatment is an oversimplification and the actual outcome of WD–MS collisions is very uncertain. Using hydrodynamic models, Ruffert (1992) demonstrated that, in the case of off-axis collisions ($r_{\text{peri}} \sim r_{\text{MS}}$), a disk may ultimately form with as little as $\sim 10\%$ of the mass being expelled from the system. However, others (e.g., Shara & Shaviv 1977; Shara & Regev 1986; Michaely & Shara 2021) have argued that, in the case of head-on collisions with little angular momentum, nuclear burning ignited from a shock created as the WD passes supersonically through the MS star may produce roughly 10^{48} – 10^{50} erg, comparable to the binding energy of the MS star. This suggests the majority of the disrupted MS star material becomes unbound from the system. Any unbound material is expected to expand at a velocity of the order of the WD’s escape velocity (roughly $7 \times 10^8 \text{ cm s}^{-1}$ for a $\approx 1 M_{\odot}$ CO WD). As shown in Michaely & Shara (2021), the characteristic timescale for this adiabatically expanding shell to become optically thin (roughly 10^6 – 10^8 s) can be combined with the energy generated from nuclear burning to estimate a total luminosity $L \approx 10^{48} \text{ erg} / (10^6\text{--}10^8 \text{ s}) \approx 10^{40}\text{--}10^{42} \text{ erg s}^{-1}$ for these collisions, comparable in brightness to a kilonova (e.g., Metzger et al. 2010) and a factor of 10–100 times dimmer than a standard core-collapse supernova. We reserve for future study a more detailed examination of potential transient signatures associated with these events.

Regardless of whether the disrupted stellar material ultimately remains bound to the WD following the collision, the original MS star is destroyed. Thus, the cumulative effect of these WD–MS collisions is a depletion of the MS star population. If measurable, this depletion may provide an observational test of the results presented here. In the NGC 6397-like model shown in Figure 3, a total of 323 WD–MS collisions occur once the cluster has undergone core collapse. The 323 MS stars destroyed through these collisions is negligible compared to the total number of MS stars in the entire cluster (roughly 2×10^5 at late times). However, only 500 MS stars reside within the innermost 0.1 pc (within the WD subsystem; see Figure 3). Of the 323 total WD–MS collisions, roughly 90% occur within the innermost 0.1 pc. Thus, within the central region, the depletion of MS stars through WD collisions is significant.

As a result of mass segregation, we expect the most massive MS stars to preferentially reside in the center of the cluster. This includes blue straggler stars (BSSs) that were formed from previous star–star mergers (e.g., Bailyn 1995; Shara 1999; Ferraro et al. 2012). In total, we identify 39 BSSs¹¹ in the best-fit model for NGC 6397 (simulation 17). In this model, we identify 94 BSS–WD collisions (roughly 30% of all 323 WD–MS collisions), more than double the total number of BSSs identified in the model. We conclude that WD collisions may lead to a significant depletion of BSSs in core-collapsed clusters. To this point, Piotto et al. (2004) analyzed a catalog of nearly 3000 BSSs observed in Galactic GCs and noted that the

¹¹ Here we define a BSS simply as any MS star with mass in excess of the MS turnoff mass ($M_{\text{to}} \approx 0.8 M_{\odot}$ for old clusters like NGC 6397). In these models, nearly all BSSs are formed through previous stellar collisions. See Kremer et al. (2020b) for further discussion of BSSs in CMC models.

BSS frequency in post-core-collapse GCs is comparable to the frequency in normal GCs, even though post-core-collapse clusters have relatively higher central densities. We can speculate that this may be explained in part by the regulation of BSSs through collisions with WDs. We reserve more detailed study of this possibility for future work.

Additionally, if one of the members of an MS–MS binary collides with a WD during a binary-resonant encounter, the original MS–MS binary is disrupted. In this case, we expect WD–MS collisions to reduce the number of MS–MS binaries in the cluster. In total, 82 MS–MS binaries are destroyed through WD–MS collisions in our NGC 6397–like model of interest. These 82 destroyed binaries are negligible compared to the total number of MS–MS binaries in the entire cluster (roughly 10^4 for our models with 5% primordial binary fraction). However, only 76 MS–MS binaries reside within the innermost 0.1 pc, indicating that in the cluster’s center, WD–MS collisions destroy a significant fraction of MS–MS binaries.

7. Discussion and Conclusions

7.1. Summary

1. Using a set of N -body models that effectively match the present observed properties of NGC 6397, we demonstrate that this cluster likely contains a central population of $\sim 10^3$ WDs ($\sim 10^3 M_\odot$ in total mass) within its innermost 0.07 pc. This supports the earlier finding of Rui et al. (2021b) and provides a natural explanation for the dark diffuse population reported in NGC 6397 by Vitral & Mamon (2021).
2. We argue that such WD-dominated cores with central densities $\geq 10^6 \text{ pc}^{-3}$ are a feature of all core-collapsed clusters at present day. Once all stellar-mass BHs have been dynamically ejected, the cluster core is no longer supported against collapse and lower-mass stellar populations (in particular, CO and ONe WDs) efficiently segregate to the cluster center. Ultimately, “burning” of central WD binaries halts the core-collapse process.
3. The high central densities of WDs in core-collapsed clusters facilitate formation and dynamical hardening of WD binaries. Ultimately these binaries will merge through either GW inspiral or direct collision with other WDs. We predict a WD merger rate of up to roughly $f \times 50 \text{ Gpc}^{-3} \text{ yr}^{-1}$ in the local universe, where f is the fraction of all globular clusters that have undergone core collapse. For Milky Way globular clusters, $f \approx 0.2$.
4. Prior to merger, inspiraling WD binaries will be observable as GW sources. Over its anticipated 5 yr mission lifetime, we estimate LISA may resolve of the order of one WD–WD binary at millihertz frequencies in NGC 6397 and of the order of a few WD–WD binaries in Galactic core-collapsed clusters overall. Proposed decihertz GW detectors such as DECIGO may resolve GW merger signals from dozens of these systems in clusters out to distances of roughly 1 Gpc.
5. The vast majority ($\gtrsim 90\%$) of all WD mergers identified in our models have total mass greater than the Chandrasekhar limit. The outcome of these WD mergers is uncertain, with some possibilities including an explosive transient like a Type Ia SN, formation of a young massive WD, or NS formation via accretion-

induced collapse. At most, WD mergers/collisions from clusters may constitute roughly 0.1%–1% of the overall Type Ia SN rate. If a fraction of mergers lead to massive WD remnants, these objects may be identifiable by their unique location on the H-R diagram to the left of the standard WD cooling sequence. Alternatively, if WD mergers/collisions produce NSs, these NSs may be detectable as young pulsars/millisecond pulsars or magnetars in old GCs.

6. Finally, we show that dynamical interactions between WDs and MS stars in core-collapsed clusters lead to WD–MS collisions occurring at a rate of up to $f \times 1000 \text{ Gpc}^{-3} \text{ yr}^{-1}$ in the local universe. Although the exact outcome of these collisions is uncertain, previous studies have shown they may be observed as bright transients with peak luminosities comparable to kilonovae. Regardless of the exact outcome, we predict that WD–MS collisions reduce the number of blue straggler stars and MS–MS binaries by a factor of a few within the innermost regions of core-collapsed clusters.

7.2. WD–Main Sequence Star Binaries

Also relevant is the formation of WD–MS binaries, some of which may be hardened to the point of Roche lobe overflow. In the left two panels of Figure 11, we show all distinct WD–MS binaries found at late times in our NGC 6397–like models. Blue points denote accreting systems while black and gray points indicate detached systems with CO/ONe WDs and He WDs, respectively. On average, we identify 287 detached WD–MS binaries and 23 accreting systems per model at any given snapshot in time in our NGC 6397–like models. We find that 65% of the detached systems, but only 25% of the accreting systems, form through dynamical interactions rather than as primordial binaries.

Observationally, these accreting binaries are expected to be identified as cataclysmic variables (CVs). CVs are well observed in GCs (e.g., Knigge 2012) and also well studied theoretically (e.g., Grindlay et al. 1995; Ivanova et al. 2006). In particular, Belloni et al. (2016, 2017b, 2017c, 2019) have studied CVs in detail using the MOCCA-Survey Database of GC models. The studies by Belloni et al. have demonstrated, among many other points, that the detectable CV population in clusters is composed primarily of CVs formed from primordial binaries (with most being formed through common envelope evolution) and in fact dynamical interactions are more likely to break apart primordial CV progenitors than lead to dynamical formation of new CVs. This is consistent with the findings of Kremer et al. (2020b) and with this study, where (as noted above) only a small fraction of accreting WD–MS binaries in our NGC 6397–like models form dynamically. Additionally, these studies have demonstrated that only a few percent of all CVs in a particular GC are likely to be detectable and that high primordial binary fractions (see Kroupa et al. 2013; Belloni et al. 2017a) are necessary to reproduce the observed number of CVs in NGC 6397 and other clusters.

In NGC 6397 specifically, 15 CVs have been observed (Cohn et al. 2010). In Rui et al. (2021a), we pointed out that our best-fit model for NGC 6397 contains a comparable number of accreting WD–MS binaries. In Cohn et al. (2010), the observed sample of CVs is divided into “faint” (9 in total) and “bright” (6 in total) categories, indicative of the apparent

Figure 11. All WD–MS binaries identified at late times in our NGC 6397-like models. Left and middle panels: orbital separation vs. WD mass (left) and MS companion mass (middle). In these panels, black (gray) circles indicate systems with a CO/ONe (He) WD. Blue circles indicate accreting systems. We denote as vertical dashed lines the boundary in WD mass separating CO and ONe WDs (left panel) and the boundary in MS mass separating our definitions of “faint” and “bright” systems, following Cohn et al. (2010). Right panel: cumulative fraction of accreting WD–MS binaries within the inner 100'' in our models (solid lines) compared to the distributions inferred from observed CVs in Cohn et al. (2010) (dashed lines). For reference, we also include the distribution of main-sequence turnoff (MSTO) stars (blue curve).

magnitude of each object. As pointed out in Cohn et al. (2010), the brightness of each system is determined by the mass of the MS companion. In our models, we use an MS mass of $0.5 M_{\odot}$ to separate the faint and bright systems. At a distance of 2.3 kpc, a $0.5 M_{\odot}$ MS star would be observed with an apparent V-band magnitude of roughly +21 mag, consistent with the faint/bright boundary in Cohn et al. (2010); see their Figure 3. Of the roughly 23 accreting WD–MS binaries found on average in our models, roughly 16 and 7 fall into the faint and bright categories, roughly consistent with the observed numbers in Cohn et al. (2010).

In the right-hand panel of Figure 11, we show the radial distribution of our faint and bright model CVs within the inner 100'' of our models compared to the radial distributions of observed systems published in Cohn et al. (2010). Solid lines denote model distributions while dashed lines denote observed distributions. For reference, we also show as a blue curve the radial distribution for main-sequence turnoff (MSTO) stars (defined simply as any MS star with mass in the range $[0.9, 1] \times M_{\text{to}}$, where M_{to} is the turnoff mass).

The radial distribution of faint CVs matches well both the observed distribution and the MSTO distribution, consistent with the results of Cohn et al. (2010). Furthermore, the bright CVs (pale solid red curve) in our models are more centrally concentrated than the faint CVs. Previous studies (e.g., Nelemans et al. 2016) have argued that nova eruptions prevent stable accretion and CV formation for low-mass WDs ($M \lesssim 0.7 M_{\odot}$), motivated in part by the fact that WDs observed in CVs generally have high mass (e.g., Zorotovic et al. 2011). Along these lines, we show as a dark red curve the distribution of bright CVs excluding the systems with WD masses $< 0.7 M_{\odot}$. As shown, in this case, the bright population matches much more closely the observed distribution of bright CVs (dashed red curve). Finally, note that of the roughly seven bright accreting WD–MS binaries found per model, roughly two on average feature a WD of mass $0.7 M_{\odot}$.

The agreement in our models with observations of overall numbers and radial distributions of CV candidates is satisfying. However, we emphasize that the physical processes relevant to CVs and their potential detectability are far more complex than

considered here. We reserve more detailed study of accreting WD–MS binaries for future work.

7.3. Effect of Primordial Binary Fraction

Here we explore how the results of this study may depend upon the primordial binary fraction in clusters. Stellar-mass BH binaries are expected to form primarily through dynamical processes regardless of the details assumed about the primordial binary population (e.g., Chatterjee et al. 2017). However, it is not immediately clear whether the primordial binary fraction may play a more prominent role in the WD case. We include an additional model (21 in Table 1) assuming a 50% primordial binary fraction. We summarize here the primary differences between this model and our fiducial primordial binary fraction of 5%.

Although the *total* number of WDs remains largely unchanged, the number of He WDs does change markedly with the binary fraction. This is unsurprising given that He WDs form exclusively through binary evolution processes (see Section 2). When the primordial binary fraction increases by a factor of 10 from 5% to 50%, the number of He WDs also increases by roughly a factor of 10 (see Table 1).

We find that the number of WD mergers does not change significantly with binary fraction (columns 10–12 of Table 1). Additionally, the total number of WD–MS collisions is largely unchanged; we identify 316 collisions in model 21 compared to an average of 263 for the models with 5% primordial binary fraction. This indicates that the rates of WD mergers and WD–MS collisions are dependent primarily on the high densities of WDs achieved in the centers of core-collapsed clusters.

We explore this point further in Figure 12. Here we plot versus time the total number of binaries of all types (top panel), the total number of BH–BH binaries (middle panel), and the total number of massive WD–WD binaries (bottom panel). We show the evolution for model 21 with $f_b = 50\%$ (black curves) and model 10 with $f_b = 5\%$ (blue curves). Note that all other cluster parameters, including the total cluster mass, are identical in these two models. We focus on massive WDs (in this plot, defined simply as the ONe WDs) to explore specifically the *dynamically active* WDs that dominate WD

Figure 12. Total number of binaries of all types (top panel), total number of BH–BH binaries (middle), and total number of massive WD binaries (here defined simply as ONe WDs; bottom panel) vs. time for model 21 (primordial binary fraction of 50%) and model 10 ($f_b = 5\%$). Populations that are dominated by dynamics (BHs at early times when a BH subsystem is present and WDs at late times when a WD subsystem forms) converge to the same binary fraction, independent of the assumed primordial binary fraction.

subsystems (see Figure 3). As shown, the overall number of binaries (the majority of which are low-mass binaries that live dynamically unperturbed in the cluster halo) remains markedly different throughout the full cluster evolution for these two

assumptions of primordial binary fraction. However, for populations shaped significantly by dynamics, the total number of binaries (and thus binary fraction) converges to a single value, independent of the assumed primordial binary fraction. Notably, we show this is relevant for BHs at early times ($t \lesssim 10$ Gyr), while a BH subsystem is present, and for massive WDs at late times ($t \gtrsim 10$ Gyr), once a dense WD subsystem has formed. We reserve a more detailed exploration of the dynamical processes that may explain these features for future work.

We do find that the numbers of accreting and detached WD–MS binaries are sensitive to the primordial binary fraction, since the majority of these systems are dynamically inactive low-mass binaries. In our $f_b = 50\%$ model, we find on average 1670 detached WD–MS binaries at late times and on average 162 accreting systems (117 and 45 of which fall into the faint and bright categories described in Section 7.2). Given that a large fraction of these binaries found in the models at late times are primordial, it is not surprising that a factor of 10 increase in primordial binary fraction yields a roughly factor of 10 increase in the late-time binary counts. As discussed in Belloni et al. (2019), only a few percent of accreting WD–MS binaries in a given cluster may in fact be observed as CVs when taking into account observational considerations. In this case, a relatively large primordial binary fraction may in fact be necessary to produce CV counts on a par with those observed in NGC 6397 (and in other clusters), as is pointed out by Belloni et al. Again, we reserve for future work a more detailed examination of the observable features of the CV candidates in our CMC models.

We show more detailed information on the total numbers of WD–WD and WD–MS binaries of various types found in each simulation in Tables 2 and 3 in the Appendix.

Table 2
WD–WD Binaries

(1)	MS + MS (2)	WD + WD (3)	He + CO (4)	He + ONe (5)	CO + CO (6)	CO + ONe (7)	ONe + ONe (8)
1	11,429.41 (66.18)	166.91 (31.32)	51.77 (2.09)	1.95 (0.86)	58.45 (12.82)	22.32 (11.73)	5.55 (3.59)
2	12,574.53 (57.29)	190.41 (28.29)	66.06 (3.53)	0.18 (0.0)	77.53 (11.82)	20.24 (8.65)	5.65 (3.65)
3	12,053.24 (60.35)	154.12 (31.76)	58.47 (3.76)	2.24 (0.71)	60.76 (15.71)	14.29 (8.0)	6.47 (3.47)
4	12,086.5 (66.2)	143.3 (27.4)	54.9 (5.0)	1.25 (0.6)	52.3 (12.2)	16.55 (7.8)	3.55 (1.8)
5	10,731.55 (55.38)	174.12 (23.89)	58.28 (2.71)	0.0 (0.0)	65.68 (11.4)	21.29 (7.32)	4.83 (2.09)
6	12,945.31 (38.92)	225.0 (23.38)	71.08 (2.08)	0.92 (0.08)	100.23 (11.31)	27.38 (7.77)	3.92 (1.85)
7	11,808.33 (73.1)	158.33 (28.43)	63.38 (5.43)	2.0 (0.43)	44.0 (9.29)	15.43 (8.43)	6.48 (4.14)
8	12,013.2 (69.3)	125.8 (24.65)	60.1 (4.6)	1.85 (0.75)	34.95 (9.9)	12.6 (6.0)	4.45 (2.8)
9	11,378.28 (60.38)	192.26 (27.51)	69.96 (3.64)	1.0 (0.34)	78.47 (13.83)	17.09 (6.4)	5.57 (3.02)
10	11,917.93 (62.43)	149.75 (25.75)	65.04 (4.71)	1.93 (0.21)	46.43 (11.29)	13.32 (6.64)	4.36 (2.68)
11	12,704.06 (37.18)	217.41 (20.29)	73.0 (2.06)	0.94 (0.35)	95.82 (9.0)	26.12 (6.29)	5.12 (2.35)
12	12,455.19 (44.08)	228.7 (21.16)	70.51 (2.43)	2.76 (0.27)	97.57 (10.27)	23.95 (6.32)	4.62 (1.7)
13	12,484.5 (51.67)	201.78 (25.94)	76.89 (4.0)	1.72 (0.11)	68.94 (9.94)	26.5 (9.11)	6.89 (2.56)
14	13,415.45 (59.7)	201.35 (28.6)	67.55 (3.75)	1.35 (0.2)	83.95 (14.1)	24.25 (7.45)	5.25 (2.9)
15	12,253.53 (68.47)	169.0 (32.76)	67.29 (4.18)	0.53 (0.12)	54.0 (12.94)	23.65 (11.35)	6.29 (3.88)
16	12,832.91 (61.45)	175.36 (29.5)	72.32 (4.73)	2.36 (0.5)	53.5 (12.5)	16.05 (8.77)	5.77 (2.41)
17	12,041.12 (61.59)	177.76 (28.29)	64.12 (3.71)	1.47 (0.76)	57.76 (11.53)	21.76 (9.65)	4.88 (2.35)
18	13,267.29 (37.48)	225.38 (16.81)	79.76 (2.38)	2.24 (0.14)	98.43 (7.57)	23.52 (5.29)	6.48 (1.33)
19	14,590.73 (0.45)	45.45 (0.0)	5.73 (0.0)	0.0 (0.0)	9.36 (0.0)	2.36 (0.0)	0.0 (0.0)
20	14,783.0 (0.07)	130.87 (0.0)	15.87 (0.0)	0.0 (0.0)	41.27 (0.0)	1.0 (0.0)	0.0 (0.0)
21	82,915.06 (131.18)	1018.0 (33.12)	395.76 (4.76)	7.71 (0.82)	422.24 (21.53)	18.24 (3.65)	3.12 (1.18)

Note.—Average number of WD–WD binaries of various types found in late-time ($t > 10$ Gyr) snapshots for all models. The numbers in parentheses show average number of binaries within 0.1 pc (i.e., within the WD subsystem).

Table 3
WD–MS Binaries

(1)	WD + MS Binaries			Accreting WD + MS		
	He + MS (2)	CO + MS (3)	ONe + MS (4)	All (5)	Faint (6)	Bright (7)
1	170.77 (3.36)	76.55 (12.95)	14.05 (6.59)	18.82 (1.64)	12.36 (0.0)	6.45 (1.64)
2	209.71 (4.82)	91.94 (15.47)	12.35 (3.59)	19.59 (1.59)	11.71 (0.06)	7.88 (1.53)
3	199.59 (4.59)	75.06 (12.41)	13.41 (5.24)	18.41 (0.65)	14.82 (0.12)	3.59 (0.53)
4	191.75 (4.95)	91.2 (15.6)	12.3 (4.4)	24.55 (1.5)	19.1 (0.15)	5.45 (1.35)
5	192.15 (3.66)	95.75 (11.57)	16.66 (4.11)	27.23 (1.28)	17.05 (0.11)	10.18 (1.17)
6	240.92 (1.77)	111.38 (10.08)	12.69 (3.54)	30.92 (0.23)	22.85 (0.15)	8.08 (0.08)
7	145.43 (3.43)	78.9 (15.1)	13.67 (6.0)	16.38 (0.86)	14.1 (0.38)	2.29 (0.48)
8	133.75 (3.55)	71.65 (11.9)	17.4 (7.0)	17.85 (1.55)	11.0 (0.1)	6.85 (1.45)
9	154.81 (2.85)	118.68 (13.55)	15.53 (5.34)	19.68 (0.62)	15.77 (0.13)	3.91 (0.49)
10	132.89 (3.11)	72.93 (12.46)	15.82 (6.36)	15.96 (1.07)	10.61 (0.07)	5.36 (1.0)
11	198.82 (2.24)	100.0 (9.12)	14.76 (3.82)	16.53 (0.06)	12.59 (0.0)	3.94 (0.06)
12	181.3 (2.92)	111.68 (9.08)	20.46 (3.7)	19.7 (0.84)	11.81 (0.08)	7.89 (0.76)
13	225.33 (3.61)	98.11 (12.5)	18.83 (5.5)	33.06 (1.33)	22.72 (0.44)	10.33 (0.89)
14	260.45 (4.95)	110.9 (11.8)	17.15 (5.1)	31.2 (1.2)	21.5 (0.1)	9.7 (1.1)
15	232.06 (3.88)	89.88 (13.53)	14.76 (5.65)	31.18 (0.82)	21.35 (0.24)	9.82 (0.59)
16	233.32 (5.05)	102.45 (15.64)	12.59 (4.0)	32.0 (2.23)	22.14 (0.45)	9.86 (1.77)
17	237.0 (5.59)	102.94 (14.76)	14.47 (4.94)	33.82 (1.06)	25.53 (0.06)	8.29 (1.0)
18	255.71 (2.38)	110.9 (6.9)	19.57 (3.52)	37.52 (0.62)	27.38 (0.05)	10.14 (0.57)
19	303.0 (0.0)	92.73 (0.0)	3.82 (0.0)	52.09 (0.0)	27.18 (0.0)	24.91 (0.0)
20	647.93 (0.07)	164.33 (0.0)	4.0 (0.0)	68.07 (0.0)	47.87 (0.0)	20.2 (0.0)
21	1450.35 (8.29)	413.29 (16.94)	36.24 (6.82)	174.88 (2.47)	128.76 (0.53)	46.12 (1.94)

Note.—Average number of WD–MS binaries of various types found in late-time ($t > 10$ Gyr) snapshots for all models. The numbers in parentheses show average number of binaries within 0.1 pc.

7.4. Future Work

Weatherford et al. (2018, 2020) showed that mass segregation measurements constrain the total number and total mass of BH subsystems in globular clusters. This result arises directly from the connection between BH populations and the overall cluster dynamics. As we have shown here (specifically see Figure 5), WD subsystems are also tracers of cluster dynamics, so mass segregation measurements may similarly be used to predict WD subsystems in GCs. Specifically, we expect clusters exhibiting more mass segregation (parameterized with the metric Δ in Weatherford et al. 2020) to feature relatively dense central WD populations. In Weatherford et al. (2020), we predicted details of BH subsystems in roughly 50 GCs observed in the ACS Survey. A future study may place similar constraints upon WD subsystems in these specific clusters or others. While we have focused here on rates of WD mergers and other transients in NGC 6397 as a representative example of a core-collapsed cluster, detailed predictions of WD populations in core-collapsed clusters more broadly would enable more precise estimates of the rates predicted here. Of course, a larger set of cluster models spanning a broader range in cluster masses and other properties would be ideal for such a study.

We considered here direct collisions between WDs (i.e., $r_p < R_1 + R_2$). However, more distant close encounters in the tidal disruption or tidal capture regime may also lead ultimately to a WD merger. The minimum pericenter distance for a pair of WDs to be tidally captured may be a few to 10 times larger than the physical WD radius (e.g., Samsing et al. 2017). Thus, if tidal capture were included (for both single–single and binary-mediated encounters), the WD merger rate estimated in Section 4.2 may increase to roughly $\mathcal{O}(100)$ Gpc $^{-1}$ yr $^{-1}$. The

inclusion of tidal capture may similarly increase the rates of WD–MS collisions described in Section 6. Of course, the tidal capture process is highly uncertain and depends on physics beyond the scope of the current version of CMC. We reserve study of this possibility for future work.

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Appendix

In Table 2, we show the average number of WD–WD binaries of various types found in all late-time cluster ($t > 10$ Gyr) snapshots for all simulations. In parentheses, we show the average number of each binary type found within the innermost 0.1 pc (see Figure 3). Table 3 shows the average number of WD–MS binaries of various types for each simulation, again limited only to late-time snapshots. Columns 2–4 show average binary counts for detached and accreting systems combined, while columns 5–7 show specifically the counts for accreting systems (as discussed in Section 7.2).

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