Linear bias and halo occupation distribution of emission-line galaxies from *Nancy Grace Roman Space Telescope*

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ABSTRACT

We present measurements of the linear galaxy bias of $H\alpha$ and [O III] emission-line galaxies (ELGs) for the High Latitude Spectroscopic Survey (HLSS) of *Nancy Grace Roman Space Telescope* (or *Roman*), using galaxy mocks constructed using semi-analytical model for galaxy formation, *Galacticus*, with a large cosmic volume and redshift coverage. We compute the two-point statistics of galaxies in configuration space and measure linear bias within scales of $10\text{--}50 h^{-1}$ Mpc. We adopt different selection algorithms to investigate the impact of the *Roman* line flux cut, as well as the effect of dust model used to calibrate *Galacticus*, on the bias measurements. We consider galaxies with $H\alpha$ and [O III] emissions over the redshift range $1 < z < 3$, as specified by the current baseline for the *Roman* HLSS. We find that the linear bias for the $H\alpha$ and [O III] ELGs can be expressed as a linear function with respect to redshift: $b \simeq 0.9z + 0.5$ for $H\alpha$ ($1 < z < 2$), and $b \simeq z + 0.5$ for [O III] ($2 < z < 3$). We have also measured the halo occupation distributions of these $H\alpha$ and [O III] ELGs to understand their distribution within dark matter haloes. Our results provide key input to enable the reliable forecast of dark energy and cosmology constraints from *Roman*.

Key words: methods: numerical – methods: statistical – galaxies: formation – large-scale structure of Universe.

1 INTRODUCTION

As biased tracers of the underlying dark matter distribution, galaxies form primarily in the peaks of the matter density field. Therefore they are not uniformly distributed in the universe. At large scales, the distribution of galaxies reveals a coherent structure in the background of a cosmic web and this large-scale structure depends on the fundamental cosmological parameters and the physics governing the formation and evolution of galaxies. The connection of the distribution between galaxies and dark matter can be described by galaxy bias, b , which can be obtained by comparing the clustering amplitudes of galaxies in the mock galaxy catalogue and the dark matter simulation for a given cosmological model (Coil 2013). The proper modelling of galaxy bias is critical in facilitating the use of galaxy clustering as a cosmological probe.

Galaxy clustering data have been used to advance our understanding of both cosmology and galaxy formation. Retrieval of the information on large scales has been extensively studied with the linear perturbation theory of cosmic density field. The use of galaxy catalogues from spectroscopic redshift surveys has enabled the observations of large-scale structure, which provides measurements for cosmic distance scales through the baryon acoustic oscillation (BAO), and the linear growth rate through the redshift-space distortion (RSD) effect over a wide redshift range (see e.g. Cole et al. 2005; Eisenstein et al. 2005; Beutler et al. 2011, 2012; Delubac et al. 2015;

Ross et al. 2015; Ata et al. 2018; Bautista et al. 2018, and references therein). These measurements have been used to put constraints on the fundamental cosmological parameters. However, due to the lack of statistical precision and systematic accuracy, alternative theories to explain the cosmic acceleration, also known as dark energy, are not conclusively ruled out. The minimal extension to the standard model, the Λ cold dark model (Λ CDM) cosmology, is allowed by the current observational data. In order to distinguish competing theories and constrain the parameter space, future galaxy surveys are required to probe cosmic large-scale structure over wider redshift ranges and larger cosmic volumes (Wang 2008a,b).

For future galaxy surveys like *Euclid* (Laureijs et al. 2011, 2012) and NASA's *Nancy Grace Roman Space Telescope* (hereafter *Roman*; Dressler et al. 2012; Green et al. 2012; Spergel et al. 2015), galaxy clustering will be one of the main cosmological probes used to measure the properties of dark energy and constrain possible deviations of gravity from general relativity. *Roman* will mainly target $H\alpha$ and [O III] emission-line galaxies (ELGs) within redshift $1.0 < z < 3.0$, complementary to *Euclid* by design. To maximize the science return of space missions, it is necessary to optimize survey strategies. In Merson et al. (2018) and Zhai et al. (2019), we calibrated and applied a semi-analytical model (SAM) of galaxy formation, *Galacticus* (Benson 2012), to N -body simulation to produce a realistic synthetic galaxy catalogue and estimate the number densities of $H\alpha$ and [O III] emitters. Using the same SAM, we have produced an $H\alpha$ galaxy mock catalogue for the *Roman* High Latitude Spectroscopic Survey (HLSS; Zhai et al. 2021), to facilitate the development of analysis tools for *Roman* BAO/RSD science. We

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measured the clustering signal and adopted a theoretical template for galaxy power spectrum to investigate the significance of the BAO and RSD measurements. This simulated catalogue also enables an estimate of the galaxy bias. This is crucial for future surveys like *Roman* in evaluating whether we can infer the properties of dark matter correctly, and forecast the power of the survey to constrain dark energy. Merson et al. (2019) combined the SAM and halo occupation distribution (HOD) approach to produce an $H\alpha$ galaxy catalogue and predict the linear bias as a function of redshift for both *Roman* and *Euclid*. In this work, we carry out a more precise analysis by using the simulated galaxy catalogue from SAM only, to forecast the linear bias of both $H\alpha$ and [O III] ELGs and their HODs, over the entire redshift range of $1 < z < 3$ for the *Roman* HLSS. Our results can also be used for additional tests for the underlying SAM.

The bias relation between the distribution of galaxies and underlying matter has been extensively studied in literature. *Euclid* and *Roman* will be the first cosmological surveys targeting $H\alpha$ and [O III] ELGs. The detailed analysis of the $H\alpha$ and [O III] ELGs using either numerical or semi-analytical method can inform both cosmological and galaxy evolution studies. Nusser, Yepes & Branchini (2020) adopt various SAMs and empirical model for galaxy formation to investigate the biasing relation for a *Euclid*-like survey. The bias measurement at linear scale reveals a constant function of star formation rate (SFR) for star-forming galaxies. By utilizing the luminosity variation and peculiar velocity field from the galaxy distribution in redshift space, the ELGs could provide a measurement of the linear growth rate without being biased by the environmental effects (Nusser et al. 2020).

Compared with the massive galaxies at low redshifts that have been used for large-scale structure analysis from surveys like the Sloan Digital Sky Survey (SDSS), *Euclid* and *Roman* target ELGs at higher redshifts with different selection methods. It is important to investigate the connection of these ELGs and their host dark matter haloes (Wechsler & Tinker 2018). Using the observational data from the extended Baryon Oscillation Spectroscopic Survey (eBOSS) ELG program and mock catalogues, Avila et al. (2020) studied a series of models for HOD of the ELGs and investigated the impact on the clustering measurement. Using similar observational data, Guo et al. (2019) measured the occupancy of the star-forming galaxies and the evolution as a function of stellar mass within redshift range $0.7 < z < 1.2$. Although the eBOSS ELGs have different redshift distribution and selection algorithm than *Roman* and *Euclid*, their implications for the galaxy properties can provide reference information for the future surveys. On the other hand, near-infrared narrow-band surveys have been used to identify ELGs similar to the targets of *Euclid* and *Roman*. Based on the galaxy sample from High-Redshift Emission Line Survey (HiZELS), Sobral et al. (2013) measure luminosity function (LF) of $H\alpha$ galaxies from $z = 0.84$ to $z = 2.23$. Khostovan et al. (2015) measure the same statistics for $H\beta + [\text{O III}]$ and [O II] galaxies at redshifts up to 5. Combined with spectroscopic follow-ups, Sobral et al. (2015) report the LF measurement of $H\beta + [\text{O III}]$ and [O II] with an extended sky coverage of $\sim 10 \text{ deg}^2$. The compilation of these ELG data also enables a clustering analysis. Sobral et al. (2010) measure the clustering properties of $H\alpha$ galaxies at $z = 0.84$. Cochrane et al. (2017) and Cochrane & Best (2018) measure the clustering signals of $H\alpha$ galaxies at redshift up to 2.2 and investigate the dependence on luminosity, stellar mass, and SFR. A HOD method is also used to identify the typical halo mass of these $H\alpha$ emitters. Khostovan et al. (2018) measure the clustering of $H\beta + [\text{O III}]$ and [O II] galaxies within redshift range $0.8 < z < 4.7$ and study their evolution with redshift, line luminosity, and stellar mass. In addition, Khostovan

et al. (2019) investigate the clustering properties of galaxies selected by Ly α emission over redshift range $2.5 < z < 6$ and present the redshift evolution of the correlation length. Because of the limited sky coverage and the nature of narrow-band surveys, the clustering analysis is restricted to small scales and only angular correlation function is feasible. A simulated galaxy mock can provide equivalent measurements for further comparisons, but needs additional selection on the galaxies and examination of the galaxy model, thus beyond the scope of this paper that focuses on galaxy linear bias on scales above $10 h^{-1} \text{ Mpc}$. We will investigate such comparisons in future work. For other investigations of the connection between ELGs and dark matter haloes, see e.g. Hadzhiyska et al. (2021), Jimenez et al. (2020), and references therein. The connection of the *Roman* ELGs with the host dark matter haloes is not only useful for cosmology and galaxy science, the modelling of their HODs can provide a convenient way to populate galaxies within a dark matter simulation while preserving the clustering properties. This enables the production of many mock galaxy catalogues in a fast and practical manner, required for constructing the covariance matrix for the likelihood analysis (Norberg et al. 2009), and has been widely used in the literature (White et al. 2011; Zehavi et al. 2011; Manera et al. 2013; Zhai et al. 2017). The detailed investigation for the *Roman* galaxy redshift survey, presented in this work, is able to provide more details of how the dark matter haloes are populated by galaxies with different star formation history and emission lines.

The SAM calibrated and used in our work has enabled the estimate of the number density of ELGs as a function of redshift (Zhai et al. 2019). Along with the linear bias measurement in the current analysis, they provide the crucial input information to forecast the wide range of possible dark energy and cosmological science from *Roman* galaxy redshift survey, e.g. using the Fisher matrix approach (Tegmark 1997). This can serve as a convenient method to predict the constraining power on the properties of dark energy, for instance a figure-of-merit analysis (Wang 2008a). In addition, our results are useful in investigating the extra constraining power from galaxy bispectrum (Yankelevich & Porciani 2019), the constraint on neutrino masses (Hamann, Hannestad & Wong 2012), and so on.

Our paper is organized as follows. In Section 2, we introduce the galaxy mock catalogue for the *Roman* galaxy redshift survey and the selection algorithm of the sample. Section 3 presents the bias measurements from galaxy clustering, and the HOD of galaxies within the *Roman* redshift range. Finally, we discuss and conclude in Section 4.

2 METHODOLOGY

In this section, we describe the construction of the simulated *Roman* catalogues of ELGs, and the sample selection for the *Roman* galaxy redshift survey.

2.1 Galaxy formation model

The synthetic galaxy catalogue used in this paper has been constructed using the Galacticus galaxy formation model (Benson 2012). Similar to the other SAMs, Galacticus parametrizes the astrophysical processes and performs the evolution of galaxy populations within a distribution of dark matter haloes and their merger trees. The processes governing galaxy formation and evolution include gas cooling, star formation, feedback from supernovae, black hole formation, and so on. By parametrizing these processes as ordinary differential equations (ODE) and calling the ODE solver, Galacticus can perform a simulation of galaxies within a sufficiently large

volume in a timely manner and output details for the galaxy populations, including the star formation history, galaxy morphology, spectral energy distribution (SED), photometric luminosities for a set of filter transmission curves, and emission-line luminosities.

Before using Galacticus to produce the galaxy catalogue, we need to determine the free parameters in the model due to the poor prior knowledge of the astrophysical processes. This can be non-trivial since the typical number of free parameters is 15 or more (Wechsler & Tinker 2018). In our work, we do not limit ourselves to local galaxies to calibrate the model, but compare the model prediction with galaxy populations at higher redshifts relevant to *Roman*. The parameters of this model have been calibrated in Zhai et al. (2019), including the parameters for the physics of galaxy formation and the dust-attenuation model. In particular, the dust model is calibrated to produce consistent prediction of $H\alpha$ LF compared with observations from the ground-based narrow-band HiZELS (Geach et al. 2008; Sobral et al. 2009, 2013), or the number counts data collected from Wide Field Camera 3 (WFC3) Infrared Spectroscopic Parallels (WISP) survey (Atek et al. 2010, 2011; Mehta et al. 2015). The dust model applied is the Calzetti et al. (2000) model with parameter A_V to describe the strength of dust attenuation. The result is $A_V = 1.7$ for calibration based on WISP, and $A_V = 1.9$ for HiZELS. Note that higher value of A_V means stronger dust attenuation, thus the HiZELS-based calibration results a lower number density of the galaxy sample compared with the WISP-based calibration, with a preference of selecting brighter galaxies. In this paper, we present the bias measurement for ELGs with both dust models and investigate the impact on the large-scale structure analysis.

The galaxy population in this analysis is selected by the emission-line luminosity. Galacticus can output the number of ionizing photons for various species (H I, He I, and [O II]), the metallicity of the interstellar medium (ISM), the hydrogen gas density, and the volume filling factor of H II regions. We use these parameters to interpolate the tabulated libraries from the CLOUDY photoionization code (Ferland et al. 2013) and compute the emission-line luminosity for each galaxy. More details of the method can be found in Merson et al. (2018).

2.2 *N*-body simulation

The key ingredient for SAMs-like Galacticus is the set of merger trees of dark matter haloes, which can be approximately constructed using the Press–Schechter formalism (Press & Schechter 1974), or come from a cosmological *N*-body simulation. Here we have chosen the later for high fidelity, and use the merger trees extracted from the UNIT simulation¹ (Chuang et al. 2019) that assumes a spatially flat Λ CDM model with parameters consistent with *Planck* 2016 measurement (Planck Collaboration XIII 2016). The simulation contains 4096^3 particles with a box-size of $1 h^{-1}$ Gpc. This simulation has a mass resolution of $10^9 h^{-1} M_\odot$ with data product covering redshift range of $0 < z < 99$. The large volume and high resolution make this simulation sufficient for the next generation galaxy surveys, including the Dark Energy Spectroscopic Instrument (DESI), and those planned for *Roman* and *Euclid*. We refer the readers to Chuang et al. (2019) for more details of the UNIT simulation and its data products. The merger trees of the dark matter haloes are constructed using the CONSISTENT TREES software (Behroozi et al. 2013) and the final product contains more than 160 million merger trees. Applying Galacticus to this simulation allows us to build a light-cone catalogue

of galaxies. In particular, we use the method from Kitzbichler & White (2007) to determine where the dark matter haloes enter the light-cone of the observer. The resulting catalogue has an area of $\sim 2000 \text{ deg}^2$, consistent with the current baseline design of *Roman* HLSS.

2.3 Luminosity function of $H\alpha$ and [O III] emission lines

In the top row of Fig. 1, we present the luminosity function (LF) of $H\alpha$ and [O III] ELGs at $1 < z < 3$, with both dust free and dust attenuated results. The evolution with redshift indicates the star formation history of the galaxies. In order to validate the simulation, we compare the LF of $H\alpha$ and [O III] emission lines with current observations at selected redshifts. The middle row shows the LF of $H\alpha$ galaxies compared with HiZELS measurements, which was used to calibrate the SAM model. In particular, the dust model with $A_V = 1.9$ is chosen to match the LF at $z = 1.47$ from HiZELS. Our model underestimates the LF at higher redshift, indicating either the need for improvement in the Galacticus model, or that a redshift-dependent dust model is required. The bottom panel shows the comparison of [O III] ELGs with WISP measurements from Colbert et al. (2013) and the HiZELS result from Khostovan et al. (2015). Our model shows mild deviation compared with WISP and HiZELS measurements, however the amplitude is roughly consistent. Note that the measurement from Khostovan et al. (2015) is for $H\beta + [\text{O III}]$ due to resolution limit, and the overall measurement is dominated by $H\beta$ at the faint end and [O III] at the bright end. Taking this into account would make our model more consistent with observations. The performance of our model can be further improved by calibrating the SAM with more observational data sets.

In addition to the dust model calibrated directly to match the observed LF as in this work, Garn & Best (2010) propose a dust extinction model based on stellar mass. They have shown that while their model is calibrated on SDSS galaxies in the local universe, it is applicable at higher redshifts, and also at other wavelengths when combined with the Calzetti extinction law. We apply the Garn & Best (2010) dust model in our galaxy simulation and present the resultant $H\alpha$ LF in the middle panels of Fig. 1. The overall dust extinction from this stellar-mass-based model is lower than our dust model, thus brings the prediction closer to observation at $z = 2.23$ but deviate more at $z = 1.47$. This can increase the number density of ELGs that *Roman* can observe, and lower slightly the clustering amplitude and linear bias as Section 3 shows. We refer the reader to Merson et al. (2018), in which the effect of different dust models on the ELG number density is extensively studied.

2.4 Sample selection for the *Roman* galaxy redshift survey

In this paper, we focus on the forecast of galaxy linear bias for *Roman* HLSS, but the results can also be applicable to surveys like the one planned for *Euclid*. The observing strategies can impact the galaxy selection and thus linear bias measurements. *Roman* grism has a wavelength range of $1.0\text{--}1.93 \mu\text{m}$, which determines the redshift range for the emission lines of interest, as shown in Fig. 2, which includes the three primary lines $H\alpha$, [O II], and [O III]. We also show the [N II] and $H\beta$ lines as they are the main contaminants to $H\alpha$ and [O III], respectively, due to the closeness of the emission-line wavelength. Since the current Galacticus SAM model significantly underestimates the strength of [O II] emission, we will only consider $H\alpha$ and [O III] lines throughout this paper, as they define the expected *Roman* galaxy samples.

¹<https://unitsims.ft.uam.es>

Figure 1. Top: the prediction of the luminosity function (LF) for H α (left) and [OIII] (right) emission-line galaxies (ELGs) for different redshifts and dust models. The dust-free model ($A_V = 0$) shows the intrinsic distribution, while $A_V = 1.7$ and 1.9 shows two dust models to match WISP number counts and HiZELS H α LF measurements, respectively. Middle: the comparison of the H α LF with HiZELS at two high redshifts. The dust model with $A_V = 1.9$ can match the observation at $z = 1.47$ perfectly since this measurement is used in the calibration of GalactiCus. The prediction using a different dust extinction model, based on stellar mass from Garn & Best (2010), is also shown for comparison (green dashed). Bottom: the LF prediction of [OIII] ELGs compared with observational data from Colbert et al. (2013) and Khostovan et al. (2015). Note that these measurements are not used in the calibration, but they are roughly consistent with our model predictions.

Figure 2. The redshift coverage of the main emission lines of *Roman* HLSS and their main contaminant, determined by the wavelength range of *Roman* grism that is 1–1.93 μm .

One of the key characteristics of a survey is its depth, or sensitivity, i.e. the emission-line flux limit for an ELG survey. We consider three different line flux limits in our analysis: $0.5 \times 10^{-17} \text{ erg s}^{-1} \text{ cm}^{-2}$ as a reference case, $1.0 \times 10^{-16} \text{ erg s}^{-1} \text{ cm}^{-2}$ as the 6.5σ nominal depth for *Roman* HLSS, and $2.0 \times 10^{-16} \text{ erg s}^{-1} \text{ cm}^{-2}$ as the 3.5σ depth of a *Euclid*-like galaxy redshift survey. The faint limit of $0.5 \times 10^{-17} \text{ erg s}^{-1} \text{ cm}^{-2}$ is included to facilitate a depth versus area optimization study of the *Roman* HLSS. As the primary target, $\text{H}\alpha$ emission line is detectable at $z < 2.0$. Therefore we split the analysis into two subsamples with $z > 2.0$ and $z < 2.0$. In addition to a line flux cut, *Roman* and *Euclid* will apply a cut on equivalent width (EW) of the emission lines to further select bright galaxies. Although EW is correlated with line luminosity, the EW cut is necessary to improve the sample selection. The effect of EW cut on the galaxy distribution and properties will be presented in a separate paper.

At $z < 2.0$, *Roman* science requirements specify that at least two emission lines are used in measuring a redshift, with the strong line above the line flux limit. The detection of the second line may not require its strength to be above the line flux limit at 6.5σ , thus we allow for different thresholds for the second emission line. At $z > 2.0$, we only consider the [O III] line, required to be observed above the flux limit at 6.5σ , since we are not including [O II] in this study due to the current limits of Galacticus. The impact of the line flux threshold of the [O II] line will be studied in future work.

For the galaxies with $z < 2.0$, we first compute the emission-line flux for $\text{H}\alpha$ and [O III], then we set the flux limits by two variables. The first is $f_{\text{lim},1}$, this is the lower limit of the stronger line (either $\text{H}\alpha$ or [O III]), as chosen above. The second is $f_{\text{lim},2\text{R}}$ that sets the lower limit of the weak line in units of $f_{\text{lim},1}$, therefore $f_{\text{lim},2\text{R}}$ is dimensionless. We choose three values and investigate the impact on the large-scale structure analysis: $f_{\text{lim},2\text{R}} = 0.25, 0.5$, and 1.0 . For instance when $f_{\text{lim},1} = 1.0 \times 10^{-16} \text{ erg s}^{-1} \text{ cm}^{-2}$ and $f_{\text{lim},2\text{R}} = 0.5$, we select galaxies with the strongest emission line brighter than $f_{\text{lim},1}$, and the second emission line brighter than $f_{\text{lim},1} * f_{\text{lim},2\text{R}} = 0.5 \times 10^{-16} \text{ erg s}^{-1} \text{ cm}^{-2}$. At $z > 2.0$, we just apply $f_{\text{lim},1}$ to select [O III] emitting galaxies.

In Fig. 3, we show the number densities of the selected galaxies with different flux limits. The curves of the same colour merge at $z \sim 2$ due to the selection algorithm since there is only one flux cut on [O III]. The result shows a monotonic decrease as redshift increases. The flux limit parameter $f_{\text{lim},2\text{R}}$ for the second emission line has

weaker impact than $f_{\text{lim},1}$, but can be important when brighter flux cut and stronger dust attenuation are assumed.

For galaxies with $z < 2.0$, both $\text{H}\alpha$ and [O III] lines can be observed, and their relative strength may not be a constant. In Fig. 4, we plot the fraction of galaxies with $\text{H}\alpha$ as the stronger line, as a function of redshift. The left-hand and middle panels show that as we go to higher redshifts, the $\text{H}\alpha$ dominance decreases with redshift regardless of the dust model, for sufficiently faint $\text{H}\alpha$ line flux cut. The right-hand panel shows that this is not true for brighter $\text{H}\alpha$ line flux cut, for which the $\text{H}\alpha$ dominance flattens at higher redshifts. This indicates that there are more bright $\text{H}\alpha$ emitters than bright [O III] emitters at high redshifts. In addition, Fig. 4 shows the significant impact of the dust model. The intrinsic result (dust free with $A_V = 0$) shows that the $\text{H}\alpha$ dominance is around 30–70 per cent in this redshift range. However, when dust model is applied, almost all galaxies have stronger $\text{H}\alpha$ than [O III] emission (> 80 per cent), indicating that the [O III] emission line experiences more dust attenuation as predicted by the Calzetti model. Since the $\text{H}\alpha$ emission is only present at $z < 2$, we will refer to $\text{H}\alpha$ galaxies and galaxies at $z < 2$ interchangeably in the following section, and similarly [O III] galaxies refer to galaxies with $z > 2$.

Because galaxies have peculiar velocities, the observed redshift is different from the cosmological redshift due to cosmic expansion. This RSD effect can change the measured galaxy distribution and the resultant clustering signal. In our simulation, we add this effect into the galaxy catalogue by perturbing the cosmological redshift with $v_p/(ac)$, where v_p is the line-of-sight component of the velocity, a is the scale factor, and c is the speed of light. We will present clustering measurements in both real and redshift space in the following sections.

3 RESULTS

3.1 Galaxy clustering of $\text{H}\alpha$ galaxies

Galaxies do not perfectly trace the underlying matter distribution. They preferentially live in the peaks of the matter density field. This makes the galaxies biased tracers of large-scale structure, which preferentially sample the overdense regions (Kaiser 1984; Bardeen et al. 1986). In addition, the processes of galaxy formation can introduce additional deviations of the galaxy distribution from matter distribution. These factors result a relationship between the spatial distribution of galaxies and the dark matter density field: the galaxy bias. Neglecting the stochasticity and non-locality, the galaxy density contrast can be written as a function of the underlying dark matter density contrast on some scale (Coil 2013) $\delta_g = f(\delta_m)$, where $\delta \equiv \rho/\bar{\rho} - 1$ and $\bar{\rho}$ is the mean density.

On large scales (also known as linear scales), where the density fluctuations are small and evolve linearly, we can expand the function f and define the linear galaxy bias through $\delta_g = b\delta_m$. In terms of the two-point correlation function, we can measure the galaxy bias by comparing the clustering amplitudes of galaxies and matter,

$$\xi_{\text{gg}}(r) = b^2(r) \xi_{\text{mm}}(r), \quad (1)$$

where ξ_{gg} and ξ_{mm} are galaxy and matter correlation function as a function of spatial separation, respectively.

With the simulated galaxy catalogue from Galacticus, we compute the galaxy correlation function using the Landy & Szalay (1993) estimator,

$$\xi_r = \frac{\text{DD} - 2\text{DR} + \text{RR}}{\text{RR}}, \quad (2)$$

Figure 3. The galaxy number density as a function of redshift, for different dust models and flux cuts. The curves of the same colour merge at $z \sim 2$ since there is only one flux cut for galaxies $z > 2$. Three panels correspond to three values of $f_{\text{lim},1}$, the flux limit of the strongest emission lines, the colours stand for different dust attenuation and the different line types denote the various values of $f_{\text{lim},2R}$.

Figure 4. The fraction of galaxies with $H\alpha$ as the strongest emission line, with dependence on dust model and flux cuts. This result is only for samples with $z < 2.0$ since no $H\alpha$ emission is expected at higher redshift due to the grism wavelength coverage. Three panels correspond to three values of $f_{\text{lim},1}$, colours and line types have the same format as in Fig. 3.

where DD, DR, and RR are suitably normalized numbers of (weighted) data–data, data–random, and random–random pairs in each galaxy separation bin. The random catalogues are first generated with uniform distribution on a sphere and then truncated to have the same right ascension and declination boundary as the galaxy catalogue. The redshifts of the random catalogue are randomly drawn from the galaxy catalogue to have the same radial distribution. The total number of randoms is 10 times larger than galaxy catalogue to assure stable measurement of clustering. Following the same strategy as Merson et al. (2019), we measure the correlation function for each galaxy sample five times with different random catalogues. We measure the correlation function at spatial scales up to $150 \text{ Mpc } h^{-1}$. In Fig. 5, we present the clustering measurement at a few redshift bins for galaxies with $1 < z < 2$ for both real and redshift space. We find that given our sample selection and dust model, the BAO peak can be recovered successfully. The worst case corresponds to high-redshift galaxies with the brightest flux cut for the emission lines, which results in a low galaxy number density and thus the clustering signal is impacted by noise significantly. The attenuation from two dust models gives similar impacts on the clustering amplitude, although their predictions for the number densities of ELGs are different (Zhai et al. 2019). The clustering amplitude in redshift space is higher than real

space, consistent with expectation of the enhancement due to RSD effect.

3.2 Linear bias of $H\alpha$ galaxies

In order to measure the linear bias, we compute the non-linear correlation function of dark matter ξ_{nm} using the CLASS and HALOFIT functionality in the code NBODYKIT (Hand et al. 2018) with Planck 2016 cosmology, to be consistent with the dark matter simulation used in our SAM simulation. The result is shown as the cyan curve in each panel of Fig. 5. The galaxy bias is computed by taking the ratio between the correlation functions of galaxies and dark matter. The lower row of each panel shows the resultant b^2 . Same as for the galaxy correlation function, the bias is also obtained by using the mean of five repeat measurements. The error bars are omitted to clearly present the result.

The figure shows that the bias is close to a constant at scales from 10 to 50 or $60 \text{ } h^{-1} \text{ Mpc}$. At scales below $10 \text{ } h^{-1} \text{ Mpc}$, the non-linearity of the dark matter dynamics comes into play and can induce scale-dependent bias. On the other hand, at scales above 50 or $60 \text{ } h^{-1} \text{ Mpc}$, the galaxy bias deviates from a constant value and presents complicated behaviour, especially around the BAO scale. This feature is

Figure 5. The measurement of galaxy correlation function and bias for a few redshift slices, as indicated in each figure. The left-hand column shows galaxies selected with $f_{\text{lim},1} = 1.0 \times 10^{-16} \text{ erg s}^{-1} \text{ cm}^{-2}$, and the line colours and styles indicate the effect of $f_{\text{lim},2R}$ and dust models, respectively. The right-hand column shows results with $A_V = 1.7$, the line colours and styles indicate the effect of $f_{\text{lim},1}$ and $f_{\text{lim},2R}$, respectively. Note that to avoid cluttering, most of the figure legends are omitted in the middle and lower right-hand panels for galaxies at $1.3 < z < 1.4$ and $1.8 < z < 1.9$; the line colours and styles are the same as the figures in the top right-hand panel. The matter correlation function is shown as the thick cyan curve. The estimate of the galaxy bias b^2 is obtained by taking the ratio of the two-point correlation function of galaxies and that of matter. Both real space and redshift space are shown for comparison.

more significant in redshift space than in real space. This result is also pointed out in the earlier attempt presented in Merson et al. (2019), where the galaxies are H α only galaxies rather than the samples defined using two emission lines as in this paper. However, the cause for this distortion on the largest scales is similar, and a combination of several factors, such as the RSD effect, sample variance, mode coupling of the cosmic density perturbation, and so on.

With the measured galaxy correlation function, we can estimate the constant value of bias b by fitting the b^2 as shown in Fig. 5 with a constant. Based on the measurement, we fit the data within

$10 < s < 50 h^{-1} \text{ Mpc}$. The uncertainty of the bias estimate adopts the same strategy as in Merson et al. (2019) based on the root-mean-square (rms) of the difference between b and the fitted mean b_{lin} ,

$$\delta b_{\text{lin}} = \sqrt{\frac{1}{N} \sum_{10 < s < 50} (b(s) - b_{\text{lin}})^2}, \quad (3)$$

where N is the number of bins for the galaxy correlation function within $10 < s < 50 h^{-1} \text{ Mpc}$. As an example, Fig. 6 displays the resulting measurement of linear bias for galaxies selected with $f_{\text{lim},1} =$

Figure 6. Linear bias estimated as a function of redshift for both real and redshift space. The galaxies are chosen with $f_{lim,1} = 1.0 \times 10^{-16} \text{ erg s}^{-1} \text{ cm}^{-2}$ and $f_{lim,2R} = 1.0$, i.e. only galaxies with both H α and [O III] emission lines brighter than $1.0 \times 10^{-16} \text{ erg s}^{-1} \text{ cm}^{-2}$ are selected. The dust-free result (black square with error bar) is also shown for comparison with the two choices of A_V . $A_V = 1.7$ corresponds to the calibration with WISP number counts, while $A_V = 1.9$ is for the calibration based on H α luminosity function (LF) observed in HiZELS. The results with other selection criteria for the flux limit of emission lines are similar. We note that the linear bias measurement is close to a linear relation with respect to redshift.

$1.0 \times 10^{-16} \text{ erg s}^{-1} \text{ cm}^{-2}$ and $f_{lim,2R} = 1.0$, i.e. only galaxies with both H α and [O III] flux brighter than $1.0 \times 10^{-16} \text{ erg s}^{-1} \text{ cm}^{-2}$. It shows a close to linear relation for galaxy bias as a function of redshift, for both real and redshift space. The two dust models calibrated to match the WISP number counts and HiZELS H α LF, respectively, give quite consistent results. Note that the huge error bar in the redshift-space measurement for the galaxy subsample at highest redshift bin is due to the noisy measurement of the correlation function.

The measured galaxy bias as a function of redshift can be simply described as $b_{lin}(z) = az + b$, where a and b are gradient and intercept, respectively. Combining this model with the bias measurements, we construct a simple χ^2 and perform a Markov chain Monte Carlo (MCMC) test with the PYTHON code EMCEE (Foreman-Mackey et al. 2013) to obtain the constraints on a and b . We then sample from the posterior to estimate the 16 and 84 percentile as the uncertainty. In Fig. 7, we show the fitting results for different dust models and sample selections. We can see that the dust model removes fainter and less massive galaxies. This can increase the average halo mass of the galaxy sample to increase the bias, as expected. The difference between the two dust models is not as significant as we find in the clustering measurements. The fitting result of the linear model is summarized in Table 1 for real space and in Table 2 for redshift space with different sample selections and dust model.

The flux limit of the strong line, i.e. $f_{lin,1}$, has a direct impact on the linear bias. Increasing its value selects galaxies with brighter H α or [O III] emissions. This is consistent with the relationship between H α or [O III] luminosity and host halo mass (see e.g. Zhai et al. 2019). However, at higher redshifts, the impact is less significant, which is partially due to the larger fraction of [O III]-dominated galaxies and thus reduces the effect. The dependence of linear bias on $f_{lin,2R}$, the flux limit of the secondary emission line is more complicated. The result does not present a monotonic relation. The reason is partially

due to the flux ratio of H α /[O III], which has a clear dependence on the H α luminosity. However this dependence decreases with higher redshift (see for example fig. 7 in Zhai et al. 2019). Thus the scatter of flux ratio H α /[O III] at a given H α luminosity indicates that a galaxy with bright H α emission does not necessarily has bright [O III] emission and vice versa. In general, we find that the dust models and the flux limit for the emission lines can affect our estimate of the linear bias at a few to ~ 10 per cent level.

3.3 HOD of H α galaxies

Halo occupation distribution (HOD) is a statistical approach to describe the connection between galaxies and dark matter haloes. It has been used to interpret the observations of galaxy clustering over a wide range of redshifts and luminosities (see e.g. Zheng et al. 2005; Zheng, Coil & Zehavi 2007; White et al. 2011; Zehavi et al. 2011; Zhai et al. 2017). In practice, it splits the galaxies into centrals and satellites. The investigations of massive galaxies have built simple parametrizations to describe the functional forms for the centrals and satellites. However, our understanding of the HOD of the ELGs is relatively poor, although some pioneering work has been done based on simulated or observed ELGs (for instance, Geach et al. 2012; Contreras et al. 2013; Gonzalez-Perez et al. 2018; Avila et al. 2020, and references therein).

The SAM simulation in our work provides a reasonable framework for the measurement of HOD of the ELGs. In Fig. 8, we present the measured HOD using different selections and dust models for galaxies in a few redshift slices. The first prominent feature is that the HOD for centrals has a double-peak shape as a function of halo mass. The valley is around $10^{12.4} M_\odot h^{-1}$ and this position has no significant dependence on sample selection. This double-peak HOD for centrals differs from the results of studies based on luminous red

Figure 7. Linear bias of $H\alpha$ galaxies as a linear function of redshift using clustering measurement within scales of $10 < s < 50 h^{-1}$ Mpc. Both real (left) and redshift (right) space results are shown. The figure also displays the effect of changing the sample selection and dust attenuation: Top: impact of changing parameter $f_{\text{lim},2R}$, i.e. limit of the strength of the weak emission line. Galaxies are selected with the 6.5σ nominal depth for the strongest emission line and the dust model can match WISP number counts. Middle: impact of the limit of the strongest emission line. The weak line has a limit of 50 per cent of $f_{\text{lim},1}$ and the dust model can match WISP number counts. Bottom: the effect of the dust model. The strongest emission line is brighter than the 6.5σ nominal depth and the weaker line is brighter than $0.5 \times 10^{-16} \text{ erg s}^{-1} \text{ cm}^{-2}$. The flux limit does not have a significant impact on the resulting bias measurement and reveals a weak tendency that higher flux limit preferentially selects more clustered galaxies, which is consistent with expectation. The dust model has a direct impact on the linear bias, but our calibrations based on WISP and HiZELS give consistent result. The shaded area represents inner 68 per cent distribution based on a MCMC test.

galaxies (LRGs), which are consistent with a monotonic function for central occupation. We note that this double-peak behaviour in the HOD can be a combination of different factors, including sample selection, dust model, and galaxy formation physics. In the earlier attempt of Merson et al. (2019), the HOD for $H\alpha$ galaxies is measured based on Millennium Simulation. Regardless of the different sample selections and parameter sets for the SAM, they also find similar, but weaker, behaviour as ours. This feature becomes less pronounced when a higher threshold for luminosity is adopted, consistent with the tendency shown in Fig. 8. When we increase the flux limit for the emission line or dust attenuation to reduce the galaxy number density, the double-peak feature becomes less significant. This indicates that the occupancy of the second peak is dominated by less massive galaxies. Previous work based on observational data or simulation shows that the occupation of central galaxies only peaks at low mass range and quickly declines at high-mass end (Contreras et al. 2013; Gonzalez-Perez et al. 2018; Avila et al. 2020; Hadzhiyska et al. 2021).

The double-peaked nature present in the predicted HODs can be traced back to the presence of two distinct sequences in the plane of central galaxy SFR and halo mass in the Galacticus models. We have examined the origin of these two sequences and find that they are the result of the fact that, in the UNIT simulation merger trees,

some significant fraction of dark matter haloes undergo periods of mass loss (i.e. their total mass decreases with time).

Galacticus assumes that haloes accrete baryons from their surroundings at a rate proportional to their halo mass growth rate. During periods of mass loss in a halo, Galacticus instead holds the baryonic content of the halo fixed, and let it begin to increase again when the halo has grown beyond its previous greatest mass.

As a consequence, haloes undergoing mass loss have no new gas supply, and so the SFR of their central galaxies quickly declines, leading to the formation of a second sequence of galaxies in the plane of SFR and halo mass.

These periods of mass loss from haloes may be physical (driven by merging events that cause mass to be ejected), or may be purely numerical in origin (due to the choice of halo mass definition, or to failings in the halo finder and merger tree builder to link haloes together over time). A detailed examination of the origins of these periods of mass loss, and how best to model their effect on the baryonic content of haloes, is beyond the scope of this paper, but will be explored in a future work.

The satellite occupation from Galacticus is consistent with expectations, and can be represented by a functional form close to a power law, which is similar to massive galaxies at lower redshift. However, we note that this power law can break for high-redshift galaxies.

Table 1. The fitting result for the galaxy bias as a linear function of redshift: $b_{\text{lin}}(z) = az + b$, estimated from clustering measurement in real space for H α galaxies. The flux limit $f_{\text{lin},1}$ is in unit of $\times 10^{-16}$ erg s $^{-1}$ cm $^{-2}$, and parameter $f_{\text{lin},2R}$ is dimensionless.

	a	b
$f_{\text{lin},1} = 0.5$		
$f_{\text{lin},2R} = 0.25, A_V = 0.0$	0.686 ± 0.022	0.349 ± 0.034
$f_{\text{lin},2R} = 0.25, A_V = 1.7$	0.878 ± 0.05	0.166 ± 0.069
$f_{\text{lin},2R} = 0.25, A_V = 1.9$	0.895 ± 0.04	0.156 ± 0.056
$f_{\text{lin},2R} = 0.5, A_V = 0.0$	0.694 ± 0.031	0.31 ± 0.045
$f_{\text{lin},2R} = 0.5, A_V = 1.7$	0.811 ± 0.036	0.228 ± 0.052
$f_{\text{lin},2R} = 0.5, A_V = 1.9$	0.866 ± 0.031	0.175 ± 0.044
$f_{\text{lin},2R} = 1.0, A_V = 0.0$	0.785 ± 0.028	0.171 ± 0.041
$f_{\text{lin},2R} = 1.0, A_V = 1.7$	0.834 ± 0.046	0.183 ± 0.063
$f_{\text{lin},2R} = 1.0, A_V = 1.9$	0.862 ± 0.049	0.167 ± 0.068
$f_{\text{lin},1} = 1.0$		
$f_{\text{lin},2R} = 0.25, A_V = 0.0$	0.806 ± 0.038	0.192 ± 0.056
$f_{\text{lin},2R} = 0.25, A_V = 1.7$	0.918 ± 0.055	0.181 ± 0.069
$f_{\text{lin},2R} = 0.25, A_V = 1.9$	0.916 ± 0.063	0.191 ± 0.079
$f_{\text{lin},2R} = 0.5, A_V = 0.0$	0.743 ± 0.049	0.281 ± 0.063
$f_{\text{lin},2R} = 0.5, A_V = 1.7$	0.915 ± 0.06	0.156 ± 0.078
$f_{\text{lin},2R} = 0.5, A_V = 1.9$	0.907 ± 0.074	0.182 ± 0.095
$f_{\text{lin},2R} = 1.0, A_V = 0.0$	0.778 ± 0.041	0.226 ± 0.058
$f_{\text{lin},2R} = 1.0, A_V = 1.7$	0.844 ± 0.088	0.221 ± 0.118
$f_{\text{lin},2R} = 1.0, A_V = 1.9$	0.788 ± 0.085	0.337 ± 0.106
$f_{\text{lin},1} = 2.0$		
$f_{\text{lin},2R} = 0.25, A_V = 0.0$	0.809 ± 0.047	0.247 ± 0.066
$f_{\text{lin},2R} = 0.25, A_V = 1.7$	0.88 ± 0.071	0.283 ± 0.095
$f_{\text{lin},2R} = 0.25, A_V = 1.9$	0.853 ± 0.111	0.357 ± 0.129
$f_{\text{lin},2R} = 0.5, A_V = 0.0$	0.828 ± 0.051	0.208 ± 0.07
$f_{\text{lin},2R} = 0.5, A_V = 1.7$	0.859 ± 0.102	0.297 ± 0.127
$f_{\text{lin},2R} = 0.5, A_V = 1.9$	0.87 ± 0.132	0.317 ± 0.158
$f_{\text{lin},2R} = 1.0, A_V = 0.0$	0.857 ± 0.041	0.168 ± 0.058
$f_{\text{lin},2R} = 1.0, A_V = 1.7$	0.871 ± 0.132	0.31 ± 0.178
$f_{\text{lin},2R} = 1.0, A_V = 1.9$	0.807 ± 0.229	0.428 ± 0.287

3.4 [O III] galaxies

In this section, we present the linear bias measurements for galaxies at $z > 2$. Note that for this paper, the sample selection for these high-redshift galaxies ($z > 2$) is different from the lower redshift sample ($z < 2$); only the [O III] line flux is used, as $f_{\text{lin},1}$, to define the flux-selected samples. The [O II] line can be used as the second emission line for robust redshift determination for the *Roman* $z > 2$ ELG sample, which will be implemented in future work pending improvement of [O II] line flux predictions from Galacticus.

In the top rows of Fig. 9, we present the correlation function of the galaxies with a few example redshift slices. The bias measurement b^2 is shown in the bottom row. We find that the BAO peak can be recovered with these sparser samples, compared with the $z < 2$ galaxies. However, due to the lower number density, the clustering measurement becomes noisy and the BAO signal is erased to certain extent. This can be improved by enlarging the redshift bins in the analysis to include more galaxies in the measurement of the two-point correlation function. The ratio of the galaxy and the dark matter correlation functions also shows a close to constant behaviour at scales $10 < s < 50 h^{-1}$ Mpc, similar to the H α galaxies and thus enables an estimate of a constant bias on linear scales.

In Fig. 10, we present the bias measurement for [O III] ELGs using the same method as in previous section. The galaxies are selected if the [O III] line flux is higher than 0.5×10^{-16} erg s $^{-1}$ cm $^{-2}$.

Table 2. The same as Table 1, but for redshift space.

	a	b
$f_{\text{lin},1} = 0.5$		
$f_{\text{lin},2R} = 0.25, A_V = 0.0$	0.727 ± 0.046	0.598 ± 0.07
$f_{\text{lin},2R} = 0.25, A_V = 1.7$	0.886 ± 0.054	0.472 ± 0.075
$f_{\text{lin},2R} = 0.25, A_V = 1.9$	0.943 ± 0.054	0.416 ± 0.075
$f_{\text{lin},2R} = 0.5, A_V = 0.0$	0.699 ± 0.04	0.617 ± 0.057
$f_{\text{lin},2R} = 0.5, A_V = 1.7$	0.929 ± 0.062	0.393 ± 0.089
$f_{\text{lin},2R} = 0.5, A_V = 1.9$	0.908 ± 0.036	0.442 ± 0.049
$f_{\text{lin},2R} = 1.0, A_V = 0.0$	0.799 ± 0.045	0.476 ± 0.07
$f_{\text{lin},2R} = 1.0, A_V = 1.7$	0.888 ± 0.051	0.43 ± 0.07
$f_{\text{lin},2R} = 1.0, A_V = 1.9$	0.891 ± 0.061	0.434 ± 0.085
$f_{\text{lin},1} = 1.0$		
$f_{\text{lin},2R} = 0.25, A_V = 0.0$	0.807 ± 0.051	0.525 ± 0.075
$f_{\text{lin},2R} = 0.25, A_V = 1.7$	0.938 ± 0.065	0.462 ± 0.08
$f_{\text{lin},2R} = 0.25, A_V = 1.9$	0.942 ± 0.082	0.466 ± 0.104
$f_{\text{lin},2R} = 0.5, A_V = 0.0$	0.793 ± 0.041	0.519 ± 0.06
$f_{\text{lin},2R} = 0.5, A_V = 1.7$	0.962 ± 0.075	0.406 ± 0.095
$f_{\text{lin},2R} = 0.5, A_V = 1.9$	0.944 ± 0.075	0.442 ± 0.097
$f_{\text{lin},2R} = 1.0, A_V = 0.0$	0.804 ± 0.048	0.522 ± 0.06
$f_{\text{lin},2R} = 1.0, A_V = 1.7$	0.881 ± 0.094	0.489 ± 0.122
$f_{\text{lin},2R} = 1.0, A_V = 1.9$	0.826 ± 0.087	0.569 ± 0.112
$f_{\text{lin},1} = 2.0$		
$f_{\text{lin},2R} = 0.25, A_V = 0.0$	0.868 ± 0.054	0.488 ± 0.078
$f_{\text{lin},2R} = 0.25, A_V = 1.7$	0.965 ± 0.103	0.494 ± 0.125
$f_{\text{lin},2R} = 0.25, A_V = 1.9$	0.922 ± 0.105	0.57 ± 0.121
$f_{\text{lin},2R} = 0.5, A_V = 0.0$	0.85 ± 0.062	0.486 ± 0.086
$f_{\text{lin},2R} = 0.5, A_V = 1.7$	0.979 ± 0.096	0.463 ± 0.114
$f_{\text{lin},2R} = 0.5, A_V = 1.9$	0.946 ± 0.144	0.532 ± 0.178
$f_{\text{lin},2R} = 1.0, A_V = 0.0$	0.934 ± 0.042	0.4 ± 0.056
$f_{\text{lin},2R} = 1.0, A_V = 1.7$	0.948 ± 0.153	0.515 ± 0.205
$f_{\text{lin},2R} = 1.0, A_V = 1.9$	0.893 ± 0.207	0.618 ± 0.297

The stronger dust attenuation (higher A_V) selects brighter and more massive galaxies, which increase the galaxy bias as expected. Given the estimated uncertainty, the two dust models give consistent result within 1σ . Compared with the H α ELGs, the two dust models increase the bias estimates significantly for the [O III] ELGs, due to the fact that dust imposes more attenuation on [O III] emission than H α . The distribution of the measurements in the figure also presents a linear relation of galaxy bias with redshift. We fit with a linear relation as introduced in Section 3.2 and present the result in Fig. 11. We note that the flux limit has a stronger effect on the bias of the $z > 2$ galaxies than the $z < 2$ galaxies; the bias can change by roughly 20 per cent. The nominal depth for *Roman* galaxy survey of flux above 1×10^{-16} erg s $^{-1}$ cm $^{-2}$ is able to observe a significant number of [O III] emitting and highly biased galaxies. This can provide robust measurement for the clustering signal to infer cosmological information. Compared with the galaxies at $z < 2$, these [O III] galaxies are more biased due to the early phases of the dark matter evolution and the redshift dependence of dark matter halo bias. The fitting result of the linear bias model is summarized in Table 3.

We measure the HOD of these [O III] galaxies to better understand their distribution within dark matter haloes and present the result in Fig. 12 for a few redshift slices. The prominent feature is similar to that of the H α galaxies at $z < 2$. The central occupation shows a clear double-peak behaviour as a function of halo mass. Either it is caused by physical reasons of mass loss of dark matter haloes, or numerical issues in the simulation, we will investigate this in future

Figure 8. Halo occupation distribution (HOD) of the $H\alpha$ galaxies for redshift slices as indicated in each panel. The effect of changing the selection parameters and dust model is also shown. Top: the effect of changing dust attenuation for galaxies selected with $f_{\text{lim},1} = 1.0 \times 10^{-16} \text{ erg s}^{-1} \text{ cm}^{-2}$ and $f_{\text{lim},2R} = 0.5$, the intrinsic distribution without dust attenuation ($A_V = 0$) is also shown as black curves. Middle: the effect of selection parameter $f_{\text{lim},2R}$ for galaxies selected with $1.0 \times 10^{-16} \text{ erg s}^{-1} \text{ cm}^{-2}$ for the strongest emission line and WISP-calibrated dust model. Bottom: the effect of changing the flux limit of the strongest line $f_{\text{lim},1}$ for galaxy samples defined with $f_{\text{lim},2R} = 0.5$ and WISP-calibrated dust model. We present the occupation of centrals (dashed), satellites (dotted), and the total (solid), respectively.

work. Similar to the $z < 2$ galaxies, the satellite occupation is also close to a power-law form, but with some break at high redshift.

3.5 Comparison of HOD with eBOSS

In order to further investigate whether our Galactica simulation can make reasonable predictions for HODs, we compare the HOD results with the latest eBOSS ELG measurement (Avila et al. 2020). The eBOSS ELG program creates a catalogue of thousands of galaxies within the redshift range of $0.6 < z < 1.1$, selected using the Dark Energy Camera Legacy Survey (DECaLS) photometric survey. The

finalized sample has an average redshift $z = 0.865$ with a number density of $n_{\text{eBOSS}} = 2.187 \times 10^{-4} (\text{Mpc } h^{-1})^{-3}$. At this redshift, the *Roman* HLSS can only observe $H\alpha$ emission due to the wavelength range of its grism (see Fig. 2). Therefore, we use the $H\alpha$ flux to define our galaxy mock. We apply flux limit $f_{\text{lim}} = 5 \times 10^{-16}$ and $10 \times 10^{-16} \text{ erg s}^{-1} \text{ cm}^{-2}$ with two dust models $A_V = 1.7$ and 1.9 . This gives us four different galaxy samples with number densities 1.65, 1.08, 0.38, and 0.27 times that of eBOSS ELG. We measure their HODs and compare with the eBOSS measurement in Fig. 13. Although our galaxy sample has different target selection than eBOSS that uses $[\text{O II}]$ doublet to identify galaxy redshift, our prediction of

Figure 9. The measurement of galaxy correlation function and bias for a few redshift slices of [O III] galaxies, as labelled in the legend. Since these galaxies only have [O III] emission bright enough, the sample selection is different from the H α galaxies in terms of a single flux limit $f_{\text{lim},1}$. The figure displays the effect of dust attenuation for galaxies with a [O III] flux brighter than $0.5 \times 10^{-16} \text{ erg s}^{-1} \text{ cm}^{-2}$. The matter correlation function is shown as the thick cyan curve, and the galaxy bias is measured in the bottom panels.

Figure 10. Linear bias of the [O III] galaxies estimated as a function of redshift for both real and redshift space. The galaxies are chosen with $f_{\text{lim},1} = 0.5 \times 10^{-16} \text{ erg s}^{-1} \text{ cm}^{-2}$ and the colours are coded for dust attenuation. The result indicates a significant impact of the dust attenuation, compared with the low-redshift H α galaxies. The measurement of galaxy bias is close to a linear relation with respect to redshift.

HOD has similar amplitude when the number density is close to that of eBOSS. The satellite occupancy shows excellent agreement in terms of the shape and amplitude. The halo mass dependence can be described by a power law at high-mass end. The central occupancy in both Galacticus and eBOSS shows a similar shape with a peak at intermediate mass scale, with eBOSS peaking at slightly lower mass scale. In addition, the overall amplitude of the central occupancy of Galacticus is higher and its shape flattens at high-mass end instead of dropping quickly. This discrepancy can be caused by a combination of factors: the difference in the selection algorithms of *Roman* galaxy redshift survey and eBOSS, the calibration of Galacticus for the parameters governing star formation history and galaxy formation, the dust models used in the analysis, and so on.

3.6 A practical fit of ELG bias at $1 < z < 3$

In Fig. 14, we present the bias measurement of ELGs for the entire redshift range of *Roman* HLSS. We apply $f_{\text{lim}} = 1 \times 10^{-16} \text{ erg s}^{-1} \text{ cm}^{-2}$ and $f_{\text{lim},2R} = 1.0$ to choose H α galaxies, and $f_{\text{lim}} = 1 \times 10^{-16} \text{ erg s}^{-1} \text{ cm}^{-2}$ for [O III] galaxies. Using the measurement with dust model $A_V = 1.7$, we perform a linear fit of the bias measurement for H α and [O III] galaxies, respectively, shown as the red line with shaded area. The fitting result can also be found from Tables 1–3. In redshift space, we summarize the results as

$$\begin{aligned} \text{H}\alpha (1 < z < 2) : b &= 0.88z + 0.49, \\ \text{[O III]} (2 < z < 3) : b &= 0.98z + 0.49. \end{aligned} \quad (4)$$

Figure 11. Linear bias of [O III] galaxies as a linear function of redshift using clustering measurement within scales of $10 < s < 50 h^{-1}$ Mpc. Both real (left) and redshift (right) space results are shown. The figure also displays the effect of the flux limit of the emission line and dust attenuation. Top: galaxies are selected with the WISP-based dust model and colours stand for the flux limit. Bottom: effect of the dust model for galaxies with [O III] emission-line flux brighter than $1.0 \times 10^{-16} \text{ erg s}^{-1} \text{ cm}^{-2}$, i.e. the 6.5σ nominal depth of *Roman*. The flux limit has a direct impact on the galaxy bias with brighter galaxies are more biased. The two dust models give consistent estimate of the galaxy bias, similar to the $\text{H}\alpha$ galaxies at low redshift. The shaded area represents inner 68 per cent distribution based on an MCMC test.

Table 3. The flux limit $f_{\text{lin},1}$ is in unit of $\times 10^{-16} \text{ erg s}^{-1} \text{ cm}^{-2}$. The fitting result for the galaxy bias as a linear function of redshift: $b_{\text{lin}}(z) = az + b$, estimated from clustering measurement in both real and redshift space for [O III] galaxies within $2 < z < 3$.

	a	b
Real space		
$f_{\text{lin},1} = 0.5, A_V = 0.0$	0.842 ± 0.028	0.062 ± 0.068
$f_{\text{lin},1} = 0.5, A_V = 1.7$	0.928 ± 0.093	0.185 ± 0.218
$f_{\text{lin},1} = 0.5, A_V = 1.9$	0.91 ± 0.128	0.261 ± 0.291
$f_{\text{lin},1} = 1.0, A_V = 0.0$	0.906 ± 0.032	0.063 ± 0.078
$f_{\text{lin},1} = 1.0, A_V = 1.7$	0.917 ± 0.183	0.37 ± 0.407
$f_{\text{lin},1} = 1.0, A_V = 1.9$	0.75 ± 0.27	0.716 ± 0.612
Redshift space		
$f_{\text{lin},1} = 0.5, A_V = 0.0$	0.923 ± 0.067	0.196 ± 0.169
$f_{\text{lin},1} = 0.5, A_V = 1.7$	1.03 ± 0.113	0.276 ± 0.27
$f_{\text{lin},1} = 0.5, A_V = 1.9$	1.07 ± 0.124	0.226 ± 0.278
$f_{\text{lin},1} = 1.0, A_V = 0.0$	1.018 ± 0.047	0.116 ± 0.12
$f_{\text{lin},1} = 1.0, A_V = 1.7$	0.98 ± 0.251	0.49 ± 0.558
$f_{\text{lin},1} = 1.0, A_V = 1.9$	0.771 ± 0.318	0.99 ± 0.725

Our previous tests show that the practical choices for the dust model and flux limits for the emission lines will not have significant impact on the estimate of the linear bias. Therefore the result quoted above is a reasonable description for future analysis, especially for the investigation of the science forecast of *Roman* HLSS.

3.7 AGN contamination

Based on observation of luminous $\text{H}\alpha$ emitters from HiZELS, Sobral et al. (2016) find that the $\text{H}\alpha$ emitters are more dominated by active

galactic nuclei (AGNs) at the brighter end, in terms of the line flux and luminosity. This AGN fraction reveals no evolution with redshift. The flux cut on the *Roman* or *Euclid* galaxies can select bright $\text{H}\alpha$ emitters that can be in fact AGNs. In order to estimate the potential contamination from AGN, Fig. 15 presents the distribution of the $\text{H}\alpha$ line emissions for *Roman* galaxies at $1 < z < 2$ based on flux (left-hand panel) and L^* (right-hand panel) where redshift-dependent $L_{\text{H}\alpha}^*$ is given by $L_{\text{H}\alpha}^* = 0.45z + 41.47$ (see Sobral et al. 2016). Fig. 15 shows that *Roman* galaxies concentrate on the faint end and the overall population peaks around $2L^*$. Sobral et al. (2016) find that the AGN fraction is most correlated with $L_{\text{H}\alpha}/L_{\text{H}\alpha}^*$. Using the right-hand panel of Fig. 15, and the fitting formula given in table 4 of Sobral et al. (2016), we estimate that the AGN fraction in the *Roman* galaxy sample is around 10 per cent. Applying a brighter flux cut would remove faint galaxies and increase the AGN fraction.

Since AGNs are bright and have characteristic continuum different from typical ELGs, they can be excluded from the *Roman* galaxy sample in the spectral fitting of the 1D extracted spectrum.

4 DISCUSSION AND CONCLUSION

ELGs are the main targets of many current and future cosmological surveys. The bright nebula emissions due to star formation activity make the sample selection different from that of the red and massive galaxies at low redshifts. The results based on current observational data are not sufficient to allow simple extrapolation to higher redshifts, thus requires detailed investigations of their spatial distribution based on accurate numerical simulations. In this paper, we study the linear bias of these ELGs from *Roman* galaxy redshift survey based on clustering measurement and present their redshift evolution for various sample selections and dust models.

Figure 12. Halo occupation distribution (HOD) of the [O III] galaxies for redshift slices as indicated in each panel. The effect of limiting the line flux and dust model is also shown. Top: the effect of dust model for galaxies with [O III] flux higher than $0.5 \times 10^{-16} \text{ erg s}^{-1} \text{ cm}^{-2}$. Bottom: the effect of emission-line flux limit with dust model calibrated based on WISP number counts. We present the occupation of centrals (dashed), satellites (dotted), and the total (solid), respectively.

Figure 13. Comparison of HOD measurements with eBOSS. Left: occupancy for satellites. Middle: occupancy for centrals. Right: occupancy for total galaxies. Using *Roman* simulation, we apply flux cut $f_{\text{lim}} = 5 \times 10^{-16}$ and $10 \times 10^{-16} \text{ erg s}^{-1} \text{ cm}^{-2}$, and dust models $A_V = 1.7$ and 1.9 to define four galaxy mocks within $0.8 < z < 0.9$. The number densities of these mocks are 1.65, 1.08, 0.38, and 0.27 times that of eBOSS ELG, respectively, and their results are marked by different colours. The eBOSS measurements are from Avila et al. (2020).

In particular, we use the Galacticus SAM to perform a large-scale galaxy simulation. The model processes all the dark matter merger trees distributed within the $1 h^{-1} \text{ Gpc}$ box of the N -body simulation UNIT (Chuang et al. 2019). We then construct a light-cone catalogue using the method in Kitzbichler & White (2007). The parameters of the model are calibrated to match the current observations at high redshifts to ensure that the galaxy simulation is realistic. We used this model to predict the number densities of H α and [O III] emitters

for the *Roman* galaxy survey in Zhai et al. (2019). The same model has been used here to produce a 2000 deg^2 galaxy mock, consistent with the baseline design of *Roman* galaxy redshift survey. A galaxy clustering analysis based on this mock catalogue is performed in Zhai et al. (2021) to forecast the uncertainties of the BAO and RSD measurements. The wavelength range of the *Roman* grism has a direct impact on the redshift range of each nebula emission line, and constrains the selection of galaxy samples (see Fig. 2). We have

Figure 14. The linear bias measurement for the entire redshift range of *Roman* HLSS. The $H\alpha$ galaxies are selected by two emission lines with flux limits $f_{\text{lim},1}$ and $f_{\text{lim},2R}$, while [O III] galaxies are selected by $f_{\text{lim},1}$ only. The result shows measurements with dust free ($A_V = 0$) and two dust models. The red lines are a linear fit for measurements with $A_V = 1.7$ and the shaded area is 1σ uncertainty.

Figure 15. Distribution of $H\alpha$ emitters for *Roman* galaxies at $1 < z < 2$ as a function of flux (left) and $L_{H\alpha}/L_{H\alpha}^*$ (right). The galaxies are selected with $A_V = 1.7$ and both $H\alpha$ and [O III] emission lines are brighter than $1 \times 10^{-16} \text{ erg s}^{-1} \text{ cm}^{-2}$. The distribution becomes narrower and fainter at higher redshift, partially due to the fact that the galaxies become more [O III] dominated (Fig. 4). The weak bimodal distribution is correlated with the double-peak behaviour of HOD as explained in Section 3.3.

investigated how the clustering of the *Roman* galaxies depends on the chosen line flux limits.

Depending on the selection criteria of ELGs, we can measure the linear bias of galaxies as a function of redshift with the simulated galaxy catalogue and the dust model. We first measure the two-point correlation function of galaxies in real and redshift space and find that the BAO peak on large scales can be recovered for both $H\alpha$ and [O III] galaxies within the *Roman* redshift range, although the [O III] galaxy samples are more affected by shot noise due to the low number density. Taking the ratio of correlation function between galaxies and matter enables the measurement of galaxy bias. The result at scales $10 < s < 50 h^{-1} \text{ Mpc}$ reveals a roughly constant bias estimate. Thus we use this scale-independent value as the linear bias of galaxies. Deviation of the bias measurement from a constant value at larger scales is noticeable, which is caused by a combination of factors including the non-linear evolution of the BAO signal, the RSD effect, and sample variance due to limited cosmic volume.

We find that the scale-independent galaxy biases for both $H\alpha$ and [O III] ELGs are close to a linear function, $b(z) = az + b$, see

equation (4), consistent with previous results on $H\alpha$ ELGs (Merson et al. 2019), see Tables 1 and 2 for $H\alpha$ galaxies, and Table 3 for [O III] galaxies. For $H\alpha$ galaxies we have investigated the impact of the line flux limit and dust model on the linear bias measurement, as shown in Fig. 7. We find that the linear bias of ELGs at $1 < z < 3$ is insensitive to line flux cut or dust attenuation model, consistent with earlier work at $z < 2$ (Merson et al. 2019). We find that galaxy bias increases with redshift for ELGs, as expected, since higher redshifts correspond to earlier (more biased) phases of galaxy distribution. As dark matter haloes grow with decreasing redshift, they become more populated with galaxies, which reduce the bias factor with which galaxy distribution traces the matter distribution.

In order to better understand the distribution of ELGs within their host dark matter haloes, we have performed HOD measurements for the galaxy samples, as well as the halo mass function of the selected galaxies (see Appendix A). The noticeable feature is the double peak for the central occupancy. The second peak at high-mass end is likely caused by the mass loss of haloes during evolution. However the current model is not able to identify whether this mass loss is physical or due to numerical artefacts, therefore we leave it for future work. On the other hand, the satellite occupancies for both $H\alpha$ and [O III] galaxies are close to a power-law form, with the tendency of a break at the high-mass end. This can enable a simple parametrization for practical application in the analysis of large-scale structure.

The *Roman* galaxy redshift survey will suffer from the usual systematic effects of slitless spectroscopy (Faisst et al. 2018; Martens et al. 2019), such as line misidentification and spectral overlap, although to a lesser degree compared to *Euclid*, thanks to the higher spectral resolution and wider wavelength range of the *Roman* grism compared to the *Euclid* red grism (the *Euclid* blue grism will not be used in the wide survey). In future work, we will study the survey completeness and purity for the *Roman* galaxy redshift survey, and their impact on the observed galaxy sample and the galaxy clustering analysis.

The HOD measurement of the *Roman* galaxy sample builds a straightforward connection between galaxies and dark matter haloes, in terms of the halo mass being the only parameter. However the secondary halo properties other than halo mass can also impact the clustering signals of galaxies. This assembly bias phenomenon has

been reported in researches based on numerical simulation (see e.g. Gao, Springel & White 2005; Wechsler et al. 2006). Some of the latest studies for ELGs find that the secondary properties of dark matter haloes can affect the distribution of ELGs and thus the cosmological measurement based on large-scale structure like BAO peak (Jimenez et al. 2020). The SAM employed in our simulation can output detailed properties of galaxies, and their host haloes. This can build a more accurate connection between galaxies and dark matter haloes by using information of both internal and external halo properties, and help to minimize the systematics in the cosmological inference.

We have presented linear bias and HOD measurements for ELGs at $1 < z < 3$ in this paper, which are key inputs to the realistic forecast of dark energy and cosmological constraints from possible *Roman* galaxy redshift surveys. These in turn can be used to optimize the observing strategy for *Roman*. Our results are similarly useful to other ongoing or future galaxy surveys that use ELGs to trace cosmic large-scale structure.

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Software used: PYTHON, MATPLOTLIB (Hunter 2007), NUMPY (van der Walt, Colbert & Varoquaux 2011), SCIPY (Jones, Oliphant & Peterson 2001), GEORGE (Ambikasaran et al. 2015), EMCEE (Foreman-Mackey et al. 2013), and HANKEL (Murray & Poulin 2019).

DATA AVAILABILITY

The original dark matter halo catalogues are available from the UNIT simulation website. The galaxy mocks are available by request. A public web page presenting the mocks will be available at a later time.

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APPENDIX A: ELG HALO MASS FUNCTION

In order to better understand the distribution of galaxies within dark matter haloes, we compute the halo mass function (HMS) of the *Roman* ELGs, i.e. the number density of dark matter haloes that host *Roman* galaxies. Fig. A1 shows an example for galaxies within $1.0 < z < 1.1$, with different selection algorithms including the flux limits

Figure A1. Illustration of the halo mass function (HMS) of the *Roman* ELGs within $1.0 < z < 1.1$. Galaxies are selected with the criteria including flux limits and dust model as shown in the legend. The solid purple line is the HMS from the original UNIT simulation at $z = 1.032$.

on the emission lines and dust models. The lower amplitude for the *Roman* galaxies is mainly dominated by the selection algorithms. The flux limit can remove faint galaxies that are likely to live in less massive haloes. The requirement of both H α and [O III] emission lines and the galaxy formation physics impact the decrease of the HMS at high-mass end.

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