Measurements of Reflected Shock Tunnel Freestream Nitric Oxide Temperatures and Partial Pressure

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This paper reports on measurements of freestream nitric oxide (NO) rotational and vibrational temperatures and partial pressures, collected in the Caltech T5 reflected shock tunnel. Quantum cascade lasers, emitting mid-infrared light resonant with fundamental rovibrational NO transitions, were directed through the supersonic (Mach ~5) freestream flow. Tunable diode laser absorption spectroscopy (TDLAS) was used to measure the path-averaged rotational and vibrational temperatures of NO in the flow, in addition to the NO partial pressure. The temperature measurements demonstrate strong evidence of NO rotational and vibrational equilibrium during the 1 ms test period. Agreement between vibrational and rotational temperatures was observed in all experiments, including one $h_{\text{rot}} \approx 8$ MJ/kg and four $h_{\text{rot}} \approx 18$ MJ/kg experiments, during and after the nominal test time. Absorption from CO and H$_2$O was also observed in the TDLAS measurements, though their concentrations cannot be accurately estimated. The goal of these and future experiments is to develop and demonstrate TDLAS experimental strategies for high-enthalpy impulse facilities and to help to inform improvements of existing models and solvers used for prediction of freestream conditions.

I. Introduction

At hypersonic velocities, the onset of vibrational excitation, dissociation, and air chemistry have an impact on many parameters of interest to designers, including shock position, kinetic temperature, and heat loading [1–5]. Considerable recent efforts have been devoted to understanding and modeling internal energy relaxation and dissociation in hypersonic flows using both first-principles calculations [6–9] and reduced-order modeling [10]. At present, the validation and implementation of models, ranging in fidelity and computational cost, is hampered by the lack of experimental data directly probing hypervelocity flowfields. Spectroscopic measurements in high-enthalpy, hypersonic experimental facilities thus continue to play an important role in grounding computational models and making them robust over a wide range of conditions [11–13].

Many experimental methods for characterizing flow facilities, such as heat flux gauges or pitot rakes, are intrusive and often yield incomplete information [14,15]. Optical techniques, such as schlieren imaging, provide nonintrusive metrics to comprehensively study the whole flow structure. More pointedly, spectroscopic measurements afford the possibility of species and state-specific information, which is critical in nonequilibrium environments. From this information, a variety of parameters can be discerned, such as temperature, composition, and flow velocity. It is desirable to leverage the wealth of spectroscopic knowledge to provide insight into hypersonic flow structures and nonequilibrium air. Unfortunately, the spectra of molecular oxygen and nitrogen pose significant challenges to experimental study. The strongest and widely known quantum transitions for these molecules are in the ultraviolet range, which are challenging to access due to the complexity and bulk of ultraviolet laser systems [16,17]. Transitions that are in more accessible spectral regions are quantum mechanically forbidden and are called “dark” [18,19].

Nitric oxide (NO) serves as an excellent tracer of nonequilibrium behavior of air for the following reasons: 1) NO forms as an intermediary in both the dissociation and recombination processes in air, and 2) NO has a well-understood and easily probed infrared absorption spectrum for the observation of vibrational and rotational energy. There is considerable heritage in using NO in hypersonic facilities. Daney et al. used NO laser-induced fluorescence (LIF) for velocimetry in the Australian National University T2 and T3 free-piston shock tunnels [20]. Jiang et al. used NO planar LIF (PLIF) to investigate boundary-layer separation over models at the NASA Langley 31-Inch Mach 10 tunnel [21]. Lee et al. [22] and

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Nomenclature

$A =$ integrated absorbance, cm$^{-1}$

$A_{21} =$ Einstein $A$, s$^{-1}$

$c =$ speed of light, cm/s

$E =$ lower-state energy, cm$^{-1}$

$g =$ degeneracy

$I =$ intensity, arbitrary units

$K_B =$ Boltzmann constant, J/K

$L =$ path length, cm

$P =$ pressure, atm or MPa

$Q =$ partition function

$S =$ linstrength, atm$^{-1} \cdot$ cm$^{-1}$

$T =$ temperature, K

$w =$ weights in fitting algorithm

$\alpha =$ absorbance

$\nu =$ frequency, cm$^{-1}$

$\Phi =$ lineshape function, cm
McMillin et al. [23] used PLIF of NO to study transverse fuel injection and combustion in supersonic flows in shock tube experiments at Stanford. Mohamed et al. used tunable infrared diode lasers for absorption measurements to probe NO concentrations, temperature, and velocity at the ONERA F4 wind tunnel [24].

In addition to measurements of flow over models at hypersonic conditions, there is also considerable interest in the facility freestream itself, particularly in reflected shock tunnels. Stagnation enthalpies and pressures are usually sufficient to induce chemical reactions and vibrational excitation. After the nozzle expansion, the flow may nominally approach a condition representative of a flight altitude and Mach number, but may retain a degree of thermal and chemical nonequilibrium [25]. This nonequilibrium may subsequently affect the stagnated region may persist longer within and downstream of the nozzle at concentrations that differ from thermochemical equilibrium projections and with multiple temperatures [26,27].

Parker et al. monitored NO concentration, temperature, and velocity of various hypersonic freestream shots at Calpans-University of Buffalo Research Center (CUBRC) in Buffalo, NY [28,29]. The authors used laser absorption spectroscopy with a quantum cascade laser to probe several transitions near 5.45 μm of NO and its isotopologues. Measurements were made in both the 48-in. tunnel and the Large Energy National Shock (LENS) I tunnel. By matching the integrated areas under the absorption features, the authors concluded that the NO concentration differed from computational fluid dynamics projections. Additionally, measurements of velocity were observed to substantially disagree with projections at high stagnation enthalpies (above 10 MJ/kg), indicative of a lack of clarity of the “real gas” effects at play in the expanded flow. A study by Nonpleps and Candler attempted to reproduce the results of Parker on a theoretical basis [30]. Distributing the total enthalpy into thermal, internal (mostly vibrational), and chemical modes, and then using theoretical kinetics for internal energy transfer and chemistry, the authors found that they could not account for Parker’s lower measured NO levels (a discrepancy in mass fraction of about 4%), nor the high level of energy consolidation in velocity at the exclusion of internal modes.

The present work is part of a Stanford University, California Institute of Technology, and University of Minnesota collaboration to characterize the Caltech T5 free piston shock tunnel. Optical diagnostics have been previously employed at the T5 facility [31,32], but this study represents the first use of laser absorption on the shock tunnel. Tunable diode laser absorption spectroscopy (TDLAS) was employed to probe several rovibrational states of NO, enabling measurement of population temperatures and species partial pressures. These state populations were analyzed to ascertain the target species temperature independently, all of which is a function of temperature alone under the assumption of thermal equilibrium (i.e., $T_{trans} = T_{rot} = T_{vib}$). In this study, it was not assumed that a single temperature could define the energy distribution among absorber states. Sensitivity to multiple modal temperatures can be achieved by measuring several transitions originating from varying lower levels simultaneously. Specifically, in order to infer the rotational and vibrational temperatures independently, all simultaneous measures of NO state-specific absorbance were computationally fit to a nonequilibrium integrated absorbance model. This model is based upon the Beer–Lambert relation as expressed in Eq. (2), applying the theoretical formulation of line strength as a function of the transition-specific Einstein $A$ coefficient state energies, and other molecular quantities as described by Hanson et al. [33].

$$A_i = \int_{-\infty}^{\infty} P_i LS_i(T) \Phi_i(T, P, \nu) \, d\nu = P_i LS_i(T)$$ (2)

The integrated absorbance $A$ is typically inferred by computationally fitting absorbance data to a representative lineshape model. In this study, the Voigt lineshape was chosen for its flexibility and accuracy at the measurement conditions observed. The Voigt lineshape model is represented by a two-parameter Gaussian–Lorentzian convolution that accounts for Doppler and pressure (or collisional) broadening.

Commonly, two-color thermometry is enabled by taking the ratio of integrated absorbance between two transitions of the target species, which is a function of temperature alone under the assumption of thermal equilibrium (i.e., $T_{rot} = T_{vib} = T_{trans}$). In this study, it was not assumed that a single temperature could define the energy distribution among absorber states. Sensitivity to multiple modal temperatures can be achieved by measuring several transitions originating from varying lower levels simultaneously. Specifically, in order to infer the rotational and vibrational temperatures independently, all simultaneous measures of NO state-specific absorbance were computationally fit to a nonequilibrium integrated absorbance model. This model is based upon the Beer–Lambert relation as expressed in Eq. (2), applying the theoretical formulation of line strength as a function of the transition-specific Einstein $A$ coefficient state energies, and other molecular quantities as described by Hanson et al. [33].

$$A_i = P_i LS_i(T) = L \frac{A_{21,i} \cdot g_{2,i}}{8 \pi c \cdot \nu_{0,i} \cdot g_{1,i}} \left(1 - \exp \left(\frac{-\nu_{0,i}}{K_B T}ight)\right)$$ (3)

Assuming a Boltzmann population distribution, the model can be expressed as a function of the absorber number density or, by further assuming the ideal gas law as in Eq. (4), the absorber partial pressure:

$$A_i = P_i \frac{A_{21,i} \cdot g_{2,i}}{K_B T_{trans} Q_i(T) \cdot 8 \pi c \cdot \nu_{0,i}} \left(1 - \exp \left(\frac{-\nu_{0,i}}{K_B T}\right)\right)$$ (4)

Here, the Einstein coefficient of spontaneous emission $A_{21,i}$ [s⁻¹], upper-state degeneracy $g_{2,i}$, lower-state energy $E_{1,i}$, and vacuum line-center width $\nu_{0,i}$ [cm⁻¹] are transition-specific parameters inferred directly from the most recent HITRAN database [34,35]. Note that a change in the units of pressure is needed for Eqs. (4) and (3); specifically pressure should be expressed in MPa instead of atm. Assuming that the rotational and vibrational energy distributions can be established independently with Boltzmann temperatures $T_R$ and $T_V$, respectively, and that translational energy remains in thermal equilibrium with rotational energy (i.e., $T_{trans} = T_R$), one arrives at the following expression:

$$A_i = P_i \frac{A_{21,i} \cdot g_{2,i}}{K_B T_R Q_i(T_R, T_V) \cdot 8 \pi c \cdot \nu_{0,i}} \left(1 - \exp \left(\frac{-\Delta E_{R,i}}{K_B T_R} + \frac{-\Delta E_{V,i}}{K_B T_V}\right)\right)$$ (5)

$E_{R,1,i}$ and $E_{V,1,i}$ are the rotational and vibrational lower-state energies, whereas $\Delta E_{R,i}$ and $\Delta E_{V,i}$ are the rotational and vibrational transition energy changes, respectively.
Of special consideration in this model were the transition-specific parameters and total partition function \( Q_i \) for NO. Though the NO HITTEMP database accounts for certain hyperfine energy level splitting (i.e., magnetic interactions finer than A doubling), at the conditions observed for this study, spectral line broadening made the corresponding transition separations unresolvable. Accordingly, certain steps were taken to avoid error in the interpretation of the spectral parameters. As expected from theory, \( g_{2,i} \) was taken as \( 2J + 1 \) (rotational level \( J \)). The total partition function was manually calculated, summing the contributions from all rotational and vibrational levels, accounting for spin-splitting and A doubling, and allowing for distinct rotational and vibrational temperatures. All hyperfine transitions in HITTEMP corresponding to a given vibrational, rotational, spin-split, and A-doubled level change (up to six) were grouped together and considered as a single rovibrational transition. The linecenter frequency of a transition grouping was taken as the mean of the individual frequencies weighted by their linestrengths, though this distinction would not significantly affect any of the measurements considering the small variance among hyperfine transition energies. The Einstein A coefficient for the transition grouping was determined by summing the reference linestrengths \( (T_{\text{ref}} = 296 \text{ K for HITTRAN}) \) and inferring the corresponding rate:

\[
A_{21,i} = \frac{S_{\text{ref},i} \cdot Q_i(T_{\text{ref}}) \cdot \pi \cdot c_i^2 \cdot \exp(-E_{21,i}/k_b T_{\text{ref}}))}{[g_{2,i} \cdot \exp(-E_{1,i}/k_b T_{\text{ref}})] \cdot [1 - \exp(-\Delta E_{21,i}/k_b T_{\text{ref}})]} \tag{6}
\]

A weighted least-squares approach was taken in computationally fitting the data to the absorbance model outlined in Eq. (5). At each time step, all \( m \) concurrent integrated absorbance measurements were considered, weighting them by their corresponding measurement uncertainties. Removing this weighting scheme would impact the best-fit parameter values by less than 5%. Equation (7) represents the relevant nonlinear minimization problem, where \( A_{\text{model},i} \) is the modeled nonequilibrium integrated absorbance of transition \( i \) as given by Eq. (5), with \( P_{\text{NO}}, T_R, \) and \( T_V \) as free variables. \( A_{\text{measured},i} \) is the measured integrated absorbance inferred from the Voigt-fitted absorbance data, and \( w_i \) is the corresponding weighting factor based on the fit certainty:

\[
\begin{bmatrix}
A_{\text{measured},1}(P_{\text{NO}}, T_R, T_V) \\
\vdots \\
A_{\text{measured},m}(P_{\text{NO}}, T_R, T_V)
\end{bmatrix}
= 
\begin{bmatrix}
A_{\text{model},1} \\
\vdots \\
A_{\text{model},m}
\end{bmatrix}
\begin{bmatrix}
w_1 \\
\vdots \\
w_m
\end{bmatrix}
= 
0
\tag{7}
\]

In practice, the inputs to this algorithm were the time-varying integrated absorbances for each measured transition and their corresponding standard errors. The outputs were the best-fit time-varying NO partial pressure, rotational temperature, and vibrational temperature, as well as the fit uncertainties of each. Species concentrations in this work are presented as partial pressures because the time-varying total flow pressure was not measured, and thus mole fractions could not be inferred accurately. The roughly homogenous core-flow diameter was taken as the effective absorbing path length, as discussed with more detail in Sec. IV. The spectroscopic line-selection details, as well as notes on treatment of spectral interference are discussed in Sec. III.

III. Spectroscopic Line Selection

NO was selected as the spectroscopic target for the primary TDLAS diagnostics employed in this study in consideration of its strong rovibrational absorption spectra and relatively high expected concentrations in the T5 freestream flow. Preliminary simulations—generated by an in-house axisymmetric reacting Navier-Stokes code (discussed in Sec. IV)—predicted NO mass fractions exceeding 5% for the 18 MJ/kg total enthalpy condition and 7% for the 8 MJ/kg total enthalpy condition. According to the nozzle code (a Navier-Stokes code discussed in Sec. IV) simulations, NO maintains a high equilibrium concentration within the hot reservoir immediately upstream of the nozzle and is chemically frozen during expansion (see Fig. 1), unable to reach the low concentration expected for equilibrated air at the freestream conditions.

Fig. 1  a) Axisymmetric Nozzle code simulations of total pressure, kinetic temperature, and NO mass fraction for the T5 nozzle at the conditions of shot 1 (see Fig. 2). b) Corresponding conditions at the exit plane as a function of nozzle radial position (radius = 15.7 cm).

Table 1  Freestream and reservoir conditions for all T5 shots operated during this study (in order of operation)

<table>
<thead>
<tr>
<th>Shot #</th>
<th>Freestream pressure, Pa</th>
<th>Freestream density, kg/m³</th>
<th>Freestream temperature, K</th>
<th>Freestream velocity, km/s</th>
<th>Reservoir pressure, MPa</th>
<th>Reservoir temperature, K</th>
<th>Reservoir enthalpy, MJ/kg</th>
</tr>
</thead>
<tbody>
<tr>
<td>1 (2903)</td>
<td>30,260</td>
<td>0.03775</td>
<td>2,575</td>
<td>5,153</td>
<td>0.0554</td>
<td>56.05</td>
<td>8,676</td>
</tr>
<tr>
<td>2 (2904)</td>
<td>8,755</td>
<td>0.02726</td>
<td>1,102</td>
<td>3,628</td>
<td>0.0766</td>
<td>20.54</td>
<td>5,149</td>
</tr>
<tr>
<td>3 (2905)</td>
<td>26,860</td>
<td>0.03192</td>
<td>2,656</td>
<td>5,299</td>
<td>0.0497</td>
<td>50.63</td>
<td>8,888</td>
</tr>
<tr>
<td>4 (2906)</td>
<td>27,530</td>
<td>0.03234</td>
<td>2,677</td>
<td>5,354</td>
<td>0.0486</td>
<td>53.40</td>
<td>8,991</td>
</tr>
<tr>
<td>5 (2907)</td>
<td>27,530</td>
<td>0.03234</td>
<td>2,677</td>
<td>5,354</td>
<td>0.0486</td>
<td>53.40</td>
<td>8,991</td>
</tr>
</tbody>
</table>

Reservoir conditions (bold) are inferred directly from measurements (with the aid of fundamental shock relations in the case of temperature and enthalpy), whereas the freestream conditions are simulated by the Nozzle code.
Targeting rovibrational absorption spectra with well-resolved transitions enabled high measurement sensitivity to the rotational and vibrational energy distributions in the freestream, and hence the corresponding modal temperatures. Specifically, the fundamental rovibrational band of NO, which is active primarily in the range of 5–6 μm (see Fig. 2), was selected because of the high transition strength and isolation (low spectral blending) at the conditions of interest, and the prevalence of relatively cheap, compact infrared (IR) laser sources, detectors, optics, etc., in that spectral region. Formally, this rovibrational system is composed of overlapping fundamental bands (∆υ = 1). Each observed individual transition within this system corresponds to a specific change in vibrational/rotational/spin-split/A-doubled/etc., level. At the conditions observed in this study, the frequency difference between paired A-doubled transitions could not be resolved (distinct peak separation) and were thus considered together. Accordingly, all NO transitions referred to in this study correspond to changes in spin-split rovibrational levels, without finer distinction.

Three lasers in total were used to probe the fundamental rovibrational bands of NO: one broadly tunable external cavity quantum cascade laser (EC-QCL) referred to here as laser 1 (numbering based on physical positioning during experimentation; see Fig. 3), and two distributed feedback quantum cascade lasers (DFB QCL), lasers 2 and 4. The total tuning ranges of these lasers are indicated by the highlighted regions in Fig. 2.

The EC-QCL, from Daylight Solutions, had a large tunable range but relatively small rapid-scanning bandwidth (scan depth); only one transition could be sampled via current-injection tuning at a rate of 10 kHz. The laser was operated at a setpoint targeting Ω = 1.5; see Table 2. Unfortunately, mode-hop issues compromised data quality for this diagnostic in all but one experiment, the single shot run (shot 2) at the lower enthalpy condition.

Lasers 2 and 4, both DFB QCLs, were capable of significantly larger scan depths at the same tuning rate, enabling simultaneous measurement of many transitions during a single experiment. Two scan setpoints were used for laser 2, one targeting the spectral range ~1900–1901 cm⁻¹ (applied in all experiments but one of the higher enthalpy shots) and the second targeting ~1897–1898.5 cm⁻¹. The first setpoint of laser 2 provided measurements of several NO transitions, covering lower vibrational levels 0 through 3, and lower rotational levels spanning J'' = 6.5 to J'' = 43.5 (see Table 2). The second setpoint of laser 2 also yielded several NO transition measurements, spanning the same lower vibrational levels and lower rotational levels J'' = 5.5 to J'' = 42.5, in addition to some unexpected CO and H₂O transitions (discussed further in Sec. IV). Laser 4 was operated under one setpoint, which provided measurements of four NO transitions, together spanning the first two lower vibrational levels and lower rotational levels J'' = 40.5 to J'' = 65.5.

In some experiments, unexpected spectral interference from CO and H₂O compromised measurements of NO transitions collected with laser 2. Specifically, R1(16.5) of the vibrational fundamental band from v'' = 1 (i.e., R-branch, J'' = 16.5, Ω = 0.5), measured with the first setpoint of laser 2, overlapped significantly with a CO transition [P(52) of the ground level fundamental band], observable in the bottom left plot of Fig. 2. The contribution of the CO transition to the integrated absorbance of the blended feature was subtracted in postprocessing, as described below. Measurements collected with the second setpoint of laser 2 included two resolvable CO transitions and a strong H₂O transition.

Fig. 2 a) Simulated NO fundamental band absorbance at conditions of a higher enthalpy shot. Shaded bar regions represent the tuning ranges of the lasers used in this study (see Table 2 and Fig. 3). b, c) Simulated absorbance across the individual rapid-scanning ranges of laser 2 (b) and laser 4 (c).
An iterative processing methodology was developed to account for unexpected CO absorption interference (encountered with the first setpoint of laser 2) so that the NO absorbance contribution to a blended feature could be estimated. First, the data from laser 2 operated under its second setpoint were processed to estimate the time-varying CO partial pressure evaluated at the measured NO temperature for that experiment. Under the assumption that the CO partial pressure was roughly consistent among the higher enthalpy shots, the CO absorbance contributing to the blended transition was inferred by evaluating at the first iteration estimate of NO temperature, as well as NO partial pressure. The inference was carried out by subtracting a smaller interfering NO transition. The integrated absorbance of the NO feature, the NO transition accessed with the second setpoint of laser 2 required subtraction of a smaller interfering NO transition. The integrated absorbance of the NO transition was simulated, evaluating at the temperature and partial pressure measured with unimpacted transitions for that experiment, and subsequently subtracted from the blended NO-H\textsubscript{2}O feature. In several other cases, transitions were blended to the extent that two or more had to be fit simultaneously, with an ultimately reduced fit certainty and a corresponding effect on the inferred temperature and partial pressures. Though these subtractions and special fitting treatments increased measurement error, the collection of measured transitions for each shot was still large enough to provide strong sensitivity to rotational and vibrational temperature, as well as NO partial pressure.

Out of a total of 17 NO transitions sampled with lasers 1, 2, and 4 across all experiments, 8 required extra corrections or subtractions or were altogether omitted due to spectral interference (i.e., transition blending). Note that those transitions that were omitted from measurements are not included in Table 2. For three of these transitions the spectral interference was caused by CO and H\textsubscript{2}O absorption. In the other cases, blending of neighboring NO transitions was responsible. Despite significant errors associated with the corrections applied to many of the measured features (discussed in Sec. IV), the sheer number of measurements coupled with the wide range of accessed vibrational and rotational levels provided adequate sensitivity to the measures of interest, namely, rotational and vibrational temperatures and NO partial pressure. Future experiments will involve a careful line selection, to minimize undesired spectral interference.

### IV. Experimental Details

The measurements presented in this study were made at the T5 reflected-shock tunnel facility, at the Graduate Aerospace Laboratories at the California Institute of Technology (GALCIT). T5 can achieve reservoir conditions of 25 MJ/kg total enthalpy and test times on the order of 1–2 ms in duration (though test times were closer to 1 ms in this study) [36]. During operation, a piston is loaded into one end of a compression tube filled with a driver gas. A secondary reservoir pressurizes the volume behind the piston, accelerating it into the driver gas to speeds in excess of 300 m/s. When a steel diaphragm ruptures, a shock wave is generated in the driven test gas (air, in these experiments). The shock wave propagates through the shock tube, then reflects from the end wall, and the twice-shocked test gas (at temperatures and pressures up to 10,000 K and 100 MPa) serves as the reservoir supply for the Mach 6 contoured nozzle used in this study.
The reflected shock propagates back upstream through the shock tube and is eventually incident on the downstream-propagating interface between the expanded driver gas and postshock test gas. A tailored condition is achieved when the reflected shock–contact surface interaction results in no reflected wave, such that the reservoir remains nominally stagnated. In an undertailored condition, a reflected expansion fan is generated and propagates back toward the nozzle throat. Although a tailored condition is ideal, in practice three-dimensional and viscous effects limit the uniform cancellation of the reflected wave. An undertailored condition can be selected to maximize the test time by delaying the arrival of the driver gas. Time test begins when the nozzle flow is established after the startup transient (typically 1 ms after the incident shock arrival at the reservoir pressure gauge, $t = 0$ ms) and is terminated by the arrival of driver gas contamination. For these experiments, TDLAS data were collected for much longer than the test time; the first 4 ms of processed data are presented here.

Five shots in total were run for this study (see Table 1): four at a repeated 18 MJ/kg stagnation enthalpy condition (enabling assessment of the facility shot-to-shot consistency), and one at an 8 MJ/kg setpoint. Freestream conditions are calculated for each run using the experimental shock speed and postreflected shock reservoir pressure as inputs into axisymmetric, reacting Navier–Stokes simulations with a five-species air model [37–39], shown in Fig. 1a. The model assumes $T_{\text{sum}} = T_{\text{rot}} \neq T_{\text{vib}}$. The code was not designed to handle a time-evolving reservoir; instead the static reservoir conditions calculated from measured shock velocity and reservoir pressure are inputs to the code. Thus, in this work, only a static (i.e., constant in time) estimation of freestream conditions is reported for comparison. The simulations indicate a well-defined core flow with highly homogenous conditions at the nozzle exit (evident in the simulated exit plane conditions displayed in Fig. 1), supporting application of the path-averaged LAS measurement scheme [i.e., removal of the path-integral from the absorbance model, Eq. (1)].

The sensor developed by Stanford for the TS freestream measurements included four lasers in total (see Fig. 3). Three of the lasers were used to probe the NO fundamental rovibrational band, together spanning vibrational levels 0–3, and rotational levels 5.5–65.5. Additionally, one laser was used to probe an excited atomic oxygen transition. Because of signal-to-noise ratio (SNR) limitations encountered with this laser, in addition to suspected drift in the tuning range of the maximum number of measurement points for a given experiment) the raw absorbance data was optimal (supported by fit residuals) while grating absorbance, and by fixing the temperature- and pressure-dependent collisional broadening width at its expected value. The time-varying integrated absorbance for each transition was smoothed with a moving-average filter (quadratic regression with a span of $\sim 10$–20% of the maximum number of measurement points for a given experiment) to mitigate the effects of spurious noise on the stability of the temperature measurements (see Fig. 5). In general, the measurement quality observed was notably high, indicated by the high SNR ($\sim 40$ at peak absorbance) of these absorbance measurements.

V. Results

The raw data collected during the experiments described above, and as displayed in Fig. 3, were converted into integrated absorbance time histories by computationally fitting the transition absorbances to a Voigt lineshape model. It was observed that Voigt fitting of the raw absorbance data was optimal (supported by fit residuals) while varying Doppler-broadening linewidth, linecenter position, and integrated absorbance, and by fixing the temperature- and pressure-dependent collisional broadening width at its expected value. The time-varying integrated absorbance for each transition was smoothed with a moving-average filter (quadratic regression with a span of $\sim 10$–20% of the maximum number of measurement points for a given experiment) to mitigate the effects of spurious noise on the stability of the temperature measurements (see Fig. 5). In general, the measurement quality observed was notably high, indicated by the high SNR ($\sim 40$ at peak absorbance) of these absorbance measurements.
As outlined in Sec. II, the measured time-varying integrated absorbance data for each transition were fit to the nonequilibrium absorbance model using a weighted least-squares approach. This model was based on the assumptions of a homogenous absorbing path length equal to the core-flow diameter (10.2 in.) and that the rotational and vibrational energy distributions were independent and Boltzmann with $T_{\text{trans}} \neq T_{\text{rot}} \neq T_{\text{vib}}$. The solving routine was improved by weighting the impact of transitions according to their individual integrated absorbance uncertainties. Figure 6 displays the results for four out of the five total experiments, presented chronologically with corresponding conditions above each plot (appearing also in Table 1). The time-varying rotational and vibrational temperatures, as well as the partial pressure of NO, are all derived from the LAS measurements of NO. For comparison, the Nozzle code static prediction of temperature and $P_{\text{NO}}$ during the approximate test time, as well as the equilibrium $P_{\text{NO}}$ simulated at each condition with seven-species air (GRI-mech 3.0 [40]), and the measured reservoir pressure (mean of two sidewall transducers) are plotted. Qualitatively, the data indicate good agreement between the rotational and vibrational temperatures, particularly during and after the nominal test time $t$ (1–2 ms). The higher enthalpy shots appear to follow a similar trend in decreasing temperature and NO partial pressure,
which is mirrored in the reservoir pressure trace as this condition was undertailored. Additionally, for all four of the higher enthalpy shots (shot 5 not shown in Fig. 6) the measured $P_{\text{NO}}$ during the test time agrees more closely with the equilibrium $P_{\text{NO}}$ than the Nozzle code prediction. The lower enthalpy shot also suggests a slightly decreasing trend in temperature and NO partial pressure, but varies comparatively less. Furthermore, there is improved agreement with the Nozzle code at the lower enthalpy condition, possibly a result of a more closely tailored reservoir. It is unknown whether improved tailoring of the higher enthalpy shot condition would improve agreement of measurements with Nozzle code. To give a sense of the maximum contribution of NO to the freestream mixture composition, the approximate peak $P_{\text{NO}}$ at the higher and lower enthalpy conditions were $\sim 1400$ and $\sim 700$ Pa, corresponding to mole fractions of $\sim 5$ and $\sim 8\%$, respectively, evaluated at the Nozzle code prediction of total pressure.

In addition to the many NO transitions successfully measured, H$_2$O and CO absorption was also observed. Though the presence of measurable quantities of these species was unexpected, it is not unprecedented in hypersonic facility freestream flows [24]. The integrated absorbance from the stronger of two resolvable CO transitions (visible in Fig. 4) is plotted against time in Fig. 7. Unfortunately, without making strong assumptions about the temperature and spatial distribution of CO and H$_2$O in the freestream, their concentrations cannot be estimated. The source of CO and H$_2$O in the test section is not yet understood. Sources of carbon include the Mylar diaphragm (which is effectively vaporized shortly after reflection of the incident shock and passes through nozzle) and any residual hydrocarbon solvents used to clean the tubes between shots. Residual hydrocarbons and ambient water adsorption to the T5 walls could potentially account for the measured freestream concentrations of H$_2$O. Absorption from ambient H$_2$O outside of the test section was observed, but was easily subtracted as a background artifact in both the transmitted and incident intensities [see Eq. (1)]. In future measurement campaigns, CO and H$_2$O absorption spectra must be considered during the line-selection process, as interference from these species proved damaging to measurement quality for some NO transitions, as outlined in Sec. III. Ultimately, the observed levels of CO and H$_2$O offer an opportunity to expand the number of spectroscopic targets measured in future freestream characterization experiments. A major goal of future measurement campaigns will be to quantitatively estimate the concentrations of CO and H$_2$O in the uniform freestream core, so that the impact of such contaminants on hypersonic flow-model experiments can be evaluated.

Table 3 lists the primary sources of measurement error, and their magnitudes, for the results presented in this section. Magnitudes of error sources are presented as a percentage of the total measurement quantity. To simplify this error analysis, all sources were assumed to act on overall measurement error independently. The error in integrated absorbance $A$ is effectively the Voigt-model fit error, including interference-subtraction uncertainty when applicable. Its magnitude was estimated computationally via Monte Carlo simulation for the

![Fig. 7 Integrated absorbance of H$_2$O (a) and CO (b), both measured with the AdTech QCL (laser 2), operating under its second setpoint, for a higher enthalpy shot (shot 4; see Table 1).](image)

Table 3 Uncertainty sources and their contributions to the typical total 1-σ error for the presented measurements

<table>
<thead>
<tr>
<th>Measurement</th>
<th>Individual source contributions to total, %</th>
</tr>
</thead>
<tbody>
<tr>
<td>$T_{\text{rot}}$</td>
<td>6 (fits) 1 Spectral parameters 1 Absorbance model fit 1 --- 1 --- 8</td>
</tr>
<tr>
<td>$T_{\text{vib}}$</td>
<td>8 1 --- 1 --- 1 --- 10</td>
</tr>
<tr>
<td>$P_{\text{NO}}$</td>
<td>4 2 1 --- 9 9 --- 16</td>
</tr>
<tr>
<td>$A_{\text{H}_2\text{O}}$</td>
<td>12 --- --- --- --- --- --- 12</td>
</tr>
<tr>
<td>$A_{\text{CO}}$</td>
<td>7 --- --- --- --- --- --- 7</td>
</tr>
</tbody>
</table>

For measurements based on integrated absorbances of NO transitions, the error assigned to $A$ includes the propagated uncertainty from all the NO transitions considered simultaneously in the absorbance model.
potential impacts from the boundary layer) with custom-built optical probing the homogenous core flow of the freestream (i.e., eliminating experiments will improve upon these measurements by directly though their concentrations cannot be accurately estimated. Future measurements. Spectral parameter error is primarily the uncertain sensitive estimation of the vibrational and rotational temperature during the first half-millisecond or so, followed shortly after by a slow relaxation toward the rotational temperature. The theoretical interpretation of this trend at early times is not yet clear, but may be attributed to the transient nature of the nozzle startup process while steady-state operation is being established. Similar to the trend in temperature, the partial pressure of NO decreases steadily across all 18 MJ flows. The results demonstrate strong evidence of equilibrium among the vibrational and rotational modes, particularly during the nominal test time and beyond. For all shots, at both nominal conditions (higher enthalpy and lower enthalpy), transient behavior in the temperature and partial pressure traces is observed during the first millisecond of nozzle flow. There appears to be a compositional onward trend in vibrational temperature during the first half-millisecond or so, followed shortl by a slow relaxation toward the rotational temperature. The trend in temperature, the partial pressure of NO decreases steadily across all 18 MJ/kg experiments. This is consistent with the under-tailored nature of this condition, also evident in the nozzle reservoir pressure traces as described in Sec. IV. 6. Future experiments will adjust this test condition to achieve a more closely tailored reservoir.

VI. Conclusions

TDLAS was employed in preliminary efforts to characterize the freestream of the GAlCIT T5 reflected shock tunnel facility operating under two nominal conditions [lower (8 MJ/kg) and higher (18 MJ/kg) stagnation enthalpy], each generating Mach ∼ 5 flows. The mid-IR laser diagnostics provided time-resolved measurements of NO absorbance from several NO rovibrational transitions, enabling quantitative estimates of NO concentration. The data demonstrate a sizeable NO population and strongly indicate thermal equilibrium of this species during and after the test period (characterized by roughly static reservoir conditions). In addition to NO, measurable quantities of CO and H₂O were also observed, though their concentrations cannot be accurately estimated. Future experiments will improve upon these measurements by directly probing the homogenous core flow of the freestream (i.e., eliminating potential impacts from the boundary layer) with custom-built optical armatures, enabling a more quantitative characterization.

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