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Ising pairing in atomically thin superconductors

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Abstract

Ising-type pairing in atomically thin superconducting materials has emerged as a novel means of generating devices with resilience to a magnetic field applied parallel to the two-dimensional plane. In this mini-review, we canvas the state of the field by giving a historical account of two-dimensional superconductors with strongly enhanced in-plane upper critical fields, together with the type-I and type-II Ising pairing mechanisms. We highlight the vital role of spin-orbit coupling in these superconductors and discuss other effects such as symmetry breaking, atomic thicknesses, etc. Finally, we summarize the recent theoretical proposals and highlight the open questions, such as exploring topological superconductivity in these systems and looking for more materials with Ising pairing.

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I. INTRODUCTION

Two years after his discovery of superconductivity, Kamerlingh Onnes envisioned that superconductors could be used for generating strong magnetic fields on the order of tens of Tesla [1]. It soon turned out that superconductors discovered in the earlier times, so-called type-I superconductors, easily lost their dissipationless property in a magnetic field with a field strength as low as tens of millitesla. It was until the discovery of type-II superconductors that Onnes' initial dream became practical. Today, scientists around the world use such superconductors to generate high magnetic fields on a daily basis in medical and research settings. The field strengths of superconducting magnets stay on the order of tens of Tesla, which are governed by a fundamental parameter of the superconductor—the upper critical field (B_{c2}). For type-I superconductors, the magnetic field either gets fully screened or penetrates through the whole compound and destroys superconductivity. A first order transition occurs at a critical field of B_c . For type-II superconductors, however, the magnetic field lines can be first trapped in a bundle of pinholes—vortices with quantized fluxes, leaving the rest of the bulk still superconducting. The onset of such a mixed state is marked by the lower critical field— B_{c1} . It is until the density of the vortices, which increases with the magnetic field, reaches a certain threshold that the superconducting state and the normal state become energetically indistinguishable. At this density with a corresponding magnetic field— B_{c2} , the superconductor returns to the normal state.

One could lift the upper bound imposed by the vortex effect by drastically reducing the cross-section of a superconductor in the magnetic field. In other words, a thin film superconductor can be much robust against an in-plane magnetic field. The Ginzburg-Landau theory predicts that such an in-plane upper critical field— $B_{c2||}$ increases rapidly with the reduction of film thicknesses [2]. In ultrathin superconductors, however, the orbital effect brought by vortices becomes negligible. Instead, the spin paramagnetism emerges as the main mechanism that brings the superconductor with singlet pairing back to the normal state. A sufficiently strong magnetic field can polarize all electronic spins such that Cooper pairs with anti-aligned spins break up [3, 4]. This magnetic field is the so-called Pauli limit: B_p . By equating the superconducting binding energy with the paramagnetic energy of the normal state, one obtains that $B_p^{BCS} = 1.86T_{c0}$ (T), where T_{c0} is the transition temperature. We add BCS in our notation because the formula above is obtained by assuming a standard BCS ratio of $2\Delta = 3.53k_B T_{c0}$ for weak superconductors and a g -factor of 2. These assumptions are not necessarily followed in realistic situations. For example, the gap to T_{c0}

ratio may be much larger than the BCS ratio [5]. On the other hand, the g -factor can differ from 2, as pointed out in literatures [6, 7]. The aforementioned effects may result in a value of B_p that deviates from B_p^{BCS} . Here, however, we employ B_p^{BCS} as a conventional tool to normalize B_{c2} such that B_{c2}/B_p^{BCS} serves as the figure-of-merit when different superconductors are compared.

In aluminum films, Tedrow and Meservey [2] demonstrated that the spin paramagnetic effect was largely obeyed, although the additional effect of spin-orbit scattering should have been taken into account. Two 5-nm thick aluminum samples, for example, possessed slightly enhanced T_{c0} of 2.04 and 2.15 K, in comparison to the bulk value of 1.2 K. Their corresponding $B_{c2,\parallel}$ were 4.01 and 4.05 T, close to the calculated B_p^{BCS} of 3.79 and 4.00 T (One exemplary data set digitized from the original paper is shown in Fig. 2a). Furthermore, the aluminum thin films hosted the predicted first-order transition to the normal state at low temperature, due to the spin-paramagnetic effect.

Since it was derived based on a simple model regarding the electronic spin, the Pauli limit can be surpassed in situations where the spin orientation departs from the ideal isotropic case. In superconducting thin films incorporated with heavy elements, spin-orbit scattering can randomize the spins and substantially weaken the polarizing effect of the magnetic field [8]. Thin films may also experience the breaking of inversion symmetry along the normal direction from the substrate to the top surface. It leads to the Rashba effect that tends to align the spins in different directions in the plane, which can essentially enhance B_{c2} up to $\sqrt{2}B_p^{BCS}$ [9]. In clean superconductors, above B_p^{BCS} , the uniformly superconducting state can get replaced by a spatially ordered state –Fulde-Ferrell-Larkin-Ovchinnikov (FFLO) state with partial spin polarizations [10, 11]. Another exotic scenario is spin triplet pairing where the system would not be affected by the Pauli paramagnetic effect at all.

By the end of 2015, it became clear that $B_{c2,\parallel}$ in the atomically thin highly crystalline superconductors [12–14] can greatly surpass B_p^{BCS} . Yet none of the aforementioned mechanisms were able to explain this enhancement. It marked the advent of so-called Ising superconductors. To date, the Ising superconductivity had been discovered in many transition metal dichalcogenides [6, 15–18], as shown in Fig. 1. Their robustness of superconductivity against the in-plane magnetic field originates from the strong spin-orbit coupling together with the breaking of in-plane inversion symmetry, as was considered earlier for non-centrosymmetric superconductors of bulk crystals [19, 20]. Lately, enhanced B_{c2} in atomically thin superconductors without breaking in-plane inversion symmetry has also been reported [21, 22] (Fig. 1). It suggests a distinct type of Ising pairing in materials with strong spin-orbit couplings hosting multi-degeneracies at high symmetry

points [23, 24]. Further theoretical work not only outlines a broader material pool of potential Ising superconductors but also suggests a possible realization of topological superconductivity in these systems [25–39].

This mini-review aims at providing a progress report of atomically thin superconductors with enhanced B_{c2} that are mostly attributed to Ising pairing (Fig. 1). Reviews on a broader scope or some other specific aspects of two-dimensional (2D) superconductors can be found in Refs [40–44]. Here we collect data points from the reported Ising superconductors, hoping to construct a unique perspective at the enhancement of B_{c2} . We discuss the influence of spin-orbit coupling strengths, sample thicknesses, etc. while ending with some open questions in the field.

II. DISCOVERY OF ISING SUPERCONDUCTORS

Thanks to technical advancements, there are now a number of viable pathways to creating ultra-thin crystals that can show superconductivity [40, 42]. One direction is to directly synthesize thin films of a material, for example through molecular beam epitaxy (MBE). Another is through mechanical exfoliation where sheets of van der Waals materials can be isolated down to a few atomic layers. Alternatively, it is possible to study the physics of thin layers by selectively accumulating carriers on the surface of bulk crystals, for example with ionic liquid (IL) gating. The enhanced $B_{c2,\parallel}$ has become one intriguing property of these 2D superconductors. Here we give a historical account of selected 2D superconductors with enhanced $B_{c2,\parallel}$. Figure 1 acts to guide our discussion by plotting the ratio of $B_{c2,\parallel}/B_p^{BCS}$ from reports in the literature according to their publication date.

In a 2012 systematic study of δ -doped SrTiO₃ heterostructures, Kim et al. [45] noted that $B_{c2,\parallel}(T \rightarrow 0)$ exceeded B_p^{BCS} by a factor of 4. We show one exemplary data set digitized from the original paper in Fig. 2e. An earlier study on LaAlO₃/SrTiO₃ interface superconductors [46] already found a large $B_{c2,\parallel}/B_p^{BCS}$ ratio of 3.5. The δ -doped films embedded between cap and buffer layers of SrTiO₃ has the advantage due to its symmetric structure. It helps exclude the Rashba effect as the mechanism for the enhancement. For a quantitative analysis, Kim et al. [45] employed the Werthamer-Helfand-Hohenberg (WHH) formula:

$$\ln\left(\frac{T_{c0}}{T}\right) = \left(\frac{1}{2} - \frac{i\lambda_{SO}}{4\gamma}\right) \psi\left(\frac{1}{2} + \frac{\bar{h} + \frac{1}{2}\lambda_{SO} - i\gamma}{2T/T_{c0}}\right) + \left(\frac{1}{2} + \frac{i\lambda_{SO}}{4\gamma}\right) \psi\left(\frac{1}{2} + \frac{\bar{h} + \frac{1}{2}\lambda_{SO} + i\gamma}{2T/T_{c0}}\right) - \psi\left(\frac{1}{2}\right), \quad (1)$$

where ψ is the digamma function and the rest of the terms are:

$$\bar{h} = \frac{ev_F^2\tau_T B}{3\pi k_B T_{c0}}, \quad (2)$$

$$\lambda_{SO} = \frac{2\hbar}{3\pi k_B T_{c0}\tau_{SO}}, \quad (3)$$

$$\gamma = \sqrt{\left(\frac{\mu_B B}{\pi k_B T_{c0}}\right)^2 - \frac{1}{4}\lambda_{SO}^2}, \quad (4)$$

where v_F is the Fermi velocity, τ_T/τ_{SO} the transport/spin-orbit scattering time, μ_B the Bohr magneton. With the sample getting thinner, they found an unusual decrease of the extracted τ_{SO} while τ_T stayed almost unchanged. This dichotomy suggested that the intrinsic spin-orbit coupling may play a role in giving rise to the large $B_{c2,\parallel}(T \rightarrow 0)/B_p^{BCS}$ ratio.

Indications for the intrinsic effect of spin-orbit coupling were also found in 2013. Sekihara, Masutomi and Okamoto studied submonolayer of Pb films grown on GaAs(110) substrate [47] (Fig. 2e). There, the superconducting transition temperature dropped by as little as 2% in the in-plane magnetic field up to 14 T. The following equation was employed to fit the data:

$$\ln\left(\frac{T_{c0}}{T}\right) = \psi\left(\frac{1}{2} + \frac{3\tau_{SO}(\mu_B B)^2}{2\hbar 2\pi k_B T}\right) + \psi\left(\frac{1}{2}\right). \quad (5)$$

This equation is usually referred to as the Klemm-Luther-Beasley (KLB) formula [8]. It can be derived from Eq. (1) when considering strong spin-orbit scattering for superconductors in the dirty limit, i.e. $\lambda_{SO} \rightarrow \infty$ and $\tau_T \ll \tau_{SO}$. The extracted τ_{SO} was found to be comparable with the estimated τ_T of the Pb films: $\tau_T \sim 0.8\tau_{SO}$. This is unusual because τ_{SO} should be orders of magnitude larger than τ_T . The authors therefore proposed that the intrinsic Rashba spin splitting in their system may give rise to an inhomogeneous superconducting state similar to the FFLO state, which might account for the enhanced $B_{c2,\parallel}$. A similar conclusion was arrived by Nam et al. [48] when studying their five-monolayer Pb films grown on Si(111) substrates. The researchers suggested that the orbital effect, which is often neglected when considering purely a 2D superconductor, may be still responsible for pair-breaking because the spin degree of freedom is quenched. It highlights the importance of a close inspection of theoretical expectation of $B_{c2,\parallel}$ from different mechanisms.

The breakthrough of identifying a novel mechanism different from Rashba spin splitting or spin-orbit scattering happened in 2015/16. Three individual groups observed strongly enhanced $B_{c2,\parallel}$ in their atomically thin superconductors of 2H-MoS₂ (Ref.[12 and 13]) or 2H-NbSe₂ (Ref.[14]) (Fig. 2a). Experimentally, the researchers obtained atomically thin crystalline superconductors via two approaches. For thin flakes of 2H-MoS₂, Lu et al. [12] and Saito et al. [13]

employed the ionic liquid gating technique to electrostatically inject charge carriers and tune the top one to two layers into the superconducting state. On the other hand, Xi et al. [14] were able to mechanically exfoliate 2H-NbSe₂ down to a monolayer and still preserve the superconductivity. They found that $B_{c2,\parallel}$ exceeded B_p^{BCS} by a factor of 4 to 6. Notably, the extracted τ_{SO} by using Eq. (5) to fit the data became shorter than τ_T . This is unreasonable because the transport scattering time should be the shortest. By ruling out the spin-orbit scattering mechanism, the researchers proposed an intrinsic mechanism. It arises from the strong spin-orbit coupling together with the lack of in-plane inversion symmetry in the individual atomic layers of MoS₂ and NbSe₂. Taking a monolayer of MoS₂—one S-Mo-S sequence—for an example, its band structure consists of electron pockets located around the K and K' points of the Brillouin zone. Strong spin-orbit coupling induces spin splitting of the bands. Due to the broken inversion symmetry of its crystal structure, the spin splitting has opposite signs at the K and K' points. In the superconducting state, Cooper pairs are built up by the electrons from the two valleys. Their spins are locked to the out-of-plane direction due to the rotational symmetry. This is schematically shown in Fig. 1. An in-plane magnetic field therefore has to compete with the Zeeman-like spin splitting built into the bands, thus the superconducting state becomes more resilient to the paramagnetic effect. Such a mechanism in 2D superconductors is called Ising superconductivity.

In fact, an enhanced $B_{c2,\parallel}$ over the Pauli limit was proposed earlier in bulk crystals without symmetry centers—noncentrosymmetric superconductors by Bulaevskii, Guseinov, and Rusinov [19] as well as by Frigeri et al. [20]. By employing the specific Hamiltonian suitable for transition metal dichalcogenide monolayers, Ilic, Meyer and Houzet [49] derived the following formula for the temperature dependence of the upper critical field for Ising superconductivity:

$$\ln\left(\frac{T_{c0}}{T}\right) = \frac{\mu_B^2 B^2}{\beta_{SO}^{*2} + \mu_B^2 B^2} \text{Re} \left[\psi \left(\frac{1}{2} + \frac{i \sqrt{\beta_{SO}^{*2} + \mu_B^2 B^2}}{2\pi k_B T} \right) - \psi \left(\frac{1}{2} \right) \right], \quad (6)$$

where β_{SO}^* is the effective spin-orbit coupling strength, which may be renormalized from the intrinsic spin-orbit coupling by the disorder scattering [5].

The concept of Ising superconductivity was further bolstered by the subsequent studies of other transition metal dichalcogenides monolayers. In a WS₂ monolayer, superconductivity was again realized by the ionic liquid gating technique [15]. There, for the superconducting state with $T_{c0} = 1.54$ K, Lu et al. found that the transition temperature only decreased by 5% when a strong in-plane magnetic field of 35 T was applied [15](Fig. 2b). In a monolayer exfoliated from 2H-TaS₂ crystals,

de la Barrera et al. found that $B_{c2,\parallel}$ exceeded the highest magnetic field of their magnet (34.5 T) when the temperature was below 60% of T_{c0} [16] (Fig. 2b). They further carried out a systematic study by comparing the enhanced $B_{c2,\parallel}$ in both TaS₂ and NbSe₂. The larger $B_{c2,\parallel}/B_p^{BCS}$ ratio in TaS₂ originated from its stronger spin-orbit coupling strength, which was consistent with the density functional theory calculations. Enhanced $B_{c2,\parallel}$ was also found in monolayer WTe₂ [50, 51] as well as few-layers of 1T_d-MoTe₂ [52] (Fig. 2f). A variant of Ising superconductivity was proposed that considered the tilted spins in the momentum space. Recently, Rhodes et al. [53] further observed enhanced $B_{c2,\parallel}$ in a monolayer of MoTe₂. These materials suggest a broader scope for locked spins in superconductors with strong spin-orbit couplings [54].

We remark that there exist two different approaches for estimating the spin-orbit coupling strength for Ising pairing. Some studies employed Eq. (5) for fitting their data but interpret $3\hbar/2\tau_{SO}$ as β_{SO} [14, 16]. Others used the formula for Ising superconductivity—similar to Eq. (6)—to extract β_{SO}^* [12, 15]. Due to the completely different origins, the fitted values can greatly differ. For example, applying Eq. (5) directly to the data of MoS₂ (orange curve in Fig. 2a) gives rise to $3\hbar/2\tau_{SO} = 18$ meV. By contrast, the best fit to the same data set by using Eq. (6) yields $\beta_{SO}^* = 3.4$ meV. This value is slightly smaller than the reported value of 6 meV in literature [12]. This difference stems from the fact that Eq. (6) does not take into account the Rashba effect. Another example is NbSe₂. Applying Eq. (6) to the data set in Fig. 2a gives rise to $\beta_{SO}^* = 4.1$ meV, which is much smaller than the reported value: $2\beta_{SO} = 76$ meV [14] when Eq. (5) was employed. One should therefore be cautious in drawing comparison between the spin-orbit coupling strengths based on the listed values in the literatures.

Figure 3 compares attributes of transition metal dichalcogenide superconductors based upon their layer number and chemical composition. We draw upon two key parameters; the thickness of samples studied and the cation size. While the data set is incomplete, a trend is visible in both graphs. The $B_{c2,\parallel}/B_p^{BCS}$ ratio is enhanced by both thinning the sample (Fig. 3a) and enhancing the cation size (Fig. 3b). Thinning the sample, preferably to the monolayer limit, is necessary to realize the inversion symmetry breaking of the lattice. It is nevertheless important to note that the enhancement in the upper critical field persists even in multi-layered NbSe₂ and TaS₂. It indicates that the local inversion symmetry breaking in the plane is sufficient for spin-orbital locking, although the global inversion symmetry is not broken in multi-layer systems. The effect of cation is associated with the increase in spin-orbit coupling with its increasing Z value, which enters the superconducting behavior in the form of β_{SO}^* . The data in Fig. 3 also highlight that the enhanced

$B_{c2,\parallel}$ is a reproducible result. Three independent studies of NbSe₂ [6, 14, 16] present similar values of $B_{c2,\parallel}/B_p^{BCS}$ at the lowest measured temperatures, along with the value obtained at $T = 0$ through a KLB fit. Notably, one of the studies explored the macroscopic NbSe₂ sample grown by MBE [6]. The authors employed a pulsed magnet in combination with ultra-low temperature facility to experimentally determine $B_{c2,\parallel}/B_p^{BCS}$ down below $0.15T_{c0}$. The large enhancement in MBE grown samples is of technical importance for further investigations of Ising pairing and potential applications.

Among the transition metal dichalcogenide superconductors, a missing feature of Ising superconductivity predicted by theory was the up-turn behavior of $B_{c2,\parallel}$ at low temperature as described by Eq. (6). In monolayer cases of NbSe₂ and TaS₂ [14, 16] as well as in the ionic liquid gated WS₂ [15], the upper critical field quickly exceeded the highest magnetic field available when the temperature is still close to T_{c0} , such that the behavior of $B_{c2,\parallel}$ at $T \rightarrow 0$ was unattainable. For bilayer NbSe₂, trilayer TaS₂, as well as ionic liquid gated MoS₂ [13], on the other hand, $B_{c2,\parallel}$ showed a saturating behavior at $T/T_{c0} < 0.5$. It was suggested that the Rashba effect [12, 13] and intervalley scattering [49] in these films can renormalize the temperature behavior so that the up-turn at low temperature gets smeared out.

The non-saturating behavior was first found in a two-dimensional superconductor outside the transition metal dichalcogenide family. This time, samples grown by MBE became the protagonist. Liu et al. measured thin films of Pb grown on a special surface reconstruction layer of Pb-stripped incommensurate phase on Si(111) substrate. They observed pronounced enhancement of $B_{c2,\parallel}$ [5]. There, a more realistic B_p rather than B_p^{BCS} was estimated based on the known gap to T_c ratio of Pb. Intriguingly, they observed that $B_{c2,\parallel}$ in the Pb films with a thickness of six monolayers kept increasing with decreasing temperature down to $T \sim 0.25T_{c0}$ (Fig. 2b). Although the crystal structure of Pb itself is centrosymmetric, the authors pointed out that their special substrate hosted lattice distortion with its symmetry breaking effect permeating to thin films grown on top. Together with the strong spin-orbit coupling, ultrathin Pb films therefore possessed Ising superconductivity.

In another elemental superconductor—Sn, Liao et al. [55] found that $B_{c2,\parallel}$ could exceed B_p^{BCS} by a factor of 3. Their superconductors were made of a few atomic layers of strained α -Sn—so-called stanene—grown by MBE on PbTe/Bi₂Te₃ epitaxial layers upon a silicon (111) substrate. By measuring few-layer stanene at even lower temperatures down to $0.02T_c$, Falson et al. [21] were able to map out almost the complete phase diagram of $B_{c2,\parallel}(T)$. The same sample, as studied in Ref. [55] actually hosted an ever-growing $B_{c2,\parallel}$ as T decreased such that $B_{c2,\parallel}/B_p^{BCS}$ eventually

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 3 exceeded 4 (Fig. 2c). Of particular interest, was the up-turn behavior at low temperature, which
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 5 echoed the prediction for Ising superconductivity [Eq. (6)]. However, stanene is sharply different
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 7 from NbSe₂ or MoS₂: its crystal structure is centrosymmetric; the electronic bands are around
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 9 the Γ point, as found by angular resolved photoemission spectroscopy (ARPES). The criteria of
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 11 the then established Ising superconductivity were not satisfied. A new theoretical framework was
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 13 proposed to explain this distinct type of behavior—type-II Ising superconductivity [23, 24]. Their
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 15 theory was applicable to centrosymmetric materials with multiple degenerate orbitals. Taking
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 17 Sn for example, bands around the Fermi level stem from p_x and p_y orbitals. Without spin-orbit
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 19 interactions, the orbitals have four-fold degeneracy at the Γ point: $|p_x\rangle$, $|p_y\rangle$, spin-up ($|\uparrow\rangle$) and
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 21 spin-down ($|\downarrow\rangle$). The spin-orbit coupling lifts one layer of degeneracy and gives rise to two sets
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 23 of bands: $(|p_x + ip_y, \uparrow\rangle, |p_x - ip_y, \downarrow\rangle)$ and $(|p_x - ip_y, \uparrow\rangle, |p_x + ip_y, \downarrow\rangle)$. Here the effective Zeeman
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 25 splitting occurs between $|p_x \pm ip_y, \uparrow\rangle$ and $|p_x \pm ip_y, \downarrow\rangle$. This spin-orbit locking effect produces
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 27 essentially the same spin configurations required by Ising superconductivity, and is schematically
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 29 shown in Fig. 1. Based on this argument, Falson et al. [21] demonstrated that their theoretical
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 31 model could satisfactorily fit the experimental data. Moreover, the model also explained why the
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 33 up-turn was not always prominent even for the same triple layer Sn but on PbTe with different
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 35 thicknesses (Fig. 2c). It stemmed from the enhanced spin-tilting of the hole band as the Fermi
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 37 momentum increased with thinner PbTe. To further confirm this scenario, it is desirable to carry
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 39 out a more systematic study of the enhanced $B_{c2,\parallel}$ as a function of the Fermi level. We further
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 41 note that few-layer stanene constitutes a unique platform as properties close to $T/T_{c0} = 0$ can be
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 43 addressed. Future experiments should be directed to the understanding of the transition from the
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 45 purely paramagnetism dominated regime to the orbital effect dominated regime.

42 In fact, there exists not just one type-II Ising superconductor. In ultrathin PdTe₂ grown by
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 44 MBE, Liu et al. [22] observed largely enhanced $B_{c2,\parallel}$, exceeding B_p by a factor of 6-8 (Fig. 2d).
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 46 Notably, the PdTe₂ compound also has a centrosymmetric crystal structure and hosts electronic
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 48 bands around Γ point. Theoretical analysis pointed out that the enhanced $B_{c2,\parallel}$ was caused by
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 50 type-II Ising pairing. Notably, few-layer stanene and PdTe₂ are quite robust against air-exposure.
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 52 By contrast, ultrathin NbSe₂ and TaS₂ are quite fragile and require handling in glove-boxes and
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 54 capping with protection layers. In retrospect, the enhanced in-plane upper critical field in liquid
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 56 gated SnSe₂ as well as 1T'-MoS₂ also might be accounted for by type-II Ising paired superconduc-
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 58 tivity [23, 56]. Together, these recent findings highlighted a broader scope of 2D superconductors
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 60 hosting largely enhanced $B_{c2,\parallel}$ due to the strong spin-orbit coupling.

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3 Following the initial experimental discoveries, further theoretical analysis suggests more exotic
4 physics lurking in Ising superconductors, with the in-plane magnetic field as a tuning parameter.
5 In order to experimentally verify many of the predictions, it is important to obtain information
6 beyond temperature and magnetic field dependent resistances. Attempts to reveal the density of
7 states in Ising superconductors have provided fruitful results. Both Sohn et al.[57] and Dvir et
8 al.[58] fabricated planar tunnel junctions on NbSe₂ down to a trilayer. Either a few layers of MoS₂
9 or a thin film of AlO_x were used as the barrier. On the other hand, Costanzo et al. [59] utilized
10 the band bending in the liquid gated MoS₂ on multilayer graphene to realize a superconductor-
11 insulator-metal junction. All three groups found that the superconducting gap could be protected
12 by spin locking and stayed almost constant at small in-plane magnetic fields below around 10
13 T. Intriguingly, as revealed by Sohn et al., the gap gets continuously suppressed by ramping up
14 the in-plane magnetic field to about 38 T, rather than a first-order phase transition expected for
15 a BCS superconductor [57]. The continuous transition lends further support to the scenario of
16 Ising superconductivity. Due to the strong spin-locking of the Ising superconductor, its in-plane
17 spin susceptibility in the superconducting state stays comparable to that in the normal state. The
18 free energy of the superconducting state therefore continuously connects to that of the normal
19 state. Further exploring the potential of planar junctions, Kang et al. [60] fabricated a sandwich
20 structure consisted of NbSe₂/CrBr₃/NbSe₂ (CrBr₃ is a ferromagnetic insulator). They observed
21 nearly 100% tunneling anisotropic magnetoresistance.
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39 III. OUTLOOK

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42 One enticing property of Ising superconductors is the predicted non-trivial topology. Indi-
43 cations of unconventional pairing were recently found in few-layer NbSe₂, which manifested as
44 two-fold anisotropy in the in-plane upper critical field [61]. In fact, possible *p*-wave pairing was
45 predicted theoretically for a monolayer of MoS₂ before the strongly enhanced $B_{c2,\parallel}$ was experi-
46 mentally observed [62]. A spin triplet *s*-wave was also proposed for certain on-site and nearest
47 neighbor interaction strengths. Möckli and Khodas predicted that the in-plane magnetic field may
48 induce nodes in the dispersion with Majorana flatbands connecting them, giving possibility of re-
49 alizing nodal topological superconductivity [31]. Similar conclusion was arrived by He et al. [29].
50 By further taking into account the possible Rashba splitting in monolayer NbSe₂, Shaffer et al. [35]
51 predicted that the system may enter a topologically trivial phase unless the in-plane magnetic field
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3 is applied along one of Γ - K lines, where a crystalline topological superconducting phase occurs.
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5 It was also proposed that nodal topological phases could be achieved in magnetic islands placed
6
7 on Ising superconductors [36].

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9 As already alluded to, triplet pairing is another intriguing property that may accompany Ising
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11 superconductivity. Möckli and Khodas [31, 32] suggested that the superconducting state in mono-
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13 layer TMD becomes parity mixed with triplet pairing—particularly the f -wave. The mixing of
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15 singlet and triplet pairing in monolayer NbSe₂ was also confirmed by Wickramaratne et al. [34]
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17 through density functional theory (DFT) calculations. This triplet pairing may account for the
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19 further enhancement of $B_{c2,\parallel}$ and can still persist when disorder effect is taken into account [33]. It
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21 can also affect the density of states [63]. A recent experimental study on the superconducting gap
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23 has indeed unveiled indication of such triplet pairing [64].

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25 However, the triplet pairing may get masked by the dominant singlet pairing. Several theoret-
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27 ical groups thus outlined ways to extract the triplet pairing component. Zhou et al. [25] proposed
28
29 that the triplet pairing in Ising superconductors can induce Majorana fermions in a semi-metal
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31 wire via proximity effect. The configuration is similar to the case of nano-wires with strong Rash-
32
33 ba splittings that are proximitized by conventional s -wave superconductors [65]. However, the
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35 spin directions for the proposed semi-metal wire on a Ising superconductor lie in-plane instead
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37 of out-of-plane. The induced superconductivity was further proven to be robust against the in-
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39 plane Zeeman fields [66]. In a similar spirit, spin triplet Andreev reflection was proposed to occur
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41 between a ferromagnet-Ising superconductor junction [30]. An in-plane junction made of Ising
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43 superconductor-ferromagnet-Ising superconductor may further allow the spin triplet Josephson
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45 current to pass [67]. However, constructing such an in-plane junction may require technical inge-
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47 nuity. In general, heterostructures involving Ising superconductors serve as test-beds not only for
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49 further validating Ising pairing but also for achieving exotic properties.

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51 Experiments have shown that the spin-locking effect persists even in bilayer or trilayer of NbSe₂
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53 superconductors, for example. It indicates that the local inversion symmetry breaking is sufficient
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55 for Ising superconductivity, even though the material itself is globally centrosymmetric. By con-
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57 sidering the bilayer case, Liu [27] as well as Nakamura and Yanase [28] predicted that odd-parity
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59 superconductivity may occur. This unconventional superconductivity manifests itself either as an
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inhomogeneous FFLO state or a pair-density-wave state under an in-plane magnetic field. How-
ever, it is experimentally quite challenging to detect these exotic states. The current techniques for
measuring the FFLO state are often developed for bulk materials. Detecting the pair-density wave

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3 further requires the understanding of the local density of states in these ultrathin superconductors
4 by using scanning tunneling microscopy (STM).
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7 Carrying out tunneling spectroscopy on Ising superconductors is still under-explored. Many
8 predicted properties such as a "mirage" gap at high energies of the order of β_{SO} [38] remain to be
9 verified. It is also of particular interest to obtain the density of states in the regime where the tem-
10 perature dependent $B_{c2,\parallel}$ shows an up-turn, such as in 6-Pb, few-layer stanene, as well as PdTe₂.
11 Theories predicted unconventional pairing and possible topological properties in this regime. Fur-
12 thermore, it is favorable to probe the local density of states. Theoretically, the interplay between
13 Ising superconductors and magnetic impurities were considered by Sharma and Tewari [26] as
14 well as by Zhang et al. [37]. They predicted features that could be identified by STM. Here we
15 list some of the technical challenges of STM investigation on Ising superconductors and possible
16 solutions: 1. Many Ising superconductors are mechanically exfoliated flakes with typical sizes
17 of tens of micrometers. Specially designed markers [68] or optical lens [69] may be necessary
18 to help locate the flake with the tunneling tip. Alternatively, a macro-scale sample, realized for
19 example by MBE, may be favorable; 2. the ionic liquid gating employed, for example in inducing
20 superconductivity in MoS₂ and WS₂ Ising superconductors, is incompatible with STM. One may
21 employ alternative gating methods with similarly charge carrier tunability, such as ionic solid/gel
22 gating [70, 71]; 3. the exotic phases of Ising superconductors, predicted by theory, often occur
23 at an in-plane magnetic field beyond the Pauli limit. To clearly probe into these phases, it may
24 also be necessary to measure down to low temperature such that $T/T_{c0} < 0.5$. The combination
25 of these requirements make the STM measurement a formidable task. One feasible route may be
26 to realize Ising superconductors with lower T_{c0} such that $B_{c2,\parallel}$ stays in the range offered by a com-
27 mercially available magnet. Reduction of T_{c0} can be achieved by modulating the carrier density in
28 the existing Ising superconductors.
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46 In order to expand the experimental tools used for studying Ising superconductivity, one may
47 also need to search in the material pool for new systems [39]. There exist several reasons for this
48 proposal. First, many of the existing Ising superconductors require very high magnetic field to in-
49 duce the predicted exotic states. This is sometimes challenging to be incorporated with other tech-
50 niques such as STM. Second, nuclear magnetic resonance and thermal capacitance measurements,
51 which are powerful in identifying the FFLO state, may not be easily applied to those atomical-
52 ly thin superconductors. Superlattices, where superconducting sheets are protected by insulating
53 layers, as recently demonstrated by Devarakonda et al. [72] may provide one feasible route. This
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3 expands the approach to encompass looking for bulk crystals with a stack of Ising superconduc-
4 tors separated by effectively inert layers [73]. Apart from the type-I Ising superconductors that
5 require inversion symmetry breaking, type-II Ising superconductors rely on spin-orbit coupling
6 induced band splittings around high-symmetry points. By using this guiding principle, Wang et
7 al. [23] looked into the database of 2D materials and found a batch of potential candidates for
8 type-II Ising superconductivity, as shown in Fig. 4. This approach was based upon parameterizing
9 the strength of spin-orbit coupling vs Fermi momentum (carrier density). It was taken without
10 significant regard for whether the predicted density could be realized (many materials are in fact
11 semiconductors) or whether a material is actually superconducting. Nevertheless, a number of
12 interesting synthesis paradigms are revealed. While chalcogenides have a relatively rich history
13 of study, the properties of halides are remain relatively poorly explored, especially in the context
14 of thin films, which is the only viable path to making samples sufficiently thin if flakes can not
15 be exfoliated from larger crystals. In general, Ising superconductivity is a vibrant field that has
16 just shown its tip of an iceberg. Experiments led in the beginning, followed by theoretical under-
17 standings and predictions for novel physics. Now it is back to the task of experimentalists to probe
18 deeper and wider into this budding field.
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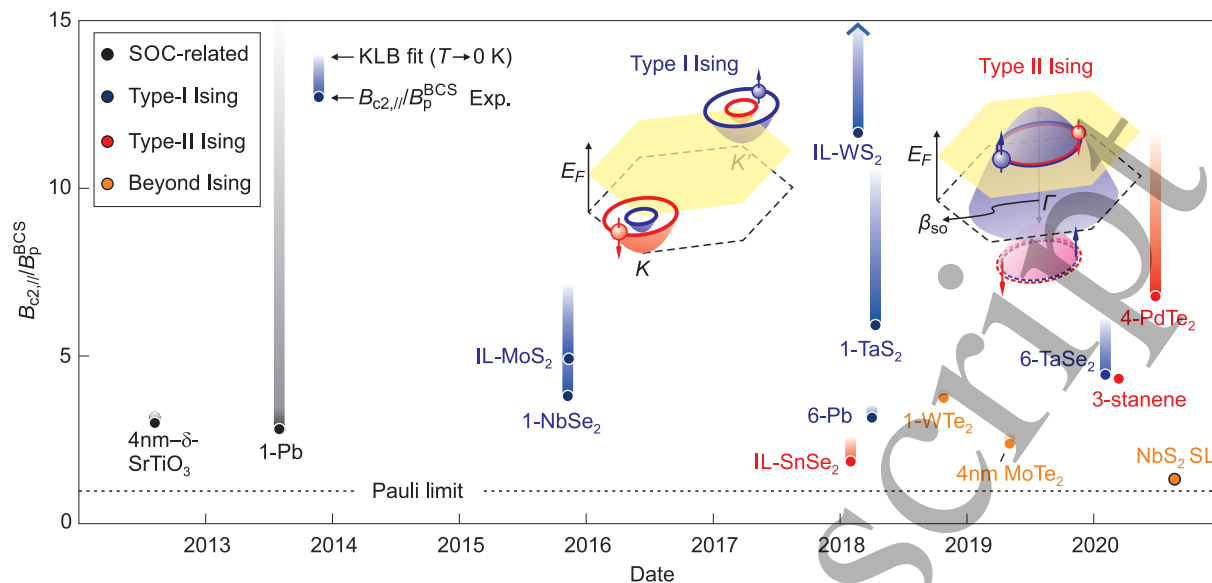


FIG. 1. **Two-dimensional superconductors with enhanced in-plane upper critical fields.** Black: spin-orbit coupling (SOC) related systems [45, 47], Blue: Type-I Ising superconducting materials [5, 12, 14–16, 18, 74]. Red: Type-II Ising superconducting materials [21, 22]. Orange: "beyond" Ising-type superconductivity [50–52, 72]. The solid symbols present the experimentally measured $B_{c2,||}/B_p^{BCS}$ ratio in each reference, which is often limited by the magnet field available. The upper bound of the faded bar indicates the extrapolated $B_{c2,||}/B_p^{BCS}$ ratio at zero temperature according to the KLB fit to the temperature dependent upper critical field (shown for example in Fig. 2). For triple layer stanene (3-stanene) and NbS₂ in a superlattice (NbS₂-SL), the measurements were carried down to temperature close to absolute zero such that the extrapolation is no longer necessary. Note that the value for WS₂ exceeds the vertical axis limit of 15. Here, "IL" corresponds to ionic liquid gated samples and the number preceding the chemical tag indicates the number of monolayers or total thickness of the device. Dashed line marks the Pauli limit. Schematic drawing as insets illustrate the band structure with spin-splitting for two types of Ising superconductivity. For type-I Ising, only one pair of bands around the K/K' points is shown.

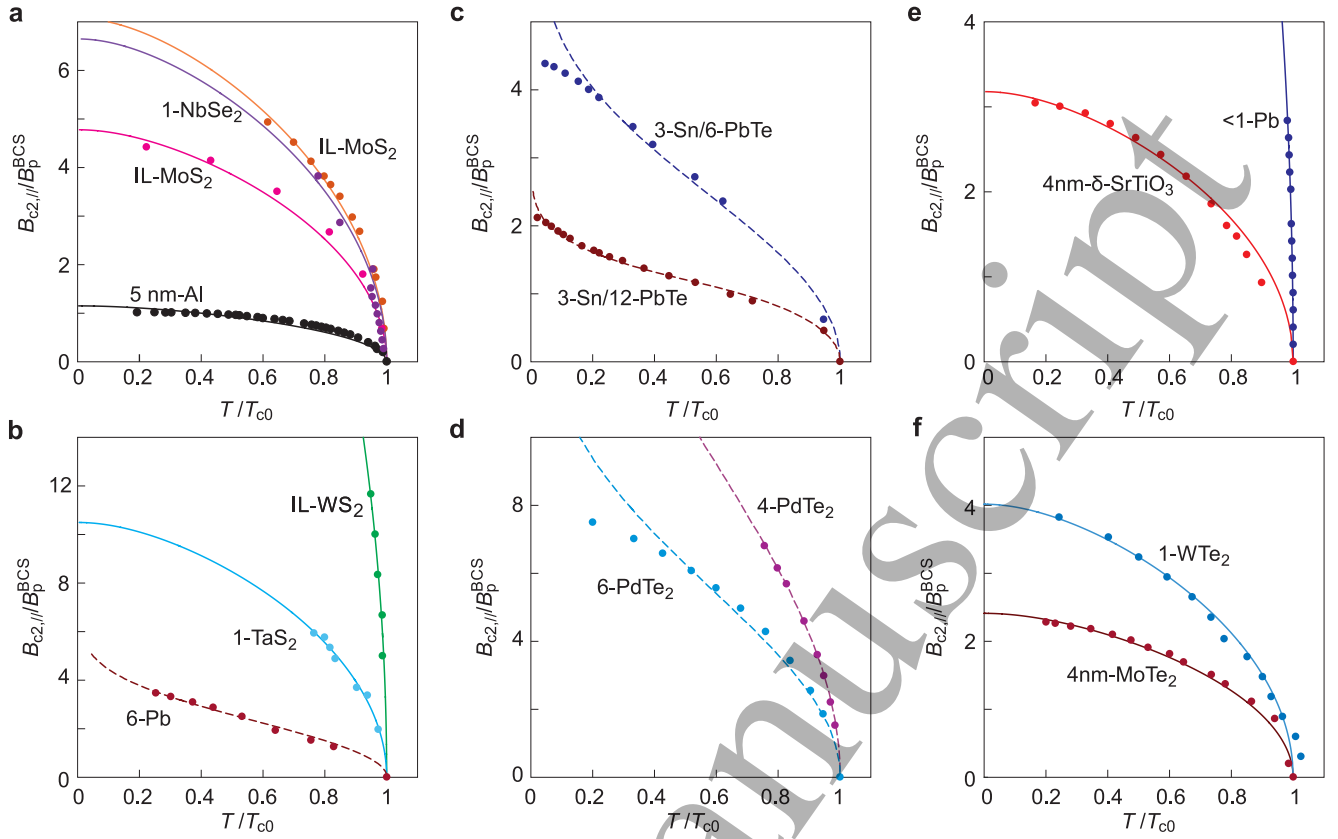


FIG. 2. **In-plane upper critical fields of selected two-dimensional superconductors.** Circles are data points digitized from the corresponding references (a: Refs. [2, 12–14]; b: Refs. [15, 16, 27]; c: Ref. [21]; d: Ref. [22]; e: Refs. [45, 47]; f: Refs. [50, 52]). Panels a and b include data from several type-I Ising superconductors. Data points for the thin aluminum are shown for comparison. Panels c and d include data from type-II Ising superconductors. Panels e and f show data from other 2D superconductors in which the enhanced $B_{c2,||}$ stems from strong spin-orbit coupling effect. Solid curves are theoretical fits by using the KLB formula [Eq. (5)]. Dashed curves are fits by using the formula for Ising superconductors [Eq. (6)]. In panels c and d, deviation between the dashed curve and the data points at low temperatures indicates that the additional Rashba effect need to be taken into account.

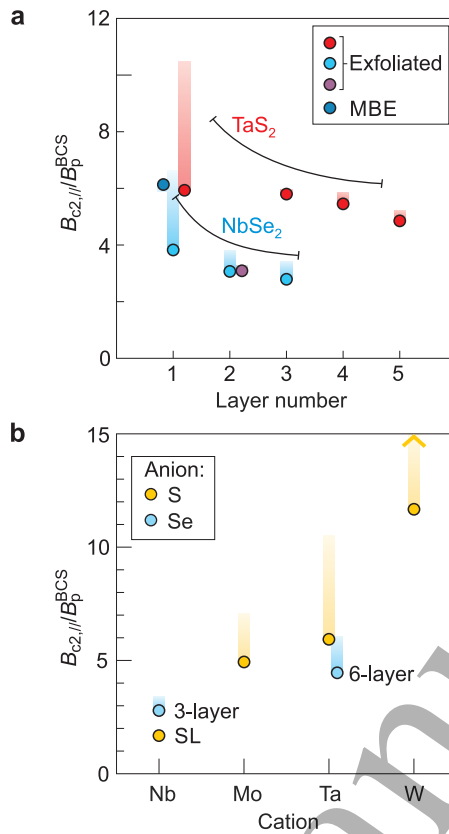


FIG. 3. **Enhancement of the in-plane upper critical fields in selected transition metal dichalcogenide superconductors.** Comparison of $B_{c2,||}/B_p^{BCS}$ as **a** a function of layer number for TaS₂ [16] and NbSe₂ [6, 14, 16], and **b** a function of cation [12–16, 18, 72]. The extrapolated $B_{c2,||}/B_p^{BCS}$ value for WS₂ exceeds the vertical axis limit of 15. The value for NbS₂ is taken from the measurement on a superlattice (SL) consisting of NbS₂ layers [72]. The relatively small value here may also be influenced by the strong Rashba effect present in the system. For selenide compounds, we compare a six-layer TaSe₂ in the 3R-phase—the thinnest one reported with a trilayer of 2H-NbSe₂, because data from thicker NbSe₂ is not available.

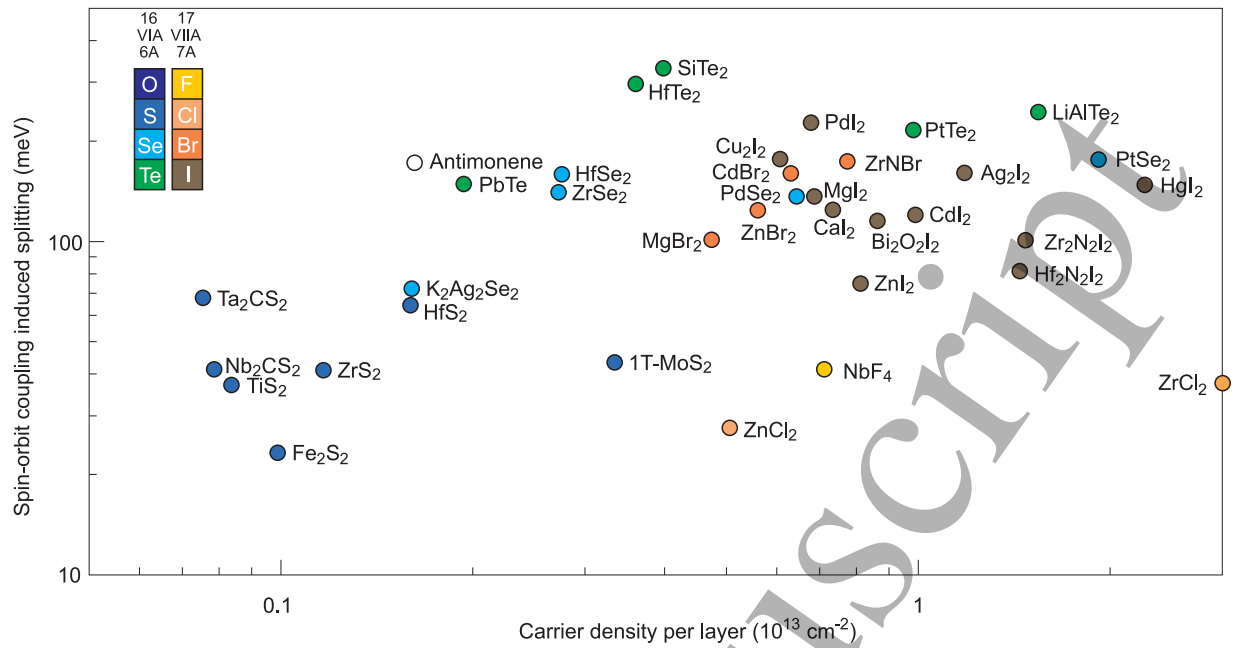


FIG. 4. **Predicted Type-II Ising superconductors.** Material platforms color coded according to anion type as a function of carrier density per layer and spin-orbit coupling induced splitting. Data points are from Ref. 23. It was proposed that the Fermi level should be tuned such that the carrier density stays below the listed values to possess pronounced enhancement. Note that ZrCl₂ possesses large splitting across the whole momentum space.