Wave-driven Mass Loss of Stripped Envelope Massive Stars: Progenitor-dependence, Mass Ejection, and Supernovae

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Received 2021 September 17; revised 2021 September 30; accepted 2021 October 1; published 2021 December 9

Abstract

The discovery of rapidly rising and fading supernovae powered by circumstellar interaction has suggested the pre-supernova mass eruption phase as a critical phenomenon in massive star evolution. It is important to understand the mass and radial extent of the circumstellar medium (CSM) from theoretically predicted mass ejection mechanisms. In this work, we study the wave heating process in massive hydrogen-poor stars, running a suite of stellar models in order to predict the wave energy and pre-explosion timescale of surface energy deposition. We survey stellar models with main-sequence progenitor masses from 20–70 $M_{\odot}$ and metallicity from 0.002–0.02. Most of these models predict that less than $\sim 10^{47}$ erg is deposited in the envelope, with the majority of the energy deposited in the last week of stellar evolution. This translates to CSM masses less than $\sim 10^{-2} M_{\odot}$ that extend to less than $\sim 10^{14}$ cm, too small to greatly impact the light curves or spectra of the subsequent supernovae, except perhaps during the shock breakout phase. However, a few models predict somewhat higher wave energy fluxes, for which we perform hydrodynamical simulations of the mass ejection process. Radiative transfer simulations of the subsequent supernovae predict a bright but brief shock-cooling phase that could be detected in some Type Ib/c supernovae if they are discovered within a couple days of explosion.

Unified Astronomy Thesaurus concepts: [Supernovae \(1668\)](#); [Radiative transfer \(1335\)](#); [Light curves \(918\)](#); [Stellar pulsations \(1625\)](#); [Late stellar evolution \(911\)](#)

1. Introduction

1.1. Rapid Transients

Type Ib/c supernovae are caused by the explosion of a massive star in which the surface H envelope has previously been lost through winds or mass transfer in a binary system (see, e.g., Yoon 2015, for a recent review). The launch of Zwicky Transient Factory has led to more detections of supernovae at hours to days after explosion. High-cadence monitoring also allows for detections of pre-supernova outbursts, e.g., in SN 2018gep at about 2 weeks before its final explosion (Ho et al. 2019). Similar outbursts have been observed in both Type II, Type Ib/c, and Type Ibn supernovae such as SN 2007bg (Milisavljevic et al. 2013), SN 2008D (Modjaz et al. 2009; Svirski & Nakar 2014), SN 2010mc (Ofek et al. 2013), PTF13efv (Ofek et al. 2016), SN 2015bh (Elias-Rosa et al. 2016), SN 2015U (Shivvers et al. 2016), and SN 2015G (Shivvers et al. 2017). SN 2009ip (Mauerhan et al. 2013; Ofek et al. 2013) provides evidence of a star resembling a Luminous Blue Variable going supernova, with a clear mass outburst 3 yr before the real explosion. These outbursts have demonstrated the possibility that a massive star can lose mass dynamically, besides its stellar wind mass loss.

Pre-supernova outbursts also connect to the formation of circumstellar medium (CSM) around the exploding star, which has been a challenge in stellar evolution theory. For very massive stars (zero-age main-sequence mass $M_{\text{ZAMS}} = 80\text{--}140 M_{\odot}$), the electron-positron pair instability drives explosive O burning and mass ejection, which accounts for an outburst of ~ 0.1 to tens of $M_{\odot}$ (Leung et al. 2019; Woosley 2019; Renzo et al. 2020). However, for lower-mass stars, the mechanisms at play are not clear.

The observed transients with a rapid rise time (from a few days to ~ 10 days) are usually associated with the existence of

some shock interaction between the ejecta and the CSM. The interaction picture has been suggested to explain many bright and rapid transients, such as SN 2006gy (Woosley et al. 2007; Blinnikov 2010), iPTF14hls (Woosley 2018), AT2018cow (Leung et al. 2020), and SN 2018gep (Leung et al. 2021).

1.2. Dynamical Evolution of Massive Stars

Late-phase nuclear burning of massive stars is rapid and strong, which can drive vigorous convective flow within the C- and O-burning regions. The convection triggers wave generation outside the convection zone, and some of these waves leak through the evanescent zones inside the star and propagate outward (Quataert & Shiode 2012). Escaped waves with sufficient energy can form shocks or dissipate via radiative diffusion when they approach the stellar surface, where they deposit their energy as an extra thermal energy source (Shiode & Quataert 2014). Even though the relative amount of energy which can successfully leak is small compared to the whole stellar energy budget, in some cases it may be sufficient to eject the outermost matter from the H and He envelope in a H-rich (Fuller 2017) or H-poor (Fuller & Ro 2018) star. The exact amount of mass ejection depends on the energy budget.

The energy injection can also change the near-surface structure of the star (Owocki et al. 2019; Kuriyama & Shigeyama 2020; Leung & Fuller 2020) and hence its observable optical appearance (Kuriyama & Shigeyama 2021). Additionally, the circumstellar medium can greatly affect the light curve of the subsequent supernova (Suzuki et al. 2019). The outburst mass and energy expected from wave heating are approximately capable of matching some well-observed transients such as SN 2000kf (Ouchi & Maeda 2021) and SN 2018gep (Leung et al. 2021).

1.3. Motivation and Outline

In Leung et al. (2021) we used a parameterized wave model to study how the stellar envelope of a H-poor star responds to the wave energy deposition. Depending on the energy deposition and duration, we estimated that the typical mass loss can reach $\sim 10^{-5}$ – $10^{-2} M_{\odot}$. In this work, we examine the energy deposition computed from realistic stellar models that self-consistently compute the wave flux escaping from the stellar core.

In Section 2, we describe the numerical methods for computing the wave heating rate from stellar models, the following hydrodynamical evolution, and radiative transfer simulations. In Section 3, we describe the wave heating rates from our suite of stellar models, and how it depends on stellar parameters such as mass and metallicity. Section 4 presents hydrodynamical simulations of the stellar response to wave heating, while Section 5 shows light curve models of the subsequent supernova. In Section 6, we discuss implications for transients and comparisons with recent work in the literature, and we conclude in Section 7.

2. Methods

We use the stellar evolution code Modules for Experiments in Stellar Astrophysics (MESA; Paxton et al. 2011, 2013, 2015, 2018, 2019) version 8118. The stellar evolutionary model assumes the default mixing length index, exponential overshooting parameter of 0.025 and the *Dutch* wind formulae (Vink et al. 2000, 2001) with a coefficient of $\eta = 0.5$. The necessary configuration files and extra subroutines are available on Zenodo.¹

Our supernova radiative transfer models uses the Supernova Explosion Code (SNEC; Morozova et al. 2015). The code is based on the prototype reported in Bersten et al. (2011, 2013), which solves for the bolometric radiative transfer assuming blackbody radiation, with a realistic opacity table taking inputs of density, temperature, and chemical composition.

In this work, each stellar evolutionary model is prepared by five steps. (1) We run the model until the core hydrogen is exhausted. (2) We remove the H envelope by relaxing the stellar mass to the helium core mass, mimicking mass stripping via a companion star. (3) We continue our evolutionary model until core collapse, now with the wave generation subroutine switched on to record the wave energy escaping from the core, but without depositing the energy in the envelope to prevent numerical difficulties. (4) For a limited set of models from (3), we add wave heat to the envelope and use the hydrodynamics module of MESA to simulate how the envelope expands and capture the mass ejection. (5) We use SNEC to compute the optical signal of the final explosion for the models from (4).

To calculate the wave heating rate of the envelope, we follow the formalism outlined in Fuller & Ro (2018), updated with the more realistic wave spectrum and calculation of nonlinear wave breaking described in Wu & Fuller (2021). In each step we calculate how much energy generated in the convective core can successfully pass through all evanescent layers and reach the surface. We first locate the position and luminosity of individual actively burning core and shells. We classify the core and shells by the dominant element being burned, e.g., helium (He), carbon (C), oxygen (O), neon (Ne),

and silicon (Si). We then integrate over the convective burning shell to estimate the wave energy flux and typical wave frequency generated by each layer.

Next, we extract the amount of escaped energy by calculating the neutrino damping attenuation factor f_{ν} and fraction of energy transmitted through the evanescent zones. The latter is approximately given by the probability of transmission through the thickest evanescent region, or equivalently the minimum transmission coefficient $T_{\min}^2$. For each angular wavenumber l , the fraction of energy which can escape is given by

$$f_{\text{esc},l} = \left(1 + \frac{f_{\nu} - 1}{T_{\min,l}^2} \right)^{-1}. \quad (1)$$

The rate of energy escape to the envelope is then $L_{\text{heat}} = \sum_{l=1}^{10} f_{\text{esc},l} \dot{E}_l$, with $\dot{E}_l$ being the wave power put into each l by convection. We assume the same angular wavenumber spectrum as Wu & Fuller (2021).

We also crudely account for wave attenuation via nonlinear wave breaking in the core, as discussed by Wu & Fuller (2021), which is especially important in stripped envelope stars. For a given wave luminosity L_{wave} which can be transmitted through the evanescent region, we calculate the nonlinear coefficient $|k_r \xi_r|_l$ by finding

$$|k_r \xi_r|_l = \left[\frac{2}{T_{\min,l}^2} \frac{L_{\text{heat},l} N [l(l+1)]^{3/2}}{4\pi \rho r^5 \omega^4} \right]^{1/2}, \quad (2)$$

where $T_{\min,l}^2$ is the transmission coefficient described above and $L_{\text{heat},l}$ is the escaped energy flux (luminosity) for a given wavenumber l . Quantities N , ρ and r and ω are the local Brunt–Väisälä frequency, density, radius, and wave frequency, respectively. The effective energy escape rate for each l is given by

$$L_{\text{esc,eff},l} = L_{\text{esc},l} / |k_r \xi_r|_l^2. \quad (3)$$

We refer the interested readers to the said references for the full description.

3. Results

3.1. Evolution of an Example H-poor Model

We first examine how the wave energy transport occurs in a typical H-poor model. To illustrate this, we take an example of $M_{\text{ZAMS}} = 60 M_{\odot}$, with $Z = 0.02$. This model evolves to form a $27.2 M_{\odot}$ He core, and later wind-driven mass loss during core helium burning leads to a final mass of $M_{\text{pre-SN}} = 17.5 M_{\odot}$.

In Figure 1 we plot the wave energy transport history of this model. We plot the wave energy deposition rate in the envelope (top left panel), cumulative deposited energy (top right panel), nonlinearity (bottom left panel), and the energy escape fraction (bottom right panel). In all the four panels, we mark the data points by color to specify which burning zone contributes the most amount of energy, with He, C, O, Ne, and Si represented by red, orange, green, blue, and purple, respectively.

From the energy deposition rate, we observe that wave heating first becomes significant during core O burning, about 0.05 yr pre-explosion. C-shell burning and O-shell burning provide additional peaks in the escaped energy at $\sim (2-4) \times 10^{-3}$ yr before collapse. After that, the energy escape rate sharply decreases. Si burning is almost insignificant to the energy budget

¹ MESA run files are uploaded to Zenodo via the link <https://doi.org/10.5281/zenodo.5542375>.

Figure 1. (Top left panel) The total energy deposition rate in the envelope as a function of time before core collapse for a H-poor model with $M_{\text{ZAMS}} = 60 M_{\odot}$ and $Z = 0.02$. The color corresponds to the type of convective burning region, which contributes the most energy, as indicated in the legend. Arrows with “O” and “O-shell” labels mark the onset of O-core and O-shell burning. (Top right panel) The cumulative deposited energy against time. (Bottom left panel) The nonlinearity attenuation factor for $l = 1$ waves in the core. (Bottom right panel) The escape fraction of $l = 1$ waves.

up to 10^{-3} yr before collapse. All told, roughly 10^{46} erg of wave energy escapes to the envelope before core collapse.

The escape fraction measures how much energy can reach the envelope after energy losses in the core and tunneling through evanescent regions. In this particular model, the escape fraction during core O burning ($\sim 2 \times 10^{-2}$ yr before core collapse) is much lower than that during subsequent shell C and O burning. Hence, most of the energy from core O burning is damped out via neutrino damping before being able to tunnel into the envelope. The energy escape rate is also greatly decreased by the nonlinearity attenuation factor (Equation (2) squared). In this model, the core O-burning phase experiences a nonlinear attenuation of about 100, while that during C-shell and O-shell burning is about an order of magnitude lower. Hence, the wave heating rate jumps from $\sim 10^{39}$ erg during core O burning to $\sim 10^{41}$ erg during C- and O-shell burning, demonstrating the importance of nonlinear suppression of wave energy transport.

3.2. Comparison with H-rich Model

To understand the features in the H-poor model, it is necessary to discuss the wave transport feature in a H-rich model. To do so, we consider a H-rich model with $M_{\text{ZAMS}} = 36 M_{\odot}$, which evolves to have a pre-explosion He-core mass of $17.0 M_{\odot}$. This

model has a similar pre-explosion He-core mass as the H-poor model in the previous section, so its core evolves similarly during late stage burning. This model transmits about 2×10^{47} erg of wave energy to the surface, about an order of magnitude higher than the corresponding H-poor model with a similar He-core mass.

The energy escape rate is much higher in the H-rich model during O burning with a value $\sim 10^{41}$ erg s $^{-1}$, which is about two orders of magnitude higher than that of the H-poor model. The later C-shell and Ne-shell burning deposit energy with the same order of magnitude (see Figure 2). The primary reason for the larger heating is that the H-rich star has a larger escape fraction and much lower wave nonlinearity compared to the H-poor model with the same $M_{\text{pre-SN}}$. In H-rich stars, the convective C-burning shell is usually narrower, such that the g-mode cavity overlying the O-burning core is wider, and the evanescent region separating it from the envelope is smaller. Hence, a larger fraction of the waves escape the core, and a smaller fraction of the wave energy is lost to photon, neutrino, or nonlinear damping.

To illustrate this idea, we examine in Figures 3 and 4 the wave propagation diagrams for two models when core O burning takes place. The models are chosen to have $M_{\text{ZAMS}} = 40 M_{\odot}$ and $Z = 0.02$. Most of the qualitative features

Figure 2. Same as Figure 1 except for a H-rich model with $M_{\text{ZAMS}} = 36 M_{\odot}$ and $Z = 0.02$.

in both H-rich and H-poor models are similar, in terms of the density and temperature profiles, and the luminosity profile. The main difference is the extensive H envelope that appears in the H-rich model that extends to $\sim 1000 R_{\odot}$. The convective energy transport peaks at $\sim 10^{-3}$ – $10^{-1} R_{\odot}$, and in both models the O-shell convective frequency is comparable, about $2 \times 10^{-3} \text{ s}^{-1}$. The major difference comes the Brunt–Väisälä frequency profiles. In the H-poor model, the convective C-burning shell is thicker, trapping more of the waves generated by the O-burning core beneath it. In the H-rich model, this convective shell is thinner, allowing the waves to more easily tunnel into the overlying radiative region between the C-burning and He-burning shells. Hence, in the H-rich models, more of the wave energy escapes from the core before it is damped.

3.3. Distribution of Stellar Mass Loss

We carry out an extensive survey of stellar models by varying two model parameters, initial ZAMS mass and metallicity. We choose a wide range of mass and metallicity to explore the potential mass loss driven by wave energy deposition. For lower metallicity models, we also lower the maximum mass simulated so that other major mass-loss mechanisms, such as the mass loss driven by the pulsational pair instability, are avoided.

In Figure 5 we plot the time-integrated escaped energy of each stellar model against its pre-explosion He-core mass

$M_{\text{pre-SN}}$. We choose $M_{\text{pre-SN}}$ as it is more closely related to the final evolution than M_{ZAMS} . The total escaped energy is integrated from after He-core burning, up to $\sim 10^{-3}$ yr before stellar collapse. We have included models with a metallicity from 0.002–0.02. A subset of H-rich models are also included for comparison. We list in Table 1 the outliers of our models and their physical origins.

The clustering of the data points demonstrates multiple features of stellar evolution at different phases. The H-rich models have the highest escaped energy E_{esc} . The energy range is consistent with previous work (Wu & Fuller 2021) showing that H-rich stars often release about 10^{47} erg before explosion for a wide range of masses. An outlier is the $M = 45 M_{\odot}$ model. This model has an extraordinarily high $E_{\text{esc}} \sim 10^{48}$ erg. The origin of the high escaped energy is the convective shell merger phenomenon, as reported in previous work (Wu & Fuller 2021). During the C-shell burning, the growing C-burning shell merges with the overlying He-burning shell, dredging He-rich matter down into the actively burning C-shell. The influx of extra He can rapidly increase the nuclear reaction luminosity due to α -capture reactions. As a result, the burning drives vigorous convection and wave generation.

On the other hand, H-poor models in general have a lower E_{esc} by an order of magnitude ($\sim 10^{46}$ erg). Regardless of their initial metallicity, most of the data points cluster in a band that starts from about 10^{46} erg at $M_{\text{exp}} \sim 5 M_{\odot}$ and then gradually decreases down to 10^{45} erg at $M_{\text{exp}} \sim 12.5 M_{\odot}$. The band

Figure 3. (Top left panel) The density and temperature profiles for the H-poor model with $M_{\text{ZAMS}} = 40 M_{\odot}$, $Z = 0.02$, taken during core O burning. (Top right panel) A wave propagation diagram showing the Brunt–Väisälä frequency (blue), $l = 1$ Lamb frequency (brown), and characteristic wave frequency (black). (Bottom left panel) The total wave and convective luminosities of the same model. (Bottom right panel) The chemical abundance profile of the same model.

gradually increases and reaches an asymptotic energy $\sim 10^{46}$ erg again at $M_{\text{pre-SN}} \sim 17.5 M_{\odot}$.

A few outlying H-poor models have larger total escaped energies, such as the $M_{\text{ZAMS}} = 38 M_{\odot}$ model, which has $E_{\text{esc}} \sim 10^{47}$ erg. The differences come from a number of physical processes which will be discussed in later sections.

3.4. Distribution of Deposition Timescale

In Figure 6 we plot the total escaped energy against deposition time t_{dep} for each model. We define the deposition time by the time before core collapse at which 50% of the total wave energy has escaped from the core. This corresponds approximately to the time before explosion of any pre-supernova mass ejection that occurs. However, whether or not the star ejects mass must be determined by hydrodynamic simulations of the envelope’s response to wave heating (e.g., Section 4 in this article and Leung et al. 2021).

Regardless of the star being H-rich or H-poor, the majority of models have deposition timescales from 10^{-3} – 10^{-1} yr. Stars with higher pre-explosion helium core masses tend to have shorter deposition timescales, but there is large scatter and the value of t_{dep} is not correlated with the escaped energy. For example, models with $M_{\text{ZAMS}} = 25 M_{\odot}$ have an outburst time as early as 0.09 yr before explosion for the model with $Z = 0.007$, but it is as low as 0.01 yr for $Z = 0.02$ and 0.001 yr

for $Z = 0.002$. Each represents a distinctive energy deposition history, and hence we expect there corresponding circumstellar environment can be very different.

We also examine how each of the burning channels contributes to the total deposited energy in each model. In Figure 7 we plot the energy deposited by waves generated from convective burning of He (top left panel), C (top right panel), O (bottom left panel) and Ne (bottom right panel). The Si channel in general contributes an insignificant amount of energy except just before core collapse.

During He burning, the majority of models scatters between 10^{43} and 10^{45} erg, which is at most about $\sim 10\%$ of the deposited energy. The extremely high value for one H-rich model corresponds to the shell merger model described in the previous section. For the C burning, the total escaped energy ranges from 10^{44} – 10^{46} erg. There is no significant trend between the pre-explosion mass and the total escaped energy.

O burning often provides the most energy and has a narrower range between $\sim 10^{45}$ and 10^{47} erg, but other types of burning are most important in a significant fraction of models. We observe a narrow band for the H-rich models, which is consistent with previous work (Wu & Fuller 2021) that O burning provides the majority of wave energy to the envelope. Ne burning has a similar scatter as the C-shell with a range from 10^{43} – 10^{46} . H-rich models have significantly higher energy from Ne burning than H-poor models.

Figure 4. Same as Figure 3 but for the H-rich model with similar helium core mass.

Figure 5. The time-integrated escaped energy from the core against pre-explosion mass for stellar models with mass and metallicity as parameters. H-rich models are included for comparison. The numbers correspond to the initial ZAMS mass.

3.5. A Case Study of a $M_{ZAMS} = 25 M_{\odot}$ Star

We next focus on a specific group of models with $M_{ZAMS} = 25 M_{\odot}$ and $Z = 0.002, 0.07$, and 0.02 . These models have a comparable total deposited energy, but each has a distinctive deposition duration. In Figure 8 we plot the cumulative energy as a function of pre-collapse time for the three models. It is

evident that the timing of the wave heating episodes varies significantly between the models, even though they each end up with $\sim 10^{46}$ erg of wave heat. Moreover, the burning phase (e.g., helium, carbon, or oxygen burning) responsible for the majority of the heat is different in each model. Clearly, models with similar He-core masses can differ greatly in both net wave energy and the deposition timescale.

Figure 6. The time-integrated escaped energy from the convective core against the characteristic energy deposition time before core collapse for stellar models in Figure 5. H-rich models are included for comparison. The numbers correspond to the initial ZAMS mass.

Figure 7. (Top left panel) The wave energy transmitted to the envelope that is generated by the He-burning shell against $M_{\text{pre-SN}}$ for both H-rich and H-poor models. (Top right panel) Same as top left panel but for the C-burning shell. (Bottom left panel) Same as top left panel but for the O-burning shell. (Bottom right panel) Same as top left panel but for the Ne-burning shell.

Figure 8. The cumulative deposited wave energy vs. the pre-explosion time for the model with $M_{\text{ZAMS}} = 25 M_{\odot}$ and $Z = 0.02$ (left panel), $Z = 0.007$, (middle panel), and $Z = 0.002$ (right panel).

Figure 9. The wave energy escape rate against time for the high wave energy H-poor model with $M_{\text{ZAMS}} = 20 M_{\odot}$ and $Z = 0.007$ (left panel) and the low wave energy H-poor model with $M_{\text{ZAMS}} = 35 M_{\odot}$ and $Z = 0.007$ (right panel).

3.6. Comparison of High and Low Energy Models

In Figure 5 and Table 1 we show that there are outliers with more escaped wave energy than most models. Here, we study them in detail. We compare two distinctive models: a H-poor model with $M_{\text{ZAMS}} = 20 M_{\odot}$ and $Z = 0.007$ (high-energy model), and a H-poor model with $M_{\text{ZAMS}} = 35 M_{\odot}$ and $Z = 0.007$ (low energy model). In Figure 9 we plot the wave heating rate of each model. The two models demonstrate qualitative similarities, but the wave heating rate is typically 2 orders of magnitude larger in the high-energy model.

How most of the energy is released at ~ 0.01 yr before collapse is different in the two models. Even though there is a sudden burst of wave energy from O- (He-) shell burning in the high (low) energy model, the corresponding escape fraction and nonlinearity during that period is very different. The high-energy model maintains a large escape fraction and a low nonlinearity (~ 1) for about 0.003 yr, while the low energy model has a small escape fraction and large nonlinearity (~ 8). This drastically impacts the energy that can successfully reach the envelope.

To further diagnose the origin of the different wave energy deposition rates of the models above, we plot in Figure 10 the density and temperature profiles (top left panel), wave propagation diagram (top right panel), the luminosity profile (bottom left panel), and the chemical abundance profile (bottom right panel) of the $20 M_{\odot}$ model at $\sim 9 \times 10^{-3}$ yr from its onset

of gravitational collapse. The choice of the model age overlaps with the time where its wave deposition energy is at its maximum. In this model, most of the wave energy arises from the energetic convective shell at $r \sim 10^{-2} R_{\odot}$, which burns carbon, oxygen, and neon and carbon at this snapshot. A recent ingestion of carbon from above has increased the burning luminosity and wave frequency. The Brunt-Väisälä frequency and the Lamb frequency profiles indicate the source of the high wave transmission. The outgoing wave frequency is about 10^{-2} s^{-1} . Waves of this frequency see only a narrow evanescent layer at $r \sim 10^{-1} R_{\odot}$ separating the core from the envelope. As a result, a large fraction of the waves can escape into the envelope and arrive the surface for heat deposition.

3.7. Shell Merger

Another important feature for massive star evolution is the occurrence of convective shell merger events, driven by convective boundary mixing (Collins et al. 2018; Davis et al. 2019; Androssy et al. 2020; Yadav et al. 2020). Shell mergers not only change the pre-collapse stellar structure of the massive star, but also provide unconventional thermodynamic conditions for the synthesis of minor elements such as Cl, K, and Sc (Ritter et al. 2018). In our case, convective shell mergers drive vigorous nuclear burning, convection, and wave energy generation, so they can lead to a wave-driven outburst (Wu & Fuller 2021).

Figure 10. The structure of a H-poor model with $M_{\text{ZAMS}} = 20 M_{\odot}$ and $Z = 0.007$ taken when the wave heating is strongest at $\sim 10^{-2}$ yr before collapse. (top left panels) the density and temperature profiles, (top right panel) the Lamb frequency (brown line) and Brunt–Väisälä frequency (blue line), together with the wave frequency (black line), (bottom left panel) the luminosity (blue line), wave luminosity (brown line), and convective luminosity (green line) profiles of the star, and (bottom right panel) the chemical abundance profile for He (red), C (orange), O (green), Ne (blue), and Si (purple).

Our $45 M_{\odot}$ H-rich model exhibits a shell merger that could generate a wave-driven outburst, as shown in Figure 11. When the merger event occurs at 0.005 yr before collapse, the energy deposition rate increases by about 3 orders of magnitude. Even though it has a duration less than 0.001 yr, more than 90 % of the deposited energy of $\sim 10^{48}$ erg comes from this event. By examining the chemical abundance profiles before and after the shell merger, we see that He has been dredged down below $10^{-1} R_{\odot}$ during the merger. This occurs when the convective mixing becomes strong during C-shell burning, causing a merger with the overlying He-burning shell that drags the He-rich material to the actively burning C-shell. This drives intense nuclear energy via α -capture reactions that further power convective motion, and wave excitation. The wave frequency also increases due to the larger convective velocities. Consequently, the wave heating rate of the envelope increases by a few orders of magnitude.

4. Response of the Envelope

4.1. Connection to Rapid Transients

Here we study the hydrodynamical response of the envelope due to wave energy deposition. In Leung et al. (2021), we demonstrated that how fast the energy is deposited affects the envelope expansion. When the energy deposition timescale is shorter than the dynamical timescale, the excited envelope develops a shock and ejects mass in the form of a pulse. On the other hand, when the energy deposition timescale is long, the envelope gradually expands and a steady wind can be driven.

To estimate how much mass can be ejected and its trajectory, we use the total escaped energy E_{esc} and the duration t_{dep} . If the

wave energy is used efficiently to eject mass, the ejected mass M_{ej} would be approximately

$$M_{\text{ej}} \sim \frac{E_{\text{esc}} R}{GM_{\text{pre-SN}}}, \quad (4)$$

where R is the radius of the pre-explosion star. Equation (4) overestimates the ejecta mass in H-rich stars (Fuller 2017; Linial et al. 2021), so our estimates for H-rich stars should be taken as upper limits. Similarly, if mass is ejected at the star’s escape speed, the CSM radius R_{CSM} would be

$$R_{\text{CSM}} \approx t_{\text{dep}} v_{\text{ej}} \sim t_{\text{dep}} \sqrt{\frac{GM}{R}}. \quad (5)$$

Fuller & Ro (2018) found that wave heating does efficiently eject mass in H-poor stars, and that the outflow velocity is slightly larger than the escape speed, such that Equations (4) and (5) are reasonable estimates.

In Figure 12 we plot R_{CSM} against M_{ej} for all the models computed in this work. The data points cluster into two groups: the H-rich models and the H-poor models. Due to their small binding energy, H-rich models are expected to eject as much as $\sim 0.5 M_{\odot}$, though the true ejected mass may be substantially smaller. If mass is ejected by an outgoing shock wave, Linial et al. (2021) argued that the ejecta mass will likely be either nearly zero or a large fraction of the H envelope, so more detailed calculations should be performed for reliable estimates of the mass loss in H-rich models.

The H-poor models exhibit a wide range of M_{ej} and R_{CSM} due to their varying wave heating rates and timescales. Most models center around $M_{\text{ej}} \sim 10^{-4} M_{\odot}$ and $R_{\text{CSM}} \sim 3 \times 10^{13}$ cm.

Figure 11. (Top left panel) The wave energy deposition rate for the model with $M_{\text{ZAMS}} = 45 M_{\odot}$, $Z = 0.02$, with the same colors as Figure 1. (Bottom left panel) Same as the top left panel but for the cumulative deposited energy. (top right panel) The chemical abundance profile before the merger event of the same model. (Bottom right panel) Same as the top right panel but after the merger event.

Figure 12. The expected CSM radius against CSM mass based on the energy deposition history for stellar models explored in this work. CSM masses should be considered as upper limits for the H-rich models. The arrow indicates the model for which hydrodynamic and radiative transfer simulations are performed in Figures 13–15.

Figure 13. (Top left panel) The density profile of the model with $M_{\text{ZAMS}} = 20 M_{\odot}$ and $Z = 0.007$ at the beginning of hydrodynamical simulation (blue solid line), 0.01 yr before collapse (green dashed line), 0.008 yr (purple dashed line), and at the onset of gravitational collapse (red dotted line). (Top right panel) Same as the top left panel but for the velocity. (Bottom left panel) Same as the top left panel but for the external mass. (Bottom right panel) Same as the top left panel but for the heating profile.

There are some outliers (corresponding to outliers in Figure 5) that have larger ejected mass ($\sim 10^{-2} M_{\odot}$) or a very large $R_{\text{CSM}} \sim 10^{14}$ cm. These are models with large wave energies or long wave heating timescales, respectively. The distribution of the data points do not depend strongly on the initial metallicity.

As shown in Leung et al. (2020, 2021), an ejected mass of $\sim 10^{-2}$ – $10^{-1} M_{\odot}$ with a radius of 10^2 – $10^4 R_{\odot}$ can power luminous SNe via CSM interaction, which explains some rapidly brightening transients with a rise time of ~ 10 days and a peak luminosity $\sim 10^{44}$ erg s^{-1} . The expected M_{CSM} is much smaller than the required values for most of our models, so we expect rapidly rising H-poor transients to be uncommon (if the CSM is generated by wave heating). The exact structure of the CSM and its impact on the explosion light curve require detailed hydrodynamics and radiative transfer calculations, which we perform for a few of our models.

4.2. Hydrodynamical Simulations

Having understood the wave deposition history, we may repeat the procedure outlined in Leung et al. (2021) of depositing the energy to the outer part of the star. In that work, the wave luminosity and duration are chosen from analytic estimates. In this work, we directly use the wave energy deposition history recorded from our stellar models above. This approach provides a more accurate prescription to study mass ejection and remove extraneous parameters.

Similar to our previous work, we excise the interior, keeping only about $1 M_{\odot}$ interior of the C shell, so that the simulation is not limited by the small time step during the advanced burning in the core. In our case, the expected mass loss is so small ($< 10^{-2} M_{\odot}$) that we do not expect the surface motion to feedback on the evolution of the core. We add the wave energy as an additional energy source in the stellar models, deposited in the envelope according to Equation (1) in Leung et al. (2021). This accounts for acoustic wave energy dissipation via weak shocks and radiative damping. For detailed implementation we refer readers to our previous work.

For demonstration, we consider the H-poor model with the largest mass ejection shown in Section 4.1, with $M_{\text{ZAMS}} = 20 M_{\odot}$ and $Z = 0.007$. In Figure 13 we plot the density, velocity, mass, and wave heating profiles at different times. The hydrodynamical simulation begins when the total wave heating energy exceeds $10^3 L_{\odot}$ for the first time. We see that until 0.01 yr before collapse, the low energy deposition rate does not lead to significant motion in the envelope. When the Ne-shell burning increases the wave heating rate, we see that the envelope quickly expands, reaching a radius $\sim 10^{2.5} R_{\odot}$. The outermost velocity can reach $\sim 10^8$ cm s^{-1} . However, we emphasize that because of the low density, the ejected mass only amounts to $\sim 10^{-2} M_{\odot}$, which is made of mostly He. The surface luminosity can temporarily increase by 2 orders of magnitude to $L \sim 10^7 L_{\odot}$. The density profile of the ejected mass is slightly steeper than a r^{-2} scaling.

Figure 14. The time evolution of the surface luminosity and effective temperature for the outbursting model shown in Figure 13.

Our analytical mass ejection and timescale estimates match the expected CSM features fairly accurately for the H-poor model with a large E_{dep} . For our example, our analytic formulae predict that M_{CSM} , $R_{\text{CSM}} \approx (0.01 M_{\odot}, 300 R_{\odot})$, whereas the simulation has M_{CSM} , $R_{\text{CSM}} \approx (0.007 M_{\odot}, 758 R_{\odot})$. However, most of the ejected mass is located below $\sim 300 R_{\odot}$ so the analytical estimate is actually quite good. When the expected mass ejection is very small, the analytic formula can overestimate the mass because the energy deposition becomes more concentrated in matter near the stellar surface.

We plot in Figure 14 the time evolution of the surface luminosity for the same model as Figure 13. When the wave heating peaks about 0.01 yr before collapse, the surface luminosity increases by a factor of ~ 100 to reach a peak luminosity of nearly $3 \times 10^7 L_{\odot}$. The temperature initially increases by a factor of a few, but decreases after the initial peak as the photospheric radius moves outward into an extended optically thick wind. The same behavior was seen in Fuller & Ro (2018). High-cadence photometric surveys may be able to detect these progenitor outbursts, like that of SN 2018gep (Ho et al. 2019).

5. Radiative Transfer of Representative Models

With the hydrodynamic stellar evolution models, we obtain realistic models of the ejected CSM density profile at the onset of collapse. We use this information to compute the light curve of the subsequent supernova using the one-dimensional radiative transfer hydrodynamics code SNEC (Morozova et al. 2015). The code solves the bolometric radiative transfer in the radiative diffusion limit, with realistic (non-constant) opacity, making it ideal to study the initial shock-cooling part of the light curve, before the ejecta becomes optically thin.

In the radiative transfer simulations, we choose a few model parameters, including the inner mass cut M_{cut} , the explosion energy E_{exp} , and the ^{56}Ni mass M_{Ni} . The simulations are initiated from our stellar progenitor models by excising the Si core (up to M_{cut}) and depositing the explosion energy E_{exp} (in units of 10^{51} erg) and ^{56}Ni with a mass M_{Ni} (in units of $M_{\odot}$). We choose M_{cut} to be the Si-core mass of the collapsing model. Explosion energies of 10^{51} – 3×10^{51} erg and ^{56}Ni masses of 0.03 – $0.3 M_{\odot}$ are used to span the range from typical to

energetic Type Ib SNe. The CSM mass and radius are taken from the hydrodynamical simulation, but the density profile has been modified to have an r^{-2} dependence to avoid numerical problems that arise due to sharp density changes.

In Figure 15 we plot the radiative transfer results of our representative wave-driven mass loss model from the preceding section. A control model with no CSM is added to highlight the effect of the CSM on the supernova appearance. The light curve has a very sharp rise and fall due to shock-cooling emission from the CSM, similar to the light curves of many Type IIb SNe. In Type IIb SNe, the shock-cooling emission comes from the low-mass extended H envelope ($M \sim 0.01 M_{\odot}$, $R \sim 200 R_{\odot}$). Our models have CSM with a similar mass and radius (though it is composed of He instead of H) and the early light curves thus look quite similar. Because of the low M_{CSM} , the shock-cooling time is short (~ 3 days), but the bolometric luminosity can be as high as $\sim 10^{44}$ erg. The high temperature ($T > 3 \times 10^4$ K) at the peak implies the shock cooling would be associated with bright UV emission.

The effective temperature and photosphere velocity also show a rapid rise and fall during the early CSM shock-cooling phase. After the initial peak, the photosphere recedes below the CSM, and the light curve then resembles a typical Type IIb or Ib SN. Higher ^{56}Ni will lead to a more significant rise in the luminosity after the shock front cools down. The explosion energy primarily changes how fast the light curve falls after day ~ 20 . A lower ^{56}Ni leads to a faster drop in the effective temperature after shock breakout, while a lower explosion energy makes the effective temperature drop slower.

The photosphere radius increases rapidly at early time as the surface traces the outer layers of the expanding ejecta during the shock-cooling phase. After that, its expansion is balanced by the recession in the Lagrangian sense such that the photospheric radius plateaus at $\sim 10^{15}$ cm. The photospheric velocity converges to $\sim 10^4$ km s^{-1} until the ejecta become transparent, with higher explosion energies creating higher photospheric velocities as expected. The ejecta becomes transparent to optical radiation at about 45–60 days after explosion, at which point SNEC’s effective temperature, photospheric radius, and velocity become unreliable.

6. Discussion

6.1. Rapidly Rising and Fading Transients

Our wave heating models can be compared to rapidly rising and fading transients (e.g., Drout et al. 2014), which may be powered by CSM interaction. For the large majority of our models, the wave heating is insufficient to eject enough mass to power observed rapidly evolving transients. The typical mass scale of wave-driven outbursts of $\sim 10^{-4} M_{\odot}$ can only sustain shock-cooling emission for $\sim 10^{-1}$ days, far shorter than the typical evolution times of ~ 10 days. The upper end of the distribution explored in this work ejects $\sim 10^{-2} M_{\odot}$, which may sustain shock cooling for ~ 1 day, still too short compared to the current population of observed rapidly evolving transients. However, our models predict that a significant fraction of ordinary Type Ib/c SNe will exhibit a bright but very brief phase of CSM interaction within hours of explosion.

Our models also shed light on the rapid rise and fall of the light curve in heavily stripped Type Ib/c SNe such as iPTF14gqr (De et al. 2018b), iPTF16hgs (De et al. 2018a), and SN 2019dge Yao et al. (2020). The short-lived shock cooling for iPTF14gqr

Figure 15. (Top left panel) The bolometric light curves of supernova models from the He star model in Figure 13 as a function of time after explosion. Models are named by the format $E_{\text{exp}}\text{-}M(^{56}\text{Ni})$ as described in the text. (Top right panel) Same as the top left panel but for the effective temperature. (Bottom left panel) Same as the top left panel but for the photosphere radius profile. (Bottom right panel) Same as the top left panel but for the photosphere velocity.

indicated a CSM mass and radius of $M_{\text{CSM}} \sim 0.01 M_{\odot}$ and $R_{\text{CSM}} \sim 3 \times 10^{13}$ cm, similar to that of our most energetic H-poor model in Figure 12. Hence, wave-driven mass loss could possibly account for the extended envelope of that event. For the other two, the authors inferred $M_{\text{CSM}} \sim 0.1 M_{\odot}$ and $R_{\text{CSM}} \sim 10^{12}$ cm for iPTF16hgs, and $M_{\text{CSM}} \sim 0.1 M_{\odot}$ and $R_{\text{CSM}} \sim 3 \times 10^{12}$ cm for SN 2019dge. Those masses are likely too large to be created by wave-driven mass loss, and the radii are likely too small. Hence, an inflated He envelope as is naturally expected in low-mass He star SN progenitors may be a more likely explanation for those events. All of these events were heavily stripped SNe (likely in binary systems) arising from low-mass progenitors whose structures are quite different from the higher-mass He stars studied here. Future calculations should investigate H-poor low-mass He stars, whose wave heating rates may be increased by degenerate neon/oxygen/silicon burning (Wu & Fuller 2021).

6.2. Shock Breakout Emission

Even though the small amount of CSM predicted by our models will not have a large impact on the optical light curves of typical Type Ib/c SNe, it may affect the shock breakout emission. Even a small amount of optically thick mass ($M \gtrsim 10^{-6} M_{\odot}$) above the photosphere may be sufficient to affect the shock breakout duration and its X-ray spectrum.

Our models are roughly consistent with the enhanced CSM density inferred around the progenitor of Type Ib SN 2008D based on its shock breakout emission Soderberg et al. (2008). Svirski & Nakar (2014; see also Balberg & Loeb 2011; Ioka et al. 2019; Ito et al. 2020) demonstrated that the CSM density at $R \lesssim 10^{14}$ cm must have been ~ 20 times larger than expected for Wolf-Rayet stars. This entails $\dot{M} \sim 10^{-3} M_{\odot} \text{ yr}^{-1}$ for a wind mass-loss rate of $5 \times 10^{-5} M_{\odot} \text{ yr}^{-1}$. Our typical models have $R_{\text{CSM}} \lesssim 10^{14}$ cm, consistent with the shock breakout constraint. They also have $M_{\text{CSM}} \sim 10^{-4} M_{\odot}$, ejected on timescales of $t_{\text{CSM}} \sim 10^{-2}$ yr, corresponding to mass-loss rates of $\sim 10^{-2} M_{\odot} \text{ yr}^{-1}$. This is only slightly larger than the inferred late-time mass-loss rate of SN 2008D. More detailed modeling of shock breakout emission (which is not accurately captured by our SNEC models) can determine whether wave-driven mass can account for the shock breakout signal of 2008D. In any case, we predict that longer-than-expected shock breakout emission may be very common in H-poor SNe, which may be tested by future wide-field UV surveys (Sagiv et al. 2014).

6.3. Comparison with Literature Work

Our work can be compared with other studies of outbursts driven by sudden energy deposition. In Kuriyama & Shigeyama (2020), energy is deposited in the stellar envelope

Table 1
Model Outliers with Large Wave Energy Deposition from Figure 5

Group	Z	$M_{\text{ZAMS}} (M_{\odot})$	Stripped?	Origin
A	0.007	20	Yes	Low $k_r \xi_r$ High f_{esc} (Ne)
B	0.02	37, 38, 47	Yes	Low $k_r \xi_r$
	0.007	37, 43	Yes	High f_{esc} (C/O)
	0.002	30, 38	Yes	
C	0.02	45	No	Shell merger (He/C)

Note. The right column lists the reason for the large wave energy, as well as the burning zone type that provides the most wave heat.

with a given deposition rate and duration, and the amount of energy is scaled with the binding energy of the envelope. The resultant mass loss ranges from $\sim 10^{-3}$ – $1 M_{\odot}$. For red supergiants losing mass via a shock, the actual mass loss sharply drops when the ratio of deposited energy to binding energy is less than roughly 0.5, as explained in Linial et al. (2021). For compact stars with mass loss via super-Eddington winds, most of the deposited energy is used to lift mass out of the gravitational potential, so the total mass lost is closer to our estimate from Equation (4), as explained in Quataert et al. (2016).

In Ouchi & Maeda (2021), a moderate heating rate of $\sim 10^{39}$ erg s $^{-1}$ is added to a $12 M_{\odot}$ star, but with a long-lasting duration of 3 yr. The total energy is about 10^{47} erg which is close to our H-rich models, but our models suggest that the expected energy is lower for H-poor stars. The deposition timescale of three years is much longer than our models, allowing the star to expand smoothly rather than eject mass via outbursts. In Owocki et al. (2019) the parameterized energy deposition in a stellar envelope is studied. Half of the envelope energy ($\sim 10^{50}$ erg) is deposited in a blue supergiant model and a mass outburst of $\sim 7 M_{\odot}$ is observed, resembling the mass eruption in the η Carinae. Such a high-energy deposition is not seen in our series of models, suggesting that other mechanisms are necessary to explain massive outbursts like that of η -Carinae.

6.4. Caveats

In this work we have assumed that the star loses all of its H envelope due to interactions from its binary companion. This is a good approximation for high-mass or high-metallicity stars where winds will likely remove any residual H envelope during core He burning. For lower-mass and lower metallicity stars, winds might not robustly remove all the H (Göteborg et al. 2017; Laplace et al. 2020), and a H envelope may remain until the end of stellar evolution. The less compact H envelope would have a lower binding energy, possibly triggering more significant expansion and/or mass loss compared to the pure He case. This scenario should be investigated in future work.

We have used bolometric radiative transfer for computing the light curves, assuming blackbody radiation. However, given the very low CSM mass, the medium becomes transparent at a very early time (~ 10 days), which could mean that photon transport depends on a frequency-dependent opacity. In order to robustly model optically thin ejecta and the associated effective temperature, multiband radiative transport becomes necessary.

7. Conclusion

We have explored the physics and consequences of wave energy transport in an extensive survey of H-poor stripped envelope massive stars. Our models account for multiple convective nuclear burning shells that generate gravity waves, and how these waves tunnel through the star and deposit energy in the envelope. These models improve upon prior efforts by employing a more realistic spectrum of wavenumbers and by including nonlinear damping of waves within the gravity mode cavity in the core of the star. We have surveyed stars with a ZAMS mass from 20–90 $M_{\odot}$ and a metallicity from 0.002–0.02.

We find that wave heating rates in the H-poor stars are somewhat different from H-rich stars. In H-poor stars, in general a smaller amount of the wave energy is able to escape into the surface layers, with typical wave energy deposition of $\sim 10^{46}$ erg during the last $\sim 10^{-2}$ yr of the star’s evolution. The smaller escape fraction is caused by a differing stellar structure at the outer edge of the helium core that creates thicker evanescent layers, trapping the waves in the core and increasing their damping via nonlinear dissipation. The majority of the wave energy that does escape arises from convective wave generation by O-burning shells. We find no convective shell mergers in our H-poor models, so energetic outbursts associated with these events did not appear in our suite of models. The overall wave heating does not vary strongly with the initial metallicity.

Using hydrodynamic stellar models including wave heating, we have also estimated the associated CSM formation structure via wave-driven mass loss. The small wave heating rates of our models in general generates a small CSM mass $\sim 10^{-5}$ – $10^{-3} M_{\odot}$, with a wide range of radial extents between 10^{12} and 10^{14} cm. Due to the high surface binding energy of compact He stars, the ejecta mass is much smaller than what is attainable from a H-rich star (which could in principle eject $\sim 10^{-1} M_{\odot}$ prior to its collapse). Hence, in most cases, we do not expect wave-driven outbursts to eject enough mass to cause interaction-powered H-poor SNe, explaining why CSM interaction is not frequently observed in Type Ib/c SNe. Our most energetic models eject $\sim 10^{-2} M_{\odot}$, which can power a bright but brief phase of shock-cooling emission, which we model using radiative transfer models with SNEC. The rapid rise and fall of the light curve is similar to that observed in some heavily stripped SNe, so this possibility should be explored in future work. We do predict a small amount of CSM around most Type Ib/c SNe, which could greatly affect the SN shock breakout signal in UV/X-ray bands.

In future work, our models will be extended to lower-mass He stars, where degenerate ignition of Ne, O, and Si may power more energetic wave-driven outbursts (Wu & Fuller 2021) with larger CSM masses and radii. Those types of outbursts remain viable candidates for interaction-powered H-poor SNe such as Type Ibn supernovae.

S.C.L. thanks the MESA development community for making the code open-sourced and V. Morozova and collaborators in providing the SNEC code open source. S.C.L. and J.F. acknowledges support by NASA grants HST-AR-15021.001-A and 80NSSC18K1017. S.W. is supported by the National Science Foundation Graduate Research Fellowship Program.

Software: MESA (Paxton et al. 2011, 2013, 2015, 2018, 2019) version 8118; SNEC (Bersten et al. 2011, 2013; Morozova et al. 2015) version 1.01; Python libraries: Matplotlib (Hunter 2007), Pandas (Reback et al. 2021), NumPy (Harris et al. 2020).

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