

# ***Supplemental Materials for: Promoting Reversibility of Multielectron Redox in Alkali-Rich Sulfide Cathodes through Cryomilling***

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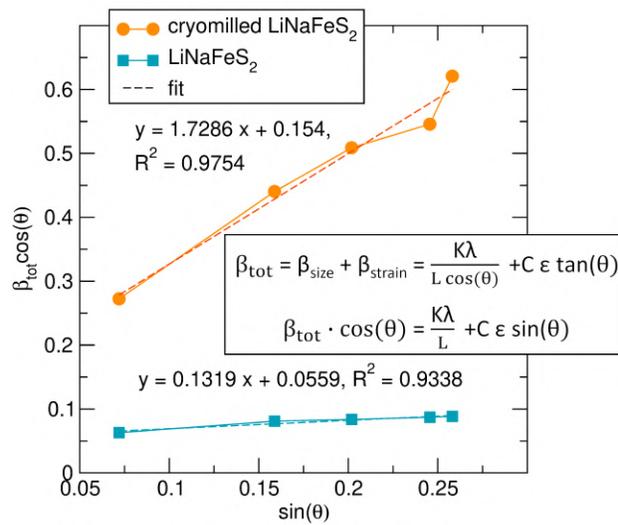


Figure S1: Williamson-Hall analysis of XRD peaks of as-prepared LiNaFeS<sub>2</sub> and cryomilled LiNaFeS<sub>2</sub>. Calculated crystallite size decreases from 1.47 nm to 0.56 nm upon cryomilling, while microstrain increases from 29800 to 425500.

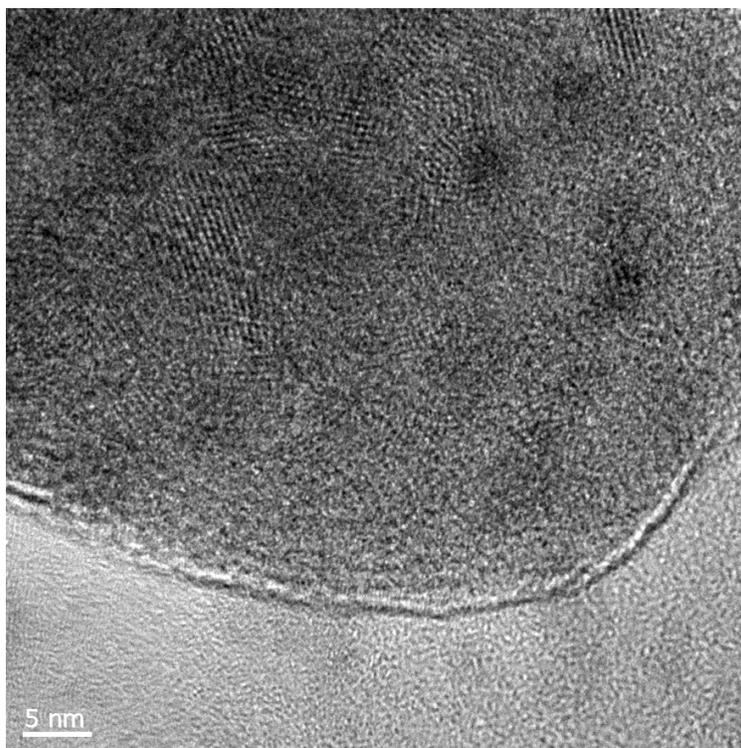


Figure S2: TEM image of as-prepared LiNaFeS<sub>2</sub>. Regions of fringes are observed throughout the particle suggesting high crystallinity.

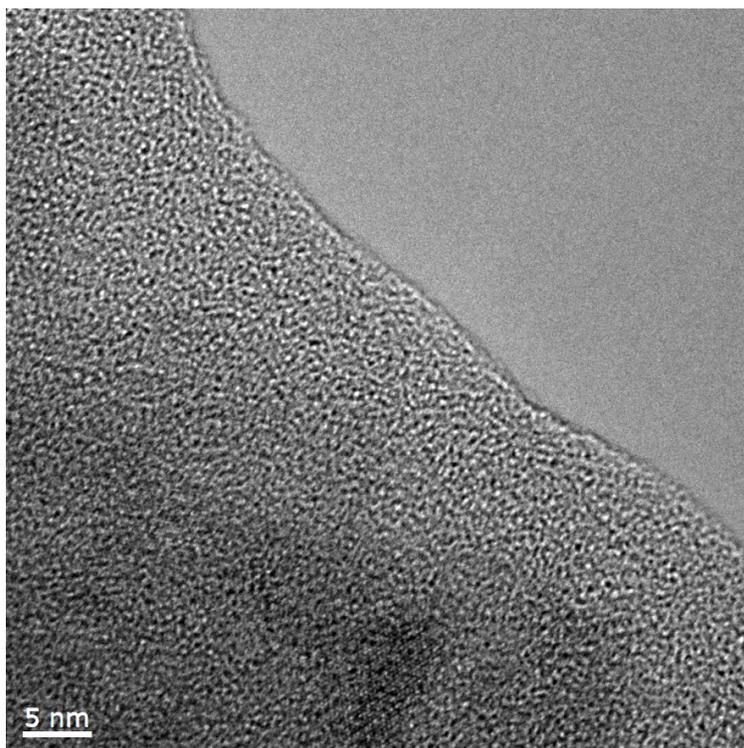


Figure S3: TEM image of cryomilled LiNaFeS<sub>2</sub>. Fewer crystalline domains are observed, which only exist in the bulk. The surface of the particle appears amorphous.

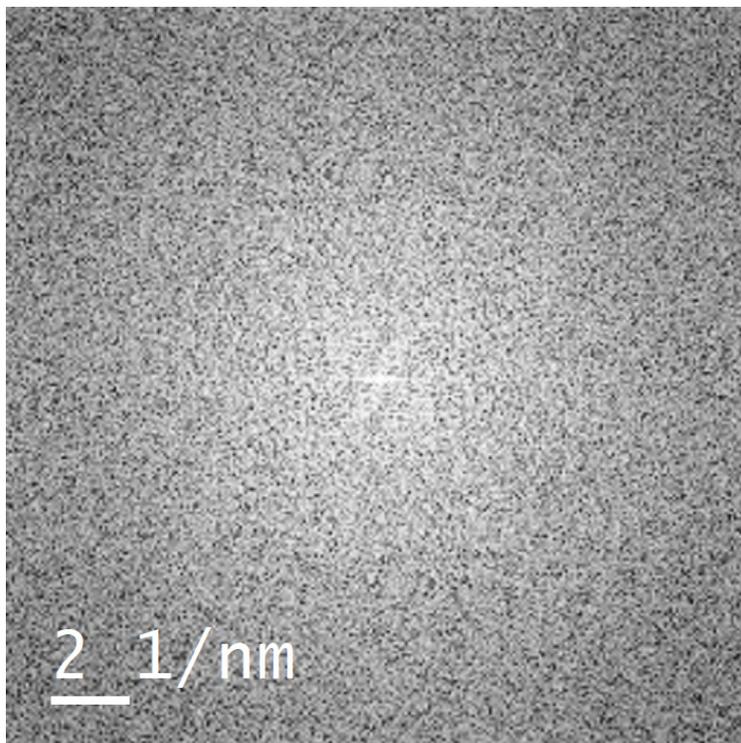


Figure S4: FFT of background carbon. The absence of a broad ring suggests that the broad ring observed in the FFT of the edge of cryomilled particle cannot be explained by carbon support alone.

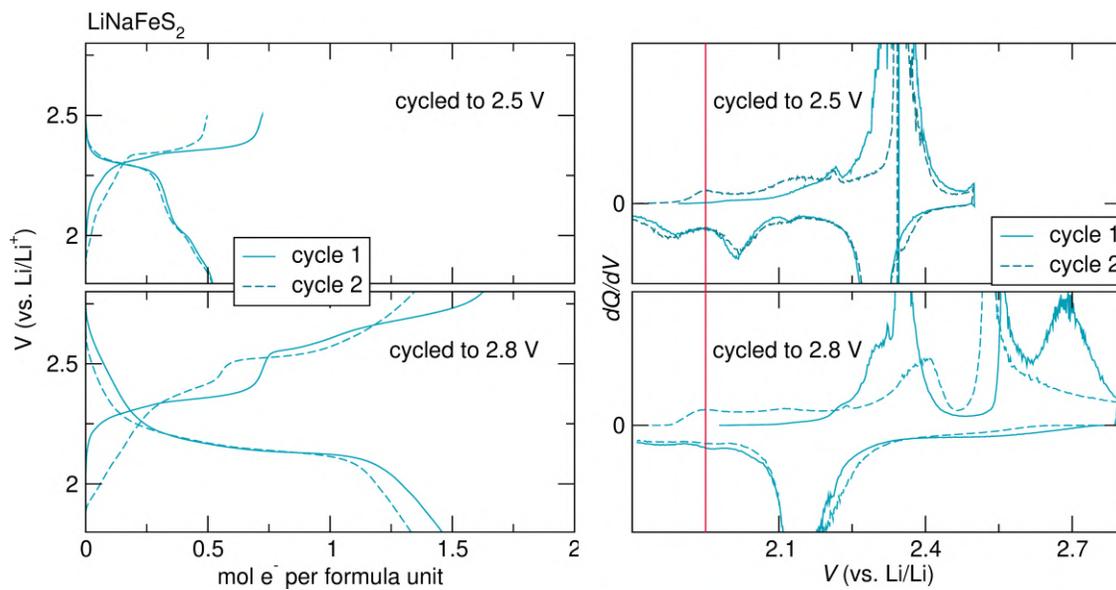


Figure S5: Galvanostatic cycling and corresponding  $dQ/dV$  plots of as-prepared  $\text{LiNaFeS}_2$  to different upper voltage cutoffs 2.5 V and 2.8 V. Both upper cutoffs exhibit the same peak in the  $dQ/dV$  plots of cycle 2.

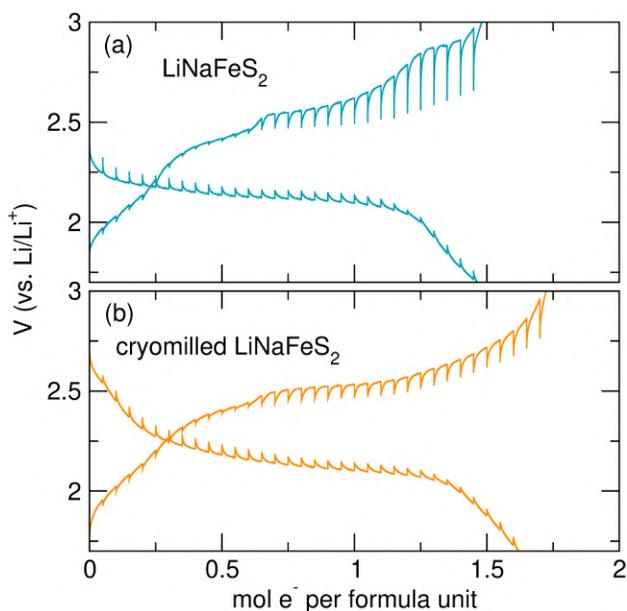


Figure S6: Cycle 13 GITT of (a) as-prepared  $\text{LiNaFeS}_2$  and (b) cryomilled  $\text{LiNaFeS}_2$ . As-prepared  $\text{LiNaFeS}_2$  continues to show higher overpotentials above 2.5 V.

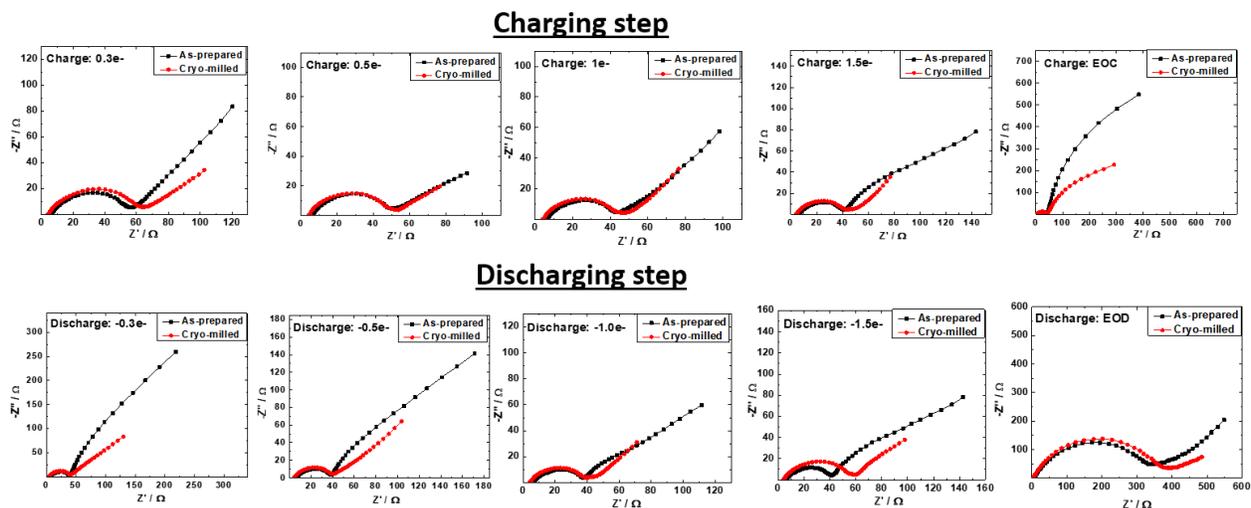


Figure S7: Intermittent EIS during cycle 1 at different states of charge. While high-frequency  $x$ -intercepts and the size of semicircles are similar, cryomilled  $\text{LiNaFeS}_2$  always shows shorter tails, suggesting lower mass transfer resistance.

$$D = \frac{R^2 T^2}{2A^2 n^2 F^4 C^2 \sigma^2}$$

Before cycling  
0.5 e<sup>-</sup> removed

$$\begin{aligned} (D_{\text{Li}^+})_{\text{cryo-milled}} / (D_{\text{Li}^+})_{\text{as-prepared}} &= (\sigma^2)_{\text{as-prepared}} / (\sigma^2)_{\text{cryo-milled}} \\ &= (120.01)^2 / (53.52)^2 \\ &= 5 \end{aligned}$$

$$\begin{aligned} (D_{\text{Li}^+})_{\text{cryo-milled}} / (D_{\text{Li}^+})_{\text{as-prepared}} &= (\sigma^2)_{\text{as-prepared}} / (\sigma^2)_{\text{cryo-milled}} \\ &= (22.89)^2 / (13.59)^2 \\ &= 2.8 \end{aligned}$$

Figure S8: Ratios of diffusion coefficients of as-prepared LiNaFeS<sub>2</sub> and cryomilled LiNaFeS<sub>2</sub> before cycling and 0.5 e<sup>-</sup> removed assuming constant surface area. Cryomilled LiNaFeS<sub>2</sub> shows higher diffusion coefficients compared to as-prepared LiNaFeS<sub>2</sub>.

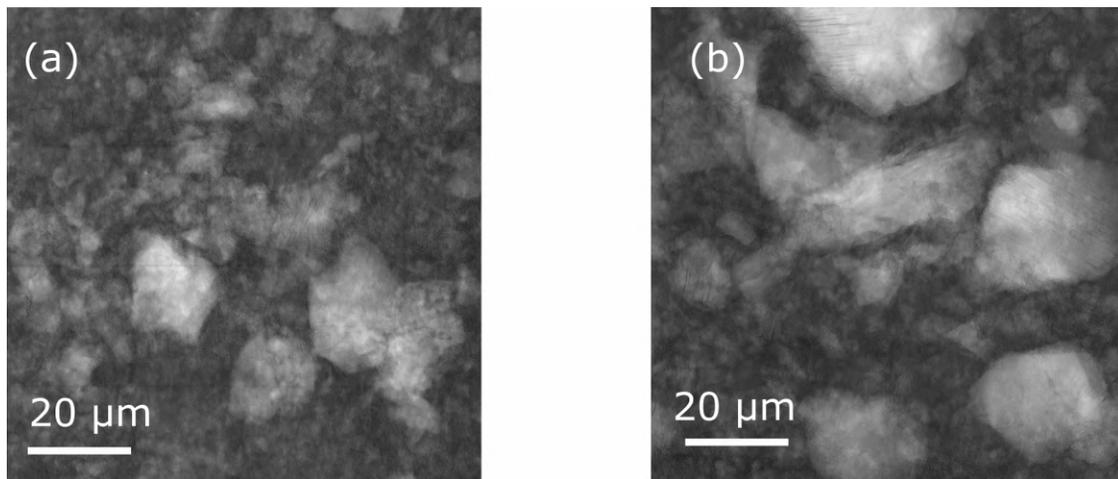


Figure S9: TXM mosaic micrographs of as-prepared LiNaFeS<sub>2</sub> (a) charged to 2.5 V, (b) fully charged to 3 V. Scale bars represent 20 μm. Particle fractures appear at 2.5 V, and more particle fractures are observed at the end of charge.

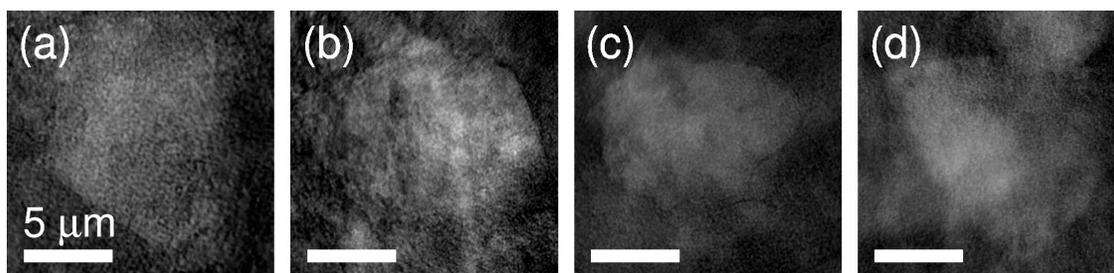


Figure S10: TXM micrographs of  $\text{Li}_2\text{FeS}_2$  (a) before cycling, (b) charged to 2.5 V, (c) charged to 3 V, and (d) discharged to 1.7 V. Scale bars represent  $5 \mu\text{m}$ .  $\text{Li}_2\text{FeS}_2$  does not show signs of fracturing in all states of charge.

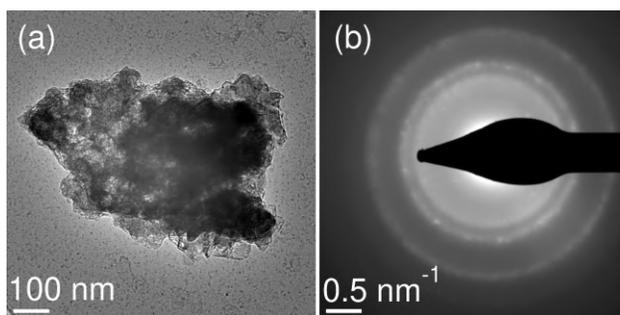


Figure S11: (a) Particle clusters of cryomilled  $\text{LiNaFeS}_2$  and (b) diffraction rings in the corresponding selected area electron diffraction (SAED) pattern. The cluster is composed of small single crystalline particles that are randomly oriented.

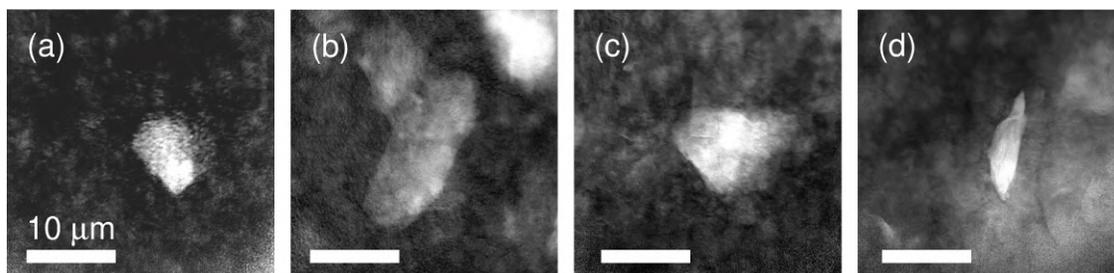


Figure S12: TXM micrographs of cryomilled  $\text{LiNaFeS}_2$  (a) before cycling, (b) charged to 2.5 V, (c) charged to 3 V, and (d) charged to 3V then discharged to 1.7 V. Scale bars represent  $10 \mu\text{m}$ . There are more smaller particles than bigger aggregates. Brightness and contrast levels are adjusted so that smaller particles can be seen better.

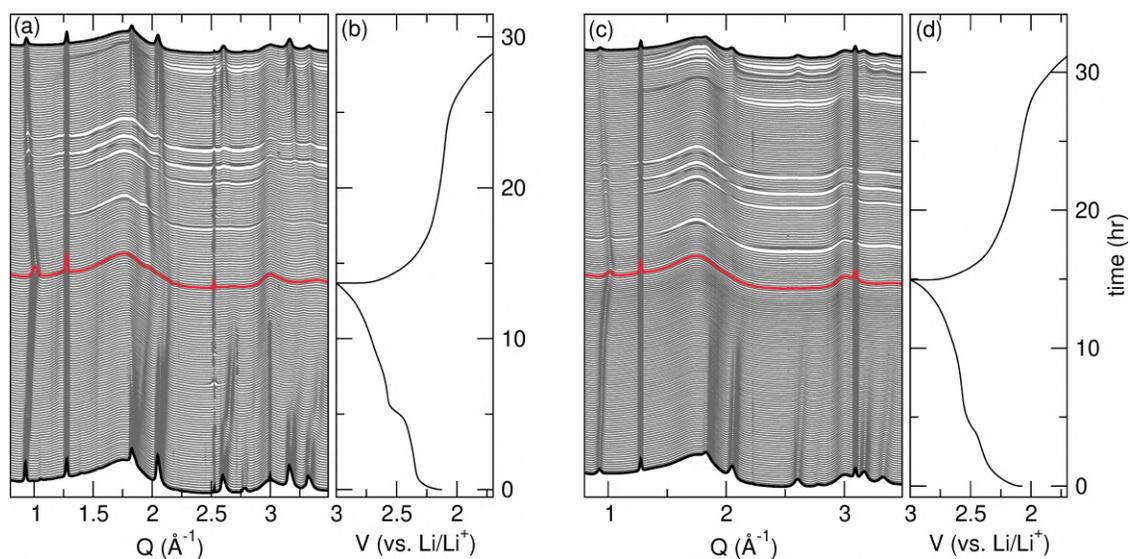


Figure S13: *Operando* sXRD of (a and b) as-prepared  $\text{LiNaFeS}_2$  and (c and d) cryomilled  $\text{LiNaFeS}_2$ . The peak at 1.26 Q corresponds to PTFE binder.

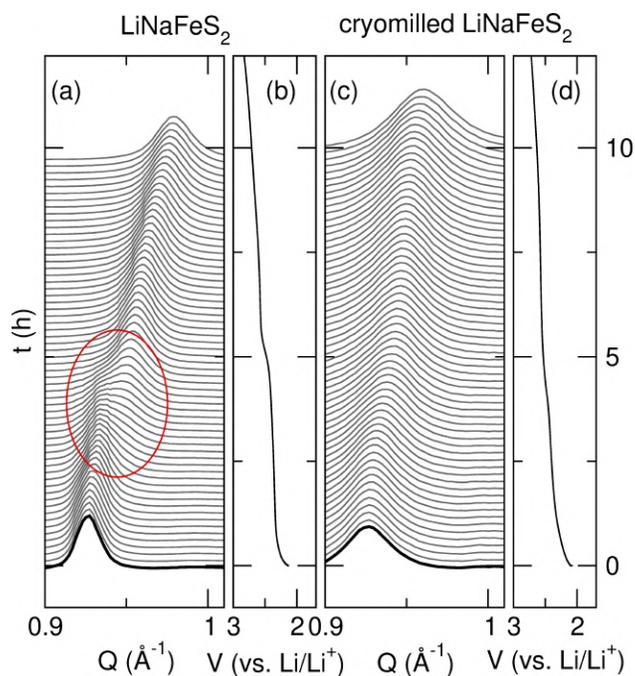


Figure S14: *Operando* sXRD of (a and b) as-prepared  $\text{LiNaFeS}_2$  and (c and d) cryomilled  $\text{LiNaFeS}_2$  magnified up to the first 10 hours of charge to highlight the new peak in as-prepared  $\text{LiNaFeS}_2$ .

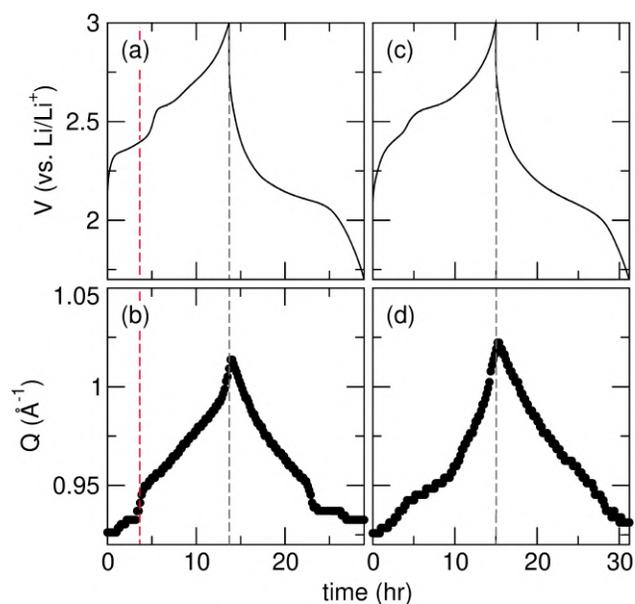


Figure S15: (a) Galvanostatic cycling data of as-prepared  $\text{LiNaFeS}_2$  and (b)  $Q$  of the (001) reflection, and (c and d) corresponding data for cryomilled  $\text{LiNaFeS}_2$ . While both materials' (001) peaks reach the same  $Q$  and thus  $d$ -spacing at the end of charge, as-prepared  $\text{LiNaFeS}_2$  exhibits a jump in  $Q$  suggesting a two-phase mechanism.

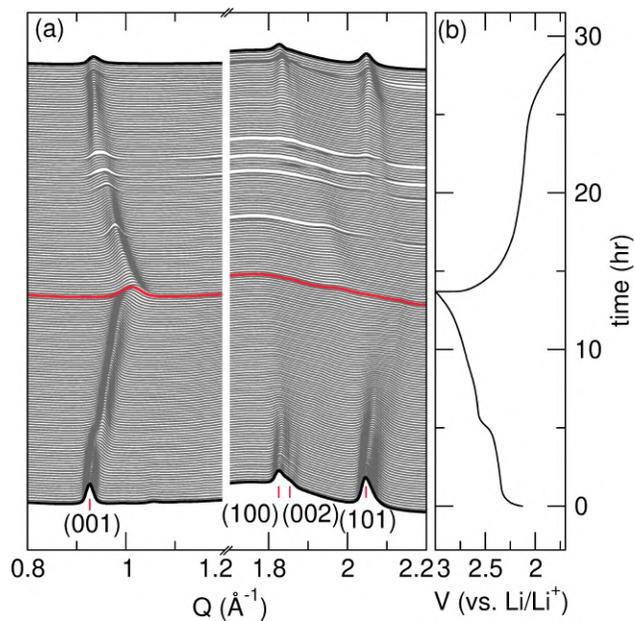


Figure S16: (a) *Operando* sXRD of as-prepared  $\text{LiNaFeS}_2$  of selected  $Q$  regions and (b) the corresponding galvanostatic cycling data.

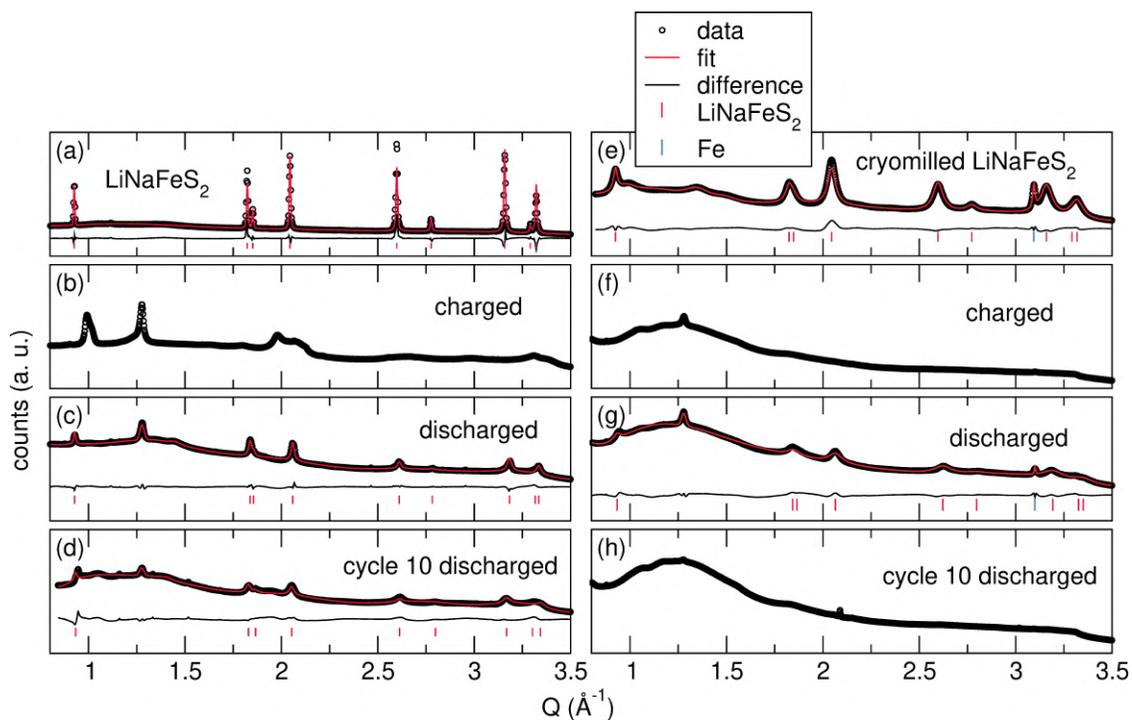


Figure S17: *Ex situ* sXRD of (a–d) as-prepared  $\text{LiNaFeS}_2$  and (e–h) cryomilled  $\text{LiNaFeS}_2$  at different states of charge. The peak at 1.26  $Q$  corresponds to PTFE. While intensity attenuation of cryomilled  $\text{LiNaFeS}_2$  precludes further analysis, diffraction patterns of discharged and cycle 10 discharged as-prepared  $\text{LiNaFeS}_2$  can be fit with Rietveld refinement.