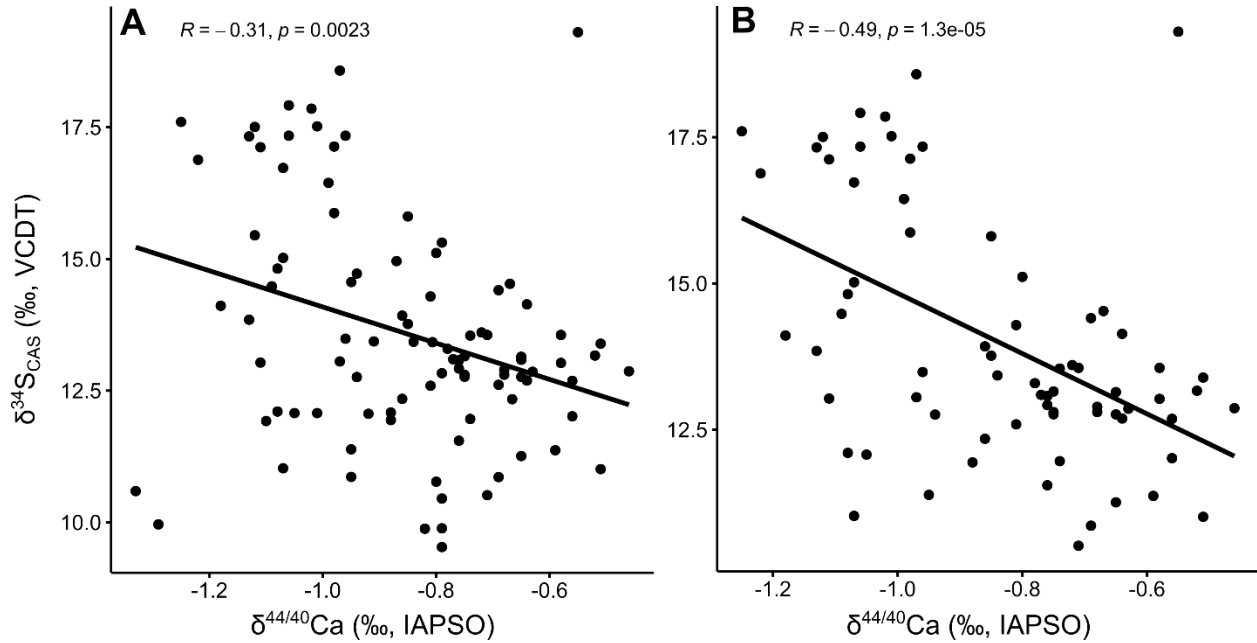


**Appendix A. Supplementary Material for “Early diagenetic constraints on Permian seawater chemistry from the Capitan Reef” by Bryant et al.**

**Table S1** - See attached excel file.



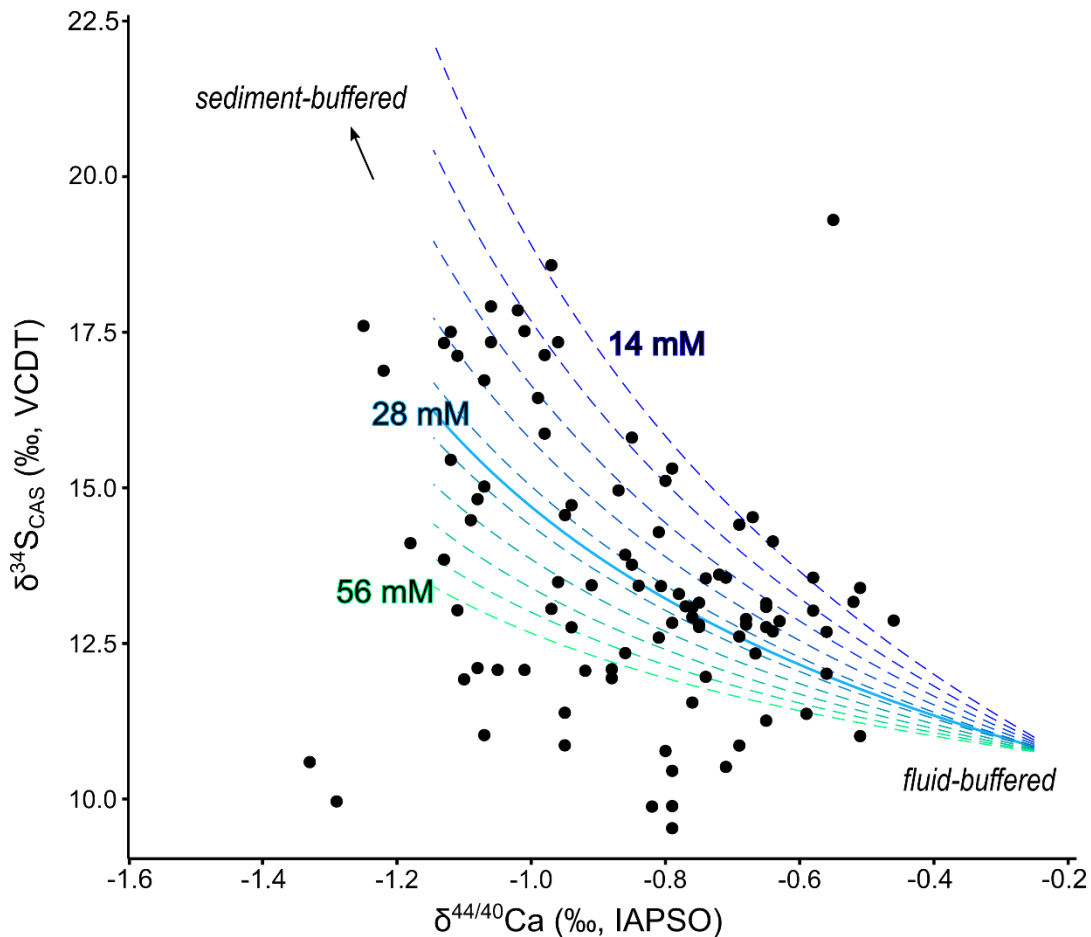
**Figure S1.** Ca and CAS S isotope data for, (A) non-sparry, calcite-dominated samples, and (B) non-sparry, non-EMC, calcite-dominated samples. The black lines are linear regressions through the data, the Pearson correlation coefficients and p-values for which are shown in the top left corner of the plots.

**Sensitivity Analysis**

To determine the importance of different variables to the model output (specifically the diagenetic calcite limb in the Ca-S phase space), we conducted a sensitivity analysis, the results of which are detailed below. Generally, all parameters were held constant while one was varied (within a sensible environmental range based on the published literature). The simplest way of quantifying changes in the model output uses the isotopic offsets (here termed  $\Delta\text{Ca}$  and  $\Delta\text{S}$ ) between the fluid and more sediment-buffered end members (boxes 1 and n in the model). The fluid-buffered end member typically has more positive  $\delta^{44/40}\text{Ca}$  and less positive  $\delta^{34}\text{S}_{\text{CAS}}$  values, whereas the sediment-buffered end member typically has more negative  $\delta^{44/40}\text{Ca}$  and more positive  $\delta^{34}\text{S}_{\text{CAS}}$  values.

### Effect of $[\text{SO}_4^{2-}]_{\text{seawater}}$

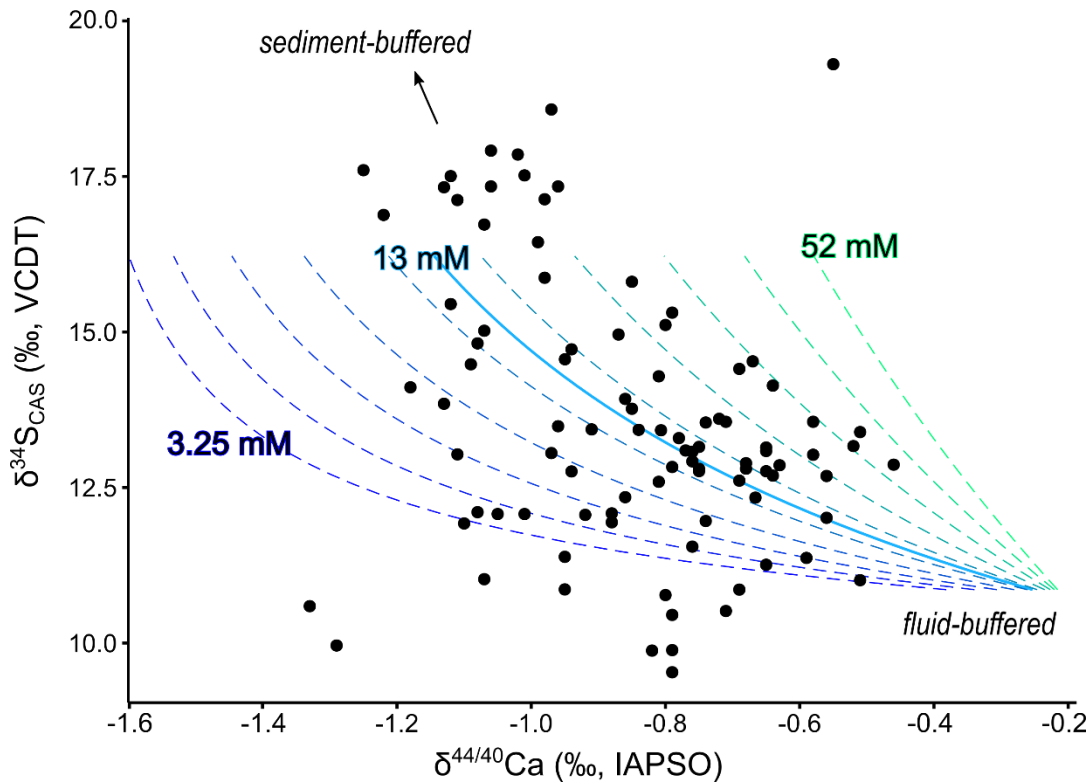
The sulfate concentration in the starting fluid ( $[\text{SO}_4^{2-}]_{\text{seawater}}$ ) has a stark effect on the model output (Figure S2). Raising  $[\text{SO}_4^{2-}]_{\text{seawater}}$  decreases  $\Delta S$ , mostly by virtue of lowering the  $\delta^{34}\text{S}$  value of the more sediment-buffered end-member (box n). In other words, sulfate is drawn down more slowly and thus pore fluids become less isotopically evolved over the length of the flow path. Conversely, lowering  $[\text{SO}_4^{2-}]_{\text{seawater}}$  increases  $\Delta S$  by increasing the  $\delta^{34}\text{S}$  value of the more sediment-buffered end-member (box n). This is because sulfate is drawn down more readily, allowing it to evolve more isotopically over the same flow path length.



**Figure S2.** Effect of changing  $[\text{SO}_4^{2-}]_{\text{seawater}}$  on the relative positions of fluid- and sediment-buffered end member diagenetic calcite in the Ca-S isotopic phase space. Black circles are the data from Figure S1A. At a  $[\text{Ca}^{2+}]_{\text{seawater}}$  of 13 mM, a  $[\text{SO}_4^{2-}]_{\text{seawater}}$  of 14 mM gives the best fit between the diagenetic calcite model limb and the upper limb of the data. The dashed lines are at increments of  $\sim 4.7$  mM between 14 and 56 mM.

### Effect of $[Ca^{2+}]_{seawater}$

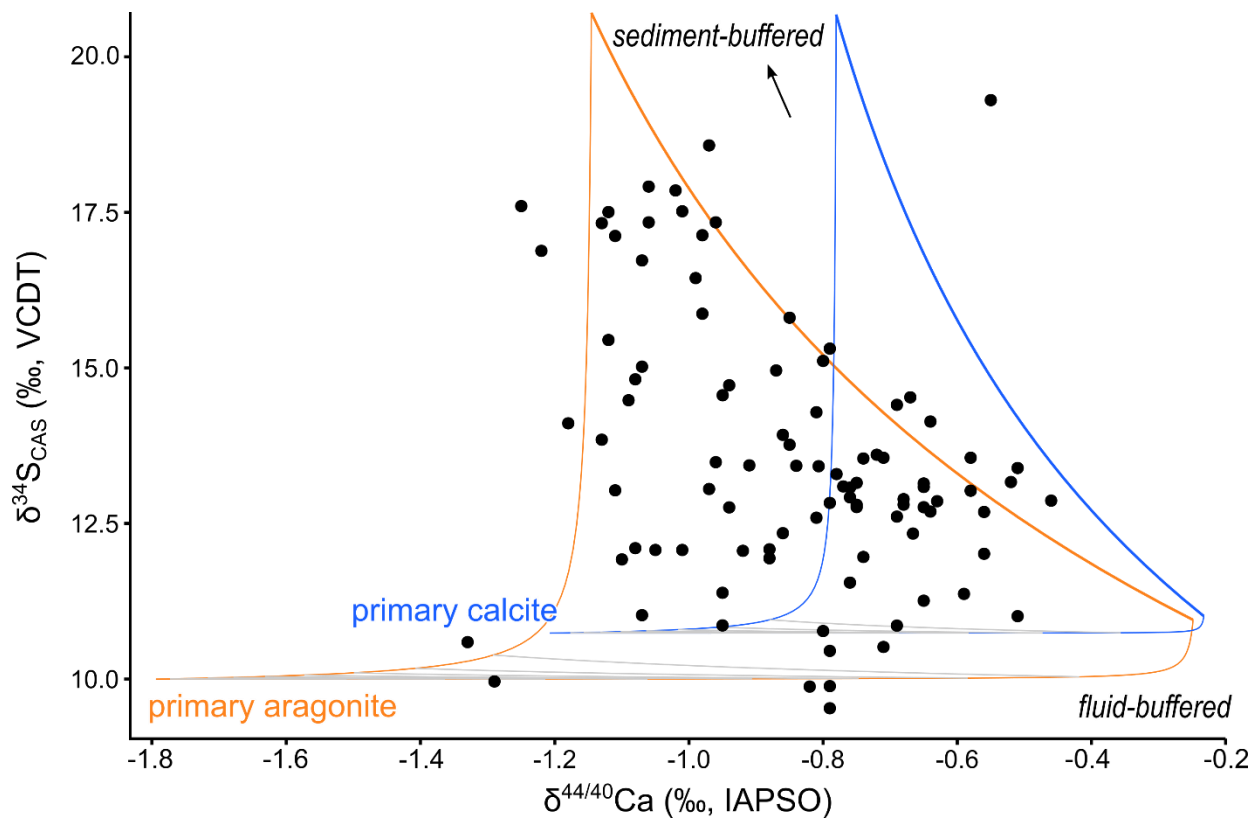
The calcium concentration in the starting fluid ( $[Ca^{2+}]_{seawater}$ ) has a similarly strong effect on the model output (Figure S3). Raising  $[Ca^{2+}]_{seawater}$  decreases  $\Delta Ca$ , mostly by virtue of increasing the  $\delta^{44/40}Ca$  value of the more sediment-buffered end-member (box n). In other words, the pore fluids are fluid-buffered over a longer flow path when there is more  $Ca^{2+}$  in the incoming seawater. Conversely, lowering  $[Ca^{2+}]_{seawater}$  increases  $\Delta Ca$  by decreasing the  $\delta^{44/40}Ca$  value of the more sediment-buffered end-member (box n).



**Figure S3.** Effect of changing  $[Ca^{2+}]_{seawater}$  on the relative positions of fluid- and sediment-buffered end member diagenetic calcite in the Ca-S isotopic phase space. Black circles are the data from Figure S1A. At a  $[SO_4^{2-}]_{seawater}$  of 28 mM, a  $[Ca^{2+}]_{seawater}$  of 20-30 mM gives the best fit (in terms of slope) between the diagenetic calcite model limb and the upper limb of the data, but fails to reproduce the full range of  $\Delta Ca$  and  $\Delta S$  represented in the data. Lowering both  $[Ca^{2+}]_{seawater}$  to ~13 mM and  $[SO_4^{2-}]_{seawater}$  to 16 mM ensures a fit to the full range of  $\Delta Ca$  and  $\Delta S$  represented in the data (see Figure S2). The dashed lines are at increments of ~5.4 mM between 3.25 and 52 mM.

*Effect of primary mineralogy (high-Mg calcite vs. aragonite)*

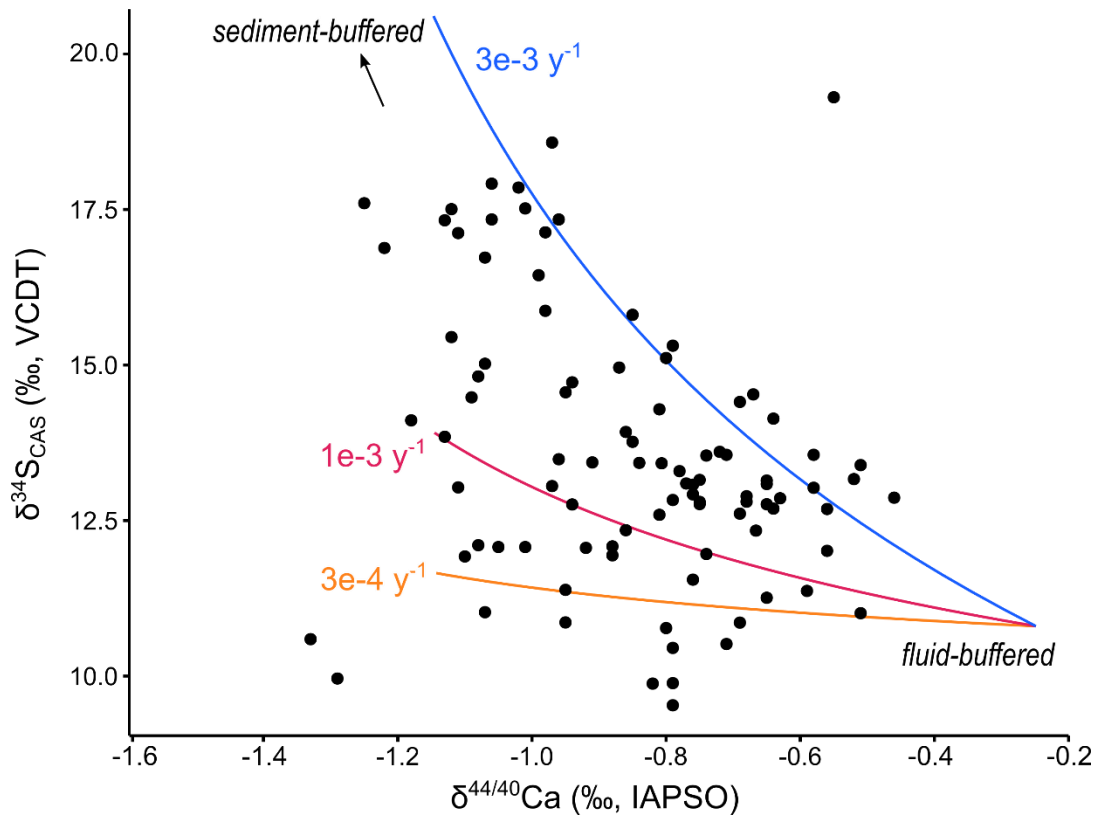
The primary mineralogy (high-Mg calcite vs. aragonite) has a great effect on the model output (Figure S4). Compared to starting with aragonite, starting with calcite gives the same  $\Delta S$ , but much smaller  $\Delta Ca$ , due to the smaller  $\delta^{44/40}Ca$  fractionation between primary calcite and fluid ( $-1.0\text{‰}$ ) vs. primary aragonite and fluid ( $-1.6\text{‰}$ ) (Gussone et al., 2005). As a result of this, the recrystallized product of primary calcite has a steeper slope than the recrystallized product of primary aragonite, assuming all other parameters remain equal. For reference,  $[Ca^{2+}]_{\text{seawater}}$  would need to be 3 mM, rather than 13 mM, for the recrystallized product of primary calcite to have a similar slope (and  $\Delta S$  and  $\Delta Ca$ ) to the recrystallized product of primary aragonite shown in Figure S4.



**Figure S4.** Effect of changing primary mineralogy (calcite vs. aragonite) on the relative positions of fluid- and sediment-buffered end member diagenetic calcite in the Ca-S isotopic phase space. Black circles are the data from Figure S1A.

### Effect of organoclastic sulfate reduction rate (MSR rate)

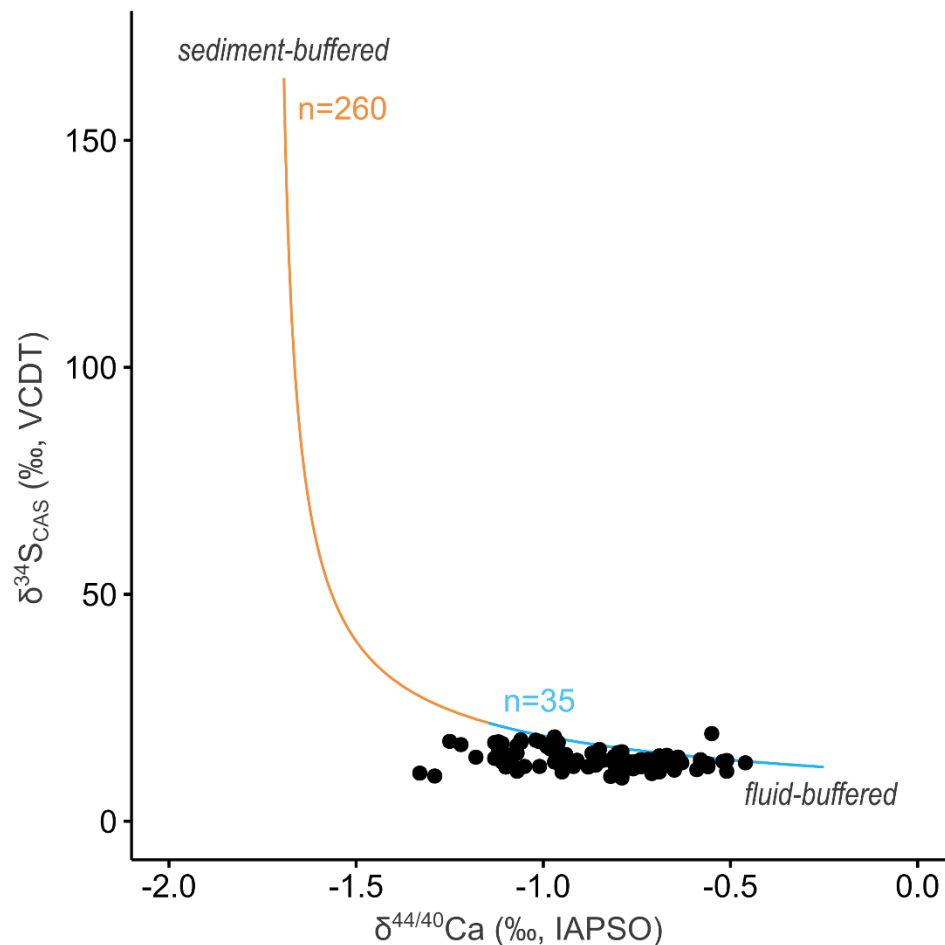
The rate of MSR has a similar effect to  $[\text{SO}_4^{2-}]_{\text{seawater}}$  on the model output. A higher rate results in a higher  $\Delta S$  by increasing the  $\delta^{34}\text{S}$  value of the sediment-buffered diagenetic calcite end member (Figure S5). In other words, in a scenario with a high MSR rate, sulfate is drawn down faster, evolves isotopically, and becomes more sediment-buffered along the fluid flow path. In comparison, in a scenario with a low MSR rate, sulfate is drawn down more slowly and stays more fluid along the same flow path (n=35).



**Figure S5.** Effect of changing MSR rate on the relative positions of fluid- and more sediment-buffered end member diagenetic calcite in the Ca-S isotopic phase space. Black circles are the data from Figure S1A.

### Effect of number of boxes ( $n$ )

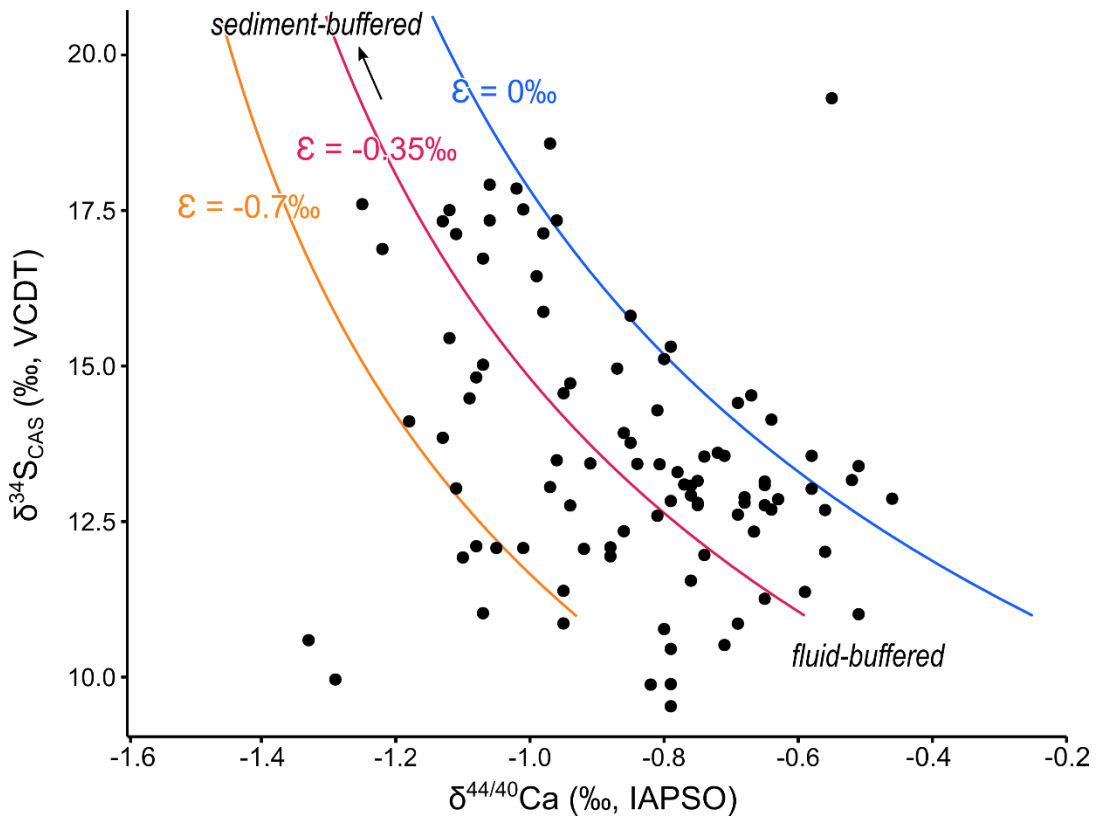
Adding boxes (i.e., longer fluid-flow path, in meters) to the model increases  $\Delta S$  and  $\Delta Ca$ , essentially extending the trajectory of the recrystallization deciles (including the 100% diagenetic calcite limb) to more positive  $\delta^{34}S_{CAS}$  values and more negative  $\delta^{44/40}Ca$ , (Figure S6). It is necessary to add enough boxes to the model to span the entire phase-space from fully fluid-buffered to more sediment-buffered in order to capture the data range within (or within instrumental error of) the model output region – in this case 35 boxes were sufficient. The true sediment-buffered endmember (with respect to sulfur) occurs at  $\sim 260$  boxes, as this length of flow-path is sufficient for the pore water sulfate concentration to be drawn down to zero by the time the primary mineral has completely recrystallized.



**Figure S6.** Effect of changing 'n' (number of boxes) on the relative positions of fluid- and sediment-buffered endmember diagenetic calcite in the Ca-S isotopic phase space. Black circles are the data from Figure S1A.

### Effect of diagenetic $\epsilon_{Ca}$

Assuming a more negative  $\delta^{44/40}\text{Ca}$  fractionation ( $\epsilon < 0\text{‰}$ ) during recrystallization slightly decreases  $\Delta\text{Ca}$  and has no effect on  $\Delta\text{S}$  – this results in a steeper slope. In addition, diagenetic calcite is shifted to more negative  $\delta^{44/40}\text{Ca}$  values. For a  $[\text{Ca}^{2+}]:[\text{SO}_4^{2-}]_{\text{seawater}}$  of 0.8125 ( $[\text{Ca}^{2+}] = 13\text{mM}$ ;  $[\text{SO}_4^{2-}] = 16\text{mM}$ ), most data are fit by assuming  $\epsilon$  is 0 to  $-0.35\text{‰}$ , but some data (mostly EMCs) require  $\epsilon$  to be as negative as  $-0.7\text{‰}$  (Figure S7).



**Figure S7.** Effect of changing the calcium isotope fractionation factor during recrystallization ( $\epsilon$ ) on the relative positions of fluid- and sediment-buffered end member diagenetic calcite in the Ca-S isotopic phase space. Black circles are the data from Figure S1.