

## Nancy Grace Roman Space Telescope Coronagraph Instrument Observation Calibration Plan

ROBERT T. ZELLEM,<sup>1</sup> BIJAN NEMATI,<sup>2,1</sup> VANESSA P. BAILEY,<sup>1</sup> ERIC J. CADY,<sup>1</sup> M. MARK COLAVITA,<sup>1</sup>  
GUILLERMO GONZALEZ,<sup>2</sup> SERGI R. HILDEBRANDT,<sup>1</sup> ERIN R. MAIER,<sup>3</sup> BERTRAND MENNESSON,<sup>1</sup> MARIE YGOUF,<sup>1</sup>  
NEIL ZIMMERMAN,<sup>4</sup> RUSLAN BELIKOV,<sup>5</sup> JOHN DEBES,<sup>6</sup> ROBERT J. DE ROSA,<sup>7</sup> EWAN S. DOUGLAS,<sup>3</sup> JULIEN GIRARD,<sup>8</sup>  
TYLER GROFF,<sup>4</sup> JEREMY KASDIN,<sup>9</sup> PATRICK J. LOWRANCE,<sup>10</sup> BRUCE MACINTOSH,<sup>11</sup> LINDSEY PAYNE,<sup>11</sup> DANIEL RYAN,<sup>1</sup>  
CAREY WEISBERG,<sup>1</sup>

ON BEHALF OF THE ROMAN SPACE TELESCOPE CORONAGRAPH INSTRUMENT PROJECT SCIENCE AND ENGINEERING TEAMS

<sup>1</sup>*Jet Propulsion Laboratory, California Institute of Technology, 4800 Oak Grove Drive, Pasadena, CA 91109, USA*

<sup>2</sup>*Center for Applied Optics, The University of Alabama in Huntsville, 301 Sparkman Drive, Huntsville, AL 35899*

<sup>3</sup>*Department of Astronomy and Steward Observatory, University of Arizona, 933 N. Cherry Ave., Tucson, AZ 85719, USA*

<sup>4</sup>*Goddard Space Flight Center, 8800 Greenbelt Rd, Greenbelt, MD 20771, USA*

<sup>5</sup>*Ames Research Center, PO Box 1, Moffett Field, CA 94035-1000, USA*

<sup>6</sup>*Space Telescope Science Institute, 3700 San Martin Drive, Baltimore, MD 21218, USA*

<sup>7</sup>*European Southern Observatory, Alonso de Córdova 3107, Vitacura, Santiago, Chile*

<sup>8</sup>*Space Telescope Science Institute, Steven Muller Building, 3700 San Martin Drive, Baltimore, MD 21218, USA*

<sup>9</sup>*Princeton University, Princeton, NJ 08544, USA*

<sup>10</sup>*IPAC, MC 314-6, California Institute of Technology, Pasadena, CA, 91125*

<sup>11</sup>*Stanford University, 382 Via Pueblo Mall, Physics Department, Stanford, CA 94305-4060, USA*

### ABSTRACT

NASA’s next flagship mission, the Nancy Grace Roman Space Telescope, is a 2.4-meter observatory set to launch no later than May 2027. Roman features two instruments: the Wide Field Imager and the Coronagraph Instrument. Roman’s Coronagraph is a Technology Demonstration that will push the current capabilities of direct imaging to smaller contrast ratios ( $\sim 10^{-9}$ ) and inner-working angles ( $3 \lambda/D$ ). In order to achieve this high precision, Roman Coronagraph data must be calibrated to remove as many potential sources of error as possible. Here we present a detailed overview of the Nancy Grace Roman Space Telescope Coronagraph Instrument Observation Calibration Plan including identifying potential sources of error and how they will be mitigated via on-sky calibrations.

### 1. INTRODUCTION

NASA’s next flagship mission, the Nancy Grace Roman Space Telescope, is a 2.4-meter observatory set to launch no later than May 2027. Roman features two instruments: the Wide Field Imager and the Coronagraph Instrument. The Coronagraph (Fig. 1) features photometry centered at 575 nm (Band 1; 10% bandwidth) and 825 nm (Band 4; 15% bandwidth), polarimetry at these same two passbands, and slit spectroscopy with a resolution of  $R \sim 50$  centered at 730 nm (Band 3; 15% bandwidth) and 825 nm (Band 4; 10% bandwidth). The Coronagraph also employs an electron multiplying charge-coupled device (EMCCD; e.g., [Morrissey 2018](#)), a detector that is optimized for low photon count rates by achieving near-zero effective read noise, and deformable mirrors (DMs) to correct for any aberrations to the wavefront (e.g., [Zhou et al. 2020](#)).

The Roman Coronagraph’s Technology Demonstration Threshold Requirement (TTR5) is: “Roman shall be able to measure (using the Coronagraph Instrument), with  $\text{SNR} \geq 5$ , the brightness of an astrophysical point source located between 6 and 9  $\lambda/D$  from an adjacent star with a  $V_{AB}$  magnitude  $\leq 5$ , with a flux ratio  $\geq 1 \times 10^{-7}$ ; the bandpass shall have a central wavelength  $\leq 600$  nm and a bandwidth  $\geq 10\%$ .” The Roman Coronagraph is expected to have the capability to observe up to a contrast ratio of  $\sim 10^{-9}$ ; in order to achieve this contrast, all Roman Coronagraph data must be calibrated in order to remove as many different sources of error as possible.

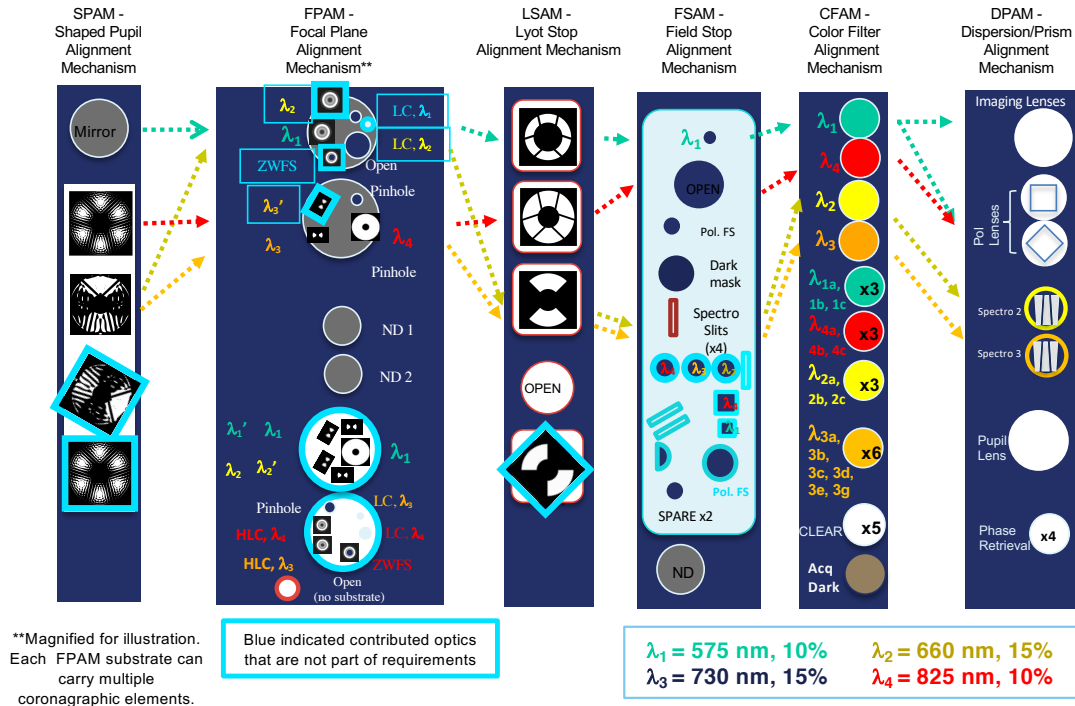
Here, we present a snapshot of the current plans for the “calibration branch”, which is a continuing work in progress and part of the overall Roman Coronagraph noise budget. The calibration branch of the Flux Ratio Noise (FRN)

Calibration Product	RSME Allocation on Fp/Fs	CBE	Margin
Charge Transfer (In)Efficiency	2.7%	1.1%	59%
Detector Noise Background	1.5%	1.5%	0%
Flat Fields	2%	0.75%	63%
Image Corrections	1%	0.71%	29%
Absolute Flux	2%	1.41%	30%
Core Throughput	1.6%	1.44%	10%
<b>Total</b>	5.0%	2.93%	41%

**Table 1.** The suballocations for the Roman Coronagraph Instrument Observation Calibrations in units of root-square-mean error (RSME) allocation on measuring the planet-to-host star flux ratio Fp/Fs during Technology Demonstration Operations.

budget includes all the errors incurred in converting the central value of the planet signal to a planet-to-host-star flux ratio ( $F_p/F_s$ ). Calibration deliverables include calibration data products and algorithms. Calibration accuracy can be affected by random noise terms—for example, detector read noise in the calibration datasets. In order to ensure accurate modeling of the error propagation, sensitivities, and tally of total error, the allocations to the calibration budget include allowance for such additional errors, leaving to each calibration area to tally the current best estimate (CBE) including these impacts. Should these “external” errors increase, there will be an impact on calibration errors. This is in keeping with other inter-relationships between delivery areas within the CGI system.

Unless otherwise explicitly noted, the calibrations discussed in this document have allocations, not requirements, on their root-mean-square error (RMSE) contributions to the planet-to-star flux ratio. Allocations can shift between various calibration products, if necessary, as the plan matures. In addition, all calibrations are currently baselined for on-sky operations and, unless otherwise noted, all processing will occur on the ground. In Table 1, we provide the current RSME allocations associated for Technology Demonstration operations, with each of the calibration products listed in detail below; note that the total roll-up of these allocations must be  $\leq 5\%$ . Goal observations (e.g., Band 4 photometry, polarimetry, and spectroscopy) build upon the calibration for TTR5 (Table 1), with potentially some changes to various allocations (to be refined).



**Figure 1.** The Roman Coronagraph features three observation modes (direct imaging, polarimetry, and spectroscopy) implemented with three different sets of masks/filters which are installed in the Coronagraph's 6 Precision Alignment Mechanisms (PAMs; SPAM, FPAM, LSAM, FSAM, CFAM, and DPAM). The dashed arrows indicate the path of light through the Coronagraph's PAMs for direct imaging or polarimetry at Bands 1 (green) and 4 (red) and spectroscopy at Bands 2 (gold) and 3 (navy). The two neutral density (ND) filters installed in the FPAM have an optical description (OD) of 4.75 ( $10^{-4.75}$  throughput attenuation) and 2.25 ( $10^{-2.25}$  throughput attenuation) while the ND filter in the FSAM has an OD of 4.75.

## 2. DETECTOR NOISE BACKGROUND

### 2.1. Purpose

The purpose of these calibrations is to correct the images for the structured background from dark current and clock-induced charge (CIC), as well as read noise leakage. These effects create a background in the image that needs to be subtracted. Since they follow shot noise statistics, collecting more dark frames reduces the noise that the dark subtraction itself will inject. Darks also have the added benefit of capturing fixed pattern noise, stray light from ray paths outside the main Coronagraph beam, and sensor glow. Since read noise leakage can be calibrated with high precision using overscan data, the dominant error, and the calibration described here, are focused on Darks and CIC.

### 2.2. Allocation

1.5% RMSE in Fp/Fs (assuming the two resolution elements have the same uncertainty, then each has an allocation of 1.1% per resolution element).

Note: The stellar signal Fs is so large that darks are negligible by comparison. Therefore, we describe here the process for calibration of photon counting target star observations.

### 2.3. Basis of Estimate

In the TTR5 case,  $F_p/F_s = 10^{-7}$ . For a 5<sup>th</sup> magnitude host star, the planet will have 0.22 photons/resel/sec. For the minimal TTR5 integration time ( $\sim 100$  images, 2 sec each), there will be  $\sim 45$  planet photons collected. Therefore, uncertainty in the dark counts should be no more than 1.5% of 45 e<sup>-</sup>, or 0.68 e<sup>-</sup>.

The dark current CBE is  $< 1$  e-/px/hr for  $> 95\%$  of pixels, or  $< 5.3$  e-/resel/hr, or  $\sim 1.5E-3$  e-/resel/sec. In 200 sec, the minimum integration time needed to reach SNR=5 on a TTR5 planet, we would expect an average of 0.3 e-/resel/200 sec

We next consider the combined effect of dark current and CIC. We conservatively assume CIC acts entirely as a static two-dimensional pattern that must be calibrated for each pixel independently. The EOL CBE for combined dark+CIC is 0.06 e-/resel/frame. After 100 frames, the minimum number of frames needed to achieve SNR=5 on a TTR5 planet assuming 2 second exposures, we expect an average of 6 e<sup>-</sup> (standard deviation = 2.45 e<sup>-</sup>) per resel. In order to meet the allocation, we need to reduce this dark current+CIC error by a factor of  $2.45 \text{ e}^- / 0.68 \text{ e}^- = 3.6$ . This means we need  $3.6^2 = 13x$  more frames to produce a measurement of the mean dark + CIC counts per 100 images that is accurate to 0.68 e-/resel or better. Therefore, we will need 1300 2-second frames (about 45 min integration time) to achieve the allocated root mean square error in the master dark + CIC image with no margin.

### 2.4. Calibrations

Dark current may have a repeatable two-dimensional structure and CIC likely also has a repeatable structure (for a given detector clocking scheme). Any on-orbit changes to the sensor thermal configuration can change the dark pattern and radiation damage can change both darks and CIC. While we may find that in practice these patterns undergo little change over time, our baseline is to measure them for every observation campaign.

These darks are collected in temporal proximity to the Tech Demo observation data, in order to ensure the dark levels are pertinent. Ideally, dark collection is split equally into two blocks: just before and just after the entire observation sequence. The Coronagraph will take darks when it is in “secondary” status (i.e., during WFI observations), so that no Coronagraph on-sky time is wasted on dark collection. The Coronagraph has the same data rate allocation in secondary mode as in primary mode, and standby power is sufficient for dark collection; a “dark” (non-transmissive) blank-off filter will be used during dark collection. There are no other constraints placed on observatory operations.

### 2.5. Processing

The data processing is done on the ground in the Data Analysis Environment using software that shall be provided. These frames are processed in the same way as target frames, including photon counting and associated corrections. The mean dark and CIC per pixel per image is computed from the ensemble of unilluminated images. It is subtracted from coadded photon-counted target data, with the appropriate scale factor to account for the number of frames.

### 2.6. Future Work

Once we have the opportunity to measure darks with the flight detector, we will have more insight on the stability of the dark pattern. This stability will inform the plan on how frequently the dark calibration should be updated.

### 3. CHARGE TRANSFER INEFFICIENCY

#### 3.1. Purpose

The effects of Charge Transfer Inefficiency (CTI) are seen as the trailing of charge in the readout direction on a CCD during readout. Charge traps in the pixels temporarily capture and release electrons during parallel and serial readout on their way to the amplifier. The traps are caused by radiation damage to the silicon lattice. As such, the density of charge traps increases over the mission lifetime of a CCD in a space telescope. Mitigating the effect of these traps is necessary to recover the true astrophysical signal.

The overall density of charge traps has been monitored on Hubble’s ACS/WFC, confirming that it is increasing approximately linearly over time due to the accumulated effects of radiation damage. CTI is the most important factor limiting high precision observations with HST (Massey et al. 2014) and the upcoming Euclid mission (Skottfelt et al. 2017).

#### 3.2. Allocation

2.7% RMSE in Fp/Fs (assuming the two resolution elements have the same uncertainty, then each has an allocation of 1.9% per resolution element).

#### 3.3. Basis of Estimate

The bases of estimate are a published trap pumping analysis of radiation damaged EMCCDs, similar to the Coronagraph flight EMCCD (Bush et al. 2021), and simulations of image corruption with the CTI simulation/correction software ArCTICPY, which yield a CBE <1.6% RSME in Fp/Fs (>41% margin) . About 98% of the CTI trailing in Hubble images can be corrected in post-processing; the resulting fractional residual flux errors are near 0.3% (Massey et al. 2014)). However, to date none of the published studies address CTI image corruption and correction for photon-counted images. Since the Coronagraph will employ photon counting for the planet observations, we have performed a first round of simulations to gauge the magnitude of CTI trailing on its photometry.

The publication of pixel densities for five species of charge traps by Bush et al. (2021) for several levels of proton radiation fluences spanning the range of expected fluences during the Roman mission permits us to predict the individual trap densities for any point in the mission. The other basic trap parameters that are derived from trap pumping frames include trap locations, capture cross sections, and charge release time constants. Charge trails behind warm pixels on dark frames can also be used to derive trap densities and release time constants, but only as a global average.

To test the magnitude of corruption to photon counted images, ArCTICPY was employed to produce CTI trailing on simulated images. Figure 2 shows the predicted count rate based on an input flux map with 500 rows and 20 columns with a line of constant charge at row 490 (from the readout register). This setup takes account of the fact that the Coronagraph image will be located about 500 pixels from the readout register on the CCD. This is important, because the amount of charge trapping will increase with the number of pixels traversed during readout. 332 frames with only Poisson noise and an EM gain of 5000 were generated, each with traps. The frames were then photon-counted, co-added and corrected for coincidence efficiency loss. This test indicated that an upper limit of 1.1% per resel (1.6% RSME on Fp/Fs, assuming that any two resels have the same uncertainty) could be set on the effect of CTI on the measured counts in photon counting mode.

#### 3.4. Calibrations

The total trap density in the Hubble ACS CCD has increased linearly over timescales of years, demonstrating that while CTI needs to be monitored regularly over the Roman mission; a timescale of months between measurements should be adequate. (For context, the Coronagraph Tech Demo Phase ends at ~21 months after launch.) Frames are collected using the trap pumping method, which is a planned capability of the flight camera. In trap pumping mode, the Coronagraph EMCCD is provided dark conditions by inserting a dark mask. Then a series of clocking sequences are applied that 1) inject extra charge into the pixels via the clock induced charge process, thereby creating what looks like a flat frame, and 2) the clocking is modified to allow these charges to interact with any traps. At the end of this process, the image shows “dipoles” where neighboring pixels near the trap show excess and loss. These are then analyzed to get the trap release times. Trap pumping frames must be obtained at multiple sensor temperatures in order to derive accurate release time constants for each species of charge trap from the resultant dipole images; different species have different temperature dependencies. The temperature range should range from cold operating temperature to cold + ~50 K (or the maximum operating temperature, whichever is lower), and should include the

nominal operating temperature. The EM gain setting is not directly relevant, since the CTI effects are all prior to the gain process. However, to improve the SNR of the dipoles, the EM gain setting should be the value that optimizes the dipole images in the trap pumping frames

Due to the planned temperature cycling of the Coronagraph EMCCD, operated cold only during Coronagraph observations to limit radiation damage, trap pumping calibration frames should be acquired during both warm-up and cool-down cycles. Warming the sensor will anneal a fraction of the trap lattice defects and thus alter their densities. Trap pumping frames acquired during a warm-up cycle will provide knowledge of trap densities during the prior Coronagraph observations. Trap pumping frames acquired during a cool-down phase will provide knowledge of trap densities applicable to the next set of Coronagraph observations. At a minimum, trap pumping should be performed at sensor temperatures spanning 450 K and include the nominal temperature. The precise values of the sensor’s temperature are not important, but they need to be known after the fact.

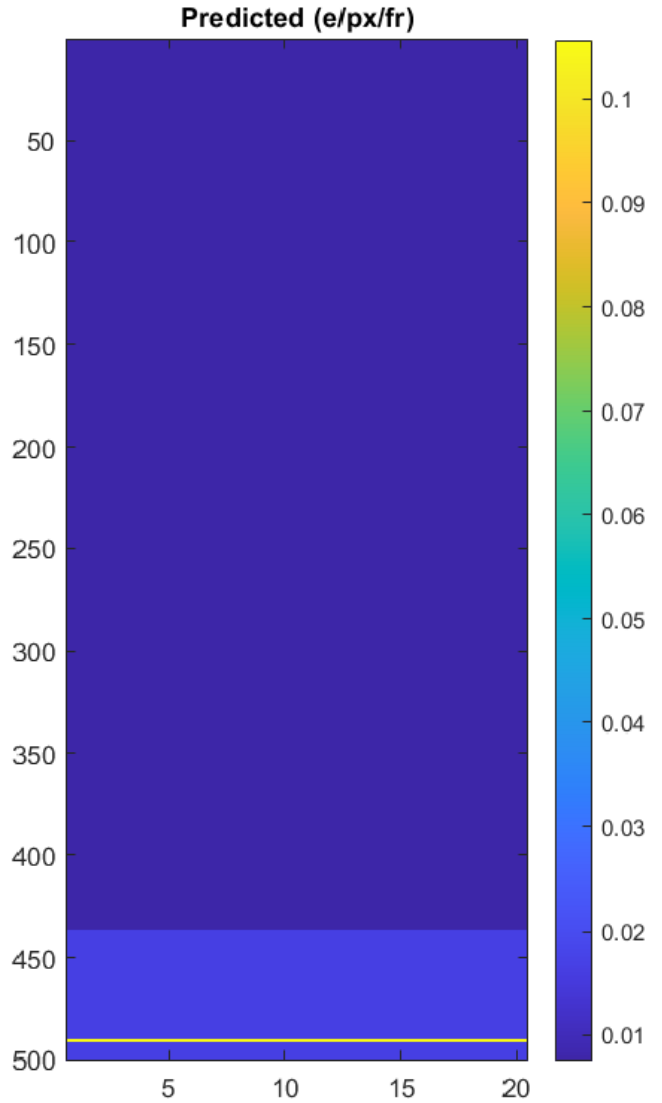
### 3.5. Processing

The trap properties will be measured from the trap pumping frames and warm pixels in the dark frames using the analyses described in [Bush et al. \(2021\)](#) and [Massey \(2010\)](#) on ground; requisite software, using a modified version of the ArcticPy CTI correction software, shall be developed.

### 3.6. Future Work

To date none of the published studies address CTI image corruption and correction for photon-counted images, and CTI effects are expected to be worse. Since the Coronagraph will employ photon counting for the planet observations, we are conducting simulations to gauge the magnitude of CTI trailing on its photometry.

Given that each photon-counted image typically has only a few non-zero pixels, it is not possible to reconstruct the charge lost from astrophysical sources from individual images, as is done in the current version of ArcticPy CTI correction software. A modified algorithm will need to be developed.



**Figure 2.** Predicted rate (e-/pixel/frame) from an input flux map with 500 rows and 20 columns with line of charge at row 490. The readout register is at the top of the image. The top 435 lines include only the expected dark current. The bottom 65 rows also include background at 10% the level of the line charge, also the expected level for TTR5. The co-added image based on 332 photon counted simulated frames from this flux map yielded an upper limit of 1.1% per resel (1.6% RSME on  $F_p/F_s$ , assuming that any two resels have the same uncertainty) on the erosion of the counts in the line of charge.

## 4. FLAT FIELDS

### 4.1. Purpose

Please note that the content below is an overview of the flatfielding operations currently planned for the Roman Coronagraph. For more information, including more details into the simulations of the proposed observing sequences that established our Basis of Estimate, please see [Maier et al. \(2022\)](#).

Three effects are expected to impact the Coronagraph’s effective throughput at three different spatial scales: 1. high-spatial-frequency responses in the form of pixel-to-pixel gain variations, 2. mid-spatial-frequency responses (“measles” due to particle deposition on the detector, as observed by heritage Hubble/WFPC1 data (WFPC1 Instrument Science Report 92-11), and focal plane mask substrates), and 3. low-spatial-frequency responses (fringing and vignetting effects; please note that fringing effects are negligible at Band 1 TTR5 wavelengths). Given that the Coronagraph will be observing the planet-to-star flux ratio  $F_p/F_s$  and that the location of the planet will not necessarily be known a-priori, the planet and star will likely fall on different portions of the focal plane, and thus each will be subject to a different system throughput. Therefore, a relative throughput calibration, in the form of a flat field, is necessary to “translate” observations at one position of the focal plane (e.g., the planet) to any other (e.g., the host star). These flat fields can then be combined with Absolute Flux Calibrations (Section 7), whereby a standard star is observed at a single position on the focal plane, to provide absolute flux calibrations for the entire focal plane.

### 4.2. Allocation

The RMSE in  $F_p/F_s$  allocated to flat fields is 2.0% on the ratio of the values of any two resolution elements (assuming the two resolution elements have the same uncertainty, then each has an allocation of  $\leq 1.41\%$  per resolution element).

### 4.3. Basis of Estimate

Our current best estimate (CBE) for the root square mean error on Band 1 flat fields is 0.45% (0.53%) per resel, if using Uranus (Neptune) as a flat field source, corresponding to margins of 68% and 62% per resel, respectively. Assuming that any two resolution elements have the same uncertainty, then these CBEs are 0.64% (68% margin) and 0.75% (63% margin), for Uranus and Neptune, respectively. These CBEs are derived from detailed simulations of the Coronagraph flat field observations of Neptune and Uranus. Please see “On-sky Calibrations” below for more details.

### 4.4. Calibrations

The Coronagraph does not have an internal calibration source, so we will instead use an astrophysical source as a natural “flat lamp”. While various sources were considered, including nebulae and galaxies (e.g., the Andromeda Galaxy M31), the Solar System planets Uranus and Neptune were found to be ideal candidates due to their observational availability over the Coronagraph Technology Demonstration phase, their relatively large angular size (allowing any single exposure to sample a large number of pixels simultaneously; Uranus:  $\sim 3.5$  arcseconds diameter; Neptune:  $\sim 2.5$  arcseconds diameter), and their ability to achieve high SNR measurements in comparatively short exposure times by merit of their comparatively high surface brightnesses (Uranus: 8.2 V-mag/arcsecond<sup>2</sup>; Neptune: 9.4 V-mag/arcsecond<sup>2</sup>). Roman does not have non-sidereal tracking capabilities. We will acquire the planets by first acquiring a nearby star and then sending a timestamped pointing offset to the known position of the planet to “ambush” the targeted solar-system object, and as such will incur an inefficiency at the start of the sequence, as we must allocate buffer time to allow for absolute-time observations within the otherwise event-driven Roman paradigm. Planet motion over the course of 1 exposure ( $\sim 0.15$  arcsec/min for Uranus and  $\sim 0.09$  arcsec/min for Neptune) is negligible compared to size of the raster pattern (described below) and so will not impact the retrieved flatfields.

Given their angular sizes, neither planet will fully cover the focal plane (the entire unvignetted area for direct imaging is a circle with diameter of 7.2 arcseconds). We will dither the planet across the focal plane with a series of fixed-time telescope repointings. Typical dither step sizes will be 1.2 arcseconds, and we will take one or more exposures per position (for calibrating the entire unvignetted focal plane- Uranus: 25 dither positions; Neptune: 36 dither positions).

Simultaneously during an exposure, we will initiate a Fast Steering Mirror (FSM) circular raster pattern with a radius of 0.95 arcseconds conducted over 1 minute to flatten out any spatial variations in the planet itself. For Band 1 TTR5 observations, the Coronagraph will require  $\sim 0.6$ -hours of wall clock time (exposure time + overheads) for Uranus and  $\sim 0.9$ -hours of wall clock time (exposure time + overheads) for Neptune for the entire unvignetted field of view in direct imaging mode (a circle of diameter 7.2 arcseconds). Execution times are conservative estimates; if only calibration of the TTR5 FOV ( $\sim 1$  arcsecond diameter) is desired, the number of dithers, and thus the amount of

time to construct a flat, could be reduced significantly (e.g., Uranus: 9 dither positions taking 0.2 hours to complete; Neptune: 20 dither positions taking 0.5 hours to complete). Thus, the numbers provided here for the entire unvignetted FOV are a conservative estimate of the total number of dithers and time needed to construct a flat field. Flats will be collected both with and without the focal plane mask (FPM) in place to enable the search for any depositions on the FPM substrate itself, which would affect the measured spatial response. This ‘‘FPM map’’ can then be used to correct any data taken with a slightly different FPM position.

We verified the use of Uranus and Neptune as flat sources via detailed simulations (Maier et al. 2022). For these simulations, we used actual Hubble/WFC3 images of Uranus and Neptune from the URANUS-MAPS (ID: 15262) and NEPTUNE-MAPS (ID: 15502) programs taken with WFC3’s UVIS F547M filter, which is similar to the Coronagraph’s Band 1. Six Hubble images each of Uranus and Neptune are chosen as inputs. Each set of 6 consists of 3 pairs of images: the 2 images in each pair were taken 10 minutes apart, and the 3 pairs are all separated by several hours in time. This allows us to simulate the effects of any temporal variation in the flat field source due to planet rotation. The images were then convolved with a flat disk to simulate rastering during integration by moving the FSM, and individual exposures were constructed to simulate dithers of the planet across the entire unvignetted portion of the focal plane over multiple exposures (Uranus: 25 dithers; Neptune: 36 dithers). A matched filter of the planet was constructed from all of the dithered images; this filter was then divided out from each filter to remove the coherent astrophysical signal. The residuals from this division are the measurement of the Coronagraph’s flatfield. We find that this method works well, providing  $\geq 61\%$  margins for TTR5.

#### 4.5. Calibration Frequency

Given the potential for time variability in flat fields, as demonstrated with heritage Hubble/STIS measurements (STIS Instrument Science Report 99-06), we conservatively adopt an observing strategy where flat fields are measured as close to an observing campaign as possible to monitor for any temporal variations. To accurately map depositions on the mask substrates, we recommend conducting flat field calibrations before and as close to an observation campaign.

#### 4.6. The Roman Coronagraph Configuration

As noted above, Coronagraph flats will be conducted both with and without the focal plane mask (FPM) in place.

#### 4.7. Processing

A matched filter method will be implemented to divide out the common-mode planetary signal, leaving behind residuals due to the flat field. As described in detail above, Uranus or Neptune will be dithered across the field of view over multiple exposures to expose the focal plane to photons. Each dither will be centroided and stacked on top of each other to create a matched filter via a median. This matched filter is then in turn divided out from each individual dither; and the residuals are the Coronagraph flat field for that epoch. These flat fields will be constructed on ground.

#### 4.8. Future Work

Future work includes conducting a robust trade study of the FSM raster size vs. the dither step size, the explicit simulation of the raster pattern as opposed to approximating it with a uniform disk, precise modeling of resel size/plate scale, including Roman pointing instability and planet orbital motion, and perform more robust modeling of the required number/timespan of images included in each matched filter.

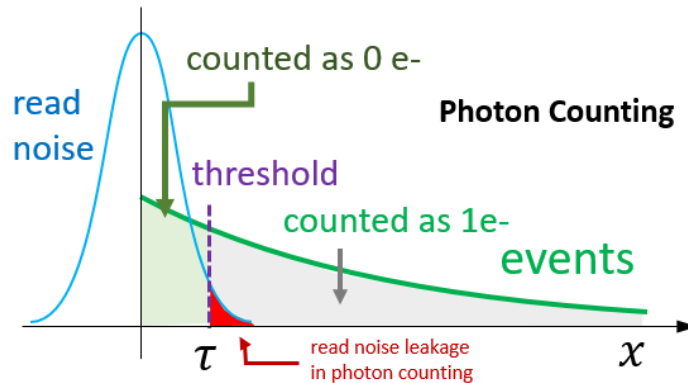


## 5. IMAGE CORRECTIONS

### 5.1. Purpose

Image corrections primarily include the photon counting photometric corrections used to correct for thresholding and coincidence losses when photon counting. These, along with cosmic ray tail and hot pixel identification, are among the image corrections, and are allocated a total  $F_p/F_s$  RSME error of 1%. In photon counting, the EMCCD will be operated at high gain ( $>3000\times$ ) at relatively high frame rates. Thresholding is applied to make the read noise effectively 0. In thresholding, all pixels with analog counts greater than some threshold, typically around 3–5 times the read noise (standard deviation), are counted as 1 photon. The rest of the pixels, i.e., those below the threshold, are assigned 0 counts for that frame. The choice of threshold is a free parameter chosen by the data analyst, based on a trade between false positive rejection and efficiency. The data collection is always analog, and photon counting is always a post-processing step. Since no allowance is made for more than one electron being generated in a single pixel and frame, these “coincidence” cases are undercounted.

Thus, photon counting mode raises two possible sources of uncertainty: thresholding and coincidence loss. Thresholding loss occurs when we record zero electrons when there actually was 1 (or more) image electrons from any source; electron multiplication (EM) is a stochastic process and not all input electrons are amplified by the same exact gain factor. Coincidence loss occurs when we record 1 electron, but there were in fact multiple electrons present in the pre-EM pixel. See Figure 3 for an illustration.



**Figure 3.** Threshold effects in photon counting. There is a tradeoff between increasing threshold to reduce read noise and excluding signal from the target source. The thresholding and coincidence loss corrections depend on knowledge of EM gain and threshold.

Also contributing to the photon counting error is the error from nonlinearity and K gain knowledge as well as cosmic rays. The measured planet-to-star flux ratio  $F_p/F_s$  must not be biased by more than 0.1% due to cosmic rays events that are misidentified as real photons; this is part of the total error allocation (described below).

### 5.2. Allocation

The RMSE in  $F_p/F_s$  allocated to photon counting photometric corrections is  $\sim 1\%$  per two resolution elements. Since threshold and gain knowledge apply to the entire image, we conservatively take per resel errors as per pixel errors and also assume the per-resel errors do not combine via the root-sum-square, but add linearly. Thus, per pixel, the allocation is 0.5% RMSE on the planet-to-star flux ratio  $F_p/F_s$ . There is a threshold over gain multiplier to go to intrinsic fractional errors, with the result that, for photon counting corrections: 1. the EM gain knowledge allocation is 4.1% fractional error on EM gain and 2. the K gain & linearity knowledge combined allocation is 2.5% fractional error on K gain & nonlinearity.

### 5.3. Basis of Estimate

The correction needed for photon counted frames consists of running an algorithm (Nemati 2020) that takes in the co-added photon counted image, the number of frames that were used to create it, the EM gain, K gain, and the nonlinearity table (these last two will be products of the nonlinearity calibrations). This algorithm then yields the

fully-corrected mean expected rate in units of electrons per pixel per frame. That correction has an inherent error of  $< 0.1\%$  when done at the 3<sup>rd</sup> order level. The dominant errors are those arising from calibration error on the EM gain (3.8%) and the photon counting threshold. The threshold knowledge error arises from K gain calibration error (CBE 2.5%). There is, in the case of these two error sources a suppression factor of (t/G), i.e., threshold over gain, which works out to be  $\sim 1/10$ . This means that in Fp/Fs fractional error units, the contributions from these two error sources are 0.38% and 0.25%, respectively. Also these are the numbers per resel. For the total error we double the number; since these numbers are not independent; they do not combine via the root-sum-square. Other error contributions in this category are the error in cosmic ray tail removal and hot pixel removal, for which we set an upper limit of 0.1% per pixel.

Here we give a simple statistical argument to estimate the allowed rate of "false negatives" (cosmic rays incorrectly identified as photons from the planet or star). We first determine the "false negative" rate that would produce a 0.1% error on the flux of a TTR5 planet, which has a planet-to-star flux ratio Fp/Fs of  $10^{-7}$  and a V-mag 5 host star. (Given that the bias on Fs is small compared to the bias on Fp, because Fs is much brighter, we use observations of the planet's flux Fp as the limiting case). A TTR5 planet around a V=5 host produces  $\sim 0.22$  photons/resel/sec. The "resolution element" or "resel" is the FWHM-diameter aperture,  $\sim 5.3$  pixels in Band 1. In a 5 second exposure, an average of 1.4 planet photons are collected in a resel. For a 0.1% change to the measured planet flux, there can be no more than 1 "false negative" (false photon) per  $\sim 710$  images. (Recall that in photon counting mode, only 1 photon is recorded, regardless of the size of the deposited charge in the pixel). If we conservatively assume that the entire  $\sim 5$  pixel resel would be filled by a single missed cosmic ray event, the allowed false negative event rate falls to 1 per  $\sim 3500$  images. We next calculate the fraction of cosmic ray pixels that must be misidentified to result in 1 false negative per resel per 3500 5-second images. The typical Galactic Cosmic Ray flux is taken to be 5 particles/cm<sup>2</sup>/s (Gaia saw 2-4 particles/cm<sup>2</sup>/s; Kirsch 2018). This equates to  $\sim 45$  cosmic ray hits per 1024x1024 pixel image (13  $\mu\text{m}$  pixels). Assuming that cosmic ray rates follow Poisson statistics, the 90<sup>th</sup> percentile upper limit is 53 cosmic ray hits per image. Given the cosmic ray trail geometry described above, this equates to a  $\sim 2.5\%$  covering fraction of the image. Multiplying the allowed false negative rate per resel by the covering fraction yields an allowed misclassification rate of 1 per  $\sim 90$  cosmic rays. This level of rejection has been achieved with prototype software tested on laboratory images from a commercial-grade EMCCD.

There is also the K gain and nonlinearity errors. A K gain error causes knowledge error in the threshold, and hence looks like a threshold error. A nonlinearity error shifts the fraction of the PDF that is above the selected threshold, and hence is similar to a gain error. For this reason, we assume they have the same t/G (typically 0.1) suppression factor as threshold and gain errors. These two errors are allocated 2% in native units, and the CBE is 1.8% in native units (fractional error), based on photon transfer curve analysis (see Calibrations below). After the suppression factor, the contributions are 0.2% and 0.18%, respectively. In total the CBE for this error is 0.36% per pixel, and 0.71% total, in fractional Fp/Fs units.

The CBE for the K gain and nonlinearity calibration is 1.8% per 2 resels. This yields a margin of 10% relative to the allocation of 2%. The basis of estimate is a photon transfer curve (PTC) analysis (Janesick 2007) of non-uniformly illuminated flats collected in a lab setting. PTC analysis yields the K gain, read noise, non-linearity correction, and full well capacity (FWC). The theoretical basis of the PTC analysis is the variance equation for a CCD:

$$\text{variance (DN}^2\text{)} = \text{mean counts (DN)/K gain} + \text{read noise variance (DN}^2\text{)}$$

the first term is the shot noise and the second term is the read noise. By plotting the measured variance against the mean counts, the inverse of the slope gives the K gain and the y-intercept gives the read noise variance; the slope can be better constrained when an independent measure of the read noise is employed from the raw frame pre-scan region (which we will use). Deviations from a straight line on the PTC plot yield the non-linearity correction (also called relative gain), except near FWC; sudden jumps on the curve could also be indicative of improper clocking voltage settings, which would have to be addressed prior to flight.

We applied a PTC analysis on a large dataset collected in the lab with an EM gain setting of 1. The average K gain for counts  $< 500$  was found to be  $16.581 \pm 0.084 \text{ e}^-/\text{DN}$ . The RMS of the ratio of the measured to the smoothed relative gain is 0.75%; it is somewhat smaller for mean counts below 3000 DN. If we RSS this value with the 0.50% error for the average K gain, we obtain a total error per resel of 0.90%; for two resels it is 1.8%. These errors are in native units. To convert them to units appropriate for photon counting error, they need to be multiplied by the suppression factor noted above (0.1), yielding 0.18% for its contribution to the photon counting error.

#### 5.4. Calibrations

Calibration will involve collection of images of Neptune or Uranus over a range of exposure times between 1 second and the maximum allowed just before saturation. The maximum exposure times for Uranus and Neptune without the ND filter are about 354 s and 2280 s, respectively, for 75% full-well capacity. Since Uranus or Neptune will be used as flat field sources, these images can be collected either just before or just after observing these planets for flats while the telescope is still pointed at them. The longest exposure time also will be dictated by the changes incurred from the planet’s rotation during an exposure set. Since they both have a full rotation in  $\sim 17\text{--}19$  hours, then only  $\sim 0.3$  degrees will rotate in a minute; therefore, the planet should not significantly change during a set of exposures lasting  $\sim 1\text{--}5$  mins. Neptune subtends an angle of 2.3 arcseconds, and Uranus subtends 3.5 arcseconds. With the CGI pixel scale of 0.0218 arcseconds, these amount to 106 and 161 pixels across, respectively. The relatively small size of the planet disk at the focal plane will result in a large range in counts in each image (brightest at disk center and faintest far from the planet disk). Six images will be taken per exposure set.

#### 5.5. Processing

A ground data processing pipeline will be implemented based on the [Nemati \(2020\)](#) algorithm. This algorithm needs the EM gain as well as the threshold and the counts in true electron units. To derive these inputs, three calibrations are needed:

*EM gain calibration* – this is done by a maximum likelihood fit to the prescan data from the observation data itself. The allocation is a fractional error of 4.1% of the EM gain with a goal of 1% in obtaining the EM gain. The prescan portion contains clock-induced charge (CIC) events which undergo EM gain. An algorithm has been developed by B. Nemati and S. Miller (will be published in 2021) that can extract EM gain using a maximum likelihood fit to the distribution of counts, which include CIC, “partial CIC”, and read noise.

*K gain and linearity calibration* - the conversion gain is calibrated along with the nonlinearity using illuminated frames. Apply PTC analysis using stacking + differencing method, including bias offset corrections and read noise estimates from the prescan region. Determine the mean K gain, relative K gain and FWC from the PTC plot. Prepare a lookup table giving the K gain dependence on mean counts for the full range of mean counts for each EM gain value.

*Bias calibration* - estimated for every frame, based on the prescan data, using existing flight algorithms. This is a single scalar value (of order  $1000 e^-$ ) that applies to the full image. The error from bias calibration is expected to be small because the prescan region has of order  $1e6$  pixels available per frame.

#### 5.6. Future Work

We will explore better fitting techniques using maximum likelihood estimation for EM gain and CIC calibrations.

## 6. ASTROMETRY

### 6.1. Purpose

To provide the absolute astrometric reference frame of the detector’s unvignetted field of view (FOV), which includes the on-sky location and position angle of the center of the Roman Coronagraph detector, the average plate scale along both perpendicular axes of the detector’s FOV, and the distortion map. The field center and position angle information is used during acquisition. In observation data processing, the position angle is used to co-align images to North-up East-left orientation.

Additionally, in coronagraph mode, the position of the star (behind the coronagraph mask) is used to co-align images during data processing. The information produced as part of the normal coronagraphic acquisition and alignment process is sufficient to meet the needs of TTR5 (see section 1) observation data processing. No further calibration of the star position is needed.

### 6.2. Requirements

Astrometric requirements include computing the location of the central pixel of the detector in the ICRF frame to within 30 mas ( $3\sigma$ ) and computing the orientation of the detector’s axes with respect to galactic north to within 0.3 degrees ( $3\sigma$ ).

Current model distortion maps indicate that distortion is less than 4 mas in the central 1 arcsec  $\times$  1 arcsec (TTR5) region of the detector, and less for the central 0.5 arcsec  $\times$  0.5 arcsec region of interest. Thus, no on-sky distortion correction is strictly necessary to meet TTR5. Nevertheless, we discuss below the operations and processing required to measure that distortion on sky and correct for it.

### 6.3. Basis of Estimate

Multiple potential astrometric targets have been identified. As an example, the JWST absolute astrometric calibration plan<sup>1</sup> relies on imaging about 218,000 stars in a 5’ $\times$ 5’ field of the Large Magellanic Cloud (LMC) (Anderson, J. 2008, JWST-STScI-001378; Anderson, J. 2016, JWST-STScI-005361) which is in Roman’s Continuous Viewing Zone (CVZ). The same field of view has been observed by the Hubble Space Telescope (HST), providing star centroids with 1 mas precision. The same star positions have been cross-calibrated with Gaia DR2 astrometric data providing a calibration field with absolute sub-mas precision (Sahlmann 2017). The LMC field is particularly ideal for astrometric calibration because, besides being in the CVZ, it has a high density of well-separated stars for the 21.8 mas pixels of the Roman Coronagraph. The LMC field’s density is also uniform, so that the distortion can be equally well-measured everywhere on the detector. While its distance of about 50 kpc also minimizes the proper motion of the stars, we will use the astrometric results derived from multiple observing campaigns (HST 2008, Gaia DR2, and JWST). Dense globular clusters in the Milky Way have also been used by HST to determine the astrometric calibration of their instruments with similar precision, including peculiar motions. Ground-based high-contrast imagers can now achieve mas precision on star-to-planet relative astrometry (e.g., SPHERE (Maire et al. 2016), GPI (De Rosa et al. 2020), and HST/WFPC2 (Casetti-Dinescu et al. 2021)). In summary, the Roman Coronagraph will leverage the extensive heritage and knowledge from current missions and ground-based telescopes to attain, and surpass, the required astrometric calibration with relatively short exposure times.

### 6.4. Calibrations

During In-Orbit Checkout, and with every observing block throughout the Tech Demo phase, the Coronagraph will observe established astrometric calibration fields. This cadence may decrease if the first 2–3 calibrations show acceptable temporal stability. The Hubble Space Telescope has established several standard calibration fields, including a 5’ $\times$ 5’ region of the Large Magellanic Cloud (which is in Roman’s Continuous Viewing Zone), mapped to  $\sim$ 1 mas precision. The James Webb Space Telescope will observe the same LMC field and additional fields, which we will leverage. Additional potential calibration fields will include some dense globular clusters that have absolute astrometric precision of  $\sim$ 1 mas or better, such as 47 Tucanae, M15, NGC 3603 or NGC 6380, which have been monitored by some large ground-based telescopes to determine their on sky astrometric calibration (e.g., SPHERE (Maire et al. 2016), GPI (De Rosa et al. 2020), and HST/WFPC2 (Casetti-Dinescu et al. 2021)).

<sup>1</sup> <https://jwst-docs.stsci.edu/jwst-data-calibration-considerations/jwst-data-absolute-astrometric-calibration>

Astrometric field observations should occur close in time to the Coronagraph tech demo observation blocks. The observatory will execute a small-pitch dither pattern on the calibration fields, with the Coronagraph obtaining one or more exposures per pointing. During these observations, the Coronagraph will have no coronagraphic masks in place and the deformable mirrors will be in an optical flat configuration. Core Throughput calibration (section 8) will measure any additional astrometric distortion due coronagraphic observations. The detector will be in analog mode.

### 6.5. *Processing*

The astrometric solution will be calculated during ground processing. The algorithm will build on heritage from JWST, HST, and ground-based system astrometric calibrations. Individual stars are identified and their centroid positions are estimated (e.g., by simple “center of mass” estimation, or using the PSF model derived in other calibration products) together with their uncertainty. The centroid positions are then correlated with the actual true positions from external analysis (e.g., the HST/Gaia/JWST analysis) and the astrometric solution is obtained. The goodness-of-fit of a few distortion models will be compared (e.g., quadratic vs cubic, including different anamorphism terms, like different plate scales along both perpendicular axes of the detector’s FOV or higher order cross-terms between both axis). The astrometric solution and its uncertainty can then be used to estimate the residual RMSE, which is the value used to justify the fulfillment of the requirements.

### 6.6. *Future Work*

Future work may improve the current analysis by:

- Selecting specific calibration sub-areas within the main LMC calibration field that provide the best astrometric precision with the least integration time
- Determining an optimal sequence of dithered observations of each calibration area, taking into account re-pointing times of the telescope
- Extending the methodology to the case of polarization, where the additional prisms may introduce an additional correction.

## 7. ABSOLUTE FLUX

### 7.1. Purpose

Flux calibration will provide the information necessary to convert observed photoelectrons to apparent magnitude. When combined with the flat field, the Coronagraph observations of photometric standard stars will enable the entire unvignetted focal plane to be absolute-flux calibrated. These calibrations will also enable the correction for the total effective throughput of the entire optical beam train (the Roman observatory and the Coronagraph itself) and, if needed, its spectral response.

Both absolute flux calibrations and flatfields are necessary to fully calibrate the Coronagraph in order to achieve both its L3 requirement to convert detector digital numbers to physical flux units and TTR5 to observe the planet-to-star flux ratio of a planet (or point source) near a bright star. Absolute flux calibrations will provide localized measurements, i.e., the part of the detector covered by the standard star, of the total effective throughput of the entire system (the Roman observatory and the Coronagraph itself). The flatfields will provide relative gain offsets for the larger focal plane, thereby allowing one to extend the “localized” absolute flux calibration beyond the pixels sampled by the standard star. This step is crucial as the Coronagraph will not necessarily know the exact location of the planet relative to its host star, thereby requiring a calibration of the larger focal plane, rather than a localized region of interest.

### 7.2. Allocation

2% RSME on  $F_p/F_s$  (assuming the two resolution elements have the same uncertainty, then each has an allocation of 1.4% per resolution element).

### 7.3. Basis of Estimate

The James Webb Space Telescope’s absolute flux calibrations will achieve a 1% precision by observing multiple photometric standard stars of various spectral types<sup>2</sup> (Bohlin & Cohen 2008; Bohlin 2010; Bohlin et al. 2014). We will leverage this heritage and implement a similar observing campaign to calibrate the Coronagraph’s absolute flux to 1%. Converting this 1% absolute flux uncertainty into planet-to-star flux ratio  $F_p/F_s$  space yields an expected root square mean error of 1.41% (30% margin on achieving TTR5).

### 7.4. Calibrations

We will adopt the operations of JWST’s absolute flux calibration method and periodically observe ( $\sim 1$ – $6$  months cadence, to be refined) 4 white dwarfs, 4 A stars, and 4 G stars. Potential standard calibrator stars for the Coronagraph TTR5, which will also be used for JWST’s absolute flux calibrations, are listed at <https://jwst-docs.stsci.edu/jwst-data-calibration-considerations/jwst-data-absolute-flux-calibration>. These observations will be conducted with the Coronagraph’s Band 1 photometric filter in place and with and without the 4.75 neutral density (ND) filter in the FSAM (Fig. 1). The ND4.75 filter is necessary to prevent saturation when observing the unocculted flux of the host star.

These observations will allow us to calibrate the throughput of the entire telescope and the Coronagraph optical beamtrain, with and without the ND filter, each to an absolute precision of 1%. Standard stars will be selected based on their current observational ability as well as their brightness to maximize observing efficiency. Without using a ND 4.75 filter, the Coronagraph can observe a star as bright as  $\sim 10.9$  V-mag in Band 1 without saturating during its 1 second minimal integration time. Given this constraint, there are 6 white dwarfs (G191B2B, GD71, GD153, LDS749B, WD1057+719, and WD1657+343), 7 A stars (1757132, 1812095, 1808347, 1802271, 1805292, 1732526, and 1743045), and 5 G stars (P330E, P177D, C26202, SF1615+001A, and SNAP-2) from JWST’s calibration target list that meet this magnitude requirement. To minimize the contribution of the photon noise from the calibrator star itself, we will image each calibrator to a sufficient SNR so that photon noise is negligible.

Since the Coronagraph’s filters are all installed in the comparatively warm location in the instrument, they are unlikely to act like a “getter” and attract depositions via condensation. However since the ND filters are in focal planes, any depositions that do occur will manifest as spatial variations. To minimize their impact, we will monitor the ND filters throughout the mission by sampling them with the same set of standard stars. A  $\sim 40$  mas x 40 mas

<sup>2</sup> <https://jwst-docs.stsci.edu/jwst-data-calibration-considerations/jwst-data-absolute-flux-calibration>

“sweet spot” will be designated on the ND filter that will be characterized in detail by dithering a standard star across it; relative changes in the sweet spot will be monitored by observing a standard star at the beginning of each new observational campaign ( $\sim 1$  per month). The sweet spot position will then be used for any stellar observations that require the ND filter. Therefore, we will not need to probe the entire field of view of the ND filter, rather just its localized sweet spot. A similar process has been developed and used by Spitzer/IRAC<sup>3</sup> to map and correct for spatial variations on the focal plane.

This calibration hinges both on the repeatability of the ND (PAM) position and on the ability to offset the star with the FSM to an arbitrary location on the focal plane. The Coronagraph’s positioning accuracy (10 mas), the positioning accuracy of the PAMs (4.2 mas on-sky), and the FSM’s relative pointing accuracy ( $< 1$  mas on-sky) provide more than sufficient precision to illuminate the ND filter’s sweet spot with a reference star (the point spread function of a star illuminating the sweet spot will have a size of 1 resel = 4.4 pixels total = 2.37 pixels wide = 51.55 mas wide). To ensure that we properly illuminate the sweet spot, we will command the FSM to do an initial pointing to the sweet spot and take an exposure. We will then command the FSM to trace out a square pattern 40 mas by 40 mas wide at an interval of 5 mas (this 5 mas step size is motivated by minimizing the contribution of core throughput uncertainties). At each 5 mas step, we will take an exposure and then, during post-processing, select the image that best aligns with the sweet spot. Given that each exposure will take on the order of 7 seconds (motivated above), this entire activity will take on the order of 10 minutes total.

### 7.5. Processing

Each individual standard star observation will be fit with an appropriate stellar model, following the prescription described in detail in Bohlin & Cohen (2008), Bohlin (2010), and Bohlin et al. (2014) to determine the Roman Coronagraph’s effective throughput and spectral response for Band 1 imaging with and without the ND 4.75 filter. Given that these observations of standard stars will be limited to one, localized position on the focal plane, we will combine these localized absolute flux calibrations with the Coronagraph on-orbit flat fields to provide an absolute flux calibration of the entire focal plane.

### 7.6. Future Work

Via detailed simulations, we will also explore using other, brighter standard stars (e.g., Vega, which is in Roman’s Continuous Viewing Zone) or even fewer stars to serve as our spectrophotometric standards to reduce exposure times. In addition, these simulations will determine requirement on measuring the total effective throughput of the entire Roman Observatory and the Coronagraph (ground calibration plans for spectral measurements in bands 1 and 4 are currently in work). Lastly, we will better define the sweet spot sweeping pattern including its size to determine if a  $40 \times 40$  dither pattern with the FSM is sufficient given pointing uncertainties.

<sup>3</sup> [https://irsa.ipac.caltech.edu/data/SPITZER/docs/irac/pcrs\\_obs.shtml](https://irsa.ipac.caltech.edu/data/SPITZER/docs/irac/pcrs_obs.shtml)

## 8. CORE THROUGHPUT

### 8.1. Purpose

The core throughput is the effect of the diffractive masks: shaped pupil mask (SPM) + focal plane mask (FPM) + Lyot stop (LS). It is defined as the ratio of the flux in the core ( $>50\%$  of peak pixel) of the source offset from the FPM center to the total flux of the illuminated area of the primary mirror, ignoring losses from reflections, transmissions, and filters. It thus includes losses from the coronagraphic masks as well as the large-angle redistribution of light due to the deformable mirror patterns or pupil masks.

The PSF morphology is expected to change as a function of its location on the focal plane. Thus, the core throughput is spatially-dependent. Since the star and planet will not be at precisely the same location on the detector when their fluxes are measured, any spatially-driven core throughput variations must be removed to calculate the true planet-to-star flux ratio  $F_p/F_s$ . In addition, the core throughput is wavelength-dependent and so the effective core throughput will be different for the planet and the star; however, this source of error is small and can be accepted with negligible impact on measured  $F_p/F_s$ .

### 8.2. Allocation

1.6% RSME on  $F_p/F_s$  (assuming the two resolution elements have the same uncertainty, then each has an allocation of 1.1% per resolution element)

### 8.3. Calibrations

The core throughput calibrations will occur immediately following each coronagraphic observation campaign to preserve the dark hole. This is a conservative calibration cadence to minimize impacts from drift, and if modeling/experience eventually shows that we can get away with a less rigid schedule, we may relax this frequency. These calibrations will consist of multi-point scans via Fast Steering Mirror (FSM) offset commands of a standard star of V-magnitude  $\geq 10.9$  (this is the brightest target that CGI can image without saturating, and therefore provides the highest SNR in the shortest exposure time) across the dark hole between 6 to  $9\lambda/D$  (e.g.: offset FSM by 10 or 20 mas, take an image, offset again, take an image).

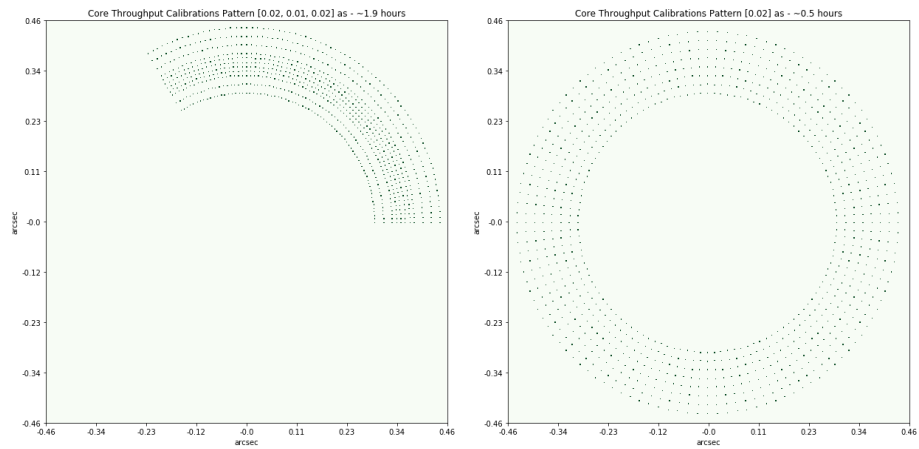
The Attitude Control System (ACS) and Reaction Wheels Assembly (RWA) jitters contribute to 15.6 mas in position uncertainty (1 sigma) on the PSF locations, despite the FSM providing small, relative offsets ( $\leq 10$  mas) at high accuracy ( $< 1$  mas) (the typical periods for ACS and RWA variations are 20 seconds and a few seconds). Thus, the PSFs will not be uniformly sampled. This effect will be mostly compensated by oversampling and interpolating the core throughput map and by taking advantage of redundancies from two different scans (Fig. 4). Two types of multi-point FSM scans will be run between 6 and  $9\lambda/D$  to properly sample the FOV: 1) a 10-mas to 20-mas sampling scan across one third of the dark hole and 2) a 20-mas sampling for  $360^\circ$ . The finely-sampled FSM scan (#1) will be done on only one third of the dark hole, exploiting the pupil symmetry, assuming that the off-axis PSFs will be the same in the two other thirds of the field of view. The coarse scan of the entire  $360^\circ$  dark hole (#2) will validate this pupil symmetry assumption by sampling the complete field of view. Assuming an exposure time per pointing of 2 seconds (including overheads) the total time needed for the full calibration is estimated to be  $< 4$  hours (with the exact time depending on the adopted pattern). This time includes the sampling of a bigger region than 6 to  $9\lambda/D$  accounting for the uncertainty on the star positioning with respect to the center of the FPM after the acquisition. We expect to coarsely sample the entire focal plane with the 20-mas sampling only once during the mission, and we would repeat the 10- to 20-mas sampling of only one third of the dark hole at the end of every observing campaign.

Core throughput maps will be constructed on ground. A  $4096 \times 4096$  floating-point pixel-based map of the spatial dependence of core throughput and a  $1024 \times 1024 \times N$  floating-point pixel-based image cube of the PSF shape will be generated (with N the total number of frames or off-axis PSFs).

### 8.4. Future Work

Future work for core throughput calibrations includes the optimization of the patterns shown in Figure 4, the simulation of calibration data and their analysis to create the final product for this calibration in the form of a  $4096 \times 4096$  floating-point pixel-based map of the spatial dependence of core throughput.





**Figure 4.** Example of patterns for HLC-Band 1 TTR5 core throughput calibrations. Several multi-point scans of a standard star will be run between  $6$  and  $9\lambda/D$  with Left a 10- to 20-mas sampling across one third of the dark hole and Right a 20-mas sampling for  $360^\circ$ . Assuming an exposure time per pointing of 2 seconds (including overheads) the time needed for the full calibration is estimated to be  $<4$  hours. This time includes the sampling of a bigger region than  $6$  to  $9\lambda/D$  accounting for the uncertainty on the star positioning with respect to the center of the FPM after the acquisition (not represented in this example, only the region from  $6$  to  $9\lambda/D$  is showed in those figures).

## 9. SPECTROSCOPY

The Band 3 spectroscopic observing mode of the Coronagraph Instrument is designed to measure the visible-wavelength spectrum of a high-contrast point source with known relative astrometric offset from a bright ( $V < 5$ ) target star (Groff et al. 2021). The spectroscopic modes use a zero optical deviation (ZOD) prism residing in the DPAM (one dedicated ZOD prism is selectable for Band 3, or the alternate Band 2 bandpass; Fig. 1) and a Field Stop Alignment Mechanism (FSAM) slit mask positioned at the expected source location. The spectroscopic target source must be inside the bowtie-shaped field of view of the SPC mask. The nominal spectral resolving power is  $R=50$  at the center wavelength of the bandpass (660 nm in Band 2 and 730 nm in Band 3). The spectral resolving power varies quadratically across the bandpass, since it is determined by the combination of the size of the main lobe of the SPC PSF, the FSAM slit mask aperture, and most significantly the wavelength-dependent dispersion characteristic of the ZOD prism.

Data acquired in the spectroscopic observing mode requires a few specialized calibrations that are not encountered for imaging data. Accurate wavelength-flux mapping of the extracted spectrum depends on a calibration of the spectral dispersion scale on the detector, and of the wavelength zero-point for the target source. An error in wavelength assignment would also translate to an error in the Fp/Fs flux ratio within a given spectral bin. A separate calibration is needed to account for the transmission of the spectroscopic target source through the FSAM slit mask; the uncertainty in this transmission factor has a separate allocation in the flux ratio error budget.

Table 2 lists the current nominal flux ratio error allocations for the Coronagraph Instrument’s spectroscopic mode. Several of the calibrations are in common with the baseline imaging mode: charge transfer efficiency, detector noise background, image corrections, absolute flux, and core throughput. However, the astrometry and flat field calibrations pertaining to imaging do not contribute to the spectroscopy error budget (viz. Table 1). Spectroscopic observations are designed so that the spectrally dispersed planet and star signals are obtained on the same detector pixels, canceling out the effect of QE variations. The flux ratio error allocations unique to spectroscopic observations are the wavelength calibration and the slit transmission. The current best estimate for each of these error sources is 1.5% in units of planet-to-star flux ratio Fp/Fs, when evaluated as the root-mean-square bias over the spectral bins of a simulated planet source.

Calibration Product	RSME Allocation on Fp/Fs	CBE	Margin
Charge Transfer (In)Efficiency	2.7%	1.1%	59%
Detector Noise Background	1.5%	1.5%	0%
Image Corrections	1.0%	0.71%	29%
Absolute Flux	2.0%	1.41%	30%
Core Throughput	1.6%	1.44%	10%
<b>Wavelength Calibration</b>	2.0%	1.5%	25%
<b>Slit Calibration</b>	2.0%	1.5%	25%
<b>Total</b>	5.0%	3.5%	29%

**Table 2.** The error suballocations for the spectroscopic mode of the Roman Coronagraph Instrument Observation Calibrations in units of root-square-mean error (RSME) allocation on measuring the planet-to-host star flux ratio Fp/Fs per spectral bin during Technology Demonstration Operations. The error sources unique to spectroscopic data — wavelength and slit calibration — are highlighted in boldface.

### 9.1. Wavelength Calibration

#### 9.1.1. Purpose

Obtain the zero optical deviation (ZOD) prism spectral dispersion scale, axis, and wavelength zero-point for a spectroscopic target source.

#### 9.1.2. Allocation

The nominal allocation is a 2 nm wavelength calibration error, which translates to 1.5% in Fp/Fs flux ratio error, when evaluated as the root-mean-square flux ratio bias over the spectral bins of a simulated planet source with this wavelength shift in Band 3.

### 9.1.3. Basis of Estimate

We analyzed the stack-up of optical and mechanical tolerances that limit the achievable wavelength calibration accuracy. The contributions to the tolerance stack-up are different for unocculted star observations (no low order wavefront sensor, “LOWFS”, loop) and occulted observations (LOWFS loop locked). During unocculted observations, the Coronagraph relies on the Attitude Control System (ACS) to keep the star at a fixed detector position. In this configuration, the ACS wander and the Coronagraph-to-WFI boresight drift are likely to be the limiting instrument stability factors.

The dispersion scale is calibrated in flight by observing a reference star through the sub-band and narrowband filters (color filters 3A, 3D, and 3E) whose center wavelengths fall inside of the full science bandpass (color filter 3F). These observations are taken with the ZOD prism in place, and without the slit in place. Apart from the boresight drift and ACS wander effects, whose impacts on the unocculted calibrations are not yet fully understood, we expect a relatively small error contribution from the uncertainty in the centroids extracted from the prism-dispersed sub-band images acquired through a narrowband filter. We can estimate the centroid errors of the calibration images using the conventional formula for the centroid uncertainty of a PSF limited by a statistical Poisson source noise:

$$\sigma_x = (\text{FWHM} / 2.35) / \text{SNR}$$

where SNR is the signal-to-noise ratio based on Poisson noise in the half-max region of the PSF. For the Band 3 shaped pupil mask PSF with FWHM = 130 mas (measured along the major axis) and SNR = 30,  $\sigma_x = 1.84$  milliarcsec. Using the detector pixel scale of 21.8 milliarcsec/pixel, we can round this up conservatively to 0.1 pixels centroid error. At 754 nm, the central wavelength of Band 3D narrowband calibration filter, this translates to 0.3 nm in wavelength offset.

The dispersion scale derived from the unocculted data must be combined with a target-specific wavelength zero-point to completely specify the wavelength calibration for a given spectroscopic target source. This zero-point is extracted from a measurement of a deformable mirror satellite spot described below. Since this calibration is acquired during an occulted star observation with an active LOWFS loop, it is not affected by the boresight drift and ACS wander effects mentioned above for the dispersion scale calibration sequence. In this case, we assume that the part of the wavelength calibration error in the zero-point estimation is dominated by the uncertainty in the centroid estimated for the deformable mirror (DM) satellite spot, combined with the knowledge error in the spectroscopic source’s position. If the satellite spot is measured with the SNR of 30, then the centroid error will be approximately 0.1 pixels, translating to 0.3 nm in wavelength calibration error. Note that the spatial frequency and orientation of the satellite spot must be tailored to the object separation and wavelength of the narrow band filter used.

Combined in quadrature, the zero-point centroid error and the narrowband dispersion scale measurement centroid errors result in 0.42 nm in wavelength error. Of the total 2.0 nm wavelength error allocation, the remaining error (up to 1.95 nm, in quadrature with this 0.42 nm) is assigned to the combined effects of jitter, boresight drift, and ACS wander on the unocculted calibration data.

### 9.1.4. Calibrations

Dispersion scale calibration data is obtained by repeated slitless observations of the prism-dispersed reference star over the set of CFAM color filters. The Band 2 calibration filter set is 2C (narrowband), 2A, 2B, 2F (broadband); the Band 3 calibration filter set is 3D (narrowband), 3A, 3E, 3F (broadband). The zero-point calibration is carried out during the first occulted reference star observation to measure a DM satellite spot through the narrowband filter and slit.

### 9.1.5. Processing

Fit a template signal to each calibrated sub-band filter image to estimate the centroid coordinates on the detector associated with the center wavelength of each filter. From the set of 3 detector pixel centroid (x, y) coordinates, do a least-squares fit to the orientation angle and cubic polynomial coefficients that best describes the spectral dispersion profile.

Co-add the satellite spot frames taken on the occulted reference star with the sinusoidal actuator applied to the first deformable mirror. Fit a response template to the satellite spot to estimate the centroid in the detector pixel coordinates. Tabulate the detector pixel centroids for each execution of the satellite spot sequence within an observation sequence.

## 9.2. Slit Calibration

### 9.2.1. Purpose

At the end of the spectroscopic data processing procedure, the planet-to-star flux ratio spectrum is obtained by dividing the signals extracted from the spectrally dispersed planet and star (unocculted). While conceptually simple, this division is complicated by the small, random offset between the planet PSF and the aperture of the FSAM (Field Stop Alignment Mechanism) slit mask, that modulates the transmission to the detector plane. The accuracy of the alignment between the PSF and slit is limited by the astrometric uncertainty and the limited precision of the FSAM mechanism. While this PSF-to-slit alignment can later be inferred during the data processing on the ground, it will be unknown during the observation campaign.

To mitigate this, a slit calibration procedure will obtain images of the unocculted, prism-dispersed reference and target stars observed through a neutral density filter, nominally ND2.25 in the FPAM ((Figure 1). These exposures will be repeated over a grid of offsets applied to the Fast Steering Mirror (FSM). After the spectroscopic campaign completes, ground data processing software will identify the star spectrum image acquired with the closest PSF-to-slit alignment to the one inferred for the dispersed target source data.

### 9.2.2. Allocation

2.0% RMSE Fp/Fs flux ratio error in relative calibration (assuming the two resolution elements have the same uncertainty, then each has an allocation of 1.4% per resolution element).

### 9.2.3. Basis of Estimate

Simulation of impact on PSF-slit misalignment on flux ratio bias indicates the current best estimate is 1.5%, assuming a relative alignment error of 10 mas (approximately 0.5 detector pixels) along the dispersion axis between the co-added star and planet spectrum arrays.

### 9.2.4. Calibrations

Slit mask transmission calibration data are taken on the reference, target, and spectrophotometric standard stars.

Reference star: Obtain broadband slitless spectra of the reference star as well as broadband slit spectra at a variety of PSF-to-slit alignments using FSM dithers. The reference star is placed at the same location relative to the nominal FPM center location as target of interest (e.g. planet) will be.

Target star: Obtain broadband slitless spectra of the target star as well as broadband slit spectra at a variety of PSF-to-slit alignments using FSM dithers. The target star is placed at the same location relative to the nominal FPM center location as target of interest (e.g. planet) will be.

Standard star: A standard star with a known visible-wavelength spectrum is placed at the same location relative to the nominal FPM center location as target of interest (e.g. planet) was. The line spread function is measured in the narrowband color filter (filter 3D) with the SPC focal plane mask in place, and no ND filter. The standard star spectrum measured through the broadband filter (filter 3F) is obtained to characterize the wavelength-dependent slit throughput.

Note that spectroscopy calibrations using bright stars (typically target and reference stars) require a neutral density (ND) filter to record an unsaturated PSF in the minimum integration time. The spectroscopy mode uses the FPAM ND filter, since the FSAM plane is configured for the slit mask during spectroscopic observations. Therefore a dedicated calibration procedure is needed for the FPAM ND2.25 transmission calibration, analogous to the Absolute Flux calibration described in Section 7. Similar to the baseline ND filter transmission calibration, the FSM is commanded to move the unocculted star over a rectangular grid of offsets surrounding the ND filter “sweet spot.” These observations are taken with the prism in the beam, so that the wavelength-dependent ND transmission can be measured.

Note the application of the FPAM ND filter excludes simultaneous use of the bowtie FPM (Fig. 1). The relative change in PSF transmission is accounted for via PSF core throughput calibration data, similar to that described in Section 8. In the case of spectroscopic data, however, the PSF throughput characterization may be restricted to a narrow region of the field of view around the target source location.

### 9.2.5. Processing

Based on comparisons to a post-processed image of the spectroscopic target source, select the image that matches the PSF-slit-detector alignment of the target.

The line spread function can also be measured at one wavelength from the response cross-section of similar exposures acquired through the narrowband filter. Combining this single wavelength LSF with PSF model from the instrument

diffraction model and the wavelength calibration product, and knowledge of the standard star's spectrum, to estimate the scaling of the LSF with wavelength.

### 9.3. *Future Work*

Additional analysis is needed to understand the impacts of jitter, boresight drift, and ACS wander effects on the unocculted star observations used for wavelength calibration. As an alternative, binary stars might also be used to calibrate the dispersion scale and eliminate those effects. Further research is needed to establish the availability of suitable binary targets with appropriate brightness ratios and angular separations. The selection of reference stars appropriate for pairing with individual spectroscopy targets also requires further analysis.

## 10. POLARIMETRY

The Roman Coronagraph should have the ability to measure the polarization fraction of faint extended circumstellar structures in both Band 1 and Band 4, with measurement uncertainties lower than three percent per spatial resolution element (Groff et al. 2021). In particular, the combination of total intensity and polarized images of highly inclined debris disks and rings provides access to the grains scattering phase function, which can inform grain size and shape - possibly even composition when measured at different wavelengths- , and also breaks some degeneracies present in total intensity images alone (e.g. between dust density and scattering efficiency spatial variations. The source linear polarization fraction is estimated through single linear polarization images recorded with four different linear polarization states (0, 45, 90 and 135 degrees), and are obtained two at a time, using one Wollaston prism, then the other.

10.1. *Optical System Mueller Matrix*10.1.1. *Purpose*

The purpose of polarimetric calibration is to determine the instrumental polarization effects which are entirely represented by the optical system end-to-end Mueller Matrix at a given wavelength. The Mueller Matrix (see monochromatic models available at <https://roman.ipac.caltech.edu/sims/Simulations.csv.html>) describes how the overall optical system turns unpolarized light into polarized light, and modifies the source linear polarization fraction and its orientation. Measuring the end-to-end system Mueller Matrix on the sky is hence crucial in order to take out instrumental polarization effects and retrieve the true source polarization properties.

10.1.2. *Allocation*

The only requirement is on the accuracy of the linear polarization fraction estimated on a target of interest, which is required to be better than 3% RMSE per spatial resolution element, for observations in both Band 1 and Band 4. There is no formal allocation for the Mueller Matrix estimation uncertainty, other than it should be precise enough to meet that top level requirement on the final linear polarization fraction estimate.

10.1.3. *Basis of Estimate*

The linear polarization fraction (LPF) estimation root-mean-square error per resel was estimated through Monte Carlo simulations and the current error budget allocation is detailed in Table 3.

Error Term	Per	Requirement	LPF rms	CBE	LPF rms
Calibrators LPF uncertainty		0.10%	0.36%	0.10%	0.36%
Calibrators LPF orientation uncertainty		1 deg	0.36%	1 deg	0.36%
Flat fielding error	Resel	2.50%	1.42%	0.50%	0.35%
CIT error	Resel	1.70%	1.21%	1.0%	0.71%
Photometric noise on target	Resel	1.00%	0.51%	1.00%	0.51%
Photometric noise on polarized standards	Resel	0.20%	1.19%	0.10%	0.58%
Photometric noise on unpolarized standard	Resel	0.20%	1.46%	0.10%	0.70%
Total LPF estimation rms error	Resel		3.00%		1.66%

**Table 3.** Linear polarization fraction (LPF) error budget (per resel) and current best estimate (CBE) of performance. Requirements and CBE are expressed in physical units. Estimated LPF rms errors are listed in columns 4 and 6 and computed for each individual error term, setting all other terms to zero, assuming that term is either at its required level (3rd column) or at its CBE level (5th column). The total LPF estimation error indicated in the last row comes from simulations including all error terms. Assuming all error terms at CBE level (including a photometric SNR of 1000:1 per resel on each of the polarized standards), observations of 3 polarization standard stars at 2 different telescope rolls, the LPF per resel will be estimated with an rms error of 1.66%.

All error terms in the above table are included in the Mueller matrix uncertainty estimate, except for the photometric noise on target.

Note: the impact of flat fielding error on the Mueller matrix estimation assumes that at a given linear polarization, a subset of the 3 polarization standards images overlap on the Coronagraph detector. Having such an overlap strongly reduces the effect of differential polarimetric flatfielding errors on the computation of the Mueller matrix, and will be guaranteed by taking -unocculted- images of each polarization standard at 5 different nominal locations.

## 10.2. Calibrations

### 10.2.1. Pre-processing

The data pre-processing will be similar to the unpolarized data, except data recorded at each linear polarization angle will be pre-processed separately. Regular flat fielding, dark subtraction, bad pixel correction, and frame centering, using the allocations provided in Table 1, will be applied to the data. The data from each linear polarization angle and pointing will be coadded.

#### 10.2.2. Polarization Effects Calibration (estimating the Mueller matrix from the observations of polarization standards)

Circumstellar disk observations will be performed at four linear polarization angles for both the target star and polarization standard stars. Also, for optimal measurement accuracy, the polarized standards should have well-known linear polarization fraction and orientations, and have linear polarizations oriented  $45^\circ$  (modulo  $90^\circ$ ) from each other.

Data are taken with a set of two Wollaston prisms, one being used at a time to provide simultaneous images ( $7.5''$  separated) at two orthogonal polarizations:  $0^\circ$  and  $90^\circ$ , or  $45^\circ$  and  $135^\circ$ . In this section we assume (and will assure via target selection) the target disk will be much brighter than the speckle noise, and thus we do not anticipate needing, and thus neglect, PSF subtraction on the calibrations outlined here. Further PSF subtraction considerations are discussed separately in Section 10.2.3 This assumption is folded in the signal-to-noise required per spatial resolution element for the polarimetric target of interest (Table 3), which includes any residual starlight background noise in addition to shot noise.

The polarization effects due to the Wollaston prisms and due to the rest of the system affects the observed Stokes parameters in the following way:

$$S_{obs} = MS_{true} \quad (1)$$

Where  $S$  is the vector of Stokes parameters,  $M$  is the Mueller matrix representing the total cumulative polarization effects through the system upstream of the Wollaston prism. The Stokes parameters measured from our data are denoted with the subscript  $_{obs}$ , while the true on-sky Stokes parameters are denoted with the subscript  $_{true}$ .

We make some reasonable assumptions in order to simplify the Mueller matrix. We assume that all objects have negligible circular polarization  $V_{true} \cong 0$  (as expected for debris disks and dust rings) and that the Coronagraph measures only the linear polarization fraction ( $\frac{\sqrt{Q^2+U^2}}{I}$ ):

$$\begin{bmatrix} I_{obs} \\ Q_{obs} \\ U_{obs} \end{bmatrix} = \begin{bmatrix} m_{00} & m_{10} & m_{20} \\ m_{01} & m_{11} & m_{21} \\ m_{02} & m_{12} & m_{22} \end{bmatrix} \begin{bmatrix} I_{true} \\ Q_{true} \\ U_{true} \end{bmatrix} \quad (2)$$

Thus, the true linear polarization fraction of the source is a function of nine Mueller matrix coefficients.<sup>4</sup>

Since the telescope will not be available for measurements in the lab prior to launch, the end-to-end polarization effects need to be calibrated through on-sky observations. We assume that the end-to-end polarization effects are measured through observations of at least three polarization calibrators (likely one unpolarized star and two polarized stars). The unpolarized star is assumed to have no polarization, so we can set two Stokes parameters to zero:  $Q_{true} = U_{true} = 0$ . Solving for the Stokes parameters for the unpolarized star (denoted with the subscript  $_1$ ) we find:

$$I_{1,obs} = m_{00}I_{1,true} \quad (3)$$

$$Q_{1,obs} = m_{01}I_{1,true} \quad (4)$$

<sup>4</sup> Models predict that the overall telescope and Coronagraph instrument polarization, polarization throughput, and cross-talk terms are constant over time but not negligible (of order up to 10% relative (REF results from Jim Maguire, Dec 2018), wavelength dependent) with respect to the precision required (3% absolute).

$$U_{1,obs} = m_{02}I_{1,true} \quad (5)$$

Thus, three Mueller matrix coefficients can be measured using the unpolarized star in the following way:

$$m_{00} = \frac{I_{1,obs}}{I_{1,true}} \quad (6)$$

$$m_{01} = \frac{Q_{1,obs}}{I_{1,true}} \quad (7)$$

$$m_{02} = \frac{U_{1,obs}}{I_{1,true}} \quad (8)$$

In order to measure the other Mueller matrix coefficients, we need to observe at least two polarized standard stars. With one polarized standard star (denoted as  $_2$  for the second calibrator) we have:

$$I_{2,obs} = m_{00}I_{2,true} + m_{10}Q_{2,true} + m_{20}U_{2,true} \quad (9)$$

$$Q_{2,obs} = m_{01}I_{2,true} + m_{11}Q_{2,true} + m_{21}U_{2,true} \quad (10)$$

$$U_{2,obs} = m_{02}I_{2,true} + m_{12}Q_{2,true} + m_{22}U_{2,true} \quad (11)$$

For the second polarized standard star (the third calibrator) we have:

$$I_{3,obs} = m_{00}I_{3,true} + m_{10}Q_{3,true} + m_{20}U_{3,true} \quad (12)$$

$$Q_{3,obs} = m_{01}I_{3,true} + m_{11}Q_{3,true} + m_{21}U_{3,true} \quad (13)$$

$$U_{3,obs} = m_{02}I_{3,true} + m_{12}Q_{3,true} + m_{22}U_{3,true} \quad (14)$$

Combining the observed  $I_{2,obs}$  and  $I_{3,obs}$  terms we solve  $m_{10}$  and  $m_{20}$ :

$$m_{10} = \frac{U_{3,true}[I_{2,obs} - m_{00}I_{2,true}] - U_{2,true}[I_{3,obs} - m_{00}I_{3,true}]}{U_{3,true}Q_{2,true} - U_{2,true}Q_{3,true}} \quad (15)$$

$$m_{20} = \frac{Q_{3,true}[I_{2,obs} - m_{00}I_{2,true}] - Q_{2,true}[I_{3,obs} - m_{00}I_{3,true}]}{Q_{3,true}U_{2,true} - Q_{2,true}U_{3,true}} \quad (16)$$

Combining the  $Q_{2,obs}$  and  $Q_{3,obs}$  terms we solve  $m_{11}$  and  $m_{21}$ :

$$m_{11} = \frac{U_{3,true}[Q_{2,obs} - m_{01}I_{2,true}] - U_{2,true}[Q_{3,obs} - m_{01}I_{3,true}]}{U_{3,true}Q_{2,true} - U_{2,true}Q_{3,true}} \quad (17)$$

$$m_{21} = \frac{Q_{3,true}[Q_{2,obs} - m_{01}I_{2,true}] - Q_{2,true}[Q_{3,obs} - m_{01}I_{3,true}]}{Q_{3,true}U_{2,true} - Q_{2,true}U_{3,true}} \quad (18)$$

And finally, combining the  $U_{2,obs}$  and  $U_{3,obs}$  terms we solve  $m_{12}$  and  $m_{22}$ :

$$m_{12} = \frac{U_{3,true}[U_{2,obs} - m_{02}I_{2,true}] - U_{2,true}[U_{3,obs} - m_{02}I_{3,true}]}{U_{3,true}Q_{2,true} - U_{2,true}Q_{3,true}} \quad (19)$$

$$m_{22} = \frac{Q_{3,true}[U_{2,obs} - m_{02}I_{2,true}] - Q_{2,true}[U_{3,obs} - m_{02}I_{3,true}]}{Q_{3,true}U_{2,true} - Q_{2,true}U_{3,true}} \quad (20)$$

Now that we have measured the nine unknowns in the Mueller matrix, we can invert the Mueller matrix to solve for the Stokes parameters:



$$S_{true} = M^{-1} S_{obs} \quad (21)$$

This procedure is done per spatial resolution element (i.e., over regions of  $2 \times 2$  pixels in Band 1, and  $3 \times 3$  pixels in Band 4) on each of the images, in order to take into account any change in polarization spatially.

Finally, the polarization fraction ( $p$ ) and angle ( $\theta$ ) of linear polarization for the target is measured:

$$p = \frac{\sqrt{Q_{true}^2 + U_{true}^2}}{I_{true}} \quad (22)$$

$$\theta = 0.5 \arctan(U_{true}, Q_{true}) \quad (23)$$

### 10.2.3. Further PSF subtraction

In the case where the extended source target of interest has a brightness comparable to the raw speckles level, polarimetric observations of a bright reference star (e.g., the dark hole digging star or the unpolarized standard) will be needed for PSF subtraction. This step occurs after the effects of instrumental polarization have been corrected using the Mueller matrix estimate provided by polarization standards observations, i.e., after an estimate of the target's  $Q_{true}$  and  $U_{true}$  images has been formed. The PSF subtraction is then applied to the target Q and U data separately, using the target and reference star Q and U images, following [van Holstein et al. \(2017\)](#). Post-processing algorithms such as principal component analysis (PCA) or KLIP will be applied to the data.

### 10.3. Future Work

- Determine a final set of suitable polarized and unpolarized standard stars.
- Determine list of polarized targets of interest. The current polarimetric simulations are conducted per spatial resolution element but do not include a full 2D simulation of an extended polarized source of interest, e.g. like the HR 4796A ring, for which visible (600-900nm) polarimetric observations have been obtained with the SPHERE/ZIMPOL instrument on the Very Large Telescope (Milli et al. 2019). Future work will concentrate on the identification of the best possible polarimetric target(s) of interests -which may not be HR 4796A - , full 2D simulations of the LPF map that could be retrieved from CGI observations of such a target in CGI band 1 and band 4, folding in all limitations set by the dark hole size and source geometry.
- In the case where the extended polarized target of interest has a brightness comparable to (or even lower than) the raw speckles level, additional polarimetric coronagraphic (occulted) observations of a bright reference star (e.g., the dark hole digging star) will be needed for PSF subtraction. This PSF subtraction step occurs after the effects of instrumental polarization have been corrected from the target and bright reference star data using the Mueller matrix estimate provided by polarization standards observations, i.e., after an estimate of the target's  $Q_{true}$  and  $U_{true}$  images has been formed. The PSF subtraction is applied to the target Q and U data separately, using the target and bright reference star Q and U images, following [van Holstein et al. \(2017\)](#). Post-processing algorithms such as principal component analysis (PCA) such as KLIP ([Soummer et al. 2012](#)) or variants to be used for extended sources will be applied to the data. Such simulations of PSF subtraction in polarimetric mode have not yet been conducted.

## 11. CONCLUSIONS

Here we presented the calibrations needed for the Nancy Grace Roman Space Telescope Coronagraph Instrument to achieve its Technology Demonstration Threshold Requirement (TTR5; Band 1 photometry to achieve a contrast ratio of  $\geq 1 \times 10^{-7}$  between 6 and 9  $\lambda/D$  for a  $V_{AB}$  magnitude  $\leq 5$  host star) as well as polarimetric and spectroscopic operations. This document is meant to provide a “snapshot” of the current status of the development of each of these calibrations products and their allocations, and will be continued to be updated as work progresses.

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