

Geoengineering: Whiter Skies?

(Supplemental Online Material)

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1 Model

To perform our simulations, we used the libRadtran software package, version 1.6 β (1, 2, 3). We used two components from this model package: `mie` and `uvspec`. The `mie` component calculates scattering properties of aerosols, which are then provided as input for `uvspec`, which is the core radiative transfer tool.

For the aerosol scattering properties, we use the Mie code `MIEV0` (4). We specify that 200 moments of the scattering phase function be calculated, which, for the experiments we

8 have performed, is more than sufficient for convergence of the summed terms of the phase
 9 function. Scattering is calculated in the entire visible spectrum, from 380 to 780 nm, with
 10 a wavelength step of 1 nm. Since we are simulating sulfate aerosols, we have specified the
 11 complex refractive index for the aerosols to be $1.43 + 0i$. For an aerosol composition of 75%
 12 H_2SO_4 and 25% water, which is typical for sulfate aerosols (5), this refractive index is valid
 13 for the range of wavelengths we investigate (6, 7). Linearly interpolating from the values
 14 given in (6), the range of refractive indices over this set of wavelengths varies from $1.428 + 0i$
 15 to $1.446 + 0i$, which is a small enough variation from the assumed value of $1.43 + 0i$ that our
 16 results are not affected. The Mie code outputs aerosol extinction, single scattering albedo,
 17 and the moments of the scattering phase function for each wavelength, based on the assumed
 18 size distribution (discussed in the following sections), which are then provided as input to
 19 the radiative transfer code `uvspec`.

20 `uvspec` is designed to calculate spectral irradiance in ultraviolet and visible wavelengths
 21 (3, 8). Our specifications are for a standard atmospheric temperature and gas profile in the
 22 summer over the continental United States. We use the DISORT algorithm (9) to calculate
 23 irradiance over the visible spectrum 380-780 nm at 1 nm intervals. All radiative transfer
 24 simulations were calculated at a reference height of 0.0 km and with a solar zenith angle of
 25 0° , except where indicated (Section 3 and Figure 1).

26 **2 Geoengineering**

27 For our geoengineering simulations, we began with Mie code simulations of unimodal lognor-
 28 mal distributions of sulfate aerosols with median radii of $r_g = \{0.1, 0.2, 0.3, 0.4, 0.5, 0.6, 0.7, 0.8, 0.9\}$
 29 μm and standard deviations of $\sigma = \{0.1, 0.25, 0.5, 1.0\}$, for a total of 36 simulations. The
 30 output from the Mie code simulations was provided as input to `uvspec` with a prescribed

31 aerosol optical depth (mid-visible, $\lambda = 550$ nm) of 0.1. We then integrated spectral irra-
32 diance over the visible spectrum and calculated the appropriate mid-visible optical depth
33 required to scale that integrated value to achieve a reduction by 0.5, 1.0, 1.5, and 2.0%.
34 Optical depths at all other wavelengths are scaled appropriately according to the extinction
35 efficiencies calculated by the Mie code. These mid-visible optical depths can be found in
36 Supplementary Table 2. The radiative transfer simulations were then redone with these
37 updated optical depth values for a total of 144 simulations.

38 Although all of our calculations are specified in terms of a percent decrease in solar ir-
39 radiance, this is calculated by integrating spectral irradiance only over the visible spectrum
40 ($\lambda = 380 - 780$ nm) instead of the total solar band. The visible band accounts for approx-
41 imately 52% of the energy in the solar spectrum, with approximately 3% occurring in the
42 ultraviolet (UV) portion and 45% in the near infrared (NIR) portion of the spectrum (10).
43 Moreover, sulfate aerosol extinction in the NIR band is approximately one order of magni-
44 tude less than in the visible and UV bands (11). Naively calculating integrated irradiance
45 values using these values, a 2% reduction in visible integrated spectral irradiance is the same
46 as a 1.19% reduction in total integrated spectral irradiance, which seemingly implies our
47 geoengineering simulations understate changes in sky color. However, these values are based
48 on the assumption that the shape of the spectral irradiance curve does not change in the
49 NIR, which, based on extrapolations of Figure 2, is not likely to be true in general.

50 We cannot resolve this uncertainty in spectral irradiance changes in the NIR. Narrow
51 absorption lines in the NIR necessitate the use of a correlated- k distribution in conducting
52 radiative transfer simulations, which does not allow for the fine spectral resolution we have
53 obtained in our simulations of visible spectral irradiance. Therefore, we have decided not
54 to pursue this route and to frame our geoengineering simulations in terms of reductions in

55 solar irradiance integrated over the visible band.

56 **3 Mount Pinatubo simulation**

57 One additional simulation we conducted was for the 1991 eruption of Mount Pinatubo as
58 a comparison to our geoengineering and pollution (Section S5 below) simulations. The
59 simulation with `mie` involved a lognormal distribution with specified effective radius of $r_{\text{eff}} =$
60 $0.5248 \mu\text{m}$ and $\sigma_g = 1.4$, which corresponds to approximate values in March 1992, 9 months
61 after the eruption (*12, 13, 14*). As in the geoengineering simulations, we used a complex
62 refractive index of $1.43 + 0i$. Our simulation with `uvspec` used a mid-visible aerosol optical
63 depth of $\tau_{550} = 0.12$, which was the value measured at the Mauna Loa Observatory (19.5°N ,
64 155.6°W) in March 1992 (*12*). At this time, the eruption showed approximately a 20%
65 decrease in direct radiation, which was compensated by a 240% increase in diffuse radiation
66 at solar zenith angle 60° (*13*). Results of our simulations of these conditions are within 4%
67 of these values.

68 **4 Thin Cirrus**

69 To account for the potential effects of optically thin cirrus clouds on our results, we performed
70 simulations including cirrus clouds. We chose typical values of cirrus clouds: cloud fraction
71 20%, cloud droplet effective radius $20 \mu\text{m}$, and ice water content of 0.005 g m^{-3} (*15*). We
72 inserted these clouds into a layer at 10 km in altitude, below the layer of stratospheric
73 aerosols. Irradiance results for these simulations, assuming a geoengineering aerosol size
74 distribution with $r_g=0.5 \mu\text{m}$ and $\sigma = 0.1$, are in Supplementary Figure 1. Increases in sky
75 brightness as a function of the size distribution are in Supplementary Table 3.

76 5 Pollution

77 For our comparisons in Figure 4, we obtained aerosol optical depth and size distribution
78 data for several urban centers (16) and averaged the values, weighted by the number of
79 observations at each site. All of these parameters had a range, corresponding to days with
80 low, high, and average aerosol conditions, which depended upon meteorology. Additionally,
81 each site had a range of Angstrom exponents, which we incorporated into the simulations.
82 All values we used for our simulations can be found in Supplementary Table 1.

83 To perform our simulations, we generated bimodal distributions which we inserted into
84 `mie`, one for each combination of low, high, and average aerosol. We then provided this as
85 input for `uvspec`, each of which had three choices of Angstrom exponent (low end of the
86 range, high end of the range, and the average value in the range), for a total of 9 simulations.
87 These results are shown in Figure 4, in which the average condition is shown as a solid colored
88 line, and the range spanned by choosing different Angstrom exponents is shown as colored
89 shading. For the `uvspec` simulations, we assumed the background aerosol profile to be urban
90 spring/summer, with background stratospheric aerosols, i.e., no recent volcanic eruptions (17
91 for further description).

92 6 Metameric Matches

93 To determine metameric matches for the spectra we generated, we follow a matching proce-
94 dure (18). Eye cones can be divided into three categories, corresponding to the wavelengths
95 to which they are sensitive: short (S), middle (M), and long (L). Supplementary Figure 2
96 shows each of the cone sensitivities as a function of wavelength, calculated for an average
97 observer (19). Using these in combination with our radiative transfer simulations, we can

98 determine the unsaturated monochromatic stimulus response (λ_u) that is a metamer match
 99 for the simulated sky color by solving the equivalence

$$\begin{aligned} & \frac{M(\lambda_u) \int L(\lambda) I(\lambda) d\lambda - L(\lambda_u) \int M(\lambda) I(\lambda) d\lambda}{\int L(\lambda) d\lambda \int M(\lambda) I(\lambda) d\lambda - \int M(\lambda) d\lambda \int L(\lambda) I(\lambda) d\lambda} \\ &= \frac{M(\lambda_u) \int S(\lambda) I(\lambda) d\lambda - S(\lambda_u) \int M(\lambda) I(\lambda) d\lambda}{\int S(\lambda) d\lambda \int M(\lambda) I(\lambda) d\lambda - \int M(\lambda) d\lambda \int S(\lambda) I(\lambda) d\lambda} \end{aligned} \quad (1)$$

100 where S, M, and L are the cone spectral sensitivities for the three cone types as a function
 101 of wavelength (Supplementary Figure 2), and $I(\lambda)$ is the diffuse spectral irradiance from the
 102 radiative transfer simulations. Values of λ_u lie at intersections of the curves corresponding
 103 to the left and right sides of the equation. Corresponding function values (either side of the
 104 above equation) evaluated at λ_u are the ratios I_w/I_u , which is the relative amounts of white
 105 (numerator) and monochromatic light (denominator) of the metamer match, where white
 106 light is defined as having equal intensity at all wavelengths. The results of these matches
 107 can be found in Figure 3.

108 7 Attempted Visualizations: Color Swatches

109 As discussed in Section 4, color is not an intrinsic property of light, making visualization of
 110 sky color rather difficult. Color perception depends upon biology, including expectations of
 111 color, but also upon the color matching function chosen to map the spectrum into RGB space,
 112 as well as the assumed white point. To illustrate the dependence of color swatches upon the
 113 color matching function and white point, Supplementary Figures 3-6 show combinations of
 114 two different choices of each, all of which are reasonable and defensible choices (20,21,22).
 115 Additionally, the RGB color space is device-dependent, in that different colors can be realized

116 on different monitors, printers, or any other means of viewing. Therefore, we have no reliable
117 way of ensuring the swatches as viewed on our computer monitors/printers will match those
118 of any reader of this paper. We are satisfied that the only way to represent absolute color is
119 to provide the full visible irradiance spectrum.

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Table 1: Specifications for urban aerosols used in Sections 5 and S5. All values are averages (16), weighted by the number of observations at each site. Since values were given as ranges, we have created multiple profiles, based on low, average, and high aerosol amounts. The urban/mixed aerosol profiles we obtained had average refractive indices of $1.43 + 0.01i$, but in our simulations of urban environments, we set these values to $1.43 + 0i$ and 1.00 , which are typical for pure sulfate aerosols (6,7). The impacts of this assumption on simulated irradiance spectra are quite small, and it has the benefit of making the urban aerosol profiles directly comparable to our geoengineering simulations. All size distributions are assumed to be bimodal lognormal. Concentrations are relative between the two modes (only the shapes of the distribution curves are important, not the values), so units are not given.

Parameter	Description	Low	Average	High
τ_{440}	Aerosol optical depth (440 nm)	0.1	0.3	1.2
α	Angstrom exponent	1.0-2.4	1.0-2.4	1.0-2.4
$n + ik$	Complex refractive index	$1.43 + 0i$	$1.43 + 0i$	$1.43 + 0i$
$\omega_{0,440}$	Single scattering albedo (440 nm)	1.0	1.0	1.0
r_{g1}	Median radius, fine mode (μm)	0.13	0.17	0.21
σ_1	Standard deviation, fine mode	0.41	0.41	0.41
C_1	Aerosol concentration, fine mode	0.014	0.0865	0.159
r_{g2}	Median radius, coarse mode (μm)	2.91	3.215	3.52
σ_2	Standard deviation, coarse mode	0.72	0.72	0.72
C_2	Aerosol concentration, coarse mode	0.013	0.058	0.103

Table 2: Values of aerosol optical depth at 550 nm used in the radiative transfer calculations to achieve the given percent reduction in integrated visible band irradiance reaching the surface (ΔI). The procedure for obtaining these is given in Section S2. r_g is the geometric mean radius, or the median radius, of the assumed unimodal lognormal distribution.

r_g (μm)	ΔI (%)	$\sigma = 0.1$	$\sigma = 0.25$	$\sigma = 0.5$	$\sigma = 1.0$
0.1	0.5	0.0696	0.0631	0.0687	0.0775
	1.0	0.1396	0.1265	0.1377	0.1554
	1.5	0.2099	0.1902	0.2071	0.2336
	2.0	0.2806	0.2543	0.2768	0.3123
0.2	0.5	0.0793	0.0624	0.0670	0.0778
	1.0	0.1591	0.1251	0.1343	0.1560
	1.5	0.2392	0.1881	0.2020	0.2346
	2.0	0.3198	0.2514	0.2700	0.3136
0.3	0.5	0.0817	0.0610	0.0653	0.0774
	1.0	0.1637	0.1224	0.1310	0.1553
	1.5	0.2462	0.1841	0.1970	0.2335
	2.0	0.3291	0.2460	0.2633	0.3122
0.4	0.5	0.0743	0.0585	0.0638	0.0770
	1.0	0.1490	0.1172	0.1280	0.1544
	1.5	0.2240	0.1763	0.1924	0.2322
	2.0	0.2995	0.2357	0.2572	0.3104
0.5	0.5	0.0612	0.0550	0.0626	0.0766
	1.0	0.1228	0.1103	0.1254	0.1536
	1.5	0.1846	0.1659	0.1886	0.2309
	2.0	0.2468	0.2218	0.2521	0.3087
0.6	0.5	0.0475	0.0517	0.0616	0.0763
	1.0	0.0953	0.1037	0.1236	0.1530
	1.5	0.1433	0.1560	0.1858	0.2300
	2.0	0.1916	0.2085	0.2484	0.3075
0.7	0.5	0.0388	0.0498	0.0612	0.0761
	1.0	0.0777	0.0998	0.1226	0.1527
	1.5	0.1169	0.1501	0.1844	0.2296
	2.0	0.1562	0.2006	0.2465	0.3069
0.8	0.5	0.0384	0.0499	0.0613	0.0762
	1.0	0.0769	0.1000	0.1228	0.1527
	1.5	0.1157	0.1504	0.1847	0.2296
	2.0	0.1546	0.2011	0.2469	0.3070
0.9	0.5	0.0457	0.0521	0.0619	0.0764
	1.0	0.0916	0.1045	0.1242	0.1531
	1.5	0.1377	0.1572	0.1868	0.2302
	2.0	0.1841	0.2101	0.2496	0.3078

Table 3: Increases in visible band integrated diffuse irradiance as a measure of diffuse sky brightness with inclusion of the effects of cirrus clouds (description in Section S4). Leftmost column indicates the percent decrease in total integrated visible band irradiance. All values given are ratios of integrated visible band irradiance (geoengineering divided by clear sky) and are rounded to two decimal places. In the clear sky simulations, diffuse irradiance comprises approximately 6% of total irradiance.

ΔI (%)	σ	r_g (μm)									
		0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9	
0.5	0.1	1.44	1.50	1.51	1.47	1.40	1.33	1.30	1.28	1.29	
	0.25	1.43	1.41	1.40	1.39	1.37	1.35	1.33	1.33	1.34	
	0.5	1.46	1.44	1.43	1.42	1.42	1.41	1.41	1.41	1.41	
	1.0	1.52	1.52	1.52	1.51	1.51	1.51	1.51	1.51	1.51	
1.0	0.1	1.86	1.96	1.98	1.91	1.78	1.65	1.57	1.54	1.57	
	0.25	1.80	1.79	1.77	1.75	1.71	1.67	1.64	1.64	1.66	
	0.5	1.88	1.86	1.84	1.82	1.80	1.79	1.79	1.79	1.80	
	1.0	1.99	2.00	1.99	1.99	1.98	1.98	1.98	1.98	1.98	
1.5	0.1	2.24	2.39	2.42	2.31	2.13	1.95	1.83	1.80	1.83	
	0.25	2.16	2.14	2.12	2.08	2.03	1.98	1.94	1.94	1.96	
	0.5	2.27	2.23	2.21	2.19	2.16	2.15	2.14	2.14	2.15	
	1.0	2.43	2.44	2.43	2.42	2.42	2.41	2.41	2.41	2.41	
2.0	0.1	2.59	2.77	2.82	2.68	2.45	2.23	2.08	2.04	2.08	
	0.25	2.50	2.48	2.45	2.40	2.34	2.27	2.23	2.22	2.25	
	0.5	2.63	2.60	2.56	2.53	2.50	2.48	2.47	2.48	2.49	
	1.0	2.83	2.84	2.83	2.82	2.82	2.81	2.81	2.81	2.81	

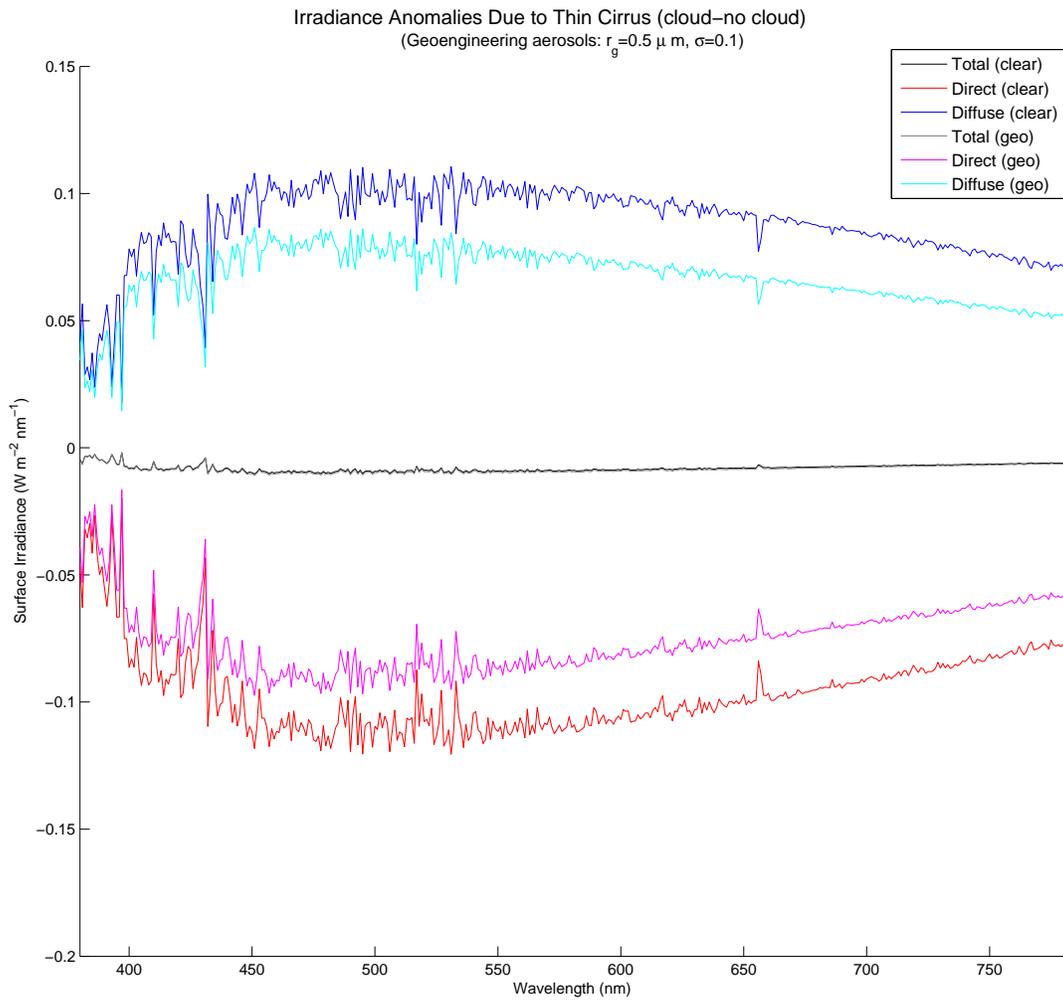


Figure 1: Geoengineering ($r_g=0.5 \mu\text{m}$, $\sigma = 0.1$) and clear sky differences when optically thin cirrus clouds are included in the simulations. All values plotted are for simulations with clouds included minus simulations with no clouds. Specifications for cirrus clouds are in Supplementary Section 4.

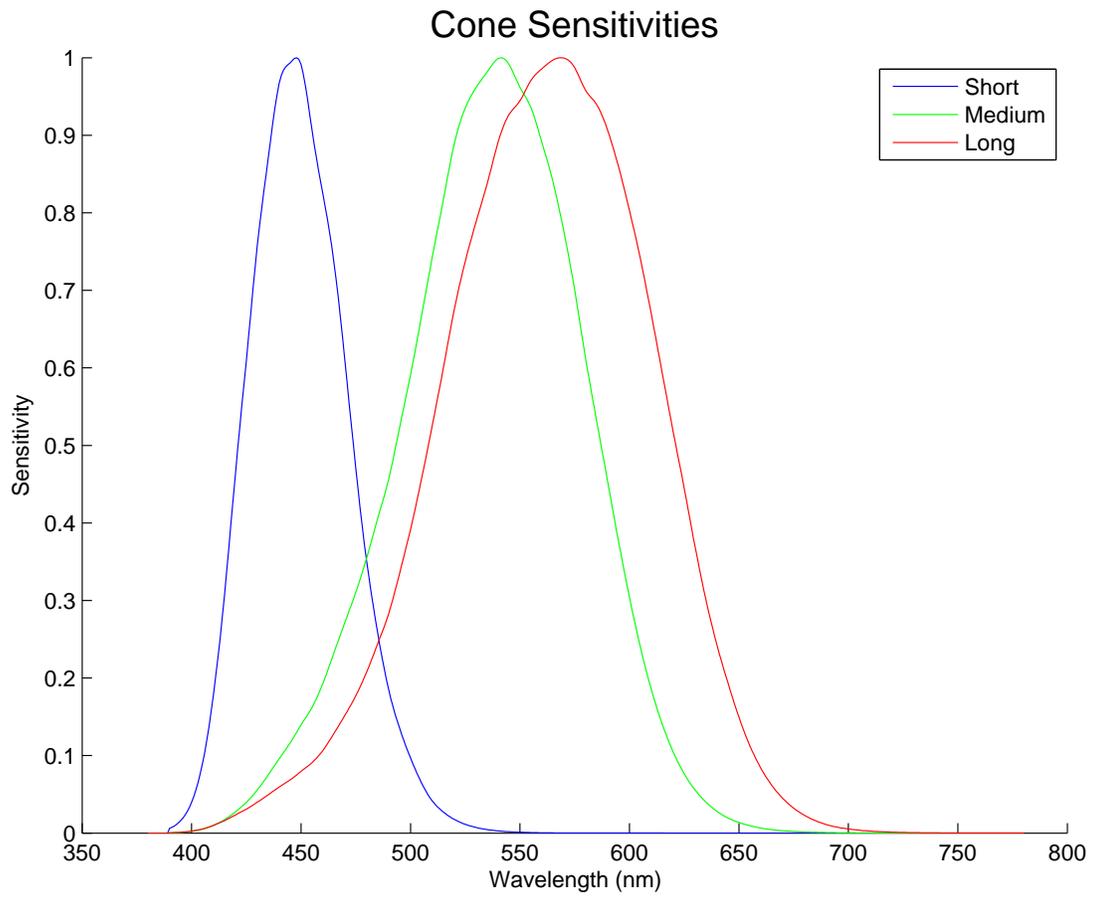


Figure 2: Average cone sensitivities used in the calculations of metameric matches (19). Values were obtained from <http://cvrl.ioo.ucl.ac.uk>. Sensitivities are shown for cones sensitive to short, medium, and long wavelengths.

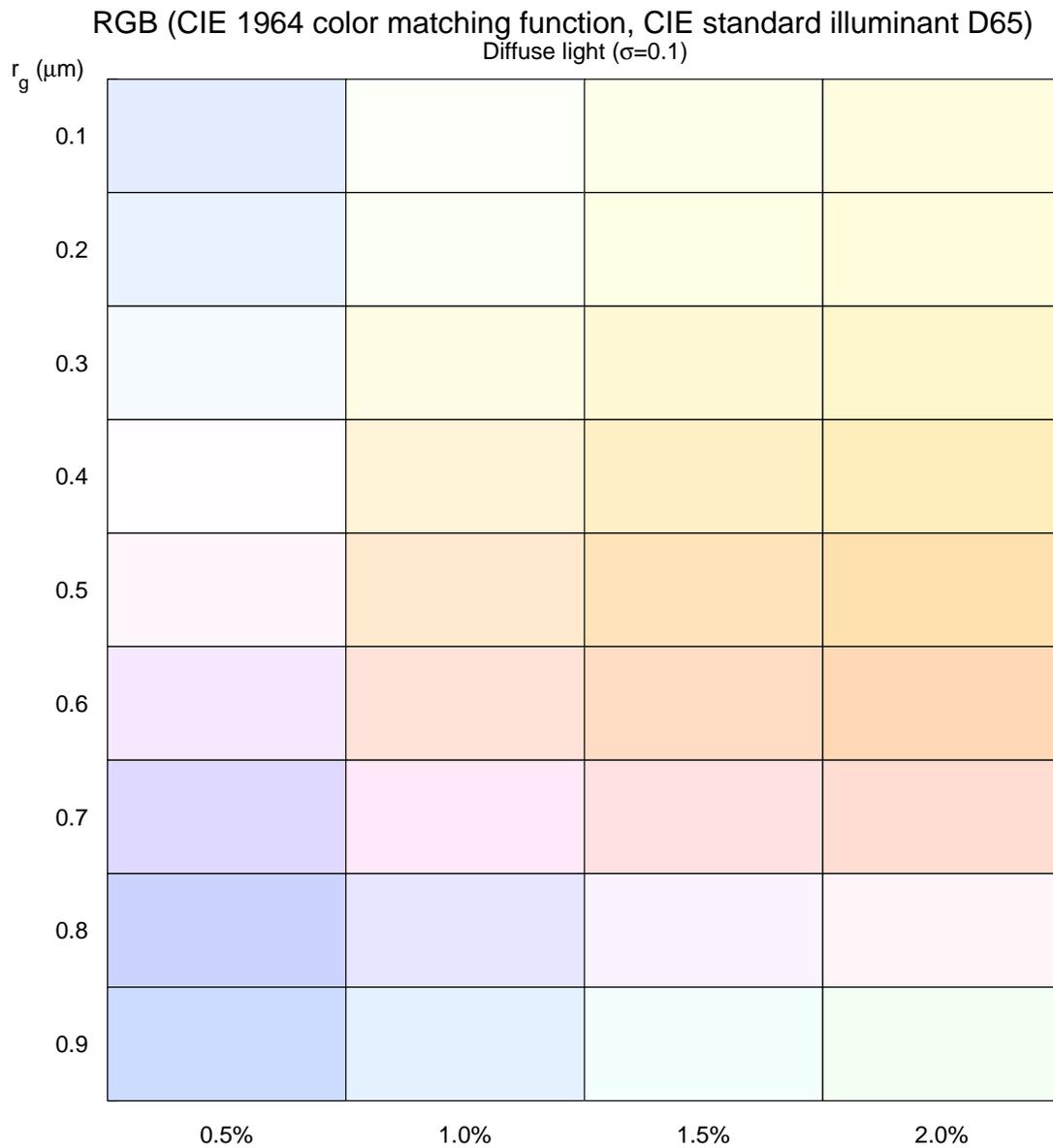


Figure 3: Color swatches of sky color from geoengineering as represented in RGB color space (one of four). To convert the diffuse light spectrum, the CIE 1964 color matching function was used (20), with a specified white point corresponding to the CIE standard illuminant D65, or a color temperature of 6504 K (21).

RGB (Stiles and Burch 10 degree color matching function, CIE standard illuminant D65)
Diffuse light ($\sigma=0.1$)

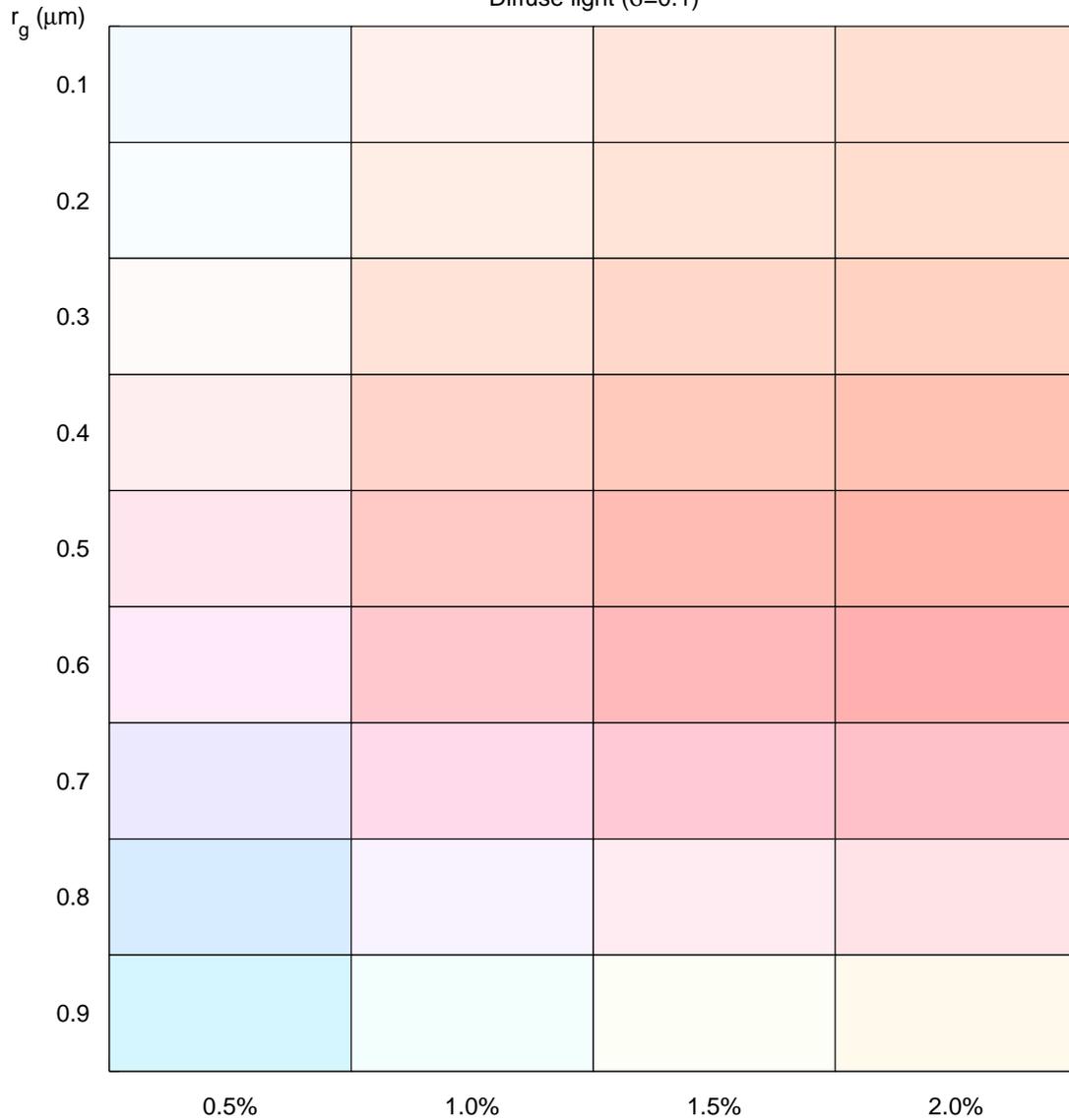


Figure 4: Color swatches of sky color from geoengineering as represented in RGB color space (two of four). To convert the diffuse light spectrum, the Stiles and Burch 10 degree color matching function was used (22), with a specified white point corresponding to the CIE standard illuminant D65, or a color temperature of 6504 K (21).

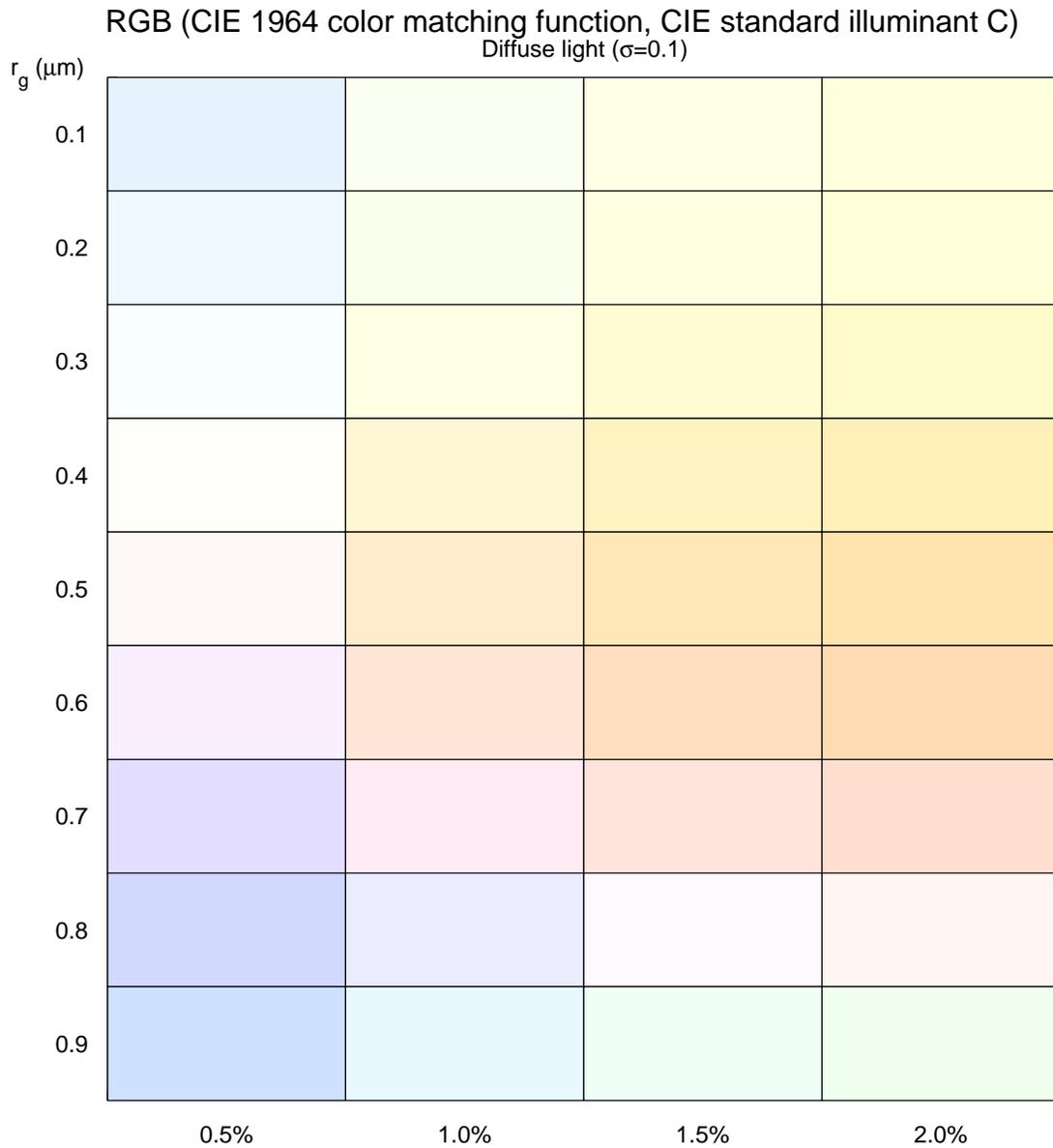


Figure 5: Color swatches of sky color from geoengineering as represented in RGB color space (three of four). To convert the diffuse light spectrum, the CIE 1964 color matching function was used (20), with a specified white point corresponding to the CIE standard illuminant C, or a color temperature of 6774 K (21).

RGB (Stiles and Burch 10 degree color matching function, CIE standard illuminant C)
Diffuse light ($\sigma=0.1$)

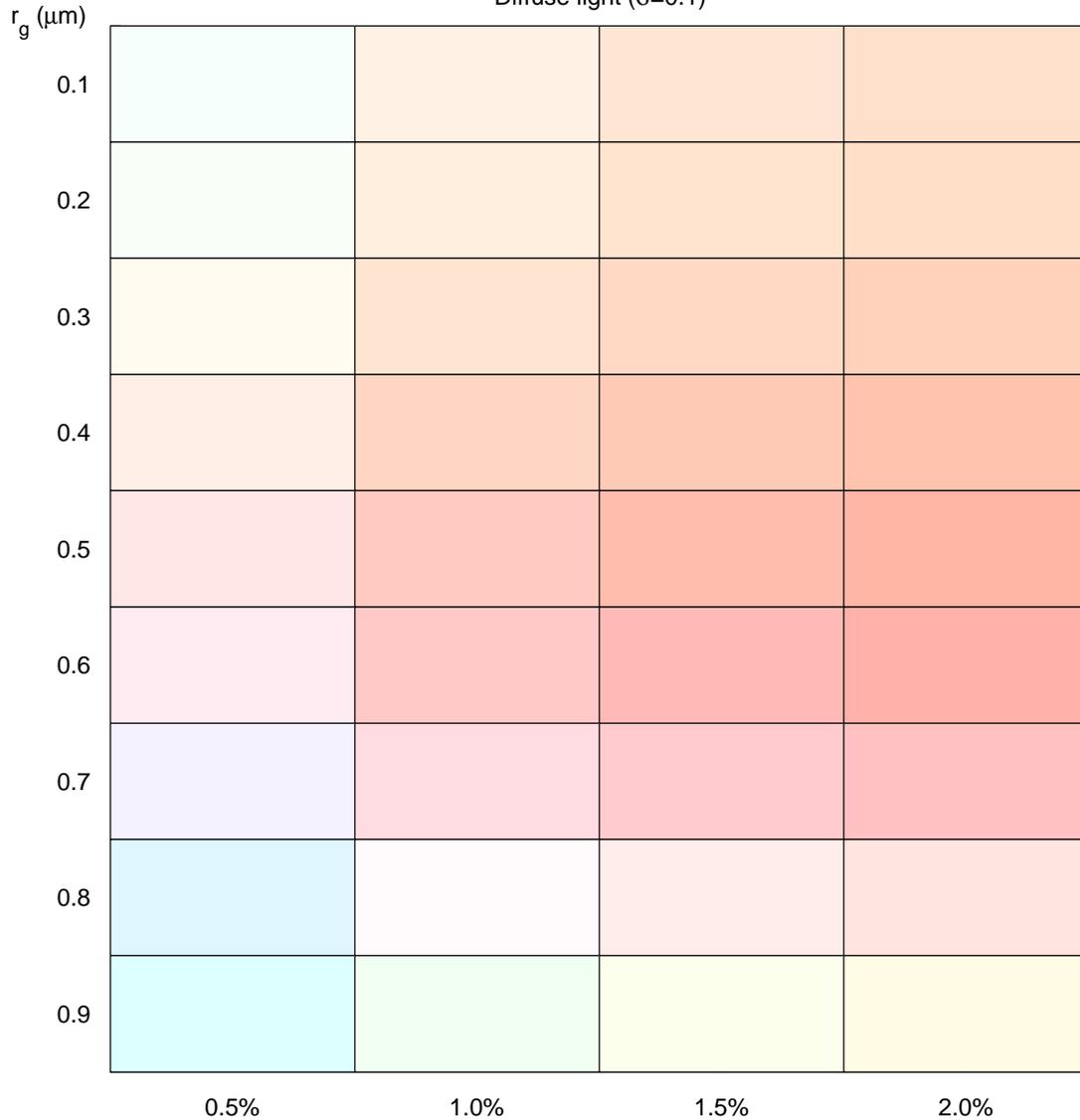


Figure 6: Color swatches of sky color from geoengineering as represented in RGB color space (four of four). To convert the diffuse light spectrum, the Stiles and Burch 10 degree color matching function was used (22), with a specified white point corresponding to the CIE standard illuminant C, or a color temperature of 6774 K (21).