



## Adiabatic Electron Transfer: Comparison of Modified Theory with Experiment

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## Adiabatic Electron Transfer: Comparison of Modified Theory with Experiment

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The radical cations of properly designed bishydrazines allow comparison of observed and calculated electron transfer rate constants. These compounds have rate constants small enough to be measured by dynamic electron spin resonance spectroscopy and show charge transfer bands corresponding to vertical excitation from the energy well for the charge occurring upon one hydrazine unit to that for the electron-transferred species. Analysis of the data for all six compounds studied indicates that the shape of the adiabatic surface on which electron transfer occurs can be obtained from the charge transfer band accurately enough to successfully predict the electron transfer rate constant and that explicit tunneling corrections are not required for these compounds.

Reactions in which a single electron is transferred are extremely important in chemistry and biology and have received a great amount of both experimental and theoretical attention since the seminal theoretical work by Marcus in the late 1950s (1, 2). Marcus introduced a method for estimating the barrier  $\Delta G_{\text{et}}^*$  for electron transfer (ET) from three parameters: the vertical reorganization energy  $\lambda$ , the electronic interaction matrix element  $V$ , and the exothermicity of the reaction  $\Delta G^\circ$ . In the simplest case (Fig. 1), a  $\Delta G^\circ = 0$  reaction,  $\lambda$  is the vertical gap between the minimum on the energy surface of the precursor and the energy surface of the product when neither the solvent nor the internal geometry are allowed to relax.  $\lambda$  is the sum of a solvent contribution ( $\lambda_s$ ) and an internal vibrational contribution ( $\lambda_v$ ), that is  $\lambda = \lambda_s + \lambda_v$ . Marcus addressed ways to estimate these quantities (1, 2). The amount of electronic mixing between the precursor and product surfaces is measured by  $V$ .

In recent years, most experimental and theoretical studies have concentrated on

long-distance ET reactions, which are initiated by photoexcitation (3). These reactions have small  $V$  and are usually very exothermic. The most important contributions that have emerged from these studies have been the development of vibronic coupling theory to treat such reactions (4) and landmark pulse radiolysis studies (5) that established the existence of the "inverted region" predicted by Marcus. Such reactions are involved in the charge separation that occurs in photosynthetic reaction centers (6), and the development of fast laser kinetic techniques has been crucial in such studies (3, 6). The great majority of biological ET reactions, however, occur in the dark and have small  $\Delta G^\circ$ . The present work focuses on a series of carefully designed molecules in which ET occurs with  $\Delta G^\circ = 0$  and without photoexcitation. These molecules display optical absorption spectra from which  $\lambda$  and  $V$  can be estimated, allowing quantitative testing of ET theory.

Symmetrical transition metal-centered intervalence (IV) compounds are conceptually the simplest ET systems and have played a major role in elucidating ET reactions since the first example was prepared in 1969 (7). In IV compounds, two metal atoms are connected by a bridging ligand, and

the overall charge formally places the metals in different oxidation states. Whether excess charge is delocalized over both metals or localized on one is determined by the relative sizes of  $\lambda$  and  $V$  (7). If  $V < \lambda/2$ , then charge localization occurs, and there are separate potential energy wells corresponding to the higher charge being on one metal or the other. These wells are displaced from each other on an ET coordinate  $X$  (Fig. 1). If  $V$  is large enough, a localized IV compound shows a charge transfer (CT) band, which allows measurement of  $\lambda$ .

Hush developed a simple theory for estimating both  $\lambda$  and  $V$  from such IV-CT bands (8). Marcus (1, 2) and Hush (8) assume that the diabatic energy surfaces (the energy wells in the absence of electronic coupling) are parabolas in a plot of energy versus  $X$ . In this case, the transition energy at the IV-CT maximum ( $E_{\text{op}}$ ) is equal to  $\lambda$ . Hush's estimate of  $V$  ( $\text{cm}^{-1}$ ), which we shall designate as  $V_{\text{H}}$  to distinguish it from other estimates, is

$$V_{\text{H}} = (0.0206/d)(\Delta v_{1/2} \epsilon_{\text{max}} E_{\text{op}})^{1/2} \quad (1)$$

where  $d$  ( $\text{\AA}$ ) is the ET distance,  $\Delta v_{1/2}$  ( $\text{cm}^{-1}$ ) is the IV-CT band width at half-height, and  $\epsilon_{\text{max}}$  ( $\text{M}^{-1}\text{cm}^{-1}$ ) is the molar extinction coefficient at the band maximum. Tunneling corrections are also assumed to be necessary to calculate the ET rate constant  $k_{\text{et}}$  (1, 2, 8). Estimation of the size of the tunneling correction requires knowing the averaged energy  $h\nu_v$  (where  $h$  is Planck's constant) of the vibrational frequencies  $\nu_v$  active in the ET process, which Hush also estimated from the IV-CT band width (8).

Symmetrical IV compounds would provide the most direct test of the validity of the ET parameters derived from their IV-CT bands, allowing comparison of the calculated rate constant with the experimental value. Unfortunately no adequate method exists for measuring the large values of  $k_{\text{et}}$  predicted for transition metal IV compounds (3). There is no transient to follow

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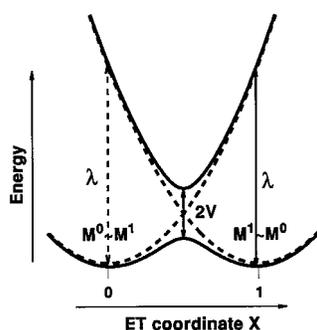
for ET within symmetrical IV compounds, precluding the use of fast laser kinetic measurements (9–11). We have prepared organic analogs of IV compounds that solve the problem of measuring  $k_{\text{et}}$  and report a classical analysis of IV-CT bands that focuses on proper estimation of the adiabatic energy surface on which ET occurs. Parameters derived from the IV-CT bands allow accurate estimation of  $k_{\text{et}}$  for our compounds without the need for explicit tunneling corrections.

We have developed IV compounds containing hydrazines as the charge-bearing units. These IV compounds have much smaller values of  $k_{\text{et}}$  than the transition metal-centered compounds, even when  $V$  is rather large, because hydrazines have far larger values of  $\lambda_{\text{v}}$  than metal complexes. We can adjust  $k_{\text{et}}$  for our compounds such that it becomes measurable by dynamic electron spin resonance (ESR), because  $\lambda_{\text{v}}$  and  $V$  are adjustable by changes in the substituents at the nitrogens and  $\lambda_{\text{s}}$  is sensitive to solvent. For the nitrogen splitting constant of  $\sim 13$  G for a hydrazine radical cation, the ESR spectrum is sensitive to intramolecular ET in an IV compound when  $k_{\text{et}}$  is near  $10^8$  s $^{-1}$  (12). We found that bishydrazines linked by two sets of four  $\sigma$  bonds have high enough  $\epsilon_{\text{max}}$  for convenient study by optical spectroscopy (12). Alteration of the remaining substituents produced compounds that were sufficiently stable in the IV oxidation state (+1) and had values of  $k_{\text{et}}$  large enough to measure (Fig. 2). The completely N,N'-bicyclic-substituted compound  $1^+$  has  $k_{\text{et}}$  near  $10^8$  at room temperature in acetonitrile (AN) (13). Compounds with unlinked third alkyl substituents at nitrogen ( $2^+$  to  $4^+$ ) have higher  $\lambda_{\text{v}}$ , and  $k_{\text{et}}$  is too small to measure accurately without thermal decomposition in AN, but we were able to measure  $k_{\text{et}}$  near room temperature using a solvent with lower  $\lambda_{\text{s}}$ , methylene chloride (MC) (14). Attaching diazabicyclooctyl groups in para positions on a benzene ring provided an aromatic-bridged compound, but  $k_{\text{et}}$  was too large to be measured accurately (15). Substitution of methyls for the ring hydrogens ( $5^+$  and  $6^+$ ) increased the N-aryl twist angle, decreasing  $V$  and  $k_{\text{et}}$ . Both  $5^+$  and  $6^+$  have measurable  $k_{\text{et}}$  in the temperature range  $T = 245 \pm 10$  K in AN and  $200 \pm 15$  K in MC (16). These studies have provided eight sets of experimental  $k_{\text{et}}(T)$  data for comparison with rate constants calculated from optically derived ET parameters.

Marcus-Hush theory assumes parabolic diabatic energy surfaces (Fig. 1). Electronic coupling  $V$  produces the double-well adiabatic energy ground-state surface  $E_1$  and excited-state surface  $E_2$ . There is an avoided crossing ( $E_2 - E_1 = 2V$ ) at  $X = 0.5$  (1,

2, 8). This is true for large values of  $V$  as well as the small values for which the expressions were originally derived (17). Using parabolic diabatic surfaces, the IV-CT band width depends only on  $E_{\text{op}}$ ; the band width at half height is Hush's high-temperature limit (htl) value,  $\Delta\nu_{1/2}^{\text{htl}} = [16RT(\ln 2)E_{\text{op}}]^{1/2}$ , where  $R$  is the gas constant, and the band is symmetrical about  $E_{\text{op}}$ . Experimental IV-CT bands are significantly broader than  $\Delta\nu_{1/2}^{\text{htl}}$  and are broader on the high-energy side of  $E_{\text{op}}$  than on the low-energy side (4, 7, 9). For our compounds,  $\Delta\nu_{1/2}^{\text{obs}}/\Delta\nu_{1/2}^{\text{htl}}$  ranged from 1.15 to 1.68. Hush rationalized observed band widths larger than  $\Delta\nu_{1/2}^{\text{htl}}$  by introducing dependence of band width on  $h\nu_{\text{v}}$ . He used tunneling factors depending on the contribution of each component of  $h\nu_{\text{v}}$  to  $\nu_{\text{v}}$  in calculating  $k_{\text{et}}$  (8). Application of his equations to our compounds produces calculated rate constants that are too small if tunneling is ignored. Hush's tunneling equations are only supposed to be valid when  $h\nu_{\text{v}} < 2RT$ , and most of the active modes estimated by dynamics calculations on  $1^+$  are larger (18). Not surprisingly, use of Hush's tunneling equations outside the range in which they are valid does not give the experimental rate constants; the calculated ones are too large.

The IV-CT absorption bands that have the observed shape (14, 16) can be simulated well by the equations derived from vibronic coupling theory (19). Band simulation is important because experimental data typically have at least some overlap of the IV-CT band with the tails of other bands, and if band shape simulation cannot be used, there is no good criterion for assessing band width accurately. Although ET parameters giving good fit to the IV-CT bands



**Fig. 1.** Marcus-Hush diagram for ET within a +1 charged symmetrical IV compound. The simplest case,  $\Delta G^\circ = 0$ , is shown. The parabolic diabatic energy surfaces are shown as broken lines, and the adiabatic surfaces for electronic coupling  $V$  (drawn for  $V = \lambda/8$ ) are shown as solid lines. Vertical energy gaps at the energy minima for both the diabatic parabolic surfaces (shown in the left well) and the adiabatic surfaces (shown in the right well) are  $\lambda = E_{\text{op}}$ .

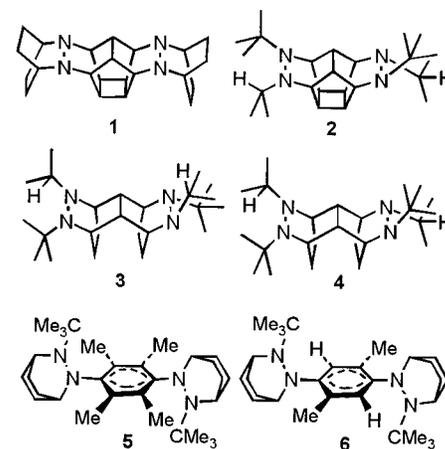
were obtained, there are serious problems in applying vibronic coupling theory to rate constant calculations for our compounds. The separation of  $\lambda$  into  $\lambda_{\text{v}}$  and  $\lambda_{\text{s}}$  is critical for calculation of  $k_{\text{et}}$ , but separation based on the band simulations proved ambiguous because the calculated  $\lambda_{\text{v}}/\lambda_{\text{s}}$  is sensitive to  $h\nu_{\text{v}}$ , and consistent values of  $\lambda_{\text{s}}$  and  $\lambda_{\text{v}}$  were not obtained when the same compound was examined in different solvents (14, 16). The vibronic coupling constant ( $S = \lambda_{\text{v}}/h\nu_{\text{v}}$ ) is large for our compounds, requiring the potential-energy surface to remain harmonic to past the 14th vibrational level (which seems unlikely) for vibronic coupling theory to work quantitatively. The IV-CT band analysis is sensitive to the vibrational level separations near vibrational levels  $S$ , but the rate constant calculation is only sensitive to separations of vibrational levels 0 to 4. When  $k_{\text{et}}$  was calculated using Jortner's double-sum rate equation, values too small by factors of  $>20$  were obtained (14, 16).

The rather large values of  $V$  for our compounds place their intramolecular ET firmly in the adiabatic rate regime (1, 2). Adiabatic reactions are those in which a system crosses from one energy well to another with a probability ( $\kappa_{\text{el}}$ ) of unity when sufficient thermal energy is available;  $\kappa_{\text{el}} > 0.99$  for  $1^+$  through  $6^+$  (20). As  $V$  becomes small,  $\kappa_{\text{el}}$  becomes much less than 1, and a reaction becomes significantly nonadiabatic. In nonadiabatic reactions,  $k_{\text{et}}$  is principally determined by vibronic coupling (1–4).

We use the “semiclassical” adiabatic rate equation (2)

$$k_{\text{et,ad}} = \nu_{\text{v}}(\lambda_{\text{v}}/\lambda)^{1/2} \exp(-\Delta G^*/RT) \quad (2)$$

where the ET rate constant is only linearly dependent on  $h\nu_{\text{v}}$  and is quite insensitive to the partitioning between  $\lambda_{\text{s}}$  and  $\lambda_{\text{v}}$ . The



**Fig. 2.** Structures of the bishydrazines giving radical cations for which  $k_{\text{et}}$  has been measured. Me, methyl ( $\text{CH}_3$ ).

only critical parameter is  $\Delta G^*$ , the energy difference between  $E_1$  at the ET transition-state maximum and at the energy minimum for the system (21, 22). The problem of estimating  $k_{\text{et}}$  for our adiabatic reactions is thus essentially reduced to finding a sufficiently accurate representation of  $E_1$  as a function of  $X$  to allow extrapolation from  $X_{\text{min}}$  to  $X = 0.5$ . We therefore have turned our attention to determining  $E_1$  as a function of  $X$  from the IV-CT band. Optical absorption band shape determined from classical theory maps the ground- and excited-state adiabatic energy surfaces through the Boltzmann factor  $\epsilon_{\text{rel}} = \epsilon/\epsilon_{\text{max}} = \exp[-(E_1 - E_{1,\text{min}})/RT]$  and the photon energy  $h\nu = E_2 - E_1$ . Thus, at 298 K,  $\epsilon_{\text{rel}}$  drops to 0.5 when  $E_1$  is  $144 \text{ cm}^{-1}$  higher than the minimum, and the vertical energy gaps between  $E_1$  and  $E_2$  at these points on the  $E_1$  surface are given by the  $h\nu$  values (Fig. 3). This allows calculation of IV-CT band shape from adiabatic surfaces without knowledge of the vibronic coupling parameters that produced these surfaces. These parameters are, in principle, very complex (22). An IV compound thus reveals its adiabatic ET surfaces near  $X_{\text{min}}$  through its IV-CT band, and adiabatic surfaces that fit a symmetrical IV-CT band must have the correct relative shapes for  $X$

about  $-0.2$  to  $+0.2$  (on the ground-state surface) and  $+0.8$  to  $+1.2$  (on the excited-state surface).

The adiabatic surfaces used in Marcus-Hush theory are derived by solving a two-state secular determinant with quadratic diabatic Hamiltonian matrix elements  $H_{\text{aa}} = \lambda X^2$  and  $H_{\text{bb}} = \lambda(1 - X)^2$  (1, 2, 17). To obtain adiabatic energy surfaces that fit the CT bands, we solved the secular determinant using modified "quartic augmented" matrix elements having a  $CX^4$  quartic term and a  $1/(1 + C)$  normalization term

$$H'_{\text{aa}} = [\lambda X^2/(1 + C)][1 + CX^2]$$

$$H'_{\text{bb}} = [\lambda(1 - X)^2/(1 + C)][1 + C(1 - X)^2]$$
(3)

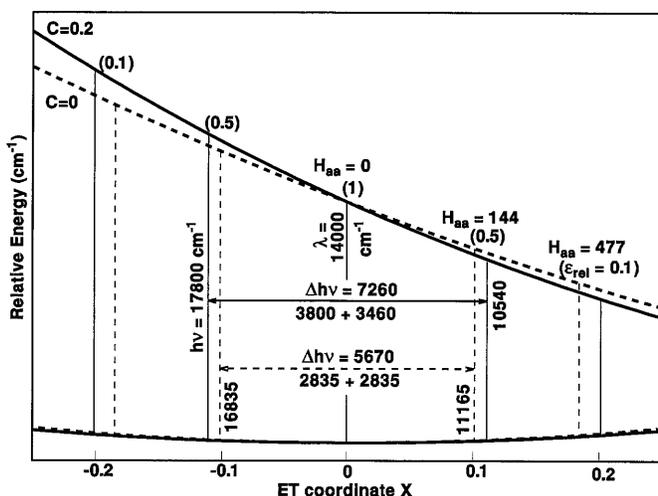
When  $C = 0$ , Eq. 3 gives the Marcus-Hush quadratic matrix elements. The width of the CT bands calculated using the modified diabatic surfaces can be adjusted by changing  $C$ . For our compounds, fits to the experimental spectra were obtained with  $C = 0.1$  to  $0.3$ . The principal effect of increasing  $C$  is to make the diabatic curves cross at a smaller energy value than the value of  $\lambda/4$  for  $C = 0$  parabolas. Crossing occurs at an energy that is smaller by the fraction  $(1 + C/4)/(1 + C)$  (for example,  $0.875$  at  $C =$

$0.2$ ). This change makes the ET barrier calculated for the adiabatic surfaces,  $\Delta G^* = E_{1,\text{max}} - E_{1,\text{min}}$ , substantially smaller than that for  $C = 0$  parabolas (23). The minima on the ground-state adiabatic surface move positive of  $X = 0$  and negative of  $1$  as  $V$  increases, and the observed width in  $X$  increases as  $C$  increases, making the interpolation to  $X = 0.5$  smaller.

The experimental and calculated rate constants are compared in Table 1. We designate the experimental  $k_{\text{et}}$  interpolated or extrapolated to 300 K from the ESR data as  $k_{\text{esr}}$ , and the  $k_{\text{et,ad}}$  calculated from Eq. 2 using the parameters that give best fit to the optical band at room temperature as  $k_{\text{opt}}$ . For all six compounds, we used  $h\nu_{\text{v}} = 800 \text{ cm}^{-1}$ , close to the value estimated by dynamics calculations on  $1^+$  (18). The value of  $k_{\text{et,ad}}$  is rather insensitive to  $\lambda_{\text{s}}$  and  $\lambda_{\text{v}}$ . We partitioned  $\lambda_{\text{v}}$  and  $\lambda_{\text{s}}$  on the basis of Marcus's dielectric continuum  $\lambda_{\text{s}}$  equation (1, 2), which can be written as  $(\lambda \text{ in kcal/mol}) \lambda_{\text{s}}(\text{AN}) = 3.64[\lambda(\text{AN}) - \lambda(\text{MC})]$ , assuming  $\lambda_{\text{v}}$  to be the same in both solvents (14). This partitioning puts  $(\lambda_{\text{v}}/\lambda)^{1/2}$  in the narrow range  $0.75$  to  $0.89$  for our compounds (24). There is currently uncertainty about evaluating  $V$  from IV-CT bands. Young and co-workers introduced a dependence on the refractive index  $n$  of the solvent in calculation of  $V$  when they derived vibronic coupling theory fits to IV-CT bands (19). Dependence of  $V$  on  $n$  does not appear in Hush's equation (Eq. 1) (8). It is not clear which formulation is to be preferred, and we therefore consider both Hush's traditional  $V_{\text{H}}$  and the lower value  $V_{\text{L}} = V_{\text{H}}/(n)^{1/2}$ , which is the expression of (19) applied to classical theory (25, 26). In almost every instance, the  $V_{\text{L}}$  values produce a  $k_{\text{opt}}/k_{\text{esr}}$  ratio closer to unity than do the  $V_{\text{H}}$  values (Table 1). The  $k_{\text{opt}}/k_{\text{esr}}$  ratios using  $V_{\text{L}}$  are close to 1 (range:  $0.9$  to  $1.6$ ) for the  $\sigma$ -bridged examples, where 300 K is within the temperature range studied. As might be anticipated, agreement is not as good for the aromatic-bridged examples, where  $k_{\text{esr}}$  had to be extrapolated from measurements at  $245 \pm 10 \text{ K}$  in AN and  $200 \pm 15 \text{ K}$  in MC. The largest ratio (for  $6^+$  in MC) is under 4, and even this calculation is probably still within experimental error of  $k_{\text{esr}}$ .

The observed IV-CT band shape demonstrates that parabolic diabatic energy surfaces should not be used in a Marcus-Hush double potential-well analysis intended to produce adiabatic surfaces. Simple classical CT band analysis, using quartic-augmented diabatic surfaces that actually fit the IV-CT band, appears to allow accurate estimation of the classical ET barrier ( $\Delta G^*$ ), because the calculated rate constant produces excellent agreement

**Fig. 3.** Origin of the larger band width and asymmetry for quartic-augmented diabatic surfaces. The hypothetical  $V = 0$  case is illustrated for simplicity. Parabolic  $C = 0$  (broken lines) and  $C = 0.2$  (solid lines) diabatic energy surfaces near the energy minimum at  $X = 0$ , drawn for  $\lambda = 14,000 \text{ cm}^{-1}$  at  $25^\circ\text{C}$  are shown, with the vertical energy gaps  $h\nu$  corresponding to  $\epsilon_{\text{rel}} = 0.5$  for both surfaces, as well as positions on the  $X$  coordinate for the  $\epsilon_{\text{rel}} = 0.1$  gaps.



**Table 1.** Comparison of observed and calculated ET rate constants.

Compound	Solvent	$k_{\text{ESR}}^{\text{vib}}$ ( $10^8 \text{ s}^{-1}$ )	$V_{\text{L}}$ (kcal/mol)	$V_{\text{H}}$ (kcal/mol)	$k_{\text{opt}}/k_{\text{ESR}}$	
					Using $V_{\text{L}}$	Using $V_{\text{H}}$
1 <sup>+</sup>	AN	1.3	3.37	3.76	1.1	2.0
2 <sup>+</sup>	MC	1.3	2.52	3.00	1.6	3.3
3 <sup>+</sup>	MC	1.1	3.02	3.60	0.9	2.0
4 <sup>+</sup>	MC	1.0	3.02	3.60	0.9	2.0
5 <sup>+</sup>	AN	8.6	2.84	3.29	0.6	1.2
5 <sup>+</sup>	MC	37.6	2.77	3.31	1.1	2.2
6 <sup>+</sup>	AN	5.4	4.22	4.88	1.6	3.4
6 <sup>+</sup>	MC	24.5	4.10	4.90	3.6	8.8

with experiment. This agreement suggests that our procedure accurately evaluates  $\lambda$  and  $V$  for these systems. It is noteworthy that, for the strongly adiabatic systems studied here, classical theory that ignores tunneling reproduces the observed rate constant, even though  $h\nu_v$  modes far larger than  $2RT$  are involved. We suggest that this success means that tunneling effects have been effectively incorporated into the calculated ground-state adiabatic surface by our band-fitting procedure. To our knowledge, there have been no prior comparisons of calculated rate constants based on optically determined ET parameters with experimental ones for ET processes that occur in the adiabatic rate regime. Our results verify that Hush's method for extracting  $V$  is quantitatively correct in the absence of intensity borrowing problems (10). The dependence on the solvent's refractive index introduced by Young and co-workers apparently produces a more accurate  $V$  value. For our high- $S$  and high- $V$  cases, classical theory is more accurate for estimating rate constants than is the use of vibronic coupling theory outside the parameter ranges for which it was designed (27). It remains to be seen how well a similar approach using  $\kappa_{el}$  in Eq. 2 will work when  $V$  is smaller and the ET reaction is not strongly adiabatic.

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9. There are significant problems in determining values of  $V$  for ET within photoexcited asymmetrical systems, which do have a transient to follow. Electronic mixing of the IV state with locally excited states is allowed, and both CT band intensities and back-ET rate constants are greatly affected by them. Good agreement with theory is obtained, but neither  $k_{et}$  nor  $\epsilon_{max}$  relates to the  $V$  shown in Fig. 1 (10). For example, the  $V$  values estimated for Paddon-Row's  $\sigma$ -bridged aromatic, cyanoolefin systems (11), which appeared to be the best-documented series of such measurements available, have recently been retracted, with the statement that both the CT band intensities and back-ET rate constants are basically determined by mixing of the IV state with locally excited states (10).
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20. We obtained  $\kappa_{el}$  using equations 36 through 38 in (2), with the  $h\nu_v = 800 \text{ cm}^{-1}$  used here.
21. Knowledge of  $\Delta G^\ddagger$  is far from sufficient to calculate  $k_{et}$  for a nonadiabatic case, where  $k_{et}$  is controlled by Franck-Condon factors, which in principle require a detailed knowledge of the contribution of all of the many modes (22) making up  $\lambda_v$  for their calculation. The adiabatic nature of our systems makes calculation of  $k_{et}$  far simpler than the case for nonadiabatic ET systems.
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23. The quartic-augmented surfaces produce a value of  $\lambda$  that is slightly higher than  $E_{op}$  but closer to  $E_{cp}$  than the  $\lambda$  obtained using vibronic coupling theory fits to the same data.  $E_{1,min}$  is slightly more negative than  $-V^2/\lambda$  obtained using parabolas, but the effect on

$E_{1,max}$  is much larger. Use of  $\Delta G^\ddagger \equiv (\lambda/4)(1 + C/4)/(1 + C) - V + V^2/\lambda$  provides an excellent approximation to  $\Delta G^\ddagger$  for our compounds.

24. We have evidence that the dielectric continuum approximation is a rather poor assumption for all of these compounds except for  $1^+$ , and that it overestimates  $\lambda_s$ . Use of a smaller  $\lambda_s$  would make  $(\lambda_v/\lambda)^{1/2}$  even closer to 1 and would not affect the estimation of  $k_{et,ad}$  significantly.
25. The  $n^{-1/2}$  dependence for  $V$  described in (19) arises from the use of a refractive index factor  $f(n) = n^3$  in an expression for radiative emission (their equation 3). More recently, these authors have suggested using a more complex expression,  $f(n) = n[(n^2 + 2)/3]^2$  [equation 3b of (26)], which they note produces a contribution that is about 11% smaller with a virtually identical dependence on  $n$ ; they also indicate in appendix 3 (26) that the true dependence may be even more complicated.
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27. Because use of only  $\lambda$  and  $C$  fits the experimental IV-CT band shape, it is hardly surprising that, when the same data are fit using the three parameters of vibronic coupling theory ( $\lambda_s$ ,  $\lambda_v$ , and  $h\nu_v$ ), strong interaction of these parameters results (14, 16). In studies using vibronic coupling theory to fit optical band shape or plots of  $k_{et}$  and  $\Delta G^\ddagger$ , it is usually stated that all three parameters were determined from the fit. This determination cannot be made for any of our data because of the strong interaction of these parameters.
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## Structure of the Carboxyl-Terminal Dimerization Domain of the HIV-1 Capsid Protein

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The carboxyl-terminal domain, residues 146 to 231, of the human immunodeficiency virus-1 (HIV-1) capsid protein [CA(146–231)] is required for capsid dimerization and viral assembly. This domain contains a stretch of 20 residues, called the major homology region (MHR), which is conserved across retroviruses and is essential for viral assembly, maturation, and infectivity. The crystal structures of CA(146–231) and CA(151–231) reveal that the globular domain is composed of four helices and an extended amino-terminal strand. CA(146–231) dimerizes through parallel packing of helix 2 across a dyad. The MHR is distinct from the dimer interface and instead forms an intricate hydrogen-bonding network that interconnects strand 1 and helices 1 and 2. Alignment of the CA(146–231) dimer with the crystal structure of the capsid amino-terminal domain provides a model for the intact protein and extends models for assembly of the central conical core of HIV-1.

The 26-kD capsid protein (CA) performs essential roles both early and late in the life cycle of HIV. Capsid is initially translated as the central region of the 55-kD Gag polyprotein, where it functions in viral assembly (1, 2) and in packaging the cellular

protein cyclophilin A (3). As the virus buds, Gag is processed by the viral protease to produce three discrete new proteins—matrix, capsid, and nucleocapsid—as well as several smaller peptides. After capsid has been liberated by proteolytic processing, it rearranges into the conical core structure that surrounds the viral genome at the center of the mature virus (1, 4). Genetic analyses have revealed that capsid also performs essential roles as the virus enters,

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