MEASUREMENTS OF CYCLOTRON FEATURES AND PULSE PERIODS IN THE HIGH-MASS X-RAY BINARIES 4U 1538–522 AND 4U 1907+09 WITH THE INTERNATIONAL GAMMA-RAY ASTROPHYSICS LABORATORY

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ABSTRACT

We present a spectral and timing analysis of *International Gamma-Ray Astrophysics Laboratory* (*INTEGRAL*) observations of two high-mass X-ray binaries, 4U 1538–522 and 4U 1907+09. Our timing measurements for 4U 1538–522 find the pulse period to have exhibited a spin-up trend until approximately 2009, after which there is evidence for a torque reversal, with the source beginning to spin down to the most recently measured period of 525.407 ± 0.001 s. The most recent *INTEGRAL* observations of 4U 1907+09 are not found to yield statistically significant pulse periods due to the significantly lower flux from the source compared with 4U 1538–522. A spectral model consisting of a power-law continuum with an exponential cutoff and modified by two cyclotron resonance scattering features is found to fit both sources well, with the cyclotron scattering features detected at ~ 22 and ~ 49 keV for 4U 1538–522 and at ~ 18 and ~ 36 keV for 4U 1907+09. The spectral parameters of 4U 1538–522 are generally not found to vary significantly with flux and there is little to no variation across the torque reversal. Examining our results in conjunction with previous work, we find no evidence for a correlation between cyclotron line energy and luminosity for 4U 1538–522. 4U 1907+09 shows evidence for a positive correlation between cyclotron line energy and luminosity, which would make it the fourth, and lowest luminosity, cyclotron line source to exhibit this relationship.

Key words: pulsars: individual (4U 1538–522, 4U 1907+09) – stars: magnetic field – stars: oscillations – X-rays: binaries – X-rays: stars

Online-only material: color figures

1. INTRODUCTION

High-mass X-ray binaries (HMXBs) are a class of binary systems consisting of a neutron star with a high-mass (~ 10 – $20 M_{\odot}$), main-sequence companion. X-ray emission from the neutron star is driven primarily by accretion of material from the main-sequence companion, typically via either Roche lobe overflow in the case of less-massive companions or the stellar wind of a higher mass companion. The neutron star’s strong ($\sim 10^{12}$ – 10^{13} G) magnetic field channels accrete material onto the magnetic poles, forming an accretion column where the majority of the X-ray luminosity is produced via inverse Compton scattering of thermal photons produced at the stellar surface and bremsstrahlung radiation from within the column. Obtaining a detailed physical picture of this process is still an open problem in X-ray astrophysics. Early work (e.g., Meszaros & Nagel 1985; Klein et al. 1996) was generally limited in its ability to properly reproduce the accreting neutron star spectrum, due to the extreme complexity of the problem. Recently, however, work by Becker & Wolff (2007) has produced promising results, successfully reproducing the continuum spectra of several high-luminosity X-ray pulsars. In addition to the base continuum, several dozen HMXBs display absorption-like features in their spectra that are identified as cyclotron resonance scattering features (CRSFs, also known as cyclotron lines), produced by

the resonant scattering of photons on electrons moving in the magnetic field; the physical modeling of these features has also seen significant progress in work by Schönherr et al. (2007). Work is currently underway to merge the continuum and cyclotron line models into a single model capable of producing an accurate, physically motivated model for accreting neutron stars (Schwarm et al. 2013; Schwarm 2013).

The accretion-powered X-ray pulsar 4U 1538–522 was discovered in the early 1970s by the *Uhuru* satellite (Giacconi et al. 1974). Its main-sequence companion is the $\sim 20 M_{\odot}$ B0 star QV Nor (Reynolds et al. 1992). X-ray pulsations were first observed from the vicinity of 4U 1538–522 by Becker et al. (1977) and Davison (1977); Davison et al. (1977) identified these as coming from 4U 1538–522. The distance to 4U 1538–522 has been variously estimated to be 5.5 ± 1.5 (Crampton et al. 1978), 6.0 ± 0.5 (Ilovaisky et al. 1979), 6.4 ± 1.0 (Reynolds et al. 1992), and 4.5 (Clark 2004) kpc. Infrequent observations post-discovery showed 4U 1538–522 to be spinning down until the late 1980s, reaching a maximum period of ~ 531 s (Makishima et al. 1987; Davison 1977; Becker et al. 1977), after which extended BATSE monitoring between 1990 and 1995 by Rubin et al. (1997) showed the source to have transitioned to a long-term spin-up trend that would last until approximately 2009, when monitoring by the Gamma-ray Burst Monitor (GBM) on board the *Fermi* satellite, along with this work, show the

source to have transitioned to a spin-down state (see Figure 2). The early *OSO-8* and *Ariel-5* observations by Becker et al. (1977) and Davison et al. (1977) also established a ~ 3.7 day orbital period and provided the first picture of the binary orbit of the system, with the orbital parameters being updated by Makishima et al. (1987), Clark (2000), and Mukherjee et al. (2006). The exact characteristics of 4U 1538–522’s orbit remain somewhat uncertain: the three aforementioned references find three different values for the eccentricity, with Makishima et al. adopting $e = 0.08 \pm 0.05$, Clark finding solutions for both circular and elliptical ($e = 0.174 \pm 0.015$) orbits, and Mukherjee et al. supporting Clark’s elliptical solution. Efforts to determine the mass of 4U 1538–522 by van Kerkwijk et al. (1995) adopted a circular orbit, while recent work by Rawls et al. (2011) finds a mass of $0.87 \pm 0.07 M_{\odot}$ for Clark’s elliptical orbit and $1.104 \pm 0.177 M_{\odot}$ for the circular solution, making 4U 1538–522 potentially one of the lightest neutron stars known. The spectrum of 4U 1538–522 is fit well by a power law with an exponential cutoff (Makishima et al. 1987), with CRSFs at 22 (Clark et al. 1990) and ~ 47 keV, tentatively reported in *BeppoSAX* data by Robba et al. (2001), but not confirmed until a combined *RXTE* and *International Gamma-Ray Astrophysics Laboratory (INTEGRAL)* analysis by Rodes-Roca et al. (2009).

4U 1907+09 is another wind-accreting X-ray binary, also discovered by *Uhuru* (Giacconi et al. 1971). It is similar to 4U 1538–522 in its long pulse period (~ 440 s), short orbital period (~ 8.4 days), and optical companion (O8/O9, as found by Cox et al. 2005). For ~ 15 yr following the identification of the source as a pulsar by Makishima et al. (1984), the pulse period increased steadily from 437.4 s in 1984 (Makishima et al. 1984) to ~ 441 s in 1998, when the spin-down trend began to slow, leading to a torque reversal in 2005 (Fritz et al. 2006). This was followed relatively quickly by another reversal in mid-2007 (Inam et al. 2009; Şahiner et al. 2011) and the source began following approximately the same spin-down trend as it had between 1987 and 1998, a trend that thus far shows no sign of changing. The initial determination of the ~ 8.4 day orbital period showed flaring twice per orbit, suggesting the source was in orbit around a Be-type star (Marshall & Ricketts 1980), although subsequent optical observations indicated that the companion was more likely a supergiant (van Kerkwijk et al. 1989). Recent optical (Cox et al. 2005) and infrared (Nespoli et al. 2008) observations have more firmly established the companion as a O8/O9 supergiant, with Cox et al. finding a distance of 5.0 kpc to the source, while Kostka & Leahy (2010) have shown that the most likely scenario to produce the observed flaring involves a dense stellar wind along with a trailing stream of material between the neutron star and companion. Observations with *Ginga* established the existence of an absorption feature, identified as a CRSF, at ~ 19 keV (Mihara 1995; Makishima et al. 1999), with a second at ~ 39 keV detected in *BeppoSAX* data by Cusumano et al. (1998).

In this paper, we first present a summary of the observations used in our analysis in Section 2, followed by a brief discussion of the pulse timing measurements made for each source in Section 3. Section 4 presents the spectral analysis of each source, where the large energy range covered by the combination of the *INTEGRAL* Soft Gamma-Ray Imager (ISGRI) and the Joint European X-ray Monitor (JEM-X) instruments proves advantageous. Finally, we discuss these results in the context of recent theoretical results regarding accretion onto magnetic poles in Section 5.

Table 1

Sources Included in the Background Subtraction Routine for 4U 1538–522 and 4U 1907+09, with 20–40 keV ISGRI Counting Rates

Source	Counts s ^{-1a}	Source	Counts s ⁻¹
4U 1538–522	3.06	4U 1907+09	1.42
4U 1700–377	32.4	GRS 1915+105	44.9
GX 339–4	22.2	4U 1909+07	2.26
OA0 1657–415	11.3	4U 1916–053	1.76
4U 1626–67	6.70	XTE J1855–026	1.30
IGR J16320–4751	5.03	Ser X-1	1.24
GX 340+0	4.78	SS 433	1.23
H 1608–522	4.25	IGR J19140+0951	1.12
H 1636–536	3.17	IGR J18483–0311	0.92
IGR J16318–4848	3.16	Aql X-1	0.79
H 1705–440	2.23	Ginga 1843+009	0.69
PSR B1509–58	1.42	XTE J1901+014	0.39
4U 1630–47	ND ^b	SWIFT J1753.5–0127	ND
XTE J1652–453	ND ^b	4U 1812–12	ND
...	...	GX 17+2	ND
...	...	PSR J1846–0258	ND
...	...	3A 1850–087	ND

Notes.

^a 20–40 keV ISGRI count rates.

^b ND: not detected in the mosaic image.

2. OBSERVATIONS

We used two of the instruments on board *INTEGRAL*: the ISGRI (Lebrun et al. 2003), which is the upper layer of the Imager on Board the *INTEGRAL* Satellite (Ubertini et al. 2003), a coded-mask telescope with a $9^{\circ} \times 9^{\circ}$ fully coded field of view (FOV), and JEM-X 1 and 2 (Lund et al. 2003), twin coded-mask telescopes with circular FOVs of diameter $4^{\circ}.8$. Early in the *INTEGRAL* mission, only one JEM-X telescope was in operation at any given time, out of concern for the lifetime of the microstrip anodes used in the detectors, but a lowered operating voltage alleviated these concerns and recent (post-2009) observations have both detectors running simultaneously. The *INTEGRAL* satellite has a ~ 3 day orbit; the science data for each orbit (or “revolution”) are divided into ~ 2 ks long pointings called Science Windows (SCWs). The nominal energy range of ISGRI is 15 keV–1 MeV, but we follow the ISGRI team’s recommendation of a lower bound of 18 keV for data taken prior to revolution 848 and 20 keV for data taken prior to revolution 1000. The JEM-X data are limited to ≥ 5 keV for similar reasons. Neither source is detected above ~ 80 keV in ISGRI or ~ 30 keV in JEM-X. We extracted spectra and light curves using version 10.0 of the standard Offline Scientific Analysis (OSA) software provided by the *INTEGRAL* Science Data Center (ISDC).

Coded-mask detectors such as those used by ISGRI and JEM-X work by deconvolving the “shadowgram” produced by opaque elements in the mask placed over the detector. While this allows imaging to be performed in the normally difficult hard X-ray band, it also means the illuminated pixels in the detector receive light from every unocculted point in the FOV and as such every significant source in the FOV must be accounted for when determining the background for a given single source. We followed the recommendation of the ISDC and provided a catalog of all sources with detection significance greater than 6.0σ in the single SCW’s image. We provide the resulting list of sources in Table 1, along with their 20–40 keV counting rate in the combined mosaic of all SCWs. The 20–40 keV ISGRI mosaic images from all SCWs are provided in Figure 1.

Figure 1. Combined 20–40 keV significance mosaics of the sky around 4U 1907+09 (left) and 4U 1538–522 (right). Displayed coordinates are right ascension and declination in degrees. For clarity, the closest sources to 4U 1907+09 have been labeled with letters; they are (a) GRS 1915+105, (b) IGR J19140+0951, and (c) 4U 1909+07. While both images cover the full $27^\circ \times 27^\circ$ partially coded FOV of the ISGRI telescope, the SCWs that were selected to form these images all have the sources within the $9^\circ \times 9^\circ$ fully coded FOV. Both sources are clearly detected in the combined mosaics.

(A color version of this figure is available in the online journal.)

2.1. 4U 1538–522

Our ISGRI dataset comprises all publicly available data where 4U 1538–522 was within the 4.5° fully coded FOV, extending from 2003 January through 2010 April. The JEM-X data are selected in a similar fashion, taking all windows within the 2.4° radius fully coded FOV. There is a three year gap in the *INTEGRAL* coverage of 4U 1538–522, with no observations between late 2005 and late 2008. In the earlier data, the total ISGRI exposure is 715 ks, with 638 and 210 ks for JEM-X 1 and 2, respectively; the later dataset totals 417 ks of ISGRI exposure, 411 ks of JEM-X 1, and 172 ks of JEM-X 2.

2.2. 4U 1907+09

We analyzed SCWs beginning in 2007 November (*INTEGRAL* revolution 608) for 4U 1907+09, overlapping slightly with the selection of Şahiner et al. (2012). Selecting SCWs according to the same criteria as used for 4U 1538–522 amounts to 892 ks of ISGRI exposure, 908 ks of JEM-X 1, and 507 ks of JEM-X 2. The average flux from 4U 1907+09 is considerably lower than that of 4U 1538–522 and is indeed at what appears to be close to a historic low for the source (comparable to that seen by Makishima et al. 1999 and Coburn 2001). As a result, it is difficult to provide strong constraints on its spectral parameters.

3. TIMING ANALYSIS

We extracted 10 s binned *ISGRI* light curves in the 20–40 keV energy band with the OSA 10.0 analysis pipeline. The only departure from the standard procedure was the use of the alternate *ii_light* tool for light curve extraction, as the standard pipeline’s light curve extraction routine is not recommended for binning times less than 60 s (Chernyakova et al. 2010). After

Table 2
Orbital Parameters

Parameter	Units	4U 1538–522 ^a	4U 1907+09 ^b
$a \sin(i)$	lt-s	53.1 ± 1.5	83 ± 4
e	...	0.18 ± 0.01	$0.28^{+0.10}_{-0.14}$
P_{orb}	day	3.728382 ± 0.000011	$8.3753^{+0.0003}_{-0.0002}$
$T_{\pi/2}$	MJD	52851.33 ± 0.01	$50134.76^{+0.16}_{-0.20}$
ω_d	...	$40^\circ \pm 12^\circ$	$330^\circ \pm 20^\circ$

Notes.

^a Mukherjee et al. (2006).

^b in ‘t Zand et al. (1998).

extraction, the light curves were barycentered using the *barycent* tool also provided in the OSA package.

Due to the low signal to noise and few pulsations covered by the individual ~ 2 ks light curves, many light curves had to be appended to each other before any period determination could be made. The composite light curve was then corrected for the orbital motion of the source, using the best available orbital parameters. As the pulse profile of the source is non-sinusoidal and the composite light curve contains a moderate number of gaps, epoch folding (Leahy et al. 1983; Larsson 1996) was used for the period search, with 1σ errors determined according to Larsson (1996).

3.1. 4U 1538–522

For 4U 1538–522, we used the elliptical orbital parameters provided by Mukherjee et al. (2006), although using Clark’s (2000) circular solution did not result in any significant change in the pulse period. For convenience, these parameters are listed in Table 2. Light curves were grouped by requiring that no gaps larger than four days be present, in order to minimize the

Figure 2. Pulse period evolution of 4U 1538–522. Binary-corrected periods found in this work are represented by red asterisks, with previous measurements (Becker et al. 1977; Makishima et al. 1987; Corbet et al. 1993; Rubin et al. 1997; Clark 2000; Baykal et al. 2006) and recent *Fermi* GBM data (Finger et al. 2009) in black. Error bars are generally smaller than the data points. 4U 1538–522 evidently underwent a torque reversal sometime in late 2008 or early 2009. The final four data points are in very good agreement with the *Fermi* GBM data; this agreement is detailed in the inset.

(A color version of this figure is available in the online journal.)

Table 3

Periods for 4U 1538–522 Determined via Epoch Folding

MJD	Period (s)
53222.176–53230.047	526.644 ± 0.003
53407.638–53415.310	526.483 ± 0.003
53429.742–53439.492	526.401 ± 0.002
53616.904–53620.899	526.424 ± 0.007
54855.844–54870.322	525.262 ± 0.002
55073.587–55090.517	525.379 ± 0.001
55250.376–55258.045	525.401 ± 0.004
55264.806–55288.806	525.415 ± 0.001

effect of large gaps in the data when performing epoch folding. Eight sets of SCWs using this grouping have sufficient time and statistics to return clear single peaks in the epoch folding results; we summarize these results in Table 3 and the source’s pulse period history is updated in Figure 2. Pulse periods from the earlier data, prior to 2008, follow roughly the same spin-up trend as originally seen by Rubin et al. (1997), with the period dropping at a rate of $\sim 0.2 \text{ s yr}^{-1}$. However, our measured pulse periods post-2008 reveal a new spin-down trend of $\sim 0.13 \text{ s yr}^{-1}$. This conclusion is supported by the results of the *Fermi* GBM Pulsar Project (Finger et al. 2009),⁷ which we also include in Figure 2. The pulse shape (see Figure 3) in the 20–40 keV band is dominantly single-peaked; the disappearance of the secondary peak in the $\gtrsim 20 \text{ keV}$ pulse profile has been seen before by Clark et al. (1990) and Robba et al. (2001), who suggested it may be due to the presence of the 22 keV CRSF. The pulse profiles from all observations do not vary significantly from group to group, with the average difference between profiles generally 20% to 50% smaller than the average noise in the profiles. This persists across the torque reversal.

3.2. 4U 1907+09

We began our 4U 1907+09 timing analysis with data from *INTEGRAL* revolution 608, roughly where the *INTEGRAL* analysis of Şahiner et al. (2012) ended. The data were binary

Figure 3. Typical 20–40 keV pulse profile for 4U 1538–522. The average pulse shape is strongly single-peaked in this energy band. This profile is for the first epoch listed in Table 3; the variations between pulse profiles for the different epochs listed are not statistically significant.

corrected according to the parameters determined by in ’t Zand et al. (1998), listed in Table 2. During the time encompassed by our analysis, the source was considerably fainter when compared with previous studies using *INTEGRAL* (Fritz et al. 2006; Şahiner et al. 2012) and was significantly ($\sim 40\%$) dimmer than 4U 1538–522 (compare the 5–100 keV fluxes for 4U 1538–522 in Tables 4 and 5 with the equivalent flux for 4U 1907+09 in Table 6). When epoch folding, no selection of SCWs from the new *INTEGRAL* data produce χ^2 distributions that are comparable with our results for 4U 1538–522 and all error-estimation procedures return errors of $\sim 1 \text{ s}$, compared with $\sim 0.001 \text{ s}$ for 4U 1538–522. As a consistency check, SCWs from *INTEGRAL* revolutions 608 through 623, already reported by Şahiner et al. (2012), were analyzed in the same manner; for this data subset alone, the epoch folding returns a statistically significant result that is consistent with Şahiner et al.’s. We thus do not report any *INTEGRAL*-derived pulse periods for 4U 1907+09 due to the faintness of the source.

4. SPECTRAL ANALYSIS

We extracted ISGRI and JEM-X spectra for 4U 1538–522 and 4U 1907+09 on a SCW-by-SCW basis using the OSA 10.0 software, combining the individual SCW spectra with the `spe_pick` tool provided in the OSA package. The extracted spectra were then modeled in *XSPEC* version 12.7.1 (Arnaud 1996). All error bars are for the 90% single-parameter confidence interval unless otherwise indicated and 5–100 keV model fluxes with 90% error bars were computed using *XSPEC*. The spectra for both sources descend into noise above ~ 50 –80 keV, depending on the particular subset of data being analyzed. Spectra were regrouped to provide roughly similar error bars for data above the noise threshold.

We present spectral fits for two continuum models. The PLCUT model (in *XSPEC*, `POWERLAW*HIGHECUT`) is a piecewise function, with a power law multiplied by a high energy exponential cutoff above some cutoff energy E_{cut} :

$$\text{PLCUT}(E) = \begin{cases} A \times E^{-\Gamma} & E < E_{\text{cut}} \\ A \times E^{-\Gamma} \exp\left(-\frac{E_{\text{cut}} - E}{E_{\text{fold}}}\right) & E \geq E_{\text{cut}}, \end{cases} \quad (1)$$

⁷ Results for 4U 1538–522 can be found at <http://gamma-ray.nsstc.nasa.gov/gbm/science/pulsars>.

Table 4
Spectral Parameters for 4U 1538–522 for 2003–2008 and 2008–2010

Continuum		Early (2003–2008)		Late (2008–2010)	
		POWERLAW	CUTOFFPL+BUMP	POWERLAW	CUTOFFPL+BUMP
Γ		$1.17^{+0.06}_{-0.07}$	$0.7^{+0.2}_{-0.2}$	$1.12^{+0.08}_{-0.14}$	$0.4^{+0.2}_{-0.5}$
Normalization	a	$3.3^{+0.6}_{-0.5}$	$2.2^{+0.8}_{-0.7}$	$2.9^{+0.6}_{-0.7}$	$1.6^{+0.5}_{-0.7}$
5–100 keV flux	b	$6.62^{+0.08}_{-3.36}$	$6.48^{+0.14}_{-0.40}$	$6.3^{+0.2}_{-0.6}$	$6.3^{+0.2}_{-0.5}$
E_{cut}	keV	$14.2^{+1.3}_{-1.0}$	...	14^{+3}_{-2}	...
E_{fold}	keV	14^{+4}_{-2}	13^{+3}_{-2}	$11.7^{+1.3}_{-1.5}$	$9.4^{+1.0}_{-1.6}$
E_{bump}	keV	...	$13.0^{+0.8}_{-0.5}$	...	$13.3^{+1.0}_{-0.8}$
σ_{bump}	keV	...	$1.7^{+0.8}_{-0.3}$	...	1.70 (frozen)
Intensity _{bump}	c	...	$1.4^{+1.3}_{-0.6}$	...	$1.2^{+2.4}_{-0.6}$
E_{c1}	keV	$21.5^{+0.5}_{-0.6}$	$22.0^{+0.6}_{-1.8}$	$21.1^{+0.8}_{-0.8}$	$21.9^{+0.8}_{-3.9}$
σ_{c1}	keV	$3.2^{+0.7}_{-0.6}$	$2.9^{+1.9}_{-1.1}$	$3.8^{+1.4}_{-1.2}$	$3.4^{+5.0}_{-1.2}$
τ_{c1}		$0.48^{+0.11}_{-0.07}$	$0.32^{+0.09}_{-0.08}$	$0.46^{+0.21}_{-0.13}$	$0.38^{+0.11}_{-0.10}$
E_{c2}	keV	50^{+5}_{-4}	50^{+4}_{-3}	...	...
σ_{c2}	keV	8^{+6}_{-3}	8^{+3}_{-2}	...	...
τ_{c2}		$0.8^{+0.6}_{-0.3}$	$1.0^{+0.4}_{-0.3}$	...	...
JEM-X 1 normalization		$0.91^{+0.06}_{-0.06}$	$0.96^{+0.06}_{-0.06}$	$0.96^{+0.11}_{-0.10}$	$0.92^{+0.09}_{-0.09}$
JEM-X 2 normalization		$1.02^{+0.07}_{-0.07}$	$1.07^{+0.07}_{-0.07}$	$1.07^{+0.12}_{-0.11}$	$1.03^{+0.10}_{-0.10}$
χ^2_{red} (dof)		1.175(44)	1.095(43)	0.7277(46)	0.6633(45)

Notes.

^a Units: 10^{-2} photons $\text{cm}^{-2} \text{s}^{-1}$ at 1 keV.

^b Units: 10^{-10} erg $\text{cm}^{-2} \text{s}^{-1}$.

^c Units: 10^{-3} photons $\text{cm}^{-2} \text{s}^{-1}$.

where A is the model flux in $\text{erg cm}^{-2} \text{s}^{-1}$ at 1 keV and E_{fold} is the e -folding energy that turns on at energies higher than the cutoff energy E_{cut} . The CUTOFFPL continuum is PLCUT with the E_{cut} parameter frozen at zero. Since this means the CUTOFFPL spectrum is being exponentially attenuated at all energies, it generally has a significantly lower photon index Γ , but its continuous nature means it lacks the sharp corner that in PLCUT can produce spurious residuals around the cutoff energy. However, CUTOFFPL on its own results in high χ^2 values for spectral fits in some cases, requiring an additional broad Gaussian component to be added to the spectral model. A feature like this at ~ 10 keV has been seen before in both 4U 1538–522 (Coburn 2001) and 4U 1907+09 (Mihara 1995; Coburn 2001; Rivers et al. 2010) as an emission feature, as well as many other HMXBs both with and without cyclotron features (although it occasionally can be modeled as an absorption feature; see, e.g., Müller et al. 2012) and is likely due to the simplistic nature of our continuum models in light of the complex physics of the actual accretion column.

There are two other commonly used continuum models, the Fermi–Dirac cutoff model FDCUT and the two power law NPEX, but neither model was capable of producing a stable fit in either source, generally returning many unconstrained parameters. We did not incorporate any photoelectric absorption, as it is not strongly pronounced at energies above a few keV, we did not include the Fe K line at 6.4 keV (Rodes-Roca et al. 2010) either, as the energy binning needed to obtain usable statistics is too coarse to observe the line.

Both sources exhibit absorption-like features in the ~ 20 and ~ 40 –50 keV range. These are typically identified as CRSFs, and a brief description of the mechanism for their production is presented in Section 5. They typically appear as broad

($\sigma \gtrsim 3$ keV), relatively shallow absorption-like features, usually modeled by multiplicative Gaussians or pseudo-Lorentzians with negative intensity. We use a local XSPEC model, GAUABS, a Gaussian optical depth profile defined by

$$\text{GAUABS}(\tau) = F_0 e^{-\tau(E)} \quad (2)$$

$$\tau(E) = \tau_0 \exp\left(-\frac{(E - E_0)^2}{2\sigma^2}\right). \quad (3)$$

The broad width and shallowness of these lines makes their detection and constraint difficult in the exponentially dropping spectra of HMXBs, especially when it comes to the higher harmonics that lie far above the cutoff energy of the spectrum. In particular, the width of the harmonic was unconstrained in some cases and we opted to fix it at its fitted value when determining errors. In very low-flux datasets, the harmonic CRSF is often not detected.

4.1. 4U 1538–522

4.1.1. Date-selected Spectra

The three year gap in *INTEGRAL* coverage of 4U 1538–522, along with the presence of the torque reversal of late 2008/early 2009, presents an obvious point at which to split the dataset, so we analyze the 2003–2005 and 2008–2010 spectra separately.

Each dataset was fit with the two aforementioned continuum models. Each continuum was modified by one or two Gaussian-profile absorption features and a constant multiplier, which was frozen at unity for the ISGRI spectra and allowed to vary for the JEM-X spectra in order to account for calibration differences between the instruments. The two continuum models provide

Table 5
Spectral Parameters for 4U 1538–522 for Three Luminosity Bins

		High				Mid				Low			
		Early		Late		Early		Late		Early		Late	
		P^a	C^b	P	C	P	CB^c	P	C	P	C	P	C
Continuum													
Γ		$1.07^{+0.10}_{-0.16}$	$0.3^{+0.2}_{-0.2}$	$1.04^{+0.12}_{-0.27}$	$0.4^{+0.2}_{-0.3}$	$1.17^{+0.07}_{-0.07}$	$0.9^{+0.2}_{-0.2}$	$1.06^{+0.09}_{-0.17}$	$0.6^{+0.2}_{-0.2}$	$1.20^{+0.12}_{-0.14}$	$0.2^{+0.2}_{-0.2}$	$1.18^{+0.12}_{-0.14}$	$0.1^{+0.2}_{-0.2}$
Normalization	d	$4.8^{+1.2}_{-1.3}$	$2.1^{+0.6}_{-0.5}$	$4.6^{+1.3}_{-1.6}$	$2.4^{+0.9}_{-0.7}$	$3.7^{+0.7}_{-0.6}$	$3.6^{+1.5}_{-1.1}$	$3.0^{+0.7}_{-0.4}$	$1.8^{+0.7}_{-0.6}$	$1.9^{+0.6}_{-0.5}$	$0.6^{+0.3}_{-0.2}$	$2.1^{+0.8}_{-0.6}$	$0.7^{+0.3}_{-0.2}$
5–100 keV flux	e	$11.4^{+0.2}_{-1.4}$	$11.4^{+0.2}_{-2.8}$	$9.9^{+0.3}_{-2.4}$	$10.1^{+0.2}_{-2.5}$	$7.1^{+0.2}_{-0.4}$	$7.1^{+0.2}_{-1.0}$	8^{+6}_{-2}	$8.3^{+0.3}_{-1.4}$	$3.2^{+0.2}_{-0.4}$	$3.22^{+0.07}_{-0.27}$	$3.9^{+0.3}_{-0.4}$	$4.0^{+0.2}_{-0.7}$
E_{cut}	keV	14^{+2}_{-2}	...	13^{+4}_{-2}	...	$13.8^{+1.8}_{-1.2}$	...	13^{+2}_{-2}	...	22^{+5}_{-4}	...	14^{+7}_{-2}	...
E_{fold}	keV	13^{+2}_{-2}	11^{+2}_{-2}	18^{+4}_{-4}	15^{+3}_{-3}	14^{+2}_{-2}	14^{+4}_{-3}	> 13.0	14^{+4}_{-4}	8^{+2}_{-2}	$8.2^{+1.0}_{-0.8}$	12^{+2}_{-4}	$8.1^{+1.3}_{-1.1}$
E_{bump}	keV	...	...	...	...	...	$12.7^{+1.0}_{-0.6}$	...	...	...	...	...	...
σ_{bump}	keV	...	...	...	...	...	2.03 (frozen)	...	...	...	...	...	...
Intensity _{bump}	f	...	...	...	...	...	$2.6^{+1.0}_{-0.9}$	...	...	...	...	...	...
E_{c1}	keV	$21.2^{+0.6}_{-0.7}$	$22.0^{+0.5}_{-0.4}$	$21.6^{+1.0}_{-1.1}$	$21.9^{+0.9}_{-0.9}$	$21.5^{+0.7}_{-0.7}$	$22.1^{+0.7}_{-0.9}$	$23.1^{+1.1}_{-1.3}$	$24.1^{+1.5}_{-1.3}$	$21.8^{+2.3}_{-1.4}$	$21.3^{+0.8}_{-0.7}$	$21.5^{+1.2}_{-1.1}$	$21.9^{+1.2}_{-1.0}$
σ_{c1}	keV	$3.7^{+1.1}_{-1.1}$	$3.4^{+0.7}_{-0.7}$	$4.0^{+1.5}_{-1.2}$	$3.8^{+1.2}_{-1.0}$	$3.3^{+1.0}_{-0.9}$	$2.8^{+2.1}_{-1.4}$	$5.6^{+1.0}_{-1.6}$	5^{+2}_{-2}	$3.4^{+0.8}_{-0.9}$	$2.2^{+1.1}_{-1.5}$	2^{+3}_{-2}	$1.6^{+1.6}_{-1.4}$
τ_{c1}		$0.56^{+0.22}_{-0.13}$	$0.60^{+0.12}_{-0.13}$	$0.6^{+0.2}_{-0.2}$	$0.6^{+0.2}_{-0.2}$	$0.45^{+0.13}_{-0.11}$	$0.40^{+0.13}_{-0.11}$	$0.6^{+0.2}_{-0.3}$	$0.65^{+0.23}_{-0.10}$	$1.0^{+0.3}_{-0.3}$	$0.6^{+1.2}_{-0.2}$	$0.8^{+7.9}_{-0.4}$	> 0.3
E_{c2}	keV	49^{+4}_{-3}	49^{+4}_{-3}	50^{+8}_{-4}	49^{+7}_{-4}	50^{+4}_{-3}	53^{+4}_{-3}	57^{+6}_{-13}	53^{+4}_{-4}	...	...	...	...
σ_{c2}	keV	8^{+4}_{-3}	10^{+3}_{-4}	15^{+14}_{-4}	16^{+11}_{-4}	8 (frozen)	10 (frozen)	14^{+5}_{-11}	10 (frozen)	...	...	...	...
τ_{c2}		$1.0^{+0.4}_{-0.4}$	$1.1^{+0.4}_{-0.5}$	$1.2^{+1.1}_{-0.5}$	$1.5^{+1.1}_{-0.5}$	$0.6^{+0.2}_{-0.3}$	$1.0^{+0.4}_{-0.4}$	$2.0^{+0.6}_{-1.5}$	$1.8^{+1.4}_{-1.0}$	...	...	...	...
JEM-X 1 normalization		$0.99^{+0.07}_{-0.07}$	$1.01^{+0.10}_{-0.09}$	$0.87^{+0.13}_{-0.12}$	$0.89^{+0.13}_{-0.11}$	$0.99^{+0.10}_{-0.09}$	$0.93^{+0.08}_{-0.08}$	$1.12^{+0.08}_{-0.13}$	$1.14^{+0.14}_{-0.12}$	$0.97^{+0.11}_{-0.10}$	$0.94^{+0.11}_{-0.10}$	$1.0^{+0.2}_{-0.2}$	$1.1^{+0.2}_{-0.2}$
JEM-X 2 normalization		$0.72^{+0.05}_{-0.05}$	$0.73^{+0.07}_{-0.07}$	$0.89^{+0.13}_{-0.13}$	$0.91^{+0.13}_{-0.12}$	$0.93^{+0.10}_{-0.09}$	$0.87^{+0.08}_{-0.08}$	$1.23^{+0.14}_{-0.14}$	$1.25^{+0.15}_{-0.14}$	$1.3^{+0.2}_{-0.2}$	$1.31^{+0.16}_{-0.15}$	$1.1^{+0.2}_{-0.2}$	$1.1^{+0.2}_{-0.2}$
χ^2_{red} (dof)		1.038(54)	1.134(55)	0.7066(50)	0.7644(51)	1.060(46)	1.090(45)	0.8842(50)	0.9487(52)	1.224(41)	1.356(42)	0.4921(41)	0.5870(42)

Notes.

^a PLCUT continuum.

^b CUTOFFPL continuum.

^c CUTOFFPL+BUMP continuum.

^d Units: 10^{-2} photons $\text{cm}^{-2} \text{s}^{-1}$ at 1 keV.

^e Units: 10^{-10} erg $\text{cm}^{-2} \text{s}^{-1}$.

^f Units: 10^{-3} photons $\text{cm}^{-2} \text{s}^{-1}$.

Figure 4. Date-selected counts spectra and models for 4U 1538–522 using the PLCUT continuum. The black points indicate the ISGRI spectrum; the red and green indicate JEM-X 1 and 2, respectively. The left panel displays the earlier dataset, comprising data from 2003 to 2008, with residuals for the PLCUT continuum with, from top to bottom, no CRSFs, one CRSF at ~ 50 keV, and CRSFs at 21.5 keV and 50 keV. The right panel contains the later dataset, spanning the years 2008–2010, and the residuals are for the continuum with no CRSFs (top) and one CRSF at 21.1 keV (bottom).

(A color version of this figure is available in the online journal.)

Table 6
Spectral Parameters for 4U 1907+09

Continuum		POWERLAW	CUTOFFPL+BUMP
Γ		$-0.9^{+0.8}_{-0.8}$	$-1.3^{+1.0}_{-0.7}$
Normalization	a	$0.03^{+0.09}_{-0.02}$	$0.04^{+0.1}_{-0.03}$
5–100 keV flux	b	$2.92^{+0.04}_{-0.31}$	$2.92^{+0.05}_{-0.20}$
E_{cut}	keV	$6.5^{+1.6}_{-2.4}$	...
E_{fold}	keV	$6.2^{+3.8}_{-1.3}$	$5.6^{+17.2}_{-1.2}$
E_{c1}	keV	$18.5^{+0.7}_{-0.7}$	$18.4^{+0.7}_{-0.7}$
σ_{c1}	keV	$3.2^{+1.1}_{-0.8}$	$3.5^{+1.1}_{-0.8}$
τ_{c1}		$0.8^{+0.2}_{-0.2}$	$0.9^{+0.3}_{-0.2}$
E_{c2}	keV	38^{+8}_{-5}	38^{+14}_{-5}
σ_{c2}	keV	8^{+14}_{-6}	9^{+18}_{-5}
τ_{c2}		$1.1^{+5.4}_{-0.8}$	$1.2^{+5.1}_{-0.9}$
JEM-X 1 normalization		$0.95^{+0.13}_{-0.12}$	$0.95^{+0.13}_{-0.12}$
JEM-X 2 normalization		$1.19^{+0.16}_{-0.15}$	$1.19^{+0.16}_{-0.15}$
χ^2_{red} (dof)		0.7774(35)	0.8260(36)

Notes.

^a Units: 10^{-2} photons $\text{cm}^{-2} \text{s}^{-1}$ at 1 keV.

^b Units: 10^{-10} erg $\text{cm}^{-2} \text{s}^{-1}$.

similar χ^2 statistics, with CUTOFFPL+BUMP being slightly superior in most cases. However, when calculating errors, it was necessary to fix the width of the 10 keV feature in the later dataset at the value found in the earlier dataset, as the decreasing sensitivity of the JEM-X telescopes at higher energies, combined with the presence of the CRSF at ~ 22 keV, resulted in unconstrained fit parameters. We will refer primarily to the PLCUT continuum results in our discussion due to this limitation. Neither continuum model shows any significant variation across the torque reversal. We list the parameters for the spectral fits for both continua in Table 4 and the spectra for the PLCUT continuum are plotted in Figure 4.

We clearly detect the fundamental CRSF at $21.5^{+0.5}_{-0.6}$ keV in the early dataset and 21.1 ± 0.8 keV in the late dataset. Adding the feature in the early spectra decreases the χ^2 per degree of freedom (dof) statistic from 327/50 to 70/47,

while in the late dataset, χ^2/dof drops from 84/49 to 33/46. There are no statistically significant differences in the fundamental CRSF across the torque reversal. The harmonic CRSF is much less significantly detected in the early dataset: its addition at 50^{+5}_{-4} keV lowers the χ^2/dof to 52/44. In the later data, the feature is not detected; adding a ~ 50 keV GAUABS component reduces the χ^2 by a negligible amount and generally has unconstrained width and depth, so we leave the feature out of our model for the late data. This non-detection is likely a product of the fact that we are adding together all spectra from after the torque reversal and the lower luminosity observations are driving down the signal-to-noise ratio. This can be more clearly seen in the following section.

4.1.2. Luminosity-selected Spectra

To more closely examine the differences between the earlier and later spectra for 4U 1538–522, we further split the date-selected SCWs into high-, middle-, and low-luminosity bins by taking a 1σ region around the average brightness SCW to be the middle-luminosity bin. The 5–100 keV flux of the source varies by a factor of ~ 3 from the lowest to highest luminosity bin. The best-fit parameters for these datasets for two continuum models are presented in Table 5. Both continuum models again provide roughly similar χ^2 statistics for each dataset. The earlier mid-luminosity bin was the only dataset in the luminosity-selected data that showed a clear need for a 10 keV feature; however, it was necessary to freeze the width of the feature at its fitted value to obtain a stable fit, due to the interaction between the ~ 22 keV CRSF and the “bump.” We additionally froze the width of the harmonic CRSF in all but one model for the mid-luminosity datasets, as a dearth of counts at high energy often led this parameter to be unconstrained. In these cases, we froze the value of the width to the value found in the same model for the corresponding high-luminosity dataset, the exception being the later mid-luminosity spectrum, where the 16 keV width of the later high-luminosity data did not produce a good fit. In that case, the width was frozen to the value found in the earlier high-luminosity data. The harmonic CRSF was not detected in the low-luminosity dataset.

In the PLCUT continuum, E_{fold} is the only parameter showing a significant correlation with luminosity, with a slope of $1.2 \pm 0.8 \text{ keV}/(10^{36} \text{ erg s}^{-1})$ (90% confidence). The correlation is significant at the $p = 0.02$ level. The other spectral parameters generally do not show clearly significant trends; Γ and E_{cut} have slight correlations, but only at the 1σ level. The missing harmonic CRSF is consistent with a lack of statistics at energies above $\sim 40 \text{ keV}$ in the low-luminosity datasets; attempting to fit a line with energy and width frozen at the value from the mid-luminosity bin results in an unbounded depth, and so we do not include the harmonic CRSF in the model for the low-luminosity data.

4.2. 4U 1907+09

The SCWs for 4U 1907+09 are overall more evenly spread throughout *INTEGRAL*'s mission, with no significant changes in pulse period derivative, so there is no logical point in time to define a date-based separation as we have done for 4U 1538–522. The best-fit spectral parameters for all analyzed 4U 1907+09 SCWs are presented in Table 6, with the folded spectrum and model residuals for the PLCUT continuum plotted in Figure 5. Previous analyses (Fritz et al. 2006; Rivers et al. 2010; Şahiner et al. 2012) have been performed using the PLCUT, FDCUT, and NPEX continua, but as is stated in Section 4, we could not obtain useful fits for the latter two. There was no evidence in the residuals for a bump feature at $\sim 13 \text{ keV}$ as has been seen in spectra from, e.g., *Suzaku* (Rivers et al. 2010); an attempt at adding in the feature produced minimal ($\ll 1$) improvements in χ^2 along with very poorly constrained energy, width, and height. Without the feature, the CUTOFFPL continuum produces equally acceptable results compared with the PLCUT continuum.

The addition of the fundamental CRSF at $\sim 18 \text{ keV}$ improves the fit significantly, lowering the χ^2 by ~ 100 . This feature can be seen primarily in the JEM-X residuals, while ISGRI, with its 20 keV lower bound, can only resolve its upper edge. The harmonic is much less significantly detected at $\sim 38 \text{ keV}$, producing a drop of ~ 10 in χ^2 in both models. Adding the harmonic without the fundamental produces a drop of ~ 20 . While the spectrum is already well fit with only one CRSF, we include both in our final models on account of their well-established existence in the literature (Cusumano et al. 1998; Makishima et al. 1999; Fritz et al. 2006; Rivers et al. 2010) and the fact that we are still capable of constraining the harmonic CRSF. Our measurement of the fundamental CRSF is compatible with the measurements by Makishima et al. (1999) and Coburn (2001), which were made using observations of the source at a similar flux, although, as will be discussed in Section 5, Makishima et al.'s measurement was made using a different model for the line, which could make that result inconsistent with ours.

An attempt was made to split 4U 1907+09's spectra into luminosity bins as we did for 4U 1538–522, but the poorer statistics for 4U 1907+09 made this unfeasible, with satisfactory fits only obtained for the brightest luminosity bin. This difficulty is illustrated by the considerably lower 5–100 keV flux of 4U 1907+09 compared with that of 4U 1538–522—the overall flux from the full 4U 1907+09 dataset was $\sim 40\%$ lower than the flux for 4U 1538–522 and was in fact considerably lower than the flux from our lowest-luminosity dataset for 4U 1538–522 (compare Table 6 with Tables 4 and 5).

5. DISCUSSION

5.1. Torque Reversal

Our pulse period measurements for 4U 1538–522 show evidence for a torque reversal in late 2008 or early 2009, although no significant spectral changes are detected that could shed light on a mechanism for this change. Pulse period evolution in accreting neutron stars like 4U 1538–522 is primarily driven by the interaction between the accreting material and the magnetic field of the star. As the field lines are locked into the neutron star, they rotate with the star and the infalling material can exert a torque on the star. Changes in the accretion rate can thus produce changes in the pulse period, but the relationship between accretion rate and torque can be very complex due to the interaction between the accreting material, which may or may not form an accretion disk, and the magnetic field of the neutron star. 4U 1538–522 is primarily a wind-accretor, as the main-sequence companion QV Nor is likely not overfilling its Roche lobe (Reynolds et al. 1992), so it is unlikely that the accreted material comes in with sufficient angular momentum to form a persistent disk, although there may be transient disk formation. However, to our knowledge, no searches for features that might indicate the existence of a transient disk (i.e., a $\sim$ few mHz quasi-periodic oscillation) have been performed.

The wind-accreting nature of the source, while it can explain the short-timescale variations in the pulse period, makes it more difficult to explain the long-term spin-up or spin-down trends observed. The torque reversal in particular is interesting: torque reversals observed in other sources have typically included large shifts in luminosity and/or dramatic spectral shifts (see, e.g., 4U 1626–67; Camero-Arranz et al. 2010). In 4U 1538–522, we see no shift in the X-ray luminosity across the reversal and the spectral parameters generally do not exhibit significant changes. Similar to 4U 1626–67 (Camero-Arranz et al. 2010) and 4U 1907+09 (Inam et al. 2009), the spin-up and spin-down rates on either side of the reversal are similar: $1.4 \times 10^{-14} \text{ Hz s}^{-1}$ for the current spin-down trend, compared with a spin-up of $1.8 \times 10^{-14} \text{ Hz s}^{-1}$ between 1990 and 2009. In the case of 4U 1907+09's most recent torque reversal, Inam et al. suggested that the model of Perna et al. (2006) may be useful as they are able to produce torque reversals without large changes in luminosity or $|\dot{\nu}|$. However, this generally requires an Alfvén radius comparable to the corotation radius of the neutron star to produce the localized propeller effect on which the Perna et al. model relies. 4U 1538–522's slow rotation speed means its $\sim 10^8 \text{ m}$ corotation radius is 1–2 orders of magnitude larger than its Alfvén radius, which is $\sim 4 \times 10^6 \text{ m}$ if spherical accretion is assumed (Lamb et al. 1973), so the recycling mechanism of the Perna et al. model is unlikely to be in effect. Meanwhile, Rubin et al. (1997) modeled 4U 1538–522's spin-up trend from 1991–1995 as simply the consequence of a random walk in the pulse frequency derivative (stemming from a random walk in the accretion torque on the neutron star) and proposed that this alone could be the source of the 1990 reversal, which would allow for the constancy of the system across the reversals. However, the nearly 20 yr spin-up trend clearly indicates that the system is not solely random walking—while for Rubin et al. the expectation value for the frequency shift was within a factor of three of the observed shift, the most recent pulse period measurements are a factor of ~ 8 larger than the expected rms excursion. Without observations tracking the actual torque reversals (as was the case with 4U 1907+09), it is difficult to address the torque reversal in any more depth.

Figure 5. Spectrum of 4U 1907+09 with the best-fitting model, a PLCUT continuum modified by two GAUABS absorption features at 18.5 and 38 keV. The second panel displays the residuals from a pure PLCUT model, the third after only the harmonic CRSF has been added, and the lower panel displays the residuals with both CRSFs.

(A color version of this figure is available in the online journal.)

5.2. Cyclotron Line Variability

We detect absorption-like features, modeled as lines with Gaussian optical depth profiles, at ~ 22 and ~ 50 keV in 4U 1538–522 and ~ 18 and ~ 38 keV in 4U 1907+09, which we identify as CRSFs. These features are produced by the quantization of cyclotron motion in the strong magnetic field of the neutron star—photons with the appropriate energy and momentum to excite an electron into a new Landau level will see an increased scattering cross section. This manifests as a set of absorption-like features produced when photons are scattered out of the line of sight. For magnetic fields of strength $\lesssim 4 \times 10^{13}$ G, the magnetic field strength can be approximated from the energy of the fundamental cyclotron line via the “12-B-12” rule: $E_{\text{cyc}} = (11.57 \text{ keV}) / (1 + z) \times B_{12}$, where z is the gravitational redshift in the scattering region and B_{12} is the magnetic field strength in units of 10^{12} G. If we assume our measured CRSF energies reflect the magnetic field at the stellar surface, this implies a magnetic field strength of $\sim 2.1\text{--}2.3 \times 10^{12}$ G for 4U 1538–522 and 2.0×10^{12} G for 4U 1907+09. Here, we have used masses for 4U 1538–522 of 0.87 ± 0.07 and $1.104 \pm 0.177 M_{\odot}$ as determined by Rawls et al. (2011) and we have assumed a mass of $1.4 M_{\odot}$ for 4U 1907+09. We have assumed a radius of 10 km for both sources.

A more in-depth investigation of the cyclotron line scattering region has been carried out by Becker et al. (2012), who predict

the behavior of the CRSF in response to the luminosity of the source. In the supercritical regime, above the effective Eddington luminosity of the accretion column, they demonstrate that the height of the scattering region should scale with luminosity, producing a negative correlation between CRSF energy and luminosity, as the scattering region moves up into regions of weaker magnetic field. Meanwhile, in subcritical sources, the infalling material comes to a halt via a combination of gas and radiation pressure. An increase in luminosity means less gas pressure is necessary, lowering the scattering region and producing a positive E_{cyc} –luminosity correlation. At even lower luminosity, below the Coulomb stopping limit L_{coul} defined by Becker et al., the sum total gas and radiation pressure does not halt the infalling material before it impacts the star and the scattering should happen at or near the stellar surface. Here, the predicted behavior of the cyclotron line energy is somewhat uncertain, although Becker et al. suggest that there should not be any large correlation of E_{cyc} with luminosity.

Adopting distances of 6.4 kpc for 4U 1538–522 (Reynolds et al. 1992) and 5 kpc for 4U 1907+09 (Cox et al. 2005) and determining the luminosity based on the 5–100 keV flux, we calculated L_{crit} and L_{coul} using Becker et al.’s formulae and found that both sources lie firmly in the subcritical ($L < L_{\text{crit}}$) regime, around or below L_{coul} . The exact location of 4U 1538–522 relative to L_{coul} varies depending on which mass is used: with the very low-mass elliptical result, the measured

Figure 6. Cyclotron line energy vs. luminosity for 4U 1538–522 (top panel) and 4U 1907+09 (bottom). Measurements from this work are represented by asterisks; the values and 90% error bars are taken from models using the PLCUT continuum. Overplotted in the heavy dashed and dot-dashed lines are curves for L_{coul} from Becker et al. (2012); in the top panel, the red heavy dot-dashed line represents L_{coul} for $M_X = 0.87 M_\odot$, while the blue dashed line uses $M_X = 1.104 M_\odot$. Luminosities and values for E_{cyc} from other works are included, along with 90% confidence intervals. Linear fits to the data are also overplotted; due to the systematic differences between Gaussian- and Lorentzian-shaped models for the cyclotron lines, there are two curves for each source: the solid includes only sources that used Gaussian-profile models for the CRSFs, while the dotted line includes Lorentzian-modeled lines (those of Mihara et al. 1998; Clark et al. 1990; Rodes-Roca et al. 2009; Makishima et al. 1999; and Inam et al. 2009) shifted upward by 1.75 keV. (A color version of this figure is available in the online journal.)

luminosities for the source lie mostly above the L_{coul} cutoff, while the higher mass circular solution has the source straddling the L_{coul} line. With no published mass measurements for 4U 1907+09, we assume the canonical neutron star parameters of $M_X = 1.4 M_\odot$ and $R_X = 10$ km, which places the source far below the L_{coul} cutoff. While the value for L_{coul} can vary widely with mass ($L_{\text{coul}} \propto M_X^{11/8}$), unless 4U 1907+09 has a very low mass similar to 4U 1538–522, it is unlikely for it to move above L_{coul} with an updated mass value. Our values for CRSF versus luminosity are plotted against L_{coul} for both sources in Figure 6. To supplement this work’s results, we also include the historical measurements of the energy of the primary CRSF for each source, limited to cases where the luminosity or flux was provided or could be derived from models. Based on our measured luminosity errors, we have assumed an error of 3% for these luminosity values.

Of course, when comparing results from different references, the issue of model choice must be addressed. Several analyses of 4U 1538–522 and 4U 1907+09 used a combination of the NPEX continuum and pseudo-Lorentzian line profiles for the CRSFs. This choice of models results in overall lower measured energies for the cyclotron lines and larger line widths compared with work that used Gaussians or the GAUABS model we have used. A formal treatment of this difference would be beyond the scope of this work: Mihara (1995) provides the analytical expression for the energy of the maximum of the pseudo-Lorentzian model, which one would expect to be close to the measured energy using a symmetric line shape, but the quantity is width-dependent ($E_{\text{max}} = E + W^2/E$) and Müller et al. (2013) point out that the width of the line can vary with the choice of the continuum model (e.g., for 4U 1907+09, Makishima et al. (1999), using NPEX, find a width of ~ 7 keV, while Inam et al. (2009) find widths of ~ 1 –3 keV when they use PLCUT). With this being the case, we opted to simply fit our data with a pseudo-Lorentzian (the CYCLABS model in XSPEC), obtaining values for E_{cl} that

were, on average, 1.75 keV lower than those we found using GAUABS. This is roughly what one would expect using Mihara (1995)’s expression with a width of ~ 6 keV.

To investigate the correlation between luminosity and CRSF energy, we performed linear fits and calculated 90% error bars for the available references for each source; however, due to the systematic uncertainty introduced by correcting for the Lorentzian-modeled points, we defined two datasets for each source: the first only taking into account those results that used Gaussian line profiles similar to this work and the second with the “corrected” Lorentzian-modeled values as well as the Gaussian-modeled lines. The historical data for each source are insufficient to draw any conclusions based on the Lorentzian-modeled data alone. For 4U 1538–522, the Gaussian-modeled data amount to 8 points: the six values from Table 5, along with measurements by Robba et al. (2001) and Coburn (2001). A linear fit to these data finds a slope of -3 ± 18 keV/(10^{37} erg s $^{-1}$), consistent with zero. Pearson’s r for this dataset is -0.4; with six dof; this is consistent with no correlation. If we attempt to include the Lorentzian-modeled points in addition to the Gaussian-modeled points, the size of the applied correction becomes a deciding factor: any correction larger than ~ 1.3 keV results in a negative slope inconsistent with zero, with our +1.75 keV shift resulting in a slope of -7 ± 4 keV/(10^{37} erg s $^{-1}$). Pearson’s r with this correction applied is 0.13, still suggesting no correlation even with the additional data, although this is tempered by the large error bars on several of the data points. For 4U 1907+09, the Gaussian-modeled dataset consists of this work along with the results of Cusumano et al. (1998), Coburn (2001), Fritz et al. (2006), and Rivers et al. (2010). A linear fit to these data produces a positive slope of 4 ± 3 keV/(10^{37} erg s $^{-1}$) and a Pearson’s r of 0.92, indicative of a correlation at the $p = 0.02$ level. However, we should note that this positive slope is dependent to some extent on the measurements of Rivers et al. (2010)—specifically, the higher luminosity measurement of the

CRSF. When that point is excluded from the dataset, Pearson's r is still 0.93, but the slope is no longer significant at the 90% level, returning a value of 3^{+5}_{-6} keV/(10^{37} erg s $^{-1}$). This weakens somewhat any conclusion that 4U 1907+09 definitely has any CRSF–luminosity correlation. The discrepancy in the effect of correcting the Lorentzian-modeled results of Makishima et al. (1999) and Inam et al. (2009) makes the inclusion of these points more suspect than was the case for 4U 1538–522. Nonetheless, including the Lorentzian-modeled points, regardless of whether they are “corrected” upward or not, often still results in a positive slope. Only when the shift is greater than ~ 1.8 keV, or the Rivers et al. (2010) point is excluded, does the slope become consistent with zero.

Considering the possibility of a correlation between CRSF energy and luminosity in 4U 1907+09, it should be noted that a CRSF energy–luminosity correlation at this low of a luminosity has not been seen until now. The only source of comparable luminosity to 4U 1538–522 or 4U 1907+09 with a well-studied luminosity versus cyclotron line energy relationship is A 0535+26 (Caballero et al. 2007), which shows no long-term trend. A 0535+26's positive trend is limited to the pulse-to-pulse analysis by Klochkov et al. (2011), which only covers higher luminosity observations where the source was above L_{coul} .⁸ With 4U 1538–522 and 4U 1907+09 operating at $L \lesssim L_{\text{coul}}$, the potential presence of a correlation is thus rather interesting—while the theoretical predictions for this luminosity regime are still somewhat speculative, the general concept was that at low luminosities, the scattering region would be essentially at the surface of the star, and an increase in luminosity would either do nothing or lift the scattering region up off the surface of the star, producing a negative trend in luminosity versus cyclotron line energy. We see something like this in 4U 1538–522, which potentially has a negative slope in L -versus- E space. However, 4U 1907+09 shows evidence for a positive correlation. This would make 4U 1907+09 the fourth CRSF source to display a positive correlation with luminosity, after Hercules X-1 (Staubert et al. 2007), A 0535+26 (Klochkov et al. 2011), and GX 304–1 (Yamamoto et al. 2011). Hercules X-1 and GX 304–1 have L -versus- E slopes of similar magnitude to 4U 1907+09, but they operate in a distinctly different luminosity regime, at $L_{\text{coul}} < L \lesssim L_{\text{crit}}$. The existence of a correlation in 4U 1907+09 would make the source somewhat of an outlier, with its luminosity sitting as far below L_{coul} and L_{crit} as it is. However, the weakness of the correlation and the low luminosity of the source make a conclusive determination difficult with the quality of data available.

6. SUMMARY

We have presented a spectral and timing analysis of the public *INTEGRAL* data for the HMXBs 4U 1538–522 and 4U 1907+09. Our pulse period measurements for 4U 1538–522 support the *Fermi* GBM pulsar monitoring project's observation of a switch to a spin-down trend starting sometime in 2009, with our measured pulse periods agreeing strongly with their results. The source shows no significant spectral changes between its spin-up and spin-down epochs and its spectrum does not change much between higher and lower luminosities. We update the spectral results for 4U 1907+09 to include the latest public

INTEGRAL data; the results agree with much of the recent work on the source. In both sources, we detect two absorption features, identified as CRSFs. The fundamental CRSF in each source is detected very significantly at ~ 22 and ~ 19 keV in 4U 1538–522 and 4U 1907+09, respectively, with harmonics detected in 4U 1538–522 at ~ 50 keV and in 4U 1907+09 at ~ 38 keV. An examination of our results along with those of past work reveals a possible negative correlation between CRSF energy and luminosity in 4U 1538–522, while 4U 1907+09's CRSF energy–luminosity relationship has evidence for a positive slope, making it the fourth cyclotron line source to display this relationship.

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⁸ The astute reader may note that Reig & Nespoli (2013) also saw evidence for a positive trend in *RXTE*/Proportional Counter Array (PCA) data from A 0535+26's 2009 giant outburst. Nespoli et al. (2013), however, note that this trend was likely in part due to an oversubtraction of the PCA background, reducing the significance of the Reig & Nespoli results.

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