## Ferromagnetism in the Manganese-Indium System

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E recently undertook an investigation of the phase equilibria in the previously unreported manganese-indium system. About twenty-five alloys, varying in manganese content from 3 to 91 weight percent in steps of about 4 weight percent, have been prepared, and over half of these specimens have been found to be ferromagnetic.

The alloys were prepared by melting 40-gram to 70-gram mixtures of the metals under argon in an induction furnace, using a Westinghouse 10-kw rf generator as a source of power. "Triangle RR recrystallized alumina" crucibles (Morgan, England) and alumina-silica thermocouple protective tubes, sealed off at one end with packed magnesia, were used. Indium of 99.97 percent purity was obtained from the Indium Corporation of America and electrolytic manganese of purity greater than 99.9 percent was obtained from the U. S. Bureau of Mines. Chemical analysis showed both materials to be at least 99.9 percent pure. A chromelalumel thermocouple, calibrated at the freezing points of tin, zinc, silver, copper, and copper-silver eutectic alloy, was used in conjunction with a Brown recording potentiometer to obtain the cooling curves of the alloys. All specimens were chemically analyzed to make sure that they were homogeneous and to determine their exact composition.

The existence of ferromagnetism in this system was suggested by Hames and Eppelsheimer, but no data were given. While we have made only qualitative magnetic measurements with a small Alnico magnet, the intensity of magnetization appears to increase regularly from 3 to about 50 weight percent manganese, and then to die out completely. An alloy containing 53.2 percent manganese is strongly ferromagnetic, while one containing 59.4 percent manganese is unaffected by the magnet, as are the subsequent alloys of increasing manganese content. The same range of ferromagnetism holds for alloys annealed and quenched from temperatures between 850 and 950°C. On the basis of these, plus incomplete thermal and metallographic data, we believe the ferromagnetism is due to a single phase, the compound Mn2In. The alloys containing up to 49 percent manganese appear to be composed of indium plus Mn<sub>2</sub>In, no eutectic mixture being formed (the solidus is at the freezing point of indium, 157.5°C).

In a private communication, Dr. R. M. Bozorth has pointed out to us that there are now definitely known about sixteen binary systems, containing no ferromagnetic elements, which show ferromagnetism. Of these binary systems, both components are metals in eight cases. The manganese-indium system described here provides a new additional case.

Thermal and metallographic measurements are being continued, as a thorough knowledge of the phase relations is needed before proceeding to further measurements of magnetic and other properties.

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1 F. A. Hames and D. S. Eppelsheimer, Nature 162, 968 (1948). See also R. R. Grinstead and D. M. Yost, Phys. Rev. 75, 984 (1949) on ferromagnetism in the Mn-Cu-In system.

## Erratum: The Li<sup>6</sup> $(n,\alpha)$ H<sup>3</sup> Reaction Spectrum [Phys. Rev. 81, 475 (1951)]

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THE sentence on lines 10 and 11 of the right-hand side of page 476 in the above article should read, "Deviations from ideal behavior of the whole apparatus are in any case less than 0.3 percent."

## Least-Squares Adjusted Values of the Atomic Constants as of December, 1950

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A S part of the work of the National Research Council Committee on Constants and Conversion Factors of Physics and at the request of its chairman, E. U. Condon, we have prepared a report,1 dated December, 1950, giving a complete re-evaluation of the atomic constants in the light of the wealth of important new and very accurate data obtained since our previous study of January, 1948. As input data we have used the most recent results of Kusch and Prodell<sup>2</sup> on the hydrogen hyperfine shift; of Hipple and his N.B.S. associates<sup>3</sup> and also of Bloch and Jefferies of Stanford4 on the proton cyclotron frequency; of Gardner and Purcell<sup>5</sup> on the electron cyclotron frequency; of Craig and Hoffman<sup>6</sup> (N.B.S.) on the faraday by electrolysis of sodium oxalate; of Bearden and associates on h/e (which latter have recently also been verified at 25 kv at this Institute by the work8 of Gaelen Felt and John Harris); of Birge9 on  $\lambda_g/\lambda_s$  and on N obtained in 1945 from a study of all experimental evidence; of the four independent sources, Hansen and Bol, 10 Bergstrand, 11 Aslakson, 12 and Essen, 13 on the velocity of light; and of Cohen<sup>14</sup> on a re-evaluation of  $R_{\infty}$  in the light of the Lamb shift.

As a result of making a number of trial adjustments, we soon discovered that the new data are likely to lead to observational equations whose observed numerics are not independent but are observationally correlated. If such correlations are ignored, a serious error of method is committed and wrong results<sup>15</sup> are obtained, because the error (or the weight) to attach to each equation cannot then be described by a single number. Instead an error matrix must be used to describe the error situation with all the intercorrelations between equations. The classical procedure for forming the normal equations of least squares no longer applies, but one of us has shown<sup>16</sup> how a generalization in matrix algebra can be used.

A simpler method may be, as we have shown in our report, to recast the equations so as to diagonalize the error and weight matrices, 17 thus removing the correlations between equations. To do this completely, it may be (and in this case was) necessary to transfer some of the observational data from the category of fixed auxiliary constants to that of the unknowns to be adjusted. For this and other more involved reasons discussed in the above report we finally concluded that a solution in the following six unknowns was required: N, e, m, h, c, and  $\lambda_g/\lambda_s$ . The present data permit of setting up, with a diagonalized error matrix, nine observational equations in these six unknowns (including equations for the direct observations on c and  $\lambda_g/\lambda_s$ ) so that the overdetermination is sufficient to yield an index of the presence or absence of systematic errors in the data from a study of the residues. The consistency of the data, so adjusted, is excellent. The somewhat abridged Table I gives the resulting adjusted values of the six primary unknowns and of other useful quantities which can be computed from them, the probable errors being all computed by the ellipsoid method. The adjusted value of  $\lambda_g/\lambda_s$  turns out to be a little lower than our input value, while that for c is a little higher.

These values must still be regarded as tentative, partly because not all of the input data are as yet quite finally settled, and also because the theoretical formula, <sup>18</sup> connecting the hydrogen fine structure shift with Sommerfeld's  $\alpha$ , is not yet known, as regards certain correction terms, <sup>18,19</sup> with the accuracy which the observational data warrant. The Bethe-Longmire correction terms give only "orders of magnitude" and may, according to H. Bethe, have to be modified by many parts in 10<sup>5</sup>. (See  $\Gamma$ -coefficients in Table I). We are also suspicious regarding the magnitude of the higher order corrections giving the electron moment in Bohr magnetons for hydrogen. This ratio is probably Z-dependent, and we are informed