

THE REST-FRAME SUBMILLIMETER SPECTRUM OF HIGH-REDSHIFT, DUSTY, STAR-FORMING GALAXIES

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ABSTRACT

We present the average rest-frame spectrum of high-redshift dusty, star-forming galaxies from 250 – 770 GHz. This spectrum was constructed by stacking ALMA 3 mm spectra of 22 such sources discovered by the South Pole Telescope and spanning $z = 2.0 - 5.7$. In addition to multiple bright spectral features of ¹²CO, [CI], and H₂O, we also detect several faint transitions of ¹³CO, HCN, HNC, HCO⁺, and CN, and use the observed line strengths to characterize the typical properties of the interstellar medium of these high-redshift starburst galaxies. We find that the ¹³CO brightness in these objects is comparable to that of the only other $z > 2$ star-forming galaxy in which ¹³CO has been observed. We show that the emission from the high-critical density molecules HCN, HNC, HCO⁺, and CN is consistent with a warm, dense medium with $T_{\text{kin}} \sim 55$ K and $n_{\text{H}_2} \gtrsim 10^{5.5} \text{ cm}^{-3}$. High molecular hydrogen densities are required to reproduce the observed line ratios, and we demonstrate that alternatives to purely collisional excitation are unlikely to be significant for the bulk of these systems. We quantify the average emission from several species with no individually detected transitions, and find emission from the hydride CH and the linear molecule CCH for the first time at high redshift, indicating that these molecules may be powerful probes of interstellar chemistry in high-redshift systems. These observations represent the first constraints on many molecular species with rest-frame transitions from 0.4 – 1.2 mm in star-forming systems at high redshift, and will be invaluable in making effective use of ALMA in full science operations.

Subject headings: galaxies: high-redshift — galaxies: ISM — galaxies: star formation — ISM: molecules

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1. INTRODUCTION

High redshift, dusty, star-forming galaxies (DSFGs) are a population of luminous ($L_{\text{IR}} > 10^{12}L_{\odot}$), dust-obscured objects undergoing short-lived intense starburst events (e.g., Blain et al. 2002; Lagache et al. 2005). First discovered by the SCUBA instrument on the James Clerk Maxwell Telescope at $850\mu\text{m}$ in the late 1990s (Smail et al. 1997; Barger et al. 1998; Hughes et al. 1998), these distant sources are sufficiently faint to make follow-up study at all wavelengths difficult. Additionally, the large beam sizes of single-dish submillimeter facilities has made the identification of optical or infrared counterparts to the submillimeter sources challenging. Their infrared luminosities imply star formation rates of hundreds to thousands of solar masses per year, making them capable of becoming massive, quiescent galaxies ($M_{*} \sim 10^{11}M_{\odot}$) in only 100 Myr (Hainline et al. 2011; Michałowski et al. 2012; Fu et al. 2013). The space and redshift distributions of these extreme starbursts are clearly important diagnostics of the buildup of structure in the universe, but remain a challenge for current galaxy evolution models (e.g., Baugh et al. 2005; Swinbank et al. 2008; Davé et al. 2010; Hayward et al. 2013). In recent years, a picture has emerged in which the majority of gas-rich galaxies lie along a so-called ‘main sequence’ in stellar mass vs. star formation rate, characterized by star formation in massive, secular disks (e.g., Noeske et al. 2007; Daddi et al. 2010; Tacconi et al. 2010; Elbaz et al. 2011; Hodge et al. 2012). A minority of objects exhibit significantly enhanced star formation rates, and are characterized by star formation triggered by major mergers (e.g., Narayanan et al. 2009; Engel et al. 2010).

Given the challenging nature of follow-up observations, the study of gravitationally lensed starburst systems continues to generate valuable insight into the properties and physics of high-redshift DSFGs. Strong gravitational lensing creates gains in sensitivity or angular resolution which allow much more detailed studies than are possible for otherwise equivalent unlensed systems. Unfortunately, the brightest sub-mm sources have such low number density ($N < 1\text{ deg}^{-2}$ for $S_{850\mu\text{m}} > 100\text{ mJy}$; Negrello et al. 2007) that large area surveys are the only way to build up a statistically significant sample. Large numbers of such objects have recently been uncovered by wide-field sub/millimeter surveys, including those conducted by the South Pole Telescope (SPT; Carlstrom et al. 2011; Vieira et al. 2010; Mocanu et al. 2013) and *Herschel*/SPIRE (Negrello et al. 2010; Wardlow et al. 2013). High-resolution follow-up imaging at $870\mu\text{m}$ has confirmed that these objects are nearly all lensed (Hezaveh et al. 2013; Vieira et al. 2013; Bussmann et al. 2013). Lensed DSFGs offer the best chance to observe these systems for spectral lines which would otherwise be too faint to detect at such great distances, allowing a more detailed characterization of the interstellar medium in these objects.

The prodigious star formation rates of DSFGs require that they contain vast reservoirs of molecular gas ($M_{\text{H}_2} \sim 10^{10}M_{\odot}$; e.g., Greve et al. 2005; Bothwell et al. 2013) from which those stars form. Probing the density, thermodynamic state, and balance of heating and cool-

ing of the interstellar gas then reveals the star-forming conditions in these extreme starbursts. Unfortunately, due to its low mass and lack of a permanent electric dipole moment, direct observations of cold H_2 are difficult. Instead, a suite of molecular and atomic fine structure lines are typically used to diagnose the interstellar medium of galaxies both locally and at high redshift. Carbon monoxide (^{12}CO) is by far the most common molecule observed at millimeter wavelengths in extragalactic objects, due to its high abundance relative to H_2 , ease of excitation, and rotational lines at frequencies of high atmospheric transmission. The ground state rotational line of ^{12}CO (1-0) ($\nu_{\text{rest}} = 115\text{ GHz}$) has been used for decades (e.g., Wilson et al. 1970) as a tracer of the bulk of the molecular gas in the interstellar medium. However, the numerical conversion between gas mass and ^{12}CO luminosity can vary by more than an order of magnitude depending on the metallicity and gas conditions of the galaxy, and the appropriate value for most high-redshift systems is uncertain (e.g., Downes & Solomon 1998; Tacconi et al. 2008; Ivison et al. 2011; Narayanan et al. 2012; Bolatto et al. 2013). Additional consideration of optically thin species, such as ^{13}CO and C^{18}O , may allow for accurate gas mass estimates, if the relative abundances of those species can be estimated.

Due to its low dipole moment ($\sim 0.15\text{ D}$), ^{12}CO rapidly becomes collisionally thermalized at densities of just $n_{\text{H}_2} \sim \text{few} \times 10^2\text{ cm}^{-3}$. Spectral features of other molecules with higher dipole moments, such as HCN, HNC, and HCO^+ , are thought to arise from regions with higher densities ($n_{\text{H}_2} \gtrsim 10^4\text{ cm}^{-3}$) where stars are actively forming (Gao & Solomon 2004). The extreme conditions required for these molecules to be collisionally excited, combined with abundances lower than that of ^{12}CO by multiple orders of magnitude (e.g., Wang et al. 2004; Martín et al. 2006), make their lines faint and observation difficult.

The extremely wide spectral range and high sensitivity of the *Herschel*/SPIRE-FTS instrument (Griffin et al. 2010) have allowed for spectral observations of nearby Ultra-Luminous Infrared Galaxies (ULIRGs) over the entire far-IR wavelength range. In the prototypical ULIRG Arp 220, for example, the ^{12}CO spectral line energy distribution (SLED) is now complete up to $J = 13 - 12$, and dozens of lines of species including [CI], H_2O , HCN, and OH and their ions and/or isotopologues have been seen in emission and absorption (Rangwala et al. 2011; González-Alfonso et al. 2012). With a sufficiently wide range of transitions observed, some degeneracies inherent in excitation modeling can be eliminated, and simple geometric models can be constructed to reproduce all the observed spectral features. Many of these lines can only be observed in local sources from space, making direct comparison between local starbursts and their high- z counterparts challenging.

At high redshift ($z \gtrsim 1$), observations of ^{12}CO and various far-IR fine structure lines have become increasingly common (for a recent review, see Carilli & Walter 2013), with well-sampled CO SLEDs available for an increasing number of objects (e.g., Weiß et al. 2007; Bradford et al. 2009; Riechers et al. 2013). Observations of other molecular species, on the other hand, remain rare due to the

faintness of their lines. Thus far, detections of fainter molecular lines have been largely confined to extraordinarily luminous, highly gravitationally magnified quasar host galaxies, and only four objects have been detected in multiple molecules or isotopes besides ^{12}CO : H1413+117 (the ‘‘Cloverleaf’’ quasar), APM 0827+5255, a highly magnified quasar host, SMM J2135-0102 (the ‘‘Cosmic Eyelash’’), a cluster-lensed ULIRG, and HFLS 3, a *Herschel*-selected starburst at $z = 6.3$. Specific observations of these objects will be discussed in more detail below.

Observations of the interstellar medium of high- z galaxies are being revolutionized with the beginning of science operations by the Atacama Large Millimeter/submillimeter Array (ALMA). In particular, ALMA has already been used in Cycle 0 to conduct a blind ^{12}CO -based redshift survey of 26 high- z star-forming galaxies (Vieira et al. 2013; Weiß et al. 2013), with spectral features seen in $\sim 90\%$ of the sample. Such redshift searches operate by scanning through large swaths of frequency space looking for bright lines of ^{12}CO , [CI], and/or H_2O . As a byproduct, they also offer the opportunity to detect emission from a variety of species whose transitions lie in and amongst the brighter lines. In contrast to previous, narrow-bandwidth targeted studies of specific transitions, blind redshift searches offer information on *all* transitions which fall within the rest-frame frequency range observed, allowing future follow-up observations to focus on detectable species.

Here, we present the detection and analysis of several lines of ^{13}CO , HCN, HNC, HCO^+ , and the CN radical in a stacked spectrum of 22 gravitationally lensed DSFGs spanning $z = 2 - 5.7$ discovered by the SPT. The stacked spectrum was created utilizing the ALMA 3 mm spectra obtained as part of the blind redshift search presented in Weiß et al. (2013), and spans 250–770 GHz (0.39–1.2 mm) in the rest frame. This stacked spectrum represents a first attempt at quantifying the relative strengths of a host of faint lines in high-redshift DSFGs and addresses the typical ISM conditions which give rise to such lines.

The paper is organized as follows: in §2, we briefly describe the sample selection and observations used in the construction of the stacked spectrum. In §3, we describe the method used to scale and stack the spectra of individual objects. We present the combined spectrum and analyze the average conditions of the ISM in these objects in §4, and conclude by comparing our derived properties to those of other high-redshift systems, constraining the average emission from individually undetected molecules, and discussing alternatives to pure collisional excitation in §5. Throughout this work we adopt a WMAP9 cosmology, with $(\Omega_m, \Omega_\Lambda, H_0) = (0.286, 0.713, 69.3 \text{ km s}^{-1} \text{ Mpc}^{-1})$ (Hinshaw et al. 2012).

2. DATA AND OBSERVATIONS

Extensive details of our target selection and ALMA 3 mm observations are given in Weiß et al. (2013). Briefly, we selected 26 bright ($S_{1.4\text{mm}} \gtrsim 20 \text{ mJy}$) point sources from the first 1300 deg^2 of the SPT Sunyaev-Zel’dovich effect survey (Vieira et al. 2010; Mocanu et al. 2013). These sources showed thermal, dust-like spectral indices between 1.4 and 2 mm and had no counterparts in existing radio and/or far-IR catalogs, which ruled out synchrotron-dominated sources and low-

redshift contaminants. The sources were required to have been detected with the Large Apex Bolometer Camera (LABOCA) at $870 \mu\text{m}$ or the Submillimeter Array (SMA) at 1.3 mm to refine their positions. Due to their extreme brightness, most of the sources were suspected to be gravitationally lensed by intervening massive galaxies, groups, or clusters (Negrello et al. 2007). This hypothesis was confirmed using high-resolution ALMA $870 \mu\text{m}$ observations (Hezaveh et al. 2013; Vieira et al. 2013), which show magnification factors $\mu = 5 - 20$. The sample is not strictly 1.4 mm flux density limited due to observational constraints, but it does constitute a representative sample of SPT sources which meet the selection criteria. The sources span redshift $z = 2.01 - 5.70$, apparent infrared luminosity $L_{\text{IR}} = 5.5 - 158 \times 10^{12} L_\odot$ (integrated from $8 - 1000 \mu\text{m}$), and dust temperature $T_d = 20 - 50 \text{ K}$, with medians of $\langle z \rangle = 3.5$, $\langle L_{\text{IR}} \rangle = 4.2 \times 10^{13} L_\odot$, and $\langle T_d \rangle = 37 \text{ K}$.

The ALMA observations were carried out during Cycle 0 in November 2011 and January 2012 with a compact configuration of the 14–17 antennas available at the time. The data comprise a spectral sweep of the 3 mm band (Band 3; Claude et al. 2008), using five tunings of the ALMA receivers to cover 84.2–114.9 GHz. Each target was observed for roughly 120 s per tuning, or a total of ~ 10 min per source. Data were calibrated in the standard way using the Common Astronomy Software Applications package (McMullin et al. 2007; Petry et al. 2012). Of the 26 targets, redshifts for 18 were unambiguously determined either from the ALMA data alone or in conjunction with additional observations from APEX, ATCA, or VLT; an additional 5 showed a single spectral feature, narrowing the redshift to two or three possible options. The final three sources showed no lines in their 3 mm spectra.

Following publication of Weiß et al. (2013), two additional single-line sources have had their redshifts confirmed – the redshift of SPT 0125-50 has been confirmed at $z = 3.9592$ by the detection of the ground state 1670 GHz water transition at 336.8 GHz in high-resolution ALMA $870 \mu\text{m}$ data (Appendix A), and the redshift of SPT 0512-59 has been confirmed as $z = 2.2334$ by the detection of [CII] by *Herschel*/SPIRE (Gullberg et al., in prep.), leaving just three sources with multiple redshift options and three sources with no redshift constraint. For the purposes of this stacking analysis, we include all sources with confirmed redshift, as well as those sources for which a single redshift option is more than 60% probable (Weiß et al. 2013, their Fig. 4). The inclusion or exclusion of the sources with ambiguous redshift does not significantly affect our conclusions, and their inclusion is not required for the detection of any faint spectral features. Conversely, the stacked spectrum and ALMA spectra of the single-line sources are not yet sensitive enough to constrain the redshifts of these sources using the combined constraints of many faint, undetected lines. The full list of sources included in this study is given in Table 1.

In order to stack and combine the spectra from multiple sources in a statistically robust manner, we must retain an estimate of the flux density uncertainty in each channel of the source spectra. We fit a point source to the calibrated visibilities of each channel of each source,

Table 1
Source Properties

Source Name	z	T_d (K)	Scaled $S_{350\ \mu\text{m}}$ (mJy)	Scaled $S_{21\ \mu\text{m}}$ (mJy)
SPT0452-50	2.0104	21	11.7	0.0
SPT0551-50	2.1232	27	18.2	0.1
SPT0512-59	2.2334 ^a	34	19.5	0.8
SPT0125-47	2.5148	41	33.5	13.2
SPT2134-50	2.7799	41	18.8	9.9
SPT0103-45	3.0917	34	22.2	0.1
SPT0550-53	3.1286 ^b	32	9.0	1.1
SPT0529-54	3.3689	32	20.7	0.1
SPT0532-50	3.3988	36	34.0	2.9
SPT0300-46	3.5956 ^b	39	12.3	0.4
SPT2147-50	3.7602	42	9.4	1.4
SPT0125-50	3.9592 ^a	44	16.5	17.7
SPT0418-47	4.2248	54	9.6	6.6
SPT0113-46	4.2328	33	13.2	0.0
SPT0345-47	4.2958	53	13.5	33.9
SPT2103-60	4.4357	39	10.7	0.7
SPT0441-46	4.4771	40	11.8	2.1
SPT2146-55	4.5672	40	10.0	3.6
SPT2132-58	4.7677	39	11.3	3.7
SPT0459-59	4.7993	37	10.1	3.6
SPT0346-52	5.6559	53	17.3	35.9
SPT0243-49	5.6990	32	18.1	1.1

Note. — Fluxes derived by scaling continuum SEDs for each source to $z = 3$ using Equation 1 (§3) before measuring the flux at rest-frame 350 and 21 μm (observed-frame 1.4 mm and 84 μm). The observed-frame 1.4 mm fluxes are used to scale the spectra of individual sources; 21 μm fluxes will be used in §5.3 to test the effect of the mid-infrared radiation field on the observed line ratios.

^a Redshift confirmed since publication of Weiß et al. (2013)

^b Most likely redshift of two possible options

using the uncertainty from this fitting procedure as an estimate of the noise in each channel. We see no signs of non-point-like structure in the calibrated continuum images, as expected at the spatial resolution ($> 4''$) of the ALMA 3 mm data. Since the sources are generally undetected in any given single channel, we fix the source position to that determined from the continuum image of all channels, where every source is robustly detected. Typical noise levels are ~ 1.5 mJy in 45 MHz channels, increasing to ~ 2.5 mJy at the high frequency edge of the ALMA bandpass as the atmospheric transmission declines. Noise levels are roughly $\sqrt{2}$ lower in the frequency range from 96.2–102.8 GHz, which was covered twice in our tuning scheme. The data were acquired with the ALMA correlator configured for 3840 channels per 2 GHz baseband. The resulting spectral resolution, ~ 1.5 km/s, is much higher than a typical galaxy line width (\sim hundreds of km/s), allowing us to average channels to increase significance.

3. STACKING METHODS

The composite spectrum is constructed from individual source spectra that are shifted in redshift and scaled to a common millimeter flux density. This is not the scaling that optimizes the S/N of the stacked spectrum, but it provides a more representative average of the wide distribution of line strengths seen in individual sources at a small cost in the final noise level.

To create the average DSFG spectrum, we begin by removing a first-order polynomial continuum from the

spectrum of each source, excluding channels with significant line emission (defined as channels with signal-to-noise ratios $S/N > 3$). We then re-scale all spectra to a common redshift, $z_{\text{common}} = 3.0$. The multiplicative scaling factor to the channel flux densities and uncertainties of each source which preserves the luminosity per unit bandwidth is

$$\left(\frac{D_L(z_{\text{source}})}{D_L(z_{\text{common}})} \right)^2 \frac{1 + z_{\text{common}}}{1 + z_{\text{source}}}, \quad (1)$$

where D_L is the luminosity distance to the original and common redshifts of each source. The choice to scale to $z = 3$ is intended to be representative of the typical redshift of DSFGs – Chapman et al. (2005) find $\langle z \rangle = 2.3$, while the redshift distribution of the sources presented here implies $\langle z \rangle = 3.5$.

We also normalize the flux density and uncertainty of each source by the 1.4 mm flux density it would have were it located at z_{common} . Because the sources have are being shifted to $z = 3$, the 1.4 mm flux densities are taken from fits to the continuum SED of each source. The dust continuum is represented by a single-temperature modified blackbody, with $\beta = 2$ and λ_0 , the wavelength at which the dust opacity is unity, fixed to 100 μm (Draine 2006). Additionally, we exclude photometric points at $\lambda_{\text{rest}} < 50\ \mu\text{m}$, as in Greve et al. (2012), because the single-temperature SED fits we use below are inappropriate at such short wavelengths, where relatively warm dust contributes significantly. The ALMA spectra are then multiplied by the factor that converts the fitted 1.4 mm (rest-frame 350 μm) flux density to a common $S_{1.4\ \text{mm}} = 15$ mJy, approximately the average brightness of the SPT sources were they all located at $z = 3$. After scaling each source to $z = 3$, DSFGs with scaled $S_{1.4\ \text{mm}} = 15$ mJy will have their ALMA flux densities unchanged, while sources fainter (brighter) than this will have their flux densities scaled proportionally higher (lower). Due to the well-known submillimeter “negative k -correction” (Blain & Longair 1993), the SPT observed and redshift-scaled 1.4 mm flux densities are nearly identical for most sources. The sources with the largest difference between observed and scaled 1.4 mm flux density are those located at the highest redshifts, where the dust opacity even at observed-frame 1.4 mm is no longer negligible. It is these sources which lower the average scaled 1.4 mm flux density to ~ 15 mJy from the observed average of ~ 20 mJy. The choice of “reference” wavelength has little effect on the results of our stacking; nearly identical results are obtained referencing to 850 μm in analogy to samples discovered by SCUBA or LABOCA.

The decision to normalize the ALMA spectra by a scaled version of the sources’ millimeter flux density is by no means unique – a variety of source properties could conceivably be used for normalization, including apparent L_{IR} , ^{12}CO line luminosity, or dust mass. The line ratios derived from these various weighting schemes are relatively robust to which quantity is used for normalization, with the majority of average line ratios agreeing to within 15% regardless of normalization choice. We choose to normalize by the scaled 1.4 mm flux density of each source as the SPT sources were selected at this wavelength.

To create a composite “template” spectrum of the SPT

DSFGs, we interpolate the spectrum of each source onto a grid spanning 240–780 GHz, the rest frequencies probed by the ALMA spectra given the redshift distribution of our sources ($z = 2.01 - 5.70$). The grid is constructed with 500 km/s spacing, which roughly corresponds to the typical full-width at half-maximum (FWHM) of the observed ^{12}CO lines. We then perform a weighted average of all sources which contribute to a given output channel, with weights determined as the inverse variance in each channel. Due to the changing number of sources which contribute at each rest frequency (ranging from two to 13), the re-scaling of each spectrum, and the noise properties of the original spectra, the noise level of the composite spectrum varies from approximately 0.11 to 1.5 mJy in each 500 km/s output channel, except in the extreme edges of the band where single sources alone remain (see Figure 2).

The template spectrum is an imperfect tool for the detection of faint lines because its regular channel grid necessarily splits the flux of most lines between multiple channels, reducing their significance. A cleaner assessment of the presence or absence of spectral features can be obtained by constructing spectra centered at the rest frequencies of potentially-detectable ISM lines. To construct these spectra, we extract the spectrum of every source that samples the line of interest in very wide 600 km/s channels centered on the target line. A constant continuum level is estimated and subtracted from each source before stacking, excluding the central 0 km/s channel and any other channels which also potentially contain other faint lines. The wide 600 km/s channel width was chosen to match the typical ^{12}CO line widths of our sources, $\langle\text{FWHM}\rangle \sim 450$ km/s. For a perfectly Gaussian line of $\text{FWHM} = 450$ km/s, a channel of 600 km/s centered at the rest frequency of the line contains $\gtrsim 90\%$ of the total line flux. This choice assumes that the widths of all lines will be roughly equivalent to the widths of ^{12}CO , but faint transitions, especially those with high critical densities, frequently show narrower line widths than ^{12}CO (e.g., Weiß et al. 2007). With 600 km/s channelization, therefore, essentially all flux from narrower lines will be contained within a single channel. The significance of the detection or non-detection of each line can then be interpreted easily based on the flux and noise properties of the central 0 km/s channel. When applied to the stacked bright ^{12}CO lines themselves, this channelization indeed recovers $\sim 90\%$ of the total integrated flux in the channel centered on the rest frequency of each line, suggesting that this chosen width is an acceptable compromise between including as much line flux as possible while excluding excess noise. We classify a line as detected if the line flux in the 0 km/s channel has $S/N > 3$.

This procedure is complicated by those species with fine and/or hyperfine structure components which are too close together to be separated, the most relevant of which is the cyanide radical CN. For these molecules, we choose the main fine structure component as the rest frequency of the line, using spectroscopic data from the JPL (Pickett et al. 1998) and CDMS (Müller et al. 2001, 2005) line catalogs. CN presents an additional complication in its $N = 4 - 3$ lines, the strongest components of which are separated by less than a typical FWHM

(~ 90 and 220 km/s) from the nearby $\text{HNC}(J = 5 - 4)$ line. These lines are blended in two adjacent 600 km/s channels. To attempt to separate them, we use the line ratio derived from the only high-redshift observation of this pair of lines, in the APM 0827+5255 quasar (Guélin et al. 2007). We assign line flux in accordance with that ratio (36% and 64% for CN(4-3) and HNC(5-4), respectively), and include an additional 33% uncertainty in the derived line fluxes.

To ensure that the stacking method does not introduce a spurious line where none exists, we use a Monte Carlo procedure to characterize the statistical properties of the stacked spectrum at a line-free frequency, 513 GHz. For each source that covers this rest-frame frequency, we extract spectra in 600 km/s channels within ± 4500 km/s. In 3000 trials, we randomly shuffle the channels of each input spectrum, then scale, normalize, and average. The flux in each channel is not altered, but the placement of the channels is randomized such that emission originally located in the 0 km/s channel may now be located in any other channel. We then stack the spectra as usual and bin the signal-to-noise (S/N) distribution of the resulting stacked channels from the entire ± 4500 km/s velocity range. This channel distribution is shown in Fig. 1, which indicates that the noise properties of the stacked spectra are well-represented by Gaussian statistics. The probability of falsely finding a stacked line with $|S/N| > 3$ is therefore very small; we expect < 0.3 false detections in the ~ 100 line frequencies we search.

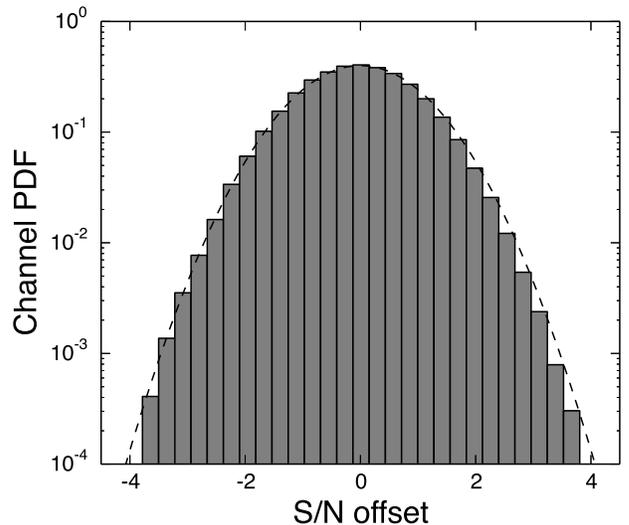


Figure 1. Testing the statistical properties of the stacking procedure. Shown is the signal-to-noise distribution of channels in the stacked spectrum near rest-frame 513 GHz, where no line is expected. The channels of the individual source spectra included in the stack were randomized before stacking, 3000 trials were used. The dashed line indicates a unit-width Gaussian distribution. The normal distribution of these channels indicates that the statistics of the stack are well-described by a Gaussian distribution with the width specified by the assumed noise level.

4. RESULTS

We show the average 250–770 GHz spectrum of the SPT DSFGs in Fig. 2, with a sample of detected and potentially-detectable ISM lines marked. A summary of the detected lines and an assortment of upper limits is

given in Table 2. This table is not intended to be an exhaustive list of useful ISM diagnostics, but rather gives a host of lines in our bandpass that may be detected in high-redshift starbursts by ALMA in the future. In addition to the ^{12}CO lines from $J = 3 - 2$ to $J = 6 - 5$, we also detect two lines each of ^{13}CO , CN, HNC, and HCO^+ , and a single line of HCN. While, as mentioned in §3, the composite spectrum cannot strictly be used to discern the strength of a faint line, all visually apparent lines are accounted for in Table 2, and no obvious lines remain unidentified. To extend the observed ^{12}CO SLED to low J , we include in Table 2 the average ^{12}CO (1–0) and ^{12}CO (2–1) luminosities of these sources as observed by the Australia Telescope Compact Array (ATCA) and reported in Aravena et al. (2013) and forthcoming papers.

Below, we analyze and discuss the detected lines in more detail. Where applicable, we use the radiative transfer code RADEX (van der Tak et al. 2007) to constrain the average ISM conditions in these galaxies. RADEX iteratively solves for the line emission and level populations of a given molecule using the escape probability formalism, and provides results comparable to Large Velocity Gradient (LVG) codes. All models use collisional rate coefficients from the LAMDA database (Schöier et al. 2005) and are carried out for the geometry of an expanding sphere. Since absolute line luminosities are proportional to the common redshift and value of $S_{1.4\text{mm}}$ chosen as a reference, we carry out our analysis using only line ratios, with the understanding that the line luminosities given in Table 2 should be taken as relative to a source with $S_{1.4\text{mm}} = 15\text{ mJy}$ at $z = 3$. For typical dust continuum SEDs of the SPT sources, this corresponds to an apparent $L_{\text{IR}} \sim 4 \times 10^{13} L_{\odot}$, with L_{IR} integrated from $8 - 1000\ \mu\text{m}$. Typical magnifications range from $\mu = 5 - 20$ (Hezaveh et al. 2013).

The results of this line excitation modeling should be viewed with caution, given the varying number of sources which contribute to each line. With a typical bandwidth of $\sim 130\text{ GHz}$ in the rest frame, at most two lines each of ^{12}CO , ^{13}CO , HCN, HNC, CN, or HCO^+ can appear in the spectrum of any given source. Thus, lines of the same molecule with $\Delta J_{\text{up}} \geq 2$ can have no contributing sources in common. Additionally, the averaging of spectra of many galaxies with varied gas conditions may distort the observed line ratios such that typical gas properties are unrecoverable. However, we show in Appendix B that conditions representative of the input conditions are recovered, subject to the degeneracies inherent in large velocity gradient modeling. Differential magnification, in which different spectral lines are magnified by different amounts, could also skew the averaged line ratios. However, a detailed accounting of the effects of differential magnification would require knowledge of the filling fractions of gas emitting in each transition and the lensing geometry of our sources, which is beyond the scope of this paper. The quantities derived from the radiative transfer modeling are intended to be representative of the gas conditions which give rise to the observed lines. Significant uncertainty in properties of the molecular gas will remain as a result of the limited sample size, the variation of fluxes between sources, and the limited number of species and transitions detected. Gas conditions de-

rived from ^{12}CO transitions in individual sources will be presented in a future publication.

4.1. ^{12}CO and its Isotopologues

4.1.1. ^{12}CO SLED

Figure 3 shows the composite ^{12}CO SLED in comparison to the well-sampled SLEDs of quasar H1413+117 ($z = 2.56$, apparent $L_{\text{IR}} = 2.4 \times 10^{13} L_{\odot}$; Barvainis et al. 1994), SMM J2135-0102 ($z = 2.32$, apparent $L_{\text{IR}} = 3.8 \times 10^{13} L_{\odot}$; Swinbank et al. 2010), and quasar APM 0827+5255 ($z = 3.91$, apparent $L_{\text{IR}} \sim 10^{15} L_{\odot}$; Egami et al. 2000). We also show the average SLED found by Bothwell et al. (2013) in a sample of (almost all unlensed) DSFGs selected at $850\ \mu\text{m}$ by SCUBA with optical or mid-IR spectroscopic redshifts. The average SLEDs of both DSFG samples are clearly less excited than those of either high- z QSO host, with the DSFG samples showing an apparent flattening or turnover near $J = 5$ similar to local starburst galaxies M82 or NGC253 (Panuzzo et al. 2010; Bradford et al. 2003). Weiß et al. (2007) and Danielson et al. (2011) use well-characterized (up to and beyond $J = 10 - 9$) ^{12}CO SLEDs of APM 0827+5255 and SMM J2135-0102, respectively, to demonstrate multiphase interstellar media in those objects, while Bradford et al. (2009) find that the ISM of H1413+117 is well represented by a single, high-excitation gas component. As our spectrum covers only six lines (or five line ratios) of ^{12}CO , none of which are clearly beyond the peak of the CO SLED, we postpone a discussion of excitation modeling in our objects until observations of ^{13}CO are added, below.

4.1.2. ^{13}CO and C^{18}O

Observations of ^{12}CO are frequently difficult to interpret because the high relative abundance of ^{12}CO molecules and low electric dipole moment cause the lines to become optically thick even at moderate densities ($n_{\text{H}_2} \lesssim 10^3\text{ cm}^{-3}$). Observations of the less abundant isotopologues ^{13}CO and C^{18}O are thus useful, as these lines are frequently optically thin and the line strengths are then proportional to the total molecular column density. For high-redshift objects, observations of ^{13}CO are also interesting due to the different formation mechanisms of the carbon and oxygen isotopes. While ^{12}C nuclei are produced during He burning in high-mass stars on rapid timescales, ^{13}C nuclei are “secondary,” formed from ^{12}C seed nuclei in intermediate-mass stars undergoing CNO cycle burning, at ages of $\gtrsim 1\text{ Gyr}$ (Wilson & Rood 1994). The formation of ^{18}O is less well understood, but the clearest route is also via a branch of the CNO cycle apparently most pronounced in massive stars, causing ^{18}O -bearing species to be enhanced in galaxies with recent massive star formation (e.g., Henkel & Mauersberger 1993). Identification of ^{13}C -bearing species could be used as a type of nucleosynthesis chronometer, since the interstellar medium must be enriched by the metals from previous generations of stars for the species to be present. At high redshift, then, the $^{12}\text{CO}/^{13}\text{CO}$ line ratio could be large, since relatively little time will have passed for young starbursts to generate ^{13}C nuclei and disperse them back into the interstellar medium (Hughes et al. 2008; Henkel et al. 2010).

Table 2
Spectral Line Properties

Line	ν_{rest} (GHz)	N_{sources}	L' (10^9 K km/s pc 2)	Line	ν_{rest} (GHz)	N_{sources}	L' (10^9 K km/s pc 2)
CO(1-0) ^a	115.2712	5	296.6 ± 16.5	CH 536	536.7614	10	9.6 ± 4.8
CO(2-1) ^a	230.5380	10	329.0 ± 12.9	OH 425	425.0363	8	-1.7 ± 2.9
CO(3-2)	345.7960	6	256.9 ± 10.2	OH 446	446.2910	10	5.0 ± 2.8
CO(4-3)	461.0408	12	179.1 ± 9.3	CN(N = 3 - 2)	340.2478	5	11.4 ± 3.5
CO(5-4)	576.2679	10	199.8 ± 16.8	CN(N = 4 - 3)	453.6067	10	9.1 ± 2.9
CO(6-5)	691.4731	2	136.3 ± 30.4	CN(N = 5 - 4)	566.9470	11	6.0 ± 5.2
¹³ CO(3-2)	330.5880	5	12.8 ± 3.6	CN(N = 6 - 5)	680.2641	2	-16.4 ± 6.0
¹³ CO(4-3)	440.7652	9	12.6 ± 3.0	SiO(7-6)	303.9270	4	-2.6 ± 4.0
¹³ CO(5-4)	550.9263	9	2.8 ± 5.8	SiO(8-7)	347.3306	6	-5.1 ± 3.6
¹³ CO(6-5)	661.0673	4	6.3 ± 5.9	SiO(9-8)	390.7284	7	-4.9 ± 4.0
C ¹⁸ O(3-2)	329.3305	5	1.4 ± 3.8	SiO(10-9)	434.1196	8	-0.0 ± 2.8
C ¹⁸ O(4-3)	439.0888	7	-6.0 ± 4.5	SiO(11-10)	477.5031	11	-3.4 ± 3.8
C ¹⁸ O(5-4)	548.8310	9	6.1 ± 5.5	SiO(12-11)	520.8782	11	8.8 ± 5.3
C ¹⁸ O(6-5)	658.5533	4	11.8 ± 6.1	SiO(13-12)	564.2440	11	-7.7 ± 5.3
[C I](1-0)	492.1606	13	47.5 ± 3.7	SiO(14-13)	607.5994	8	2.2 ± 6.6
HCN(3-2)	265.8864	2	-14.2 ± 10.1	SiO(15-14)	650.9436	4	-10.8 ± 6.0
HCN(4-3)	354.5055	6	13.4 ± 3.2	SiO(16-15)	694.2754	2	9.8 ± 9.8
HCN(5-4)	443.1161	9	4.4 ± 2.8	SiO(17-16)	737.5939	2	-5.4 ± 9.5
HCN(6-5)	531.7164	10	3.9 ± 5.0	CS(6-5)	293.9122	3	1.3 ± 6.0
HCN(7-6)	620.3040	7	7.2 ± 7.0	CS(7-6)	342.8830	5	1.2 ± 3.4
HCN(8-7)	708.8770	2	25.7 ± 10.2	CS(8-7)	391.8470	7	2.7 ± 3.7
HNC(3-2)	271.9811	3	2.2 ± 8.5	CS(10-9)	489.7510	13	-5.9 ± 3.5
HNC(4-3)	362.6303	5	16.2 ± 4.2	CS(11-10)	538.6888	10	-2.4 ± 5.4
HNC(5-4)	453.2699	10	15.6 ± 4.3	CS(12-11)	587.6162	10	9.5 ± 5.4
HNC(6-5)	543.8976	10	12.8 ± 5.1	CS(13-12)	636.5318	5	15.4 ± 9.0
HNC(7-6)	634.5108	5	-4.4 ± 10.2	CS(14-13)	685.4348	2	-1.1 ± 7.6
HNC(8-7)	725.1073	2	-3.2 ± 9.1	CS(15-14)	734.3240	2	1.3 ± 9.3
HCO ⁺ (3-2)	267.5576	2	8.5 ± 9.5	NH ₃ (1 ₀ -0 ₀)	572.4982	10	5.4 ± 5.9
HCO ⁺ (4-3)	356.7342	6	11.7 ± 3.2	N ₂ H ⁺ (3-2)	279.5117	2	-22.2 ± 10.7
HCO ⁺ (5-4)	445.9029	10	3.0 ± 2.8	N ₂ H ⁺ (4-3)	372.6725	5	-1.8 ± 3.6
HCO ⁺ (6-5)	535.0616	10	22.6 ± 4.8	N ₂ H ⁺ (5-4)	465.8250	10	0.8 ± 3.3
HCO ⁺ (7-6)	624.2085	7	16.0 ± 7.6	N ₂ H ⁺ (6-5)	558.9667	9	1.6 ± 5.2
HCO ⁺ (8-7)	713.3414	2	7.7 ± 10.4	N ₂ H ⁺ (7-6)	652.0959	4	-3.8 ± 6.0
H ₂ O(5 _{1,5} -4 _{2,2})	325.1529	5	-0.6 ± 3.8	N ₂ H ⁺ (8-7)	745.2103	2	9.0 ± 9.8
H ₂ O(4 _{1,4} -3 _{2,1})	380.1974	6	7.0 ± 3.4	CCH(3-2)	262.0042	1	38.1 ± 19.3
H ₂ O(4 _{2,3} -3 _{3,0})	448.0011	10	-2.0 ± 2.8	CCH(4-3)	349.3387	6	7.2 ± 3.3
H ₂ O(5 _{3,3} -4 _{4,0})	474.6891	12	8.2 ± 3.9	CCH(5-4)	436.6604	7	5.0 ± 2.9
H ₂ O(1 _{1,0} -1 _{0,1})	556.9360	9	-15.5 ± 5.4	CCH(6-5)	523.9704	11	13.9 ± 5.2
H ₂ O(2 _{1,1} -2 _{0,2})	752.0331	2	31.4 ± 8.8	CCH(7-6)	611.2650	7	14.2 ± 6.7
H ₂ O ⁺ 604	604.6786	8	-5.7 ± 6.7	CCH(8-7)	698.5416	2	-4.0 ± 10.5
H ₂ O ⁺ 607	607.2273	8	2.0 ± 6.5	H21 α	662.4042	4	-4.4 ± 6.1
H ₂ O ⁺ 631	631.7241	5	6.7 ± 8.4	H22 α	577.8964	10	-0.8 ± 5.5
H ₂ O ⁺ 634	634.2729	5	3.9 ± 8.6	H23 α	507.1755	11	-6.1 ± 5.4
H ₂ O ⁺ 721	721.9274	2	7.3 ± 9.2	H24 α	447.5403	10	0.8 ± 2.8
H ₂ O ⁺ 742	742.1090	2	29.3 ± 8.9	H25 α	396.9008	7	-3.8 ± 3.5
H ₂ O ⁺ 746	746.5417	2	21.8 ± 8.2	H26 α	353.6227	6	-1.0 ± 3.2
H ₂ O ⁺ 761	761.8188	2	6.9 ± 10.3	H27 α	316.4154	4	-1.4 ± 3.8
LiH(1-0)	443.9529	9	0.6 ± 2.9	H28 α	284.2506	3	-3.0 ± 7.7
CH 532	532.7239	10	12.6 ± 4.9				

Note. — All fluxes have been scaled to $z = 3$ and $S_{1.4\text{mm}} = 15\text{mJy}$, corresponding to $L_{\text{IR}} \sim 5 \times 10^{13} L_{\odot}$. Lines with $S/N > 3$ are shown in bold. For transitions with fine or hyperfine structure, only the main transition is listed, and the line may be referred to by frequency instead of quantum numbers for clarity.

^a Derived from ATCA low- J ¹²CO observations

have consistently shown solar or near-solar abundances of secondary species such as iron and nitrogen out to high redshift (e.g., Sameshima et al. 2009; Juarez et al. 2009; Nagao et al. 2012). Henkel et al. (2010) posit that the apparent contradiction may originate from the geometry of the source, with the metal-enriched gas observed in the optical and infrared largely confined to the regions nearest to the AGN, while the CO emission arises from relatively metal-poor gas hundreds or more parsecs from the AGN. The SPT DSFGs have ¹³CO emission intermediate between that of local galaxies and H1413+117, sim-

ilar to the line brightness ratios seen in SMM J2135-0102. The SPT DSFGs do not, however, have C¹⁸O emission as bright as in SMM J2135-0102, but further observations are necessary to determine the true strength of C¹⁸O in the typical SPT DSFG.

To attempt to characterize the typical gas conditions and the [¹²CO/¹³CO] abundance ratio in the SPT DSFGs, we use RADEX to model the interstellar media of the SPT DSFGs in aggregate, under the assumption that all the detected ¹²CO and ¹³CO emission arises from gas of comparable temperature and density. Since these

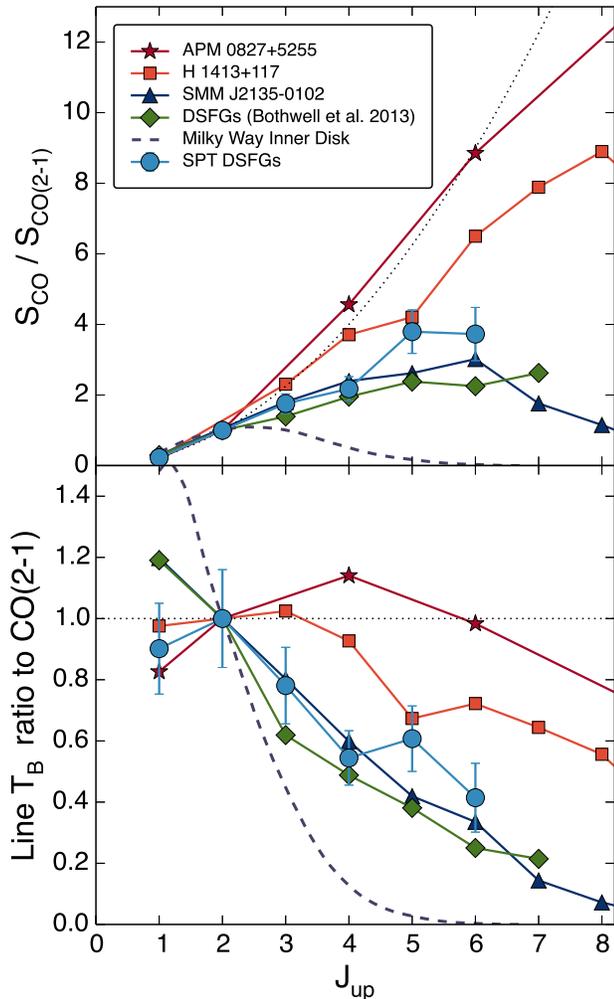


Figure 3. ^{12}CO SLEDs of the SPT DSFGs and other systems for comparison, normalized to the $J = 2 - 1$ transition. The average ^{12}CO (1–0) and (2–1) transitions are derived from data obtained with ATCA. The SLEDs are plotted both in flux units (*top*) and brightness temperature units (*bottom*). The SPT points are shown with an additional 15% systematic uncertainty from the choice of weighting; uncertainties for the other objects are not shown. The dotted line indicates thermalized, optically thick gas. The two outlying objects, H1413+117 and APM 0827+5255, both host powerful quasars.

models are compared not to the lines of a single object but rather to the average of lines of a large number of objects, we include an additional 15% uncertainty in the calculated line ratios, motivated by the variation seen when different scaling methods are applied to the sources which contribute towards individual lines. We run a grid of excitation models with free parameters $N_{\text{CO}}/\Delta v$, the column density of ^{12}CO molecules per unit line width, T_{kin} , the kinetic temperature of the gas, n_{H_2} , the number density of molecular hydrogen, and $[^{12}\text{CO}/^{13}\text{CO}]$, the relative abundance of the CO isotopologues. Our grid of models spans $N_{\text{CO}}/\Delta v = 10^{15} - 10^{19} \text{ cm}^{-2}(\text{km/s})^{-1}$, $T_{\text{kin}} = 12 - 300 \text{ K}$, $n_{\text{H}_2} = 10 - 10^6 \text{ cm}^{-3}$, and $[^{12}\text{CO}/^{13}\text{CO}] = 10 - 10^4$. In all models, we fix the background temperature of the cosmic microwave background (CMB) to $T_{\text{CMB}} = (1 + z_{\text{common}})T_{\text{CMB}}(z = 0) \sim 11 \text{ K}$, though, as

we discuss further below, any value of $T_{\text{CMB}}(z)$ provides nearly equivalent results for $z = 2 - 6$.

Many prior assumptions typically implemented during line radiative transfer modeling – for example, that the system be dynamically stable, or that the total gas mass not exceed the dynamical mass – have no straightforward analog when modeling the average excitation of a collection of sources. As such, we adopt only two priors. First, motivated by the RADEX documentation, line optical depths are constrained to be $\tau < 100$, because at optical depths exceeding 100 the line excitation temperatures are unlikely to reflect conditions in the emitting region. This prior effectively excludes the corner of parameter space defined by high ^{12}CO column density, low temperature, and low H_2 number density. Second, we require that the gas have at least enough velocity dispersion to correspond to virialized motion under its own self gravity, i.e., that K_{vir} not be $\ll 1$. A convenient parameterization of this criterion is provided in Bradford et al. (2009).

The parameter degeneracies and posterior probability distributions for each parameter are shown in Figure 4. We find that no single model fits all seven available line ratios well (minimum $\chi^2 = 10.4$ for three degrees of freedom). This likely reflects the simplicity of the modeling procedure, which represents a heterogeneous collection of galaxies as a single, homogeneous gas component of simple geometry. The column density per velocity interval is well-determined, $\sim 3 \times 10^{17} \text{ cm}^{-2}(\text{km/s})^{-1}$, indicating that the ^{12}CO lines are moderately optically thick, with $\tau \sim 1 - 10$ for the transitions considered here. The average line ratios as measured slightly prefer two solution ranges, with one solution implying a cold but very dense medium with $T_{\text{kin}} \sim 22 \text{ K}$, $n_{\text{H}_2} > 10^5 \text{ cm}^{-3}$, and $[^{12}\text{CO}/^{13}\text{CO}] \sim 700$, while the other indicates a more diffuse but hot medium, with $T_{\text{kin}} \gtrsim 100 \text{ K}$, $n_{\text{H}_2} \sim 800 \text{ cm}^{-3}$, and $[^{12}\text{CO}/^{13}\text{CO}] \sim 40$. However, further investigation indicates that this apparent bimodality is largely due to the influence of the ^{12}CO (4–3) line. If the flux of this line is increased by $\sim 30\%$, the standard degeneracy between n_{H_2} and T_{kin} is recovered. A larger sample size and studies of individual DSFGs will indicate whether this apparent deficit of ^{12}CO (4–3) is in fact real or whether it indicates that the $J \geq 5$ ^{12}CO lines are beginning to trace a second, higher-excitation gas component. Without further data, we cannot break the degeneracy between T_{kin} and n_{H_2} . If, however, the gas and dust are effectively coupled, the temperatures of gas and dust are roughly comparable. In this case, with the measured range of dust temperatures in these sources $T_{\text{d}} = 20 - 50 \text{ K}$, we obtain a density of $n_{\text{H}_2} \sim 10^4 - 10^5 \text{ cm}^{-3}$ and an abundance ratio $[^{12}\text{CO}/^{13}\text{CO}] \sim 100 - 200$. Measuring additional ^{12}CO lines would indicate whether the tentative flattening we see near $J = 5$ indeed leads to a turnover at higher J , and may help break the degeneracies present in these radiative transfer models. We note that such degeneracy is common and expected for CO SLEDs (and is illustrated clearly by Carilli & Walter 2013, their Fig. 3, and Appendix B).

With the above degeneracies in mind, for the typical submillimeter galaxy in the SPT sample, we find that ^{13}CO is likely no more than 3% as abundant as ^{12}CO . In

the best fit solution range, the ^{13}CO lines have moderate opacity – $\tau_{^{13}\text{CO}} = 0.4$ for $T_{\text{kin}} = 40\text{ K}$. Better abundance constraints require observations of purely optically thin species, or observations of sufficient depth that the optically thin wings of a centrally optically thick line can be used for abundance measurements (e.g., Muller et al. 2006).

4.2. The Dense Gas Phase

Due to its weak electric dipole moment, ^{12}CO rapidly becomes thermalized at densities above a few hundred molecules cm^{-3} . Molecules such as HCN, HNC, and HCO^+ , on the other hand, require densities $\sim 100\times$ higher for collisional excitation, and have been used extensively within the Milky Way and in local galaxies as probes of the dense phase of the interstellar medium from which stars actively form. In the rest-frame spectrum of SPT DSGs, we detect 7 lines of CN, HCN, HNC, and HCO^+ from 240–780 GHz. Specifically, we detect the (4–3) transition of all four species, the $N = 3–2$ transition of CN, the $J = 5–4$ HNC line, and the $J = 6–5$ line of HCO^+ . All lines are roughly equally bright, suggesting the emission from these lines is optically thick, nearly thermalized, and arises from a warm and dense medium. Such thermalized emission would certainly be unusual were it to arise from a single object – Knudsen et al. (2007) and Papadopoulos (2007) both find that subthermal excitation of these dense gas tracers is common, with thermalized emission of HCN up to $J = 4–3$ arising only in local ULIRG Arp 220.

The relationship between $L'_{\text{HCN}(1-0)}$ and L_{IR} appears linear over a remarkable 7–8 orders of magnitude (Wu et al. 2005), from dense galactic cores to ULIRGs, suggesting that the same gas responsible for the HCN emission also gives rise to the infrared luminosity indicative of massive star formation. This linear relation may break down for high-redshift objects (e.g., Gao et al. 2007; Riechers et al. 2007a), though many of the objects detected thus far also host active galactic nuclei which may provide an additional contribution to L_{IR} at short wavelengths. A similar relation has also been found for HCO^+ and the cyanide radical CN (Riechers et al. 2006, 2007b), though interpretation of CN is difficult due to its strong spin-spin and spin-nucleus coupling. The fine and hyperfine structure transitions of CN lie close enough to each other (\lesssim few hundreds of km/s) as to be spectrally confused for most galaxy-integrated measurements, and we make no attempt to separate the components within our very wide channels.

In comparison with other molecular ISM tracers, $L'_{\text{HCN}(1-0)}/L'_{\text{CO}(1-0)}$ may indicate a type of “dense gas fraction.” With its low critical density, CO can be interpreted as tracing the total gas mass, while HCN, HNC, and HCO^+ trace only the densest active star-forming regions. Support for this framework comes from observations showing that, in nearby spiral galaxies, $L'_{\text{HCN}}/L'_{\text{CO}} \sim 0.01–0.06$, rising to ~ 0.15 in starbursting systems (Gao & Solomon 2004). Juneau et al. (2009) use observations of the $J = 1–0$ and $J = 3–2$ transitions of HCN and HCO^+ in local (U)LIRGs and numerical simulations to show that the dense gas fraction can rise sharply during the final stages of a major merger event. In this scenario, the dissipation of angular momentum

during the galactic collision funnels vast quantities of gas to the center of the system, triggering an intense burst of star formation. In the average SPT DSGF spectrum, we find $L'_{\text{HCN}(4-3)}/L'_{\text{CO}(1-0)} = 0.045$. For the range of HCN excitation found by Papadopoulos (2007), this corresponds to $L'_{\text{HCN}(1-0)}/L'_{\text{CO}(1-0)} = 0.045–0.165$, in agreement with typical measurements of actively star-forming galaxies (Gao et al. 2007, e.g.).

The dense gas tracer lines we detect have comparable brightness, which would be unexpected if each molecule arose in the same gas conditions unless the lines are highly optically thick. However, variations in line strength between the various dense gas tracers may be attributable to a variety of chemical abundance effects. Models from Maloney et al. (1996), for example, indicate that HCO^+ may be preferentially destroyed in X-ray Dominated Regions (XDRs), while more recent simulations from Meijerink & Spaans (2005) find instead that the abundance of HNC relative to HCN may increase in the presence of an XDR. In these models, the ionization structure induced by the deeply-penetrating X-rays alters the balance of formation channels for the three molecules. HNC may also become overluminous in the centers of galaxies as the dominant reaction type shifts from ion-neutral to neutral-neutral as density increases (Aalto et al. 2002). The CN radical, meanwhile, which has a critical density intermediate between CO and HCO^+ , appears particularly well-suited to tracing regions with strong UV fields where HCN and HNC may be selectively dissociated (Boger & Sternberg 2005), as in the filaments of Orion A (Rodríguez-Franco et al. 1998). As a further complication, the high- J lines of HNC, HCN, and HCO^+ may not result from purely collisional excitation, as the presence of a strong mid-IR radiation field allows these molecules to be radiatively pumped via their first bending modes at 21, 14, and 12 μm , respectively. We discuss this possibility in more detail in §5.3.

At high redshift, the faintness of these molecular lines has historically confined their study to bright, highly magnified lensed systems, with only two objects detected in multiple transitions or species. In quasar H1413+117, observations of low- and mid- J transitions of HCN, HCO^+ , and CN indicate purely collisional excitation with $T_{\text{kin}} \sim 60\text{ K}$ and $n_{\text{H}_2} \sim 10^{4.8}\text{ cm}^{-3}$ (Wilner et al. 1995; Barvainis et al. 1997; Solomon et al. 2003; Riechers et al. 2006, 2007b, 2011). The APM 0827+5255 quasar, in contrast, is bright in HCN, HNC, and HCO^+ at least to the $J = 6–5$ lines, and the excitation of those species indicates that radiative pumping is likely in play (García-Burillo et al. 2006; Guélin et al. 2007; Weiß et al. 2007; Riechers et al. 2010). Such a finding is not unexpected, given the very hot dust ($T_d \sim 220\text{ K}$) surrounding the nuclear starburst / active nucleus in this system.

To investigate the gas conditions which could excite these lines, we again make use of RADEX models. We assume the emission from all four of these species comes from the same single gas component, not necessarily related to the origin of the CO emission discussed previously. While the medium that gives rise to these dense gas tracer lines will also contribute to the CO emission,

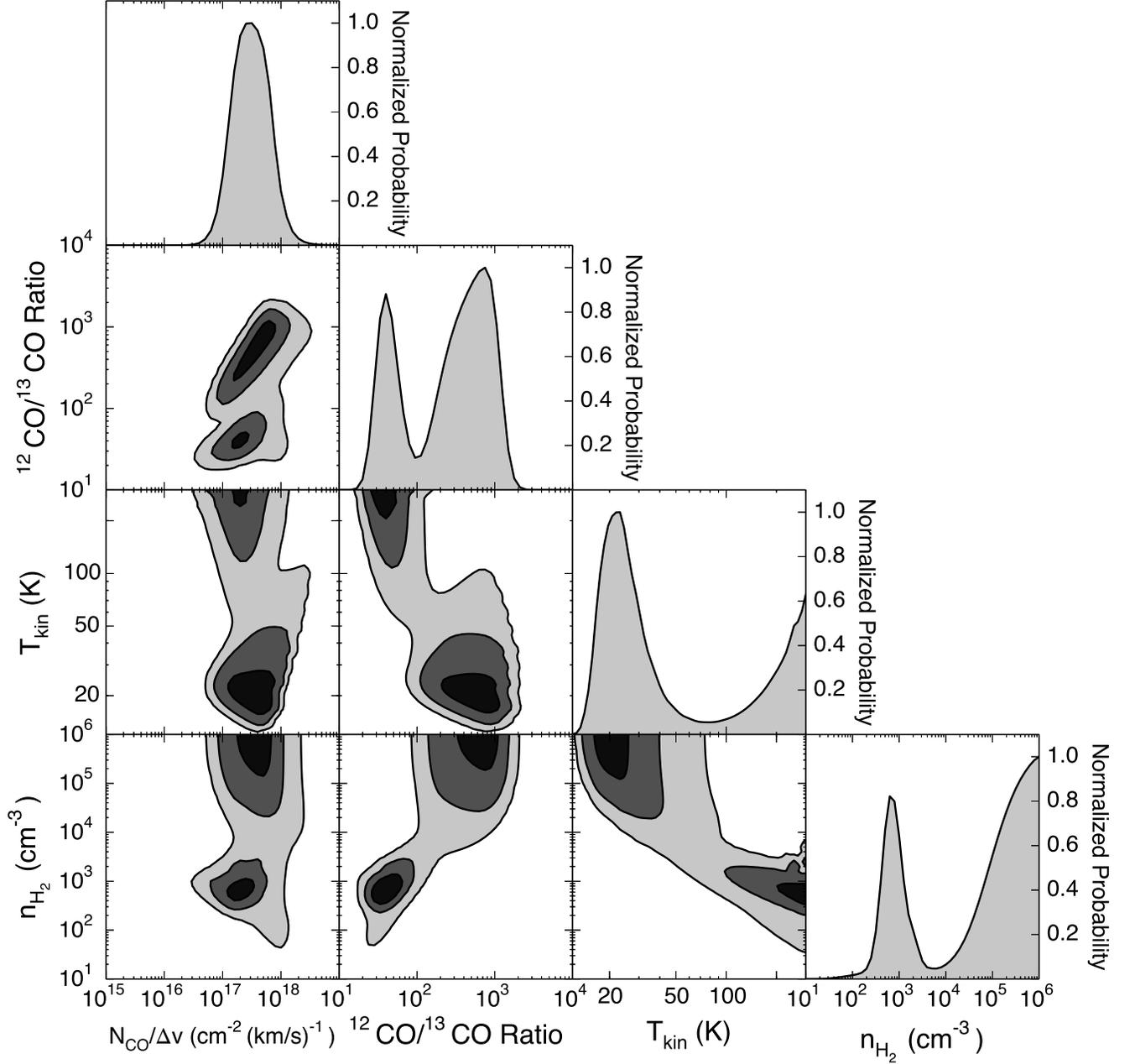


Figure 4. The results of our excitation analysis of the ^{12}CO and ^{13}CO lines detected in our composite spectrum, showing the degeneracies between parameters. Marginalized posterior distributions for the parameters along the bottom axis are shown along the diagonal. The ^{12}CO gas is thermalized at densities $n_{\text{H}_2} > 10^6 \text{ cm}^{-3}$, and most ^{12}CO molecules are in $J > 5$ levels for temperatures $T_{\text{kin}} > 150 \text{ K}$, so those regions of parameter space are equally well fit given the transitions available. Contour levels are 1, 2, and 3σ . The apparently unbounded one-dimensional marginalized parameter distributions are a direct consequence of degeneracies inherent in such modeling; expanded ranges would not lead to bounded distributions (see Appendix B).

the converse is less likely to be true, given the excitation requirements of higher critical density molecules. In order to narrow the vast parameter space that emerges when many species are modeled simultaneously, we assume the relative abundance ratios of CN, HCN, HNC, and HCO^+ are the same as in the local starburst galaxy NGC253 – namely, $[\text{HCO}^+/\text{HCN}] = 2$, $[\text{HNC}/\text{HCN}] = 0.5$, and $[\text{CN}/\text{HCN}] = 0.25$ (Wang et al. 2004). Since we only aim to infer general properties for DSFGs, this

choice is not critical; using abundance ratios as derived for the prototypical starburst galaxy M82 (Naylor et al. 2010), or even equal abundances of all four species changes the results by less than an order of magnitude in column densities and a factor of two in gas kinetic temperature. As before, we implement a prior on the line optical depth τ , require solutions with enough velocity dispersion to correspond to virialized motion under the self-gravity of the gas, and include an additional

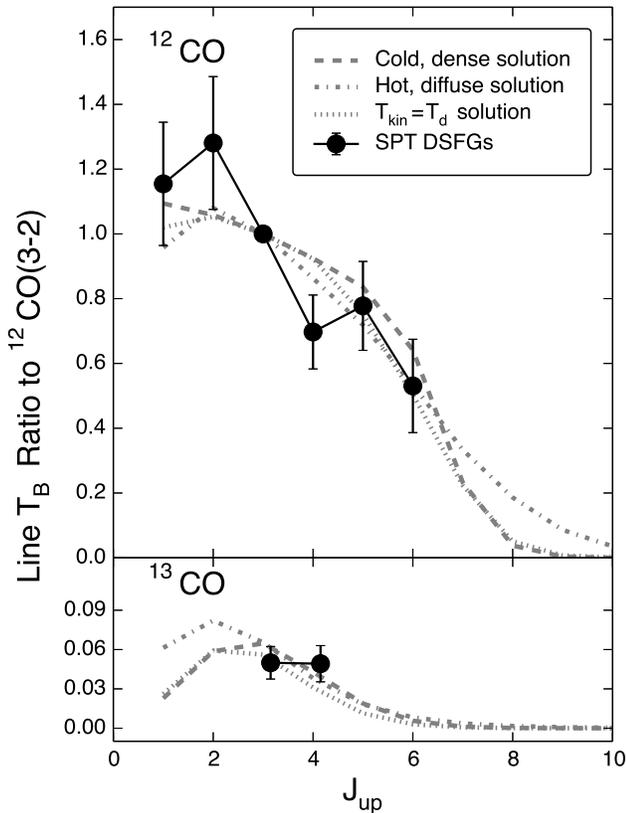


Figure 5. Representative solutions to the excitation modeling of ^{12}CO and ^{13}CO marked as dashed lines, from the parameter degeneracies shown in Figure 4. The three solutions shown demonstrate the difficulty in distinguishing gas conditions along the degenerate curve in n_{H_2} - T_{kin} . Each panel shows the line ratio, in brightness temperature units, with respect to the ^{12}CO (3–2) line. The top panels show the ^{12}CO SLED, the bottom panels the ^{13}CO SLED.

15% uncertainty in the modeled line ratios to account for the varied sources contributing to the flux of each line.

Our analysis indicates that the emission from mid- J lines of HCN, HNC, HCO^+ , and CN arises largely from warm, dense gas, with $T_{\text{kin}} \sim 55\text{K}$ and $n_{\text{H}_2} \sim 10^{5.5} - 10^{7.5}\text{cm}^{-3}$ (Fig. 6), though significant degeneracies remain. The best-fit molecular column density per velocity interval, $N_{\text{HCN}}/\Delta v \sim 10^{15}\text{cm}^{-2}(\text{km/s})^{-1}$, is high enough to indicate that the lines of species other than CN are moderately optically thick, with $\tau \sim 5 - 30$ (due to its many fine and hyperfine energy level splittings, CN is always optically thin). The high optical depth reduces the critical density for collisional excitation by a comparable factor. The prior constraint that τ not be too high effectively constrains the molecular hydrogen density to $n_{\text{H}_2} > 10^5\text{cm}^{-3}$. The extreme optical depths which would be required to fit the observed line ratios for $n_{\text{H}_2} < 10^5\text{cm}^{-3}$ lead us to investigate alternatives to pure collisional excitation in §5.3, below.

As a cross-check, we can calculate the fraction of the total ^{12}CO emission which arises from this dense gas component by assuming the ^{12}CO lines emitted by gas in the dense phase have the same filling factor as the lines of the dense gas tracer molecules. The assumption of equal filling factors effectively provides a normalization between the dense gas tracer lines and the ^{12}CO

lines. Assuming a $[^{12}\text{CO}/\text{HCN}]$ abundance ratio of 8000 as in NGC253 (Wang et al. 2004), the estimated contribution of ^{12}CO emission arising from this gas component to the total is 4 – 10% from ^{12}CO (1–0) to ^{12}CO (6–5). This confirms that fitting the two components separately is justified. The gas traced by these high-critical density molecules only begins to dominate the ^{12}CO emission beyond the $J = 8 - 7$ transition; future radiative transfer modeling of individual DSFGs will require multiple gas components when such high- J ^{12}CO lines are included.

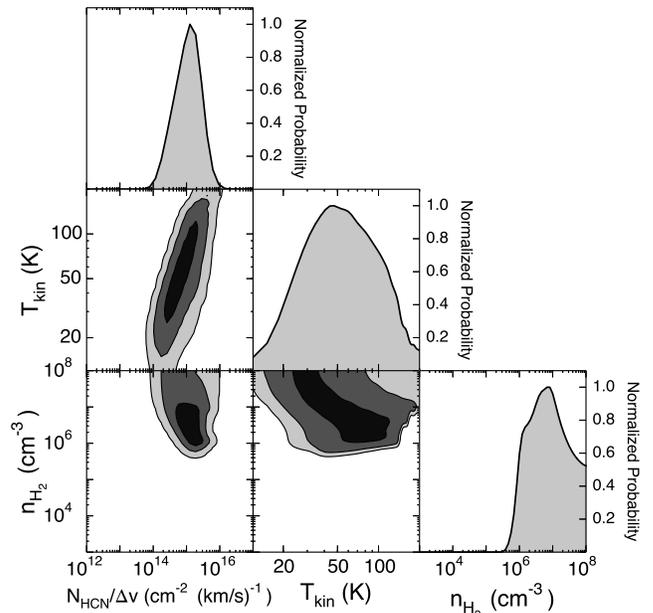


Figure 6. Parameter degeneracies in the excitation analysis of HCN, HNC, HCO^+ , and CN, as in Fig. 4. Contour levels are 1, 2, and 3σ . Again, the unbounded one-dimensional marginalized distributions reflect inherent degeneracies in the radiative transfer models, explored further in Appendix B.

5. DISCUSSION

5.1. Comparison to other High-Redshift Galaxies

Given the substantial observing time invested in the pre-ALMA era to detect the faint ISM diagnostics presented here, it is instructive to place our results in context with other well-studied high-redshift objects. We focus on three systems in particular: the lensed starburst galaxy SMM J2135-0102, and lensed quasars H1413+117 and APM 0827+5255. These objects may not be representative of the high-redshift star-forming galaxy population. APM 0827+5255, in particular, appears to be one of the most extreme objects in the universe by any measure. Our results, based on the aggregate properties of many sources, should be relatively immune to distortion by extreme outlying objects, allowing the average properties of DSFGs to be determined.

ALMA will dramatically reduce the time necessary to detect molecular ISM lines at high redshift – summed across sources, all lines we detect in our average spectrum were observed for less than 30 minutes in total, and with only $\sim 1/4$ the final number of antennas incorporated into the array. Given that each of our sources

was observed for only two minutes per tuning, and scaling to the noise level reached for the stacked transitions, we find that at full capacity, ALMA will be able to detect these faint lines and at higher spectral resolution in only half an hour per line, assuming a fiducial target galaxy with $L_{\text{IR}} = 5 \times 10^{13} L_{\odot}$. As a tool for planning future ALMA observations of high-redshift DSFGs, we show in Fig. 7 the ratio of the line luminosity of several species to the ^{12}CO line luminosity at the same rotational level for our composite spectrum and the reference objects described above. The SPT DSFGs exhibit brighter ^{13}CO emission than H1413+117, but are fainter in most other lines which trace the dense phase of the ISM. Both the SPT DSFGs and SMM J2135-0102 appear to have significantly less-highly excited high-critical density molecules at $J > 4$, underscoring the extreme conditions present in the circumnuclear region of the APM 0827+5255 quasar.

5.2. Combining Multiple Transitions of Each Species

For many species, we detect no single transition significantly, but by stacking all transitions of those species that fall within our bandpass, we can constrain the total luminosity emitted by a given molecule. As an example, there are 10 hydrogen- α radio recombination lines (H20 α to H29 α) from 250–770 GHz. In Table 3, we give the average integrated flux per transition of a number of species which have numerous lines within our bandpass. Such a table is intended to draw attention to species which are ripe for future study.

Aside from the lines with individually detected transitions, we also find significant flux in the stacked transitions of the rigid rotor CCH and in the CH $N, J = 1, 3/2 \rightarrow 1, 1/2$ doublet at 532 and 536 GHz, the first detection of these species at high redshift. The formation mechanisms of both molecules – for CH, the radiative association of C^+ and H_2 ; for CCH, the dissociative recombination of C_2H_2^+ or C_2H_3^+ – indicates that they likely trace regions of moderate density ($n \sim 10^3 \text{ cm}^{-3}$) where UV radiation controls the chemical networks (Sheffer et al. 2008; Godard et al. 2009; Gerin et al. 2010, 2011). Given the close proximity of the CH doublet lines to the $J = 6 - 5$ lines of HCN and HCO^+ , all three species can be observed simultaneously in the 3 mm atmospheric window for $z \sim 4$ sources, making this group of transitions a potentially powerful probe of the chemistry of the ISM at high redshift.

Using Table 3, we can quantify the amount of contamination to brighter lines from molecules with closely spaced frequency ladders. As an example, based on unexpectedly luminous HC_3N emission up to $J = 25 - 24$ in the highly-obscured LIRG NGC 4418 (Aalto et al. 2007), Riechers et al. (2010) speculate that the HCO^+ (5–4) flux in the APM 0827+5255 quasar may be contaminated by emission from HC_3N (49–48). From 40 transitions of HC_3N well-separated from other lines, observed nearly 250 times, we find no evidence for significant emission from HC_3N , indicating that this heavy rotor does not significantly contaminate the flux of other observed lines at high- J .

5.3. Excitation in Dense Gas Tracer Molecules

Oddities exist in the line ratios of the dense gas tracer species we have detected – the HNC(4–3) and (5–4)

Table 3
Average Combined Line Properties

Species	Transitions	Observations	$\langle L' \rangle$ (10^9 K km/s pc^2)
^{12}CO	4	30	209.3 ± 6.2
^{13}CO	4	27	10.6 ± 2.0
C^{18}O	4	26	1.2 ± 2.3
HCN	6	36	7.5 ± 1.8
HNC	6	35	12.1 ± 2.3
HCO^+	6	37	9.8 ± 1.8
CS	4	57	0.8 ± 1.6
H_2O^+	7	34	7.5 ± 2.9
CH	2	20	11.3 ± 3.4
OH	2	18	1.8 ± 2.0
CN	4	28	9.0 ± 2.1
SiO	10	75	-2.4 ± 1.4
N_2H^+	6	34	-0.7 ± 2.0
H α RRLs	10	56	-1.8 ± 1.4
CCH	6	34	7.8 ± 1.9
H_2CO	9	56	1.8 ± 1.3
HC_3N	40	249	-1.5 ± 0.8

Note. — Luminosity given is the *average* luminosity per transition; luminosities vary for individual transitions. Line averages exclude individual transitions which are strongly blended with other lines. The number of observations refers to the number of times a line was observed in a single source, summed over all sources and transitions for each species. Molecules with combined transitions detected at $S/N > 3$ are shown in bold.

lines are nearly equally luminous, and $L'_{\text{HCO}^+(6-5)}$ significantly exceeds $L'_{\text{HCO}^+(4-3)}$. Given the high critical densities of these lines ($n_{\text{crit}} > 10^7 \text{ cm}^{-3}$) which argue against purely collisional thermalization, alternate excitation mechanisms and geometrical effects must be explored.

The first possible mechanism, which is also the easiest to rule out, is that the changing CMB temperature affects the level populations of each observed line differently or that diminishing contrast between the lines and CMB alters the observed line ratios (da Cunha et al. 2013). Since our redshift search program covered a fixed observed frequency range, the highest- J molecular lines come preferentially from the highest-redshift sources, in which the higher CMB temperature can more easily populate the upper energy states. This is unlikely to offer a satisfactory explanation for our observed line ratios. From our lowest-redshift object to the highest, the CMB changes temperature only by a factor of two, from 8.2–18 K, and this temperature is still much lower than other relevant temperatures in these systems, for which $T_{\text{kin}} \sim T_d \gtrsim 30 \text{ K}$. Additionally, if the dust and gas are nearly in thermodynamic equilibrium, for a given dust temperature at $z = 0$, the thermodynamically equivalent temperature at higher redshift is $(T_{\text{kin}}^6(z = 0) + T_{\text{CMB}}^6(z))^{1/6} \approx T_{\text{kin}}(z = 0)$ so long as $T_d = T_{\text{kin}} > T_{\text{CMB}}$, assuming a dust emissivity law of $\beta = 2$ (Papadopoulos et al. 2000).

Of course, with a sample size of less than 25 objects, the “average” properties we derive may still be dominated by outliers. The faint lines we detect typically arise from spectral regions covered by 5–10 sources, and using a weighted average increases the contribution from bright

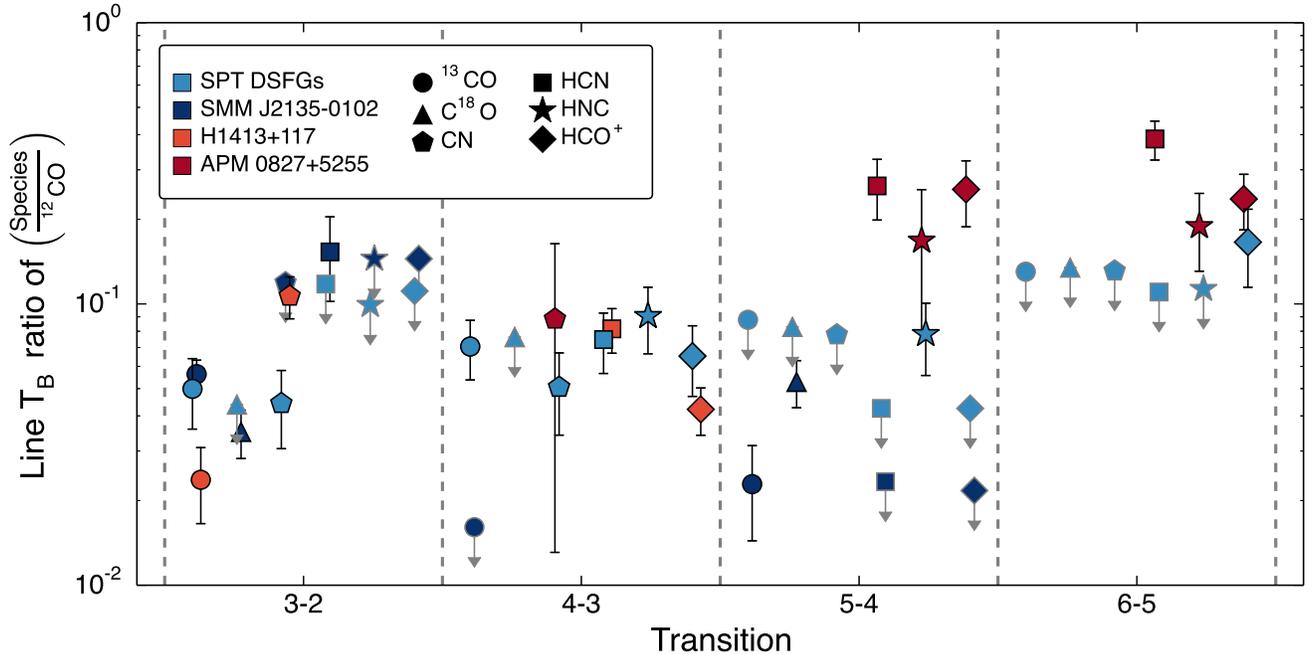


Figure 7. Comparison of faint lines in the SPT DSFGs to those detected in three high-redshift lensed sources: starburst galaxy SMM J2135-0102, and quasars H1413+117 and APM 0827+5255. Plotted is the ratio (in brightness temperature units) of the faint line to the same- J ^{12}CO line – for example, ^{13}CO (4-3)/ ^{12}CO (4-3) or $\text{CN}(N = 3 - 2)/^{12}\text{CO}$ ($J = 3 - 2$). All upper limits are 3σ . Data for SMM J2135-0102 from Danielson et al. (2011, 2013); for H1413+117 from Barvainis et al. (1997); Weiß et al. (2003); Riechers et al. (2007b); Bradford et al. (2009); Henkel et al. (2010); Riechers et al. (2011); for APM 0827+5255 from Downes et al. (1999); Wagg et al. (2005); García-Burillo et al. (2006); Guélin et al. (2007); Weiß et al. (2007); Riechers et al. (2010). The ^{12}CO (5-4) line luminosity for APM 0827+5255 is interpolated from the CO SLED presented in Weiß et al. (2007).

sources. In the least-sampled lines, a single source contributes $\sim 65\%$ of the weight to the stacked line, though out of just five or six sources. Whether our observed line ratios are truly typical of the DSFG population (lensed and/or unlensed) will become clearer as other targeted spectroscopic observations and blind redshift surveys are performed.

Alternatively, the excitation of HNC, HCN, and HCO^+ may be strongly affected by pumping by mid-infrared photons. In this scenario, a molecule in the ground vibrational state, $\nu = 0$, $J = J_i$, absorbs a mid-IR photon to excite it to the $\nu = 1$, $J = J_i + 1$ state before decaying to the $\nu = 0$, $J = J_i + 2$ state, a net change of $\Delta J = +2$. The first bending modes of HNC, HCN, and HCO^+ are at 21, 14, and $12\mu\text{m}$, respectively, so for dust-dominated continuum SEDs, which fall from 21– $12\mu\text{m}$, we might expect HNC to be more susceptible to mid-IR pumping than HCO^+ . Various studies of local IR-bright galaxies have concluded that this effect is unimportant compared to collisional excitation (Stutzki et al. 1988; Gao & Solomon 2004), but the phenomenon is still plausible for the APM 0827+5255 quasar, where very hot $T_d \sim 220\text{K}$ dust near the central AGN creates an intense radiation field in the mid-IR (Riechers et al. 2010). Whether this effect is also possible in the SPT DSFGs is less clear. No SPT source in the sample presented here shows a continuum SED with $T_d > 60\text{K}$. Detection of mid-IR absorption lines would provide definitive proof of the effectiveness of mid-IR pumping (e.g., Lahuis et al. 2007), but such observations would be extremely challenging given the faintness of these sources. Instead, we use *Herschel*/PACS measurements at 100 and $160\mu\text{m}$ to

constrain the short wavelength side of the dust SEDs (Stranget et al., in prep.), which we accomplish by allowing λ_0 , the wavelength at which the dust opacity is unity, to be a free parameter (which had previously been fixed at $100\mu\text{m}$). Since we aim only to divide the sample into two groups, the precise form of this fitting function is unimportant; nearly the same source divisions emerge when the short-wavelength side of the continuum SED is represented by a power law with index $\alpha = 2$.

With these short-wavelength SED fits in hand, we again scale all SEDs to the common redshift of $z = 3$ before dividing the sample based on rest-frame $21\mu\text{m}$ flux density. For our sample, we divide the sources into two groups, with $S_{21\mu\text{m}} > 2\text{mJy}$ and $S_{21\mu\text{m}} < 2\text{mJy}$. Both groups of sources span our entire redshift range, and the grouping is not influenced by PACS detection or non-detection (that is, sources with PACS $100\mu\text{m}$ detections are present in both groups, as are those with non-detections). Both H1413+117 and APM 0827+5255 would fall in the high mid-IR group of sources (although the continuum SEDs of our sources are less well constrained in the rest-frame mid-IR than either of these objects), and APM 0827+5255 has a stronger mid-IR radiation field than any of the SPT sources. Since dividing the sample in half lowers the number of sources for each individual transition to 2–5, we average all available transitions of each molecule to lower the uncertainty on the average line flux. To determine the significance of any difference between the high and low mid-IR groups, we also repeat the above procedure for 1000 random subsets of the sample, each containing half the total number of sources. The spread of this distribution shows the expected variation in line ratios when the sample is divided

in half at random. As shown in Fig. 8, both groups are consistent with randomly dividing the sample in half, suggesting that vibrational mode pumping is insignificant in the average SPT DSFG.

Finally, the SPT DSFGs could be subject to differential magnification which distorts the observed line fluxes. Although lensing itself is wavelength-independent, the finite size of the background source causes different regions of the lensed object to be magnified by varying amounts, leading to variations in the ratios of observed spectral lines (e.g., Downes et al. 1995). This is an important effect when the tracers in question fill different parts of the target galaxy (Serjeant 2012; Hezaveh et al. 2012). However, for these chemically related and energetically similar species, differential magnification seems unlikely to influence the line ratios we have measured.

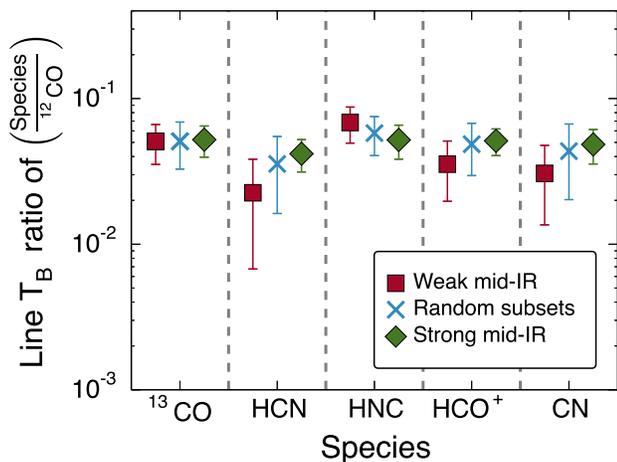


Figure 8. Line ratios in comparison to ^{12}CO determined by dividing our sample into a group with strong mid-IR flux density ($S_{21\mu\text{m}} > 2\text{mJy}$) and a group with weak mid-IR flux density ($S_{21\mu\text{m}} < 2\text{mJy}$). Also shown is the range of values (average and 16-84% interval) found when randomly drawing subsamples of half the sources (with replacement). That the high critical density molecules HNC, HCN, and HCO^+ are comparably bright in the two groups indicates that these molecules are unlikely to be pumped to high- J energy levels via their first vibrational modes in the mid-IR. Note that HCN, HCO^+ and CN are detected at only 2.0, 2.0, and 2.5 σ in the low mid-IR group of sources, respectively.

6. CONCLUSIONS

We have presented the average rest-frame millimeter spectrum of 22 gravitationally lensed dusty, star-forming galaxies at high redshift. Stacking wide-band ALMA spectra of objects from $z = 2 - 5.7$ allows faint ISM diagnostics to be studied as typical characteristics of the SPT DSFGs. Aside from bright transitions of ^{12}CO , we also find multiple much fainter molecular transitions from ^{13}CO , HCN, HNC, HCO^+ , and CN. The ^{12}CO SLED resembles that of other high-redshift DSFGs, and in conjunction with multiple ^{13}CO lines, we constrain the [$^{12}\text{CO}/^{13}\text{CO}$] abundance ratio to be $\sim 100 - 200$ for gas temperatures comparable to the dust temperatures of these sources, $T_{\text{kin}} \sim 40\text{K}$. The average SPT DSFG has ^{13}CO brightness comparable to the only other high- z star-forming system in which it has been measured (SMM J2135-0102), but does not show similarly bright C^{18}O . Our excitation analysis indicates the HNC, HCN,

HCO^+ , and CN emission arises from a warm, dense, and optically thick medium, which allows the energy levels 40–90K above the ground state to be sufficiently populated. Population of vibrational modes in these molecules is unlikely to be relevant for the typical SPT DSFG, though a small sample size and the possibility of differential magnification may explain the line ratios we observe. These observations represent the first constraints on the relative strengths of these lines in high-redshift star-forming galaxies, and will be instrumental in planning future ALMA observations of such systems.

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APPENDIX

A. REDSHIFT CONFIRMATION OF SPT 0125-50

The redshift of SPT 0125-50 was ambiguous in the ALMA 3 mm spectra obtained during Cycle 0, as only the ^{12}CO (4–3) line was clearly detected ([CI] was only tentatively detected). Its redshift has been confirmed as $z = 3.9592$ by the serendipitous detection of the ortho- H_2O ($2_{1,2} - 1_{0,1}$) line, $\nu_{\text{rest}} = 1669.90477$ GHz, in the high-resolution $870 \mu\text{m}$ ALMA Cycle 0 dataset presented in Vieira et al. (2013). The line is seen in absorption, as is common in local systems (e.g., González-Alfonso et al. 2012). The detection is shown in Figure 9.

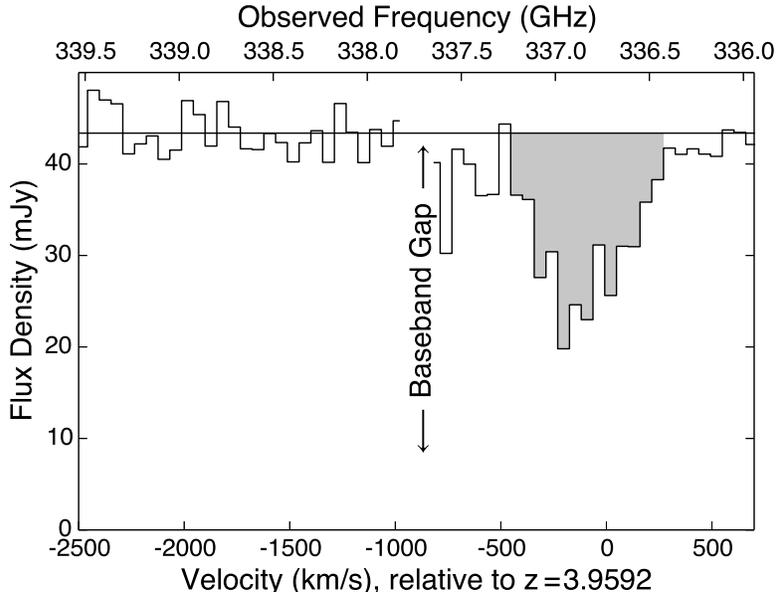


Figure 9. ALMA $870 \mu\text{m}$ spectrum of SPT 0125-50 showing the serendipitous detection of the H_2O ($2_{1,2} - 1_{0,1}$) line in absorption, which confirms the redshift as $z = 3.9592$. The continuum level derived from the line-free basebands is shown as a horizontal line, at ~ 44 mJy.

B. RADIATIVE TRANSFER MODELING OF AN INHOMOGENEOUS COLLECTION OF OBJECTS

One concern when performing radiative transfer modeling on an ensemble of sources is that variations in the ISM conditions between sources will render any inference about conditions from the averaged SLED meaningless. An analogous problem applies to galaxy-integrated measurements, at least when fitting with a single gas component, as individual galaxies are also comprised of molecular clouds with a range of temperatures, densities, etc. In the case of the SPT DSFGs, the present sample may contain objects with a range of CO excitation, from relatively quiescent gas conditions like those present in the Milky Way to the extreme excitation seen in some high-redshift quasars. We stress that the radiative transfer embodied by the RADEX modeling is intended to determine only approximate conditions that would match the limited observations given a simplified geometrical model of the source. Such simplifications apply in nearly all extragalactic and many galactic applications of the large velocity gradient radiative transfer approximation (of which RADEX is one open-source incarnation), which has now been widely used since Scoville & Solomon (1974). In this Appendix, we show that the RADEX modeling performed on a collection of sources recovers gas conditions that are representative of the input sources, subject to the degeneracy inherent in large velocity gradient models. Here, we consider only ^{12}CO for simplicity, but the conclusions are easily extended to the other molecular tracers.

We begin by attempting to recover the conditions of a single gas component by generating line ratios for a given set of parameters, with no additional scaling, weighting, or averaging. This test shows the degeneracy that is inherent to the modeling itself – certain combinations of temperature and column and number densities produce line ratios which are virtually indistinguishable. In particular, we recover the well-known degeneracy between gas kinetic temperature and number density of molecular hydrogen (Figure 10, left). Without additional information – either in the form of priors on the parameters or additional ^{12}CO lines – this degeneracy is virtually impossible to break.

We next demonstrate a more realistic scenario, in which the averaging performed in this work is applied to galaxies with a wide range of gas conditions. In this test, we generate SLEDs based on gas conditions reported in the literature that were determined with similar modeling of ^{12}CO lines. We include a variety of objects from the literature, which can generally be placed in one of three categories: Milky Way-like – relatively quiescent galaxies with ^{12}CO SLEDs that peak at $J < 5$; DSFGs and ULIRGs – galaxies with active star formation and SLEDs peaking at $5 \leq J < 7$; and QSOs – galaxies in which heating in the nuclear regions drives the SLEDs to peak at $J > 7$. For each of 22 SPT DSFGs, we randomly assign the galaxy to be represented by a single gas component model drawn from literature objects. We add

normally-distributed noise to each line in accordance with the typical S/N of our observed ^{12}CO lines (median S/N ~ 8). Finally, we calculate the average SLED, using only those lines from each object that were observed in our sample (such that, for example, the CO(1-0) line is an average of five input objects). The results of this test are shown in Figure 10, right. While avoiding the term ‘‘average’’ due to its natural mathematical connotation, conditions representative of the inputs are recovered despite the variety of conditions used to generate the input spectra. Conditions are recovered similarly well when the averaging is performed on each of the three categories of sources individually. The results of this test indicate that the uncertainty in determining gas conditions is largely dominated by the systematic uncertainty and degeneracies introduced by the radiative transfer modeling itself, rather than from the scatter of the conditions which produce the variety of observed ^{12}CO SLEDs.

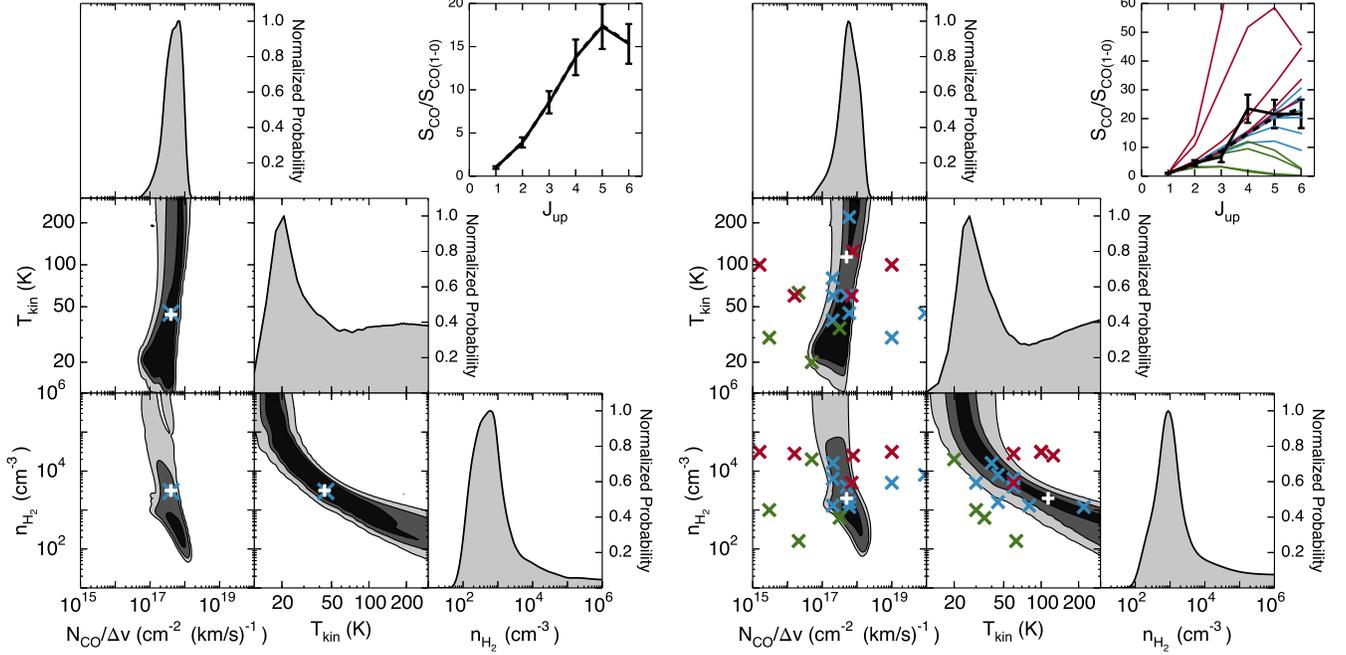


Figure 10. *Left:* Parameter degeneracies in the recovery of a single set of input conditions. The input conditions are marked in each two-dimensional marginalization as an ‘X.’ As before, contours are 1, 2 and 3σ . The upper right panel shows the modeled SLED for the input conditions (solid black line with error bars), and the best-fit model SLED (black dashed line). Unsurprisingly, the best-fit model SLED is essentially identical to the model SLED. The conditions corresponding to this best-fit SLED are shown with a white ‘+’ symbol in the marginalized parameter distributions. *Right:* Parameter degeneracies when fitting the average spectrum derived from objects with a wide range of conditions, using a stacking procedure similar to that used for the SPT DSFGs themselves. Objects with QSO-like SLEDs are colored red, DSFG-like SLEDs are blue, and Milky Way-like SLEDs are shown in green. The upper right panel includes the SLEDs of all the objects used to create the average SLED (colored lines), in addition to the average spectrum (solid black line with error bars) and best-fit model SLED (black dashed line). Again, the conditions corresponding to the best-fit SLED are shown with a white ‘+’ symbol.