

## ISM EXCITATION AND METALLICITY OF STAR-FORMING GALAXIES AT $Z \simeq 3.3$ FROM NEAR-IR SPECTROSCOPY

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### ABSTRACT

We study the relationship between stellar mass, star formation rate (SFR), ionization state, and gas-phase metallicity for a sample of 41 normal star-forming galaxies at  $3 \lesssim z \lesssim 3.7$ . The gas-phase oxygen abundance, ionization parameter, and electron density of ionized gas are derived from rest-frame optical strong emission lines measured on near-infrared spectra obtained with Keck/MOSFIRE. We remove the effect of these strong emission lines in the broad-band fluxes to compute stellar masses via spectral energy distribution fitting, while the SFR is derived from the dust-corrected ultraviolet luminosity. The ionization parameter is weakly correlated with the specific SFR, but otherwise the ionization parameter and electron density do not correlate with other global galaxy properties such as stellar mass, SFR, and metallicity. The mass–metallicity relation (MZR) at  $z \simeq 3.3$  shows lower metallicity by  $\simeq 0.7$  dex than that at  $z = 0$  at the same stellar mass. Our sample shows an offset by  $\simeq 0.3$  dex from the locally defined mass–metallicity–SFR relation, indicating that simply extrapolating such relation to higher redshift may predict an incorrect evolution of MZR. Furthermore, within the uncertainties we find no SFR–metallicity correlation, suggesting a less important role of SFR in controlling the metallicity at high redshift. We finally investigate the redshift evolution of the MZR by using the model by Lilly et al. (2013), finding that the observed evolution from  $z = 0$  to  $z \simeq 3.3$  can be accounted for by the model assuming a weak redshift evolution of the star formation efficiency.

*Keywords:* galaxies: evolution — galaxies: formation — galaxies: high-redshift — galaxies: abundances — galaxies: stellar content

### 1. INTRODUCTION

It is well established that, up to redshift  $z \simeq 6$ , the star formation rate (SFR) of star-forming galaxies (SFGs) tightly correlates with their stellar mass ( $M_*$ ), producing a so-called star-forming main-sequence (MS) where the specific SFR (sSFR  $\equiv$  SFR/ $M_*$ ) depends only weakly on stellar mass (e.g., Brinchmann et al. 2004; Daddi et al. 2007; Elbaz et al. 2007; Noeske et al. 2007; Pannella et al. 2009, 2015; Magdis et al. 2010; Peng et al. 2010; Karim et al. 2011; Rodighiero et al. 2011, 2014; Whitaker et al. 2012, 2014; Kashino et al. 2013; González et al. 2014; Speagle et al. 2014; Steinhardt et al. 2014; Renzini & Peng 2015). While the normalization of the MS increases by a factor of  $\gtrsim 20$  from  $z = 0$  to  $z = 2$ , the scatter ( $\simeq 0.3$  dex) and slope of the MS are almost independent of redshift over the entire  $0 \lesssim z \lesssim 4$  period (e.g., Salmi et al. 2012; Speagle et al. 2014; Schreiber et al. 2015). At  $z \simeq 2$ , the fraction of starbursts defined as SFGs with more than 4 times higher SFR than that of the MS is observationally constrained to be  $\sim 2\%$  of total star-forming population and they account for  $\sim 10\%$  of the cosmic SFR density (Rodighiero et al. 2011), and these fractions appear to be constant up to  $z \simeq 4$  (Schreiber et al. 2015). This indicates that galaxies spend most of

their star-forming phases on the MS due to the interplay of gas inflow, star formation, and gas outflow (e.g., Tacchella et al. 2015b).

The evolution of galaxies on the MS can be attributed to the evolution of baryon accretion into dark matter haloes (e.g., Dutton et al. 2010; Davé et al. 2012; Dekel et al. 2013; Lilly et al. 2013; Forbes et al. 2014; Sparre et al. 2015). Cosmological hydrodynamical simulations are able to reproduce the confinement of SFGs on the MS, with galaxies fluctuating within the observed SFR scatter of the MS in response to fluctuations in the accretion rate (Tacchella et al. 2015b). The simulations can also naturally reproduce the observed trend of the so-called “inside-out quenching” (e.g., Morishita et al. 2015; Nelson et al. 2015; Tacchella et al. 2015a,c): in the early phase the stellar mass profile grows in a self-similar manner, i.e., no or little radial dependence of the sSFR. Then the sSFR in the central part starts being suppressed, once the central density of the bulge reaches a critical value of  $\gtrsim 10^{10} M_\odot \text{ kpc}^{-2}$ , at the expenses of having consumed most of the gas, while star formation and mass growth still continue in the disk (Tacchella et al. 2015d). Eventually, the suppression of star formation takes place in the entire galaxy (Carollo et al. 2014; Tacchella et al. 2015c; Lilly & Carollo, in preparation). This process appears to be rapid at early cosmic times, i.e.  $z \gtrsim 2$ , with a

timescale of  $< 1$  Gyr for massive ( $M \gtrsim 10^{11} M_{\odot}$ ) galaxies (e.g., Onodera et al. 2010b, 2012, 2015; van de Sande et al. 2013; Barro et al. 2015; Belli et al. 2015), while the timescale becomes longer for less massive galaxies at later cosmic times, i.e.,  $z \lesssim 2$  (e.g., Thomas et al. 2005, 2010; McDermid et al. 2015; Tacchella et al. 2015c). Therefore, less massive SFGs will stay on the MS longer before the cessation of star formation, increasing the quenched galaxy population at later epochs (Carollo et al. 2013).

Star formation enriches the gas metal content via supernova explosions and stellar mass loss, and a tight correlation between galaxy stellar mass and gas-phase metallicity ( $Z$ ) in SFGs has been known since 1970s (e.g., Lequeux et al. 1979). The stellar mass–gas-phase metallicity relation (MZR) is now well established for galaxies in the local Universe (Tremonti et al. 2004). Studies of the MZR at high redshifts find systematically lower gas-phase metallicities than in their local counterparts at a given stellar mass, by up to  $\simeq 0.8$  dex at  $z \simeq 3$  (e.g., Carollo & Lilly 2001; Lilly et al. 2003; Kobulnicky & Kewley 2004; Savaglio et al. 2005; Erb et al. 2006a; Maiolino et al. 2008; Mannucci et al. 2009; Yoshikawa et al. 2010; Yabe et al. 2012, 2014; Henry et al. 2013; Cullen et al. 2014; Maier et al. 2014; Masters et al. 2014; Steidel et al. 2014; Troncoso et al. 2014; Zahid et al. 2014; Wuyts et al. 2014; Sanders et al. 2015, see also Hayashi et al. 2009; Onodera et al. 2010a).

The MS and the MZR are likely to be closely related to each other. There is indeed some evidence that the metallicity depends also on SFR as a second parameter in the MZR, leading to a  $Z(M_{\star}, \text{SFR})$  relation (Ellison et al. 2008; Mannucci et al. 2010; Lara-López et al. 2010). These authors found that local SFGs lie on a thin 2-dimensional (2D) surface in the 3D  $M$ – $Z$ –SFR space, with a strikingly small scatter, only 0.05 dex, in metallicity. This surface, dubbed the “fundamental metallicity relation” (FMR), has been suggested to accommodate SFGs up to  $z \simeq 2.5$  (Mannucci et al. 2010; Belli et al. 2013, but see Wuyts et al. 2014), even as the typical SFR at a given stellar mass is higher by a factor of  $\sim 20$ .

The presence of SFR as a second parameter in the MZR follows quite naturally if star formation in galaxies is regulated by their gas reservoir (Bouché et al. 2010; Davé et al. 2012; Krumholz & Dekel 2012; Dayal et al. 2013; Lilly et al. 2013; Forbes et al. 2014). A redshift-independent  $Z(M_{\star}, \text{SFR})$  relation is theoretically predicted if the parameters of the regulator, i.e., the mass-loading of the wind outflow and the star-formation efficiency, are roughly constant in time. Such a gas-regulated model also links the decline of the sSFR in galaxies to the decline of the specific accretion rate of dark matter haloes (with an offset of about a factor of two; Lilly et al. 2013). In this gas-regulation model the gas consumption timescale, that is observationally estimated to be  $\lesssim 1$  Gyr for MS galaxies (e.g., Daddi et al. 2010; Genzel et al. 2010), is shorter than the mass increase timescale, i.e.,  $\text{sSFR}^{-1}$ , so that a quasi-steady-state is maintained between inflow, star formation and outflow. However, at very high redshifts,  $z \gtrsim 3$ , the gas-regulator may break down as a number of timescales tend to converge, namely the gas depletion timescale, the halo dynamical time, and the mass increase timescale of galaxies. An important diagnostics of this break down

would may come from changes in the  $Z(M_{\star}, \text{SFR})$  relation.

Some indication that the fundamental  $Z(M_{\star}, \text{SFR})$  relation breaks down at  $z > 2.5$  has indeed been reported (Mannucci et al. 2010; Troncoso et al. 2014). However, the samples studied so far at  $z > 2.5$  do not include the most massive galaxies, i.e.,  $M \simeq 10^{11} M_{\odot}$  despite the claim that the evolution of the  $Z(M_{\star}, \text{SFR})$  relation may be more prominent at high stellar mass regime (Troncoso et al. 2014, but see Zahid et al. 2014). Also, this depends on how the local  $Z(M_{\star}, \text{SFR})$  relation is extrapolated into regions of  $(M_{\star}, \text{SFR})$  that are poorly populated at low redshifts (i.e., high stellar mass and high SFR; Maier et al. 2014).

Therefore, firmly establishing whether, and with which functional form, the  $Z(M_{\star}, \text{SFR})$  relation extends beyond  $z \sim 3$  could provide an important clue on the regulation of star formation in galaxies at such earlier epochs. In order to properly assess the existence and form of a  $Z(M_{\star}, \text{SFR})$  relation at  $z \gtrsim 3$ , it is essential to measure gas metallicities for a large number of galaxies spanning a broad range of stellar mass and SFR, including also a fair number of the most massive objects.

In this study, we use the Multi-Object Spectrograph for Infra-Red Exploration (MOSFIRE; McLean et al. 2010, 2012) on the Keck I telescope to obtain rest-frame optical emission lines that enable us to measure the gas-phase oxygen abundance,  $12 + \log(\text{O}/\text{H})$ , for a sample of SFGs at  $3 \lesssim z \lesssim 3.7$ .

Compared to the previous study of Troncoso et al. (2014), our sample and data offer several advantages: galaxies are selected in a single field, i.e., the COSMOS field, enabling us to use homogeneous multi-band photometry; our sample includes more objects with measured metallicity and extends to  $M_{\star} \simeq 10^{11} M_{\odot}$ ; resolving the  $[\text{O II}]\lambda\lambda 3726, 3729$  doublet allows us to estimate the electron density of the ionized gas. Using the measured metallicity and wealth of multi-wavelength dataset, we then study the  $Z(M_{\star}, \text{SFR})$  relation at the critical epoch to test the gas-regulator model of star formation in galaxies.

In Section 2, we introduce our data used in this study. Basic measurements of emission lines, AGN contamination, SED fitting, SFR, and spectral stacking procedure are presented in Section 3, and measurements of the ionized gas properties are reported in Section 4. In Section 5, we discuss the relation between the ionized gas properties and other galaxy properties such as stellar mass and SFR. We summarize our results in Section 6.

Throughout the analysis, we adopt a  $\Lambda$ -dominated cold dark matter ( $\Lambda$ CDM) cosmology with cosmological parameters of  $H_0 = 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$ ,  $\Omega_m = 0.3$ , and  $\Omega_{\Lambda} = 0.7$  and AB magnitude system (Oke & Gunn 1983). Unless explicitly stated, we refer “metallicity” and “ $Z$ ” with the same meaning as “gas-phase oxygen abundance” or “ $12 + \log(\text{O}/\text{H})$ ” and we use a base 10 for logarithm.

## 2. DATA

### 2.1. Sample selection

Our primary goal of the project is to measure metallicity at  $z \gtrsim 3$  using strong rest-frame optical emission lines such as  $[\text{O II}]\lambda\lambda 3726, 3729$ ,  $\text{H}\beta$ , and  $[\text{O III}]\lambda\lambda 4959, 5007$ . At  $3 < z < 3.8$ ,  $[\text{O II}]\lambda\lambda 3726, 3729$  are observed in  $H$ -

band and  $H\beta$  and  $[\text{O III}]\lambda\lambda 4959, 5007$  can be accessible in  $K$ -band.

Our primary sample has been extracted from zCOSMOS-Deep redshift catalog (Lilly et al. 2007, and in preparation). We have first selected objects in the redshift range  $3 < z_{\text{spec}} < 3.8$  which are spectroscopically classified as galaxies (i.e., neither stars nor broad-line AGN) and the redshifts are reliable with confidence classes (CC) in the range of  $2.5 \leq \text{CC} \leq 4.5$  which includes some insecure spectroscopic redshifts but which agree well with photometric redshifts (see Table 1 in Lilly et al. 2009). Then we have given higher priority for those with the expected line positions of  $[\text{O II}]\lambda 3727$ ,  $H\beta$ , and  $[\text{O III}]\lambda 5007$  being away more than 2 MOSFIRE resolution element (i.e.,  $R \sim 3600$ ) from the nearest OH line. Since it is expected that spectroscopic redshifts at  $z \sim 3$  in the optical spectra have been determined primarily by the presence of  $\text{Ly}\alpha$ , and a velocity offset in  $\text{Ly}\alpha$  relative to the systemic velocity is also expected (Erb et al. 2014; Finkelstein et al. 2011; Hashimoto et al. 2013; McLinden et al. 2011), we gave lower priority for those with some degree of OH contamination instead of fully excluding them from the sample.

The number density of the zCOSMOS-Deep selected objects is  $\lesssim 5$  per MOSFIRE FoV, so we filled the remaining multiplex with various classes of galaxies in the 2014 run which will be presented elsewhere. On the other hand, in the 2015 run, star-forming galaxies at  $3 < z_{\text{phot}} < 3.8$  have been selected from the 30 band COSMOS photometric redshift catalog on UltraVISTA photometry (McCracken et al. 2012; Ilbert et al. 2013). We have further selected objects with predicted  $H\beta$  flux of  $> 5 \times 10^{-18} \text{ erg s}^{-1} \text{ cm}^{-2}$  scaled from SFR in the catalog to  $H\alpha$  flux by using a conversion of Kennicutt & Evans (2012), assuming an intrinsic  $H\alpha/H\beta$  ratio of 2.86, and applying dust extinction by using  $E(B - V)_{\text{star}}$  from the catalog with the Calzetti extinction law (Calzetti et al. 2000). Conservatively, we adopt  $E(B - V)_{\text{gas}} = E(B - V)_{\text{star}}/0.44$  extinction in  $H\beta$  following the original recipe of Calzetti et al. (2000), though some studies suggest the factor appears to be closer to unity at high redshifts (e.g., Kashino et al. 2013; Panella et al. 2015). A MOSFIRE FoV typically contains  $\sim 25$  these photo- $z$  objects, which is enough to fill the multiplex.

Finally, we observed 54 objects, one of which was observed in both observing runs, with 43 of them having robust spectroscopic identification by one or more emission lines in the MOSFIRE spectra. Table 1 summarizes our sample of 43 objects with detected emission lines.

## 2.2. Observation and data reduction

Observation has been carried out on 20–22 Jan 2014 and 15 Jan 2015 using MOSFIRE on Keck-I (McLean et al. 2010, 2012). We used  $1''$  and  $0''.7$  slit width in 2014 and 2015 runs, respectively, which provides instrumental resolution of  $R \simeq 2500$  and  $3600$ , respectively. We observed in  $J$ ,  $H$ , and  $K$  gratings in the 2014 run because there are some lower redshift objects for which  $[\text{O II}]\lambda 3727$  falls into  $J$ -band, while only  $H$  and  $K$  gratings are used in the 2015 run. Following the exposure recommendation, we used 120 s, 120 s, and 180 s per exposure in  $J$ ,  $H$ , and  $K$  band, respectively. Exposure was done in a sequence of either AB or ABBA dithering

with a distance between A and B positions of  $2''.5$ . The Observing run and total exposure time for each object in  $H$  and  $K$  bands are listed in Table 1.

We observed a couple of white dwarfs and A0V stars per night, using them as standard stars for flux calibration.

Data were reduced with the MOSFIRE data reduction pipeline version 1.1<sup>1</sup> for the science frames and its Longslit branch to make the standard star reduction consistent with the science frames. The pipeline performs flat-fielding, wavelength calibration, sky subtraction, rectification and coaddition of each exposure, and produces rectified two-dimensional (2D) spectra with associated noise as well as exposure maps. One-dimensional (1D) spectra were extracted with  $0''.7$ – $1''$  aperture depending on the spatial extent of detected emission lines to maximize the signal-to-noise ratio (S/N). Corresponding 1D noise spectra were also extracted from 2D noise spectra by using the same aperture and summing them up in quadrature. Flux calibration was carried out using the standard star closest in time to the corresponding science exposure. At the same time with the telluric correction, we also carried out absolute flux calibration by scaling the observed standard star spectra to 2MASS magnitudes correcting for the slit loss for a point source.

## 3. BASIC MEASUREMENT

In this section, we describe the measurements of emission line fluxes, stellar population properties, dust extinction, and SFR. We also present two AGN in our sample, and spectral stacking in bins of stellar mass and SFR.

Among the 54 observed objects at  $3 \lesssim z \lesssim 3.8$ , 43 show clear detection of emission lines which allow us to measure the line properties, while 11 objects show either non-detection or very faint spectral features with too low S/N, so that we are not able to claim a detection. Among the 11 objects with non-detection, 2 objects were selected from the zCOSMOS-Deep catalog. One of them was in a slit which did not work properly, and the other is a filler object with  $\text{CC} = 2.1$  and its photometric redshift  $z_{\text{phot}} = 0.53$  differs substantially from the spectroscopic one. The rest of the objects with non-detection of emission lines were photometrically selected. We speculate that the main reasons of non-detections could be either wrong photometric redshifts or wrong emission line flux predictions propagated from the best-fit SED parameters. Also, in some of these objects emission lines may have been obliterated by the OH air glow. In the following analysis, we focus on the 43 objects with detected emission lines.

### 3.1. Emission line measurement

The emission lines are fit in two steps. In the first step,  $[\text{O II}]\lambda 3726$ ,  $[\text{O II}]\lambda 3729$ ,  $H\beta$ ,  $[\text{O III}]\lambda 4959$ , and  $[\text{O III}]\lambda 5007$  are fit simultaneously. We assume that each emission line can be described by a simple Gaussian redshifted by the same amount with a common velocity dispersion  $\sigma_{\text{vel}}$  on a constant continuum component. Therefore, free parameters of the first fitting step are redshift, velocity dispersion, flux of each emission line,

<sup>1</sup> <https://keck-datareductionpipelines.github.io/MosfireDRP>

**Table 1**  
Properties of the galaxy sample and the observation log.

ID	R.A. (deg)	Decl. (deg)	$z_{\text{phot}}$	$z_{\text{zCOSMOS}}$	Run	$t_{\text{exp},H}$ (min)	$t_{\text{exp},K}$ (min)	$B_{\text{AB}}$ (mag)	$Ks_{\text{AB}}^{\text{a}}$ (mag)
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)
434625	150.09385	2.421970	3.155	3.0717	2014	28	30	25.29	25.38
413136	150.10600	2.436190	2.838	3.1911	2014	28	30	24.91	22.99
413646	150.08025	2.469180	3.132	3.0389	2014	28	30	25.23	23.70
413453	150.13365	2.457430	3.121	3.1892	2014	28	30	25.07	22.24
434585	149.84702	2.373020	3.435	3.3557	2014	28	30	24.66	22.82
434571	149.83784	2.362050	3.142	3.1292	2014	28	30	25.77	24.36
413391	149.78424	2.452890	3.469	3.3626	2014	28	30	24.78	22.44
427122	150.07483	2.032280	2.917	3.0454	2014	28	30	25.14	24.64
434148	150.03551	1.965090	3.144	3.1457	2014	28	30	25.13	23.63
434082	150.35009	1.904380	3.449	3.4750	2014	28	42	24.34	22.65
434126	150.37178	1.947200	3.427	3.2715	2014	28	42	25.35	23.76
434139	150.38895	1.956150	3.108	3.0355	2014	28	42	24.86	23.74
434145	150.40089	1.963460	3.442	3.4208	2014	28	42	25.35	23.05
434242	150.29841	2.075330	3.271	3.2376	2014	28	30	25.74	24.04
406390	150.29878	2.068820	3.149	3.0487	2014	28	30	25.05	23.41
406444	150.33032	2.072270	3.400	3.3060	2014	28	30	24.45	21.71
434227	150.32680	2.053940	3.355	3.2136	2014	28	30	24.71	22.57
191932	150.27605	2.299900	3.414	...	2015	56	72	26.03	23.41
434547	150.27003	2.333980	3.261	3.1875	2015	56	72	25.49	23.54
192129	150.30078	2.300540	3.457	3.5002	2015	56	72	24.83	22.89
193914	150.31923	2.306690	3.023	...	2015	56	72	24.65	23.43
212863	150.29286	2.367090	3.372	...	2015	56	72	26.14	23.69
195044	150.32696	2.310780	3.185	3.1149	2015	56	72	25.14	23.38
208115	150.31325	2.351720	3.661	...	2015	56	72	25.71	22.52
200355	150.33103	2.327790	3.476	...	2015	56	72	25.87	23.48
214339	150.31607	2.372240	3.392	...	2015	56	72	25.94	22.44
411078	150.35142	2.322420	3.106	3.1104	2015	56	72	23.84	22.44
212298	150.34268	2.365390	3.107	3.1024	2015	56	72	25.26	22.79
412808	149.83413	2.416690	3.274	3.3050	2015	72	84	25.05	24.13
223954	149.83188	2.404150	3.436	...	2015	72	84	25.62	23.75
220771	149.83628	2.393190	3.473	...	2015	72	84	26.63	24.64
219315	149.83952	2.388460	3.240	...	2015	72	84	25.72	23.90
434618	149.89213	2.414710	3.289	3.2819	2015	72	84	25.18	23.24
221039	149.86938	2.394510	3.069	...	2015	72	84	25.00	23.05
215511	149.84826	2.376170	3.424	...	2015	72	84	26.33	23.92
217597	149.86534	2.382770	3.415	...	2015	72	84	26.76	24.06
211934	149.84725	2.364040	3.773	...	2015	72	84	28.08	24.44
434579	149.86179	2.366931	3.145	3.1889	2015	72	84	26.16	23.87
217753	149.89451	2.383700	3.438	...	2015	72	84	26.51	23.06
218783	149.92082	2.387060	3.504	...	2015	72	84	25.57	22.80
217090	149.91827	2.381250	3.669	...	2015	72	84	26.21	24.41
210037	149.90451	2.357800	3.579	...	2015	72	84	27.06	24.33
208681	149.90551	2.353990	3.342	3.2671	2015	72	84	24.20	22.17

**Note.** — (1) Object ID; (2) Right ascension; (3) Declination; (4) Photometric redshift from [Ilbert et al. \(2013\)](#); (5) Spectroscopic redshift from zCOSMOS-Deep; (6) Observing run; (7) Exposure time in  $H$ -band; (8) Exposure time in  $Ks$ -band; (9)  $B$ -band total magnitude; (10)  $Ks$ -band total magnitude.

<sup>a</sup>  $Ks$  magnitudes are not corrected for emission lines.

and continuum component. The continuum is assumed to be a constant within each band, i.e., [O II] $\lambda$ 3726 and [O II] $\lambda$ 3729 have the same continuum in  $H$ -band and so do  $H\beta$ , [O III] $\lambda$ 4959, and [O III] $\lambda$ 5007 in  $K$ -band. In the second step, [Ne III] $\lambda$ 3869, H $\delta$ , [Ne III] $\lambda$ 3969 + He $\epsilon$ , H $\delta$ , and H $\gamma$  are fit individually by fixing the redshift and line width derived in the first path and leaving the line flux and constant continuum as free parameters. We used MPFIT<sup>2</sup> ([Markwardt 2009](#)) for the fitting. During the procedure, we put constraints on  $\sigma_{\text{vel}}$  and emission line fluxes to be larger than the instrumental resolution and to be positive, respectively.

To obtain each parameter and the associated uncertainty, we carried out a Monte Carlo simulation by perturbing each pixel value of the spectra with the associ-

ated noise multiplied by a normally distributed random number. Mean and standard deviation of the measured distribution of  $10^3$  realizations are adopted for each parameter and its  $1\sigma$  uncertainty ( $\sigma_{\text{MC}}$ ), respectively. The best-fit spectra and observed 1-dimensional spectra are shown in [Figure A1](#). We computed another  $1\sigma$  error ( $\sigma_{\text{direct}}$ ) for each emission line flux directly from the associated noise spectrum by integrating  $\pm 2\sigma_{\text{vel}}$  from the line center in quadrature. In the case of  $F_{\text{MC}}/\sigma_{\text{direct}} > 3$ , where  $F_{\text{MC}}$  is flux measured by the Monte Carlo simulation, we claim the detection of the emission line and use  $\sigma_{\text{MC}}$  as the corresponding  $1\sigma$  error. Otherwise, we adopt  $3\sigma_{\text{direct}}$  as the  $3\sigma$  upper limit.

Measured  $H\beta$  fluxes were corrected for underlying stellar absorption by assuming  $\text{EW}(H\beta) = 2 \text{ \AA}$  ([Nakamura et al. 2004](#)). To compute EW, the continuum flux was estimated from the total  $Ks$ -band magnitude. The re-

<sup>2</sup> <http://www.physics.wisc.edu/~craigm/idl/fitting.html>

sulting correction factor is up to  $\simeq 20\%$  with a median of  $3\%$ .

**Table 2** lists measured redshifts, reddening uncorrected emission line fluxes, and correction factors applied to stellar  $H\beta$  absorption.

In **Figure 1**, the MOSFIRE spectroscopic redshifts are compared with those from zCOSMOS-Deep or with photometric redshifts. Agreement between MOSFIRE and zCOSMOS-Deep spectroscopic redshifts is almost perfect with a standard deviation of 0.004 in ( $z_{\text{MOSFIRE}} - z_{\text{zCOSMOS}}$ ). Photometric redshifts also agree well with the spectroscopic ones with no catastrophic failure. The normalized median absolute deviation of ( $z_{\text{MOSFIRE}} - z_{\text{phot}}$ )/(1 +  $z_{\text{MOSFIRE}}$ ) is 0.027 which is consistent with what reported in [Ilbert et al. \(2013\)](#) for high redshift galaxies. The redshifts of our sample are in a range of  $2.97 < z < 3.69$ , with a median of 3.27.

### 3.2. Note on AGN contamination

There are two AGN candidates in the sample which are excluded in the following analysis as nuclear activity is not the main focus of this paper. The object, 413453, has an X-ray counterpart detected in the *Chandra*-COSMOS survey (CID 3636 in [Civano et al. 2011](#)) as well as in the more recent *Chandra* COSMOS Legacy Survey ([Marchesi et al. 2016](#); [Civano et al. 2016](#)). Although the object is not classified as a broad-line AGN in the zCOSMOS-Deep catalog, it actually shows C IV $\lambda$ 1549 emission in the optical spectra. Therefore, the [O III] and  $H\beta$  emission lines are likely to be contaminated by nuclear activity.

Object 208115 is not detected in X-ray but it shows very strong [Ne III] $\lambda$ 3869 emission with [Ne III] $\lambda$ 3869/[O II] $\lambda$ 3727  $\simeq 2.5$  and [O III] $\lambda$ 4363/ $H\gamma$   $\simeq 0.7$ , which appears to be due to AGN rather than star formation. The median values of [O III] $\lambda$ 4363/ $H\gamma$  for the local star-forming galaxies and AGN sample presented by [Shirazi & Brinchmann \(2012\)](#) are 0.13 and 0.39, respectively (M. Shirazi, private communication; see also [Francis et al. 1991](#); [Vanden Berk et al. 2001](#)).

### 3.3. Stellar population properties

In this section, we carry out the spectral energy distribution (SED) fitting to the broad-band photometry. We started from the PSF-homogenized UltraVISTA photometry catalog ([McCracken et al. 2012](#))<sup>3</sup>. Since our objects are in a narrow redshift range and have small angular extent (**Figure B1**), we adopted *uBVrizYJHK* aperture magnitudes measured within  $2''$  apertures. These magnitudes were first corrected for the Galactic extinction based on the calibration of dust map by [Schlafly & Finkbeiner \(2011\)](#) and a extinction curve by [Fitzpatrick \(1999\)](#) with  $R_V = 3.1$ . Then the aperture correction to the total magnitude was made by applying an average difference between aperture and AUTO magnitudes across the used photometric bands. Finally, 0.369 mag was subtracted from *B*-band magnitude as instructed in the README file of the catalog<sup>4</sup>. Since one of the ob-

jects (434579) does not have a counterpart in the UltraVISTA catalog, but found in the previous CFHT/WIRC *K*-selected catalog ([McCracken et al. 2010](#)), we adopted the photometry from the latter. Optical-NIR photometry was then matched with *Spitzer*/IRAC photometry in 4 channels by the S-COSMOS survey ([Sanders et al. 2007](#)) with a search radius of 1 arcsec. We used  $1''.9$  aperture flux and corrected it for total flux by using conversion factors listed in the README file of the catalog.

#### 3.3.1. Correction for emission line contributions in broad-band magnitudes

Given the detection of strong emission lines in our MOSFIRE spectra, a significant contribution from them to the broad band flux is expected (e.g., [Schaerer et al. 2013](#); [Stark et al. 2013](#)). We have estimated the contribution by comparing the broad-band magnitudes and emission line fluxes. The contribution of [O II] $\lambda\lambda$ 3726, 3729 to *H*-band flux ranges from 1.2 to 80%, with a median of 5.7% and 8 objects contributing  $> 10\%$ . In the *K*-band,  $H\beta$  and [O III] $\lambda\lambda$ 4959, 5007 contribute from 6 to  $\sim 100\%$  with a median of 21% and 6 objects showing  $> 50\%$ . In the case of the very high contributions, close to 100%, the continuum broad-band magnitudes are close to the detection limit.

Looking at the optical spectra from zCOSMOS-Deep, we have also estimated the contribution of Ly $\alpha$  to *V*-band magnitudes. There are 20 objects with zCOSMOS-Deep spectra and 7 of them shows Ly $\alpha$  in emission, which contributes less than 10% of the broad-band flux.

Another strong rest-frame optical emission line,  $H\alpha$ , does not contribute any of broad-band fluxes considered here, since it is located in the gap between the *K*-band and the IRAC 3.6  $\mu\text{m}$  band at the redshift of our sample.

We have corrected *H*- and *K*-band magnitudes for the emission lines, while no correction has been applied for Ly $\alpha$  given its minor contribution to the broad-band flux.

#### 3.3.2. SED fitting

SED fitting was carried out for the emission line corrected photometry by using the template SED-fitting code ZEBRA+ which is an updated version of photometric redshift code ZEBRA<sup>5</sup> ([Feldmann et al. 2006](#)). Redshifts were set to the spectroscopic ones. As templates, we used composite stellar population models generated from the simple stellar population models of [Bruzual & Charlot \(2003\)](#) with a Chabrier initial mass function (IMF; [Chabrier 2003](#)). We employed an exponentially declining star formation history (SFH),  $\propto \exp(-t/\tau)$ , with  $\log \tau/\text{yr} = 8-11$  with steps of 0.1 dex. Ages range in  $\log \text{age}/\text{yr} = 6-9.5$  with steps of 0.1 dex where the upper limit of the age is chosen to be an approximate age of the universe at  $z = 3$ . Metallicities of  $0.2Z_{\odot}$ ,  $0.4Z_{\odot}$ , and  $Z_{\odot}$  were used. We also allowed dust extinction with  $E(B - V) = 0-0.8$  mag with steps of 0.05 mag following the Calzetti extinction curve ([Calzetti et al. 2000](#)). The median values of stellar mass<sup>6</sup>, SFR,  $\tau$ , age,  $A_V$ ,

preparation). The former zero-point suffered from the uncertainty caused by the combination of sharp Balmer absorption features of the calibration stars and the location of the blue edge of the filter which is sensitive to temperature and humidity, while the latter is less sensitive to exact knowledge of the bandpass.

<sup>5</sup> <http://www.astro.ethz.ch/carollo/research/zebra.html>

<sup>6</sup> Sum of living stars and remnants.

<sup>3</sup> [http://terapix.iap.fr/article.php?id\\_article=844](http://terapix.iap.fr/article.php?id_article=844)

<sup>4</sup> This offset was introduced to convert the photometric zero-point in [Capak et al. \(2007\)](#) derived by using spectrophotometric standard stars to that based on sources with flat spectrum such as moderate redshift galaxies ([Ilbert et al. 2009, 2013](#); [Laigle et al., in](#)

**Table 2**  
Emission line measurements.

ID (1)	$z_{\text{MOSFIRE}}$ (2)	$F([\text{O II}]\lambda 3727)$ (3)	$F([\text{Ne III}]\lambda 3869)$ (4)	$F(\text{H}\beta)^{\text{a}}$ (5)	$F([\text{O III}]\lambda 4959)$ (6)	$F([\text{O III}]\lambda 5007)$ (7)	$f_{\text{corr}}(\text{H}\beta)$ (8)	$f_{\text{em},H}$ (9)	$f_{\text{em},K}$ (10)
434625	3.07948	$2.41 \pm 0.27$	$< 0.88$	$< 1.40$	$1.70 \pm 0.18$	$5.28 \pm 0.20$	1.00	0.07	1.00
413136	3.19037	$< 3.56$	$< 1.21$	$1.17 \pm 0.31$	$< 0.71$	$1.84 \pm 0.31$	1.10	0.00	0.08
413646	3.04045	$< 6.75$	$< 2.31$	...	$< 3.61$	$3.95 \pm 0.31$	1.00	0.00	0.21
413453	3.18824	$< 4.84$	$< 3.05$	$< 2.64$	$2.89 \pm 0.31$	$10.27 \pm 0.35$	1.00	0.00	0.14
434585	3.36345	$2.94 \pm 1.23$	$< 3.69$	$1.56 \pm 0.46$	$< 1.14$	$3.77 \pm 0.96$	1.09	0.07	0.12
434571	3.12729	$< 3.57$	$< 4.23$	...	$1.24 \pm 0.11$	$3.03 \pm 0.19$	1.00	0.00	0.30
413391	3.36544	$3.16 \pm 0.47$	$< 3.71$	$0.91 \pm 0.26$	$2.22 \pm 0.24$	$4.84 \pm 0.69$	1.22	0.04	0.09
427122	3.04157	$< 2.24$	$< 0.47$	$0.44 \pm 0.13$	$< 0.66$	$1.90 \pm 0.14$	1.04	0.00	0.29
434148	3.14780	$1.29 \pm 0.24$	$< 0.30$	$< 0.51$	$< 0.61$	$2.26 \pm 0.10$	1.00	0.04	0.11
434082	3.46860	$5.84 \pm 0.38$	...	$4.33 \pm 0.33$	$6.97 \pm 0.41$	$20.96 \pm 0.51$	1.02	0.08	0.49
434126	3.27209	$2.90 \pm 0.40$	$< 0.87$	$1.19 \pm 0.23$	$2.14 \pm 0.34$	$7.93 \pm 0.36$	1.03	0.10	0.50
434139	3.03623	$< 7.31$	$< 0.79$	$< 1.83$	$< 3.41$	$6.25 \pm 0.42$	1.02	0.00	0.35
434145	3.42400	$5.15 \pm 0.77$	$< 4.47$	$< 3.23$	$3.65 \pm 0.48$	$11.91 \pm 0.48$	1.02	0.09	0.35
434242	3.23290	$1.44 \pm 0.34$	$< 1.44$	$1.37 \pm 0.34$	$2.16 \pm 0.18$	$6.98 \pm 0.33$	1.01	0.28	0.59
406390	3.05272	$2.16 \pm 0.57$	$< 0.56$	$< 2.31$	$< 1.39$	$4.35 \pm 0.48$	1.00	0.06	0.18
406444	3.30355	$5.15 \pm 0.80$	$1.27 \pm 0.27$	$2.86 \pm 0.34$	$4.27 \pm 0.38$	$9.66 \pm 0.73$	1.13	0.01	0.10
434227	3.21501	$< 2.54$	$< 2.40$	$< 2.06$	$< 2.50$	$5.56 \pm 1.05$	1.00	0.00	0.10
191932	3.18246	$1.50 \pm 0.12$	$< 0.52$	$< 0.57$	$0.92 \pm 0.10$	$2.69 \pm 0.11$	1.14	0.05	0.11
434547	3.19167	$1.33 \pm 0.10$	$< 0.23$	$0.40 \pm 0.05$	$0.90 \pm 0.05$	$2.81 \pm 0.07$	1.16	0.04	0.14
192129	3.49466	$1.82 \pm 0.14$	...	$1.25 \pm 0.12$	$1.44 \pm 0.14$	$3.61 \pm 0.19$	1.10	0.04	0.12
193914	2.96871	$1.76 \pm 0.28$	$0.52 \pm 0.06$	...	$2.01 \pm 0.11$	$6.45 \pm 0.09$	1.00	0.04	0.27
212863	3.29183	$1.83 \pm 0.08$	$< 0.25$	$1.29 \pm 0.11$	$2.05 \pm 0.10$	$5.46 \pm 0.13$	1.03	0.25	0.34
195044	3.11091	$1.42 \pm 0.21$	$< 0.15$	$0.30 \pm 0.11$	$0.26 \pm 0.08$	$0.76 \pm 0.10$	1.00	0.03	0.04
208115	3.63568	$1.49 \pm 0.13$	$3.70 \pm 0.10$	$6.78 \pm 0.16$	$17.99 \pm 0.25$	$53.21 \pm 0.30$	1.00	0.06	1.00
200355	3.56796	$1.71 \pm 0.10$	...	$1.34 \pm 0.15$	$2.94 \pm 0.17$	$7.47 \pm 0.27$	1.04	0.07	0.37
214339	3.60885	$1.59 \pm 0.20$	$< 0.43$	$0.83 \pm 0.18$	$1.34 \pm 0.25$	$3.98 \pm 0.31$	1.27	0.04	0.08
411078	3.11280	$6.07 \pm 0.14$	$1.99 \pm 0.07$	$4.23 \pm 0.20$	$10.26 \pm 0.10$	$29.80 \pm 0.13$	1.02	0.10	0.55
212298	3.10781	$3.97 \pm 0.20$	$0.65 \pm 0.10$	$2.25 \pm 0.11$	$2.54 \pm 0.09$	$7.18 \pm 0.24$	1.05	0.04	0.21
412808	3.30614	$1.48 \pm 0.09$	$0.57 \pm 0.06$	$1.04 \pm 0.08$	$2.25 \pm 0.11$	$7.63 \pm 0.13$	1.01	0.06	0.67
223954	3.37076	$1.72 \pm 0.11$	$< 0.61$	$0.59 \pm 0.13$	$1.30 \pm 0.12$	$3.38 \pm 0.14$	1.09	0.06	0.21
220771	3.35871	$0.77 \pm 0.10$	$0.20 \pm 0.04$	$0.37 \pm 0.08$	$< 0.24$	$1.14 \pm 0.10$	1.06	0.79	0.18
219315	3.36253	$0.96 \pm 0.09$	$0.21 \pm 0.05$	$< 0.23$	$0.75 \pm 0.12$	$1.61 \pm 0.10$	1.00	0.05	0.10
434618	3.28463	$2.45 \pm 0.09$	$< 0.26$	$0.98 \pm 0.08$	$1.72 \pm 0.14$	$5.18 \pm 0.09$	1.08	0.06	0.21
221039	3.05515	$4.67 \pm 0.15$	$0.66 \pm 0.05$	$1.73 \pm 0.08$	$3.00 \pm 0.24$	$8.49 \pm 0.10$	1.05	0.10	0.29
215511	3.36345	$2.44 \pm 0.17$	$0.40 \pm 0.08$	$1.12 \pm 0.13$	$2.32 \pm 0.16$	$5.76 \pm 0.20$	1.03	0.10	0.43
217597	3.28377	$1.69 \pm 0.09$	$0.24 \pm 0.04$	$0.52 \pm 0.10$	$1.39 \pm 0.18$	$3.77 \pm 0.12$	1.06	0.09	0.31
211934	3.35538	$1.32 \pm 0.28$	$< 0.09$	$0.53 \pm 0.16$	$0.43 \pm 0.11$	$1.63 \pm 0.16$	1.05	0.23	0.22
434579	3.18653	$0.82 \pm 0.09$	$< 0.34$	$0.23 \pm 0.07$	$0.54 \pm 0.08$	$1.28 \pm 0.09$	1.22	0.05	0.09
217753	3.25408	$2.38 \pm 0.45$	$< 0.54$	$1.26 \pm 0.21$	$< 0.80$	$1.82 \pm 0.18$	1.09	0.06	0.08
218783	3.29703	$1.91 \pm 0.16$	$< 0.30$	$0.75 \pm 0.10$	$0.87 \pm 0.12$	$2.53 \pm 0.22$	1.19	0.05	0.07
217090	3.69253	$1.69 \pm 0.16$	...	$1.65 \pm 0.19$	$3.25 \pm 0.21$	$9.10 \pm 0.36$	1.00	0.17	1.00
210037	3.69083	$2.07 \pm 0.43$	...	$< 0.61$	$1.10 \pm 0.35$	$4.10 \pm 0.77$	1.00	0.48	0.39
200681	3.26734	$3.58 \pm 0.30$	$< 0.91$	$2.34 \pm 0.16$	$1.04 \pm 0.17$	$3.31 \pm 0.19$	1.11	0.05	0.07

**Note.** — (1) Object ID; (2) Spectroscopic redshift measured from MOSFIRE spectra. The associated  $1\sigma$  error is typically an order of  $\lesssim 10^{-4}$ ; (3)  $[\text{O II}]\lambda 3727$  (i.e.,  $[\text{O II}]\lambda 3726 + [\text{O II}]\lambda 3729$ ) flux; (4)  $[\text{Ne III}]\lambda 3869$  flux; (5)  $\text{H}\beta$  flux; (6)  $[\text{O III}]\lambda 4959$  flux; (7)  $[\text{O III}]\lambda 5007$  flux; (8) Correction factor for  $\text{H}\beta$  absorption assuming  $2 \text{ \AA}$  in the equivalent width; (9) and (10) fraction of emission line contribution in  $H$ - and  $K$ -band, respectively. All fluxes are in unit of  $10^{-17} \text{ erg s}^{-1} \text{ cm}^{-2}$ , and they are not corrected for dust extinction. Quoted upper limits are  $3\sigma$  upper limit.

<sup>a</sup> Fluxes are not corrected for the underlying stellar absorption. To correct it, one need to multiply  $F(\text{H}\beta)$  by  $f_{\text{corr}}(\text{H}\beta)$ .

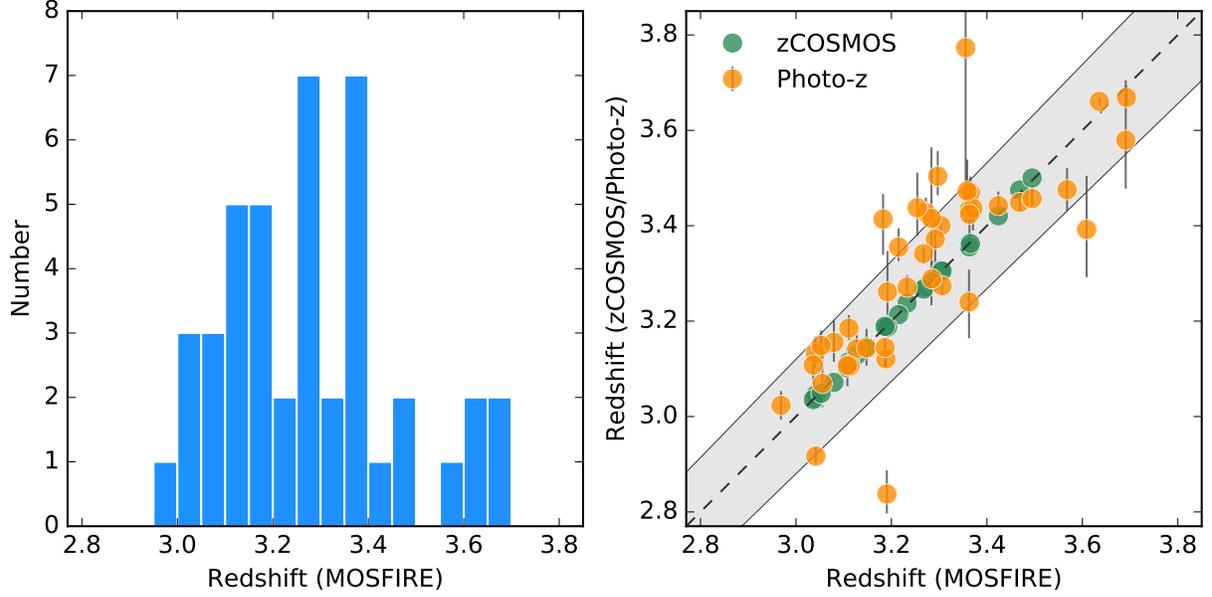
and metallicity and corresponding 68% confidence intervals derived by marginalizing the likelihood distribution were returned as the output. **Figure C1** in **Appendix C** shows the best-fit template and emission line corrected observed photometry.

An exponentially declining SFH may not be the best approximation for SFGs at high redshift (e.g., **Renzini 2009**; **Maraston et al. 2010**; **Reddy et al. 2012**). Although the age derived here is formally meant to be the time elapsed since the onset of star formation, it should actually be regarded as the time interval before the present during which the bulk of stars were formed. Indeed, 85% of the sample show  $\text{age}/\tau < 2$ , which means that the fitting procedure returns a nearly constant SFR. However, in our main analysis of MZR we will use only the stellar mass among the outputs of the SED fitting, as the stellar mass is quite stable against the choice of SFH. For exam-

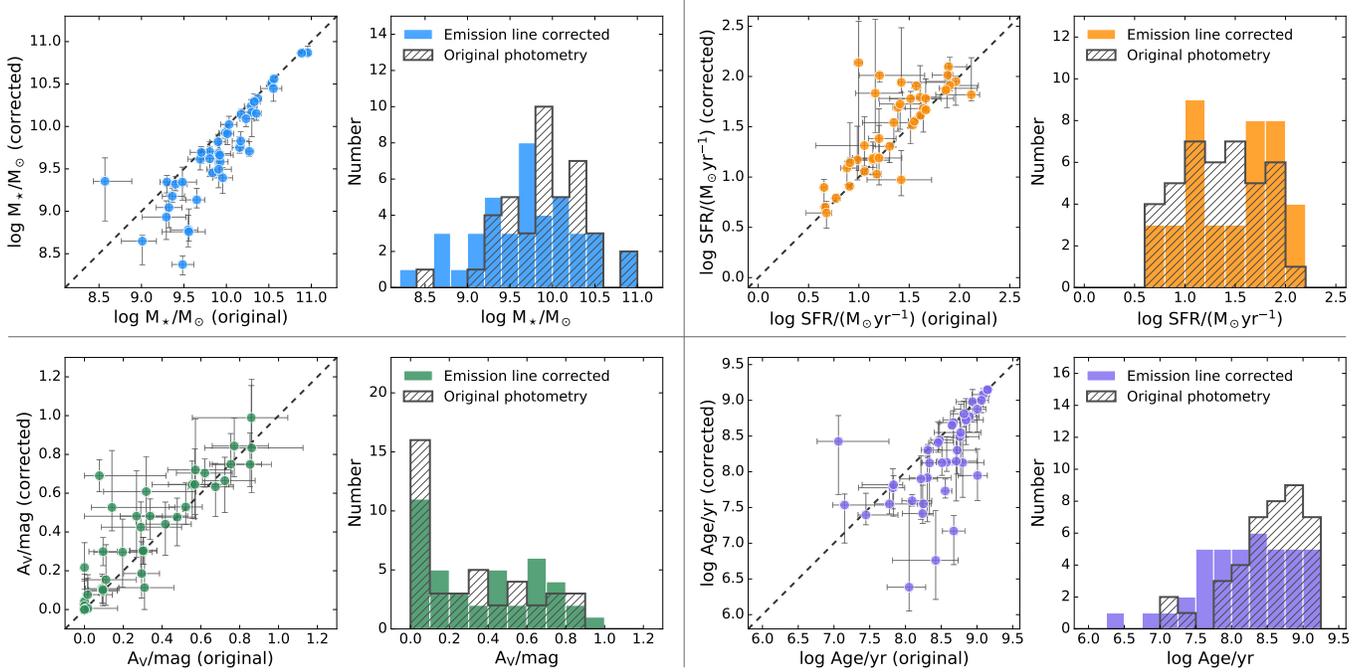
ple, employing a constant or delayed-exponential SFHs would change the stellar mass by only 0.1 dex. On the other hand, the SFR and dust extinction will be derived only from the rest-frame UV properties.

**Figure 2** compares various outputs from the SED fitting based on the original photometry with those derived from emission line corrected photometry, and their distributions. Emission line corrected stellar masses ( $M_{\star}^{\text{corr}}$ ) are generally lower than those from the original photometry ( $M_{\star}^{\text{original}}$ ) and the effect is more prominent in less massive galaxies. The median difference in stellar mass is  $\log M_{\star}^{\text{corr}} - \log M_{\star}^{\text{original}} = -0.13$  dex. On the other hand, the median differences in SFR,  $A_V$ , and age of stellar populations are  $-0.03$ ,  $-0.02$ , and  $0.12$  dex, respectively.

**Figure 3** shows the difference in the best-fit parameters



**Figure 1.** *Left:* MOSFIRE redshift distribution of the sample. *Right:* Comparison of spectroscopic redshifts measured in MOSFIRE spectra with those from zCOSMOS-Deep and photometric redshift from Ilbert et al. (2013).

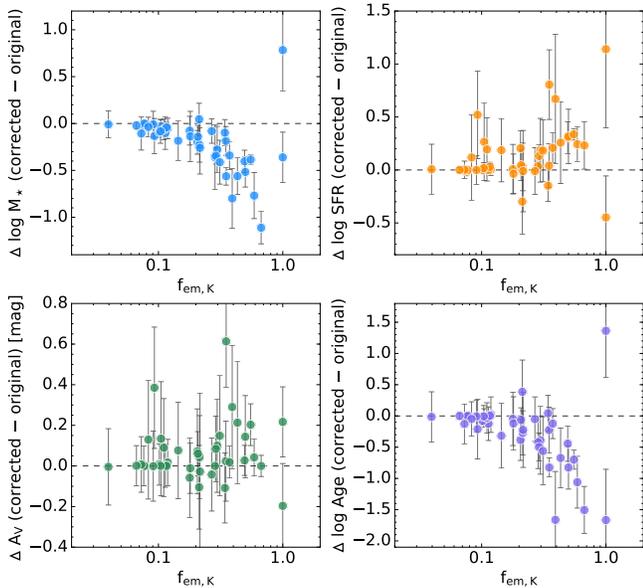


**Figure 2.** At each quadrant, a pair of panels shows the comparison of outputs from SED fitting with and without the corrections for strong emission line contributions to the broad-band fluxes (*Left*) and the distribution of each SED parameter (*Right*). Hatched and color-filled histograms show those derived based on photometry with and without the correction for emission line contributions, respectively. The following parameters are shown: *Top left:* Stellar masses. *Top right:* SFR. *Bottom left:* Attenuation at  $V$ -band,  $A_V$ . *Bottom right:* Age since the onset of star formation.

as a function of the fraction of emission line fluxes in the  $K$ -band. Stellar mass and age show decreasing trends in the difference with increasing emission line contributions. SFRs are also affected by large emission line contributions, but the trend appears weaker than those on stellar mass and age. On the other hand, no clear trend can be seen in  $A_V$ . This can be understood as longer wavelength bands are more sensitive to the stellar mass

and age, while SFR and dust extinction are primarily captured by the rest-frame UV part of the SED, where emission line contribution is not important.

There are two objects, 434625 and 217090, which have a  $\sim 100\%$  contribution from emission lines in the  $K$  band, and they do not seem to follow the general trend of the rest of our sample in Figure 3. These two objects are the only ones without detection both in the  $K$  band (after



**Figure 3.** Difference in the best-fit SED fitting parameters (stellar mass, SFR,  $A_V$ , and age in clockwise from top left panel) between those derived from the original and emission line corrected photometry as a function of the fraction of emission line fluxes in  $K$ -band.

emission-line correction) and in any of the IRAC bands. At  $z \simeq 3.3$ , only observing at wavelengths on and beyond the  $K$  band one can capture the rest-frame wavelength of  $> 4000 \text{ \AA}$  which is essential to properly estimate the mass-to-light ratios of galaxies. This is likely the main reason why the two objects do not follow the trends, especially in stellar mass and age.

All this indicates the importance of a proper assessment of emission line contribution in near-infrared bands at  $z > 3$  (e.g., Schaerer et al. 2013; Stark et al. 2013). In the following analysis, we adopt  $M_*^{\text{corr}}$  for the stellar masses of galaxies in our sample.

#### 3.4. UV slope and dust extinction

We computed the UV spectral slope  $\beta_{\text{UV}}$  defined as  $f_\lambda \propto \lambda^{\beta_{\text{UV}}}$  by fitting a linear function to the observed broad-band magnitudes from the  $r$  to the  $J$  band which cover the rest-frame wavelength range  $1400 \lesssim \lambda \lesssim 2800 \text{ \AA}$  at  $z = 3.27$ . We used the rest-frame wavelengths corresponding to the Galaxy Evolution Explorer (*GALEX*) far-UV (FUV;  $\lambda_c \simeq 1530 \text{ \AA}$ ) and near-UV (NUV;  $\lambda_c \simeq 2300 \text{ \AA}$ ) bands to derive  $\beta_{\text{UV}}$  photometrically, following the recipe used in Pannella et al. (2015). For all objects in the sample, this choice of passbands encloses the rest-frame UV wavelengths with which UV slopes are determined. Following Nordon et al. (2013), magnitude errors are further weighted by  $1 + |\lambda_{\text{filter}} - \lambda_{\text{FUV}}|/\lambda_{\text{FUV}}$ , where  $\lambda_{\text{filter}}$  and  $\lambda_{\text{FUV}}$  are the rest-frame central wavelengths of each photometric band and that of *GALEX* FUV. By using the best-fit relation,  $\beta_{\text{UV}}$  was derived as

$$\beta_{\text{UV}} = \frac{\log(f_{\lambda, \text{FUV}}/f_{\lambda, \text{NUV}})}{\log(\lambda_{\text{FUV}}/\lambda_{\text{NUV}})} \quad (1)$$

$$= -0.4 \frac{(m_{\text{FUV}} - m_{\text{NUV}})}{\log(\lambda_{\text{FUV}}/\lambda_{\text{NUV}})} - 2, \quad (2)$$

where  $m_{\text{FUV}}$  and  $m_{\text{NUV}}$  are the AB magnitudes in the *GALEX* FUV and NUV bands, respectively (Nordon et al. 2013; Pannella et al. 2015). Then assuming the Calzetti extinction law (Calzetti et al. 2000; Pannella et al. 2015),  $\beta_{\text{UV}}$  was converted to dust attenuation at  $\lambda = 1530 \text{ \AA}$  with

$$A_{\text{UV}} = 4.85 + 2.31\beta_{\text{UV}}, \quad (3)$$

which assumes an intrinsic (un-extincted) slope  $\beta_{\text{UV}}(A_V = 0) = -2.10$  (Calzetti et al. 2000).

In Figure 4, the values of  $A_V$  from UV and SED fitting are compared, having converted  $A_{\text{UV}}$  to  $A_V$  by assuming the Calzetti extinction law. There appears to be no tight correlation between the two estimates, perhaps because dust extinction degenerates with other parameters such as SFH and age in broad-band SED fitting (e.g., Kodama et al. 1999; Michałowski et al. 2014). Two outliers, 214339 and 211934, as indicated in Figure 4, turn out to be the faintest galaxies in our sample. Indeed, the broad-band SED of these objects shown in Section C appears to be quite noisy, which makes a robust estimate of  $\beta_{\text{UV}}$  difficult.

Figure 5 shows  $A_{\text{UV}}$  vs. stellar mass. There is a trend with more massive galaxies being more dust attenuated. The sample of  $z \simeq 3.4$  SFGs from Troncoso et al. (2014) is also shown, with on average a higher dust extinction compared to our sample. Note that in their study extinction was derived from broad-band SED fitting, while ours was based on  $\beta_{\text{UV}}$  slope. Troncoso et al. (2014) specifically selected Lyman break galaxies (LBGs) with redshifts from near-IR spectroscopy, while we selected objects partly based on the availability of spectroscopic redshifts, which automatically puts a limit on  $B_{\text{AB}} = 25 \text{ mag}$  for those galaxies culled from the zCOSMOS-Deep sample. Moreover, targets were selected based on the predicted  $H\beta$  flux of  $> 5 \times 10^{-18} \text{ erg s}^{-1} \text{ cm}^{-2}$ . Though this flux limit does not seem to be too high, the combination of these two criteria could result in selecting bluer, less dust attenuated objects compared to the standard LBG selection employed by Troncoso et al. (2014).

Another noticeable feature of Figure 4 is that there is an appreciable number of objects ( $\sim 20\%$ ) showing  $A_V$  close or equal to zero, which seems somewhat at odds with the relatively high SFR of galaxies in our sample. The adopted calibration of the  $\beta_{\text{UV}}-A_{\text{UV}}$  relation in Equation (3) was established at  $z = 0$  but the relation could be different at high redshift for a number of reasons, such as different intrinsic  $\beta$  slope due to stellar population properties, IMF, SFH (e.g., Reddy et al. 2010; Wilkins et al. 2011), or different extinction curve than one assumed here (e.g., Reddy et al. 2015). Castellano et al. (2014) investigated the UV dust extinction for a sample of LBGs at  $z \simeq 3$ , obtaining an intrinsic slope of  $\beta_{\text{UV}} = -2.67$  which is significantly steeper than widely used values of  $\beta_{\text{UV}} = -2.10$  (Calzetti et al. 2000) and  $\beta_{\text{UV}} = -2.23$  (Meurer et al. 1999). Indeed, for our galaxies with  $A_V$  close or equal to zero the measured  $\beta_{\text{UV}}$  is close to or slightly steeper than  $-2.10$ , either because of measurement errors or because the intrinsic slope is actually steeper than  $-2.10$ .

#### 3.5. Star-formation rate

##### 3.5.1. UV luminosity

**Table 3**  
Stellar mass, dust extinction, and star formation rate.

ID	$\log M_*$ ( $M_\odot$ )	$A_V$ (SED) (mag)	$A_V$ (UV) (mag)	$\log \text{SFR}$ (SED) ( $M_\odot \text{ yr}^{-1}$ )	$\log \text{SFR}$ (UV) ( $M_\odot \text{ yr}^{-1}$ )	$\log \text{SFR}$ (H $\beta$ ) ( $M_\odot \text{ yr}^{-1}$ )
434625	$9.35^{+0.28}_{-0.47}$	$0.11^{+0.19}_{-0.11}$	$0.33 \pm 0.14$	$0.97^{+0.29}_{-0.16}$	$1.09 \pm 0.06$	$< 1.40$
413136	$10.51^{+0.03}_{-0.04}$	$0.30^{+0.07}_{-0.07}$	$0.84 \pm 0.10$	$1.52^{+0.02}_{-0.02}$	$1.86 \pm 0.04$	$1.63 \pm 0.12$
413646	$9.35^{+0.08}_{-0.13}$	$0.75^{+0.16}_{-0.15}$	$0.43 \pm 0.12$	$1.82^{+0.37}_{-0.06}$	$1.32 \pm 0.05$	...
413453	$10.91^{+0.02}_{-0.02}$	$0.30^{+0.07}_{-0.07}$	$0.83 \pm 0.09$	$1.46^{+0.02}_{-0.02}$	$1.80 \pm 0.04$	$< 1.94$
434585	$10.24^{+0.08}_{-0.08}$	$0.11^{+0.08}_{-0.08}$	$0.38 \pm 0.07$	$1.56^{+0.03}_{-0.04}$	$1.71 \pm 0.03$	$1.59 \pm 0.13$
434571	$9.04^{+0.15}_{-0.24}$	$0.30^{+0.17}_{-0.18}$	$0.08 \pm 0.17$	$1.17^{+0.33}_{-0.20}$	$0.80 \pm 0.08$	...
413391	$10.17^{+0.07}_{-0.29}$	$0.53^{+0.29}_{-0.12}$	$0.54 \pm 0.08$	$1.94^{+0.54}_{-0.10}$	$1.88 \pm 0.04$	$1.48 \pm 0.13$
427122	$8.93^{+0.19}_{-0.26}$	$0.00^{+0.00}_{-0.00}$	$0.28 \pm 0.20$	$0.70^{+0.03}_{-0.04}$	$0.90 \pm 0.09$	$0.88 \pm 0.15$
434148	$9.70^{+0.12}_{-0.13}$	$0.10^{+0.08}_{-0.08}$	$0.02 \pm 0.14$	$1.06^{+0.02}_{-0.02}$	$0.92 \pm 0.06$	$< 0.84$
434082	$9.75^{+0.13}_{-0.07}$	$0.03^{+0.12}_{-0.03}$	$0.35 \pm 0.07$	$1.69^{+0.03}_{-0.24}$	$1.74 \pm 0.03$	$2.03 \pm 0.04$
434126	$9.13^{+0.14}_{-0.09}$	$0.48^{+0.09}_{-0.12}$	$0.41 \pm 0.12$	$1.73^{+0.05}_{-0.25}$	$1.39 \pm 0.05$	$1.44 \pm 0.10$
434139	$9.18^{+0.09}_{-0.07}$	$0.44^{+0.11}_{-0.16}$	$0.11 \pm 0.12$	$1.68^{+0.05}_{-0.23}$	$1.09 \pm 0.05$	$< 1.41$
434145	$9.71^{+0.11}_{-0.09}$	$0.69^{+0.08}_{-0.08}$	$0.69 \pm 0.11$	$2.01^{+0.02}_{-0.07}$	$1.77 \pm 0.05$	$< 2.04$
434242	$8.78^{+0.17}_{-0.20}$	$0.04^{+0.14}_{-0.04}$	$0.00 \pm 0.22$	$0.90^{+0.08}_{-0.24}$	$0.66 \pm 0.10$	$1.30 \pm 0.14$
406390	$9.61^{+0.10}_{-0.13}$	$0.66^{+0.12}_{-0.16}$	$0.61 \pm 0.11$	$1.88^{+0.09}_{-0.19}$	$1.62 \pm 0.05$	$< 1.73$
406444	$10.87^{+0.08}_{-0.02}$	$0.10^{+0.07}_{-0.07}$	$0.84 \pm 0.05$	$1.61^{+0.02}_{-0.02}$	$2.26 \pm 0.02$	$2.07 \pm 0.06$
434227	$10.14^{+0.06}_{-0.06}$	$0.42^{+0.13}_{-0.25}$	$0.64 \pm 0.11$	$1.78^{+0.07}_{-0.45}$	$1.86 \pm 0.05$	$< 1.75$
191932	$9.93^{+0.10}_{-0.06}$	$0.64^{+0.12}_{-0.12}$	$0.48 \pm 0.16$	$1.54^{+0.03}_{-0.21}$	$1.24 \pm 0.07$	$< 1.16$
434547	$9.62^{+0.14}_{-0.21}$	$0.65^{+0.18}_{-0.18}$	$0.55 \pm 0.12$	$1.79^{+0.31}_{-0.21}$	$1.49 \pm 0.06$	$1.05 \pm 0.08$
192129	$10.33^{+0.05}_{-0.03}$	$0.00^{+0.00}_{-0.00}$	$0.19 \pm 0.10$	$1.20^{+0.03}_{-0.04}$	$1.37 \pm 0.04$	$1.46 \pm 0.06$
193914	$9.32^{+0.09}_{-0.08}$	$0.63^{+0.12}_{-0.15}$	$0.28 \pm 0.11$	$1.95^{+0.06}_{-0.24}$	$1.30 \pm 0.05$	...
212863	$9.91^{+0.10}_{-0.13}$	$0.19^{+0.16}_{-0.13}$	$0.56 \pm 0.17$	$1.03^{+0.19}_{-0.03}$	$1.31 \pm 0.08$	$1.55 \pm 0.08$
195044	$9.69^{+0.07}_{-0.13}$	$0.75^{+0.16}_{-0.11}$	$0.55 \pm 0.10$	$1.91^{+0.28}_{-0.05}$	$1.56 \pm 0.05$	$0.84 \pm 0.16$
208115	$10.86^{+0.02}_{-0.02}$	$0.00^{+0.00}_{-0.00}$	$0.01 \pm 0.12$	$1.11^{+0.02}_{-0.02}$	$1.12 \pm 0.05$	$2.11 \pm 0.05$
200355	$9.83^{+0.11}_{-0.12}$	$0.02^{+0.14}_{-0.02}$	$0.45 \pm 0.15$	$1.09^{+0.07}_{-0.17}$	$1.35 \pm 0.07$	$1.60 \pm 0.08$
214339	$10.56^{+0.02}_{-0.02}$	$0.00^{+0.00}_{-0.00}$	$1.16 \pm 0.17$	$0.91^{+0.02}_{-0.02}$	$2.19 \pm 0.08$	$1.81 \pm 0.12$
411078	$9.45^{+0.02}_{-0.02}$	$0.30^{+0.07}_{-0.07}$	$0.00 \pm 0.06$	$1.91^{+0.02}_{-0.04}$	$1.38 \pm 0.03$	$1.75 \pm 0.03$
212298	$10.15^{+0.11}_{-0.08}$	$0.84^{+0.14}_{-0.16}$	$0.81 \pm 0.10$	$2.10^{+0.04}_{-0.21}$	$1.83 \pm 0.04$	$1.85 \pm 0.04$
412808	$8.37^{+0.10}_{-0.12}$	$0.00^{+0.10}_{-0.00}$	$0.08 \pm 0.14$	$1.14^{+0.40}_{-0.05}$	$0.99 \pm 0.06$	$1.24 \pm 0.07$
223954	$9.68^{+0.12}_{-0.13}$	$0.15^{+0.18}_{-0.13}$	$0.24 \pm 0.15$	$1.17^{+0.18}_{-0.07}$	$1.16 \pm 0.07$	$1.11 \pm 0.11$
220771	$9.34^{+0.18}_{-0.21}$	$0.01^{+0.17}_{-0.01}$	$0.00 \pm 0.33$	$0.64^{+0.12}_{-0.15}$	$0.56 \pm 0.15$	$0.79 \pm 0.16$
219315	$9.82^{+0.09}_{-0.09}$	$0.00^{+0.00}_{-0.00}$	$0.00 \pm 0.20$	$0.79^{+0.03}_{-0.04}$	$0.80 \pm 0.09$	$< 0.56$
434618	$10.09^{+0.08}_{-0.09}$	$0.08^{+0.09}_{-0.08}$	$0.32 \pm 0.13$	$1.18^{+0.04}_{-0.16}$	$1.28 \pm 0.06$	$1.34 \pm 0.06$
221039	$9.58^{+0.05}_{-0.04}$	$0.70^{+0.07}_{-0.07}$	$0.41 \pm 0.08$	$2.01^{+0.02}_{-0.02}$	$1.51 \pm 0.03$	$1.54 \pm 0.04$
215511	$9.39^{+0.12}_{-0.18}$	$0.48^{+0.24}_{-0.21}$	$0.32 \pm 0.17$	$1.31^{+0.29}_{-0.21}$	$1.03 \pm 0.08$	$1.40 \pm 0.08$
217597	$9.50^{+0.15}_{-0.22}$	$0.72^{+0.26}_{-0.23}$	$0.50 \pm 0.23$	$1.38^{+0.30}_{-0.21}$	$1.05 \pm 0.10$	$1.14 \pm 0.13$
211934	$9.66^{+0.20}_{-0.24}$	$0.83^{+0.35}_{-0.23}$	$1.61 \pm 0.52$	$1.19^{+0.32}_{-0.27}$	$1.82 \pm 0.23$	$1.67 \pm 0.24$
434579	$10.02^{+0.10}_{-0.10}$	$0.48^{+0.10}_{-0.10}$	$0.36 \pm 0.39$	$1.31^{+0.03}_{-0.16}$	$1.05 \pm 0.17$	$0.74 \pm 0.20$
217753	$10.29^{+0.09}_{-0.07}$	$0.99^{+0.17}_{-0.15}$	$0.80 \pm 0.16$	$1.78^{+0.19}_{-0.12}$	$1.56 \pm 0.07$	$1.66 \pm 0.09$
218783	$10.45^{+0.10}_{-0.15}$	$0.53^{+0.12}_{-0.09}$	$0.72 \pm 0.12$	$1.67^{+0.13}_{-0.02}$	$1.75 \pm 0.05$	$1.45 \pm 0.07$
217090	$8.65^{+0.07}_{-0.28}$	$0.22^{+0.13}_{-0.22}$	$0.00 \pm 0.13$	$2.14^{+0.41}_{-1.07}$	$0.95 \pm 0.06$	$1.51 \pm 0.07$
210037	$8.76^{+0.27}_{-0.11}$	$0.61^{+0.18}_{-0.20}$	$0.77 \pm 0.20$	$1.83^{+0.74}_{-0.39}$	$1.50 \pm 0.09$	$< 1.43$
208681	$10.86^{+0.02}_{-0.02}$	$0.30^{+0.07}_{-0.07}$	$0.35 \pm 0.05$	$1.86^{+0.02}_{-0.02}$	$1.75 \pm 0.02$	$1.74 \pm 0.04$

We adopt the calibration of the UV luminosity-based SFR from [Daddi et al. \(2004\)](#) after converting from Salpeter IMF to Chabrier IMF by applying an offset of 0.23 dex:

$$\text{SFR}_{\text{UV}}(M_\odot \text{ yr}^{-1}) = 6.65 \times 10^{-29} L_{\text{UV,corr}} (\text{erg s}^{-1} \text{ Hz}^{-1}), \quad (4)$$

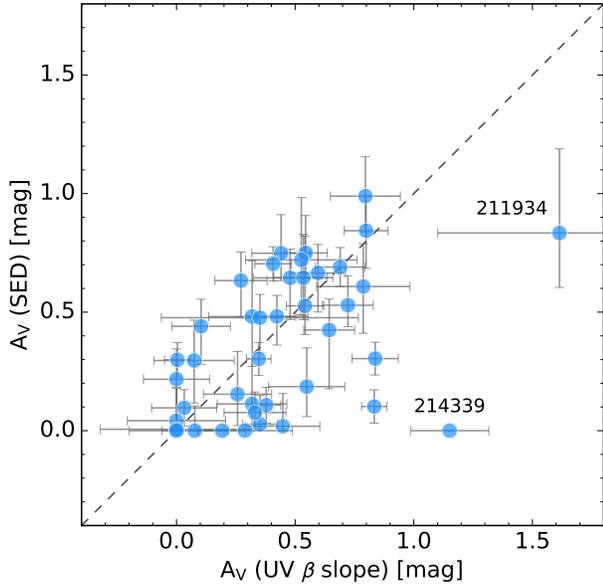
where  $L_{\text{UV,corr}}$  is extinction corrected UV luminosity derived using

$$L_{\text{UV,corr}} = L_{\text{UV,obs}} \times 10^{0.44 A_{\text{UV}}}. \quad (5)$$

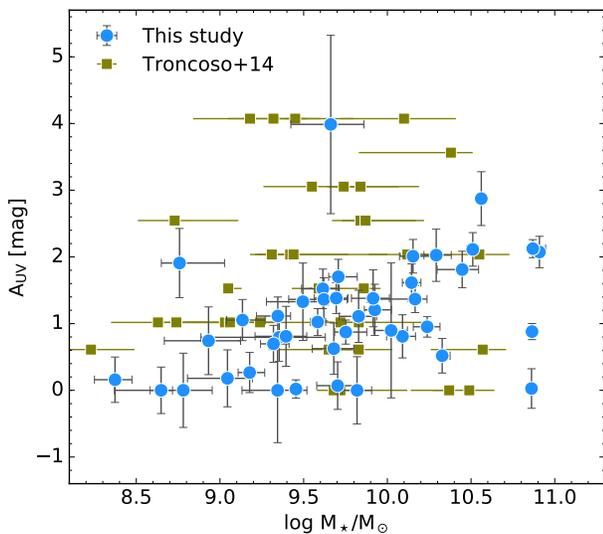
Here, the UV luminosity is measured at rest-frame 1500 Å.

In the left panel of [Figure 6](#), we compare the UV-based SFRs with those from SED fitting, showing that the two measurements agree well with each other.

[Figure 7](#) shows SFR as a function of stellar mass for  $z \simeq 3.3$  SFGs. Our sample covers about 2.5 dex in stellar mass from  $\log M_*/M_\odot \lesssim 8.5$  to  $\simeq 11$ , essentially following the MS at  $z = 3.27$  derived by [Speagle et al. \(2014\)](#) which also traces the parent sample of  $z \simeq 3.3$  SFGs shown with gray-scale. We also derived the best-fit relation between stellar mass and SFR for our sample,



**Figure 4.** Comparison of the attenuation at  $V$ -band estimated from SED fitting with that converted from  $A_{UV}$  derived with UV  $\beta$ -slope and the Calzetti extinction law. Dashed lines correspond to the one-to-one relation.



**Figure 5.**  $A_{UV}$  vs. stellar mass. Our sample is shown in blue circles and those taken from Troncoso et al. (2014) are shown with green squares. UV attenuation for Troncoso et al. (2014) are converted from  $E(B - V)$  from broad-band SED fitting by assuming the Calzetti law.

finding

$$\begin{aligned} \log \text{SFR}/(M_{\odot} \text{ yr}^{-1}) \\ = (1.52 \pm 0.05) + (0.49 \pm 0.08) \times (\log M/M_{\odot} - 10), \end{aligned} \quad (6)$$

shown with the solid line. Because of the sample selection based either on the availability of spectroscopic redshift or on the predicted  $H\beta$  flux, our sample is likely to be biased against especially low mass and low SFR galaxies. We believe this is the main reason why we obtained a flatter MS slope compared to that of the parent sample and that of the Speagle et al. (2014) MS. We will use

Equation (6) only to separate the sample into bins of  $M_{*}$  and sSFR to create composite spectra (see Section 3.6).

For comparison, overplotted in Figure 7 is the sample of  $z \simeq 3.4$  SFGs from Troncoso et al. (2014). Their sample shows an even flatter slope than ours. Again, this could be due to their sample selection based on the LBG technique, which prefers galaxies with blue SED and show a flat SFR–stellar mass relation (e.g., Erb et al. 2006b). Note that their SFRs are based on  $H\beta$  luminosity with extinction correction assuming an extra extinction in nebular component, i.e.,  $E(B - V)_{\text{neb}} = E(B - V)_{\text{star}}/0.44$ , while UV-based SFRs are used for our sample. Thus, both our best-fit and Troncoso et al. (2014) distributions appear to be flatter than the canonical MS (Speagle et al. 2014), which can result from a bias favoring low-mass SFGs with above average sSFR and disfavoring high-mass galaxies with high dust extinction. Relatively low dust extinction is indeed obtained for our sample in the analysis above. In particular, we might miss high metallicity objects due to this possible bias, if the correlation between metallicity and dust extinction claimed at an intermediate redshift  $z \simeq 1.6$  (Zahid et al. 2014) still holds at  $z \sim 3.3$ .

### 3.5.2. $H\beta$ luminosity

We converted  $H\beta$  luminosities to the  $H\alpha$  luminosities, assuming an intrinsic  $H\alpha/H\beta$  ratio of 2.86 (Case B recombination with  $T = 10^4$  K and  $n_e = 10^2 \text{ cm}^{-3}$ ; Osterbrock & Ferland 2006). Then the SFR based on  $H\alpha$  was computed following Kennicutt & Evans (2012),

$$\log \text{SFR}_{H\alpha}(M_{\odot} \text{ yr}^{-1}) = \log L_{H\alpha}(\text{erg s}^{-1}) - 41.27. \quad (7)$$

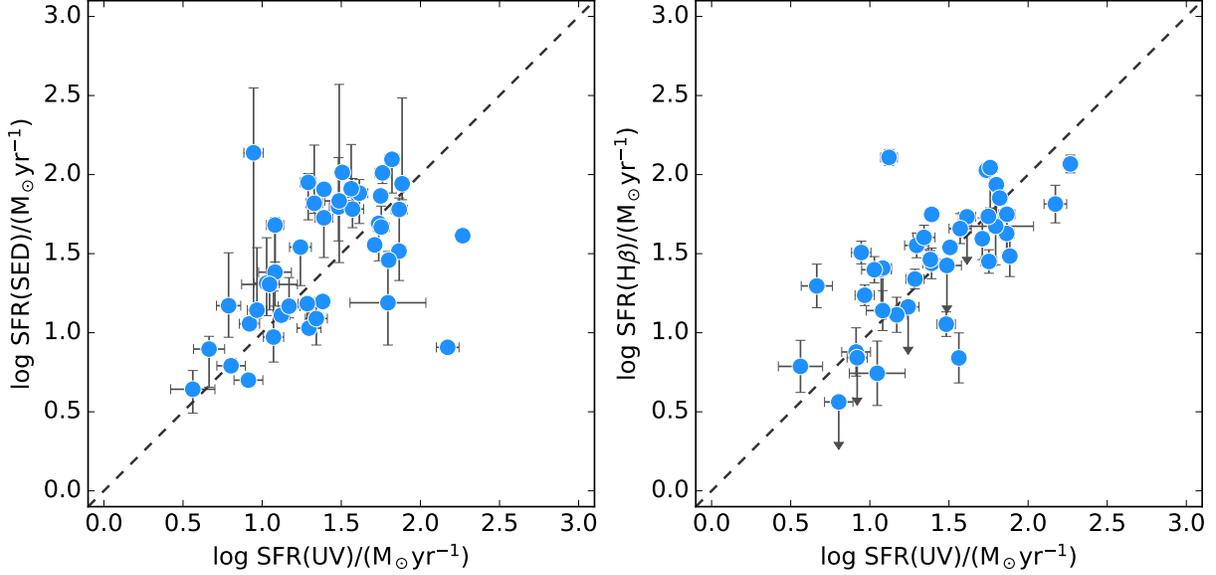
For the objects in which  $H\beta$  is not detected with more than  $3\sigma$ , we adopted  $3\sigma$  upper limits.

In the original recipe by Calzetti et al. (2000), calibrated with local UV-luminous starbursts, nebular emission lines are attenuated more than stellar light following  $E(B - V)_{\text{neb}} = E(B - V)_{\text{star}}/0.44$ . However, there have been various claims in recent years indicating that at high redshift these two components may suffer similar attenuations (e.g., Erb et al. 2006b; Kashino et al. 2013; Pannella et al. 2015; Puglisi et al. 2016). Therefore, we assumed the same amount of attenuation for the stellar light as for emission lines, which actually provides a good agreement between UV-based and  $H\beta$ -based SFRs as shown in the left panel of Figure 6.

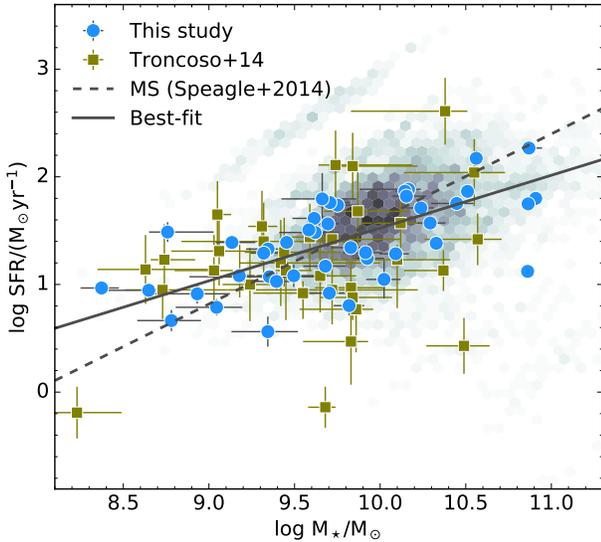
In addition to the relation between nebular emission lines and stellar continuum extinction, there is an uncertainty in the choice of the extinction curve for nebular emission lines. Related to the original derivation of the Calzetti et al. (2000) relation, the Milky Way extinction curve (Cardelli et al. 1989) or small Magellanic cloud (SMC) extinction curve (Gordon et al. 2003) is often preferred (e.g., Steidel et al. 2014). In the estimate of  $H\beta$ -based SFRs we use the Calzetti et al. (2000) extinction curve. Note that for our range of  $A_V$ , the change between Calzetti et al. (2000) and Cardelli et al. (1989) extinction curves is very minor: at most 2% for the  $H\beta$  flux and 0.03 dex for  $\log([\text{O III}]/[\text{O II}])_{\lambda 3727}$ .

### 3.6. Composite spectra

In the next sections we will compare various properties of the ionized gas with global properties of galax-



**Figure 6.** Comparison of SFR derived by UV luminosity with that derived from broad-band SED fitting (*Left*) and  $\text{H}\beta$  (*Right*),  $\text{H}\beta$  SFRs are corrected for dust extinction from UV  $\beta$ -slope and assuming  $E(B-V)_{\text{neb}} = E(B-V)_{\text{star}}$ . Dashed lines show the one-to-one relation.



**Figure 7.** SFR–stellar mass relation for galaxies at  $3 < z < 3.8$ . Blue circles are shows UV-based SFR of our sample and background pixels show SFR from SED fitting of photo- $z$  selected galaxies at  $3 < z < 3.8$  (Ilbert et al. 2013). Green squares are galaxies at  $3 < z < 5$  by Troncoso et al. (2014). SFR of their objects are estimated from  $\text{H}\beta$  luminosity. Dashed line indicate the star-forming main sequence at  $z = 3.27$  (Speagle et al. 2014).

ies, such as stellar mass, SFR, and sSFR. Besides carrying out such comparison for individual galaxies, we will also compare average properties. For this purpose, we created composite spectra in bins of stellar mass and SFR. The sample, excluding the two AGN candidates, was split in three bins in stellar mass,  $\log M/M_{\odot} < 9.5$ ,  $9.5 < \log M/M_{\odot} < 10.0$ , and  $\log M/M_{\odot} > 10.0$ , and two bins in SFR, above and below the best-fit MS shown as the dashed-line in Figure 7, i.e.,  $\Delta_{\text{MS}} < 0$  and  $\Delta_{\text{MS}} > 0$  where  $\Delta_{\text{MS}} \equiv \text{sSFR}/\text{sSFR}_{\text{best-fit}}$ .

First, spectra of each object in both  $J$ - and  $H$ -band were normalized by total  $[\text{O III}]\lambda 5007$  flux and regis-

tered by a linear interpolation to the rest-frame wavelength grid of  $0.25\text{\AA}$  interval which is slightly finer than the spectral resolution for the highest redshift object of our sample. We also normalized the corresponding noise spectra by total  $[\text{O III}]\lambda 5007$  flux and registered to the identical rest-frame wavelength grid but interpolated in quadrature. Then composite spectra were constructed by taking an average at each wavelength pixel weighted by the inverse variance. We constructed the associated noise spectra via the standard error propagation from the individual noise spectra.

Emission line fluxes are measured by fitting a Gaussian to each emission line by assuming a common velocity shift and a velocity dispersion. We fit simultaneously  $[\text{O II}]\lambda\lambda 3726, 3729$ ,  $\text{H}\beta$ ,  $[\text{O III}]\lambda\lambda 4959, 5007$ , and  $[\text{Ne III}]\lambda 3869$  with continuum described by a second order polynomial. We computed the flux values and their  $1\sigma$  errors by means of a Monte Carlo simulation with  $10^3$  realizations.

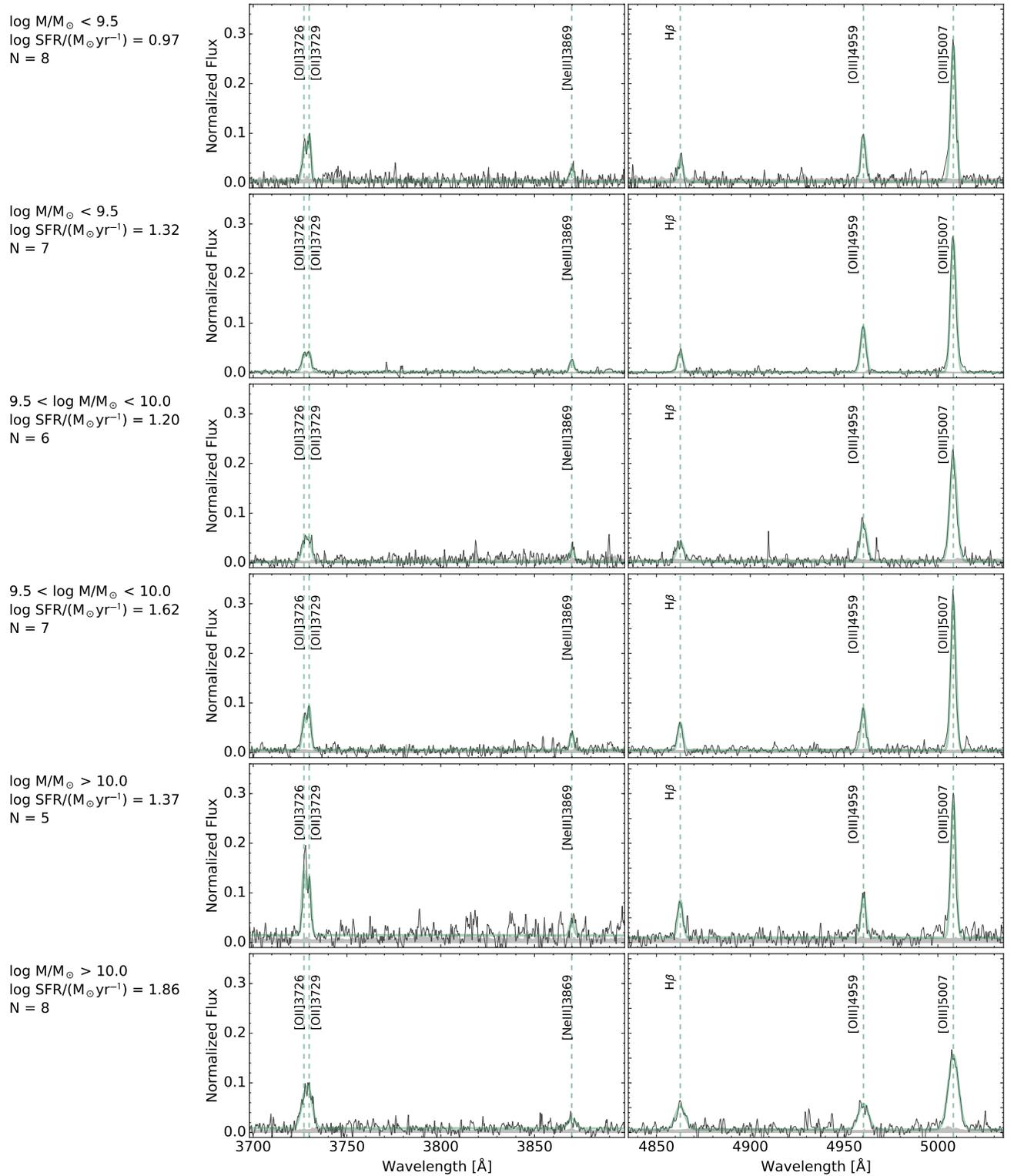
The resulting stacked spectra are shown in Figure 8. We adopt median stellar mass, SFR, and  $A_V$  whenever they are used in the subsequent analysis (see Table 4).

#### 4. MEASUREMENTS OF IONIZED GAS PROPERTIES

In this section, we derive physical properties of ionized gas, namely gas-phase oxygen abundance, ionization parameter, and electron density, of our sample. The obtained values are listed in Table 4 and Table 5 for the stacked spectra and individual objects, respectively.

##### 4.1. Gas-phase oxygen abundance

The primary indicator for gas phase metallicity,  $12 + \log(\text{O}/\text{H})$ , in this study is  $R_{23} \equiv ([\text{O II}]\lambda 3726 + [\text{O II}]\lambda 3729 + [\text{O III}]\lambda 4959 + [\text{O III}]\lambda 5007) / \text{H}\beta$  (Pagel et al. 1979; Kobulnicky & Phillips 2003). For the metallicity measurement, we adopt the empirical calibration by Maiolino et al. (2008) in which low metallicity regime ( $12 + \log(\text{O}/\text{H}) \lesssim 8.3$ ) is directly calibrated by the elec-



**Figure 8.** Composite spectra in bins of stellar mass and SFR above and below the best-fit "main sequence" (Figure 7). The range of stellar mass, median SFR, and number of objects stacked in each bin is indicated at each row. The panels show the observed composite spectra (black) with associated  $1\sigma$  noise (gray) and the best-fit Gaussians for the emission lines (green). For each mass bin, the upper/lower panels show the composite spectra of galaxies below/above the adopted main sequence.

**Table 4**  
Properties of stacked spectra.

$N_{\text{obj}}$	$\log M_{\star}$ ( $M_{\star}/M_{\odot}$ )	$\log \text{SFR}$ ( $M_{\odot} \text{ yr}^{-1}$ )	$A_V$ (mag)	$\log q$ ( $\text{cm s}^{-1}$ )	$\log n_e$ ( $\text{cm}^{-3}$ )	$12 + \log(\text{O}/\text{H})$
(1)	(2)	(3)	(4)	(5)	(6)	(7)
Above the best-fit MS						
8	9.26	0.97	0.20	$7.77^{+0.01}_{-0.01}$	$1.92^{+0.21}_{-0.31}$	$8.15^{+0.09}_{-0.10}$
6	9.82	1.20	0.34	$7.86^{+0.01}_{-0.01}$	$2.51^{+0.09}_{-0.10}$	$8.04^{+0.11}_{-0.12}$
5	10.29	1.37	0.35	$7.69^{+0.01}_{-0.01}$	$2.86^{+0.05}_{-0.06}$	$8.38^{+0.08}_{-0.09}$
Below the best-fit MS						
7	9.13	1.32	0.28	$7.95^{+0.01}_{-0.00}$	$2.45^{+0.06}_{-0.06}$	$7.97^{+0.10}_{-0.10}$
7	9.66	1.62	0.55	$7.76^{+0.01}_{-0.01}$	$2.01^{+0.15}_{-0.18}$	$8.15^{+0.09}_{-0.10}$
8	10.34	1.86	0.76	$7.74^{+0.01}_{-0.01}$	$1.92^{+0.25}_{-0.41}$	$8.41^{+0.08}_{-0.09}$

**Note.** — (1) Number of objects in the bin; (2) Median stellar mass; (3) Median SFR; (4) Median  $A_V$ ; (5) Ionization parameter; (6) Electron density; (7) Gas-phase oxygen abundance.

tron temperature method. At this metallicity scale, the theoretical calibration has been known to have difficulties in reproducing the observed emission line ratios, e.g., [Kewley & Dopita \(2002\)](#). This appears to still exist in the recent photoionization models by [Dopita et al. \(2013\)](#) as shown in [Figure 9](#), i.e., calibration lines by [Maiolino et al. \(2008\)](#) show higher ratios at low metallicity than those from [Dopita et al. \(2013\)](#). The line ratios from the stacked spectra ([Figure 8](#)) are shown as hexagon symbols in [Figure 9](#), clearly showing that at low metallicities the photoionization models by [Dopita et al. \(2013\)](#) cannot account for all five line ratios simultaneously.

For our metallicity estimates, following [Maiolino et al. \(2008\)](#) we used the five extinction-corrected line ratios shown in [Figure 9](#), namely  $R_{23}$ ,  $[\text{O III}]\lambda 5007/\text{H}\beta$ ,  $[\text{O III}]\lambda 5007/[\text{O II}]\lambda\lambda 3726, 3729$ ,  $[\text{O II}]\lambda\lambda 3726, 3729/\text{H}\beta$ , and  $[\text{Ne III}]\lambda 3869/[\text{O II}]\lambda\lambda 3726, 3729$ , for the metallicity estimate. For the stacked spectra, we corrected for dust extinction with the median  $A_V$  derived from the  $\beta_{\text{UV}}$  slope.

For the metallicity analysis of individual galaxies we removed seven objects without  $3\sigma$  detection in  $[\text{O II}]\lambda 3726 + [\text{O II}]\lambda 3729$  and the two AGN candidates (one of two is also  $[\text{O II}]\lambda 3727$  non-detection). This leaves us with 35 objects. In the case that either  $[\text{O III}]\lambda 4959$  or  $[\text{O III}]\lambda 5007$  are undetected at the  $3\sigma$  level, the other  $[\text{O III}]$  flux is complemented by assuming an intrinsic line ratio of  $[\text{O III}]\lambda 5007/[\text{O III}]\lambda 4959 = 3$ . For eight objects without  $> 3\sigma$   $\text{H}\beta$  detection, we used the  $\text{H}\beta$  flux estimated from the UV-based SFR, given the relatively tight correlation between the SFRs from the two estimators as shown in [Figure 6](#).  $[\text{Ne III}]\lambda 3869$  is detected for 10 out of the 35 objects.

The gas-phase oxygen metallicity was then derived with the maximum likelihood method, first computing

$$\chi^2 = \sum_i \frac{(\log I_{i,\text{M08}} - \log I_{i,\text{obs}})^2}{\sigma_{i,\text{obs}}^2 + \sigma_{i,\text{rms}}^2}, \quad (8)$$

where  $I_{i,\text{M08}}$  and  $I_{i,\text{obs}}$  are  $i$ th line ratio from [Maiolino et al. \(2008\)](#) calibration at a given  $12 + \log(\text{O}/\text{H})$  and the one from observed spectra. Further,  $\sigma_{i,\text{obs}}$  and  $\sigma_{i,\text{rms}}$  are the errors in the observed line ratio and intrinsic scatter measured as in [Jones et al. \(2015\)](#) for  $z = 0.8$  galaxies. Then, we translated  $\chi^2$  to the likelihood distribution using  $\mathcal{L} \propto \exp(-\chi^2/2)$ . The metallicity and its confidence interval are then defined as the median and the 16 to 84 percentiles of the probability distribution, respectively.

Note that the [Maiolino et al. \(2008\)](#) calibration adopted in this study implicitly assumes the ionization parameter at a given metallicity to be independent of redshift, as it is derived for local SFGs. Recent studies of gas-phase metallicity of high redshift SFGs show an offset in the BPT diagram with higher  $[\text{O III}]/\text{H}\beta$  ratio at a given  $[\text{N II}]/\text{H}\alpha$  ratio, which can be ascribed either to an elevated ionization parameters in high redshift galaxies (e.g., [Kewley et al. 2013](#)), or to an enhanced N/O abundance ratio at a fixed O/H ratio (e.g. [Masters et al. 2014](#); [Sanders et al. 2016](#); [Yabe et al. 2015](#); [Cullen et al. 2014](#); [Nakajima & Ouchi 2014](#)). Moreover, [Sanders et al. \(2016\)](#) have argued that there is no significant change in ionization parameter at a fixed metallicity from  $z \sim 0$  to  $z \sim 2.3$ . Unfortunately, the  $[\text{N II}]\lambda 6583/\text{H}\alpha$  ratio that is used to break the degener-

acy of metallicity estimates from  $R_{23}$  cannot be obtained from the ground for the redshift of our galaxies, but will become possible with the *James Webb Space Telescope*. [Maier et al. \(2015\)](#) suggest that  $[\text{O III}]\lambda 5007/\text{H}\beta$  ratio can be used to break the degeneracy, with galaxies with  $\log [\text{O III}]\lambda 5007/\text{H}\beta > 0.26$  having  $12 + \log(\text{O}/\text{H}) < 8.6$  on the [Kewley & Dopita \(2002\)](#) metallicity scale. Indeed, our sample with  $12 + \log(\text{O}/\text{H}) < 8.6$  always have  $\log [\text{O III}]\lambda 5007/\text{H}\beta > 0.26$ , confirming the [Maier et al. \(2015\)](#) result.

#### 4.2. Ionization parameter

The ionization parameter,  $q$ , is defined as  $q \equiv Q_{\text{H}^0}/4\pi R_s^2 n$ , where  $Q_{\text{H}^0}$  is the flux of ionizing photons above the Lyman limit,  $R_s$  is the Strömgen radius, and  $n$  is the local number density of hydrogen atoms (e.g., [Kewley & Dopita 2002](#)). The ionization parameter can be derived through a  $q$ -sensitive line ratio,  $O_{32} \equiv [\text{O III}]\lambda\lambda 4959, 5007/[\text{O II}]\lambda\lambda 3726, 3729$  (e.g., [McGaugh 1991](#)). Here, we adopt a metallicity dependent  $[\text{O III}]/[\text{O II}]-q$  relation of [Kewley & Dopita \(2002\)](#) parameterized by [Kobulnicky & Kewley \(2004\)](#) as

$$\log q = \left\{ 32.81 - 1.153y^2 + [12 + \log(\text{O}/\text{H})] (-3.396 - 0.025y + 0.1444y^2) \right\} \times \left\{ 4.63 - 0.3119y - 0.163y^2 + [12 + \log(\text{O}/\text{H})] (-0.48 + 0.0271y + 0.02037y^2) \right\}^{-1}, \quad (9)$$

where  $y = \log O_{32}$ . The results are reported in Table 5.

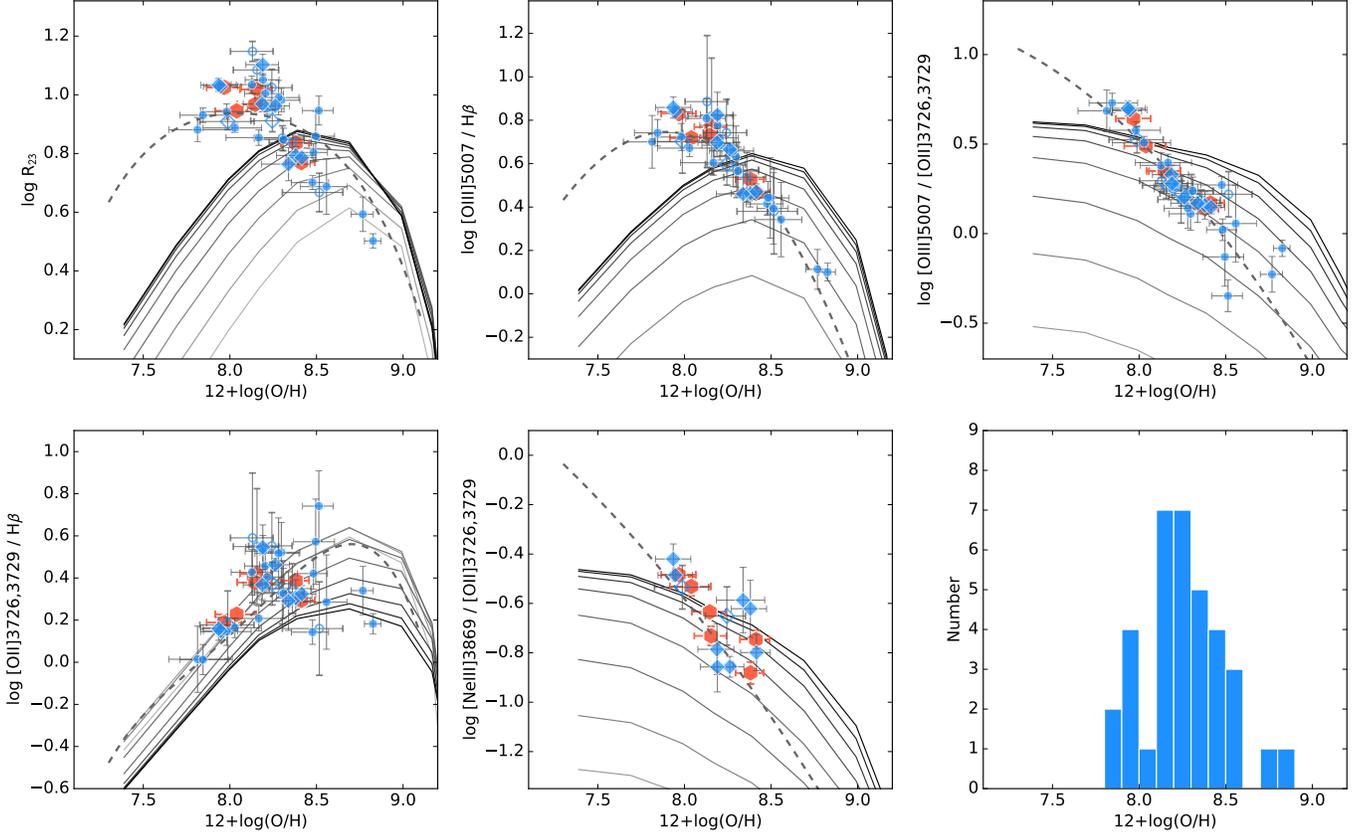
Note that the ionization parameters derived in this way are not fully self-consistent, as we used the [Maiolino et al. \(2008\)](#) calibration for gas-phase metallicity (see [Section 4.1](#)) which implicitly assumed ionization parameters of normal star-forming galaxies in the local Universe. Note also that in this and the following analysis all emission line fluxes have been corrected for dust extinction using  $E(B - V)_{\text{star}}$  derived based on  $\beta_{\text{UV}}$  slope by assuming the Calzetti extinction curve and  $E(B - V)_{\text{neb}} = E(B - V)_{\text{star}}$ .

#### 4.3. Electron density

The relatively high spectral resolution of MOSFIRE allows us to resolve the  $[\text{O II}]\lambda\lambda 3726, 3729$  doublet as seen in individual spectra. The ratio of the two  $[\text{O II}]$  lines is sensitive to electron density ([Osterbrock & Ferland 2006](#)) and we used the [PyNeb](#)<sup>7</sup> package ([Luridiana et al. 2015](#)) to compute the electron density  $n_e$  of the line-emitting regions of our galaxies. We assumed an electron temperature of  $T_e = 10^4$  K. At low to intermediate redshift,  $T_e$  is indeed observed to be  $\sim (1-2) \times 10^4$  K via the direct measurements of the  $[\text{O III}]\lambda 4363$  line (e.g., [Izotov et al. 2006](#); [Nagao et al. 2006](#); [Andrews & Martini 2013](#); [Ly et al. 2014](#); [Jones et al. 2015](#)). Assuming a higher  $T_e$ , e.g.,  $2 \times 10^4$  K, the resulting  $n_e$  will become systematically higher by  $\sim 0.15$  dex.

When one of the  $[\text{O II}]$  lines is not detected at the  $3\sigma$  level, either upper or lower limits of  $n_e$  are derived from

<sup>7</sup> <http://www.iac.es/proyecto/PyNeb/>



**Figure 9.** Best-fit metallicity vs observed line ratios for our sample. Diamonds show objects with detected  $[\text{O II}]\lambda\lambda 3726, 3729$ ,  $[\text{O III}]$ , and  $[\text{Ne III}]\lambda 3869$ , while circles are those with detected  $[\text{O II}]\lambda\lambda 3726, 3729$  and  $[\text{O III}]$ . Filled and open symbols show those with and without  $\text{H}\beta$  detection, respectively. In case of undetected  $\text{H}\beta$ , its flux is supplemented from UV SFR. Orange open pentagon shows the values obtained from the stacking of all non-AGN objects. Solid lines are photo-ionization models by [Dopita et al. \(2013\)](#) with  $\kappa = 20$  for the  $\kappa$ -distribution of electron energies. Gray scale of each line indicates  $\log q = 6.5, 6.75, 7.0, 7.25, 7.5, 7.75, 8.0, 8.25, 8.5$  from faint to thick, where  $q$  is ionization parameter defined as the ratio of the ionizing photon flux passing through a unit area and the local number density of hydrogen atoms. Dashed lines show a empirical calibration by [Maiolino et al. \(2008\)](#) that we adopted in this study. Bottom left panel is a histogram of  $12 + \log(\text{O}/\text{H})$ .

the  $3\sigma$  flux limit of the line. In the case that both of  $[\text{O II}]$  lines are detected, we have carried out a Monte Carlo simulation with 500 realizations by perturbing the measured line ratios with the associated  $1\sigma$  uncertainties. The median and 16 and 84 percentiles of the resulting distribution have been taken as  $n_e$  and  $1\sigma$  confidence interval, respectively.

## 5. DISCUSSION

### 5.1. Relation between ionized gas and galaxy properties

**Figure 10** shows the relation between  $R_{23}$  and  $O_{32}$ . The local,  $z \simeq 0$  galaxy sample shown in the background was selected from the OSSY catalog ([Oh et al. 2011](#)) as star-forming based on the BPT diagram ([Baldwin et al. 1991](#); [Kewley et al. 2006](#)) by requiring all four emission lines ( $\text{H}\beta$ ,  $[\text{O III}]\lambda 5007$ ,  $\text{H}\alpha$ , and  $[\text{N II}]\lambda 6583$ ) as well as  $[\text{O II}]\lambda 3727$  with  $\text{S/N} > 3$ . The higher line ratios of  $z \sim 3.3$  galaxies relative to the local SFGs indicate that our galaxies have higher ionization parameter, on average ([Nakajima & Ouchi 2014](#); [Shirazi et al. 2014](#)). Our  $z = 3.3$  galaxies lie along the tail of the local distribution and extend it to higher  $\log R_{23}$  and  $\log O_{32}$  values, typical of SFGs at  $z = 2-3$  (e.g., [Henry et al. 2013](#); [Nakajima & Ouchi 2014](#); [Sanders et al. 2016](#)). Locally, the tail of the distribution consists of metal-poor galaxies, typically

with  $12 + \log(\text{O}/\text{H}) \lesssim 8.5$ . Since the majority of our sample also shows  $12 + \log(\text{O}/\text{H}) \lesssim 8.5$  (See [Section 4.1](#)), we argue that the ionization parameter could be similar at a given metallicity in both low and high redshift galaxies, consistent with [Sanders et al. \(2016\)](#).

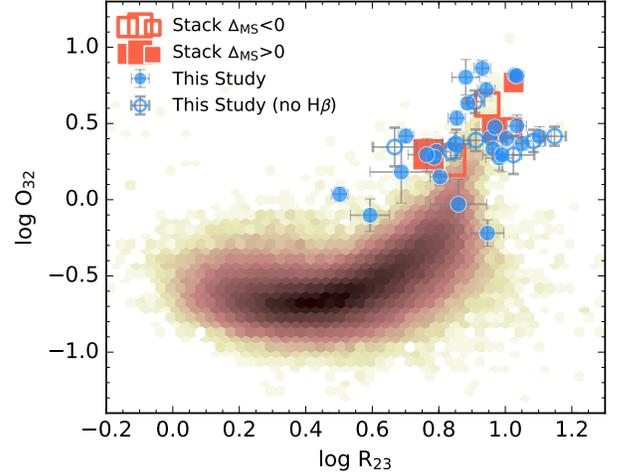
**Figure 11** compares various galaxy physical quantities with the ionization parameter. The strong correlation between  $\log q$  and  $12 + \log(\text{O}/\text{H})$  is trivial, as both  $12 + \log(\text{O}/\text{H})$  and  $\log q$  strongly depend on  $[\text{O III}]/[\text{O II}]$ . Among the other parameters shown in [Figure 11](#), we do not find significant correlations between any of them, with the exception of the SFR- $\log q$  plot. The Spearman's correlation coefficient between SFR and  $\log q$  is  $-0.35$ , corresponding to a two-sided  $p$ -value of 0.04, when considering objects without upper or lower limit in  $\log q$ . A similar, but more significant correlation between SFR and  $O_{32}$  is found by [Sanders et al. \(2016\)](#) for  $z \sim 2.3$  SFGs, with a two-sided  $p$ -value of 0.002. This correlation can be understood as a result of a correlation between SFR and metallicity and an anti-correlation between ionization parameter and metallicity ([Pérez-Montero 2014](#), but see [Dors et al. 2011](#)). [Nakajima & Ouchi \(2014\)](#) and [Sanders et al. \(2016\)](#) found correlations of  $O_{32}$  with stellar mass and sSFR as well as with SFR. While we do not see such correlations for individual objects, stacked data

**Table 5**  
Ionizing gas properties.

ID	$\log q$ ( $\text{cm s}^{-1}$ )	$\log n_e$ ( $\text{cm}^{-3}$ )	$12 + \log(\text{O}/\text{H})$
434625	$7.72^{+0.06}_{-0.06}$	...	$8.13^{+0.12}_{-0.13}$
413136	$> 7.42$	...	...
413646	$> 7.40$	...	...
413453	...	...	...
434585	$7.71^{+0.18}_{-0.19}$	$> 3.23$	$8.56^{+0.12}_{-0.15}$
434571	$> 7.50$	...	...
413391	$7.67^{+0.07}_{-0.08}$	$2.65^{+0.29}_{-0.44}$	$8.30^{+0.11}_{-0.12}$
427122	$> 7.50$	...	...
434148	$7.74^{+0.09}_{-0.10}$	...	$8.30^{+0.13}_{-0.16}$
434082	$7.86^{+0.06}_{-0.06}$	$2.11^{+0.24}_{-0.47}$	$8.03^{+0.15}_{-0.18}$
434126	$7.77^{+0.07}_{-0.07}$	$3.01^{+0.29}_{-0.41}$	$8.13^{+0.11}_{-0.12}$
434139	$> 7.49$	...	...
434145	$7.71^{+0.07}_{-0.07}$	...	$8.16^{+0.12}_{-0.14}$
434242	$7.93^{+0.11}_{-0.10}$	$< 2.51$	$7.81^{+0.20}_{-0.17}$
406390	$7.83^{+0.13}_{-0.16}$	$> 2.90$	$8.52^{+0.14}_{-0.21}$
406444	$7.74^{+0.07}_{-0.08}$	$< 2.77$	$8.38^{+0.09}_{-0.11}$
434227	$> 7.87$	...	...
191932	$7.73^{+0.06}_{-0.07}$	$2.33^{+0.28}_{-0.39}$	$8.36^{+0.11}_{-0.13}$
434547	$7.71^{+0.05}_{-0.05}$	$2.76^{+0.17}_{-0.20}$	$8.19^{+0.09}_{-0.10}$
192129	$7.87^{+0.06}_{-0.08}$	$2.71^{+0.19}_{-0.26}$	$8.48^{+0.09}_{-0.12}$
193914	$7.85^{+0.07}_{-0.08}$	...	$7.99^{+0.15}_{-0.16}$
212863	$7.83^{+0.06}_{-0.08}$	$2.77^{+0.11}_{-0.13}$	$8.17^{+0.14}_{-0.19}$
195044	$7.38^{+0.07}_{-0.07}$	...	$8.51^{+0.08}_{-0.09}$
208115	...	...	...
200355	$7.91^{+0.06}_{-0.06}$	...	$7.98^{+0.14}_{-0.15}$
214339	$7.75^{+0.08}_{-0.08}$	$2.69^{+0.26}_{-0.46}$	$8.31^{+0.12}_{-0.15}$
411078	$7.98^{+0.03}_{-0.03}$	$2.60^{+0.07}_{-0.07}$	$7.95^{+0.10}_{-0.10}$
212298	$7.72^{+0.05}_{-0.05}$	...	$8.42^{+0.08}_{-0.09}$
412808	$7.97^{+0.05}_{-0.05}$	...	$7.94^{+0.10}_{-0.10}$
223954	$7.74^{+0.05}_{-0.06}$	$2.12^{+0.25}_{-0.38}$	$8.20^{+0.11}_{-0.12}$
220771	$7.70^{+0.10}_{-0.10}$	$2.81^{+0.29}_{-0.42}$	$8.34^{+0.12}_{-0.15}$
219315	$7.74^{+0.07}_{-0.07}$	$2.71^{+0.23}_{-0.31}$	$8.24^{+0.11}_{-0.12}$
434618	$7.74^{+0.05}_{-0.05}$	$2.45^{+0.14}_{-0.17}$	$8.21^{+0.10}_{-0.11}$
221039	$7.70^{+0.04}_{-0.04}$	$2.54^{+0.10}_{-0.12}$	$8.26^{+0.08}_{-0.09}$
215511	$7.79^{+0.05}_{-0.06}$	$1.96^{+0.30}_{-0.39}$	$8.19^{+0.10}_{-0.11}$
217597	$7.74^{+0.06}_{-0.06}$	$2.52^{+0.16}_{-0.23}$	$8.19^{+0.09}_{-0.10}$
211934	$7.52^{+0.13}_{-0.13}$	...	$8.50^{+0.11}_{-0.13}$
434579	$7.68^{+0.10}_{-0.10}$	$< 2.78$	$8.28^{+0.12}_{-0.14}$
217753	$7.60^{+0.10}_{-0.10}$	$2.96^{+0.37}_{-0.42}$	$8.77^{+0.06}_{-0.07}$
218783	$7.65^{+0.06}_{-0.06}$	...	$8.48^{+0.08}_{-0.09}$
217090	$7.99^{+0.06}_{-0.06}$	$2.38^{+0.27}_{-0.43}$	$7.84^{+0.15}_{-0.13}$
210037	$7.67^{+0.10}_{-0.11}$	$2.48^{+0.30}_{-0.47}$	$8.24^{+0.12}_{-0.13}$
208681	$7.77^{+0.06}_{-0.06}$	$3.32^{+0.23}_{-0.26}$	$8.83^{+0.05}_{-0.05}$

points show some hints of a similar correlation for  $\log q$  with stellar mass and sSFR.

In Figure 12 we also compare various physical parameters with the electron density measured from the line ratio of [O II] $\lambda\lambda 3726, 3729$  doublet. The measured electron densities of  $\sim 100\text{--}1,000 \text{ cm}^{-3}$  are about one order of magnitude higher than those of typical SFGs at  $z = 0$ , roughly consistent with those reported for other high redshift galaxies (e.g., Masters et al. 2014; Shirazi et al. 2014; Sanders et al. 2016; Shimakawa et al. 2015). In Figure 12 there is no indication of strong correlations in any of the parameters with the electron density, which is also confirmed by the very low Spearman's rank correlation coefficients, indicating less than  $1\sigma$  significance,



**Figure 10.**  $O_{32}$  vs  $R_{23}$ . Individual galaxies from our sample are shown in blue circles with filled and open ones corresponding to those with and without  $H\beta$  detection, respectively.  $H\beta$  fluxes of objects without  $H\beta$  detection are estimated from UV-based SFR. For the stacked data shown in orange squares, open and filled squares represent  $\Delta_{\text{MS}} < 0$  and  $\Delta_{\text{MS}} > 0$ , respectively, with the size proportional to the median stellar mass of each bin. Since error bars for the stacked points are smaller than the size of the symbols, they are not shown here. Background pixels show the distribution of local SFGs selected based on the BPT diagram drawn from the SDSS line measurement catalog of Oh et al. (2011).

for individual objects as well as for stacked points.

Shimakawa et al. (2015) measured the electron density of a sample of  $H\alpha$  narrow-band-selected SFGs at  $z = 2.5$  through resolved [O II] $\lambda 3727$  doublet. They found a positive correlation with a  $4\sigma$  significance between  $n_e$  and sSFR. However, from Panel (c) of Figure 12, the correlation between sSFR and  $n_e$  does not seem to be strong in our sample. If at all, there is a hint for an opposite trend with higher sSFR galaxies with lower  $n_e$ . Based on a larger sample at  $z \sim 2.3$ , Sanders et al. (2016) also do not find any correlation of electron density with stellar mass, SFR or sSFR.

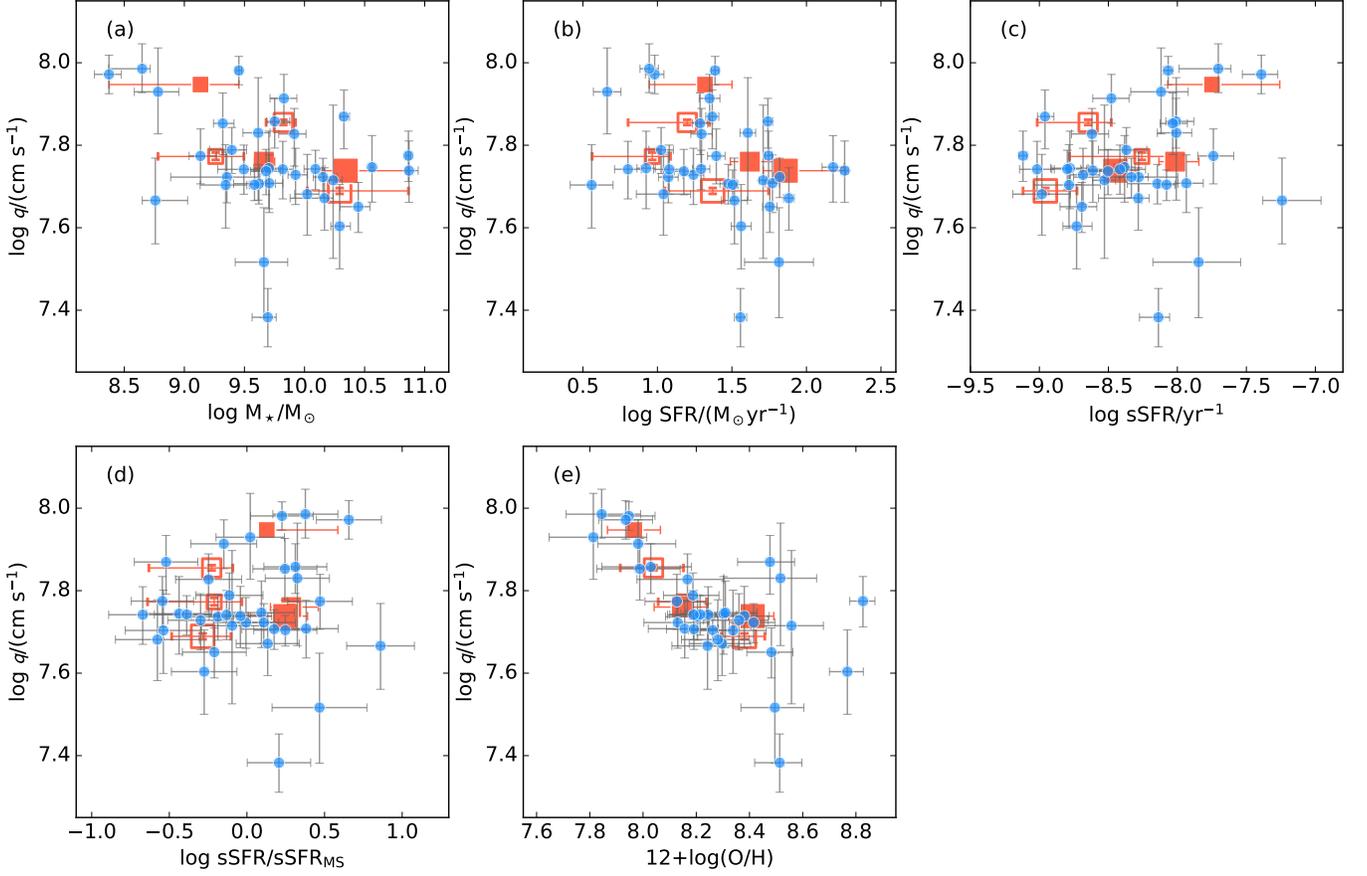
## 5.2. [O II] luminosity as a SFR indicator

The [O II] $\lambda 3727$  emission line luminosity has been used as an indicator of SFR (e.g., Kennicutt 1998), though it depends not only on SFR, but also on metallicity and ionized gas properties. Figure 13 shows the relation between the [O II] luminosity and the UV-based SFR. Here, both quantities were extinction corrected using UV-based estimates and assuming  $E(B - V)_{\text{neb}} = E(B - V)_{\text{star}}$  as before. The [O II] luminosities of our sample do not seem to follow the calibration of  $\text{SFR}([\text{O II}])$  by Kewley et al. (2004), shown as the dashed line in Figure 13. We derived the best-fit calibration of [O II] $\lambda 3727$  SFR for our  $z \gtrsim 3$  main-sequence galaxies as

$$\log \text{SFR}_{[\text{O II}]} (M_{\odot} \text{ yr}^{-1}) = \log L_{[\text{O II}]} (\text{erg s}^{-1}) - 41.17, \quad (10)$$

having fixed the slope to unity. Our best-fit gives 0.22 dex lower SFRs compared to the Kewley et al. (2004) calibration. If the extinction towards H II region were higher, like the original Calzetti law, i.e.,  $E(B - V)_{\text{gas}} = E(B - V)_{\text{star}}/0.44$ , then the discrepancy would become more prominent.

The elevated [O II] luminosity relative to the local rela-



**Figure 11.** Comparison of the ionization parameter of our sample with (a) stellar mass, (b) SFR, (c) sSFR, (d)  $\Delta_{\text{MS}} \equiv \text{sSFR}/\text{sSFR}_{\text{MS}}$ , and (e) gas-phase oxygen abundance  $12 + \log(\text{O}/\text{H})$ . Symbols are same as [Figure 10](#).

tion could be due to a change in the physical condition of star-forming regions as discussed above, i.e., higher ionization parameter and electron density in high redshift galaxies.

### 5.3. Mass–metallicity relation

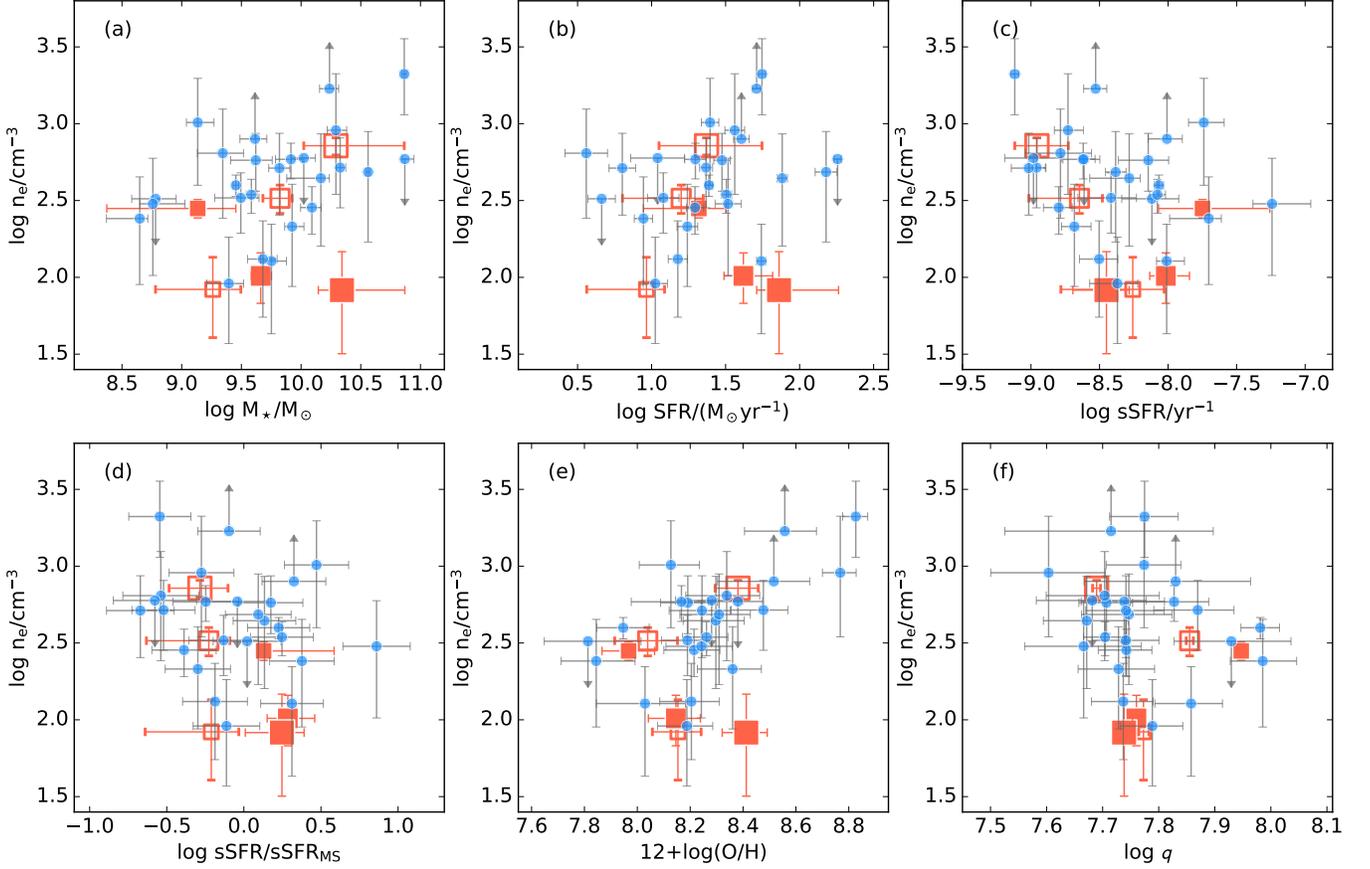
[Figure 14](#) shows the MZR for our galaxies, both individually and for the stacked spectra, in comparison with the MZRs at lower redshifts. The MZR at  $z = 0.07, 0.7,$  and  $2.2$  are from [Tremonti et al. \(2004\)](#), [Savaglio et al. \(2005\)](#), and [Erb et al. \(2006a\)](#), respectively, converted to the same metallicity calibration, and parameterized by [Maiolino et al. \(2008\)](#). We also plot the MZR at  $z \simeq 3.4$  from [Troncoso et al. \(2014\)](#) and that at  $z = 0$  taken from [Mannucci et al. \(2010\)](#). The majority of our sample follows the previously defined MZR at  $z \simeq 3.4$ , i.e., our MZR offsets by  $\simeq 0.7$  dex and  $\simeq 0.3$  dex from those at  $z \simeq 0$  and  $z \simeq 2$ , respectively. There are, however, a few objects showing higher metallicity, by up to  $0.3$ – $0.4$  dex compared to the stack points. Due to a small sample size especially at  $M_* > 10^{10.5} M_\odot$ , we do not attempt to constrain the turnover mass of MZR here. Instead, we carried out a linear regression and found the best-fit MZR for the individual objects in our sample as

$$\begin{aligned} 12 + \log(\text{O}/\text{H}) \\ = (8.36 \pm 0.03) + (0.31 + 0.05) \times (\log M_*/M_\odot - 10) \end{aligned} \quad (11)$$

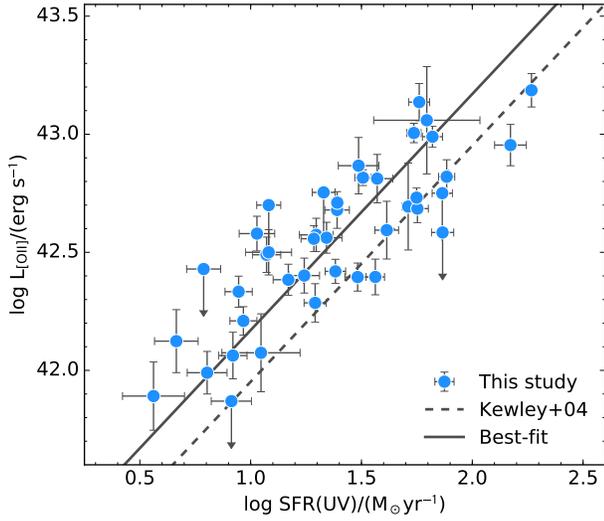
which is shown in the left panel of [Figure 14](#) with dashed line.

In [Figure 14](#) we plot ranges between minimum and maximum stellar masses in each bin as error bars for the stack points. The metallicities from the stacked spectra appear to be lower than the average or median of the individual measurements at a given stellar mass bin. This may be due to the way employed for stacking: we normalized each spectrum by the total  $[\text{O III}]\lambda 5007$  flux and then stacked with weights proportional to the inverse variance. This procedure gives more weights for  $[\text{O III}]$  bright objects which tend to have lower metallicities. Indeed, as shown in [Figure D1](#) in [Appendix D](#), objects with higher S/N in  $[\text{O III}]$  tend to have lower metallicity. The same trend is also seen in [Troncoso et al. \(2014\)](#) for SFGs at  $z \simeq 3.4$ . Their best-fit MZR for the average of individual measurements shows higher metallicity than that of the measurement on the stacked spectra (dot-dashed and dotted lines in the left panel of [Figure 14](#), respectively). We also tried stacking with the  $[\text{O III}]$  normalization but without weighing, and measuring metallicity in the same way, finding about  $0.1$  dex higher  $12 + \log(\text{O}/\text{H})$  compared with those presented above. However, our conclusion does not depend on the choice of the stacking method since our analysis on the metallicity is based mainly on individual objects.

[Figure 15](#) shows that there appear to be no correlation between  $12 + \log(\text{O}/\text{H})$  and SFR relative to the distances from the best-fit MZR and MS within the error bars for



**Figure 12.** Comparison of the electron density of our sample with (a) stellar mass, (b) SFR, (c) sSFR, (d)  $\Delta_{\text{MS}} \equiv \text{sSFR}/\text{sSFR}_{\text{MS}}$ , (e) gas-phase oxygen abundance  $12 + \log(\text{O}/\text{H})$ , and (f) ionization parameter  $\log q$ . Symbols are same as Figure 10.



**Figure 13.**  $[\text{O II}]\lambda 3727$  luminosity vs UV-based SFR. Solid line shows the best-fit linear regression with a slope of unity computed by using `LTS_LINEFIT` (Cappellari et al. 2013). Dashed line corresponds to Equation 4 in Kewley et al. (2004) converted from Salpeter to Chabrier IMF.

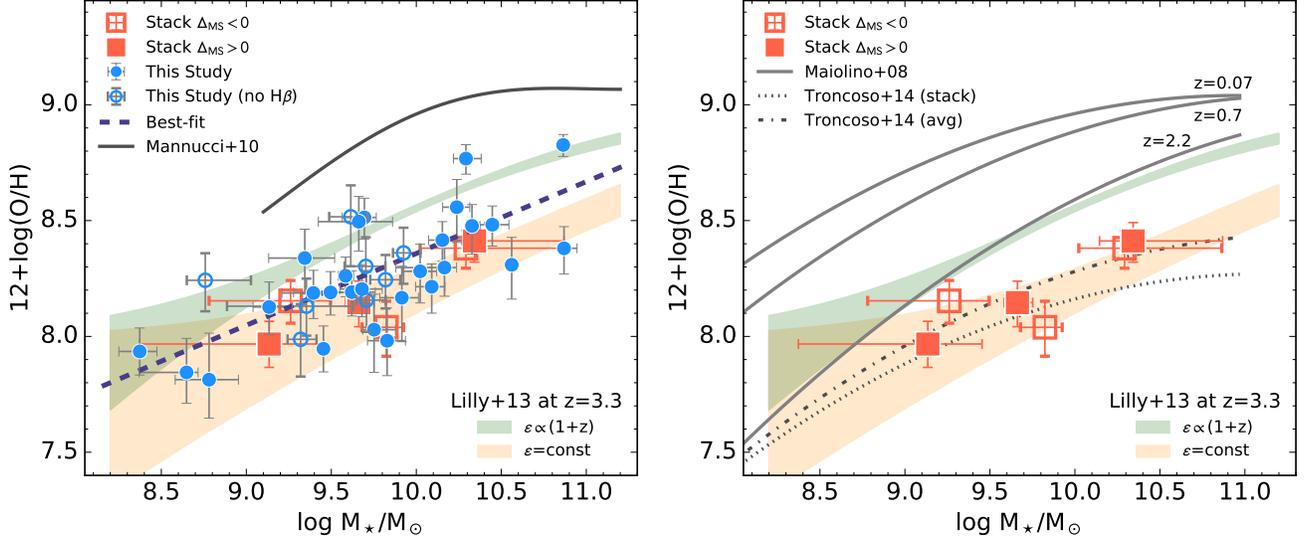
both stack and individual points, respectively. A similar behavior has been reported for  $z \sim 2$  SFGs (Steidel et al. 2014; Wuyts et al. 2014; Sanders et al. 2015), while Zahid et al. (2014) found an anti-correlation between SFR and

metallicity in a sample of SFGs at  $z \sim 1.6$  (see also Yabe et al. 2015). This suggests that the role of SFR as a second parameter in the MZR may be less important at  $z \simeq 3.3$  compared to that in the local Universe (e.g., Mannucci et al. 2010; Andrews & Martini 2013). We shall return to this issue in Section 5.4.

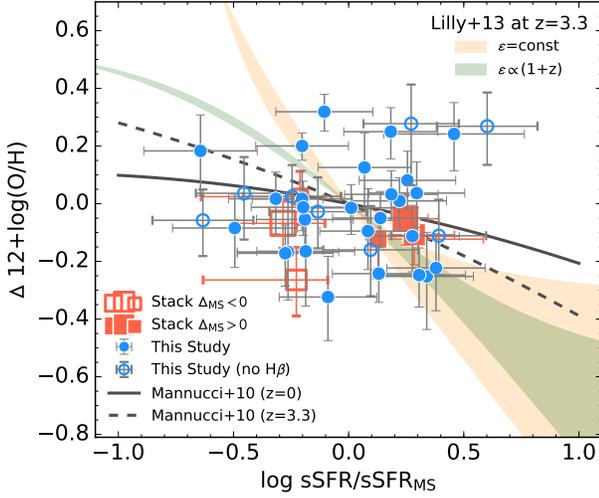
The redshift evolution of metallicity at a stellar mass of  $10^{10} M_{\odot}$  is illustrated in the right panel of Figure 16. For the comparison, data points at different redshifts are taken from Tremonti et al. (2004) for  $z = 0.07$ , Savaglio et al. (2005) for  $z = 0.72$ , and Erb et al. (2006a) for  $z = 2.2$  after corrected to the same metallicity calibration used here by Maiolino et al. (2008); Troncoso et al. (2014) for  $z = 3.4$ ; Zahid et al. (2014) for  $z = 1.55$ ; Henry et al. (2013) for  $z = 1.7$ ; Cullen et al. (2014) for  $z = 2.2$ ; Steidel et al. (2014) for  $z = 2.3$ ; and Sanders et al. (2015) for  $z = 2.3$ . Note that all these data are converted to the metallicity calibration of Maiolino et al. (2008), when needed.

#### 5.4. Mass–metallicity–SFR relation

Mannucci et al. (2010) found that in the local Universe SFGs lie close to a three-dimensional surface in the space with SFR, stellar mass and metallicity as coordinates (see also Lara-López et al. 2010). They also found that SFGs lie close to the same surface at least to  $z \simeq 2.5$ , suggesting the existence of the so called fundamental metallicity relation (FMR) and showed that a projection of the surface over the plane with coordinates  $12 + \log(\text{O}/\text{H})$  and



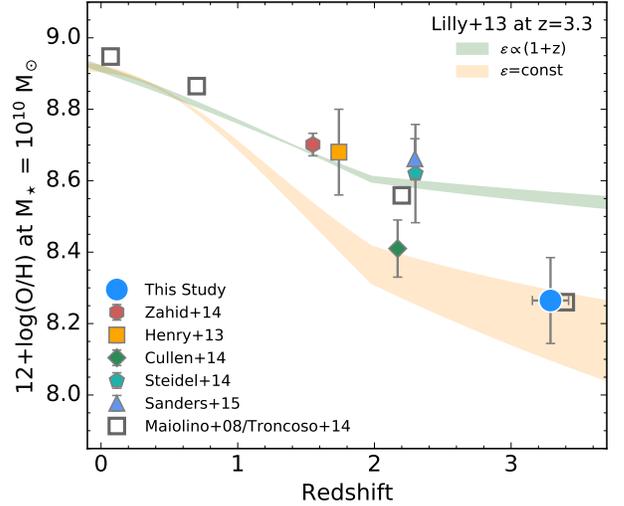
**Figure 14.** (Left) Mass–metallicity relation of our sample is shown with circles. The filled and open circles are those with and without  $H\beta$  detection, respectively. Squares represent the measurements on the stacked spectra in bins of stellar mass and SFR. The bins above and below the best-fit MS are shown with filled and open symbols. The best-fit linear relation for our sample is shown with dashed line. Solid line is the  $z = 0$  relation (Mannucci et al. 2010). (Right) Our  $z \sim 3.3$  stacked data points (orange squares) shown in the left panel are compared with MZR at various redshifts. Solid lines are taken from Maiolino et al. (2008) for  $z = 0.07, 0.72,$  and  $2.2$  relations by Tremonti et al. (2004), Savaglio et al. (2005), and Erb et al. (2006a), respectively. Dotted and dot-dashed lines are mass–metallicity relations from Troncoso et al. (2014) defined based on the measurement on the stacked spectra and the average of individual objects, respectively. Two filled regions are predictions at  $z = 3.3$  by a gas-regulation model by Lilly et al. (2013) shown in the left panel. In both panels, orange and green shaded areas are prediction from a gas-regulator model (Lilly et al. 2013) fixing the star formation efficiency  $\epsilon$  to the locally calibrated value and allowing  $\epsilon$  to increase as  $(1+z)$ . The areas enclose the case for  $0 < Z_0/y < 0.1$ .



**Figure 15.** Difference of  $12 + \log(O/H)$  from the best-fit linear regression in the MZR for our sample,  $12 + \log(O/H) = 8.358 + 0.31(\log M_*/M_\odot - 10)$ , as a function of  $\Delta_{MS}$ . Symbols of data points and two filled regions are same as Figure 10 and Figure 14, respectively, and solid and dashed lines represent the fundamental  $Z(M_*, SFR)$  relation by Mannucci et al. (2010) adjusted to  $z = 0$  and  $z = 3.3$  MS, respectively. Lilly et al. (2013) models and Mannucci et al. (2010) relations are obtained for  $M = 10^{10} M_\odot$  galaxies.

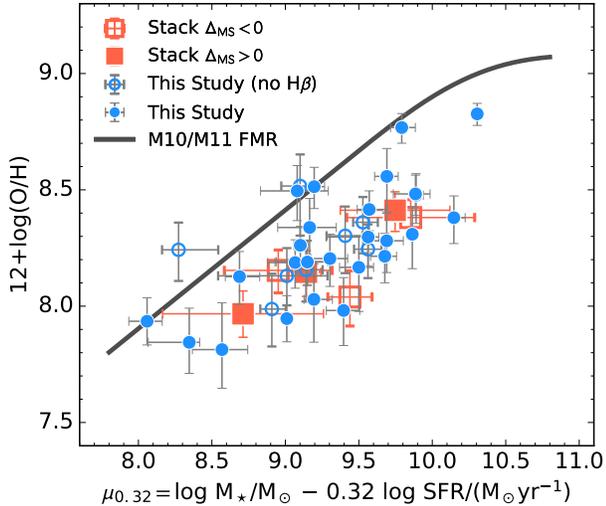
$\mu_{0.32} \equiv \log M/M_\odot - 0.32 \log SFR/(M_\odot \text{ yr}^{-1})$  is able to minimize the scatter about the surface itself. Figure 17 shows such two-dimensional plane, where most of the objects in our sample are offset from the locally defined FMR by  $\simeq 0.3$  dex.

Comparing the left panel in Figure 14 and Figure 17, it is not obvious whether in the case of our galaxies us-



**Figure 16.** Redshift evolution of MZR. Our  $z \sim 3.3$  data is shown with a filled circle. The data point and error bar indicate the average and standard deviation of the metallicity of the objects with  $\log M_*/M_\odot = 10 \pm 0.2$ . Open squares are adopted from Table 5 in Maiolino et al. (2008) for  $z = 0.07, 0.72,$  and  $2.2$  relations by Tremonti et al. (2004), Savaglio et al. (2005), and Erb et al. (2006a), respectively. An open square at  $z = 3.4$  is taken from Troncoso et al. (2014). Filled symbols at  $z < 3$  are taken from the following literature: Zahid et al. (2014) for  $z = 1.55$  (hexagon), Henry et al. (2013) for  $z = 1.7$  (square), Cullen et al. (2014) for  $z = 2.2$  (diamond), Steidel et al. (2014) for  $z = 2.3$  (pentagon), and Sanders et al. (2015) for  $z = 2.3$  (triangle). Two filled regions are predictions at  $z = 3.3$  by a gas-regulation model by Lilly et al. (2013) shown in Figure 14.

ing  $\mu_{0.32}$  as a coordinate reduces the scatter in metallicity in the MZR, as it does locally. We left the  $\alpha$  in  $\mu_\alpha \equiv \log(M_*) - \alpha \log(SFR)$  as a free parameter, and

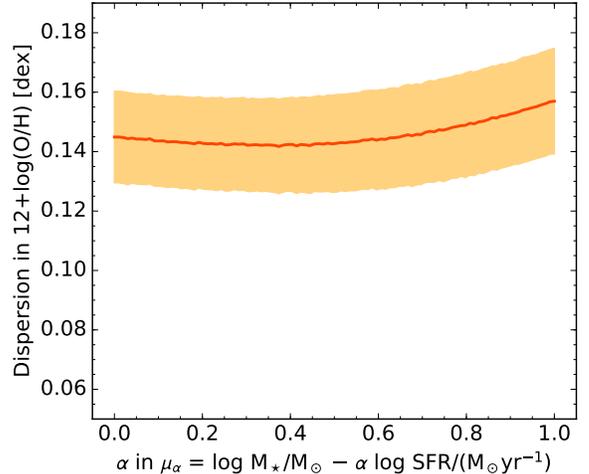


**Figure 17.** Comparison of gas-phase oxygen abundance with  $\mu_{0.32} \equiv \log(M_*/M_\odot) - 0.32 \log(\text{SFR}/[M_\odot \text{ yr}^{-1}])$ . Fundamental metallicity relation proposed by Mannucci et al. (2010) is shown with the solid line extended to  $\mu_{0.32} < 9.5$  following Mannucci et al. (2011).

computed the standard deviation around the best-fit linear regression in the  $12 + \log(\text{O}/\text{H}) - \mu_\alpha$  relation for our sample. The scatter as a function of  $\alpha$  is shown in Figure 18. Mannucci et al. (2010) claimed that at  $z = 0$  with  $\alpha = 0.32$  the scatter decreases to  $\simeq 0.02$  dex compared to  $\simeq 0.06$  dex in the case of the simple MZR (i.e.,  $\alpha = 0$ ). In contrast, varying  $\alpha$  does not seem to reduce the observed scatter around the best-fit line for our  $z = 3.3$  galaxies, but it remains essentially constant around 0.15 dex. We should note that the typical uncertainties of metallicity from strong lines are in general comparable to the scatter in the MZR, in this study as well as in the literature (e.g., Marino et al. 2013; Steidel et al. 2014), which may explain why by varying  $\alpha$  the scatter does not change. Indeed, the number of objects in our sample is still too small to overcome the dominance of the measurement error and to draw firm conclusions on the intrinsic scatter of our  $z \sim 3.3$  MZR. To push down the sampling error, orders of magnitude larger samples would be required, e.g.,  $\gtrsim 10^5$  objects are used in the study of Mannucci et al. 2010 for the local galaxies, whereas  $z \gtrsim 2$  samples include only  $\gtrsim 10^{1-2}$  objects).

### 5.5. A comparison with a simple gas-regulator model

Because of the redshift evolution in both the MS and metallicity, our sample spans a parameter space which is not well covered by the local galaxy population (Maier et al. 2014). Therefore, an extrapolation of the  $Z(M_*, \text{SFR})$  relation is inevitable when trying to compare the local relation with the high redshift one. A more physically motivated relation among the three parameters,  $Z(M_*, \text{SFR})$ , is proposed by Lilly et al. (2013), which indeed can reproduce the FMR at  $z = 0$  and at  $z \simeq 2.3$  with a sensible choice of parameters. We then use the  $Z(M_*, \text{SFR})$  relation in Equation (40) in Lilly



**Figure 18.** Standard deviation around the best-fit linear regression in the  $12 + \log(\text{O}/\text{H}) - \mu_\alpha$  relation as a function of  $\alpha$ , where  $\mu_\alpha \equiv \log(M_*) - \alpha \log(\text{SFR})$ . Solid line and filled region are median and  $1\sigma$  confidence interval based on  $10^4$  bootstrap resampling.

et al. (2013):

$$Z_{\text{eq}}(M_*, \text{SFR}) = Z_0 +$$

$$\frac{y}{1 + \lambda(1 - R)^{-1} + \varepsilon^{-1} \left\{ (1 + \beta - b)\text{SFR}/M_* - (1 - R)^{-1} \frac{1.2}{t} \right\}}, \quad (12)$$

where  $Z_{\text{eq}}$  is the equilibrium metallicity,  $Z_0$  is the metallicity of the incoming gas,  $y$  is the chemical yield,  $\lambda$  is the mass-loading factor ( $\equiv$  outflow rate/SFR),  $R$  is the fraction of mass return due to stellar evolution,  $\varepsilon$  is the star formation efficiency ( $\text{SFE} \equiv \text{SFR}/M_{\text{gas}}$ ),  $\beta$  is the MS slope defined as  $\text{SFR} \propto M_*^{1+\beta}$ , and  $t$  is the age of the Universe in units of Gyr. In Lilly et al. (2013)  $\lambda$  and  $\varepsilon$  are parameterized as follows:

$$\lambda = \lambda_{10} m_{10}^a \quad (13)$$

$$\varepsilon = \varepsilon_{10} m_{10}^b, \quad (14)$$

where  $m_{10}$  is the stellar mass in units of  $10^{10} M_\odot$ .

Following Lilly et al. (2013), we fix the  $\varepsilon$  and  $\lambda$  parameters to the values that reproduce the local FMR of Mannucci et al. (2010), and then use Equation (11) to derive the MZR at  $z = 3.3$  predicted by this regulator model. The result is shown in Figure 14 with the orange shaded area encompassing the cases between  $Z_0/y = 0$  and  $Z_0/y = 0.1$ .

Observations suggest that the SFE may be higher at higher redshift (e.g. Daddi et al. 2010; Genzel et al. 2010). We also show with the green shaded area in Figure 14 the model predictions in the case for  $\varepsilon \propto (1 + z)$ . These two cases virtually enclose our  $z \simeq 3.3$  sample, while the majority of them is consistent with the prediction with non-evolving  $\varepsilon$ .

In Section 5.4 we have shown that the scatter of the MZR does not change appreciably by introducing the SFR as a second parameter. Together with the observed data, Figure 15 shows the corresponding relations as predicted by the regulator models as well as those observationally defined and extrapolated for the MS at  $z = 3.3$ . In general, compared to our data a steeper dependence is

predicted of the metallicity offset from the MZR as function of the SFR offset from the MS. Although this apparent mismatch may be due to large errors and small sample size, it may give some insight into the functional form of the SFH of the galaxies studied here. Indeed, the dependence of metallicity on SFR would disappear if galaxies were evolving at constant SFR, i.e.,  $d\text{SFR}/dt \simeq 0$  (see [Appendix E](#) for the detail).

In [Figure 16](#) we compare the redshift evolution of the MZR at  $M_\star = 10^{10} M_\odot$  with the model predictions described above. The evolving  $Z(M_\star, \text{SFR})$  relation assuming  $\varepsilon \propto (1+z)$  traces the observed trend up to  $z \simeq 2.5$ , with an exception for the data point of [Cullen et al. \(2014\)](#). As mentioned above, our sample appears to prefer a non-evolving star formation efficiency, as do the data by [Maier et al. \(2014\)](#) at  $z \sim 2.3$ . However, the observational scatter of  $\gtrsim 0.1$  dex for the high redshift measurements may hamper to distinguish models at better than the  $\simeq 2.5\sigma$  level. On the other hand, the departure in metallicity from the original  $z = 0$  FMR by [Mannucci et al. \(2010\)](#), as seen in [Figure 17](#), can be due the extrapolation of the local FMR into a parameter space which is basically unpopulated at  $z = 0$ . Perhaps a more suitable  $\gamma$  would lie in-between the two cases above, 0 and 1. For instance, a recent study by [Genzel et al. \(2015\)](#) derived  $\gamma = 0.34 \pm 0.15$ , based on a combined analysis of CO and dust scaling relations at  $0 \lesssim z \lesssim 3$ . Of course, the other parameters of the regulator model and their mass dependence may also evolve with redshift, hence being different at  $z \simeq 3.3$ , but the current sample size is too small to explore the entire parameter space.

## 6. SUMMARY

Using the rest-frame optical spectra of 43 normal star-forming galaxies lying close to the star-forming main-sequence at  $z \sim 3.3$ , we carried out a study of the properties of the ionized gas and their relations with global galaxy parameters. Our main results can be summarized as follows.

1. Strong optical emission lines contribute significantly to the broad-band flux, especially in the  $K$  band, with a median of 21%, but up to  $\sim 100\%$  in a few cases. These emission lines affect the estimate of stellar masses from SED fitting by 0.13 dex (median), but the difference may exceed  $\sim 0.5$  dex when the emission line contribution is  $\gtrsim 40\%$ .
2. A comparison between UV- and  $H\beta$ -based SFRs suggests a lower additional extinction toward H II regions at  $z \sim 3.3$ , compared to the local calibration [Calzetti et al. \(2000\)](#).
3. The ionization parameter appears to be systematically higher than its average for the local SFGs, extending the local relationship in the  $R_{23}$  vs.  $O_{32}$  diagram. The ionization parameter derived from the  $O_{32}$  indices does not show any correlation with galaxy global properties, except with the SFR. However, the correlation between SFR and ionization parameter for our sample is not very significant ( $\simeq 2\sigma$ ) compared with those in the literature (e.g., [Sanders et al. 2016](#)). Electron density derived from resolved  $[\text{O II}]\lambda 3727$  doublets also does not show any correlation with galaxy properties.
4. The MZR of our  $z \sim 3.3$  galaxies shows a  $\sim 0.7$  dex offset from the local relation and a  $\sim 0.3$  dex offset relative to  $z \sim 2$ , indicating very rapid evolution of gas-phase metallicity at  $z \sim 3$ .
5. Among our galaxies at  $z \simeq 3.3$  we do not find any correlation of metallicity with SFR. If such a correlation exists it has to span a metallicity range narrower than measurement errors.
6. Our  $z \sim 3.3$  sample does not follow the locally defined FMR, with metallicities being offset by  $\sim 0.3$  dex compared to the value predicted by the FMR for  $z = 3.3$ . This mismatch may result from the extrapolation of the  $Z(M_\star, \text{SFR})$  relation empirically defined at  $z = 0$  to  $Z$ , SFR and  $M_\star$  combinations which are not well populated by  $z = 0$  galaxies, hence giving an incorrect prediction for the evolution of MZR.
7. For our sample, no projection of the  $Z(M_\star, \text{SFR})$  relation to the  $\mu_\alpha$  space is able to reduce the scatter in metallicity, suggesting that the SFR may not play a significant role as a second parameter in the MZR. However, the uncertainties in metallicity determination and the small sample size prevent us to draw a firm conclusion on this issue.
8. A comparison of the MZR of our galaxies and those at different redshifts with the prediction of a simple gas-regulator model suggests that a weakly evolving star formation efficiency could better account for the observed redshift evolution of MZR.

The data presented herein were obtained at the W.M. Keck Observatory, which is operated as a scientific partnership among the California Institute of Technology, the University of California and the National Aeronautics and Space Administration. The Observatory was made possible by the generous financial support of the W.M. Keck Foundation. The authors wish to recognize and acknowledge the very significant cultural role and reverence that the summit of Mauna Kea has always had within the indigenous Hawaiian community. We are most fortunate to have the opportunity to conduct observations from this mountain. The observations were partly carried out within the framework of Subaru-Keck time exchange program. This research made use of [Astropy](#)<sup>8</sup>, a community-developed core Python package for Astronomy ([Astropy Collaboration et al. 2013](#)), [APLpy](#)<sup>9</sup>, an open-source plotting package for Python, and [matplotlib](#)<sup>10</sup>, a Python 2D plotting library ([Hunter 2007](#)). We thank Scott Dahm, Marc Kassis, Jim Lyke, and Greg Wirth, and the rest of the staff at the Keck observatory for supporting the observations, Andreas Faisst, Nicholas Konidaris, Luca Rizzi, and Benny Trakhtenbrot for the assistance on the MOSFIRE data reduction, and Roberto Maiolino, Claudia Scarlata, and Maryam Shirazi for insightful discussions. We thank

<sup>8</sup> <http://www.astropy.org>

<sup>9</sup> <http://aplpy.github.com>

<sup>10</sup> <http://matplotlib.org>

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*Facilities:* Keck I (MOSFIRE)

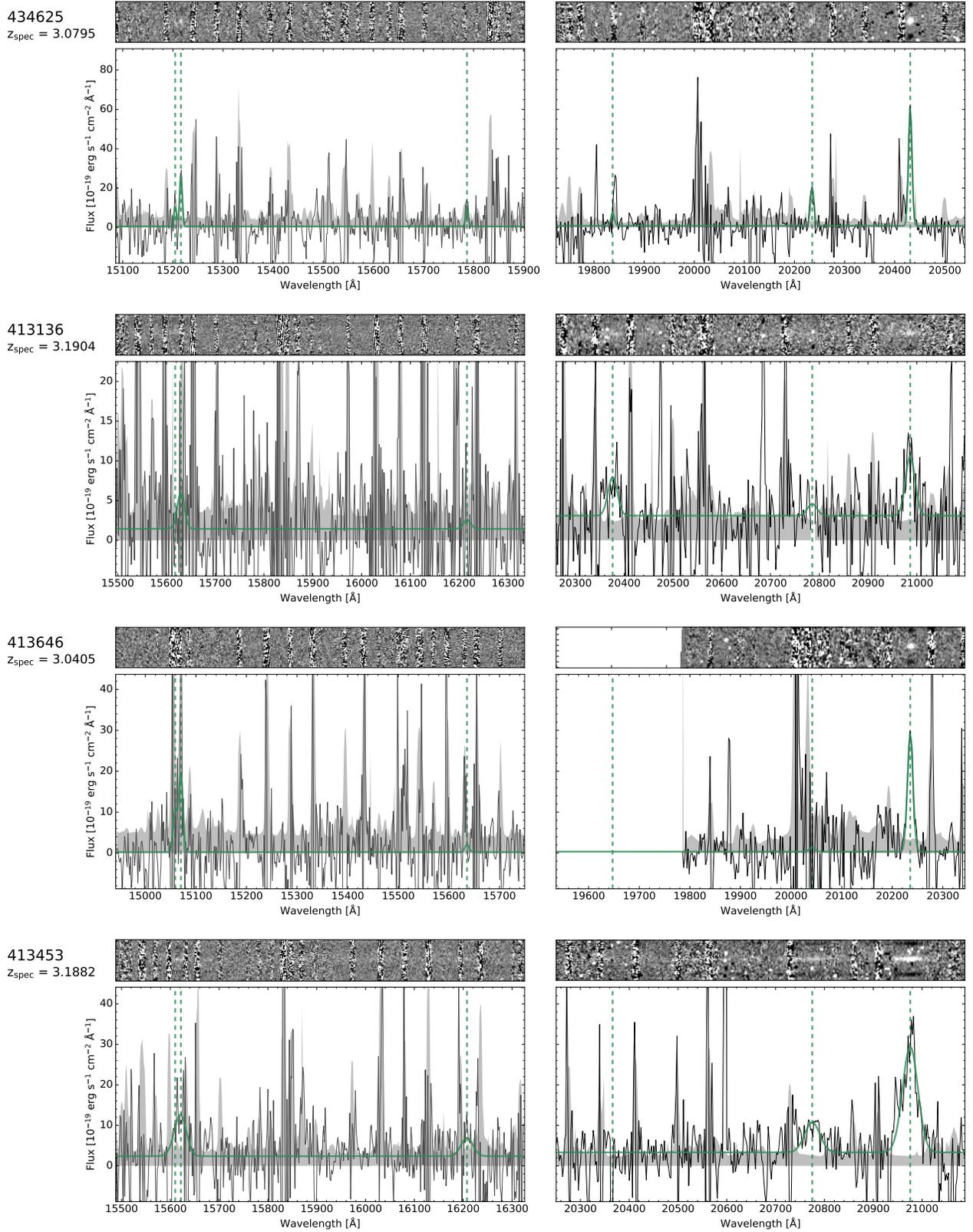
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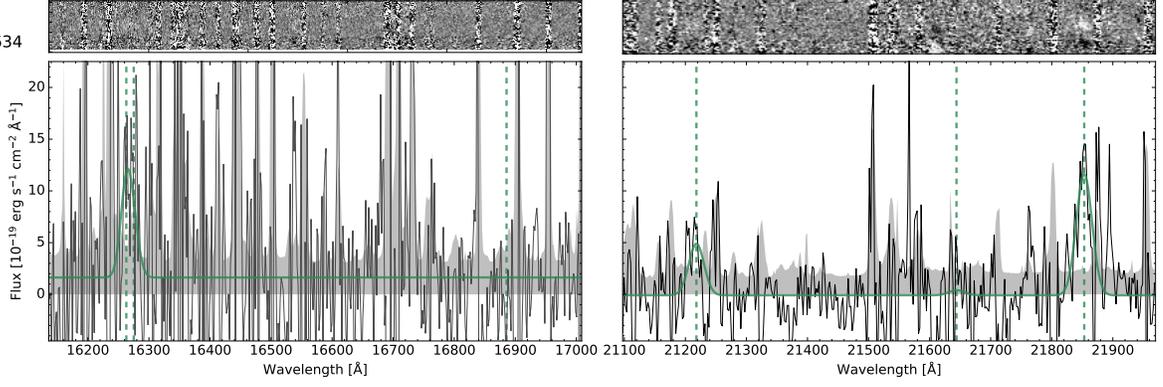
## APPENDIX

## A. MOSFIRE SPECTRA

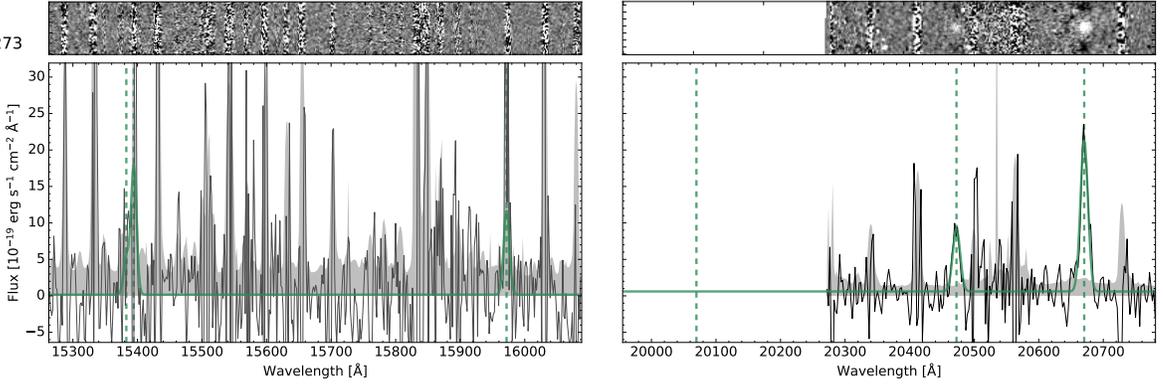


**Figure A1.** MOSFIRE spectra of each object in  $H$ - (left) and  $K$ -band (right). (Top) 2-dimensional spectra. (Bottom) 1-dimensional spectra for objects (solid line),  $1\sigma$  noise (gray filled area), and the best-fit (green solid line). From left to right, dashed lines indicate the location of  $[\text{O II}]\lambda\lambda 3726, 3729$ ,  $[\text{Ne III}]\lambda 3869$ ,  $\text{H}\beta$ , and  $[\text{O III}]\lambda\lambda 4959, 5007$ .

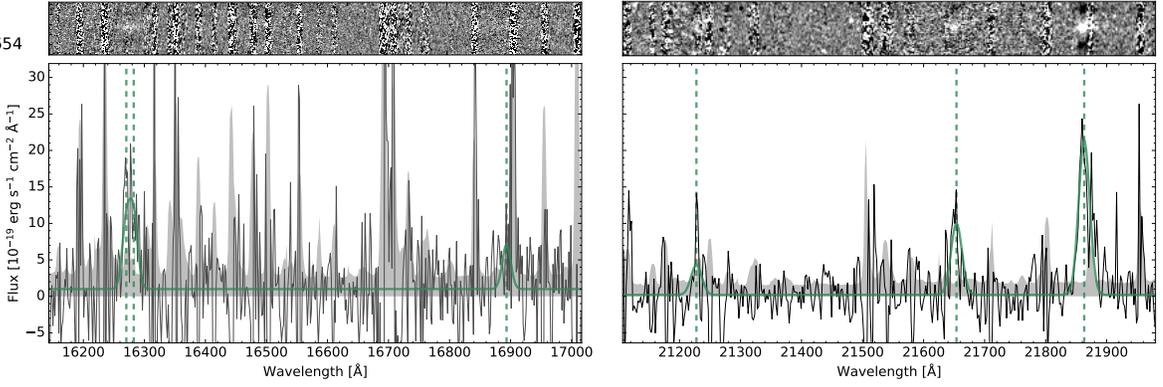
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 $z_{\text{spec}} = 3.3634$



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 $z_{\text{spec}} = 3.1273$



413391  
 $z_{\text{spec}} = 3.3654$



427122  
 $z_{\text{spec}} = 3.0416$

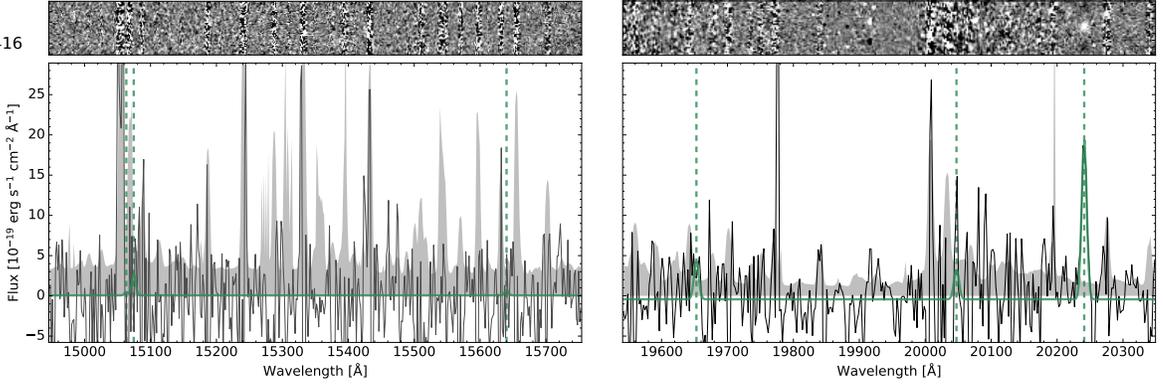
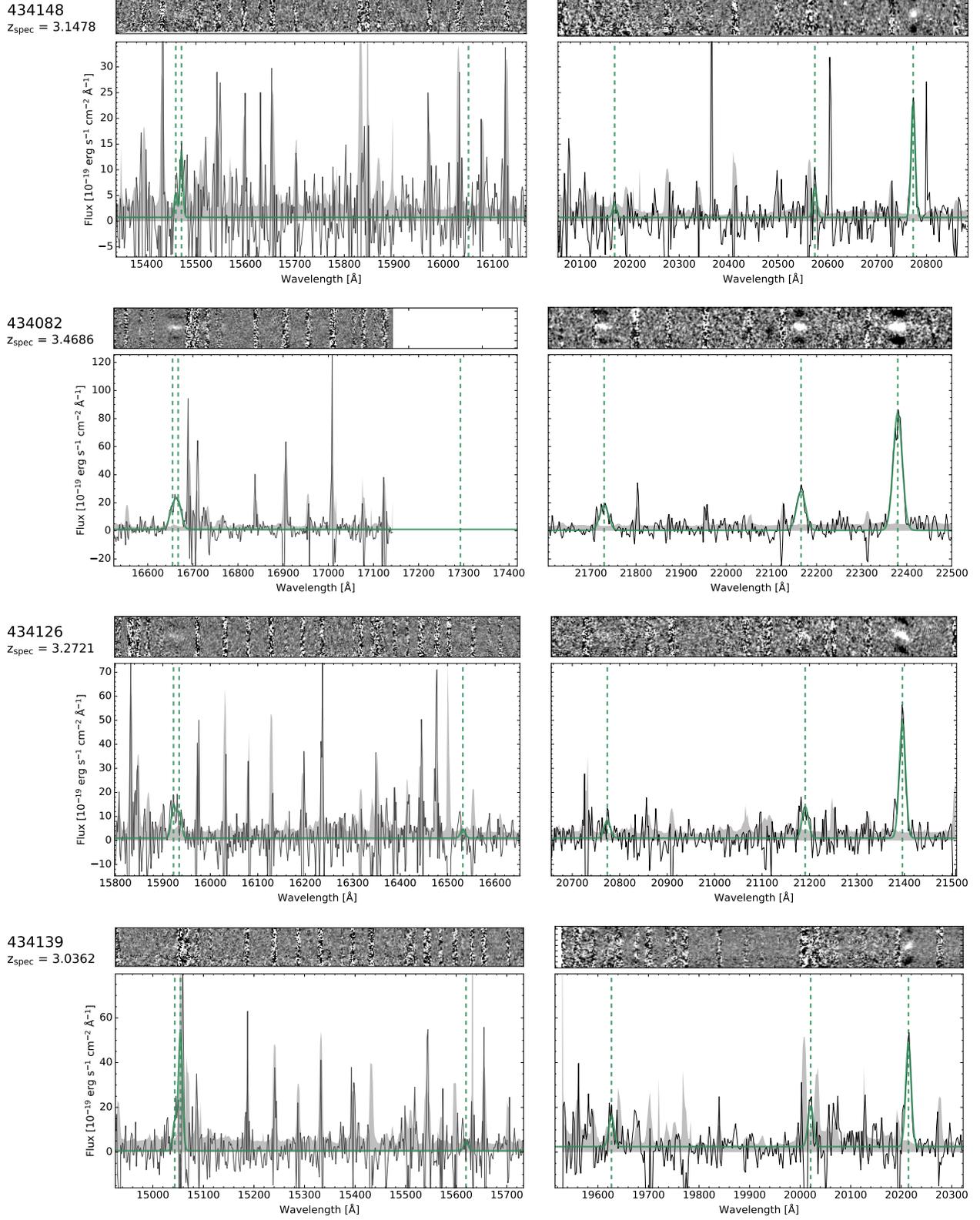


Figure A1. *continued.*

Figure A1. *continued.*

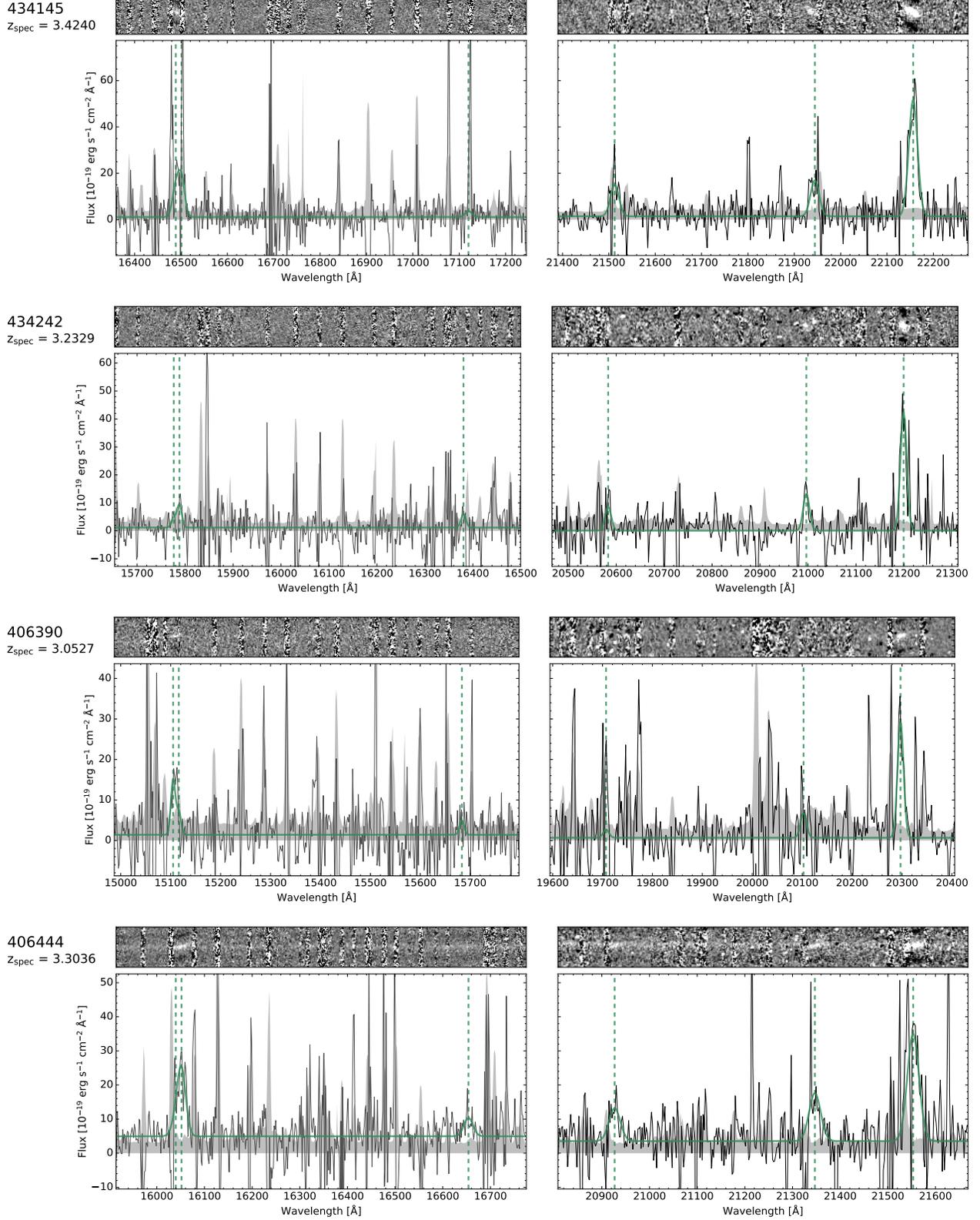
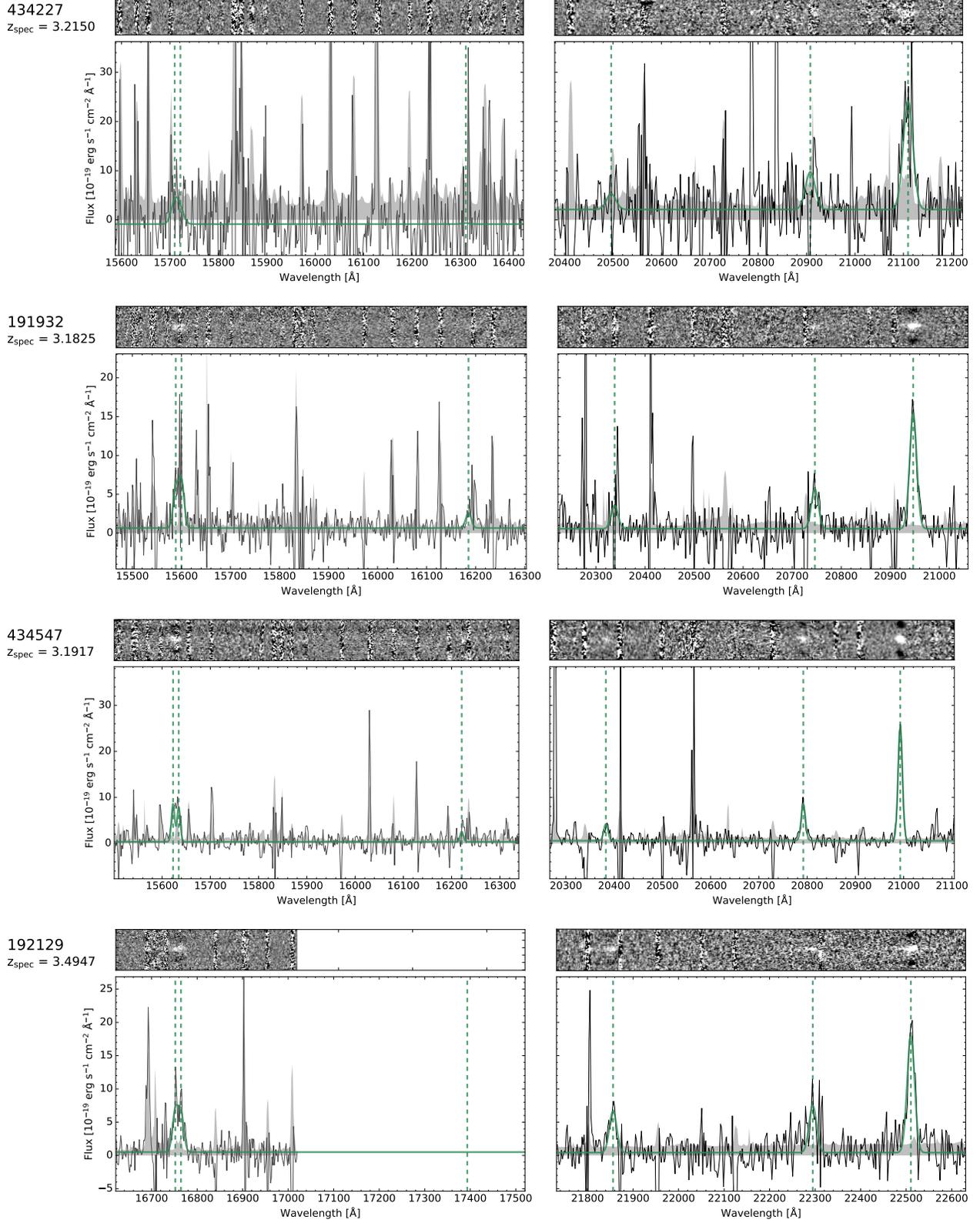


Figure A1. *continued.*

Figure A1. *continued.*

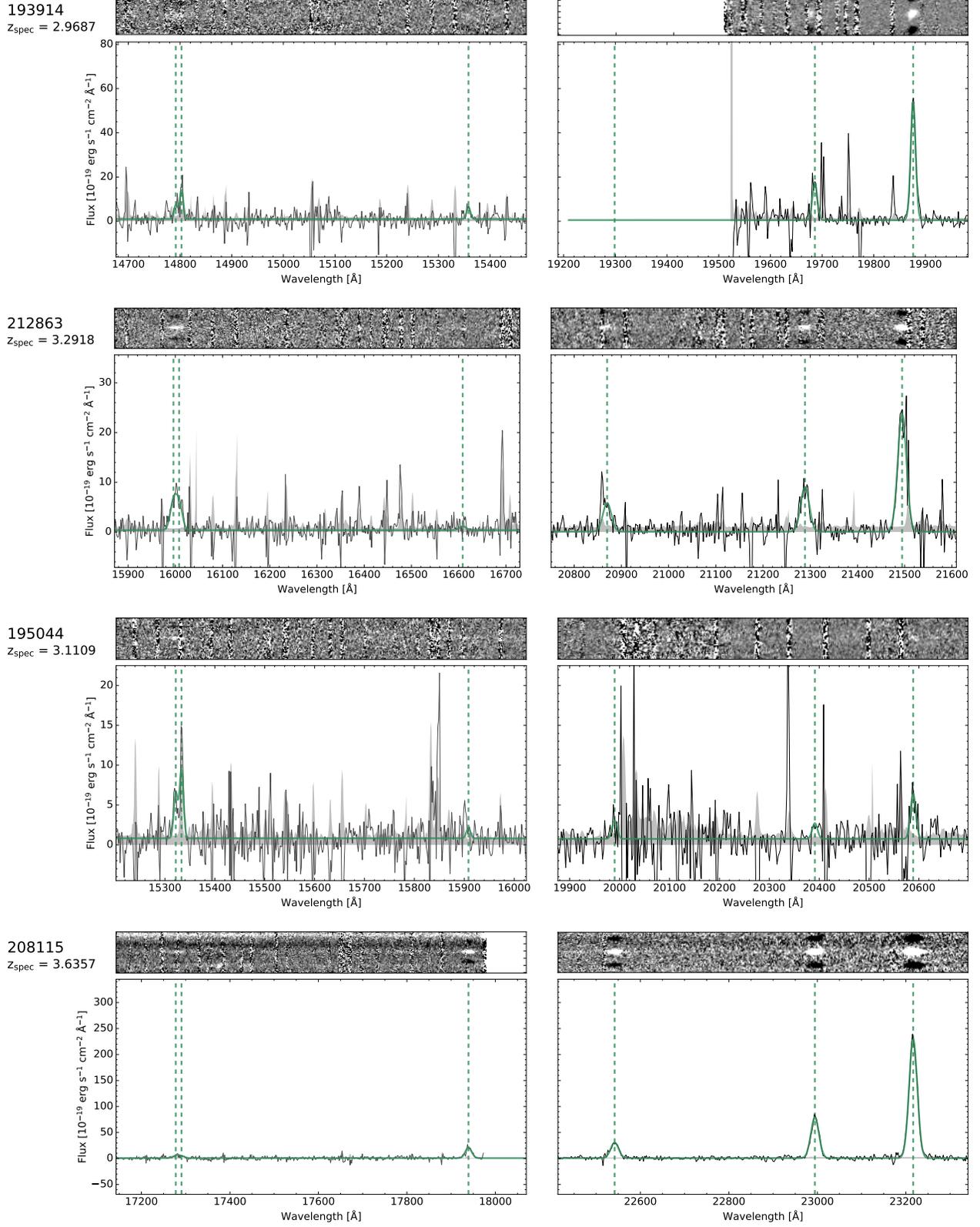
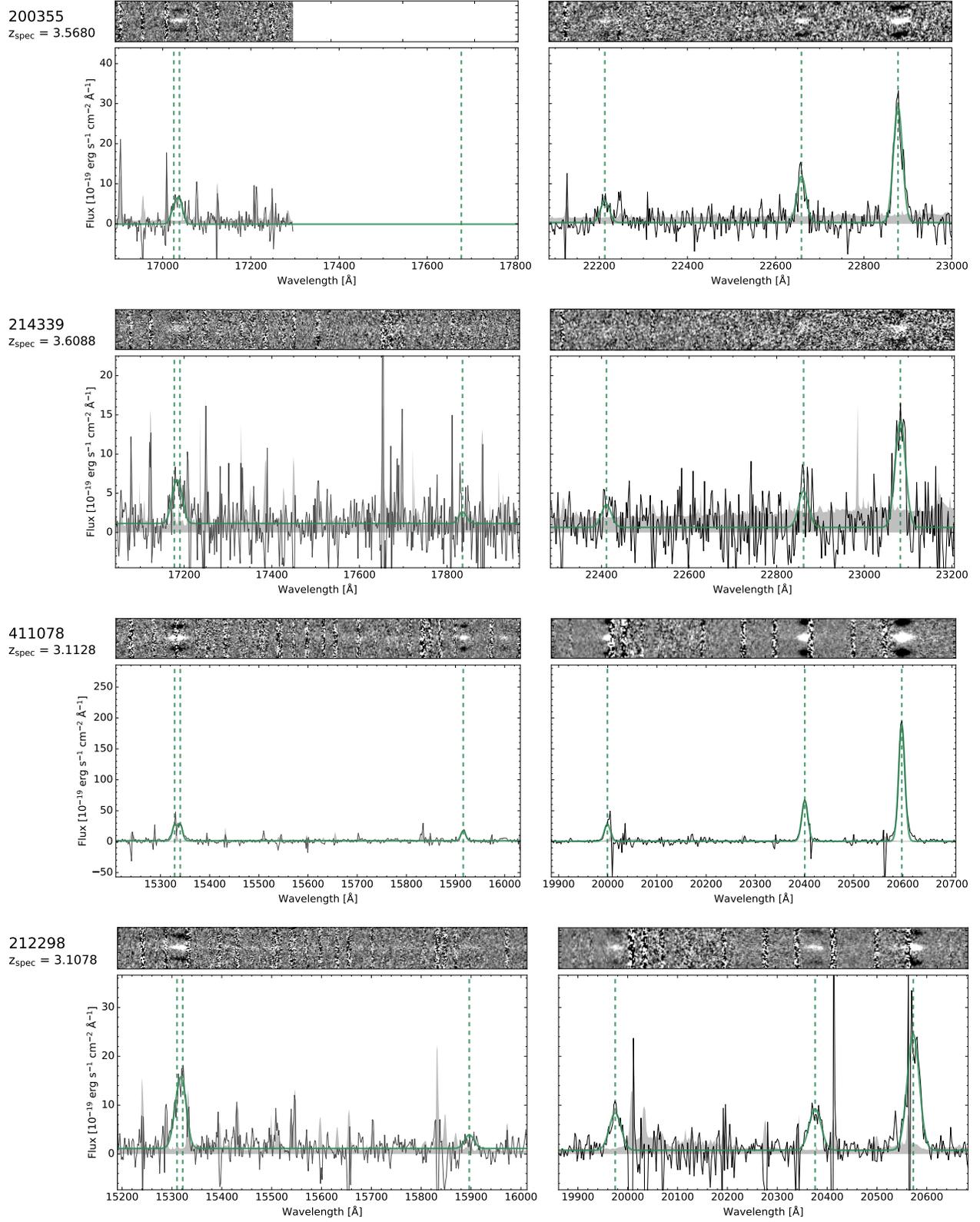


Figure A1. *continued.*

Figure A1. *continued.*

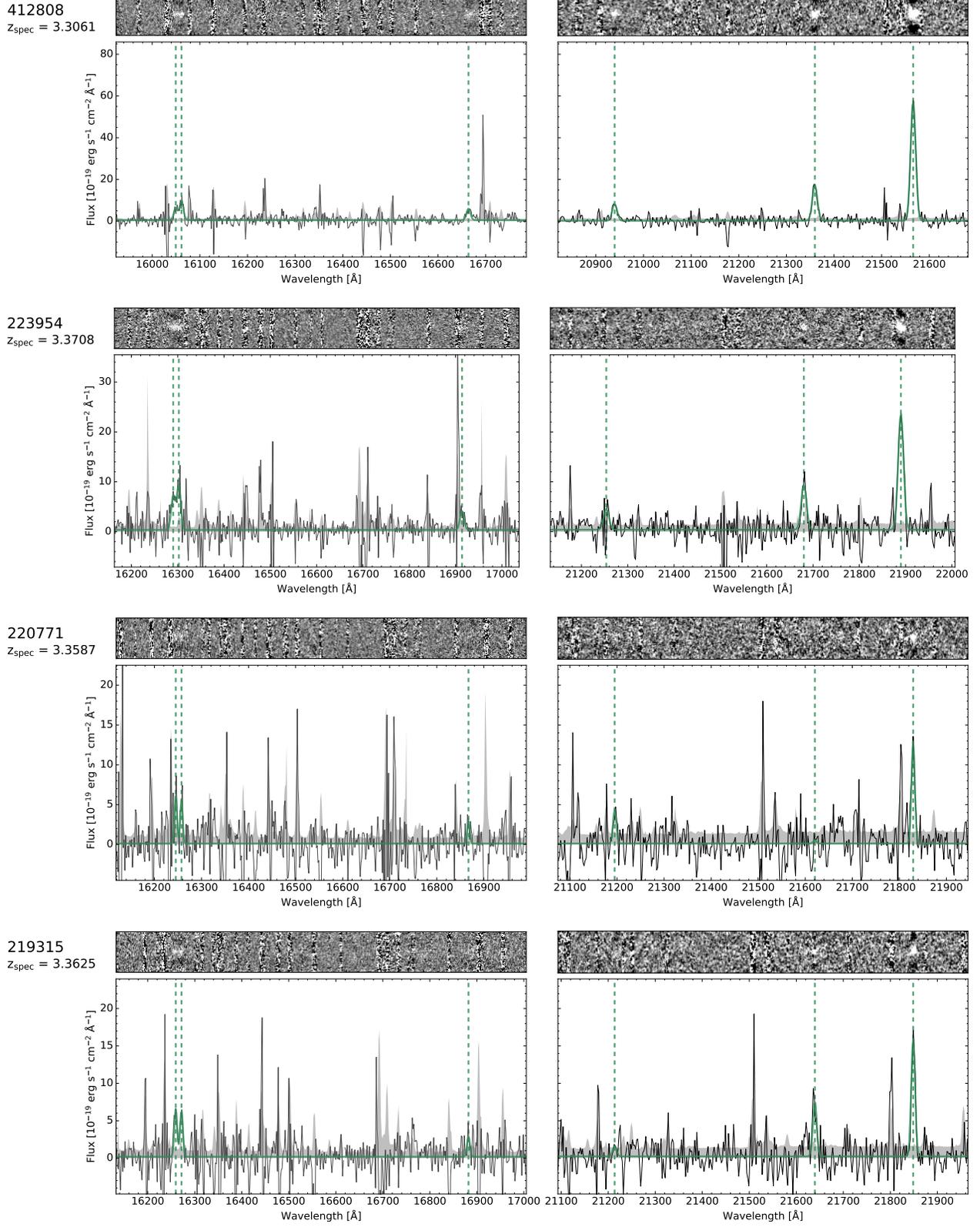
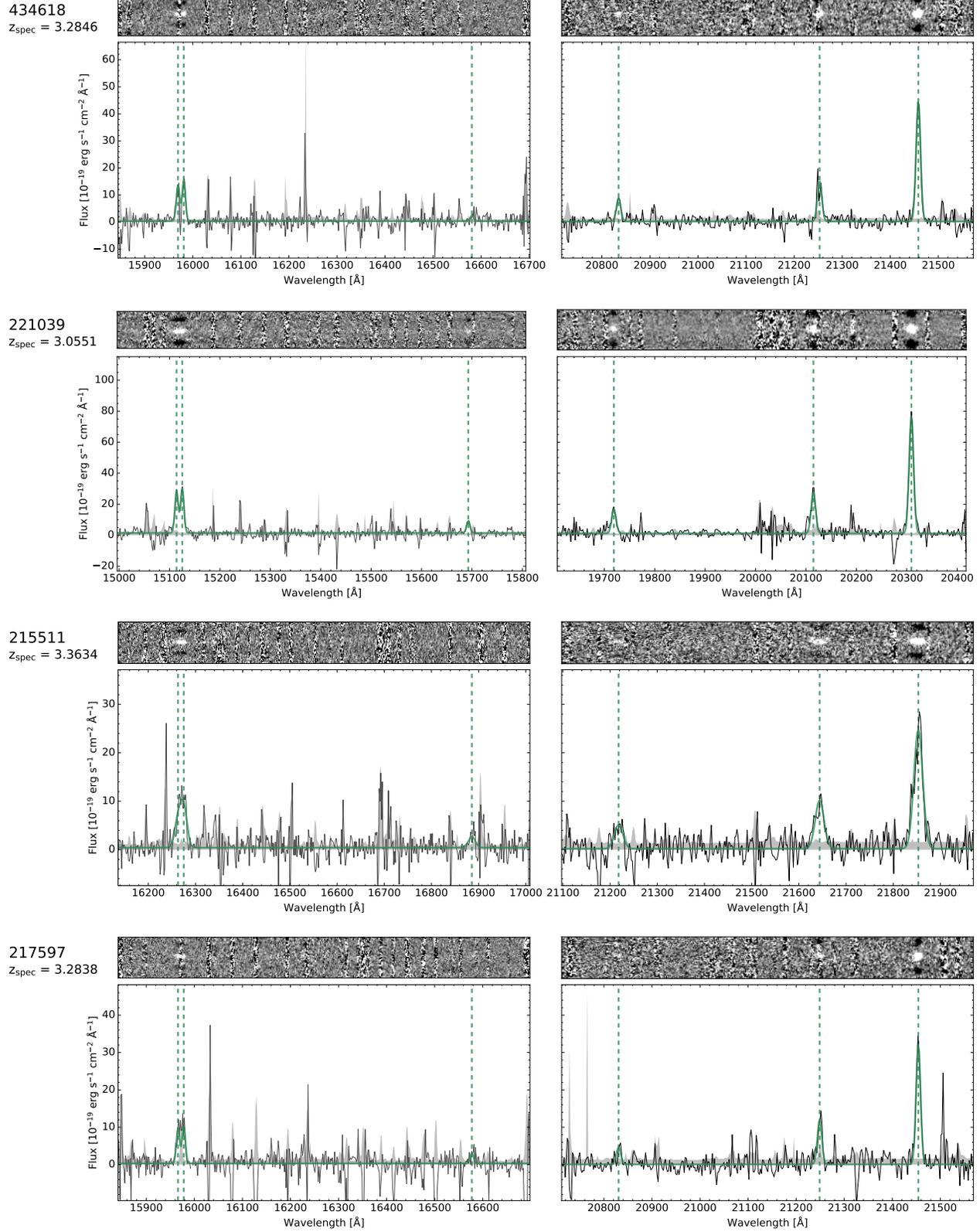
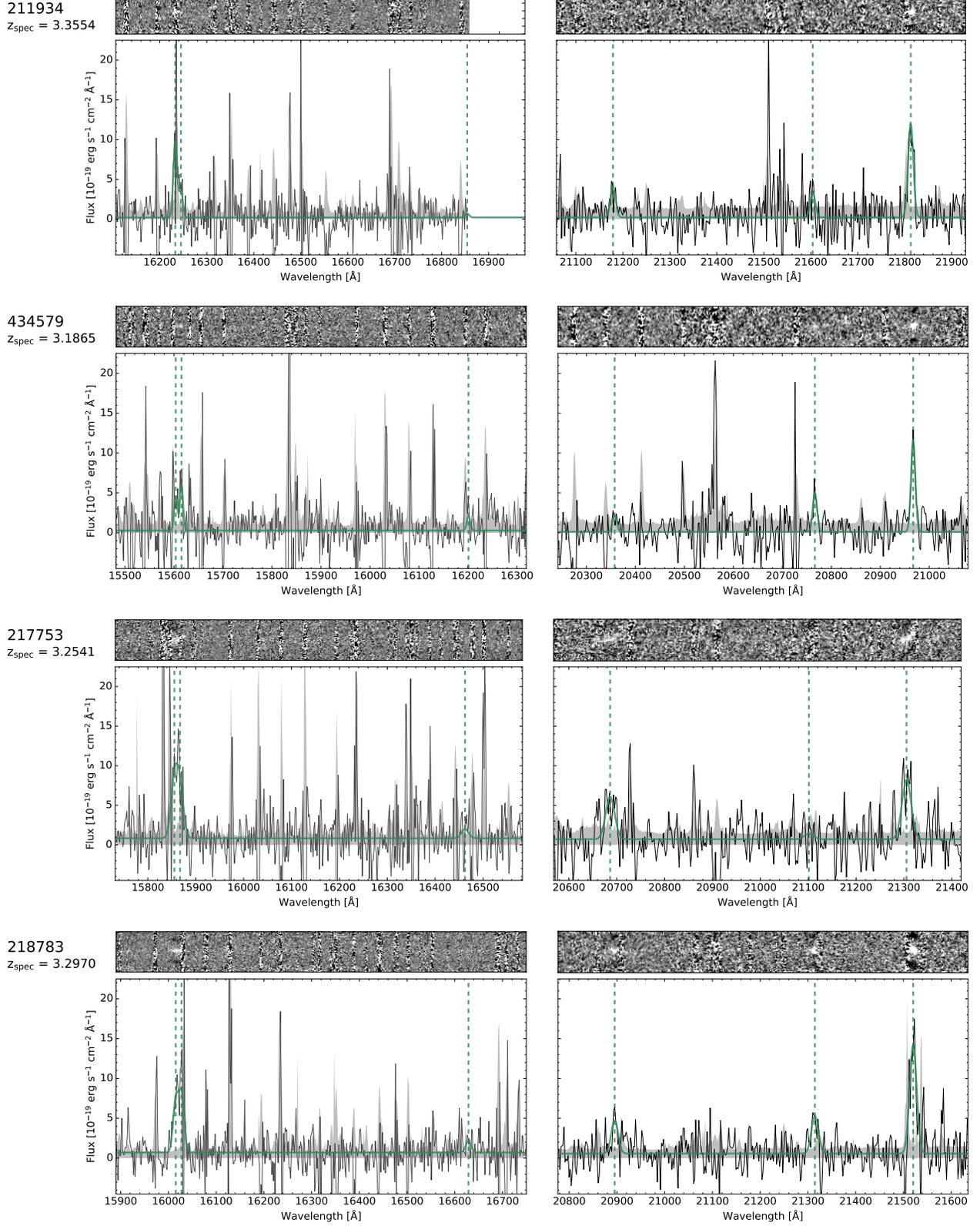
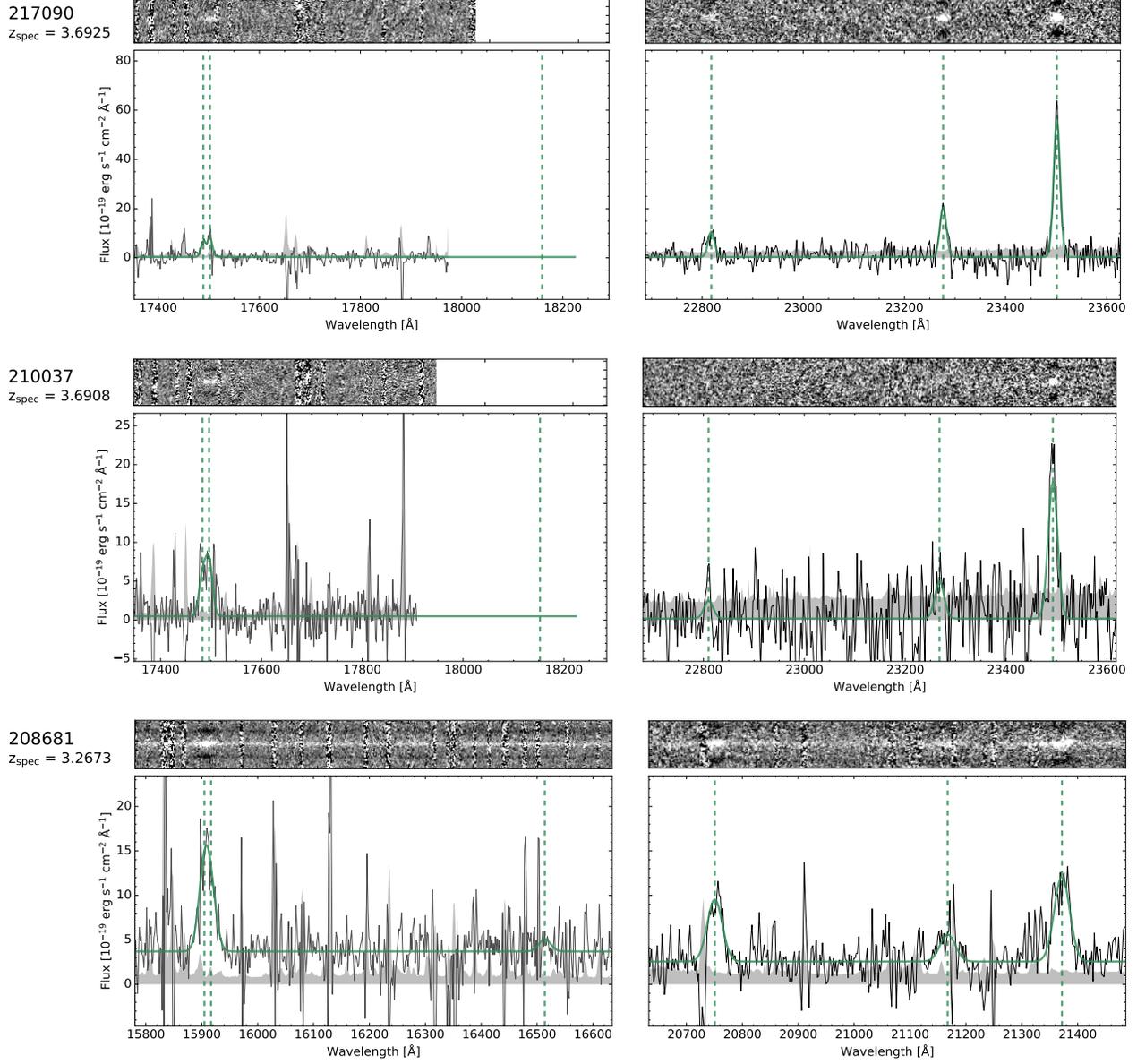
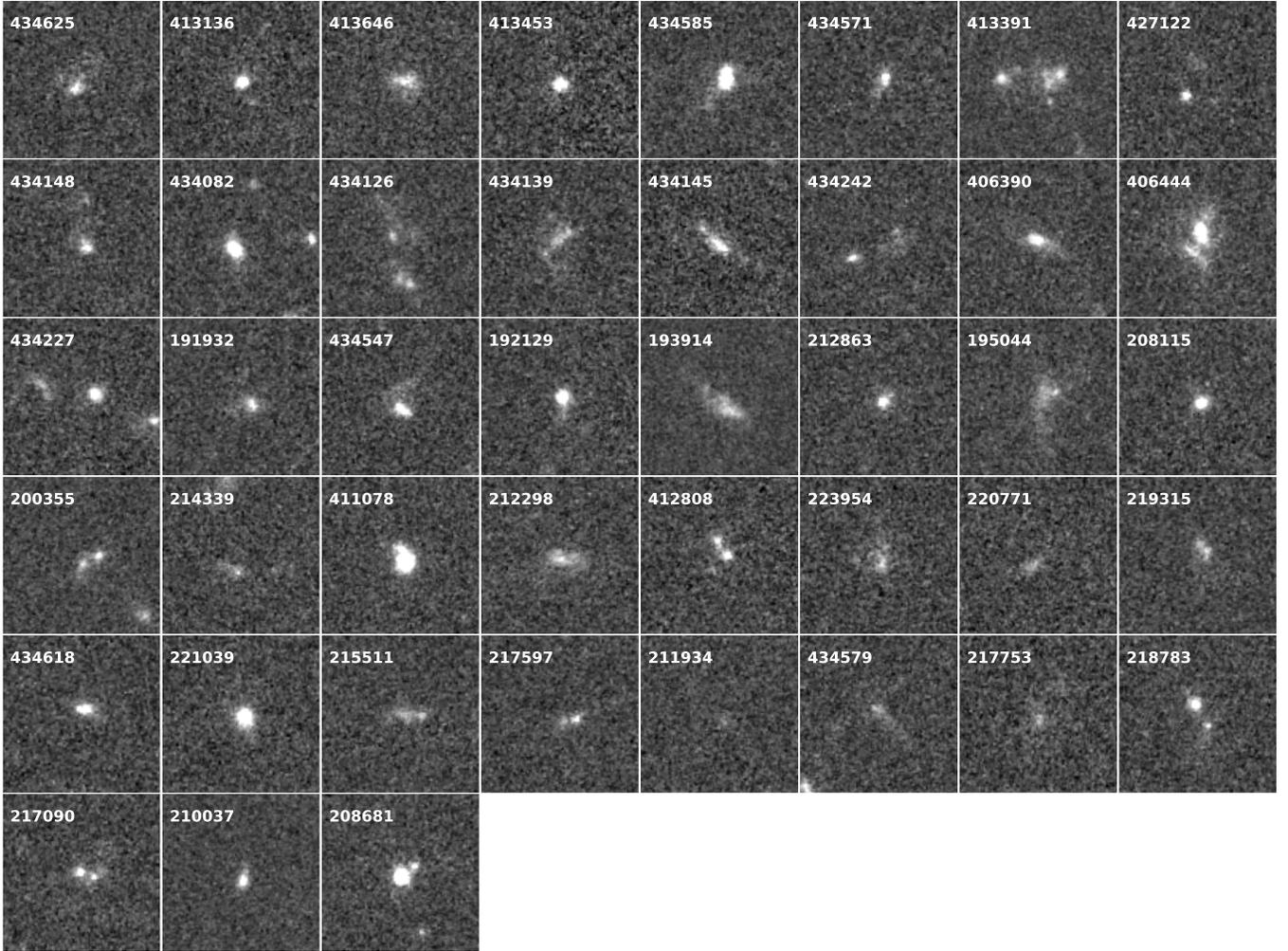


Figure A1. *continued.*

Figure A1. *continued.*


 Figure A1. *continued.*

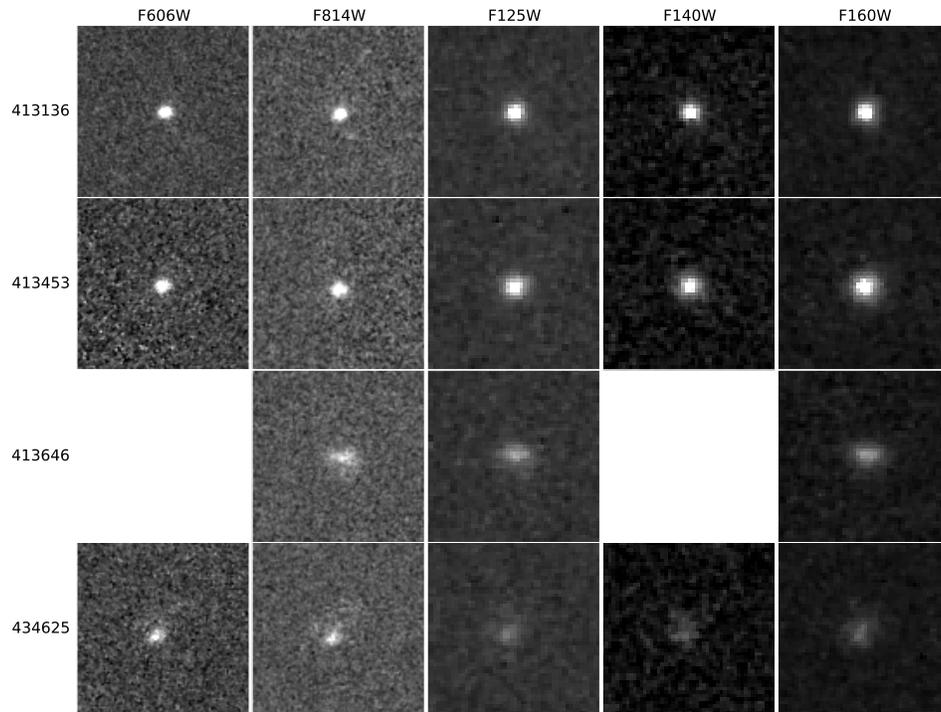
Figure A1. *continued.*



**Figure B1.** *HST*/ACS F814W stamps of the sample. North is up and the size of each stamp is  $3 \times 3$  arcsec<sup>2</sup>.

## B. HST IMAGE STAMPS

**Figure B1** shows *Hubble Space Telescope* (*HST*) Advance Camera for Surveys (ACS) F814W stamps of those with robust spectroscopic redshifts. For those observed with the CANDELS and 3D-HST surveys (Grogin et al. 2011; Koekemoer et al. 2011; Brammer et al. 2012; Skelton et al. 2014), ACS F606W, Wide Field Camera 3 (WFC3) F125W, F140W, and F160W images are shown in **Figure B2**.



**Figure B2.** *HST* CANDELS stamps of the sample. North is up and the size of each stamp is  $3 \times 3$  arcsec<sup>2</sup>. ACS/F814W image is the same as in [Figure B1](#) and WFC3/F140W image is from 3D-HST.

## C. BROAD-BAND SED

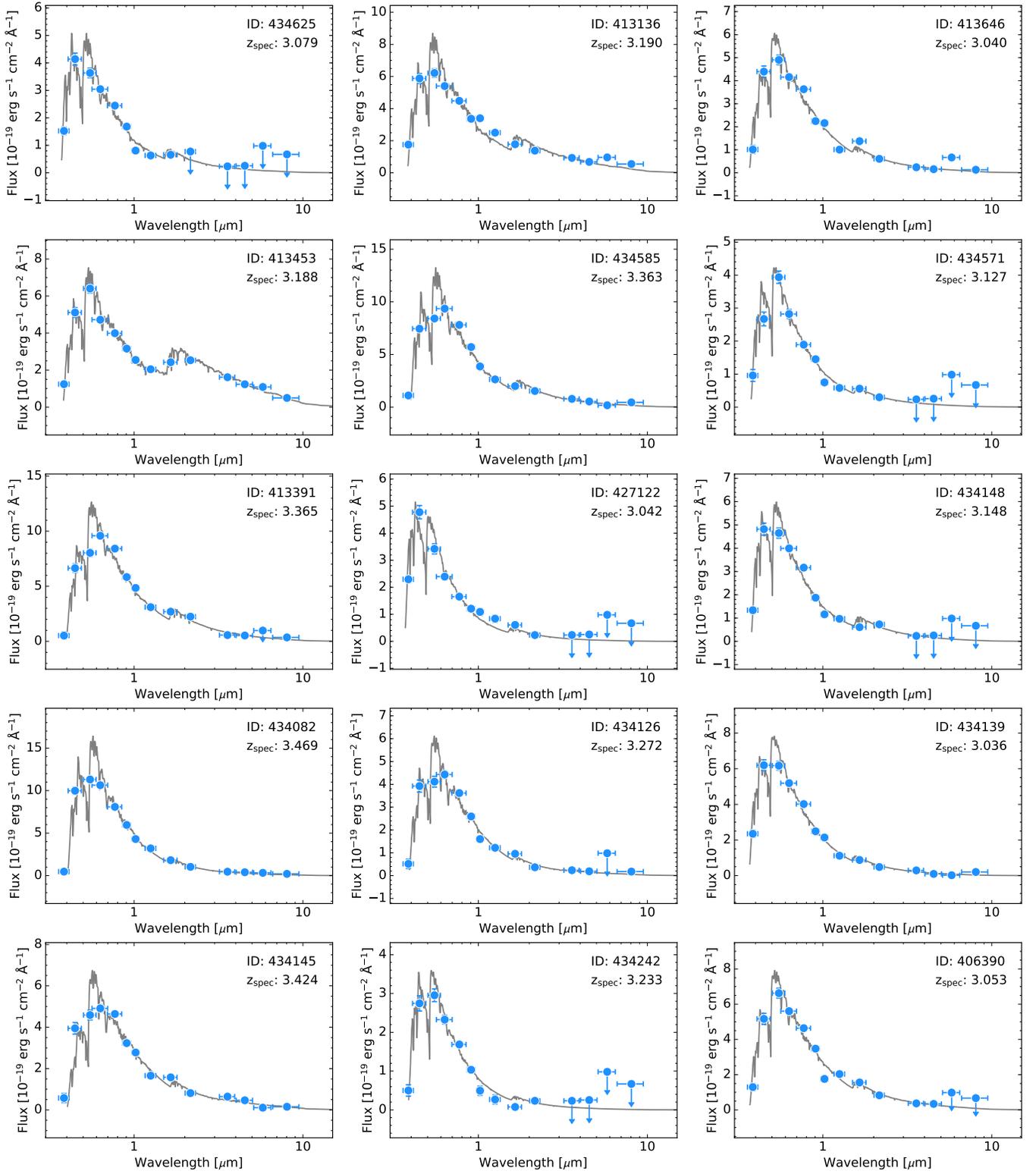
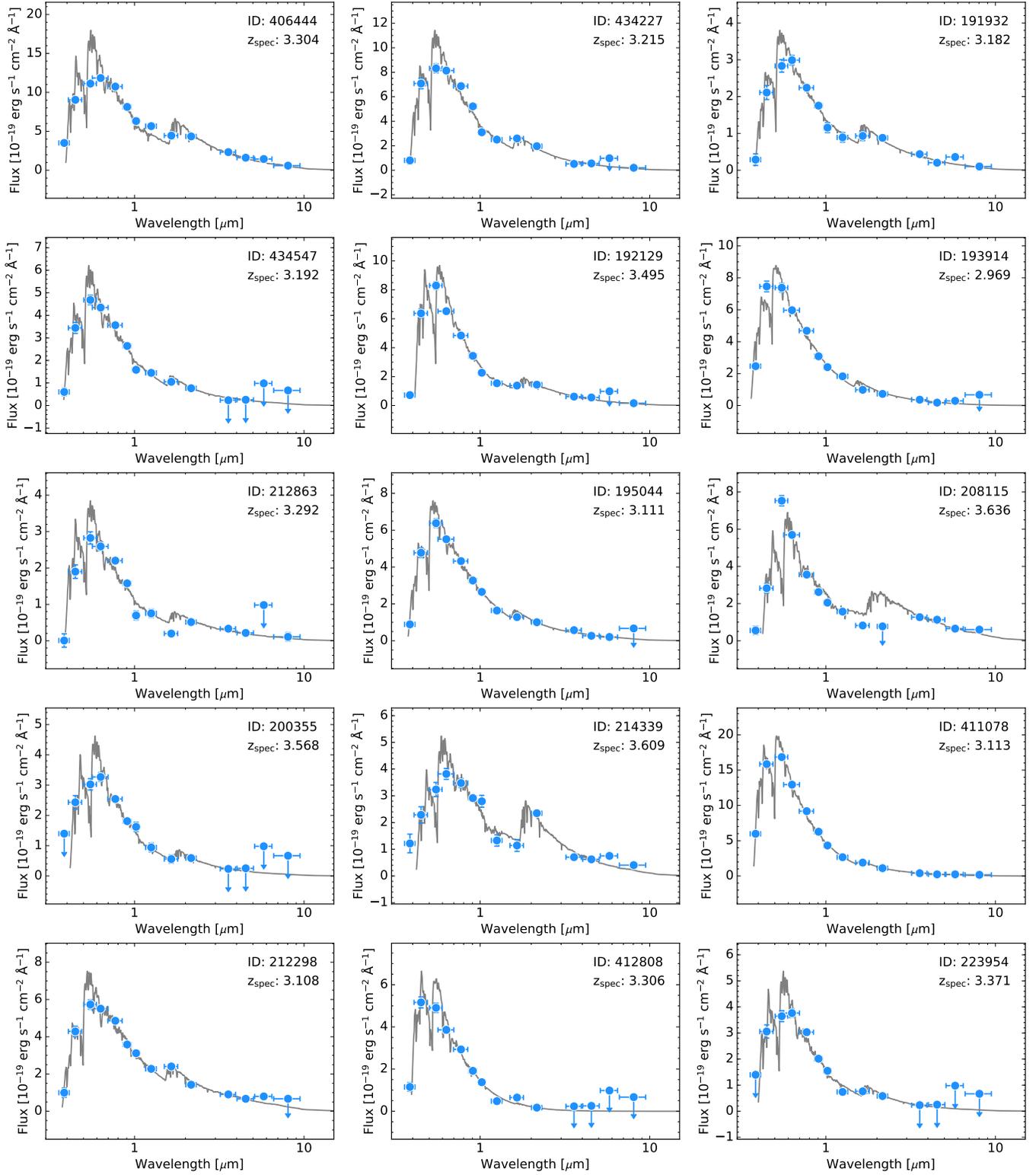
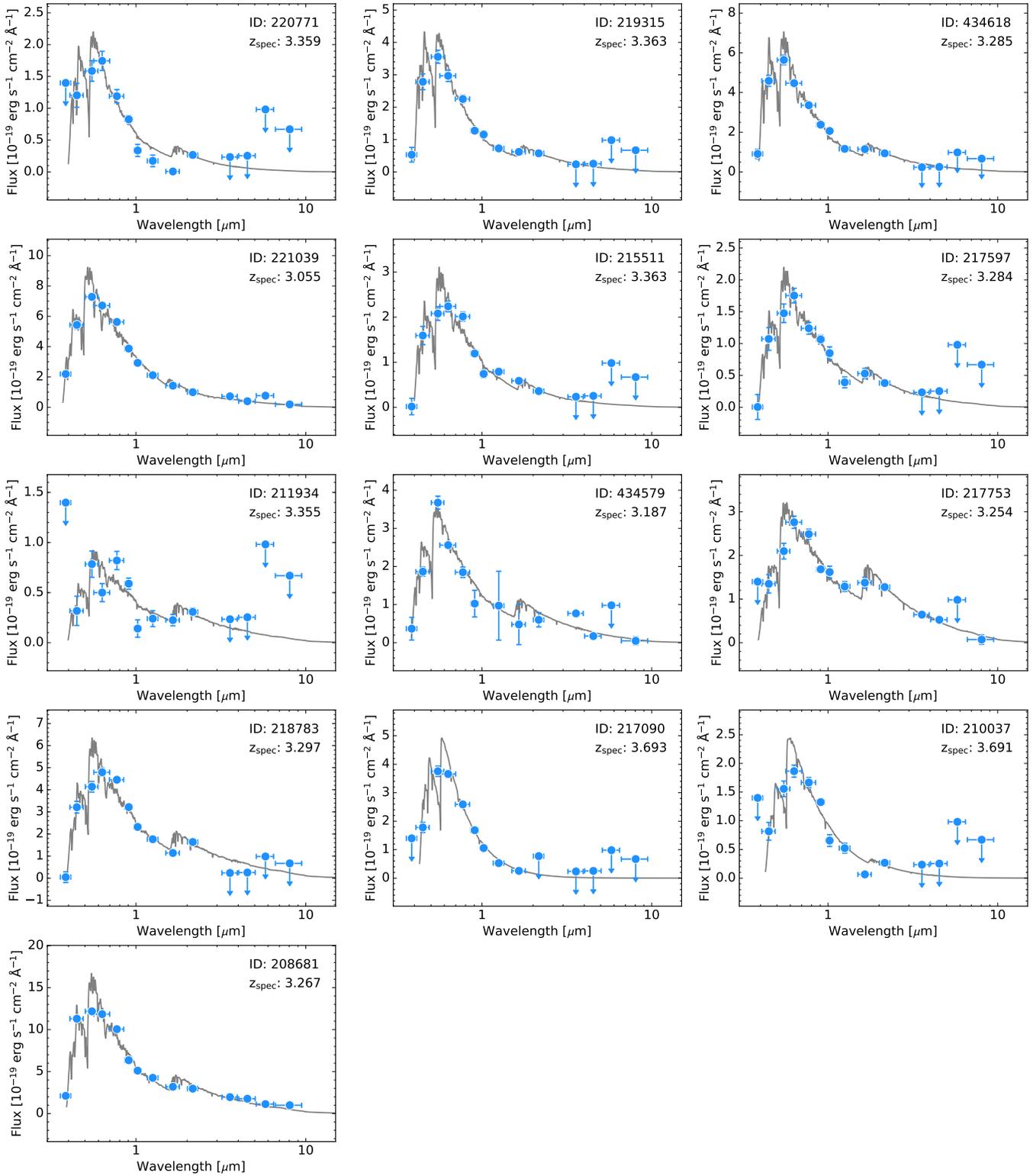


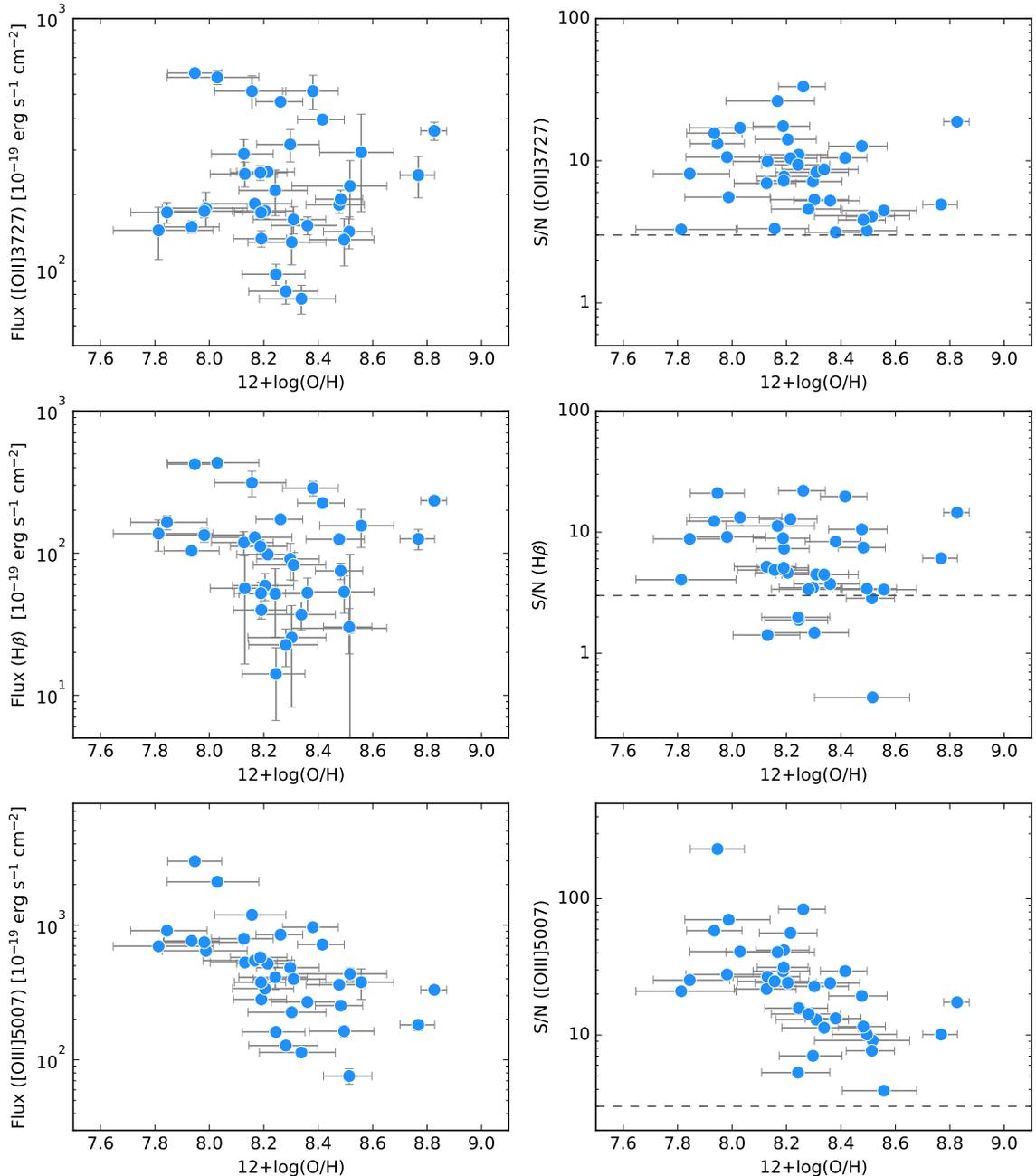
Figure C1. Best-fit SED.

Figure C1. *continued.*


 Figure C1. *continued.*

## D. WHO DOES CONTRIBUTE THE MOST IN THE STACKING?

Figure 9 shows each line ratio as a function of  $12 + \log(\text{O}/\text{H})$  and distribution of  $12 + \log(\text{O}/\text{H})$ . Stacked spectrum shows lower metallicity than the median metallicity of all objects. The same trend was seen in a previous work by Troncoso et al. (2014) in which they found slightly lower metallicity at a given stellar mass for the stacked measurement than the average of individual measurement. At least in our case, this discrepancy can be explained by the way we stacked spectra. We normalized each spectrum by the  $[\text{O III}]\lambda 5007$  luminosity and stacked them weighted by the inverse variance at each wavelength pixel. Therefore, the resulting emission lines of stacked spectrum are dominated by objects with higher S/N and less OH sky line contamination. In Figure D1, we show absolute fluxes and S/N ratios of strong emission lines as a function of gas-phase oxygen abundance for individual galaxies. As seen from the figure,  $[\text{O III}]$  is indeed dominated by metal-poor objects, while  $\text{H}\beta$  and  $[\text{O II}]\lambda 3727$  emission lines have more contribution from more metal-rich objects. However, in the case that only  $[\text{O III}]$  has enhanced flux with respect to the other lines, the line ratios used to investigate the metallicity tend to favor low metallicity, in particular for the  $[\text{O III}]/[\text{O II}]\lambda 3727$  ratio.



**Figure D1.** *Left:* Fluxes of  $[\text{O II}]\lambda 3727$  (Top),  $\text{H}\beta$  (Middle), and  $[\text{O III}]\lambda 4959$  (Bottom) as a function of gas-phase oxygen abundance. *Right:* Signal-to-noise ratios for the same emission lines as the left panels as a function of  $12 + \log(\text{O}/\text{H})$ . Dashed lines indicates S/N = 3.

## E. ON THE SFR DEPENDENCE IN METALLICITY IN THE REGULATOR MODEL OF LILLY ET AL. (2013)

The general form of gas-phase metallicity in a quasi-steady state of the gas regulator model by Lilly et al. (2013) is their Equation (28) as follows.

$$Z_{\text{eq}}(M_{\star}, \text{SFR}) = Z_0 + \frac{y}{1 + \lambda(1 - R)^{-1} + \varepsilon^{-1} \left\{ M_{\star}^{-1} \cdot \text{SFR} + (1 - R)^{-1} \frac{d \ln \mu}{dt} \right\}}. \quad (\text{E1})$$

Since  $\mu = \varepsilon^{-1} \cdot \text{sSFR}$ ,  $d \ln \mu / dt$  is calculated as

$$\begin{aligned} \frac{d \ln \mu}{dt} &= -\varepsilon^{-1} \frac{d\varepsilon}{dt} + \text{SFR}^{-1} \frac{d\text{SFR}}{dt} - M_{\star}^{-1} \frac{dM_{\star}}{dt} \\ &= -\varepsilon^{-1} \frac{d\varepsilon}{dt} + \text{SFR}^{-1} \frac{d\text{SFR}}{dt} - (1 - R) \text{sSFR}, \end{aligned} \quad (\text{E2})$$

where  $dM_{\star}/dt$  is substituted by  $(1 - R)\text{SFR}$  as this term describes the build-up of long-lived stars in the system (see Lilly et al. 2013).

Substituting the denominator of the second term in Equation E1 by Equation E2 yields

$$\begin{aligned} &1 + \lambda(1 - R)^{-1} + \varepsilon^{-1} \left\{ M_{\star}^{-1} \cdot \text{SFR} + (1 - R)^{-1} \frac{d \ln \mu}{dt} \right\} \\ &= 1 + \lambda(1 - R)^{-1} + \varepsilon^{-1} (1 - R)^{-1} \left\{ \text{SFR}^{-1} \frac{d\text{SFR}}{dt} - \varepsilon^{-1} \frac{d\varepsilon}{dt} \right\}. \end{aligned} \quad (\text{E3})$$

Therefore, Equation E1 can be written as

$$Z_{\text{eq}}(M_{\star}, \text{SFR}) = Z_0 + \frac{y}{1 + \lambda(1 - R)^{-1} + \varepsilon^{-1} (1 - R)^{-1} \left\{ \text{SFR}^{-1} \frac{d\text{SFR}}{dt} - \varepsilon^{-1} \frac{d\varepsilon}{dt} \right\}}. \quad (\text{E4})$$

If the SFR of the system is constant, obviously there is no SFR dependence in metallicity as  $d\text{SFR}/dt = 0$ .