



## THE RED SUPERGIANT CONTENT OF M31\*

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### ABSTRACT

We investigate the red supergiant (RSG) population of M31, obtaining the radial velocities of 255 stars. These data substantiate membership of our photometrically selected sample, demonstrating that Galactic foreground stars and extragalactic RSGs can be distinguished on the basis of  $B - V$ ,  $V - R$  two-color diagrams. In addition, we use these spectra to measure effective temperatures and assign spectral types, deriving physical properties for 192 RSGs. Comparison with the solar metallicity Geneva evolutionary tracks indicates astonishingly good agreement. The most luminous RSGs in M31 are likely evolved from  $25\text{--}30 M_{\odot}$  stars, while the vast majority evolved from stars with initial masses of  $20 M_{\odot}$  or less. There is an interesting bifurcation in the distribution of RSGs with effective temperatures that increases with higher luminosities, with one sequence consisting of early K-type supergiants, and with the other consisting of M-type supergiants that become later (cooler) with increasing luminosities. This separation is only partially reflected in the evolutionary tracks, although that might be due to the mis-match in metallicities between the solar Geneva models and the higher-than-solar metallicity of M31. As the luminosities increase the median spectral type also increases; i.e., the higher mass RSGs spend more time at cooler temperatures than do those of lower luminosities, a result which is new to this study. Finally we discuss what would be needed observationally to successfully build a luminosity function that could be used to constrain the mass-loss rates of RSGs as our Geneva colleagues have suggested.

**Key words:** galaxies: individual (M31) – galaxies: stellar content – Local Group – stars: massive – supergiants

**Supporting material:** machine-readable tables

### 1. INTRODUCTION

Massive stars spend most of their lives as OB stars. The most massive of these ( $>\sim 40 M_{\odot}$ ) then evolve into Wolf–Rayet (WR) stars, possibly after passing through a luminous blue variable (LBV) phase. In contrast, massive stars with masses below  $\sim 30 M_{\odot}$  spend their He-burning lives as red supergiants (RSGs) after passing through a yellow supergiant (YSG) stage during their quick journey across the Hertzsprung–Russell diagram (HRD). At some intermediate masses ( $\sim 30 M_{\odot}$ , say) stars may pass through both a RSG and WR phase, passing through the YSG phase twice. The exact mass ranges corresponding to these various stages, along with the relative lifetimes spent in these regions of the HRD, depend heavily on the initial metallicity of the gas out of which these stars form, as radiation pressure acting on highly ionized metals results in mass loss that strongly influences this evolution. Thus, characterizing the luminous populations of nearby galaxies allows us to perform exacting tests of massive star evolution as a function of metallicity. (For a recent review, see Massey 2013.)

The Andromeda Galaxy (M31) plays a unique role in such studies, as it provides the only nearby extragalactic example where the metallicity is solar and above (Zaritsky et al. 1994; Sanders et al. 2012). Previous work on the massive star population of M31 has established the WR content (Neugent et al. 2012a), identified YSGs (Drout et al. 2009), discovered

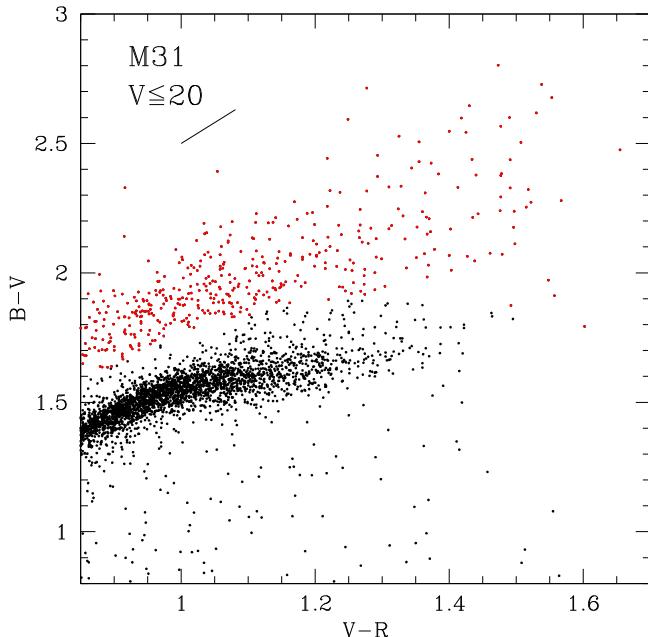
LBV candidates (Massey 2006; Massey et al. 2007a, 2016), and laid the groundwork for the current study by performing a preliminary reconnaissance of its RSG population (Massey 1998; Massey et al. 2009). Work on the unevolved massive star population suggests that only a few percent of the total number O stars and B supergiants have been identified (Massey et al. 2016).

In this paper we set out to complete our identification of the RSG population of M31 down to  $\sim 15 M_{\odot}$ , using a combination of spectroscopy and photometry. Massey et al. (2007b) showed that samples of red stars in the right color and magnitude range to be RSGs were badly contaminated ( $\sim 80\%$ ) by foreground red dwarfs. However, for cool stars ( $T_{\text{eff}} \leq 4300$  K),  $B - V$  becomes primarily an indicator of surface gravity due to line-blanketing in the  $B$  band, while  $V - R$  remains primarily a temperature indicator (Massey 1998). Thus there is a relatively clean separation in a  $B - V$  versus  $V - R$  two-color plot between foreground dwarfs and RSGs. We show an example of such an effort in Figure 1 based upon Massey et al. (2009).

Prior efforts at spectroscopic confirmation have been relatively modest. Massey (1998) “confirmed” about 20 RSGs in M31. In some cases the spectroscopic confirmation is based on clear radial velocity information, but in other cases it is based on softer criteria, such as the strengths of the Ca II triplet lines; these criteria were not always in good agreement. Massey et al. (2009) identified a sample of 437 RSG candidates in M31 from the Local Group Galaxy Survey (LGGS)  $BVR$  photometry of Massey et al. (2006), and obtained radial velocities of 124 of these stars, but derived physical properties (effective temperatures and bolometric luminosities) for only 16 stars in their sample. Furthermore, the photometrically selected RSG and foreground candidates did not always prove to be what was

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**Figure 1.** Two-color diagram of red stars in M31. The points in red are suspected RSGs from Table 1 of Massey et al. (2009), while the points in black represent suspected foreground stars. The photometry is taken from the LGGS (Massey et al. 2006), with  $V \leq 20.0$ . The typical reddening vector for M31 stars is shown by the diagonal line.

expected when observed spectroscopically. We decided it was time for a more complete study.

This investigation is timely. As the evolutionary models improve, knowledge of the RSG content of M31 will provide us with a powerful magnifying glass<sup>4</sup> for examining the predictions of these models, and for better constraining the input. For instance, Maeder et al. (1980) argued that the relative number of RSGs and WRs should be a strong function of the metallicity, with proportionately fewer RSGs found at higher metallicities. Further, the number of RSGs gives another way of estimating the expected number of unevolved O stars, a value that is poorly constrained observationally (Massey et al. 2016).

An even more exciting possibility is for us to use our knowledge of the RSG content of M31 to determine the mass-loss rates for RSGs. As recently shown by Meynet et al. (2015) the time-averaged mass-loss rates of RSGs are very poorly constrained by observations, as much of the action occurs episodically. The consequences of this significantly affect our interpretation of the populations of the upper part of the HRD. For instance, according to the models, enhanced mass loss during the RSG phase leads to the prediction that the *majority* of blue and YSGs are post-RSG objects (Meynet et al. 2015). In addition, enhanced mass-loss rates during the RSG phase may solve the so-called “red supergiant problem.” RSGs have long been thought to be the progenitors of type II-P supernovae; Smartt et al. (2009), however, argued that the observed upper mass limit of the progenitors of type II-P supernovae is  $17\text{--}18 M_{\odot}$  rather than the  $30 M_{\odot}$  or more one would expect from what the models. Ekström et al. (2012) argues that an improved mass-

loss prescription during the RSG phase leads naturally to this result, as the mass-loss rates are then significantly enhanced for the highest mass RSGs, leading to a likely scenario where these stars lose most of their hydrogen-rich envelopes and exploded instead as type II-L or even type Ib supernovae.

The validity of this resolution rests on the assumption that the RSG mass-loss rates have been seriously underestimated. Meynet et al. (2015) and Georgy et al. (2015) proposed a novel way of determining if this is correct. The evolution models predict that the luminosity functions of RSGs will have a strong dependence on the average mass-loss rates for RSGs, becoming steeper (fewer high luminosity RSGs) with higher mass-loss rates. However, this requires an unbiased knowledge of the RSG content of a mixed-age population in which the (global) star-formation rate has remained essentially constant over the relevant evolution time period (20–30 Myr). Model calculations are currently underway for this undertaking. Our study here does not provide an answer, but it provides an vital toe-in-the-door that delineates the observational hurdles associated with constructing the required bias-free luminosity function.

In Section 2 we will explain our sample selection and the spectroscopy we obtained for our study. In Section 3 we will use these data for our analysis, first distinguishing RSGs from foreground stars using the radial velocities (Section 3.1) and comparing these results to our expectations based on our two-color diagrams. We will also measure effective temperatures and spectral types (Section 3.2), and compute other physical properties, such as the bolometric luminosities. We will then compare these to what the Geneva evolutionary tracks predict (Section 3.3). Finally, in Section 4 we will summarize our results and discuss what future work is needed in order to construct a sufficiently deep luminosity function for constraining the RSG mass-loss rates.

## 2. OBSERVATIONS

### 2.1. Sample Selection

Our primary goal was to see how accurately we could use the  $(V - R, B - V)$  two-color selection method of Massey (1998) to distinguish actual RSGs from Galactic foreground stars. In this way, M31 serves as an excellent (high-metallicity) test bench. For some galaxies, such as the Magellanic Clouds, most of the systemic radial velocity is actually due to the reflex motion of the Sun. Thus, although foreground disk dwarfs are easily distinguished from Magellanic Cloud members (Neugent et al. 2010, 2012b), halo red giants would be hard to distinguish from Magellanic Cloud RSGs on the basis of radial velocities alone. (Statistically, however, we can argue that few halo red giants are expected in the appropriate magnitude range; see Section 4 of Neugent et al. 2012b.) M31 has a systemic velocity of  $\sim 300 \text{ km s}^{-1}$  and a rotational velocity of  $\sim 250 \text{ km s}^{-1}$  (Massey et al. 2009 and references therein.) Thus there is an “alligator’s jaws” shaped area in the NE section of M31 where it is difficult to separate foreground dwarfs from M31 members, but over most of the galaxy the separation is very clean. (See Figure 5 of Drout et al. 2009.)

In selecting targets to observe, we used the 437 photometrically selected RSG candidates given in Table 1 of Massey et al. (2009). These are the stars marked as red in Figure 1 and they meet the following criteria: (1)  $V < 20$ , corresponding roughly to  $\log L/L_{\odot} \sim 4.4$  for early K-type stars and  $\log L/L_{\odot} \sim 4.8$  for mid M-type stars. (2)  $V - R \geq 0.85$  (and correspondingly

<sup>4</sup> Kippenhahn & Weigert (1990 p. 192) liken these evolved stages to “a sort of magnifying glass, [which reveals] relentlessly the faults of calculations of earlier phases.” We are indebted to our colleague Andre Maeder for calling this quote to our attention.

$B - V \geq 1.5$ ) to restrict the sample to K-type stars and later, roughly corresponding to  $T_{\text{eff}} < 4300$  K given typical reddening for M31 RSGs.<sup>5</sup> (3)  $B - V > -1.599(V - R)^2 + 4.18(V - R) - 0.83$  to separate the low surface gravity RSGs from the high surface gravity foreground Galactic stars. Some of these stars had previously measured radial velocities (Table 2 of Massey et al. 2009), which could then serve as radial velocity templates. Of the 437 stars, 36 (8.2%) of them were somewhat crowded and given lower priorities in the Hectospec assignments.

This project was “piggy-backed” on our primary program to continue to monitor a sample of WR binaries in M31 (Neugent & Massey 2014). We observed six of these WR configurations with slightly different supergiant and foreground candidate red stars included on the otherwise unused fibers. In addition, we observed one configuration that consisted only of red stars. In all we successfully observed 255 RSG candidates and 98 foreground candidates, many of them multiple times.

## 2.2. Spectroscopy

The observations were all made with Hectospec, a 300-fiber spectrometer on the 6.5 m MMT (Fabricant et al. 2005). The 270 lines  $\text{mm}^{-1}$  grating was used, providing a reciprocal dispersion of  $1.2 \text{ \AA pixel}^{-1}$ , and a spectral resolution of  $4.5\text{--}5.2 \text{ \AA}$  from  $3650\text{--}9200 \text{ \AA}$  in first order. Since no blocking filter is used, there is some contamination from second-order blue in the far red, but given the colors of these stars, this is pretty minimal; the grating is blazed at  $5000 \text{ \AA}$ . The six “WR configurations” were observed for 90 minutes each (UT 2014 September 24, September 26, November 21, November 22, November 26, and November 28); the one “red star” configuration was observed for 60 minutes (UT 2014 October 1). The observations were made in a self-staffed queue; P. M. and collaborator Kathryn Neugent were present for the November observing.

The reductions were previously described by Evans & Massey (2015). For each of the seven configurations, some fibers were assigned to blank sky in order to facilitate sky subtraction. Calibration exposures included HeNeAr and quartz lamp exposures. The data were all run through the SAO pipeline, with the night-sky lines used to adjust the wavelength zero-points relative to the HeNeAr exposures that were made in the afternoon. As part of the reduction procedure, the wavelengths were corrected to the heliocentric rest frame. Observations of the spectrophotometric standard Feige 34 were made midway through the semester, and were used to produce sensitivity curves by Nelson Caldwell, who kindly made these available to us.

## 3. ANALYSIS

### 3.1. Membership: RSGs versus Foreground Stars

We measured radial velocities from each of the spectra using XCSAO, an IRAF<sup>6</sup> cross-correlation tool. As described in Evans

<sup>5</sup> Our interpretation of the  $V - R$  cutoff requirements differs slightly from that stated by Massey et al. (2009), who state that  $V - R \geq 0.85$  corresponds to an intrinsic  $(V - R)_0$  of 0.81 ( $T_{\text{eff}} \leq 4000$  K). Yet, we expect  $E(V - R) \sim 0.6E(B - V)$  (Schlegel et al. 1998). The M31 OB stars in the LGGS have a median reddening of  $E(B - V) = 0.13$ , so this would correspond to  $E(V - R)_0 = 0.77$ , not 0.81. But, the actual M31 RSG sample has higher reddening, with  $E(B - V) \sim 0.3$  for reasons probably associated with circumstellar dust (Massey et al. 2005). Thus,  $E(V - R) \sim 0.18$  and  $(V - R)_0 \sim 0.67$ , corresponding more to an  $T_{\text{eff}} \leq 4300$  K. This allows early-type K stars to be included in the sample.

<sup>6</sup> IRAF is distributed by the National Optical Astronomy Observatory, which is operated by the Association of Universities for Research in Astronomy (AURA) under a cooperative agreement with the National Science Foundation.

& Massey (2015), we used 21 Hectospec spectra of six M31 RSGs for which Massey et al. (2009) had already determined radial velocities. (Those velocities, in turn, were tied to three legitimate late-type radial velocity standards.) The cross-correlation was restricted to the  $8350\text{--}8750 \text{ \AA}$  region around the Ca II  $\lambda\lambda 8498, 8542, 8662$  triplet, lines that are very strong in RSGs. This process also allows us to avoid the wide molecular features, atmospheric bands, and so on. For each individual program spectrum, a single velocity was produced by averaging the results from the 21 velocity templates, weighting each appropriately by the internal error from the cross-correlation (i.e., weights were the squares of the reciprocal errors). For the stars with multiple observations, a weighted average was then determined.<sup>7</sup> We list the radial velocities in Table 1.

Massey et al. (2009) demonstrated that the radial velocities of M31’s H II regions and RSGs agreed very well, and that the expected radial velocities of these Population I objects could be approximated by a linear relationship with  $(X/R)$ ,

$$V_r = -295 + 241.5(X/R),$$

where  $X$  is the distance along the semimajor axis and  $R$  is the galactocentric distance within the plane of M31. Such a linear approximation agrees well with the more complex two-dimension velocity field determination of Sofue & Kato (1981) and other studies (e.g., Hurley-Keller et al. 2004), and is equivalent to saying that the rotation curve is flat. In contrast, we expect the foreground red stars to cluster around a velocity of  $0 \text{ km s}^{-1}$ , with some scatter indicative of the radial velocity dispersion of nearby red dwarfs in this particular direction.

In Figure 2 we show a plot of the radial velocity with  $(X/R)$  for all of our data. We see that the vast majority of the candidate RSGs (red points) follow the expected relationship between  $V_r$  and  $(X/R)$ , while the vast majority of the candidate foreground stars (black points) cluster around  $0 \text{ km s}^{-1}$  as expected. The foreground candidates were observed only as part of the single “red star” configuration, and hence are distributed over the limited range of  $(X/R) \sim 0.25\text{--}1.0$ . We have used the larger sample size here to improve on the radial velocity relation, deriving

$$V_r = -311.8 + 242.0(X/R).$$

Over the range  $(X/R) = -1$  to  $+1$ , the expected  $V_r$  from this relationship differs from that of the Massey et al. (2009) determination by  $-16.3$  to  $-17.3 \text{ km s}^{-1}$ . This may be compared to the overall scatter around the relationship of  $25 \text{ km s}^{-1}$ . Recall that the radial velocity “standards” for the new measurements came from adopting the radial velocities determined by Massey et al. (2009). We checked our new measurements against the old to make sure this  $\sim -17 \text{ km s}^{-1}$  was due to better coverage in  $(X/R)$  and not some reduction issue. Indeed, there is only a small systematic offset between the new and old measurements; the mean difference (in the sense of new minus old) is  $-7.4 \text{ km s}^{-1}$  with a scatter of  $12.3 \text{ km s}^{-1}$  and median difference  $-5.9 \text{ km s}^{-1}$  using 73 stars in

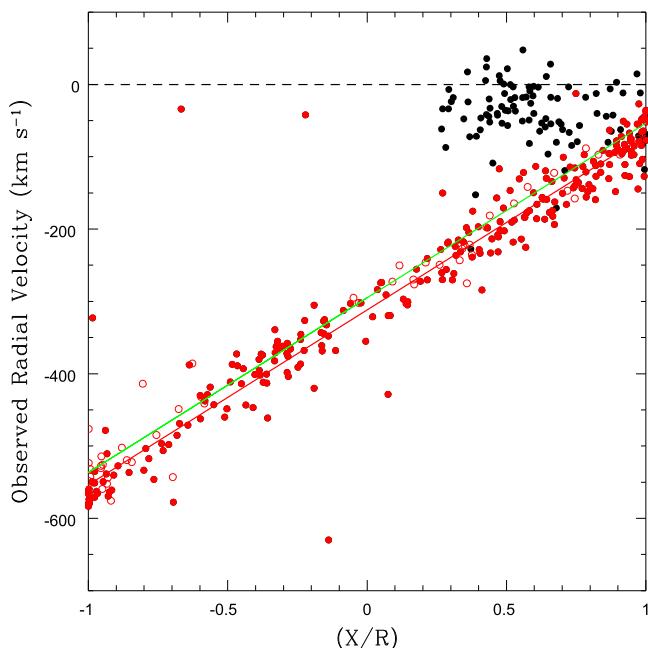
<sup>7</sup> Prior to 2014, the SAO pipeline reductions did not include correcting the wavelength scale to heliocentric; this change caused a certain amount of confusion and consternation during our initial attempts to understand our results. We are indebted to Nelson Caldwell for help in tracking down this issue.

**Table 1**  
Radial Velocities of RSG and Foreground Candidates

Star	$X/R^a$	$V_{M31}^b$	$V_{\text{obs}}^b$	$V_{\text{eff}}^b$	$N_{\text{obs}}$	TDR <sup>c</sup>	Old $V_{\text{obs}}^{\text{b,d}}$	Phot. Type <sup>e</sup>
J003950.86+405332.0	-0.586	-436.5	-433.0	0.5	6	14.4	...	RSG
J003950.98+405422.5	-0.563	-431.0	-418.4	0.7	3	14.5	...	RSG
J003957.00+410114.6	-0.409	-393.8	-446.9	0.6	6	12.7	-442.4	RSG
J004015.18+405947.7	-0.491	-413.5	-411.5	0.5	6	12.9	-406.8	RSG
J004015.86+405514.1	-0.638	-449.0	-387.9	0.9	4	8.7	...	RSG
J004019.15+404150.8	-0.999	-536.2	-564.6	1.2	1	13.4	-551.9	RSG
J004020.06+410651.3	-0.326	-373.8	-362.6	0.5	5	15.8	...	RSG
J004023.84+410458.6	-0.375	-385.5	-374.1	1.2	2	9.0	...	RSG
J004025.36+404623.1	-0.967	-528.6	-565.2	0.6	6	10.6	...	RSG

**Notes.**<sup>a</sup>  $X$  is the distance along the semimajor axis and  $R$  is the galactocentric radius within the plane of M31.<sup>b</sup> Radial velocities in km s<sup>-1</sup>.<sup>c</sup> Tonry & Davis (1979)  $r$ -parameter.<sup>d</sup> From Massey et al. (2009).<sup>e</sup> Photometric type based upon  $B - V$  versus  $V - R$ ; fgd—foreground.

(This table is available in its entirety in machine-readable form.)



**Figure 2.** Radial velocities of foreground and RSG candidates. The radial velocities of our foreground (black) and RSG (red) candidates are plotted against  $(X/R)$ , where  $X$  is the distance along the semimajor axis, and  $R$  is the galactocentric separation within the plane of M31. Filled red circles are from the present paper; open red circles are from Massey et al. (2009). The black dashed line indicates  $0 \text{ km s}^{-1}$  and we expect that foreground galactic stars will cluster near this value. The green line denotes the radial velocity vs.  $(X/R)$  relation for M31 from Massey et al. (2009), while the red line denotes the revised version given here.

common.<sup>8</sup> If we include the 50 additional RSGs with radial velocities from Massey et al. (2009) for which we do not have new radial velocities, we obtain a very similar relation,

$$V_r = -310.0 + 239.7(X/R).$$

<sup>8</sup> This excludes one outlier with a huge difference, J004217.99+410912.7, whose velocity measurement here is  $118 \text{ km s}^{-1}$  more positive than that in Massey et al. (2009). Neither measurement agreed well with the expected radial velocity; possibly the star is a radial velocity variable (binary).

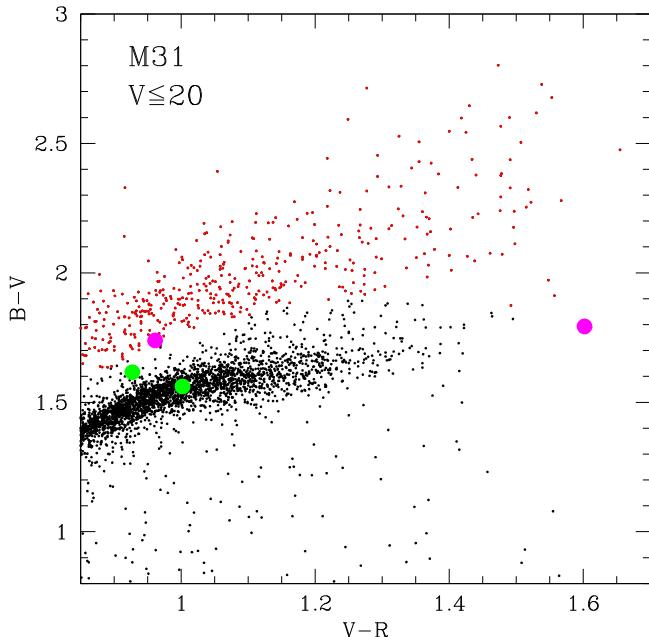
Although our photometric classification was obviously extremely successful, we can see that there were a few RSGs misclassified photometrically as foreground stars, a few foreground stars misclassified as RSGs, and a few RSGs with interestingly discrepant radial velocities. Let us consider each of these cases in turn.

Drouet et al. (2009) argued that confusion with foreground stars sets in at radial velocities  $\geq -150 \text{ km s}^{-1}$ . There are two foreground candidates (black points) more negative than that in Figure 2, each near the RSG velocity relation. In other words, two stars whose velocities indicate they are indeed RSGs despite having been classified photometrically as foreground stars. These are J004458.49+421219.2 and J004406.92+412307.2. We denote their position in the two-color diagram in Figure 3 with large green points. We see that one of these stars (J004458.49+421219.2) has photometry right on the border between what we defined as a RSG candidate and what we called a foreground candidate; the other, J004406.92+412307.2, really “should” be a foreground star according to the photometry.

There are three stars photometrically classified as RSGs that have velocities consistent with their actually being foreground stars: J004105.97+403407.9, J004303.26+404710.9, and J004431.71+415629.1. We mark two of these stars with large magenta symbols in Figure 3; the third (J004105.97+403407.9) has such unrealistic photometry ( $V - R \sim 4.7$ ) that it would fall well to the right on the plot. That star is extremely crowded according to the LGGS. The other two stars have photometry that is right on the borderline between the separation of RSGs and foreground stars. Of these, the one with the redder  $V - R$  has very poor spectra, as well as a surprisingly large  $V - R$  color.

Thus, of all 354 stars with new data, only one star is surprisingly inconsistent with its photometric classification versus its radial velocity. We conclude that the photometric classification using the  $V - R$ ,  $B - V$  two-color diagram appears to be a very robust way of separating foreground stars from RSGs without needing radial velocities, at least at high metallicities.

The final type of discrepancy is when a RSG candidate has a surprising velocity with respect to its position in M31, but its



**Figure 3.** Location of discrepantly classified stars (from Figure 2) in two-color diagram. The same as Figure 1 but with large symbols denoting the location of the four stars whose radial velocities disagree with the photometric classification. Green symbols are stars photometrically classified as foreground objects but whose radial velocities are consistent with M31 membership, while magenta symbols are stars photometrically classified as RSGs, but whose radial velocities are consistent with membership in the Milky Way. A fifth star, whose photometry is confused by crowding, is located off the right side of this plot.

velocity is not consistent with it being a foreground star either. Evans & Massey (2015) discuss J004330.06+405258.4, the star with a radial velocity of  $-630 \text{ km s}^{-1}$  at  $(X/Y) = -0.138$ . They conclude that this is an bona fide runaway RSG, the first discovered on the basis of its radial velocity, and the first known extragalactic massive star runaway. A significant percentage (10%–50%) of unevolved massive stars are OB runaways (Gies & Bolton 1986, and references therein), with discrepant radial velocities ( $>30 \text{ km s}^{-1}$ ) compared to other OB stars in their neighborhood. Runaways probably occur via dynamical evolution (Gies & Bolton 1986; Fujii & Portegies Zwart 2011). Few evolved massive runaways are known, doubtless because of the difficulties in recognizing such objects once they are older and have moved further from their birthplace. J004330.06+405258.4 has a radial velocity that is  $300 \text{ km s}^{-1}$  more negative than that expected from M31's rotation curve, and Evans & Massey (2015) note that the object is located some  $\sim 20'$  (4.6 kpc) from the plane of the disk, consistent with it having a transverse velocity similar to its radial velocity motion.

We find three other potential runaways in Figure 2: J004217.99+410912.7 has a radial velocity of  $-323 \text{ km s}^{-1}$  rather than the  $-533 \text{ km s}^{-1}$  expected for  $(X/R) = -0.985$ . We have five observations of this star, all with similar velocities. However, an older measurement by Massey et al. (2009) disagrees with these, with a value of  $-440 \text{ km s}^{-1}$ . The difference in radial velocity between the Fall 2014 observations reported here and the Fall 2005 observations of Massey et al. (2009) might suggest the star is a long-period binary, but the large velocity difference would be more indicative of a short-period binary, which we can essentially rule out from our five new measurements. These results are puzzling.

J004112.27+403835.8 and J004228.99+412029.7 can be seen in Figure 2 at  $(-0.695, -577 \text{ km s}^{-1})$  and  $(0.075, -428 \text{ km s}^{-1})$ . These stars also might be runaways as their radial velocities are expected to be  $-462 \text{ km s}^{-1}$  and  $-277 \text{ km s}^{-1}$ , respectively. Both stars have multiple observations, with good agreement in their measurements, as evidenced by the low standard errors of the means given in Table 1, i.e., 1.0 and  $1.3 \text{ km s}^{-1}$ . However, the spectrum of J004228.99+412029.7 is that of a very early K-type, or even late G-type; this is consistent with the low value for the Tonry & Davis (1979)  $r$ -parameter we obtained, indicating a relatively poor match with the M-type radial velocity templates we used in measuring the velocities.

### 3.2. Effective Temperatures, Spectral Types, and Physical Parameters

Spectral types for the M31 RSGs were determined by comparing their spectra to those of Galactic RSGs observed by Levesque et al. (2005). Those Galactic RSGs had spectral types that were generally well established in the literature, although in a few cases they were reclassified by Levesque et al. (2005). The agreement between these were usually exact, although occasionally there would be a difference of one spectral subtype, i.e., M1 I versus M2 I. The primary criteria were those described by Levesque et al. (2005), i.e., the strengths of the TiO bands for M- and late K-types, and the strengths of the G band and Ca I  $\lambda 4226$ . We list these spectral types in Table 2. In the few cases where no spectral type could be assigned, the stars are likely not RSGs at all, but are somewhat earlier members of M31.

Effective temperatures were determined following the procedures described by Levesque et al. (2005) using the  $2 \times$  solar metallicity MARCS atmosphere models used by Massey et al. (2009). For the vast majority of our M31 RSGs we had multiple observations; each of these spectra were fit independently; what are shown are the median values. The uncertainty in our fitting is approximate 50 K. These temperatures are given in Table 2. Note that in a few cases effective temperatures could not be measured reliably.

There are eight stars in common between our study here and that of Massey et al. (2009); we list a comparison of the spectral types and effective temperatures in Table 3. In preparing this we were chagrined to discover a significant error in Massey et al. (2009): the effective temperatures they listed were based upon the solar metallicity MARCS models and not the  $2 \times$  solar metallicity MARCS model as stated in the text. Experimentation showed that this introduced a systematic difference of 75 K, i.e., that fitting the spectra used by Massey et al. (2009) with the  $2 \times$  solar model rather than the  $1 \times$  solar model require temperatures that are roughly 75 K higher. We have therefore adjusted the Massey et al. (2009) effective temperatures by that amount in making this comparison. We find the agreement in the effective temperatures determined from our new spectra to be quite consistent. The only significant discrepancy in spectral type is for J003957.00+410114.6. We have six observations of that star; all yield a spectral type in the range of M3–M4 I, consistent with our effective temperature. We are forced to conclude that the Massey et al. (2009) spectral type is a mistake rather than a sign of variability, given that the effective temperature given for the star by Massey et al. (2009) is much cooler than what they found for other M0 I stars, and is more like that of a M3 I type.

**Table 2**  
Physical Properties

Star	Type	$T_{\text{eff}}$	$K$ -band Photom.		$M_K$	$\log L/L_{\odot}$	$R/R_{\odot}$
			$K_s$	Source <sup>a</sup>			
J003950.86+405332.0	M1 I	3850	14.45	M	-10.03	4.86	600
J003950.98+405422.5	M4 I	3650	14.20	M	-10.28	4.89	700
J003957.00+410114.6	M4 I	3650	15.08	F	-9.40	4.54	470
J004015.18+405947.7	M3 I	3700	14.26	M	-10.22	4.89	670
J004015.86+405514.1	K2 I	3950	15.62	M	-8.86	4.42	340
J004019.15+404150.8	M2 I	3750	14.61	M	-9.87	4.76	570
J004020.06+410651.3	M0 I	3900	14.60	M	-9.88	4.81	560
J004023.84+410458.6	K5 I	3975	15.69:	M	-8.79	4.40	330
J004025.36+404623.1	M0 I	3900	15.29:	M	-9.19	4.53	400
J004025.75+404254.8	K5 I	3925	...	X	...	...	

**Note.**<sup>a</sup> M—2MASS (Cutri et al. 2003), F—FLAMINGOS (Massey et al. 2009), X—no data.

(This table is available in its entirety in machine-readable form.)

**Table 3**  
Comparison with Massey et al. (2009)

Star	Spectral Type		Effective Temperature	
	New	Old	New	Old <sup>a</sup>
J003957.00+410114.6	M4 I	M0 I	3650	3775
J004035.08+404522.3	M2 I	M2.5 I	3750	3775
J004047.82+410936.4	M3 I	M3 I	3650	3725
J004124.80+411634.7	M2 I	M3+? I	3725	3700
J004255.95+404857.5	M2 I	M2 I	3800	3750
J004428.71+420601.6	M0 I	M0 I	3825	3900
J004454.38+412441.6	M0 I	M2 I	3850	3800
J004514.95+414625.6	M1 I	M2 I	3800	3750

**Note.**<sup>a</sup> Adjusted by +75 K; see text.

In the past, our standard procedure (e.g., Levesque et al. 2005, 2006; Massey et al. 2009; Levesque & Massey 2012) has been to use the model fitting to determine  $E(B - V)$ . However, our recent experiences with fiber spectrophotometry has been disappointing. Hectospec uses an atmospheric dispersion compensator, and a careful study by Fabricant et al. (2008) demonstrates that the flux calibration of Hectospec data is good to a few percent on extended sources. However, we have found that flux calibrating point sources in crowded fields is considerably less successful. In many cases the reddening required to fit the fluxed spectrophotometry are clearly non-physical, i.e., requiring zero or negative  $E(B - V)$ . We have encountered similar problems in modeling Magellanic Clouds RSGs using 2 Degree Field fiber data from the Australian Astronomical Observatory in a separate project. We have thus decided to adopt the median  $E(B - V) = 0.3$  ( $A_V = 1.0$ ) found by Massey et al. (2009) for their sample of M31 RSGs. This is somewhat larger than the average reddening of OB stars (Massey et al. 2007b), which is consistent with what we find from a comparison to the reddening of OBs and RSGs in the Milky Way (Levesque et al. 2005) and Magellanic Clouds (Levesque et al. 2006), and which is attributable to circumstellar reddening by dust (Massey et al. 2005).

To minimize the effect that  $A_V$  is poorly determined individually for our stars, we have chosen to rely on near-IR

(NIR)  $K$ -band photometry, as  $A_K$  is only about 10% of  $A_V$ , and the bolometric correction is small and fairly insensitive to the temperature. This also has the advantage of avoiding the typical  $\sim 0.9$  mag variability seen in  $V$  (Levesque et al. 2007); no such variability is seen at  $K$ , a point also emphasized by Massey et al. (2009). Of the 255 stars in our sample, 37 have targeted  $K$ -band photometry using the NIR photometer FLAMINGOS (Massey et al. 2009); for the rest, we adopt 2MASS (Cutri et al. 2003) values where available. We perform the same conversion to bolometric luminosity in the same manner as Massey et al. (2009):

$$K = K_s + 0.04$$

$$K_0 = K - 0.12A_V = K - 0.12$$

$$M_K = K_0 - 24.40$$

$$M_{\text{bol}} = M_K + BC_K,$$

where  $K$  is the “standard” (such as it is) photometric band (see, e.g., Carpenter 2001),  $K_s$  is the observed 2MASS or FLAMINGOS photometry,  $K_0$  is the de-reddened  $K$ -band magnitude,  $M_K$  is the absolute  $K$ -band magnitude where we have assumed a true distance modulus of 24.40 (0.76 Mpc, van den Bergh 2000),  $M_{\text{bol}}$  is the bolometric magnitude, and  $BC_K$  is the bolometric correction in the  $K$ -band, a small but positive number (e.g., Bessell et al. 1998; Levesque et al. 2005). We determine  $BC_K$  from the effective temperature  $T_{\text{eff}}$  following Massey et al. (2009) as follows:

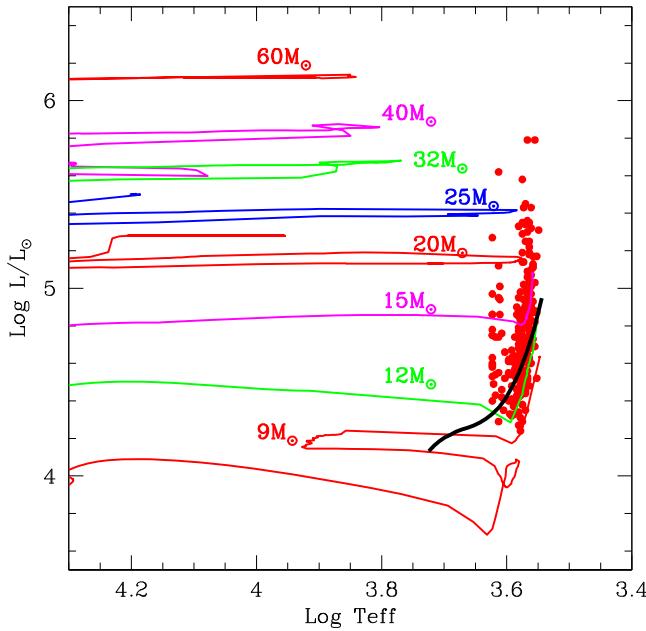
$$BC_K = 7.149 - 1.5924 \left( \frac{T_{\text{eff}}}{1000 \text{ K}} \right) + 0.10956 \left( \frac{T_{\text{eff}}}{1000 \text{ K}} \right)^2,$$

where the relationship is derived from the MARCS models. Finally, of course,

$$\log L/L_{\odot} = (M_{\text{bol}} - 4.75)/-2.5.$$

### 3.3. Comparison with Evolutionary Tracks

Having derived physical properties for our sample of RSGs, we compare their location in the HRD to that predicted by the evolutionary tracks in Figure 4. In making this comparison, we encounter a difficulty: so far, only solar (Ekström et al. 2012) and sub-solar (Georgy et al. 2013) versions of the new Geneva



**Figure 4.** Location of the RSGs in the HRD. We have plotted the location of M31’s RSGs in the HRD using the values in Table 2. The evolutionary tracks are from Ekström et al. (2012), computed for solar metallicity and an initial rotation of 40% of the critical breakup speed. The initial masses are shown for each track. The black curve corresponds to  $V = 20$ , our estimated complete- ness limit.

tracks are available. Sanders et al. (2012) recently conducted a comprehensive study of the chemical abundances of M31’s H II regions, finding that  $\log(\text{O/H})+12 = 9.0\text{--}9.1$  ( $2 \times$  solar) in the center of M31 with a shallow galactocentric gradient ( $-0.01$  to  $-0.02$  dex kpc $^{-1}$ ), in accord with the older study of Zaritsky et al. (1994). (A value of  $\log(\text{O/H}) + 12 = 8.7$  is considered typical of the solar neighborhood, and hence our description of  $2 \times$  solar.) However, one of the most intriguing results to come out of the Sanders et al. (2012) study is the large scatter in the oxygen abundance measures, which these authors argue is *intrinsic* and not observational. As their Figure 8 shows, at a galactocentric distance of 10–12 kpc, the values for  $\log(\text{O/H})+12$  vary from 8.5 to 9.3 dex. Thus, the solar metallicity evolutionary tracks are not inappropriate either. However, the changes in the physical parameters we would have derived using solar metallicity models are extremely modest. We would have to decrease our effective temperatures by 75 K, the approximate systematic difference between the solar and  $2 \times$  solar MARCS atmospheric models as discussed earlier. This translates to a very modest  $\sim 0.01$  dex decrease in the effective temperature and a 0.02 dex decrease in the bolometric luminosity, i.e., the change is comparable to the point sizes in the figure.

The agreement between the evolutionary tracks and the locations of stars in the HRD is nothing short of remarkable. There are only four stars whose luminosities appear to be higher than what the tracks allow. The two highest luminosity stars in the figure are J004520.67+414717.3 (M1 I) and J004539.99+415404.1 (M3 I) are both found at  $X/R > 0.9$  where there is considerable overlap in the radial velocities of RSGs and foreground stars; we thus are relying primarily on their photometry to classify these as supergiant members. The photometry of the first of these clearly places it in the RSG category (J004520.67+414717.3 has  $B - V = 2.68$ ,

$V - R = 1.55$ ), while the photometry of the second is more marginal (J004539.99+415404.1,  $B - V = 1.70$ ,  $V - R = 0.94$ ). The next two most luminous stars are not necessarily discrepant with the evolutionary tracks, as somewhere between 25 and 32  $M_{\odot}$  may extend over to the RSG phase. These stars have  $\log L/L_{\odot} \sim 5.6$  and are J004428.12+415502.9 (K2 I,  $X/R = 0.75$ ) and J004428.48+415130.9 (M1 I,  $X/R = 0.82$ ), located where there is more support from the radial velocities for membership. However, the photometry of J004428.12+415502.9 has an unusually large  $B - V$  value (2.05) for its  $V - R$  value (0.95). Finally, there are three stars all with  $\log L/L_{\odot}$  of 5.45–5.47, J004125.23+411208.9 (M0 I,  $X/R = -0.29$ ), J004312.43+413747.1 (M2 I,  $X/R = 0.45$ ), and J004514.91+413735.0 (M1 I,  $X/R = 0.64$ ), where the radial velocities leave no question as to membership; these stars, however, are consistent with the  $25 M_{\odot}$  track. We conclude that only J004520.67+414717.3 seems to be discrepant with what the evolutionary tracks predict; this high luminosity star may warrant further investigation.

There is an interesting bifurcation in the location of the RSGs in the HRD, with two branches separated by increasingly large differences in effective temperatures at higher luminosities. Is this real, or an artifact of our analysis? The warmer stars are those classified as early K-type, while the cooler stars are classified as M-type; the larger gap at higher luminosities is a reflection that the median spectral type for the M-type stars increases with luminosity. For instance, for the stars with  $\log L/L_{\odot}$  less than 5.0, the median spectral type is M0 I; for stars with  $\log L/L_{\odot} \geq 5.0$ , the median spectral type is M2 I. (Correspondingly the median effective temperatures are 3850 K and 3750 K, respectively.) This bifurcation is partially reflected in the evolutionary tracks; we see for the  $25 M_{\odot}$  track a short loop that results in increased time spent in region occupied by the early K-type supergiants. To quantify this further, in Table 4 we compute the amount of time the evolutionary tracks predict a star will spend in the RSG regime ( $<4300$  K) as a function of effective temperature, in the effective temperature range 4100–4350 K and 3600–4100 K. We see that the gap (which occurs around 4100–4150 K) actually occurs in the  $25 M_{\odot}$  track. Although the gap is not present in the 15 or  $20 M_{\odot}$  track we note that the percentage of “warm” versus “cool” RSGs does increase with increasing luminosity, in much the same way as is reflected by the quantity of stars seen in the HRD. A more exact comparison will be made when the higher metallicity tracks become available.

The numbers in Table 4 do reveal that the  $25 M_{\odot}$  track may not extend quite far enough to cooler temperatures, although this may well be an artifact of the metallicity of the solar track being too low for the M31 RSGs; we expect the Hayashi limit<sup>9</sup> to shift to cooler temperatures with increasing metallicities (see the discussion in Levesque et al. 2006).

#### 4. SUMMARY AND DISCUSSION

We have shown that the photometric separation of RSGs and red foreground stars using a  $B - V$  versus  $V - R$  diagram works extremely well, at least at the  $1.5 \times$  solar metallicity of M31. The exceptions were stars whose photometry was

<sup>9</sup> The Hayashi limit is the coolest temperature at which a star would remain hydrostatically stable (Hayashi & Hoshi 1961).

**Table 4**  
Lifetimes (years) for RSGs from the Ekström et al. (2012) Evolutionary Tracks

Initial Mass ( $M_{\odot}$ )	Effective Temperatures (K)						“Warm”/“Cool” <sup>a</sup>
	3700–3800	3800–3900	3900–4000	4000–4100	4100–4200	4200–4300	
25	0	63,000	30,00	800	3000	12,000	15%
20	151,000	149,000	20,000	6000	4300	5400	3%
15	380,000	8000	3000	2000	2000	2000	0.3!%

**Note.**

<sup>a</sup> “Warm” is 4100–4300 K while “cool” is  $<4100$  K.

suspect, or marginally on the borderline between that expected for the two sequences. There was only one exception out of 354 stars.

The agreement between the evolutionary tracks and the locations of RSGs in the HRD is excellent; there is one star, J004520.67+414717.3, whose photometry places it clearly in the RSG category and yet its high luminosity ( $\log L/L_{\odot} \sim 5.8$ ) appears to be inconsistent with what the evolutionary tracks predict; it will be interesting to see if this star is still discrepant when higher metallicity tracks become available. The bifurcation in the effective temperatures that increases with increasing luminosities is only partially reflected in the evolutionary tracks. This is consistent with the small extra loop in the  $25 M_{\odot}$  track but is not indicated by the other tracks. At higher luminosities the median spectral type becomes slightly later than at lower luminosities; i.e., higher mass RSGs spend more time at cooler temperatures than do stars of lower mass.

#### 4.1. Completeness of the Current Sample

Using the same LGGS photometry that we employ here, Massey et al. (2009) identified 437 stars as likely RSGs based on the two-color diagrams. Of these, we have new spectra and spectral types for 255 (about 60%) of these stars. The Massey et al. (2009) study determined radial velocities for 124 of the 437 stars in the original sample. We have new observations of 74 of those 124 stars, and have included the 50 additional stars with radial velocities from Massey et al. (2009) in Figure 2. We successfully compute physical properties for 192 stars from these 255 stars; the others are either lacking 2MASS  $K$ -band photometry or we were unable to fit their effective temperatures. Massey et al. (2009) only measured physical properties for 16 stars (their radial velocity spectra were at high dispersion and did not provide the necessary amount of wavelength coverage); we have new observations for right of those stars here, and have compared the derived properties in Table 3. We have chosen to ignore the other eight stars, as Massey et al. (2009) inadvertently used solar (rather than  $2\times$  solar) models in deriving their physical properties. Thus Figure 4 and Table 2 reflect the physical properties of about 44% of the original sample.

#### 4.2. Extension to Fainter Limits

As discussed in the Introduction, an exciting possibility is to use the luminosity function of RSGs in M31 to provide a constraint on the mass-loss rates of these stars. In his preliminary work, C. Georgy (2015, private communication) has shown that the slope of the luminosity function is fairly sensitive to the assumed mass-loss rates. However, the slopes of the luminosity functions are fairly parallel for  $\log L/L_{\odot} > 4.5$ ; for this to be useful requires extending our

knowledge of the RSG populations down to  $\log L/L_{\odot} \sim 4.2$  or lower.

We include in Figure 4 the current completeness limit set by  $V \leq 20.0$  as a solid black line.<sup>10</sup> Including the coolest stars, we would consider the current sample complete to  $\log L/L_{\odot}$  of 4.8. Thus, we would need to extend this work about 0.6 dex fainter, or about 1.5 mag, to  $V \sim 21.5$ . The photometry in the LGGS is good enough to distinguish foreground and RSGs at that level: the expected  $1\sigma$  error in  $B - V$  would be about 0.05 (c.f. Table 6 in Massey et al. 2006) which is still acceptable (see Figure 1). What is lacking, however, is the necessary NIR photometry. The 2MASS point-source catalog peters out around  $K_s \sim 15.0$  in M31; optimally we would need to extend this to  $K_s \sim 16.5$ . It may not be practical to obtain optical spectroscopy at this level; Massey et al. (2009) notes that extending the study to just  $V = 21.0$  would increase the number of RSG candidates to 1750; we calculate here that extension to  $V = 21.5$  would then include  $\sim 3200$  stars.

Photometry alone would allow us to fix the effective temperatures well enough to determine the bolometric luminosities. According to the MARCS models,  $\Delta T_{\text{eff}}/\Delta(J - K) = -1777 \text{ K mag}^{-1}$  and  $\Delta BC_K/\Delta(J - K) = 1.33$ , both extremely linear (rms of 10 K and 0.005 mag, respectively) over the RSG effective temperature range. Thus a signal-to-noise ratio of 30 at  $J$  and  $K_S$  would allow us to determine a  $\log L/L_{\odot}$  of 0.02 dex (about the size of the points in Figure 4), and provide a temperature precision of 70 K, just a little worse than the 50 K precision we claim for the spectral fitting. We have proposed to do exactly this in the next observing season.

#### 4.3. Concluding Remarks

Meynet et al. (2015) has emphasized the importance of mass loss during the RSG phase regarding the further evolution of these stars, and has raised the alarming possibility that the majority of blue and yellow supergiants we observe are post-RSG objects. Modern estimates of the mass-loss rates  $\dot{M}$  are of the order  $10^{-4} M_{\odot} \text{ yr}^{-1}$  (van Loon et al. 2005), but the total amount of mass lost during the RSG phase as a function of luminosity is poorly constrained observationally for several reasons. First, it requires measuring mid-IR excesses for RSGs with known distances; this sample contains only about  $\sim 20$  RSGs (see, e.g., Table 3 in van Loon et al. 2005). Second, even so these measurements only tell us the dust production rate; we then have to apply an uncertain dust-to-gas ratio (300–500?). Third, and most importantly, knowing the mass-loss rates for a scant number of stars does not tell us much about what the time-averaged values actually are, as most of the mass lost

<sup>10</sup> There are stars below this line owing to the fact that we used  $K$ -band photometry to construct the HRD, and that the  $V$ -band brightness of RSGs is variable at the 0.9 mag level or beyond (Levesque et al. 2007).

during the RSG phase happens during relatively brief outbursts. The star VY CMa may be the most spectacular example, as its circumstellar material suggests that its mass-loss rate was a factor of  $\sim 20$  higher in the past than it is at present (Smith et al. 2001; Decin et al. 2006).

Extension of our work here to fainter limits now has the potential of allowing us to measure the time-average mass-loss rates using the luminosity functions of these objects. We have established that our photometric technique is sufficient to distinguish RSGs from foreground stars, and combining this technique with NIR photometry has the potential for addressing this in a novel way, as outlined by Meynet et al. (2015) and Georgy et al. (2015). A more complete knowledge of the RSG population of M31 should allow us to answer this intriguing question.

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*Facility:* MMT (Hectospec).

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