

# Numerical simulations and infrared spectro-interferometry reveal the wind collision region in $\gamma^2$ Velorum

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## ABSTRACT

Colliding stellar winds in massive binary systems have been studied through their radio, optical lines and strong X-ray emission for decades. More recently, near-infrared spectro-interferometric observations have become available in a few systems, but isolating the contribution from the individual stars and the wind collision region still remains a challenge. In this paper, we study the colliding wind binary  $\gamma^2$  Velorum and aim at identifying the wind collision zone from infrared interferometric data, which provide unique spatial information to determine the wind properties. Our analysis is based on multi-epoch Very Large Telescope Interferometer/Astronomical Multi-BEam Recombiner (VLTI/AMBER) data that allows us to separate the spectral components of both stars. First, we determine the astrometric solution of the binary and confirm previous distance measurements. We then analyse the spectra of the individual stars, showing that the O star spectrum is peculiar within its class. Then, we perform three-dimensional hydrodynamic simulations of the system from which we extract model images, visibility curves and closure phases that can be directly compared with the observed data. The hydrodynamic simulations reveal the 3D spiral structure of the wind collision region, which results in phase-dependent emission maps. Our model visibility curves and closure phases provide a good match when the wind collision region accounts for 3–10 per cent  $\gamma^2$  Vel's total flux in the near-infrared. The dialogue between hydrodynamic simulations, radiative transfer models and observations allows us to fully exploit the observations. Similar efforts will be crucial to study circumstellar environments with the new generation of VLTI instruments like GRAVITY and MATISSE.

**Key words:** methods: numerical – techniques: interferometric – binaries: spectroscopic – stars: individual:  $\gamma^2$  Velorum – stars: winds, outflows – stars: Wolf–Rayet.

## 1 INTRODUCTION

$\gamma^2$  Velorum<sup>1</sup> ( $\gamma^2$  Vel hereafter) is the closest Wolf–Rayet (WR) star, located at 336 pc (see for instance North et al. 2007). It is therefore a unique laboratory to scrutinize the physics of WR stars. They display strong, broad emission lines due to their powerful winds

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‡ O. Chesneau started the collaboration for this article. He unfortunately passed away before publishing it.

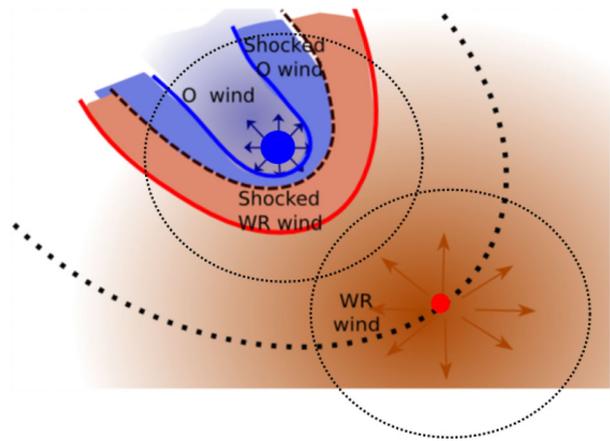
<sup>1</sup> Other names denominations include WR 11, HD 68273.

(see Crowther 2007, for a review). The resulting mass-loss rate is crucial to the final evolution of these massive stars. In binaries with massive stars, like  $\gamma^2$  Vel, they are thought to be the progenitor systems of the compact object mergers detected with gravitational wave observatories (Abbott et al. 2016). Due to their very short lifetime, WR stars trace recent massive star formation, which is the main source of stellar feedback and chemical enrichment in galaxies.

$\gamma^2$  Vel is composed of a WC 8 component in a close binary system with an O star companion in a 78.5 d orbit. It has been extensively studied by means of photometry, spectroscopy, spectropolarimetry and spectro-interferometry, making it likely the best known WR + O system in our Galaxy. Masses, spectral types and flux ratios of the components, as well as the distance of the system have been subject of numerous studies (e.g. Schaerer, Schmutz & Grenon 1997; Schmutz et al. 1997; Van der Hucht et al. 1997; Millour et al. 2007; North et al. 2007). Detailed modelling of the optical and infrared spectra, based on radiative transfer models in expanding atmospheres determines the stellar and wind parameters for both stars (De Marco & Schmutz 1999; De Marco et al. 2000). De Marco & Schmutz (1999) and van der Hucht (2001) establish the O star as an O7.5 III-I type, which is hotter than previous estimates, where blends with lines from the WR star were not accounted for (Baschek & Scholz 1971; Conti & Smith 1972; Schaerer et al. 1997).

Millour et al. (2007, hereafter Paper I) refined the distance to the system ( $368^{+38}_{-13}$  pc) using an accurate astrometric measurement from the Astronomical Multi-BEam Recombiner (AMBER, Petrov et al. 2007) operated at the Very Large Telescope Interferometer (VLTI). In that first paper, we also revised the spectral types of the WR and O star through the comparison with radiative transfer models for both components. We discussed the origin of strong residuals in the absolute visibility curves, speculating they would come from the free-free emission of the wind collision zone (WCZ) between the two stellar winds, but could not provide conclusive evidence. The detection of the WCZ is a major observational challenge as the semimajor axis of the binary is 3.5 thousandths of an arcsecond (milliarcsecond or mas – 1.2 au at the distance of the binary) and, according to Hanbury Brown et al. (1970), North et al. (2007) and Millour et al. (2007), the stellar radii are below a milliarcsecond.

The collision of the two hypersonic winds results in a dense, hot shocked region, as sketched in Fig. 1. The shocked region manifests itself in various ways. First evidence comes from periodic variability in emission lines (St.-Louis, Willis & Stevens 1993), as the shocked region eclipses line forming regions during a fraction of the orbit. Due to its  $10^7$ – $10^8$  K temperature, the WCZ is directly detected in X-rays and analysis of the light curves and spectra constrain the opening angle of the shocked region and mass-loss rates of the winds (Willis, Schild & Stevens 1995; Stevens et al. 1996; Rauw et al. 2000; Schild et al. 2004). Direct detection of the WCZ has been elusive in other wavebands. Non-thermal radio emission, which is often detected in colliding wind binaries as a result of particle acceleration at the shocks remains undetected (Williams et al. 1990). Dust emission often found in binaries with a WR component (WC9 subtypes, see e.g. WR 104 in Tuthill et al. 2008) is also notably absent (Monnier et al. 2002). Direct observations of the WCZ in the optical and infrared remain a challenge, as it is strongly overshadowed by the wind and/or photospheric emission of the binary. It has only been possible for the very bright  $\eta$  Carinae system, where the angular separation between the stars is much larger (Weigelt et al. 2016). While signatures of the WCZ are likely present in the data presented in Paper I, a firmer answer requires



**Figure 1.** Schematic view of  $\gamma^2$  Vel in the plane of the binary showing the WR wind (red) and O wind (blue) and their shocked counterparts. Both winds are separated by a contact discontinuity (dashed black line). The dotted arc shows the orbit of the WR star around the O star. The dotted circles show the regions referred to as the WR star and the O star. The stellar discs, binary separation and shocked regions are roughly to scale.

more data and a detailed model of the structure and dynamics of the interaction region.

The shocked winds are separated from each other by a contact discontinuity (see Fig. 1), which may be subject to various instabilities (Stevens, Blondin & Pollock 1992). Close to the binary, the hydrodynamic structure is essentially determined by the momentum flux ratio of the winds and radiative cooling. In  $\gamma^2$  Vel, we expect the shocked structure to be heavily bent towards the O star, which has a less dense wind. Further out, orbital motion turns the shocked structure into a spiral (Lamberts et al. 2012). While analytic estimates provide the location of the shocked region between the stars and the asymptotic opening angle of the WCZ (Lebedev & Myasnikov 1990), hydrodynamic simulations are necessary to determine the complete 3D geometry of the interaction region, especially at distances where the spiral structure cannot be neglected. Only numerical simulations provide a complete model of the density, velocity and temperature conditions in the WCZ (Pittard 2009). These can then be used to model data to be compared with observations. For instance, Walder, Folini & Motamen (1999), Henley, Stevens & Pittard (2005) computed X-ray data based on hydrodynamic simulations. Comparison with observations suggested that radiative braking is probably at work in  $\gamma^2$  Vel. Radiative braking (Gayley, Owocki & Cranmer 1997) may occur when the shocked region is very close to the secondary star and is pushed away by the strong radiation pressure of the latter. It results in a larger opening angle than would be expected from the wind parameters of the stars.

Infrared interferometry offers a unique opportunity to directly probe the WCZ and put constraints on its spatial extension and relative flux. With this paper, we report on the follow-up AMBER observations on this system (Section 2). First, using a geometrical model, we refine the orbital solution of the binary using the wide orbital coverage of the data. Our continuum and spectral analysis provides further information on the residuals discussed in Paper I, that were tentatively attributed to the wind–wind collision zone between the two stars (Section 3). We then present the 3D hydrodynamic simulations that establish the properties of the WCZ (Section 4). Based on the simulations, we compute model images and then compare the resulting visibility curves and closure phases with the data (Section 5). We then discuss how the direct

**Table 1.** Log of  $\gamma^2$  Vel observations, sorted by date, including the data of Paper I, which we have reprocessed for the purpose of the current paper. The spectral configuration distinguishes between low resolution (LR), medium resolution (MR) and high resolution (HR) configurations. #Obs. is the number of observations of  $\gamma^2$  Vel during the considered night. ‘Orb.’ stands for ‘Orbital solution determination’ and ‘Spec.’ stands for ‘Spectral separation’ in the ‘Used for?’ column. In the data set from 2006 February 7, baselines are all aligned in a direction perpendicular to the binary direction, making it useless (see text and Fig. A1 for details).

Night	Calibrators HD	Spec. conf.	Band	#Obs.	Used for?	MJD	Orb. phase
2004 December 25	75063	MR	<i>K</i>	4	Orb., Spec.	53365.18–20	0.315
2006 February 7	73155	MR	<i>H</i>	1	–	53774.15	0.523
2006 December 29	34053, 53840, 81720	LR	<i>H, K</i>	1	Orb.	54099.28	0.663
2007 March 7	37984, 69596	LR	<i>H, K</i>	1	Orb.	54166.13	0.514
2007 March 31	68763	MR	<i>K</i>	2	Orb., Spec.	54190.06–08	0.819
2008 December 20	68512, 75063, 69596	HR	<i>K</i>	6	Orb.	54821.18–37	0.857
2008 December 21	35765, 68512, 69596	MR	<i>K</i>	8	Orb., Spec.	54822.15–37	0.870
2008 December 22	68512, 69596	MR	<i>K</i>	8	Orb., Spec.	54823.15–38	0.882
2010 January 22	68512, 69596	MR	<i>H</i>	8	Orb., Spec.	55219.07–28	0.924
2012 January 6	23805, 36689, 67582, 82188	LR	<i>H, K</i>	1	Orb.	55932.27	0.005

combination of numerical simulations and observational data opens new possibility for the study of massive binary systems (Section 6) and conclude (Section 7).

## 2 OBSERVATIONS AND DATA PROCESSING

### 2.1 Observations

AMBER is a three-telescope spectro-interferometric combiner (Petrov et al. 2007) operating at the VLTI. It allows one to observe in the infrared *J*, *H* and *K* bands simultaneously at a low spectral resolution of  $\lambda/\Delta\lambda = 35$ , or the *H* or *K* bands at a medium spectral resolution of  $\lambda/\Delta\lambda = 1500$ , and small chunks of the *K* band at high spectral resolution of  $\lambda/\Delta\lambda = 12\,000$ , with an angular resolution of a few thousandth of an arcsecond. Since Paper I,  $\gamma^2$  Vel was observed with AMBER several times using all the available spectral configurations. We cover a wide range of orbital phases shown in Fig. 3 over a little more than 7 yr.<sup>2</sup>

Table 1 lists the different epochs available together with the corresponding orbital phases. Of interest, are extensive observing campaigns in 2008 and 2010 where we used full nights to stack up high-signal-to-noise ratio data of the system. By far, these nights provide the most accurate spectro-interferometric data sets of  $\gamma^2$  Vel at one single orbital phase each. The medium spectral resolution data of 2004 December 25 was already used in Paper I to determine the distance of the system.

The other data sets, obtained with low(er) spectral resolution, give less insights to the details of the binary system, but provide us with astrometric measurements along its orbit. The (*u*, *v*) plane coverage of each observation is shown in Fig. A1.

The interferometric field of view is approximately equal to the Airy pattern of one telescope, i.e. typically 50 mas for the *K*-band UT (unit telescope) observations performed before 2008, or 250 mas for the *K*-band AT (auxiliary telescope) observations in 2008 and after. The interferometer is sensitive to a fraction of this field of view

without any bias, as the use of fibres to perform spatial filtering has an impact on the effective unbiased field of view (Tatulli, Mège & Chelli 2004). In our case, the whole system is much smaller than the Airy disc of the field of view; therefore, we do not expect to have a significant bias on the  $\gamma^2$  Vel measurements.

The formal angular resolution of our observations is set to be the resolution at the longest baseline length, here  $\approx 130$  m, i.e.  $\approx 3.5$  mas at  $2\ \mu\text{m}$ . However, the interferometer is sensitive to much smaller objects thanks to the precision of the measurements. For example, with a 3 per cent accuracy on one visibility measurement with a 130 m baseline, one can measure a 91 per cent fringe contrast at the  $3\sigma$  level. At  $2\ \mu\text{m}$ , this corresponds to a uniform disc of 0.95 mas diameter. This ‘super-resolution’ effect can be further improved by stacking measurements.

### 2.2 Data reduction

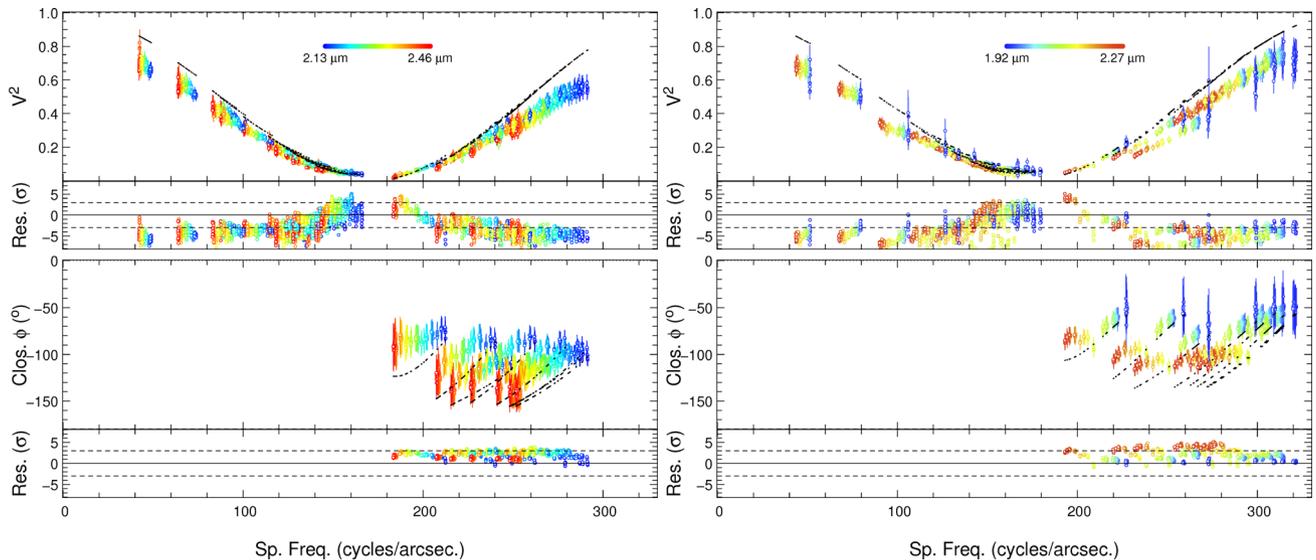
The AMBER data sets consist of spectro-interferometric measurements: namely one spectrum, three dispersed squared visibilities, three dispersed differential visibilities, three dispersed differential phases and one dispersed closure phase per individual measurement (see Fig. A3 for illustrations of these observables). The data reduction scheme is now relatively settled for bright sources (see details in Tatulli et al. 2007; Chelli, Utrera & Duvert 2009). We use the standard AMDLIB data reduction library, version 3.0.4, plus our own additional scripts for calibration (Millour et al. 2008). Some data sets present specific issues, namely:

- (i) 2006 February 7: There is only one science and one calibrator record, and this data set presents baselines all aligned in the same direction. Unfortunately, the binary axis is perpendicular to the baseline direction, and the measurement is not used in our analysis.
- (ii) 2012 January 6: The system is close to periastron; therefore, the binary star is not formally resolved by the interferometer.

## 3 ANALYSIS OF AMBER DATA WITH A GEOMETRICAL MODEL

To model the interferometric data, we use the software FITOMATIC (Millour et al. 2009b), which was developed in-house according

<sup>2</sup>The interferometric data will be publicly available at the Optical Interferometry Database from the Jean-Marie Mariotti Center <http://oidb.jmmc.fr/index.html>.



**Figure 2.** Continuum visibilities (top plots) and closure phases (bottom plots), together with residuals (smaller plots), from our high-fidelity observing campaign from 2008, projected along the binary star direction (to ease the reading of the binary star modulation). Left: 2008 December 21, right: 2008 December 22. The dashed lines representing the two point sources geometrical model are too high in visibility and too far from zero in closure phase when compared with the measurements, showing that a ‘two point sources’ model cannot perfectly fit the data. The colours show the wavelength dependence.

to the lessons learned from [Paper I](#) to account for chromatic interferometric data sets.<sup>3</sup> FITOMATIC is written in the scientific data language YORICK.<sup>4</sup> It reads OIFITS files [optical interferometry FITS, Pauls et al. (2004)]. The user defines a model of the source, according to a set of pre-defined models including point sources, uniform discs, or Gaussian discs (as used in Millour et al. 2009b; Chiavassa et al. 2010; Chesneau et al. 2014). These models can be combined together to build up more complicated models, like the 3D-pinwheel nebula model used by Millour et al. (2009a). Another option is to compute brightness distributions from models, as for the rotating and expanding disc model used in Millour et al. (2011). Once the parameters are set, the Fourier Transform of the modelled brightness distribution is computed and synthetic observables (squared visibilities, differential visibilities, differential phases and closure phases) are computed at the wavelengths and projected baselines of the observations. The specific aspect of FITOMATIC is its ability to define vector-parameters, i.e. parameters that may depend on wavelength and/or time.

These synthetic observables are then compared to the observed ones by computing square differences, which are minimized by varying the model parameters. A simulated annealing algorithm is used to scan the parameter space and optimize the fit globally (finding the least squares absolute minimum). In this section, we present an analysis of the squared visibilities and closure phases based on geometrical models of the system. The complex visibility is the Fourier transform of the brightness distribution of a source. Its amplitude is related at first order to the size of the source, and its phase to its position and structure. The squared visibility is simply the squared modulus of the complex visibility, and therefore is related to the source’s size. The closure phase is an ‘instrument free’ combination of the phases for each baseline in a triplet of apertures and relates to the asymmetry of the source. The differential phase is another way of measuring phases. At first order, it is related to

the source position (photocenter) at a given wavelength, relative to its position at another wavelength. More details can be found in Lachaume (2003). The analysis based on model images stemming from the hydrodynamic simulation is presented in Section 5.

### 3.1 Continuum analysis

We first focus on the continuum regions in our spectra (see Fig. 4 in Section 3.3). We perform this first analysis on the two nights of 2008 December with medium spectral resolution ( $R = 1500$ ) since these two nights offer the best stability of the instrument and atmosphere transfer function (better than 3 per cent for both nights). We checked that the results obtained here are consistent throughout the whole data set.

As in [Paper I](#), we first compare the AMBER data with a two point sources model, representing the two stars. Fig. 2 shows the best-fitting models for the squared visibilities and closure phases for 2008 December 21 and 2008 December 22. The reduced  $\chi^2$  is not good: 10.7 for the 21st and 12.5 for the 22nd and there are several discrepancies that are clearly above the noise limit, as in [Paper I](#). It is interesting to note that the higher visibilities in the model (in the 40–100 and the 280–320 cycles arcsec<sup>-1</sup> intervals) are systematically larger than the measurements, and the measured closure phase is systematically closer to zero than the binary model values.

In [Paper I](#), we added a fully resolved uniform component to explain this effect. This additional flux greatly improves the agreement with the data (reduced  $\chi^2$  of 1.1 and 2.3 for the 21st and 22nd, respectively). However, such a uniform component around the binary has little physical justification. Therefore, we now focus on more physically relevant alternatives including resolved stellar components discussed here, and the WCZ model presented in Section 5.

We first use a Gaussian model for the WR and its wind and a uniform disc model for the O star. Our approach is similar to North et al. (2007): the Gaussian model for the WR star is imperfect but good enough for this study, as the star and its wind are marginally resolved by the interferometer. Its full width at half-maximum (FWHM) is

<sup>3</sup> FITOMATIC is available at <http://fitomatic.oca.eu>.

<sup>4</sup> Developed by D. H. Munro, Lawrence Livermore National Laboratory, <http://yorick.github.io>.

**Table 2.** Comparison between the AMBER data and several geometrical models in the continuum. The best-fitting reduced  $\chi^2$  is given for each case. The last line combines data from both nights.

Night	$\chi^2$ 2 pt <sup>a</sup>	$\chi^2$ 2 pt + cont. <sup>b</sup>	$\chi^2$ G <sup>c</sup> + UD <sup>d</sup>	$\theta_G$ (WR star)	$\theta_{UD}$ (O star)
2008 December 21	10.7	1.1	1.3	$\theta_G \leq 1$ mas	$1.5 \leq \theta_{UD} \leq 1.9$ mas
2008 December 22	12.5	2.3	3.1	$0.5 \leq \theta_G \leq 1.1$ mas	$0.5 \leq \theta_{UD} \leq 1.3$ mas
21 + 22	13.8	3.2	3.8	$0.39 \leq \theta_G \leq 1.32$ mas	$0.75 \leq \theta_{UD} \leq 1.63$ mas

Notes. <sup>a</sup>Point source. <sup>b</sup>Fully resolved component. <sup>c</sup>Gaussian disc. <sup>d</sup>Uniform disc.

related but not necessarily equal to the continuum-emitting region of the WR star. The FWHM definition of the WR size differs from the definition given in Paper I [uniform disc (UD) diameter] and the relation between both is detailed in table 3 of Paper I. However, since the stars are barely resolved, we can use a fixed factor of  $\approx 0.65$  between Gaussian FWHM and uniform disc diameter to compare both (see e.g. values in table 1 of Haniff, Scholz & Tuthill 1995). The resolved stellar components model (reduced  $\chi^2$  of 1.3 and 3.1 for the 21st and 22nd, respectively) matches the data equally well as the model with a resolved uniform component, and makes more physical sense. We also combined the nights of 21st and 22nd to refine the values of the resolved diameters. The reduced  $\chi^2$  is less good in this case because binary motion is not included in this simple model.

Table 2 provides a summary of the different models tested here. We note that the best match to the data results in rather large stellar diameters. We find a typical size of  $\approx 1.1$  mas for the diameter of O star, and a typical FWHM of  $\approx 0.9$  mas for the WR star. These values are about a factor two to three higher than the values computed in Paper I (diameter of 0.48 mas for the O star and 0.28 for the WR star) and North et al. (2007). Given the distance of the system, this corresponds to a radius of 51  $R_\odot$  and 36  $R_\odot$  for the O and WR star, respectively.

To strengthen this unexpected result, we performed the same analysis using the LITPRO software<sup>5</sup> (Tallon-Bosc et al. 2008). LITPRO corroborates our findings and also provides a correlation matrix that shows a strong anticorrelation ( $-0.9$ ) between the two stellar sizes. This means that the sizes may be interchanged, meaning a stellar diameter of 0.9 mas for the O star and 1.1 mas for the WR star. The latter situation would be a bit more in line with spectral analysis for the O star (De Marco & Schmutz 1999), but would be worse for the WR star.

### 3.2 Astrometry

One product of the model fitting process is the astrometry of the binary star (separation, position angle) at all the observed epochs, listed in Table A1. The three different models presented in Table 2 provide the same astrometric measurements within 0.02 mas, or 20 microarcsec.

We adjust these data points with a classical Newtonian orbit with seven parameters (period  $P$ , semimajor axis  $a$ , eccentricity  $e$ , periastron passage date  $T_0$ , longitude of periastron  $\omega_{WR}$ , position angle of node  $\Omega$  and inclination angle of the orbital plane relative to the line of sight  $i$ ). To do so, we use a Markov Chain Monte Carlo algorithm with a simulated annealing algorithm for the hundreds of chain links we used, out of which we kept a few orbital parameters sets within  $1\sigma$  error.

This allows us to provide an independent orbital solution of the system compared to North et al. (2007), obtained with optical interferometry. We first computed a solution with all the parameters free, including the eccentricity and period. This solution provides a final eccentricity ( $0.29 \pm 0.01$ ) that is quite far from the previous best estimate based on radial velocities (Schmutz et al. 1997). It also results in an orbital period in tension with previous results. Similarly to North et al. (2007), we find that the period  $P$  and the time of periastron passage  $T_0$  are strongly mutually dependent.

We independently compute the eccentricity with our two measurements close to periastron (2012 January 6) and close to apastron (2007 March 7). Let  $R$  be the ratio between the two astrometric separations, the eccentricity  $e$  can be calculated as  $e = \frac{1-R}{1+R}$ . We find  $e = 0.34$  with this method. This further casts doubt on the result with  $e$  and/or  $P$  as free parameters. The latter may stem from underestimated or overestimated error bars on some data points (especially in 2004), and/or not taking into account measurements correlations. As such, we discarded this first solution.

For the two presented solutions, we adopted the value of  $P$  to 78.53 d and  $e$  to 0.326 or 0.334, as determined by Schmutz et al. (1997) and North et al. (2007), respectively. Overall, we find a solution that is very close to the one of North et al. (2007) and that refines some error bars, especially the semimajor axis, which is more precisely defined and slightly smaller. As we use the same method as described in their paper, it is not surprising that we find a distance of  $345\text{--}346 \pm 7$  pc that is compatible with their distance. We also find stellar masses that are compatible with their values. These results are listed in Table 3. The astrometric data at the observed phases together with the best astrometric orbit of  $\gamma^2$  Vel from North et al. (2007) are plotted in Fig. 3.

Our distance estimate is consistent with North et al. (2007) and the revised *Hipparcos* measurement (van Leeuwen 2007). The current uncertainties on the distance of  $\gamma^2$  Vel ( $\approx 2$  per cent) are dominated by the error on the maximal radial velocities of the stars ( $K_1$  and  $K_2$  parameters in Schmutz et al. 1997). A factor 10 improvement on these parameters would allow to reach sub-percent accuracy for the distance of the system with the current astrometric data set. Unfortunately, a 10 times better estimate of the semimajor axis would reduce the error on the distance by only 0.5 per cent. This calls for a better understanding of the spectral variability of the emission lines of the  $\gamma^2$  Vel spectra in order to improve the radial velocities accuracy and  $K_1$  and  $K_2$  values.  $\gamma^2$  Vel is too bright for direct parallax measurements with *GAIA*, a new distance measurement will only be available with the last data release.

### 3.3 Spectral analysis

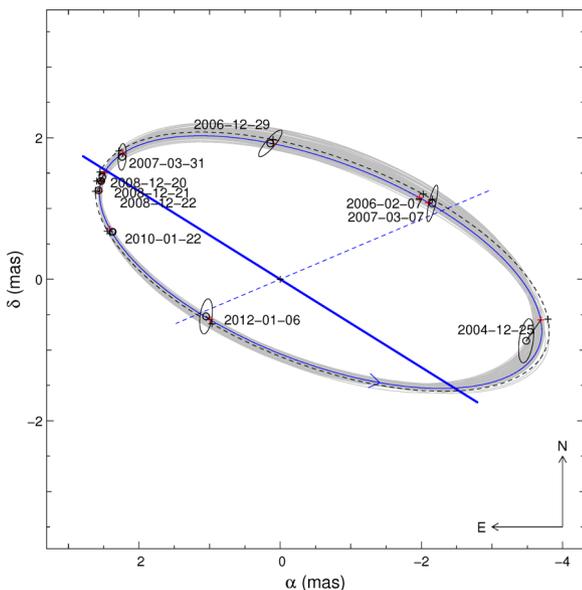
In Paper I, we isolated continuum regions to determine the astrometric solution and then separated the spectral components using a radiative transfer model. Here, we can determine both simultaneously without the need for a spectroscopic model. The modelled binary system can be set in FITOMATIC to have a free spectrum for

<sup>5</sup> Available at <http://www.jmmc.fr/litpro>.

**Table 3.** Parameters of the system from the literature and from the current work when the eccentricity  $e$  is left as a free parameter or fixed to the North et al. (2007) value or the Schmutz et al. (1997) value.

Parameter	Literature	This paper ( $e = 0.334$ )	This paper ( $e = 0.326$ )
Distance (pc)	$336^{+8}_-7^a$ , $368^{+38}_-13^b$	$345 \pm 7$	$346 \pm 7$
Period $P$ (d)	$78.53 \pm 0.01^c$	Fixed (78.53)	Fixed (78.53)
Semimajor axis $a$ (mas)	$3.57 \pm 0.05^a$	$3.48 \pm 0.02$	$3.47 \pm 0.02$
Eccentricity $e$	$0.334 \pm 0.003^a$ , $0.326 \pm 0.01^c$	Fixed (0.334)	Fixed (0.326)
Periastron $T_0$ (d)	$50120.4 \pm 0.4^a$	$50120.7 \pm 0.2$	$50120.6 \pm 0.2$
Peri. long. $\omega_{\text{WR}}$ ( $^\circ$ )	$67.4 \pm 0.5^a$	$68.3 \pm 0.9$	$67.8 \pm 0.9$
PA of node $\Omega$ ( $^\circ$ )	$247.7 \pm 0.4^a$	$247.6 \pm 0.4$	$247.1 \pm 0.3$
Inclination $i$ ( $^\circ$ )	$65.5 \pm 0.4^a$	$65.5 \pm 0.7$	$65.4 \pm 0.8$
$M_O$ ( $M_\odot$ )	$28.5 \pm 1.1^a$	$28.4 \pm 1.5$	$28.7 \pm 1.7$
$M_{\text{WR}}$ ( $M_\odot$ )	$9 \pm 0.6^a$	$8.9 \pm 0.5$	$9.0 \pm 0.5$

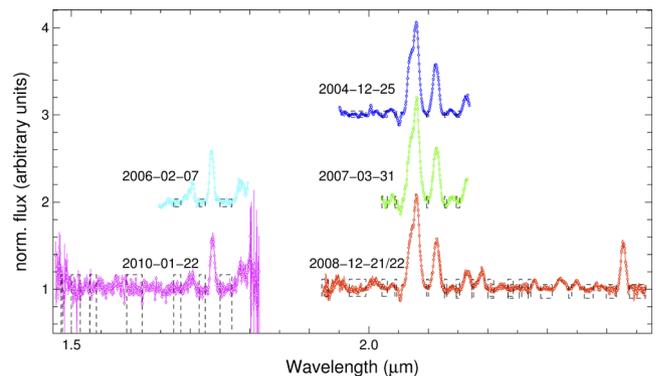
Notes. <sup>a</sup>North et al. (2007). <sup>b</sup>Paper I. <sup>c</sup>Schmutz et al. (1997).



**Figure 3.** Orbital phases and positions of the WR star component relative to the O component for the different epochs related in this paper, with  $e$  fixed to 0.334 and  $P$  fixed to 78.53 d. The solid blue ellipse represents the new orbit, while the dotted ellipse represents the North et al. (2007) orbit. The small circles and ellipses represent the measured astrometric points, while the red crosses show the expected positions of the WR star with the new orbital solution. The blue thick line represents the line of nodes and the dashed line the semimajor axis of the system. The direction of motion is represented by an arrow. The grey ellipses show similarly significant results of the Markov chain computation.

each source. We do not expect this to lead to a major difference in the final result compared to Paper I.

The medium spectral resolution spectra of  $\gamma^2$  Vel in 2004, 2006, 2007, 2008 and 2010 are shown in Fig. 4. As the spectra from the point sources are free parameters in our model, we can separate the spectrum from each star, the result of which is shown in Figs 5 and 6. The best-fitting model compared with the spectrally dispersed AMBER data is shown in Fig. A3. The differential phases, combined with the spectrum and the orbital elements allow an exact separation of the spectra of the components of a multiple system (Petrov et al. 1996). The quality of this fit indicates that the spectra are successfully separated. However, the persistent shift observed at all wavelength between the observed and the model squared visibility shows that a binary model is insufficient. That triggered



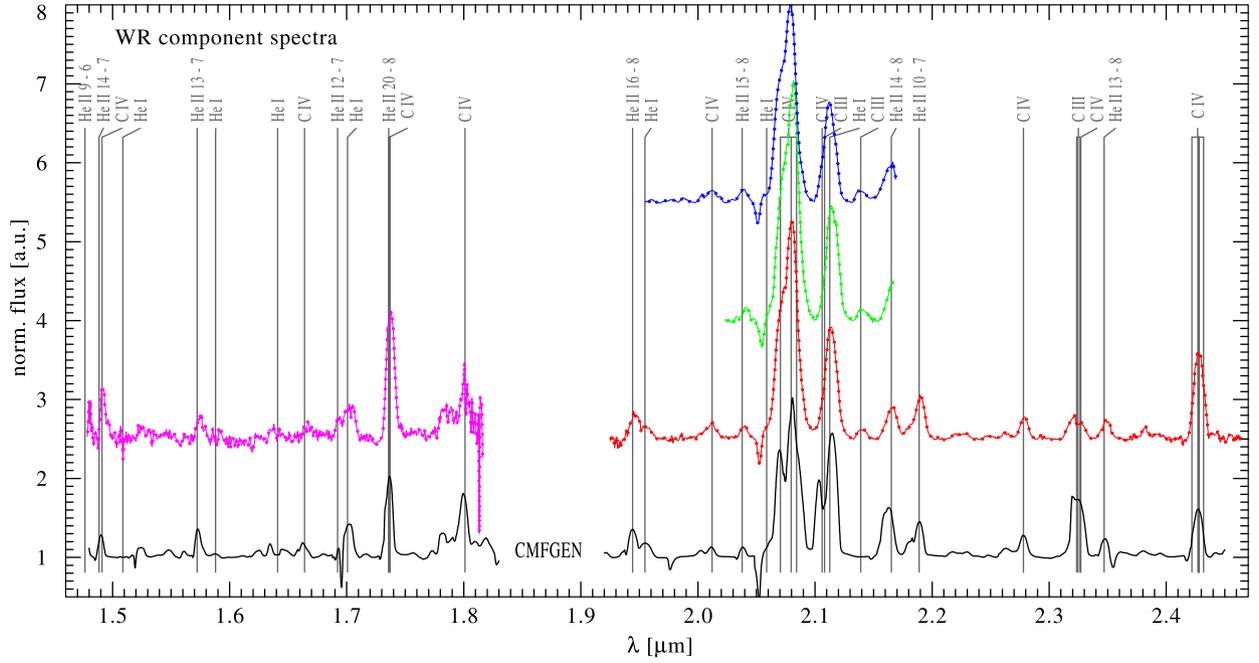
**Figure 4.** Spectra of the  $\gamma^2$  Vel system obtained with AMBER. The continuum normalization was determined within the dashed boxes. The colours correspond to different epochs: 2004 (blue, orbital phase  $\phi = 0.32$ ), 2006 (cyan,  $\phi = 0.52$ ), 2007 (green,  $\phi = 0.82$ ), 2008 (red,  $\phi = 0.87$ ) and 2010 (magenta,  $\phi = 0.92$ ). Spectra of the different epochs are offset for clarity.

the development of the complete model described in Section 5. We can nevertheless analyse the separated spectra as the data sets of 2008 and 2010 provide the full combined  $K$ - and  $H$ -band spectra, respectively. Therefore, we identify several more lines compared to Paper I (see Table A2). In the following, we describe the spectral classification and spectral variability observed in the different epochs.

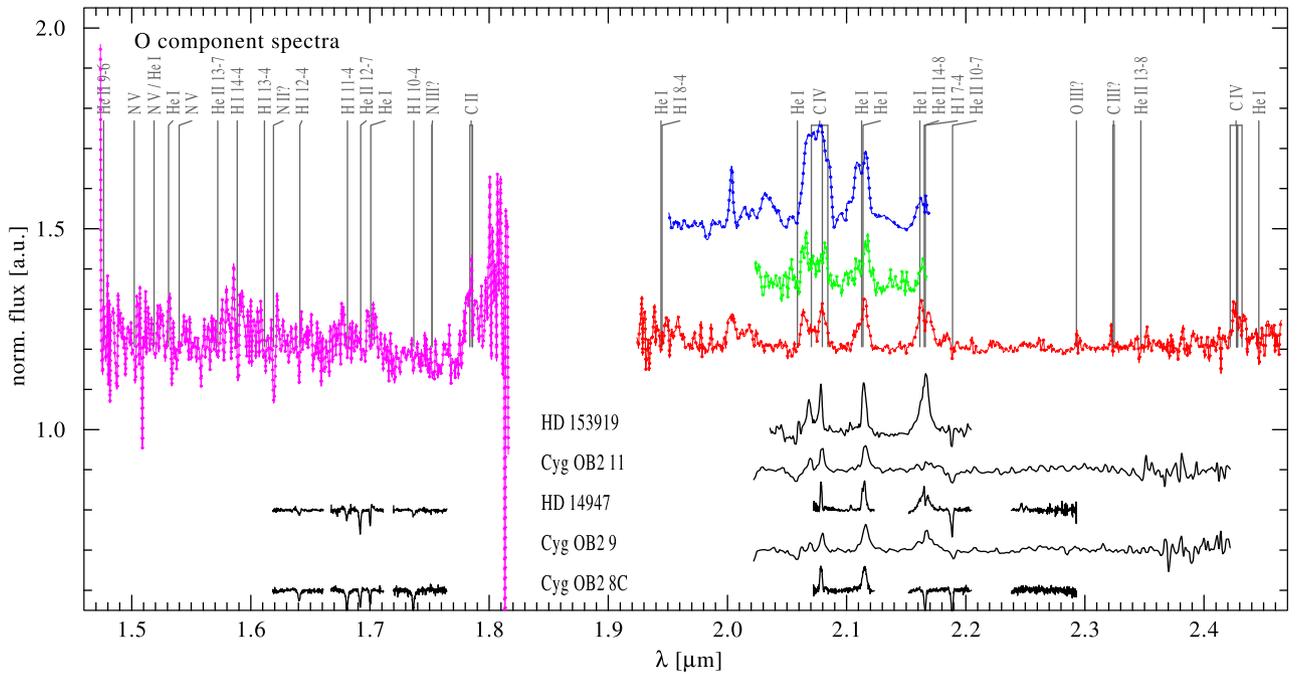
### 3.3.1 Spectrum of the WR star

Fig. 5 shows the full  $H$ - and  $K$ -band spectra of the WR star alone, with line identifications also listed in Table A2. It exhibits similar features to Paper I, i.e. very broadened emission lines of carbon and helium. The most prominent lines are the C IV multiplet ( $\lambda$  2.0705–0842  $\mu\text{m}$ ) and He II line series, as well as the He I absorption ( $\lambda$  2.0587  $\mu\text{m}$ ). Following Crowther et al. (2006), we use the  $K$ -band spectrum to measure the line ratio C IV 2.076/C III 2.110 and confirm the spectral type of the WR star as WC 8.

We include the CMFGEN (Hillier & Miller 1998; Dessart et al. 2000) model spectrum of the WR star presented in Paper I, which was computed on a much larger wavelength range than presented at that time. It is shown for comparison in Fig. 5. CMFGEN solves the radiative transfer equation, in a non-local thermal equilibrium, spherically symmetric expanding atmosphere and determines the resulting spectra. The overall match with the spectrum extracted from the data is excellent at all epochs.



**Figure 5.** Normalized separated spectra of the WR component of  $\gamma^2$  Vel with line identifications (see Fig. 4 for colour code of the different epoch data), shifted in flux by a constant for easier viewing. At the bottom, we show the good match to the CMFGEN model spectrum from Paper I (black line).



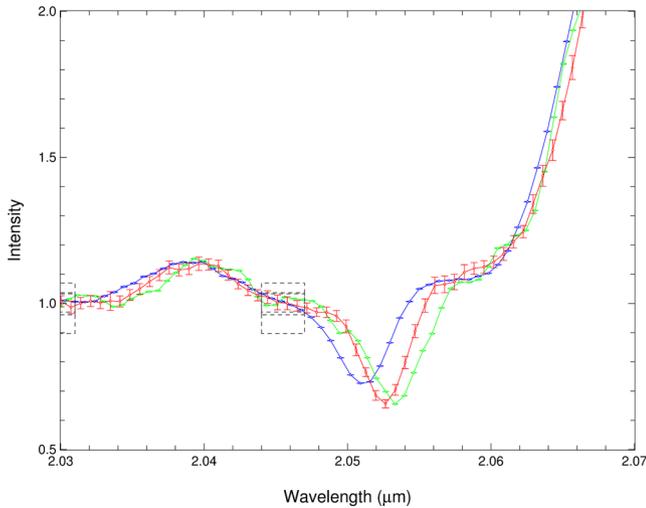
**Figure 6.** Normalized separated spectra of the O star component of  $\gamma^2$  Vel (the colour code is the same as in Fig. 4), the spectra are offset by a constant for clarity. For comparison, we include template spectra of O supergiants by Hanson et al. (1996, 2005). Although the latter provide the best match to the  $\gamma^2$  Vel spectrum, the spectrum from  $\gamma^2$  Vel is clearly more complex.

### 3.3.2 Spectrum of the O star

The O star spectrum is shown in Fig. 6. It displays a series of emission lines, which we tentatively identify (see Table A2). There are hydrogen lines of the Brackett series as well as helium, carbon and nitrogen features. We also see emission at 2.01  $\mu\text{m}$  but the spectrum might be contaminated due to the presence of the  $\text{CO}_2$  ro-vibrational atmospheric bands in this spectral region and residual C IV emission from the WR component.

As the interferometer only marginally resolves the binary star, the spectrum we refer to as ‘the O star spectrum’ actually corresponds to an area around the star (see dashed circle around the stars in Fig. 1). As such, it potentially contains emission from the O star, as well as the colliding wind region and some contribution of the free WR wind.

For classification of the spectral type, we retrieve template spectra from Hanson, Conti & Rieke (1996) and Hanson et al. (2005).



**Figure 7.** Wavelength shift and amplitude variation of the WR spectrum around the He II  $\lambda$  2.059  $\mu\text{m}$  absorption feature. The blue, green and red spectra correspond to 2004, 2007 and 2008, i.e.  $\phi = 0.36, 0.77$  and  $0.83$ , respectively.

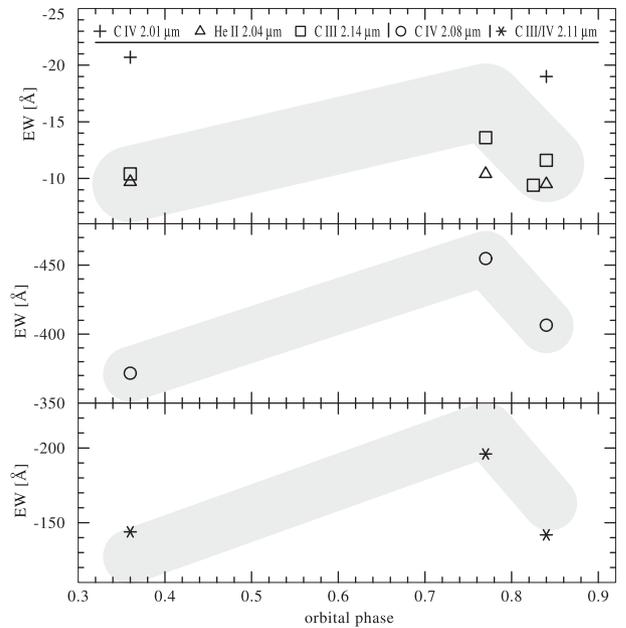
These catalogues contain observed infrared spectra for a variety of stars, and especially O-type stars. In Fig. 6, we show the five closest matches to the O star component of the  $\gamma^2$  Vel spectrum. We compare these spectra by calculating least squares between the templates and the observed spectrum.

Comparison with single O star spectra finds good agreement, for example with members of the Cygnus OB2 association: No. 8C (O5 If), No. 9 (O5 If+) and No. 11 (O5 If+) as well as and HD 14947 (O5 If). De Becker (2013) argues that for supergiants star like HD 14947, the soft thermal X-ray emission is rather underluminous compared to regular single O stars. This is because of the higher wind density, which also give rise to emission lines in the optical and infrared regime. Following these templates, we find a preference for an O5 If classification of the O component.

However, the best-matching spectrum in the near-infrared seems to be the one of HD153919, a high-mass X-ray binary with a O6.5Iaf+ star (Jones et al. 1973). By definition, high-mass X-ray binaries are composed of a massive star and a compact object (neutron star or black hole). The X-ray emission is orders of magnitude higher than for colliding stellar winds and results from the heating of the stellar material as it is accreted onto the compact object (see e.g. Jaisawal & Naik 2015, and references therein). This fact hampers further comparison with  $\gamma^2$  Vel. Still, the resemblance between spectra highlights the difficulty to classify the O star and supports the evidence that our ‘O star spectrum’ is in fact a composite of the O star and additional heated material, i.e. the WCZ.

### 3.3.3 Spectral variability

The spectral variability in the WR spectrum is shown in detail with the He I absorption line at 2.0587  $\mu\text{m}$  in Fig. 7. The variability is mainly made of a wavelength shift, which is likely due to the radial velocity of the star. We also note small amplitude variations, especially between 2004 and 2008. Variations are present between 2007 and 2008 (recorded at approximately the same orbital phase), though smaller, that may be due to the presence of clumps in the WR wind and/or instabilities in the shocked region, especially of the material along the line of sight to the inner part of the binary. Short-term variability has already been reported in  $\gamma^2$  Vel (Baade,



**Figure 8.** Measured EWs of emission lines in the WR K-band spectrum over orbital phase. A clear trend is visible with stronger emission approaching periastron passage.

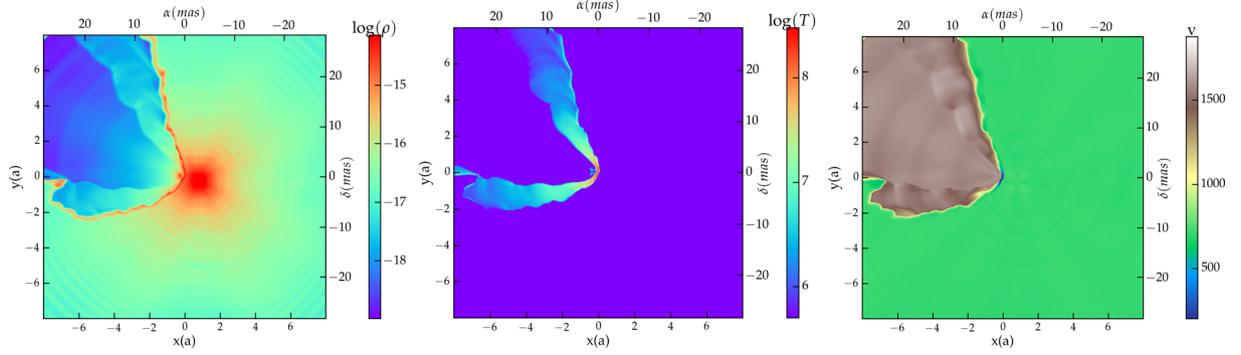
Schmutz & van Kerkwijk 1990) and in other WR systems (see e.g. Luehrs 1997; Stevens & Howarth 1999).

In addition, we measure equivalent widths (EWs) for the prominent emission lines in the WR K-band spectrum over the available data of all epochs. Fig. 8 shows the measured EWs, clearly changing with the orbital phase. Varricatt, Williams & Ashok (2004) suggest that such trend can be explained by less dust emission diluting the spectra near periastron passage. However, we do not have a satisfactory explanation for this observation, as  $\gamma^2$  Vel is not a dust-emitting WR star, thus eliminating the impact of dust on the spectral lines (Monnier et al. 2002).

The O star spectrum also shows temporal variability, which seems to be strongly dependent on the orbital phase. Indeed, the 2007 and 2008 spectra (roughly at the same orbital phase) look almost identical, whereas the 2004 spectrum (taken at opposite phase) exhibits striking differences: for example, the C IV lines exhibit a flat-top profile in 2004, while it looks asymmetric and double-peaked in the 2007 and 2008 spectra.

The line profiles and variations in relation to the orbital motion are discussed by Ignace, Bessey & Price (2009) and Henley, Stevens & Pittard (2003). They respectively focus on forbidden emission lines and X-ray lines forming in the WCZ, and clearly show line variations from flat-topped to double peak profiles. Since the O star spectrum in our case most likely also contains contributions from the WCZ and maybe even the WR wind, we might expect to see spectral variability as described above along the orbit.

In the next sections, we perform hydrodynamic simulations of the system and extract corresponding model data. Thanks to the spatially resolved interferometric data, we focus on the detection of the shocked region around the O star. While we attribute the residuals in the O star spectrum as coming from the WCZ, detailed modelling of the line profiles in order to constrain wind parameters such as the opening angle as suggested by Ignace et al. (2009) is beyond the scope of this paper. Focusing on the continuum emission from a large field of view, we determine the flux ratio of the WCZ.



**Figure 9.** Density ( $\text{g cm}^{-3}$ ), temperature (K) and velocity ( $\text{km s}^{-1}$ ) in the mid-plane of the binary for  $\phi = 0.3$ . The WR star is located in the lower right corner and the O star in the upper left. The length scale is the semimajor axis and the plot is centred on the centre of mass of the binary. The colliding wind region is wrapped around the O star.

## 4 HYDRODYNAMIC MODEL

### 4.1 Numerics

We use the hydrodynamics code `RAMSES` for our simulations (Teyssier 2002). This code uses a second-order Godunov method to solve the hydrodynamics equations

$$\begin{aligned} \frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{v}) &= 0 \\ \frac{\partial (\rho \mathbf{v})}{\partial t} + \nabla \cdot (\rho \mathbf{v} \mathbf{v}) + \nabla P &= 0 \\ \frac{\partial E}{\partial t} + \nabla \cdot [\mathbf{v}(E + P)] &= n^2 \Lambda(T), \end{aligned} \quad (1)$$

where  $\rho$  is the density,  $n$  the number density,  $\mathbf{v}$  the velocity and  $P$  the pressure of the gas. The total energy density  $E$  is given by

$$E = \frac{1}{2} \rho v^2 + \frac{P}{(\gamma - 1)}, \quad (2)$$

where  $\gamma$  is the adiabatic index, set to  $5/3$  to model adiabatic flows. We include a passive scalar to distinguish both winds.  $\Lambda$  is the radiative cooling rate of the gas, based on Sutherland & Dopita (1993). This cooling curve assumes an optically thin gas in ionization equilibrium. We assume solar abundances for both winds, which underestimates the cooling in the WR wind for temperatures below  $10^7$  K (Stevens et al. 1992) by a factor of a few.

We use the MinMod slope limiter together with the HLLC Riemann solver to avoid numerical quenching of instabilities. We perform 3D simulations on a Cartesian grid with outflow boundary conditions. The size of the simulation domain is 16 times the binary semimajor axis, or about 60 mas, largely covering the emitting region of the system. The resolution is uniform set to  $N_x = 1024$ . This resolution is slightly lower than in other numerical work (Pittard 2009; Lamberts et al. 2012) but is sufficient to capture the dynamics of the interaction region and allow comparison with observations. Our physical resolution is about  $2 \times 10^{11}$  cm, which should yield limited numerical heat conduction at the interface between the winds (Parkin & Pittard 2010). To check the impact of resolution, we perform a simulation of the system covering eight times the binary separation with  $N_x = 1024$  (twice the effective resolution of our reference simulation) and find that differences in the emission maps are below 5 per cent, confirming that our resolution is sufficient.

To simulate the winds, we keep the same method as used in Lamberts, Fromang & Dubus (2011), which was largely inspired from Lemaster, Stone & Gardiner (2007). Around each star, we

**Table 4.** Wind parameters used for the hydrodynamic simulation. Data taken from (a) St-Louis et al. (1993), (b) De Marco & Schmutz (1999), (c) North et al. (2007).

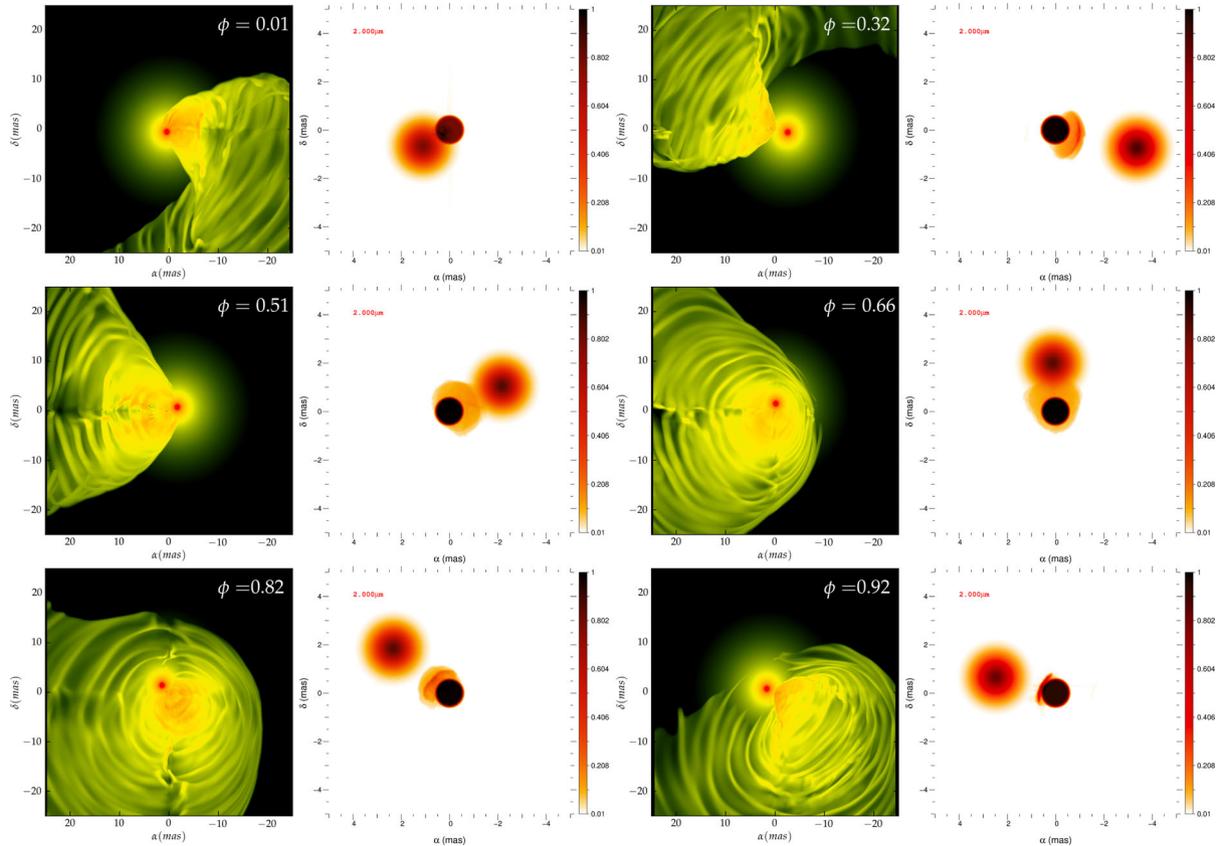
	WR	O
$v_\infty$ ( $\text{km s}^{-1}$ )	$1550 \pm 150$ (a)	$2500 \pm 250$ (b)
$\dot{M}$ ( $M_\odot \text{ yr}^{-1}$ )	$8 \pm 4 \times 10^{-6}$ (c)	$1.8 \pm 0.36 \times 10^{-7}$ (b)

create a wind by imposing a given density, pressure and velocity profile in a spherical zone centred on the stars, of radius  $l_O$  and  $l_{WR}$  for each star. These zones are reset to their initial values at each time-step to create steady winds. To allow for spherical symmetry, we set the  $l_{WR}$  to eight computational cells (in radius). The same large value for  $l_O$  could impact the shocked structure, which is very close to the O star. Therefore, we set  $l_O$  to four computational cells, which does not impact the formation of the WCZ. As a trade-off, the spherical symmetry of the wind is less good than for the WR star, but this does not strongly impact the large-scale structure of the O star wind, which is set by the binary interactions (see Fig. 9). The orbital motion of the stars is determined using a leapfrog method. As the orbital velocity is negligible with respect to the speed of the winds, each wind can be considered isotropic in the frame corotating with the corresponding star.

Table 4 shows the wind parameters for our simulation, found in the literature and compatible with our `CFMGGEN` model for the WR star. We use the orbital parameters derived in Section 3. The temperature in the winds is set to  $10^5$  K, which is much higher than expected in stellar winds. However, given the speed and density in the winds, this value guarantees that the winds are highly supersonic, in which case the shocked region is unaffected by the value of the pre-shock temperature. For distances beyond  $l_{WR}$  and  $l_O$ , the temperature evolves according to the equations of hydrodynamics and the cooling curve (equation 1). The momentum flux ratio of the winds, which is the main parameter determining the position and opening angle of the shocked region is given by Lebedev & Myasnikov (1990):

$$\eta \equiv \frac{\dot{M}_{WR} v_{WR}}{\dot{M}_O v_O} \simeq 26. \quad (3)$$

This value is compatible with the  $\eta = 33$  from De Marco et al. (2000), with the main difference coming from the mass-loss rate of the WR star, which depends on the clumping factor (Schild et al. 2004). Considering the uncertainties on the stellar wind parameters (see Table 4),  $\eta_{\min}$  can be as low as 9 and  $\eta_{\max}$  as high as



**Figure 10.** Volume rendering of the logarithm of the density in the shocked region (left) and the square root of the continuum intensity maps at  $2\ \mu\text{m}$  (right; different scale) at six of the observed phases ( $\phi = 0.01, 0.32, 0.51, 0.66, 0.82, 0.92$  from upper left to lower right). The same fluxes of each component were used here: 54 per cent of the total flux for the O star (uniform disc), 41 per cent for the WR star (Gaussian disc) and 5 per cent for the WCZ. On the volume rendering, the WR star is a bright red spot while the O star is too embedded in the wind collision region to be distinguished.

64. When instabilities and radiative effects are dynamically negligible, the intersection between the semimajor axis and the contact discontinuity between the winds is given by

$$r = a \frac{\sqrt{\eta}}{1 + \sqrt{\eta}}, \quad (4)$$

where  $a$  is the binary separation. Especially for the higher values of  $\eta$ , the wind collision is close to the O star, where the WR wind has reached its terminal velocity. At such close distance, the wind from the O star has not reached its terminal velocity yet. Assuming a velocity law  $v_{\text{O}} = v_{\text{O}\infty}(1 - R_{\text{O}}/r)^{\beta}$  with  $\beta \simeq 0.8$  (Puls et al. 1996), the O star wind can be as low as  $v_{\text{O}} \simeq 2070\ \text{km s}^{-1}$  at the wind collision at periastron, which can yield an effective  $\eta_{\text{max}} \lesssim 70$ .

However, this close to the O star, radiative breaking by radiation pressure of its photons on the WR wind could strongly slow the latter down. This locally decreases the momentum flux ratio of the winds (Gayley et al. 1997). According to the orbital and wind parameters of  $\gamma^2\ \text{Vel}$ , radiative breaking is necessary to allow for a wind collision region, otherwise the shocked region would crash onto the stellar surface. Based on models of X-ray spectroscopy, Henley et al. (2005) suggest a shock opening half angle of  $\simeq 85^\circ$  close to the apex of the shock. While the value of the opening angle is still debated (see e.g. Rauw et al. 2000), radiative breaking will largely increase  $\eta_{\text{min}}$ . As our simulations do not include radiative breaking, we set the winds of both stars to their terminal velocity.

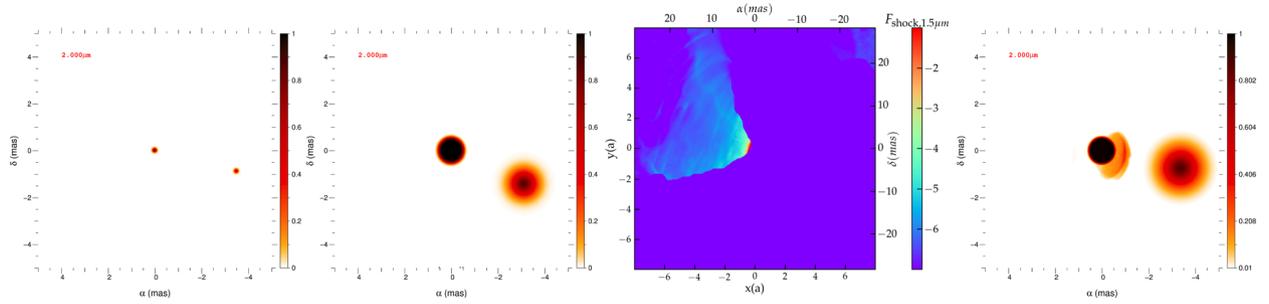
We have performed two simulations with  $\eta = 26$  and 36 and find that the difference in the hydrodynamic structure cannot be

distinguished when comparing our model data with observations. As such, we use the  $\eta = 26$  results for the remainder of this paper. While smaller or larger values of  $\eta$  are plausible, the values we tested represented the most realistic range given the current data. Our simulation does not model clumps in the winds, which are likely destroyed in the WCZ (Pittard 2007).

## 4.2 Hydrodynamic structure

The density, velocity and temperature maps are shown in Fig. 9 for orbital phase  $\phi = 0.3$ , i.e. when the binary is roughly in the plane of the sky, which is close to the 2004 observation. The results of these maps are compatible with the maps presented in Henley et al. (2005), which focused on the inner region of the binary. The density map shows both shocks (also seen on the velocity and temperature maps) and the contact discontinuity at the interface between both shocked winds. Due to the lower density, the O star wind is less subject to radiative cooling and has a temperature of more than  $10^8\ \text{K}$  at the apex of the shock. The WR wind on the other hand rapidly cools down to below  $10^6\ \text{K}$  beyond the apex of the shocked region. The temperature in our model agrees well with *Chandra* measurements of triplet-lines, associated with  $4 \times 10^6\ \text{K}$  gas at roughly twice the binary separation (Skinner et al. 2001). While both winds are highly supersonic before the shocks, their velocity is almost zero in the shocked region close to the apex. Further out in the shocked region, the winds progressively reaccelerate.

The first and third columns of Fig. 10 show a volume rendering of the 3D structure of the interaction region. It shows the logarithm



**Figure 11.** Model continuum emission at  $\phi = 0.3$  at  $2.0 \mu\text{m}$ . From right to left: model two point sources, geometrical model with an extended Gaussian disc (WR star) and uniform disc (O star), emission from the WCZ, total image with stellar discs and the WCZ. Images 1, 2 and 4 represent the square root of the intensity, while the third one represents the log of the flux. The flux has been renormalized to the maximal flux in all images.

of density at the outer edge of the shocked region, projected on the plane of the sky at the observed phases. Within  $\approx 5$  times the binary separation, the orbital motion of the binary has limited impact on the WCZ structure, which keeps its conical structure with symmetric arms, albeit off-centred with respect to the binary axis (Parkin & Pittard 2008). Further out, the spiral structure becomes apparent. Its step depends on the velocity of both stellar winds as well as the orbital velocities (Lamberts et al. 2012) and varies throughout the orbit. Around periastron (between  $\phi = 0.75$  and  $\phi = 0.1$ ), when the orbital velocity is highest, more than a quarter of a step of the spiral is present within the simulated region and we see the shocked structure wrap around itself.

The shocked region can be subject to various hydrodynamic instabilities. They are responsible for the wobbly aspect of the shocked region in the volume rendering in Fig. 10. The velocity difference between the winds leads to the development of the Kelvin–Helmholtz instability. As the velocity gradient at the interface is small, the growth of the instability remains small and the instability is linear (Lamberts et al. 2011). As energy is radiated away from the shocked region, the shocked shell gets narrower, and may be distorted by the thin-shell instability (Vishniac 1994). Because cooling is limited in  $\gamma^2$  Vel, the development of this instability is limited. Performing a simulation without orbital motion, we find that instabilities only change the total flux in the shocked region by at most 5 per cent on time-scales of a tenth of the orbital period.

## 5 MODEL DATA

In this section, we compute model flux maps of  $\gamma^2$  Vel at different observed wavelengths. We use the hydrodynamic simulation to determine the emission from the wind collision region and use the extended disc models described in Section 3.1 for the stars. We then use the resulting images to compute model visibility curves and closure phases with FITOMATIC and go beyond the geometrical point-source model from Paper I (see Section 3). We then compare the resulting continuum visibility curves with the observed ones and estimate the emission from the WCZ.

Based on our hydrodynamic model, we can estimate the IR continuum emission of the WCZ. The bremsstrahlung (free–free) emissivity at frequency  $\nu$  (in  $\text{erg s}^{-1} \text{cm}^{-3} \text{Hz}^{-1}$ ) is given by

$$\epsilon_{\nu}^b \simeq 6.81 \times 10^{-38} Z^2 n_e n_i g_b T^{-1/2} e^{-h\nu/k_B T}, \quad (5)$$

where  $Z$  is the average ionic charge,  $n_e$  and  $n_i$  the number density of electrons and ions respectively,  $g_b$  the Gaunt factor set to unity and  $h$  and  $k_B$  the Planck and Boltzmann constants, respectively.

We use the density and temperature provided by the hydrodynamic simulation to model the free–free emission from the winds.

Thanks to the passive scalar, we can discriminate between the shocked O star and WR wind and take into account their distinct chemical compositions. The emitted flux is given by adding up the contributions of  $\epsilon_{\nu}^b$  from both shocked region. We account for free–free absorption along the line of sight to the observer, using the absorption coefficient

$$\kappa_{\nu}^b \simeq 3.7 \times 10^8 Z^2 n_e n_i g_b T^{-1/2} \nu^{-3} (1 - e^{-h\nu/k_B T}) \quad (\text{cm}^{-1}). \quad (6)$$

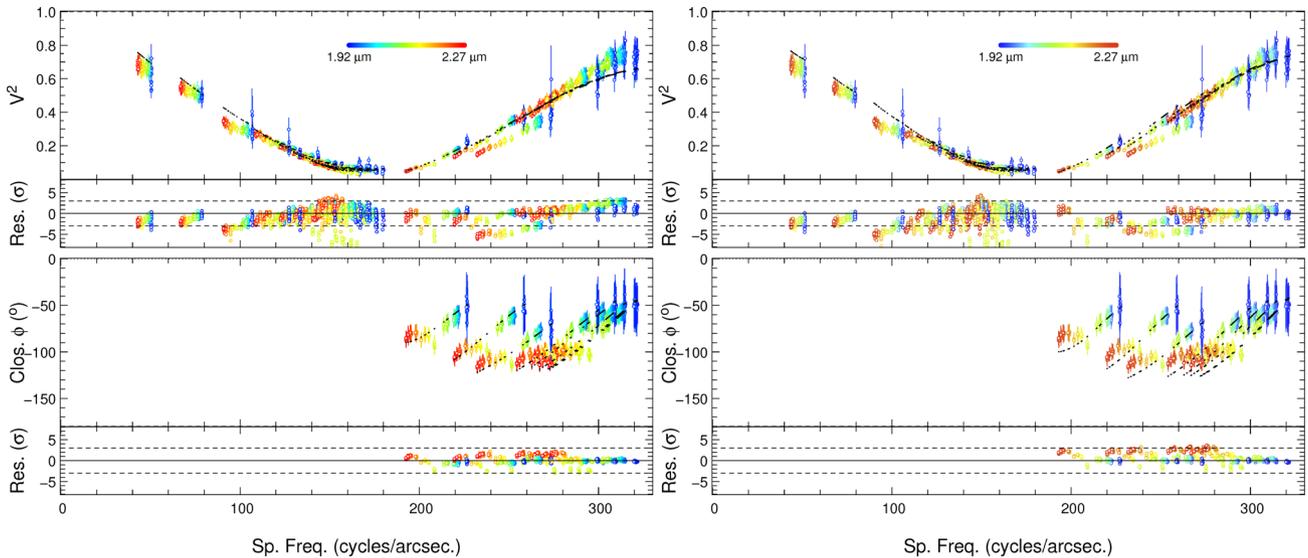
Fig. 11 shows the build-up of the final model image when the binary is in the plane of the sky ( $\phi = 0.3$ , close to the 2004 observation). The first and second images respectively show the images with the point sources and stellar discs described in Section 3.1. The third image shows only the emission of the shocked regions, which we identify using density and pressure criteria. The emission is very concentrated at the apex of the shock, due to the high temperature and density. The final image is the complete composite image.

The second and last columns of Fig. 10 show the total flux along the line of sight at  $2.0 \mu\text{m}$  along the orbit using our complete model. On the left of each image is the volume rendering of the WCZ to guide the analysis of the model images. At all phases, the emission of the WCZ is highly concentrated at the apex of the shock, folded over the O star. Its flux rapidly drops beyond a distance of roughly 1 mas. The impact of the shocked region on the final images is modulated by the angular separation between the stars and the orientation of the shock cone with respect to the line of sight.

When the stars are at minimal projected separation ( $\phi \simeq 0.01$ ), the highest emission of the WCZ is spatially coincident with, and outweighed by the emission of the stars. When the stars are further apart (large angular separation, e.g. around  $\phi = 0.32, 0.82$ ), the WCZ becomes more apparent, and distorts the spherically symmetric nature of the emission of the wind emission. In these cases, the total received flux is set by the orientation and shape of the WCZ. When the orbital plane is close to the plane of the sky, the shock cone is seen nearly edge on (e.g.  $\phi = 0.32, 0.82, 0.92$ ). As a result, the column density is very high near the apex of the shock, resulting in a small region of high flux. When we are seeing the shock cone more face-on (e.g.  $\phi = 0.51, 0.66$ ), the column density of shocked material is lower, and we see a more extended region with lower flux.

Around periastron, our composite images show an *apparent* crash of the wind collision region on the O star ( $\phi = 0.92$ ). As we will detail in the discussion (Section 6), this is because the stellar radii turn out to be larger than expected. At such close distance to the stars, radiative braking from the O star is expected to push away the interaction region, preventing a crash.

Comparing a full hydrodynamic model coupled with simplified radiative transfer with interferometric data is a daunting task. At



**Figure 12.** Continuum visibilities and closure phases from our high-fidelity observing campaign (night of 2008 December 22) with the geometrical model (left) and the complete model (right) superposed in black. The colours show the wavelength dependence.

this point, our model does not include the line formation regions that would require to couple the hydrodynamics with a non-LTE radiative transfer model such as *CFMGEN*. Fig. 12 shows visibility curves and closure phases of  $\gamma^2$  Vel at  $\phi = 0.88$  (2008 December 22) based on our complete model (right). The left-hand panel shows the model with resolved stellar discs (see Section 3.1). The addition of the extended emission from the WCZ results in an improved squared visibility at the highest and lowest frequencies compared to the model with only the resolved stars with the side-effect of a slightly less good agreement for the closure phases. Especially at highest cycle per arcsec, the complete model shows better visual agreement with the data. In this model, the WCZ accounts for a total flux fraction between 3 and 10 per cent of the total flux.

## 6 DISCUSSION

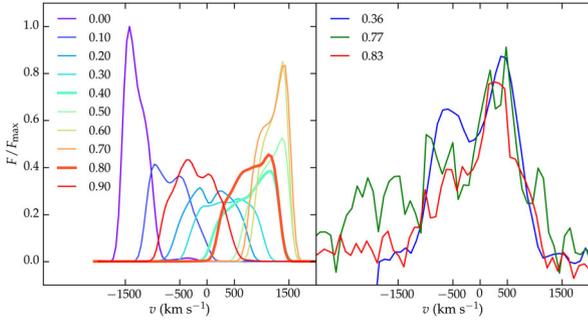
In the former section, we analysed the spectro-interferometric AMBER data creating model observables to compare with, based on a complete hydrodynamic model of the WCZ. The high spatial resolution achieved with interferometry is necessary to resolve the binary separation. Previous interferometric observations in the optical continuum (Hanbury Brown et al. 1970; North et al. 2007) have determined the orbital parameters of the binary. However, the stellar wind from the WR star and the WCZ benefit from observations at longer wavelengths due to their thermal free-free emission. Using AMBER data at one orbital phase, in Paper I we showed that an extended emission component of at most 5 per cent of the total flux was necessary to match the observed absolute visibilities. This additional component was tentatively attributed to the WCZ.

In this paper, the presence of the WCZ is more firmly established and its flux contribution to the continuum is estimated to be 3 per cent from the  $2\ \mu\text{m}$  continuum observations. While this is a very small contribution, its strongly asymmetric and phase-dependent nature produces detectable variations in the interferometric signal. In order to go beyond the initial results from Paper I, the hydrodynamic simulation was necessary to create model images. It reveals a complex density, velocity and temperature structure. Due to the inclination of the system and its eccentricity, the aspect of the spiral changes drastically throughout the orbit and wraps around itself

around periastron. All of this contributes to the final observables and would not have been accounted for with analytic models. As the current data set does not allow for complete reconstruction of the image [as in Weigelt et al. (2016) for  $\eta$  Carinae], one has to construct a model for the system and compare its observables with the data. While the model we propose has a strong physical motivations, a unique solution for the system’s emission cannot be formally identified with the continuum data.

Beside the continuum study, we have presented the first model independent spectral separation of the WR and O star component in the near-infrared. While the WR spectrum can be reproduced with well-established models, we fail to explain the second component spectrum with any O star model alone. From the hydrodynamic simulation, we confirm that the latter is contaminated by the emission/absorption in WCZ, which also gives a likely explanation of its variability. A full analysis of the line profiles, which are influenced by the geometry, density and temperature of the WCZ can ultimately determine the stellar wind parameters (Henley et al. 2005). According to the analysis of the ‘O star spectrum’, we expect the WCZ line emission to account for as much as 20 per cent of the O star flux. As such, a similar analysis with the line emission would allow us to strongly constrain the emission properties (size and flux) of the WCZ.

A complete analysis of the line emission would require a radiative transfer model for the whole system, which is clearly beyond the scope of this paper. We can have a foretaste of the result of such work by computing the flux-weighted line-of-sight velocity histograms of the WCZ from the hydrodynamic simulations, as is shown in Fig. 13. While this histogram only models the WCZ contribution to the line profiles, it shows that strong line variability is expected throughout the orbit, reminiscent of the observed variability in the O star spectrum. According to the orientation of the WCZ along the orbit (see the 3D structure in Fig. 10), the line profile may vary from fully blueshifted to fully redshifted emission, including a flat-top phase. Similar trends were found by Ignace et al. (2009) in forbidden line profiles based on a geometrical model of the WCZ. Unfortunately, our orbital coverage is too sparse to fully observe this phenomenon in the obtained spectra. Still, we find that our simulations predict higher velocities than observed in the emission lines. On top of this,



**Figure 13.** Left: Smoothed histogram of the flux-weighted line-of-sight velocity of the WCZ at different phases (colour coding shown on the plot). The phases closest to the observed phases have thicker lines. Right: Observed O star spectrum for the  $\lambda 2.11 \mu\text{m}$  He I blended line.

the WCZ, with its  $10^6$ – $10^8$  K temperature and enhanced density is also an additional photon source. As such, it may affect the ionization state and line emission in the free WR and O winds, possibly leading to the variability in the He II absorption profile in Fig. 7. While these aspects are currently speculative, combining a fully hydrodynamic model with a complete radiative transfer model to compute the line profiles in spectro-interferometric data, while arduous, is clearly the way forward to fully exploit the next generation of instruments.

Our data analysis yields stellar radii in the  $K$  band which are about twice as large as estimated with optical interferometric data in North et al. (2007) and predicted from spectral analysis and based on theoretical models for the stellar evolution and atmospheres De Marco & Schmutz (e.g. 1999). The latter still present important uncertainties, in particular for the hottest, biggest and most massive stars. This is partially related to the rarity of these objects due to a combination of the initial mass function and short lifetime. The evolution of massive stars is highly sensitive to mass-loss and rotation, the latter being very poorly constrained (Maeder & Meynet 2000). These uncertainties are enhanced by binarity, which is likely to have affected the evolution of  $\gamma^2$  Vel (Eldridge 2009). Possible alternate explanations for the scale resolved emission is the presence of an additional emission component in the system such as fall-back shocked material. Similarly to the WCZ, the latter will decrease the angular size of the stars needed to fit the model. While this explanation is highly speculative, it highlights the difficulty to understand these rare hot, massive and large stars.

A side-effect of the larger-than-expected stellar radii is that the WCZ appears to crash onto the O star photosphere around periastron. In our simulations, we have assumed instantaneous wind acceleration and did not directly model radiative effects such as the radiative braking of the WR wind expected at periastron. According to Gayley et al. (1997) and Rauw et al. (2000), the latter is expected to be important in  $\gamma^2$  Vel and will push the WCZ away from the O star and yield a stable shocked structure. In our simulation, we assumed immediate wind acceleration, which actually overestimates the opening angle of the WCZ at periastron, somewhat counterbalancing the lack of radiative braking. As such, we do not expect the resulting WCZ to be qualitatively different from the WCZ in our hydrodynamic simulations. Simulations of  $\eta$  Carinae including radiative effects show a widened shock opening angle and also an increased development of instabilities (Parkin et al. 2011). As the development of instabilities is limited in  $\gamma^2$  Vel, the latter should not impact our comparison with the interferometric data.

## 7 CONCLUSIONS

In this paper, we have studied the colliding wind region in  $\gamma^2$  Vel combining near-infrared spectro-interferometric data from AMBER/VLTI with a 3D hydrodynamic model.

As our data provides good coverage of the orbital period, we confirm the orbital parameters from North et al. (2007). At phases where higher spectral resolution is available, we are able to separate the composite spectrum in a WR component and a component with and around the O star. Using CFMGEN, a model for radiative transfer in expanding stellar atmospheres, we confirm the WC 8 spectral type and wind parameters of the WR star compatible with De Marco et al. (2000). We fail to satisfactory match the O star component with the spectrum of an O star alone, both with theoretical models and template spectra from other O-type stars. We interpret this as a signature of strong contamination by the WCZ, as was suggested in Paper I. This is supported by the phase-locked line profile variability in the spectrum. Additional evidence comes from the hydrodynamic simulation showing the wind collision region shrouding the O star.

The 3D hydrodynamic simulation includes orbital motion of the binary and covers 16 times the binary separation, a physical extension never modelled before for this system. It reveals the spiral nature of the WCZ, particularly marked around periastron. Based on the hydrodynamic variables in the simulation, we determine the free-free emission in the wind collision region. We combine it with a model for the extended emission of the stars to produce model emission maps at different wavelengths. We find that most of the emission in the WCZ is concentrated at the apex of the shocked region, around the O star. Depending on the projected angular separation of the stars and the orientation of the shocked region, the WCZ has more or less impact on the final flux map. We use these model images to derive interferometric observables. Our model, where the WCZ contributes 5 per cent to the continuum emission, is in good agreement with the observed data. This constraint on the WCZ in  $\gamma^2$  Vel with spectro-interferometric observations demonstrates how the hydrodynamic models enhance the scientific output of the data.

To improve our understanding of this emblematic system, there are clear paths forward, both on the observational and theoretical side:

(i) Updated, and especially more precise, radial velocity measurements would allow one to reach a sub-percent accuracy on the distance of  $\gamma^2$  Vel. Having such an accuracy on the distance of this system would be extremely interesting, as it could become a calibrator probe for *GAIA* distances to binaries.

(ii) Medium-spectral resolution interferometric data are needed at many more orbital phases (here the spectroscopic analysis focused on only two phases) to better characterize the system. Better spatial resolution is needed to resolve the stars themselves, i.e. reach longer baselines and/or shorter wavelengths. This may be achieved with *GRAVITY*, or with a future visible interferometric instrument at the VLTI. While the object might be too poorly resolved for full imaging on the VLTI, *GRAVITY*, thanks to its six baselines and its fringe tracker, will provide much more accurate data for modelling, and might open the possibility to evaluate to measure accurately the spectrum of different parts of the WCZ.

(iii) A line analysis of the WCZ would then require to couple the hydrodynamic simulation presented in this paper together with a non-LTE radiative transfer code similar as *CFMGEN*.

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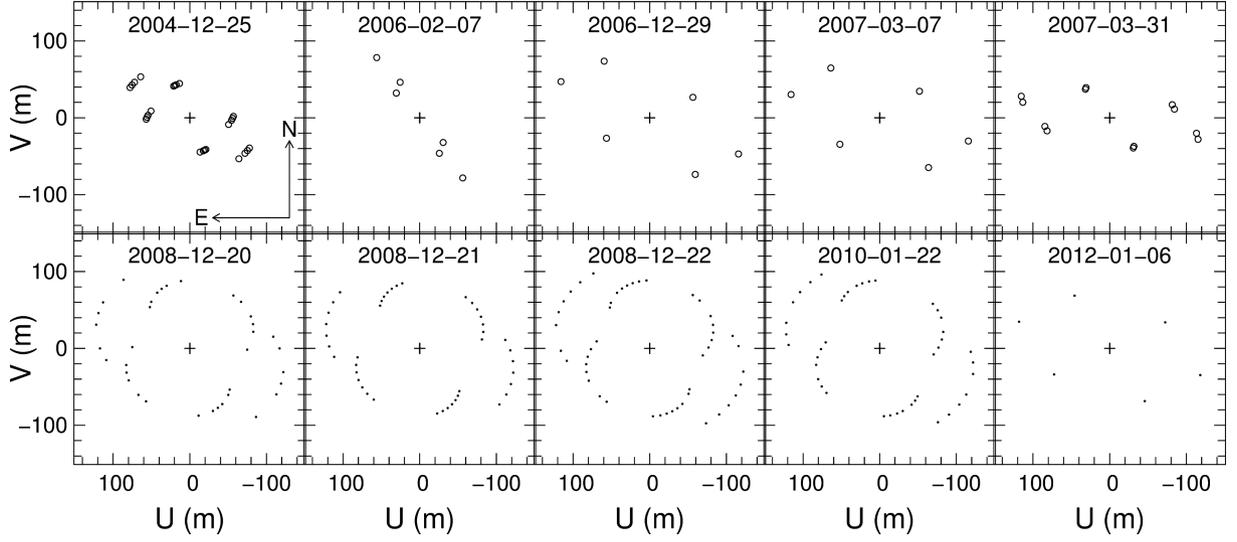
## APPENDIX A: DATA ANALYSIS

A1 ( $u, v$ ) coverage

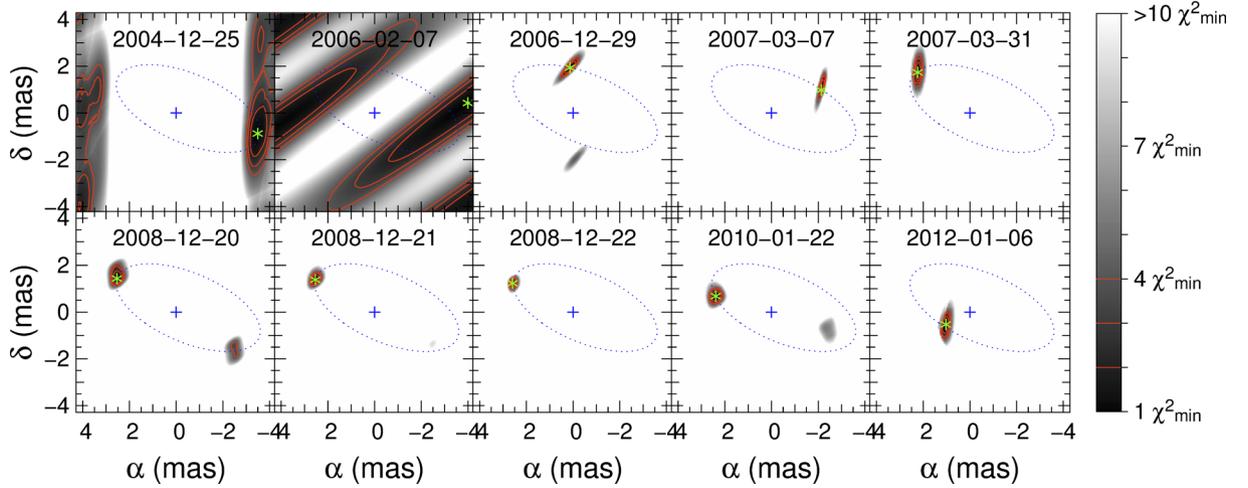
Fig. A1 shows the ( $u, v$ ) plane coverage of our observations.

A2  $\chi^2$  maps and astrometry

Fig. A2 shows the  $\chi^2$  maps of our model along the orbit. There is a unique solution for most of our data sets except from 2006 for the reasons explained in the main body of the text. The resulting astrometric measurements are provided in Table A1.



**Figure A1.**  $(u, v)$  plane of the observations for each epoch. Note that the North is up and the East is left, as if the  $(u, v)$  coordinates were seen on the plane of the sky. The circles represent the UTs, the dots represent the ATs.



**Figure A2.**  $\chi^2$  maps for our binary star model positions for each epoch of observation, showing the orbital motion of the system. The green asterisks show the best-match position to our data, while the red contours are the 1, 2 and 3 $\sigma$  error contours.

**Table A1.** Astrometric measurements of  $\gamma^2$  Vel.  $\Delta\alpha$  and  $\Delta\delta$  represent the angular separation in right ascension and declination, respectively, in mas.  $\sigma_{\text{major axis}}$  and  $\sigma_{\text{minor axis}}$  are the uncertainties on  $\Delta\alpha$  and  $\Delta\delta$ , respectively, represented by the sigma of a Gaussian tilted by the angle  $\theta_{\sigma_{\text{major axis}}}$ .<sup>a</sup>

Date	$\Delta\alpha$	$\Delta\delta$	$\sigma_{\text{major axis}}$	$\sigma_{\text{minor axis}}$	$\theta_{\sigma_{\text{major axis}}}$
2004 December 25	-3.48	-0.87	0.31	0.10	-8.5
2006 February 7	-3.93	0.39	3.11	0.35	126.5
2006 December 29	0.14	1.92	0.24	0.06	-40.8
2007 March 7	-2.15	1.07	0.27	0.05	-193.4
2007 March 31	2.24	1.73	0.19	0.06	176.3
2008 December 20	2.52	1.44	0.07	0.04	179.2
2008 December 21	2.54	1.39	0.04	0.03	-29.7
2008 December 22	2.57	1.26	0.03	0.02	-16.7
2010 January 22	2.37	0.67	0.04	0.04	-19.4
2012 January 6	1.05	-0.52	0.24	0.08	172.2

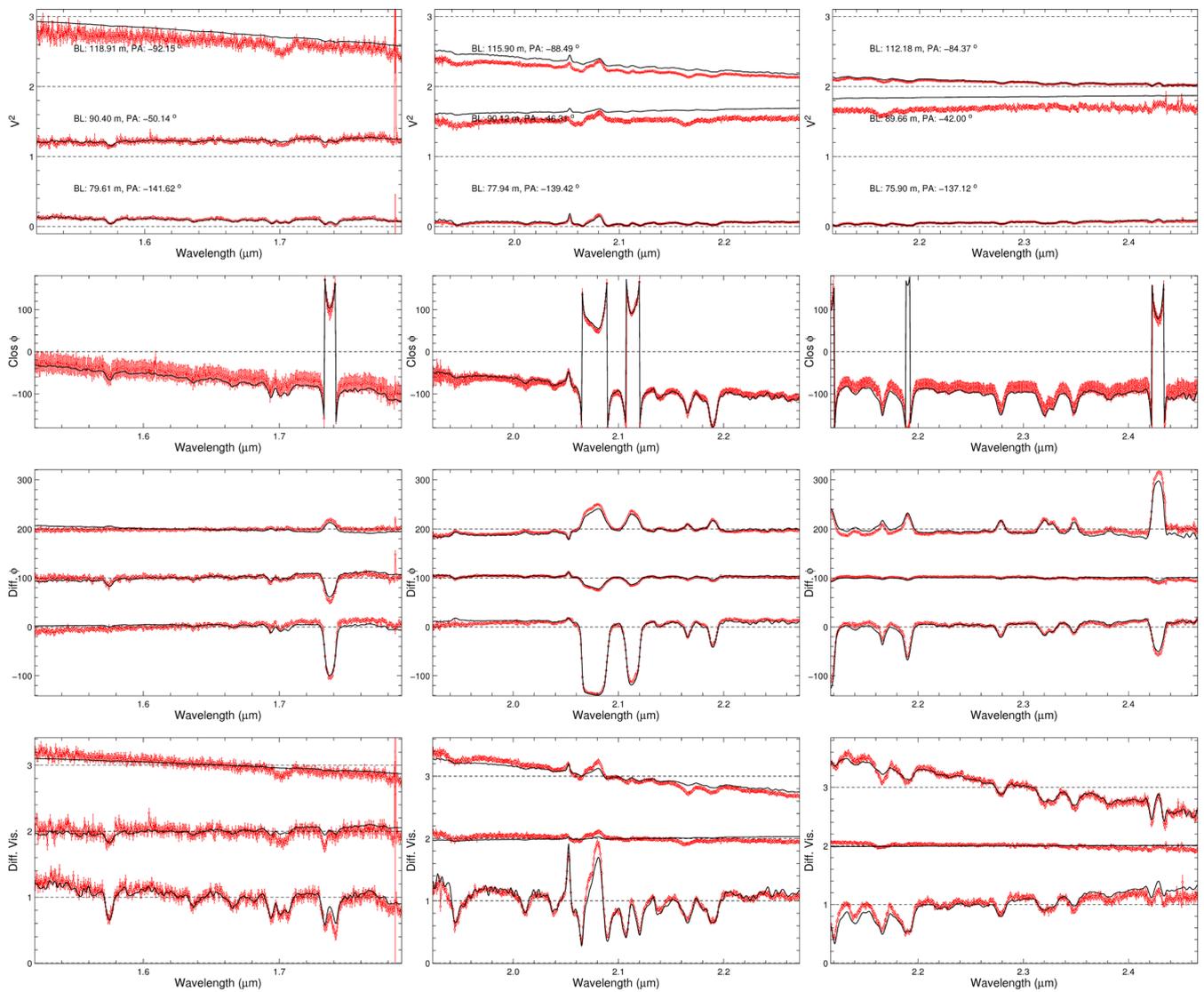
*Note.* <sup>a</sup> $\sigma_{\text{major axis}}$  and  $\sigma_{\text{minor axis}}$  have been normalized by the square root of the number of observations.

### A3 Model fitting in the lines

In Fig. A3, we show a sub-sample of our 2008 and 2010 observations (red lines), together with the best-fitting two point sources model (black). As the  $H$ -band 2010 data set was obtained at a similar orbital phase as the 2008 data sets, we selected similar baselines so that the visibilities, closure phases, differential phases and differential visibilities can be compared directly.

### A4 Line identification

Table A2 provides the lines identified in the WR and O star spectrum.



**Figure A3.** Illustration of the AMBER data as well as the model-fitting process used on the emission lines to extract the spectra of the WR star and the O star. The observed data are in red, while the best-fitting two point sources model is plotted in black. From top to bottom: Squared visibilities, closure phases, differential phases and differential visibilities. We selected similar baselines for the three nights. Left: Night of 2010 January 22. Middle: Night of 2008 December 22. Right: Night of 2008 December 21.

**Table A2.** Line list for *H*- and *K*-band spectra. Line identification made use of the NIST data base (Kramida et al. 2015) and Varricatt et al. (2004). ‘?’ denotes tentative identifications.

WR star		O star	
$\lambda$ ( $\mu\text{m}$ )	Line	$\lambda$ ( $\mu\text{m}$ )	Line
1.4764	He II 9–6	1.4764	He II 9–6
1.4885	He II 14–7	1.5022	N V
1.491	C IV	1.5188	N V / He I
1.5088	He I	1.5310	He I
1.5723	He II 13–7	1.5399	N V
1.588	He I	1.5723	He II 13–7
1.641	He I	1.5885	H I 14–4
1.664	C IV	1.6114	H I 13–4
1.6922	He II 12–7	1.619	N II?
1.7007	He I	1.6411	H I 12–4
1.7359	He II 20–8	1.6811	H I 11–4
1.736/737	C IV	1.6922	He II 12–7
1.801	C IV	1.7007	He I
		1.7367	H I 10–4
		1.7521	N III?
		1.7838/858/860	C II
1.9442	He II 16–8	1.9442	He I
1.9548	He I	1.9451	H I 8–4
2.012	C IV	2.0587	He I
2.0378	He II 15–8	2.0705/796/842	C IV
2.0587	He I	2.1126	He I
2.0705/796/842	C IV	2.1138	He I
2.1061	C IV	2.1614	He I
2.1081	C III	2.1651	He II 14–8
2.1126	He I	2.1661	H I 7–4
2.139	C III	2.1890	He II 10–7
2.1651	He II 14–8	2.2929	O III?
2.1890	He II 10–7	2.3234/47	C III?
2.278	C IV	2.3469	He II 13–8
2.3234/247/265	C III	2.4219–4318	C IV
2.3270	C IV	2.4460	He I
2.3469	He II 13–8		
2.4219–4318	C IV		

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