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1 Contribution of topographically-generated submesoscale 2 turbulence to Southern Ocean overturning

3 Xiaozhou Ruan¹, Andrew F. Thompson¹, Mar M. Flexas¹ & Janet Sprintall²

4 ¹*Environmental Science & Engineering, California Institute of Technology*

5 ²*Scripps Institution of Oceanography, University of California, San Diego*

6 Supplementary material

7 1. Estimates for water mass transformation rates:

8 The water mass transformation rate can be expressed, following Marshall et al. (1999), using a
9 diapycnal velocity $\tilde{\mathbf{e}}$, as

$$T = - \int \int_A \tilde{\mathbf{e}} \cdot \mathbf{n}_b dA = \int \int_A \frac{\nabla \cdot \mathbf{F}_b}{|\nabla b|} dA. \quad (1)$$

10 Here $b = -g(\rho - \rho_0)/\rho_0$ is the buoyancy and ρ_0 is a reference density, A is the area of a buoy-
11 ancy surface across which the diapycnal transport is measured, \mathbf{n}_b is the unit vector normal to the
12 isopycnal and \mathbf{F}_b is the turbulent buoyancy flux. It has been argued that the vertical buoyancy flux
13 scales with the dissipation rate as $\Gamma\epsilon$, where Γ is the mixing efficiency (Osborn 1980). Thus, the
14 buoyancy flux divergence can be estimated as $\Gamma\epsilon/h$ where h is the thickness of the bottom mixed
15 layer (BML); this assumes that the buoyancy flux vanishes at the solid bottom. Using a mixing
16 efficiency $\Gamma = 0.2$, a typical bottom mixed layer thickness $h = 100$ m and a local vertical stratifi-
17 cation $N^2 = \frac{\partial b}{\partial z} = 10^{-6} \text{ s}^{-2}$, the diapycnal velocity can be estimated as $2 \times 10^{-4} \text{ m s}^{-1}$, or ~ 20 m
18 day^{-1} . Considering a 5 km-wide boundary current (associated with the southern boundary of the

19 ACC) that flows along the continental slope for a distance of 500 km in southern Drake Passage
20 (Fig. S4; Orsi *et al.* 1995), A is $2.5 \times 10^9 \text{ m}^2$. Using equation (5), this yields a local water mass
21 transformation rate of 0.5 Sv. We acknowledge that the mixing efficiency, Γ , is uncertain in this
22 area, nevertheless, this likely remains an underestimate since only the shear-induced mechanism is
23 accounted for here.

24 The use of the vertical buoyancy gradient N^2 assumes that the diapycnal mixing and asso-
25 ciated water mass modification is a local, one-dimensional (vertical) process, which relies on the
26 rapid export of modified water into the interior. McDougall and Ferrari (2017) hypothesize that
27 water masses may be modified and upwell in boundary layers over sloping topography. In this
28 case, N^2 should be replaced by the lateral buoyancy gradient across the continental slope. Esti-
29 mating this value across multiple glider sections gives a value of roughly $5 \times 10^{-8} \text{ s}^{-2}$ (Fig. 1c).
30 This smaller buoyancy gradient suggests a local diapycnal velocity 20 times larger than the pre-
31 vious estimate using the vertical buoyancy gradient. We note that the lateral buoyancy gradient is
32 a more challenging quantity to estimate, especially if the incropping of density surfaces is hetero-
33 geneous along the slope (see, for instance, Fig. 4 in Thompson and Heywood, 2008). Now we
34 estimate the area of relevant buoyancy surfaces A within the BML using the BML thickness of 100
35 m and a longitudinal distance of 500 km along Southern Drake Passage which yields $A = 5 \times 10^7$
36 m^2 . The water mass transformation rate can be thus estimated to be 0.2 Sv. It is important to
37 note that, according to the hypothesis, the excessive (upwelling) diapycnal volume flux along the
38 bottom boundary layers has to be largely compensated by diapycnal downwelling in the stratified
39 mixed layers globally. While the estimates above are associated with some uncertainty, they are

40 sufficiently large to warrant further investigation.

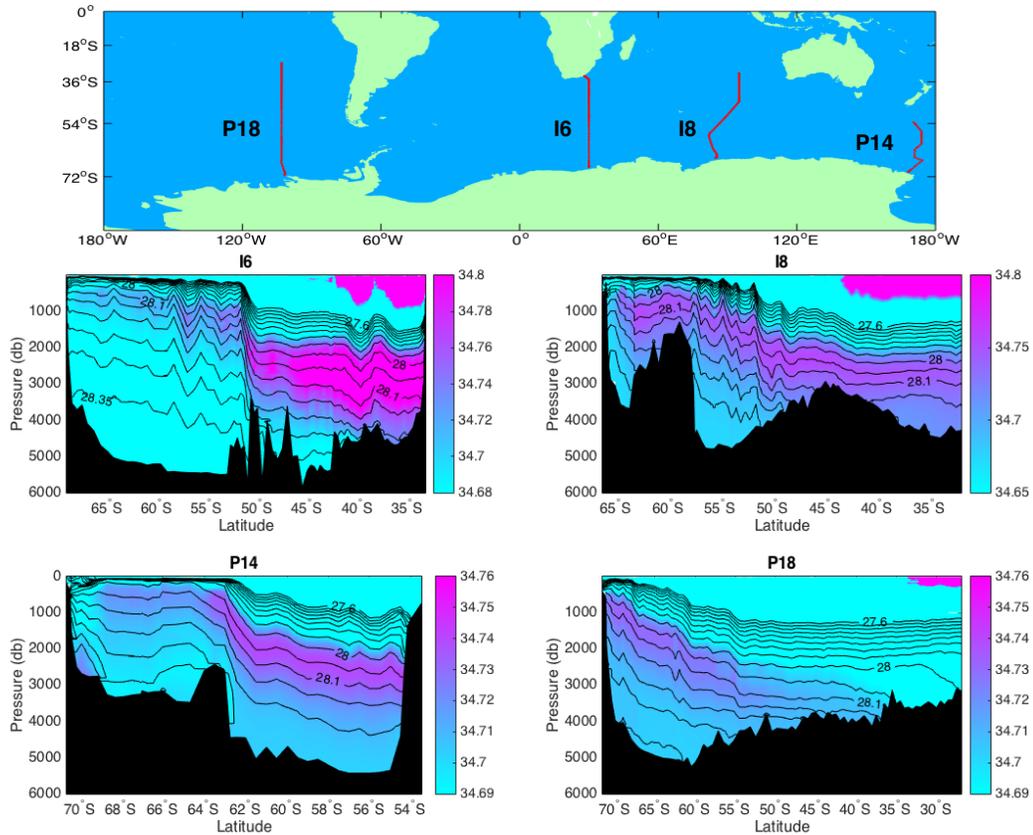
41 2. Extrapolation to the circumpolar Southern Ocean using numerical model output:

42 In order to estimate the circumpolar relevance of the proposed mechanism, we turn to output from
43 a high-resolution global numerical model to examine the interactions between ACC fronts and
44 major topographic features in the Southern Ocean.

45 LLC4320 is a global ocean and sea ice simulation that represents full-depth ocean processes.
46 The simulation is based on a Latitude/Longitude/polar-Cap (LLC) configuration of the MIT gen-
47 eral circulation model (MITgcm; Marshall *et al.* 1997; Hill *et al.* 2007). The LLC grid has 13
48 square tiles with 4320 grid points on each side (hereafter called LLC4320) and 90 vertical levels
49 for a total grid count of 2:21010. Horizontal grid spacing ranges from 0.75 km near Antarctica
50 to 2.2 km at the Equator and vertical levels have 1-m thickness near the surface to better resolve
51 the diurnal cycle. The simulation is initialized from a data-constrained global ocean and sea ice
52 solution provided by the Estimating the Circulation and Climate of the Ocean, Phase II (ECCO2)
53 project (Menemenlis *et al.* 2005, 2008; Losch *et al.* 2010), and includes atmospheric pressure and
54 tidal forcing (Menemenlis *et al.* 2014). The inclusion of tides allows for successful reproduction of
55 shelf-slope dynamics and water mass modification (Flexas *et al.* 2015). Surface boundary condi-
56 tions are from the European Center for Medium-Range Weather Forecasts (ECMWF) atmospheric
57 operational model analysis, starting in 2011. The sections shown in Figure S4 correspond to a
58 snapshot of LLC4320 on 29/11/2011.

59 Assuming that there are strong interactions between deep-reaching ACC currents and sloping

60 bottom topography near the Kerguelen Plateau, Campbell Plateau, Drake Passage and ridges and
61 fracture zones in the South Pacific and Atlantic, as seen in Figure S4, then a conservative estimate
62 for A in equation (5) would be $2.5 \times 10^{10} \text{ m}^2$ (an average of 5km-wide narrow front is assumed).
63 This area estimation would yield a global transformation of LCDW of 5 Sv for the local vertical
64 process. For the along-bottom diapycnal upwelling framework, we estimate the area A to be
65 $5 \times 10^8 \text{ m}^2$ which yields a transformation rate of 2 Sv (with the possible compensating downwelling
66 neglected).



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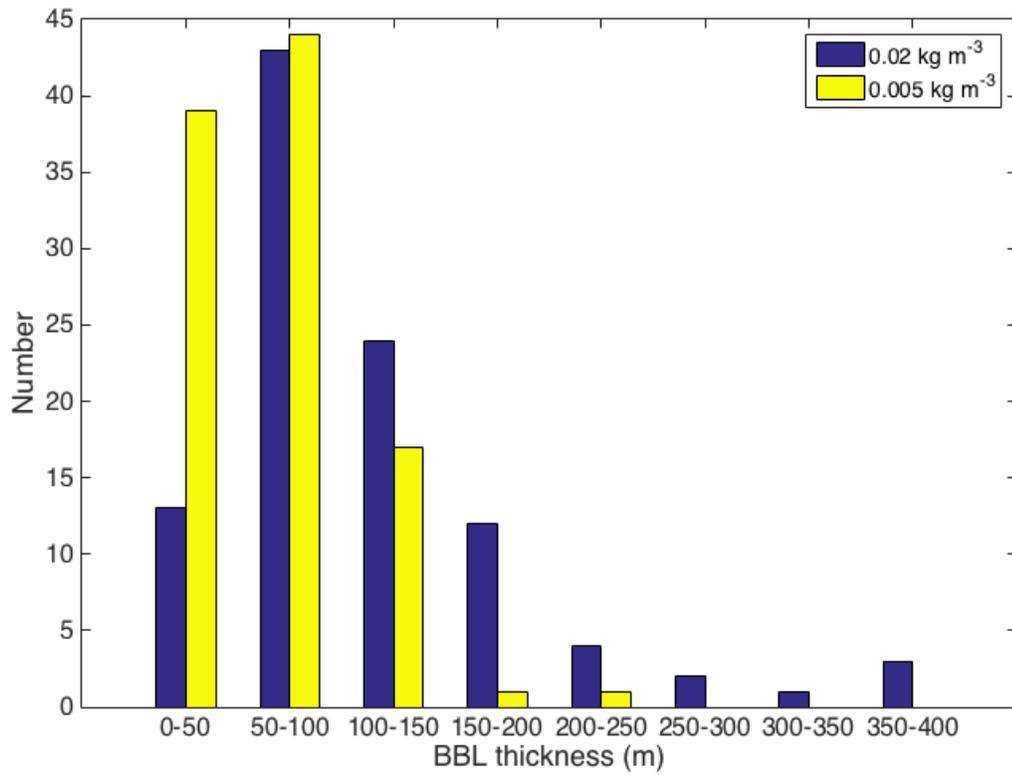
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Figure S1: Salinity distributions from WOCE transects (summer measurements) I6, I8, P14 and P18 (Orsi and Whitworth 2005). The purple colors highlight that Lower Circumpolar Deep Water (characterized by a salinity maximum) incrops on the Antarctic continental slope and deeper topographic features broadly around Antarctica. Neutral density surfaces are indicated as black contours.



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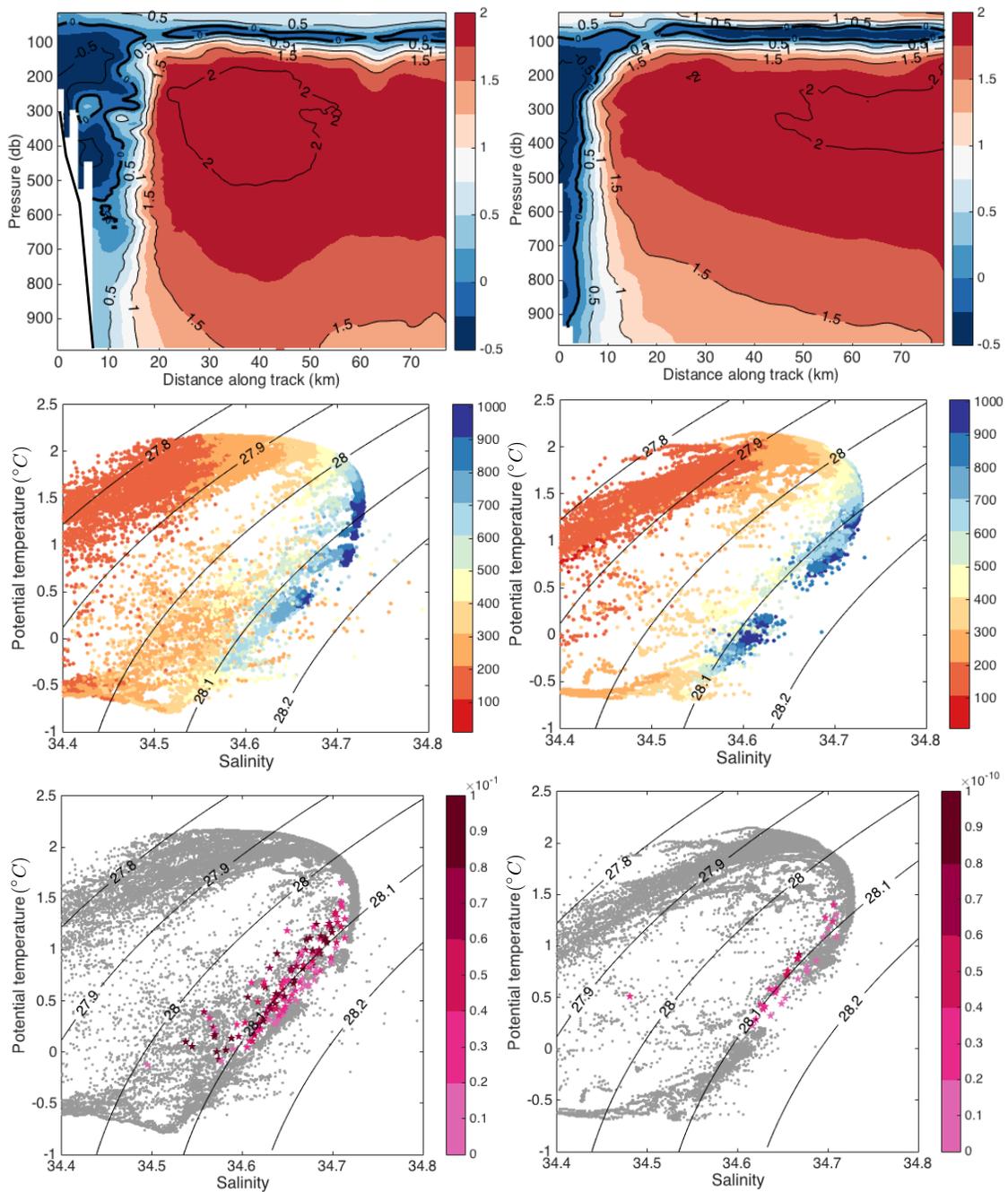
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Figure S2: Statistics of bottom mixed layer (BML) thickness (m) based on a $\Delta 0.02 \text{ kg m}^{-3}$

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threshold (blue) and a $\Delta 0.005 \text{ kg m}^{-3}$ threshold (yellow).



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Figure S3: Two transect examples of CDW being close to (left panels; Transect 5) and away

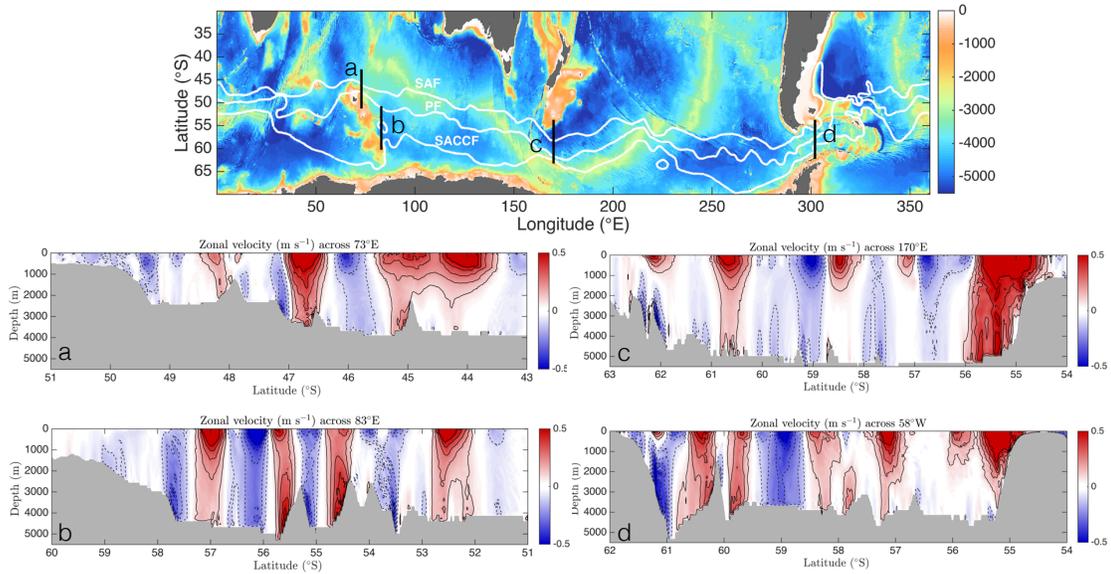
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from (right panels; Transect 8) the slope. (Upper panels) Potential temperature sections.

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Isothermals are labeled every 0.5°C. The 2°C contour roughly defines the location of the

81 Bdy. The 0°C isotherm (in bold black) marks the front separating warm CDW from cold
82 shelf water. (Middle panels) Θ/S diagram of glider data colored by depth (in meters). (Lower
83 panels) Positive Ertel PV (in magenta) over all data sampled for each given transect (in gray).



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Figure S4: Zonal velocity snapshots across topographic features in the Southern Ocean from a high-resolution numerical model (See model introduction in Supplementary Material). Transects a, b, c and d correspond to Northern and Southern Kerguelen Plateau, Campbell Plateau (including the Macquarie Ridge) and Drake Passage. White contours in the upper panel are the climatological frontal positions in the Southern Ocean (Orsi *et al.* 1995) and black straight lines correspond to the transects from which zonal velocity snapshots are shown below. Black contours in the lower four panels are zonal velocities (eastward, positive, solid lines). Contour levels are from 0.1m/s to 0.5m/s with a 0.1m/s interval. Deep-reaching fast boundary currents (some with bottom velocity intensification) interacting with sloping topography can be seen widely in the Southern Ocean across the chosen major topographic features.

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