The California-Kepler Survey. V. Peas in a Pod: Planets in a *Kepler* Multi-planet System Are Similar in Size and Regularly Spaced*

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Abstract

We have established precise planet radii, semimajor axes, incident stellar fluxes, and stellar masses for 909 planets in 355 multi-planet systems discovered by *Kepler*. In this sample, we find that planets within a single multi-planet system have correlated sizes: each planet is more likely to be the size of its neighbor than a size drawn at random from the distribution of observed planet sizes. In systems with three or more planets, the planets tend to have a regular spacing: the orbital period ratios of adjacent pairs of planets are correlated. Furthermore, the orbital period ratios are smaller in systems with smaller planets, suggesting that the patterns in planet sizes and spacing are linked through formation and/or subsequent orbital dynamics. Yet, we find that essentially no planets have orbital period ratios smaller than 1.2, regardless of planet size. Using empirical mass–radius relationships, we estimate the mutual Hill separations of planet pairs. We find that 93% of the planet pairs are at least 10 mutual Hill radii apart, and that a spacing of ~ 20 mutual Hill radii is most common. We also find that when comparing planet sizes, the outer planet is larger in $65\% \pm 0.4\%$ of cases, and the typical ratio of the outer to inner planet size is positively correlated with the temperature difference between the planets. This could be the result of photo-evaporation.

Key words: catalogs – planetary systems – stars: fundamental parameters – surveys

Supporting material: machine-readable table

1. Introduction

Multi-planet systems provide a fossil record of the physics that drive planet formation. The *Kepler* Mission (Borucki et al. 2010) has enabled detailed statistics of hundreds of coplanar multi-planet systems (Latham et al. 2011; Lissauer et al. 2011, 2012; Fabrycky et al. 2014; Lissauer et al. 2014; Rowe et al. 2014). In the *Kepler* multi-planet systems, multiple planets transit the star, resulting in measured orbital periods and planet-to-star radius ratios for each transiting planet. The observed and statistically inferred orbital properties in multi-planet systems have been used to deduce possible planet formation histories (Fang & Margot 2012; Hansen & Murray 2013; Malhotra 2015; Pu & Wu 2015; Steffen & Hwang 2015; Ballard & Johnson 2016; Xie et al. 2016).

Until recently, the stellar properties in the population of *Kepler* multi-planet systems were poorly understood. The majority of these stars had only photometric characterization via the *Kepler* Input Catalog (KIC; Brown et al. 2011). The

uncertainties inherent in broad passband stellar characterization resulted in uncertainties of 16% in the stellar masses and 42% in the stellar radii, on average (Mullally et al. 2015; Johnson et al. 2017).

With the goal of clarifying the stellar and planetary properties of *Kepler*’s multi-planet systems, the California-*Kepler* Survey (CKS) determined precise stellar and planetary properties for 355 *Kepler* multi-planet systems containing 909 transiting planets. Petigura et al. (2017, CKS I) presented the host star spectra and their observational properties effective temperature (T_{eff}), surface gravity ($\log g$), metallicity ($[\text{Fe}/\text{H}]$), and projected stellar rotation velocity ($v \sin i$). These observed quantities were converted to physical stellar parameters stellar mass (M_*), stellar radius (R_*), and age using stellar evolutionary models (Johnson et al. 2017, CKS II). The improved stellar characterization results in a median uncertainty of 5% in the stellar mass and 10% in the stellar radius.

With improved stellar parameters, it is possible to improve the characterization of planets as well. In CKS II, the updated stellar parameters were used to compute planetary radii (R_p), semimajor axes (a), and equilibrium temperatures (T_{eq}) for the planets orbiting these stars. The improved stellar and planetary parameters enable a more accurate and precise characterization of the multi-planet systems than was previously available.

In this paper, we examine several properties of *Kepler*’s multi-planet systems that are clarified by the improved stellar

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parameters. In Section 2, we describe how the multi-planet systems analyzed herein were selected. In Section 3, we show that the planetary sizes are related within multi-planet systems. In Section 4, we show that the period ratios between adjacent planets are related within multi-planet systems. In Section 5, we explore the relation between these patterns and search for underlying physics. In particular, we show that planet size and planet spacing are correlated. Using the updated planet radii and semimajor axes, we employ empirical mass–radius relationships to compute the pairwise mutual Hill separations for the multis. We also explore a correlation between the ratio of planet sizes and their equilibrium temperatures. We conclude in Section 6.

2. The Sample

The initial set of CKS systems with multiple transiting planet candidates consists of 469 stars with at least two transit-like signals and a total of 1215 transit-like signals that were at one time flagged as *Kepler* Objects of Interest (KOIs). From these, we discarded the known false positives, removing 59 non-planetary signals as determined in CKS I. We then discarded stars that were diluted by at least 5% by a second star in the *Kepler* aperture (as determined in the stellar companion catalog of Furlan et al. 2017), removing 30 stars hosting 69 planet candidates. We discarded planets for which Mullally et al. (2015) measured $b > 0.9$, for which the high impact parameters adversely affected our ability to determine accurate planet radii, removing 75 planet candidates. We removed planets for which the measured signal-to-noise ratio (SNR) was less than 10, as these planets have poorly determined radii and impact parameters, removing 48 planet candidates.¹⁴ Finally, we discarded systems that have been reduced to one valid planet candidate (55 systems). After these cuts, our sample of “CKS multis” contained 909 high-purity planet candidates, which we henceforth call planets, in 355 multi-planet systems.

Figure 1 shows the architectures of CKS systems with at least four transiting planets. Each row corresponds to one planetary system. The systems are ordered by stellar mass, which is listed to the right of each system. We identify several architectural features by eye, which merit further investigation: (1) the size of one planet in a system is a good predictor of the sizes of other planets in the same system, (2) the spacing between a pair of planets in a system is a good predictor of the spacing of additional planets in that same system, (3) the smallest planets have the closest spacings, (4) when planets are not the same sizes, the outer planets are usually larger. Below, we quantitatively investigate these observations.

3. Planets in the Same System have Similar Sizes

Is the size of one planet in a given system a good predictor of the size of the next planet? To test this, we measured the correlation between the size of a planet, R_j , and the size of the next planet in the system, R_{j+1} , in order of increasing orbital period. To avoid detection-based asymmetries in the distribution, we only included pairs that were detectable with signal-to-noise ratio (S/N) > 10 when their orbital positions were swapped. The expected S/N of a planet with size R_p and orbital period P orbiting a star with bulk density ρ_* , radius R_* , and 6 hr

Figure 1. Architectures of CKS multis with at least four transiting planets. Each row corresponds to one planetary system (name on y-axis) and shows the planet semimajor axes (x-axis; note the log scale). The point sizes correspond to the planet radii, and the point colors correspond to the equilibrium temperatures (see key to the right). The systems are ordered by stellar mass, which is listed to the right of each system. The inner solar system is included for comparison.

Combined Differential Photometric Precision ($\text{CDPP}_{6 \text{ hr}}$, a measure of the stellar photometric noise over 6 hr; Christiansen et al. 2012) is

$$\text{SNR} = \frac{(R_p/R_*)^2 \sqrt{3.5 \text{ yr}/P}}{\text{CDPP}_{6 \text{ hr}} \sqrt{6 \text{ hr}/T}} \quad (1)$$

¹⁴ We also tried a more conservative cutoff of $S/N > 20$, which did not change the results.

Figure 2. The radius of a planet, R_j , vs. the radius of the next planet out, R_{j+1} , in the CKS multi-planet systems. There is a large and significant correlation (Pearson- $R = 0.62$, $p < 10^{-5}$) between the size of a planet and its neighbor. Although the outer planet radius is correlated with the inner planet radius, $65.4\% \pm 0.4\%$ of the points sit above the $y = x$ line. Uncertainties in the stellar radii lead to an 11% uncertainty in the position of each point along the $y = x$ axis; uncertainties in transit depths lead to a $\sqrt{2} \times 4\%$ uncertainty in the position of each point along the $y = -x$ axis (see orange cross).

$$T = 13 \text{ hr} (P/1\text{yr})^{1/3} (\rho_*/\rho_\odot)^{-1/3}. \quad (2)$$

If the smaller planet, when placed at the larger orbital period, produced $S/N > 10$, the planets were included in our sample of adjacent pairs. Of the 554 original pairs of planets, 504 passed the swapping criterion. We then tested whether a correlation was present in these pairs of planets.

Using the Pearson- R correlation test, we find that there is a large ($r = 0.65$) and significant ($p < 10^{-5}$) correlation between the sizes of adjacent planets (Figure 2). A planet in a multi-planet system is likely to be the size of its neighbor.

A correlation in adjacent planet sizes can arise from either astrophysics or from detection biases. One might imagine that the correlation is driven by the tail end of small planets ($R_p < 1 R_\oplus$). Planets of this size are only detectable around $\sim 10\%$ of the stars in our sample (~ 30 stars), and the smaller planets are even less detectable. If we restrict our sample to planets with $R_p > 1 R_\oplus$, the Pearson- R correlation has $r = 0.53$ and $p < 10^{-5}$, meaning that the correlation between the sizes of adjacent planets larger than $1.0 R_\oplus$ is still strong and significant. Furthermore, although planets smaller than $1.0 R_\oplus$ would be hard to detect around other stars, it would be easy to detect larger transiting planets in the same systems, if they existed.

To further examine the role of detection biases in shaping the observed correlation, we conducted a series of bootstrap tests. The null hypothesis underlying our bootstrap tests is that drawing each planet radius at random, with no regard for which star the planet originally orbited or which other planets were orbiting the star, and then subjecting this sample to the detection biases of *Kepler* can produce a correlation between R_j and R_{j+1} . The procedure was as follows:

Figure 3. The radius distribution of the 909 planets in the CKS multis. The Fulton Gap at $2 R_\oplus$ is visible (Fulton et al. 2017). Note that planets larger than $4 R_\oplus$ constitute only 7.8% of the distribution, and planets larger than $8 R_\oplus$ account for just 2.4% of the distribution. The majority of the patterns presented herein are driven by the sub-Neptune-sized planets, not giant planets. Planets were drawn at random, with replacement, from this distribution to construct bootstrap trials investigating planet radii like the one shown in Figure 4.

1. Construct a bootstrap trial by drawing planet radii at random, *with replacement*, from the distribution of observed planet radii¹⁵ around all of the CKS multis (see Figure 3). Note that this procedure has no regard for which star the planet originally orbited. Note also that this procedure does not assume any relation between R_j and R_{j+1} .
2. For each real CKS multi-planet host star, draw the number of planet radii equal to the number of transiting planets detected around that star, and place the planets at the observed orbital periods for that star.
3. Check that for each pair of planets, the smaller planet is detectable ($S/N > 10$) when placed at the longer orbital period. Discard any undetectable pairs.
4. Compute the Pearson- R correlation between the detectable pairs of R_j and R_{j+1} . An example bootstrap result is shown in Figure 4.
5. Repeat 1000 times for each star, recording the Pearson- R value and p -value of each trial (Figure 5).

Figure 4 shows one example of a bootstrap trial and the resulting correlation. The low Pearson- R value and near-unity p -value demonstrate a lack of correlation between adjacent planet sizes in this trial. These values are typical of our 1000 trials, which are summarized in Figure 5. Our bootstrap tests were unable to reproduce the correlation between R_j and R_{j+1} pairs observed in real multi-planet systems.

For example, the upper right corner of Figures 2 and 4—pairs of large planets, which are readily detectable—differ. In the observed distribution, there are many pairs of large planets near (8, 8). However, the bootstrap rarely realizes such pairs. This is because only 7.8% of the planets have $R_p > 4 R_\oplus$, and so drawing two such planets from the distribution in a row is unlikely ($0.078^2 = 0.006$). In the hypothesis underlying the bootstrap trials (each planet does not know about its neighbor), it is much more likely to draw a pair of planets with sizes of (2, 8) or (8, 2), as planets of $2 R_\oplus$ are very common.

The discrepancy between the observed and bootstrap-generated planet pairs indicates that a null hypothesis influenced by detection biases cannot generate the observed

¹⁵ We also tried drawing radii from a log-normal distribution, with no appreciable difference in the results.

Figure 4. The radius of a planet, R_j , vs. the radius of the next planet out, R_{j+1} , in one of 100 bootstrap trials of the CKS multis (see the text). The bootstrap-generated distributions do not resemble the correlation between the sizes of adjacent planets in the CKS multis in Figure 2.

Figure 5. Left: the Pearson-R correlation between R_j and R_{j+1} in the observed distribution of CKS multis (orange line), as compared to the 1000 bootstrap trials drawn from the entire sample of 909 planets in the CKS multis (blue histogram). Right: the p -value of the Pearson-R correlation between R_j and R_{j+1} in the observed distribution of CKS multis (orange dotted line, upper limit), as compared to the 1000 bootstrap trials (blue histogram). The bootstrap trials do not exhibit the correlation between the inner and outer radii, demonstrating that the correlation is likely due to astrophysics, not detection biases.

correlation. Therefore, the correlation between the sizes of adjacent planets is likely driven by astrophysics.

To quantitatively compare the real and bootstrap distributions, we collapsed the two-dimensional (2D) distributions into one dimension by computing R_{j+1}/R_j for each pair. Figure 6 compares the observed and bootstrap-constructed distributions for the pairs of planet radii. Using an Anderson–Darling test,

Figure 6. The ratios of planet sizes for adjacent pairs within the same system (black line) compared to a control sample of detection-limited bootstrap trials (blue line). In both the observed and the bootstrap distributions, pairs are only counted if the smaller planet in the pair is detectable at the longer orbital period. The p -value of an Anderson–Darling test comparing the observed vs. bootstrap distributions of planet radius ratios is $<10^{-5}$; with a confidence of $>99.9999\%$, we can rule out the hypothesis that these two populations come from the same underlying distribution. The distribution of observed planet radius ratios is significantly more peaked at 1.0 than the bootstrap distribution, indicating that planets in the same system are preferentially the same sizes.

we find a p -value of $<10^{-5}$, allowing us to conclude with $>99.9999\%$ confidence that the observed pairs of planet radii are not drawn from the same distribution as the bootstrap-generated pairs of planet radii. The observed distribution has a much sharper peak at a planet size ratio of 1.0 than the bootstrap distribution, meaning that planets in multi-planet systems are more likely to be similarly sized to each other than what we would expect drawing their sizes at random. In the observed CKS multis, the distribution of R_{j+1}/R_j has a mean value of 1.29, a median of 1.14, and a standard deviation of 0.63.

The work presented here builds on previous studies of *Kepler* multi-planet systems. Lissauer et al. (2011) also found that planets in multi-planet systems tend to be the same size, but with a much smaller sample of planets in multi-planet systems, resulting in only 71 independent, detectability-corrected ratios. Our work repeats their experiment but with 504 independent, detectability-corrected ratios.

4. Planets in the Same System have Similar Spacings

In Figure 1, the planets appear evenly spaced in log semimajor axis. Because $\log(A) - \log(B) = \log(A/B)$, constant differential log-spacing corresponds to a constant spacing ratio.

Within each observed system of three or more planets, we tested whether the orbital period ratio of adjacent planets, P_{j+1}/P_j , was correlated with the orbital period ratio of the next pair of planets out, P_{j+2}/P_{j+1} . As *Kepler* observed for a finite amount of time, finding planets out to about 1000 days at most, our sensitivity to large ratios of orbital periods is incomplete. If we find an example of $P_{j+1}/P_j = 10$, it is extremely unlikely that we would also be able to detect $P_{j+2}/P_{j+1} = 10$ in the same system, although a third planet might be detectable at $P_{j+2}/P_{j+1} = 2$. Therefore, we limited our study to planet pairs with period ratios smaller than 4 (i.e., somewhat compact planetary systems; this number is justified in Section 5.1). These selection criteria resulted in 373 planets (165 pairs) around 104 stars. The resulting orbital period ratios are shown in Figure 7.

In each group of three planets in a row, there is an apparent correlation between the orbital period ratio of the inner and

Figure 7. In systems with three or more planets, the orbital period ratio of the outer periods vs. the orbital period ratio of the inner planets. There is a large and statistically significant correlation (Pearson-R = 0.46, $p < 10^{-5}$) between the orbital period ratios of the inner and outer planets.

outer pairs of planets. We computed a Pearson-R correlation of 0.46, with a significance of $p < 10^{-5}$, which indicates that there is a strong, significant correlation between the orbital period ratios of planets in the same system.

As above, we used a bootstrap analysis to test whether the observed correlation in adjacent orbital periods could arise from detection biases. The null hypothesis we formulated was that the orbital period ratio between one pair of planets was not, a priori, related to the orbital period ratio of the next pair of planets in the same system. Our procedure for constructing the bootstrap trials was as follows:

1. Construct a bootstrap trial by drawing each orbital period ratio at random, *with replacement*, from the distribution of observed orbital period ratios smaller than 4 (Figure 8). Note that this procedure has no regard, a priori, for which star the planet pair originally orbited, or what the orbital period ratios among other planets in the system might be.
2. For each real CKS multi-planet host star, draw the number of orbital period ratios equal to the number of transiting planets observed around that star, minus one.
3. To map the orbital period ratios to orbital periods, draw an orbital period P_1 at random, *with replacement*, from the observed distribution of orbital periods of the innermost transiting planet in each system.
4. Multiply the orbital period P_1 by the first drawn orbital period ratio to get the second orbital period, P_2 . Repeat (replacing P_1 with P_2 , etc.) until each planet has been assigned an orbital period.
5. Remove any planets with orbital periods greater than 1071 days (the maximum observed orbital period of a planet in the CKS multis).
6. Remove any planets that are not detectable (i.e., $S/N \leq 10$) at their randomly assigned orbital periods.
7. Among the remaining (detectable) planets in the bootstrap trial, compute the orbital period ratios for each adjacent pair of planets.

Figure 8. The distribution of the orbital period ratios of adjacent planets in the CKS multis. As *Kepler* observed for a finite amount of time, we are more sensitive to patterns in which the orbital period ratios of the planets are small. (A large orbital period ratio necessitates at least one long orbital period.) Therefore, we limited our study to orbital period ratios smaller than 4 (dotted vertical line).

Figure 9. The orbital period ratio of adjacent planets vs. the orbital period ratio of the next pair of adjacent planets in one of 1000 bootstrap trials of the CKS multis with 3 or more transiting planets (see the text). The lack of correlation between the spacings of adjacent planet pairs in the bootstrap trial is different from the strong correlation in the distribution of observed orbital period ratios (Figure 7).

8. Compute the Pearson-R correlation between each inner (P_{j+1}/P_j) and outer (P_{j+2}/P_{j+1}) orbital period ratio, in systems that retain three or more detectable planets. Figure 9 shows one example.
9. Repeat 1000 times, recording the Pearson-R and p -value of each bootstrap trial (Figure 10).

Figure 9 shows one example of a bootstrap trial and the resulting correlation. The low Pearson-R value and near-unity p -value demonstrate a lack of correlation between the orbital period ratios of adjacent pairs of planets in this trial. These values are typical of our 1000 trials, which are summarized in Figure 10. Our bootstrap tests were unable to reproduce the distribution of P_{j+1}/P_j and P_{j+2}/P_{j+1} pairs observed in real multi-planet systems, indicating that detection biases alone cannot generate the observed correlation. Therefore, the correlation between the spacings of adjacent pairs of planets is likely driven by astrophysics.

Figure 10. Left: the Pearson-R correlation between the inner (P_{j+1}/P_j) and outer (P_{j+2}/P_{j+1}) period ratios in the observed distribution of CKS multis with three or more planets (orange line), as compared to the 1000 bootstrap trials (blue histogram). Right: the p -value of the Pearson-R correlation between the period ratios in the observed distribution of CKS multis (orange dotted line, upper limit), as compared to the 1000 bootstrap trials (blue histogram). The bootstrap trials do not reproduce the significance of the observed correlation, demonstrating that the correlation is likely due to astrophysics, not detection biases.

To quantitatively compare the real and bootstrap distributions, we collapsed the 2D distributions into one dimension by computing $\mathcal{P} = (P_{j+2}/P_{j+1})/(P_{j+1}/P_j)$ for each pair. Figure 11 compares the observed and bootstrap-constructed distributions for the pairs of planet radii. Using an Anderson–Darling test, we find a p -value of 0.0012, allowing us to conclude with 99.9% confidence that the observed pairs of planet radii are not drawn from the same distribution as the bootstrap-generated pairs of planet radii. The observed distribution has a sharper peak at a ratio of ratios of orbital periods of 1.0 than the bootstrap distribution, meaning that planets in multi-planet systems are more likely to have correlated spacings than what we would expect drawing their orbital period ratios at random. The lower significance of this correlation than for the correlation between adjacent planet sizes likely stems from the smaller number of pairs (165) than were available for the study of adjacent planet radii (504), as comparing orbital period ratios requires at least three planets in a system. In the observed CKS systems of three or more planets, the distribution of $\mathcal{P}$ has a mean value of 1.03, a median of 1.00, and a standard deviation of 0.27.

Malhotra (2015) and Steffen & Hwang (2015) have also characterized the period ratio distributions of the *Kepler* multis. Malhotra (2015) noted that the distribution of planet spacings, $\mathcal{D} = 2^{(a_2 - a_1)/(a_1 + a_2)}$, is approximately log-normal. Our result differs from theirs in that we explored how the orbital spacing between one pair of planets and the next pair in the same system are correlated. Steffen & Hwang (2015) also examined the relationships between the period ratios of adjacent pairs of planets, but only for those in which one pair (or the product of the pairs) was near 2.2.

Figure 11. The ratio of orbital period ratios for each adjacent triple of planets within the same multi-planet system (black line) compared to a control sample of detection-limited bootstrap trials (blue line). In both the observed and the bootstrap distributions, pairs are only counted if the smaller planet in the pair is detectable at the longer orbital period. The p -value of an Anderson–Darling test comparing the observed vs. bootstrap distributions of planet radius ratios is 0.0013; with a confidence of >99%, we can rule out the hypothesis that these two populations come from the same underlying distribution. The distribution of observed ratios of orbital period ratios is significantly more peaked at 1.0 than the bootstrap distribution, indicating that planets in the same system have a preferred spacing.

Figure 12. The average planet size in an adjacent pair (R_p avg) vs. the orbital period ratio of the pair, for the CKS multis. There is a slight positive correlation (Pearson-R = 0.26, p -value $< 10^{-5}$) between the average planet size and the orbital period ratio. The relationship is strongest at small period ratios.

5. Physical Underpinnings

How do planets know to be the same size? How do they know how far apart to form? Below, we explore the relationship between planet size and spacing and estimate the planet spacings in terms of mutual Hill radii. We also examine how stellar incident flux relates to planet size ratios.

5.1. The Relation between Planet Size and Spacing

In Figure 1, the systems with the smallest planets appear to have the closest spacings, and the systems with larger planets appear to have larger spacings. Extending this observation to the full sample of CKS multis, we find a correlation between

the sizes of planets and their orbital period ratios (Figure 12). There is a statistically significant positive correlation ($r = 0.26$, $p < 10^{-5}$) between the orbital period ratio and average planet size in a pair. The correlation is particularly visible for $P_{j+1}/P_j < 4$, over which range the planet size increases with increasing orbital period ratio.

Two features in Figure 12 draw the eye. There is a striking wall at $P_{j+1}/P_j = 1.2$: essentially no planets are closer together than this. The wall spans an order of magnitude in planet size, extending from the smallest planets ($R_p \approx 0.5 R_\oplus$) to Neptune-sized planets. Also, there is an absence of small planets at large orbital period ratios.

We investigated whether some artifact of the *Kepler* pipeline for multi-planet systems could produce the wall at $P_{j+1}/P_j = 1.2$. According to Tenenbaum et al. (2013), the procedure for investigating a light curve in which one transiting planet candidate has already been found is as follows: “The transit signatures from the fitted planet model are removed from the flux time series; and the residual flux time series is then searched for additional TCEs.” There is no mention of any period filtering that would exclude planets that are closer together than a period ratio of 1.2. Furthermore, planets that have a period ratio of 1.2 (or even 1.1) but are initially overlapping in transits quickly become out of phase, and so after a few orbits the transits occur in different places in the light curve. Hence, we do not identify any aspect of the *Kepler* pipeline that would produce the wall at a period ratio of 1.2.

The period ratio boundary at 1.2 was predicted by Deck et al. (2013), who used numerical integrations and analytical calculations to demonstrate that when planets get closer together than $\frac{a_2 - a_1}{a_1} < 1.46(\mu_1 + \mu_2)^{2/7}$ (where μ is the planet-to-star mass ratio), they are very likely to stumble into a resonance overlap of two or more first-order mean motion resonances, leading to dynamical chaos and eventual Lagrange instability. Even though low-mass planets might be Hill stable in these configurations, their entanglement in resonance overlap is fatal for stability. For planets of $M_p/M_\star \approx 10^{-5}$, i.e., roughly $3 M_\oplus$, with low eccentricities ($e < 0.04$), the typical minimum Lagrange-stable separation corresponds to a period ratio of about 1.2 (Deck et al. 2013, Figure 12). Although some planets can survive closer than this separation if they fall in an island of stability,¹⁶ there are very few planets for which this appears to be relevant.¹⁷

We investigated the absence of small planets at large orbital period ratios. The smallest planets ($R_p < 1 R_\oplus$) are the closest to each other, with typical orbital period ratios from 1.2 to 2.0. These sub-Earths orbit 22 stars, and so the clustering of all these planets at small orbital period ratios is not a coincidence derived from a small number of systems with compact architectures. Among the sub-Earths alone (45 pairs), the Pearson-R coefficient is 0.44, with $p = 0.002$.

Is the correlation between orbital period ratio and planet size astrophysical? We used the bootstrap method of Section 4 to test how moving the small planets to a variety of orbital separations would affect their detectability. Although planets smaller than $1 R_\oplus$ are detectable around their parent stars at $P_{j+1}/P_j \sim 4$ (Figure 13), no such planets have been found. None of the 1000 bootstrap trials generated a correlation with larger Pearson-R or smaller p -value than the observed

Figure 13. The average planet size in an adjacent pair (R_p avg) vs. the orbital period ratio of the pair in one bootstrap realization. There is no correlation between the average planet size and the orbital period ratio. The smallest planets ($R_p < 1 R_\oplus$) are detected at orbital period ratios of 4, in this example, demonstrating that the structure in the lower left of Figure 12 is not sculpted by detection biases.

distribution. Thus, the lack of small planets at orbital period ratios of ~ 4 in our sample is probably not solely based on detection bias, as we could have found such planets. Therefore, the clustering of small planets at very close orbital period ratios in Figure 12 is very likely sculpted by astrophysics.

5.2. Planets are 20 Mutual Hill Radii Apart

One astrophysical interpretation that links planet sizes and spacing is the idea that planets communicate with their neighbors through gravitational interactions. We therefore considered the separation between a pair of planets in terms of their gravitational influence, of which the mutual Hill radius is the natural unit. The mutual Hill radius of two planets of masses m_j and m_{j+1} orbiting a star of mass $M_\star$ at semimajor axes a_j and a_{j+1} is

$$R_H = \left(\frac{m_j + m_{j+1}}{3 M_\star} \right)^{1/3} \frac{(a_j + a_{j+1})}{2} \quad (3)$$

and the separation between two planets, in units of mutual Hill radii, is

$$\Delta = (a_{j+1} - a_j)/R_H \quad (4)$$

(Gladman 1993).

It is useful to note that Δ is related to but not directly proportional to the orbital period ratio, $\mathcal{P} \equiv P_{j+1}/P_j$. Using *Kepler*’s third law to rewrite Equations (3) and (4) in terms of orbital periods, we have

$$\Delta = 2 \left(\frac{m_j + m_{j+1}}{3 M_\star} \right)^{-1/3} \left(\frac{\mathcal{P}^{2/3} - 1}{\mathcal{P}^{2/3} + 1} \right). \quad (5)$$

As the period ratios we are considering tend to be small (~ 1 to 4), subtracting one in the numerator and adding one in the denominator significantly alters the fraction, making Δ distinct

¹⁶ Based on serendipitous initial relative mean anomalies.

¹⁷ Kepler-36 is one such exception and was scrutinized in Deck et al. (2013).

Table 1
CKS Multis Properties

Star	KOI	Kepler Name	M_* ($M_\odot$)	R_* ($R_\odot$)	CDPP _{6 hr}	b	Period (days)	R_p ($R_\oplus$)	σR_p ($R_\oplus$)	T_{eq} (K)	R_p avg. ($R_\oplus$)	P_{j+1}/P_j	Δ_{RH}
K00041	K00041.02	Kepler-100 b	1.107	1.55	23.33	0.51	6.88	1.35	0.23	1186	0.0	0.0	0.0
K00041	K00041.03	Kepler-100 d	1.107	1.55	23.33	0.59	35.33	1.54	0.31	687	1.95	2.75	31.23
K00041	K00041.01	Kepler-100 c	1.107	1.55	23.33	0.58	12.81	2.37	0.34	965	1.86	1.86	20.15
K00046	K00046.01	Kepler-101 b	1.156	1.58	54.61	0.03	3.48	5.69	0.73	1443	0.0	0.0	0.0
K00046	K00046.02	Kepler-101 c	1.156	1.58	54.61	0.41	6.02	1.18	0.16	1203	3.43	1.72	12.91

Note. R_p avg., P_{j+1}/P_j , and Δ_{RH} are parameters that relate a pair of adjacent planets. In this table, each value is listed with the *outer* planet of the pair.

(This table is available in its entirety in machine-readable form.)

from the period ratio, especially for the smallest planets, which all have $P_{j+1}/P_j < 2$.

To compute planet separations in mutual Hill radii, it is necessary to adopt planet masses. We converted our precise planet radii to estimates of planet masses (M_p) and densities (ρ_p) via the empirical mass–radius relationships of Weiss & Marcy (2014) and Weiss et al. (2013):

$$\begin{aligned}
 R_p/R_\oplus < 1.5: \\
 \rho_p &= 2.43 + 3.39(R_p/R_\oplus) \text{ g cm}^{-3} \\
 M_p &= (\rho_p/5.51 \text{ g cm}^{-3})(R_p/R_\oplus)^3 M_\oplus
 \end{aligned} \tag{6}$$

$$\begin{aligned}
 1.5 \leq R_p/R_\oplus \leq 4.0: \\
 M_p &= 2.69(R_p/R_\oplus)^{0.93} M_\oplus
 \end{aligned} \tag{7}$$

$$\begin{aligned}
 4.0 < R_p/R_\oplus < 9.0: \\
 M_p &= 0.86(R_p/R_\oplus)^{1.89} M_\oplus.
 \end{aligned} \tag{8}$$

$$\begin{aligned}
 9.0 \leq R_p/R_\oplus: \\
 M_p &= 100 M_\oplus; \text{ i.e., } M_J.
 \end{aligned} \tag{9}$$

The original formulation of Equation (8) includes a very weak dependence on the incident stellar flux ($(F/F_\oplus)^{0.057}$). Because this weak dependence might not be valid, we apply $F = 100 F_\oplus$ as a substitute. Also, the masses of Jupiter-sized planets vary widely. Because only 2% of the planets are in this size range, the results are insensitive to the masses we assume for these planets.

The calculated mutual Hill radii, along with other useful system properties, are available in Table 1. Although there is large scatter in the planet masses with respect to these mean empirical relations (Marcy et al. 2014; Weiss & Marcy 2014; Rogers 2015; Wolfgang & Lopez 2015; Chen & Kipping 2017), we have no reliable basis for deciding which planet masses should be higher or lower than the mean, and so we adopt a simple one-to-one mapping of radius to mass. Furthermore, as the Hill radius scales as $m^{1/3}$, uncertainties in the mass of order a few do not seriously affect the estimated mutual Hill radius.

The orbital separations in mutual Hill radii are shown in Figure 14. The top panel is a histogram of the CKS multis, including sub-samples of the CKS multis with two, three, or at least four transiting planets, and annotations corresponding to the mutual Hill radii of solar system planets. The bottom panel is the cumulative distribution function. The majority of *Kepler* planets (93%) are at least 10 mutual Hill radii apart, and the distribution of mutual Hill radii peaks at around 20. Fang & Margot (2012), Pu & Wu (2015), and Dawson et al. (2016) have also estimated that the *Kepler* planets have a typical

Figure 14. Top: separation in mutual Hill radii between adjacent pairs of transiting planets, assuming the empirical mass–radius relations from Weiss & Marcy (2014) and Weiss et al. (2013). The CKS multis are shown (black line), as are the sub-samples with two (green), three (cyan), or at least four (purple) transiting planets. Planet pairs in the solar system are shown as dotted lines, with the planet names at the top of the plot. Bottom: same as top, but showing the cumulative distribution function.

spacing of about 20 mutual Hill radii, but our updated planet radii and stellar masses allow more precise empirical estimates.

Systems with high multiplicity of transiting planets (4+) tend to have the smallest Hill separations, shown in purple. For example, the *Kepler*-11 planets have $\Delta < 10$. However, the masses of these planets are known: the *Kepler*-11 planets all have systematically low densities, making their masses smaller than what we predicted from a simple mass–radius relationship. Because many compact systems with TTVs have systematically low densities (Weiss & Marcy 2014), a more sophisticated mass–radius relation is necessary to quantitatively link the compactness of a system, the planet radii, and the planet masses.

For systems that have larger Hill separations, it is possible that the eccentricities and/or mutual inclinations of the planets are larger, requiring larger separations between the planets for stability. For systems with pairs of planets more than about 20 mutual Hill radii apart, it is also possible that another planet

Figure 15. The average planet radius in an adjacent pair, R_P avg., vs. the estimated spacing in mutual Hill radii between those planets, Δ_{RH} . The colors correspond to the orbital period ratio, P_{j+1}/P_j . The negative correlation between planet size and mutual Hill radius ($r = -0.26$, $p < 10^{-5}$) appears to arise from an absence of points in the lower left corner of the plot. Specifically, planets smaller than $1 R_\oplus$ are at least 16 mutual Hill radii apart. The absence in the lower left corner is related to the absence of planets closer together than a period ratio of 1.2.

resides between them, but either does not transit or has not been detected. It also possible that systems with large dynamical separations are not maximally packed.

If the mutual Hill radius, rather than the orbital period ratio, is the fundamental unit underlying planet spacing, we should expect no correlation between separation in mutual Hill radii and planet size. The mutual Hill radius incorporates the mass of the planet, and so ideally, the computation of mutual Hill radius separation should remove the contribution of planet size. Figure 15 shows the separation in mutual Hill radii versus the average planet size. A Pearson-R test finds a significant negative correlation between planet size and separation in mutual Hill radii ($r = -0.2$, $p < 10^{-5}$). This correlation is driven by an absence of points in the lower left corner of the plot. Planets smaller than $1 R_\oplus$ are all farther apart than 16 mutual Hill radii. It would have been easier to detect these planets if they were closer together (i.e., if they had shorter orbital periods), and so the absence of very small planets at close dynamical spacings is not due to detection bias.

The colors in Figure 15 indicate the orbital period ratio of each pair. The closest pairs, with $P_{j+1}/P_j \approx 1.2$, are red. The colors run parallel to the lower left edge, suggesting that the absence of points in the lower left corner is related to the absence of any planets closer together than an orbital period ratio of 1.2 (Figure 12).

5.3. Temperature Difference Correlates with Planet Size Ratios

In $65.4\% \pm 0.4\%$ of planet pairs in the CKS multis, the outer planet is larger than the inner planet. We investigate whether incident stellar flux is correlated with the asymmetry of planet sizes. For each adjacent pair of planets, we consider the

Figure 16. The ratio of adjacent planet sizes vs. their difference in expected equilibrium temperatures. There is a slight positive correlation (Pearson- $R = 0.23$, p -value $< 10^{-5}$) between the temperature difference and the planet size ratio. To guide the eye, averages in bins of $\log(\Delta T)$ are shown as red squares. This correlation is consistent with photo-evaporation, which should result in inner planets being smaller than outer planets.

difference in their estimated equilibrium temperatures based on the incident stellar flux at each planet¹⁸: $\Delta T_{eq} = T_{inner} - T_{outer}$.

In Figure 16, we investigate whether the difference in equilibrium temperature is correlated with the size ratio of the outer to inner planet. (The size ratio is simply y/x from Figure 2.) We find a slight correlation: the greater the temperature difference between the inner and outer planet, the larger the ratio of their sizes. In particular, there is an absence of planet pairs with a larger inner planet when the temperature difference is large. Photo-evaporation (e.g., Lopez et al. 2012; Owen & Wu 2013; Zahnle & Catling 2017) could produce such an effect, as the expectation from photo-evaporation is that inner planets should be smaller than outer planets (assuming identical core masses), and that this effect should be more pronounced when the temperature difference is larger.

Is the correlation between the planet size ratio and temperature difference due to astrophysical processes such as photo-evaporation, or a detection bias? Repeating the bootstrap procedure of Section 3, we find that bootstrap trials do not reproduce the observed distribution (Figure 17 shows one example). Rather, the bootstrap trials generate detectable planet pairs that populate the lower right corner of the plot (pairs in which the inner planet is larger, even when the temperature difference is large), demonstrating that such planets would have been detectable. Thus, the size ratio versus temperature difference trend is likely due to astrophysics, although the significance is marginal. Determining whether photo-evaporation or some other physics is underlying the correlation will require further investigation and is beyond the scope of this paper.

Ciardi et al. (2013) also found that, after correcting for detectability, the outer planet is larger than the inner planet in 68% of pairs, but this was only true for planets larger than

¹⁸ Assuming a bond albedo of 0.3, as in CKS II.

Figure 17. The ratio of adjacent planet sizes vs. the difference in their equilibrium temperatures in one of 1000 bootstrap trials. The lack of correlation in the bootstrap trial is different from the modest correlation between equilibrium temperature difference and planet size ratio (Figure 16).

$3 R_{\oplus}$. Restricting their sample to planets smaller than $3 R_{\oplus}$, they found no preference for smaller inner planets, whereas we do (67% of outer planets are larger in pairs where both planets are smaller than $3 R_{\oplus}$; see Figure 2). The difference in their analysis and ours likely results from our larger sample.

6. Summary and Discussion

In this paper, we have found the following observational results among the *Kepler* systems with multiple transiting planets:

1. In a given multi-planet system, each planet’s size is strongly correlated with the size of its neighbor.
2. In a given system with three or more transiting planets, the ratio of orbital periods between two adjacent planets is correlated with the orbital period ratios of other adjacent planets in that system.
3. There is a correlation between planet size and planet spacing: smaller planets tend to have smaller orbital period ratios.
4. Converting planet radii to estimated masses, we find that planets tend to be about 20 mutual Hill radii apart. Planets are rarely closer together than 10 mutual Hill radii. Higher multiplicity systems are more packed than lower multiplicity systems.
5. Planets spanning 0.5 to $4 R_{\oplus}$ have orbital period ratios as small as 1.2, but not smaller. This corresponds to a mutual Hill radius of >16 for the smallest planets ($R_p < 1 R_{\oplus}$).
6. In 65% of planet pairs, the outer planet is larger than the inner planet. The ratio of the outer planet to inner planet size is correlated with the temperature difference between the inner and outer planet.

How do the observed patterns in the CKS multis relate to theories of planet formation? The correlation between planet size and planet spacing—at least for the close planetary pairs—suggests that dynamics play a key role in the final planet sizes

and/or the final planet spacings. In particular, how do the patterns in the CKS multis relate to theories of in situ formation versus disk migration?

6.1. In Situ Formation

Lissauer & Stewart (1993) noted, “The self-limiting nature of runaway growth strongly implies that massive protoplanets form at regular intervals in semimajor axis.” In short, this is because protoplanets grow until they have accumulated all of the available material in their feeding zone.¹⁹ Likewise, Kokubo & Ida (1998) noted, “Protoplanets with the same order masses ... (are) the inevitable outcome of planetary accretion.” If oligarchs that formed via runaway growth remained undisturbed since their formation, they should still be at regular intervals today and should still have similar masses. That the CKS multis are similarly sized planets at regular intervals might indicate that they are aged oligarchs that suffered relatively few mass-doubling giant impacts, compared to the solar system terrestrial planets. For comparison, the standard deviation of R_{j+1}/R_j among the CKS multis is 0.63, whereas among the solar system terrestrial planets it is 1.01. Future work that reproduces the typical intra-system variance in planet size and spacing via a detailed dynamical model might be revealing about the prevalence of giant impacts in the CKS multis.

Protoplanetary formation theory does not generally include the acquisition of gas, which is an important factor in the final planet size, as just a few percent hydrogen by mass can double a planet’s radius. If the protoplanets of similar masses are forming at the same time, as long as the gas fraction does not vary by many orders of magnitude between the innermost and outermost planet, it is plausible that the planets acquire similar amounts of gas, which would explain why they grow to be the same size. Millholland et al. (2017) find that planets in the same system tend to have similar masses, strengthening the evidence that similarly sized planets are remnants of planet formation.

6.2. Disk Migration

On the other hand, perhaps the CKS multis experienced Type I disk migration that brought them to their present locations. One criterion for this formation mechanism is that the majority of the planets are not caught in mean motion resonances (Fabrycky et al. 2014). To escape resonant capture, the planets would need low masses (compared to their stars) and sufficiently high eccentricities (Pan & Schlichting 2017). However, because the Type I migration rate scales with planet mass, the planet masses might need to be finely tuned to reproduce the observed correlated spacing of planets, or would need to escape from resonance after migrating in a locked configuration. Furthermore, for many of the *Kepler* systems, the tight spacing ($\Delta < 20$) requires low eccentricities for dynamical stability (Fang & Margot 2012; Petrovich 2015; Pu & Wu 2015; Dawson et al. 2016), which places an upper bound on plausible eccentricities achieved during migration.

One particularly intriguing population for disentangling the histories of in situ formation versus disk migration is the very

¹⁹ An annulus centered on the star in which the velocity difference between the protoplanet and a swarm of planetesimals is sufficiently small that the gravitational force of the protoplanet wins over competing forces on the planetesimals (Lissauer & Stewart 1993; Goldreich et al. 2004).

small planets ($R_p < 1 R_\oplus$), which have orbital period ratios of 1.2, but wide separations ($\gtrsim 20$) in terms of mutual Hill radii. That the planets are not closer together than a period ratio of 1.2, even though Hill stability allows it, is probably evidence that chaos and eventual Lagrange instability dominates at $P_{j+1}/P_j < 1.2$. Although these planets could, in theory, have orbital period ratios larger than 1.2, all of the pairs detected so far have orbital period ratios clustered near the wall at 1.2. What can the absence of sub-Earths at larger orbital period separations (and larger mutual Hill radii) tell us about formation theory? Either (1) sub-Earths form near the stability limit, or (2) migration tends to bring sub-Earth sized planets to the stability limit and park them at that limit.

6.3. Kepler and the Solar System

In the bottom panel of Figure 14, the cumulative distribution function for the solar system (dotted line) traces the distribution for the CKS multis. It is difficult to calculate the significance of the similarity because the solar system has only nine planets (including Pluto). The similarity in the mutual Hill radii between the CKS multis and the solar system is striking because the *Kepler* planetary systems are often distinguished from the solar system with the phrase “dynamically packed.” However, Figure 14 underscores that in a dynamical sense, their orbital separations are very similar. The orbital separations of the *Kepler* planets in units of au are small compared to the solar system, but this is not so in units of mutual Hill radii.²⁰

Nonetheless, the *inner* solar system (our terrestrial planets) are quite far apart in mutual Hill radii, unlike the *Kepler* systems. The top panel of Figure 14 shows that Venus and Earth, Earth and Mars, and Mars and Mercury are all >20 mutual Hill radii apart (Mercury and Venus are more than 60 mutual Hill radii apart). Also, the orbital period ratios between all these planet pairs are larger than 1.2. Although our solar system has an overall resemblance, in terms of dynamical packing, to the CKS multis, the amount of space between the terrestrial planets is rare among the *Kepler* planets.

Perhaps the wide spacing of planets in our inner solar system is due to the influence of Jupiter (Chambers 2001; Levison & Agnor 2003; Gomes et al. 2005). A more rigorous search for giant companions to the *Kepler* multi-planet systems is necessary to better contextualize our solar system among other multi-planet systems.

6.4. The Future

Measurements of the masses and eccentricities in systems of regularly spaced planets, especially in systems where photo-evaporation has played at most a minor role, will test the predictions of in situ formation models and Type I migration models. Obtaining accurate planet multiplicity, planet masses, and planet orbital dynamics in such systems might elucidate how the majority of the *Kepler* sub-Neptune-sized planets formed.

As the TESS primary mission is expected to obtain at most a year of continuous photometry (in the continuous viewing zones Ricker et al. 2015), it will not be as sensitive to long-period planets in multi-planet systems as *Kepler* was. Additional planet searches using radial velocity data, transit follow-up, astrometry from *Gaia*, and direct imaging with a

small inner working angle (such as from WFIRST with a starshade) will help extend our sensitivity to as many planets as possible in multi-planet systems. Such observations are necessary to further test the predictions of planet formation theories and to understand if our solar system is common or rare.

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Facilities: Keck:I (HIRES), *Kepler*.

²⁰ Malhotra (2015) and others have also made this point.

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