



# Galaxy Ellipticity Measurements in the Near-infrared for Weak Lensing

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## Abstract

We investigate the value of the near-infrared imaging from upcoming surveys for constraining the ellipticities of galaxies. We select galaxies between  $0.5 \leq z < 3$  that are brighter than expected *Euclid* sensitivity limits from the GOODS-S and N fields in CANDELS. The co-added CANDELS/HST *V+I* and *J+H* images are degraded in resolution and sensitivity to simulate *Euclid*-quality optical and near-infrared (NIR) images. We then run GALFIT on these simulated images and find that optical and NIR provide similar performances in measuring galaxy ellipticities at redshifts  $0.5 \leq z < 3$ . At  $z > 1.0$ , the NIR-selected source density is higher by a factor of 1.4 and therefore the standard error in NIR-derived ellipticities is about 30% smaller, implying a more precise ellipticity measurement. The good performance of the NIR is mainly because galaxies have an intrinsically smoother light distribution in the NIR bands than in the optical, the latter tracing the clumpy star-forming regions. In addition, the NIR bands have a higher surface brightness per pixel than the optical images, while being less affected by dust attenuation. Despite the worse spatial sampling and resolution of *Euclid* NIR compared to optical, the NIR approach yields equivalent or more precise galaxy ellipticity measurements. If systematics that affect shape such as dithering strategy and point-spread function undersampling can be mitigated, inclusion of the NIR can improve galaxy ellipticity measurements over all redshifts. This is particularly important for upcoming weak lensing surveys, such as with *Euclid* and *WFIRST*.

*Key words:* gravitational lensing: weak – cosmology: observations

## 1. Introduction

Weak gravitational lensing (WL) is a slight deflection of light rays from distant galaxies when they propagate through the tidal gravitational field of intervening large-scale structure. The amplitude of the WL distortion can be used to map dark matter and measure dark energy by statistically quantifying the shear distortions encoded in the observed shapes of background galaxies, namely, galaxy ellipticities (e.g., Kaiser et al. 1995; Bartelmann & Schneider 2001). The ellipticities of galaxies are typically distorted only about 1% by WL (Troxel & Ishak 2015), so the WL signal in individual galaxies is challenging to detect. WL measurements thus rely on averaging over a very large sample to obtain the distortions and sufficiently unbiased estimates of galaxy shapes, which in turn require a correction for the impact of the point-spread function (PSF) of the telescope. In that sense, WL observations demand high-quality images because it requires a large number density of resolved galaxies and high signal-to-noise ratio (S/N), while minimizing the PSF corrections and related systematic uncertainties, with well-sampled PSFs (Massey et al. 2013; Schrabback et al. 2018).

*Euclid* (Laureijs et al. 2011) is a survey mission designed to understand the expansion and growth history of the universe and is scheduled to launch in the next decade. *Euclid* will image 15,000 deg<sup>2</sup> of sky in one broad optical band VIS spanning 550–920 nm and three additional near-infrared (NIR) bands (*Y*, *J*, and *H*). *Euclid* will detect cosmic shear with VIS by measuring ellipticities of  $\sim 30$  resolved galaxies per arcmin<sup>2</sup> with a resolution better than 0".18 (PSF FWHM) with 0".1 pixels. The near-infrared bands will primarily be used to derive photometric redshifts for the weak lensing (WL) sample, in conjunction with ground-based observations

at visible wavelengths. The *Euclid* wide survey is expected to provide WL galaxy shape measurements for 1.5 billion galaxies with space-quality resolution.

To measure WL through surveys, one should measure galaxy ellipticities and its uncertainty, including systematics, very accurately. In particular, it is necessary to measure the shapes of typically faint and small, distant galaxies with high-S/N observations. In this work, we demonstrate that NIR bands result in a comparable or more precise galaxy ellipticity measurement compared to optical bands for WL studies despite their worse spatial resolution (0".3 compared to 0".18) and pixel sampling (0".3 versus 0".1 pixel scale). There are several advantages to using NIR bands (Tung & Wright 2017); first, NIR wavelengths sample the rest-frame optical light, which traces the older stellar population (hence the bulk of stellar mass) and is less affected by dust extinction. The VIS band covers the rest-frame UV and blue wavelengths, which predominantly traces emission from star-forming regions (Dickinson 2000). In particular, the shapes of galaxies as seen in the rest-frame UV are more clumped and irregularly distributed than older stellar populations. The second advantage is that galaxies in the NIR bands have an intrinsically smoother light distribution resulting in a lower shape noise than in the optical (Schrabback et al. 2018). Third, NIR images of galaxies have a higher surface brightness with more than nine times the number of source photons per pixel, based on a calculation using images in this study; this is at least partly due to the relative importance of the bulge compared to the disk as a function of wavelength. Finally, we find that the NIR bands are sensitive to a larger number density of distant galaxies than the VIS band (see Section 2).

In this paper, we study the shapes of the galaxy sample expected from *Euclid*-quality imaging and forecast how we can improve the shape measurement by using co-added NIR images.<sup>3</sup> To do that, we select galaxies from *HST*/Cosmic Assembly Near-infrared Extragalactic Legacy Survey (CANDELS; Grogin et al. 2011; Koekemoer et al. 2011) observations satisfying the *Euclid* sensitivity limits and simulate *Euclid*-resolution images. The structure of this paper as follows. The sample selection using CANDELS data is introduced in Section 2. We describe the procedure of simulating *Euclid*-quality optical and NIR images from *HST* images in Section 3. In Section 4, we explain how GALFIT (Peng et al. 2002) is used to measure the ellipticity of galaxies after accounting for the PSF and compare the ellipticities obtained from GALFIT in simulated *Euclid* and CANDELS images. Finally, we present our conclusions in Section 5.

## 2. Initial Sample Selection

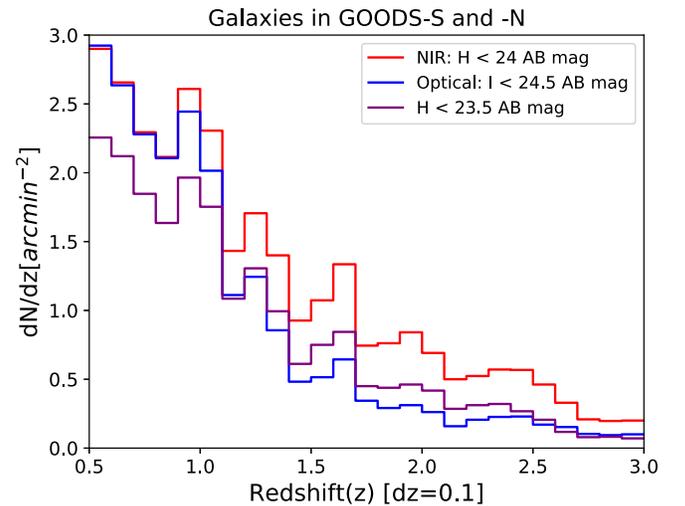
We select a sample of galaxies at optical and near-infrared (NIR) wavelengths from the *HST*/CANDELS survey that closely resembles the *Euclid* WL sample. Among the five CANDELS fields, we use the GOODS-S and GOODS-N fields that include the CANDELS Deep survey and cover about  $340 \text{ arcmin}^2$  in *V* ( $0.606 \mu\text{m}$ ), *I* ( $0.814 \mu\text{m}$ ), *J* ( $1.25 \mu\text{m}$ ), and *H* ( $1.6 \mu\text{m}$ ). These fields are several magnitudes deeper than the *Euclid* survey. We use CANDELS photometric redshifts measured for all galaxies by Dahlen et al. (2013), unless spectroscopic redshifts are available. For the WL shape measurement, the *Euclid* survey will detect galaxies in a broad optical *R+i+z* band (VIS:  $0.55\text{--}0.92 \mu\text{m}$ ) down to 24.5 mag ( $10\sigma$ ). It will use three additional NIR bands (*Y*, *J*, *H* in the range of  $0.92\text{--}2.0 \mu\text{m}$ ) reaching AB mag 24 ( $5\sigma$ ) in each. To achieve the required dark energy figure of merit through WL, the surface density of resolved galaxies needs to be at least  $30 \text{ arcmin}^{-2}$  (*Euclid* Red book; Laureijs et al. 2011).

We start by replicating the *Euclid* expected sensitivity selection on the CANDELS catalogs. We find that  $I < 24.5$  AB mag results in about 30 galaxies per  $\text{arcmin}^2$  with a mean redshift of  $\sim 0.9$ , which is consistent with the *Euclid* requirement. Applying the *Euclid*  $H < 24$  mag selection on the CANDELS NIR sample, results in a mean  $z \sim 1.1$  with about 37 galaxies per  $\text{arcmin}^2$ . The redshift distribution of each sample selection is shown in Figure 1. One clear advantage of the NIR is at  $z > 1$ , where the NIR bands select many more galaxies than the optical. This suppresses the shape noise induced by the intrinsic ellipticities of distant galaxies if the individual ellipticity uncertainties were similar to that in the optical; we assess the veracity of this in the following sections. In this study, we specifically use galaxies at a redshift range of  $0.5 \leq z < 3$  to compare ellipticities estimated from optical and NIR images.

## 3. *Euclid* Images Made from *HST*/CANDELS Images

We simulate *Euclid* VIS and NIR images using *HST*/CANDELS *V* ( $0.606 \mu\text{m}$ ), *I* ( $0.814 \mu\text{m}$ ), *J* ( $1.25 \mu\text{m}$ ), and *H* ( $1.6 \mu\text{m}$ ). Each of the *Euclid* VIS, *Y*, *J*, and *H* bands will have

<sup>3</sup> The simulated *Euclid* images in this paper do not have *Euclid*-specific systematics dealing with dither strategy, field distortion, PSF variations, and intrapixel quantum efficiency variations that will be investigated in the future. However, it should be noted that these affect both optical and near-infrared images.



**Figure 1.** Number density of galaxies at a redshift range,  $0.5 \leq z < 3.0$ , in the GOODS-S and GOODS-N fields. We compare number density of galaxies in redshift bins of width  $\delta z = 0.1$  of different galaxy samples, selected using expected magnitude depths of the *Euclid* survey. The red histogram represents an NIR selection of  $H < 24$  mag, while the blue histogram is for  $I < 24.5$  mag. We also subselect galaxies having  $H < 23.5$  mag based on the quality of their ellipticity fits and present their redshift distribution with the purple histogram (see a further explanation about this selection in Section 4.3). At  $z > 1.0$ , the NIR yields a higher surface density of galaxies than in the optical. The median (mean) redshift is 0.95(1.1), 1.1(1.3), and 1.0(1.2) for the optical, NIR, and  $H < 23.5$  selected sample, respectively, within a redshift range of  $0.5 \leq z < 3.0$ .

four images taken per unit area of sky with  $0''.1$  pixel scale in the VIS and  $0''.3$  pixel scale in the NIR bands (Laureijs et al. 2011). For the VIS images, we combine the CANDELS *V*- and *I*-band images that span the bandwidth of the *Euclid* VIS band,  $0.55\text{--}0.92 \mu\text{m}$ . In both the VIS and NIR bands, there will be significant correlated noise if co-added images are made on a finer pixel scale with just four frames. By combining the *J*- and *H*-band images, we can both increase the signal to noise in the NIR and drizzle on a factor of two oversampled pixel scale with a point kernel (e.g., CANDELS WIDE survey, Grogin et al. 2011; *HST*/ACS COSMOS, Rhodes et al. 2007), thereby minimizing the impact of correlated noise. We therefore combine the CANDELS *J*- and *H*-band images (*Euclid* *J*:  $1.16\text{--}1.58 \mu\text{m}$ , *H*:  $1.52\text{--}2.04 \mu\text{m}$ ). We estimate that the *Euclid* survey strategy results in a median of between 10 and 11 valid frames per pixel when combining all three bands, *Y*, *J*, and *H*. However, the PSF undersampling in the shortest-wavelength band and color gradients across such a wide wavelength range may introduce other systematics. The impact on the under-sampled PSF as a result of the drizzling and the *Euclid* dither strategy is beyond the scope of this work and is currently being investigated. Furthermore, since the CANDELS *Y*-band imaging does not cover the entire GOODS-S and -N fields, we avoid including the *Y*-band in this analysis.

The step-by-step procedure to simulate the *Euclid*-quality images is outlined below:

1. Produce cutouts of science and noise images (*rms*) for each galaxy from the large *HST*/CANDELS *V*, *I*, *J*, and *H* mosaics.
2. Combine *V* and *I* or *J* and *H* by weighting each pixel according to the weight map (inverse variance), i.e.,  $f_{\text{comb}} = (f_1 w_1 + f_2 w_2) / (w_1 + w_2)$ , where  $f_{1,2}$  and  $w_{1,2}$

are the pixel values of science image and weight map, and  $w_{1,2} \sim 1/rms_{1,2}^2$ . Because each pixel value has noise associated with it, and the noise is somewhat heterogeneous due to the observing strategy, an inverse variance weighting is the optimal approach to combine images and increases the signal to noise of co-added images (Koekemoer et al. 2011).

3. Rebin the pixel scale from  $0''.06$  of CANDELS to  $0''.1$  ( $V+I$ ) or  $0''.15$  ( $J+H$ ). By using co-added  $J+H$  images, which will double the number of images, the co-added NIR images can be drizzled onto a  $0''.15$  pixel scale, half of the original NIR pixel scale. This is challenging to do for VIS since only four frames will be taken.
4. Smooth the combined images with a Gaussian kernel to correct for the difference in PSF FWHM between *HST* and *Euclid* (for optical,  $0''.1$  versus  $0''.18$ ; for NIR,  $0''.18$  versus  $0''.3$ ).
5. Make noise maps for the  $V+I$  and  $J+H$  following a random Gaussian distribution with  $1\sigma$  measured from the quoted sensitivity of *Euclid* VIS and NIR images. For the VIS images, the sensitivity is 24.5 mag at  $10\sigma$  (estimated from an extended source with a  $0''.3$  radius; Cropper et al. 2012). For the NIR images, the sensitivity is 24 mag at  $5\sigma$  in each band (measured from a point source), respectively. By combining the  $J$  and  $H$  bands, the effective sensitivity is therefore 24 AB mag at  $7\sigma$ .
6. Add the noise maps to the images to obtain the simulated *Euclid*  $VI(V+I)$  and  $JH(J+H)$  images. Since CANDELS' background noise is negligible (more than 50 times smaller than that of *Euclid*), we do not remove the noise in the CANDELS images before adding *Euclid* noise maps.

A few galaxies in the sample (1% and 3% in  $JH$  and  $VI$ , respectively) are not observed in  $J$  and  $V$  bands because the CANDELS coverage of the field at different bands varies slightly. Thus, after excluding these sources, we have 7248 galaxies for  $VI$  and 9887 galaxies for  $JH$ . For illustrative purposes, the images of five galaxies in the CANDELS  $I$  and  $H$  bands, the simulated *Euclid*  $VI$  and  $JH$  images, and their GALFIT fits are shown in Figure 2.

## 4. Ellipticity Measurements using GALFIT

### 4.1. Masking Sources

Weak lensing measurements, due to the small signal, typically rely on averages over a large number of galaxies. As a result, they usually require aggressive masks of samples to correct systematic effects. In particular, due to the sensitivity limit and spatial resolution, we find that *Euclid* will suffer from blending of galaxies with nearby objects and nondetections that the higher spatial resolution of the VIS band may be able to reveal. As demonstrated in Figure 2, the spatial resolution and S/N of simulated *Euclid* images (third and fourth columns) unsurprisingly appear to be significantly worse than CANDELS images (first and second). We therefore run a source detection algorithm, SExtractor (Bertin & Arnouts 1996), on the  $VI$  and  $JH$  cutouts in Section 3 and remove sources for which the photometry as measured by the SExtractor, AUTO MAG, deviates from the expected magnitude ( $I$ - or  $H$ -band magnitude from the CANDELS photometry catalog) by more than two times the uncertainty in the difference between derived and expected magnitudes. In

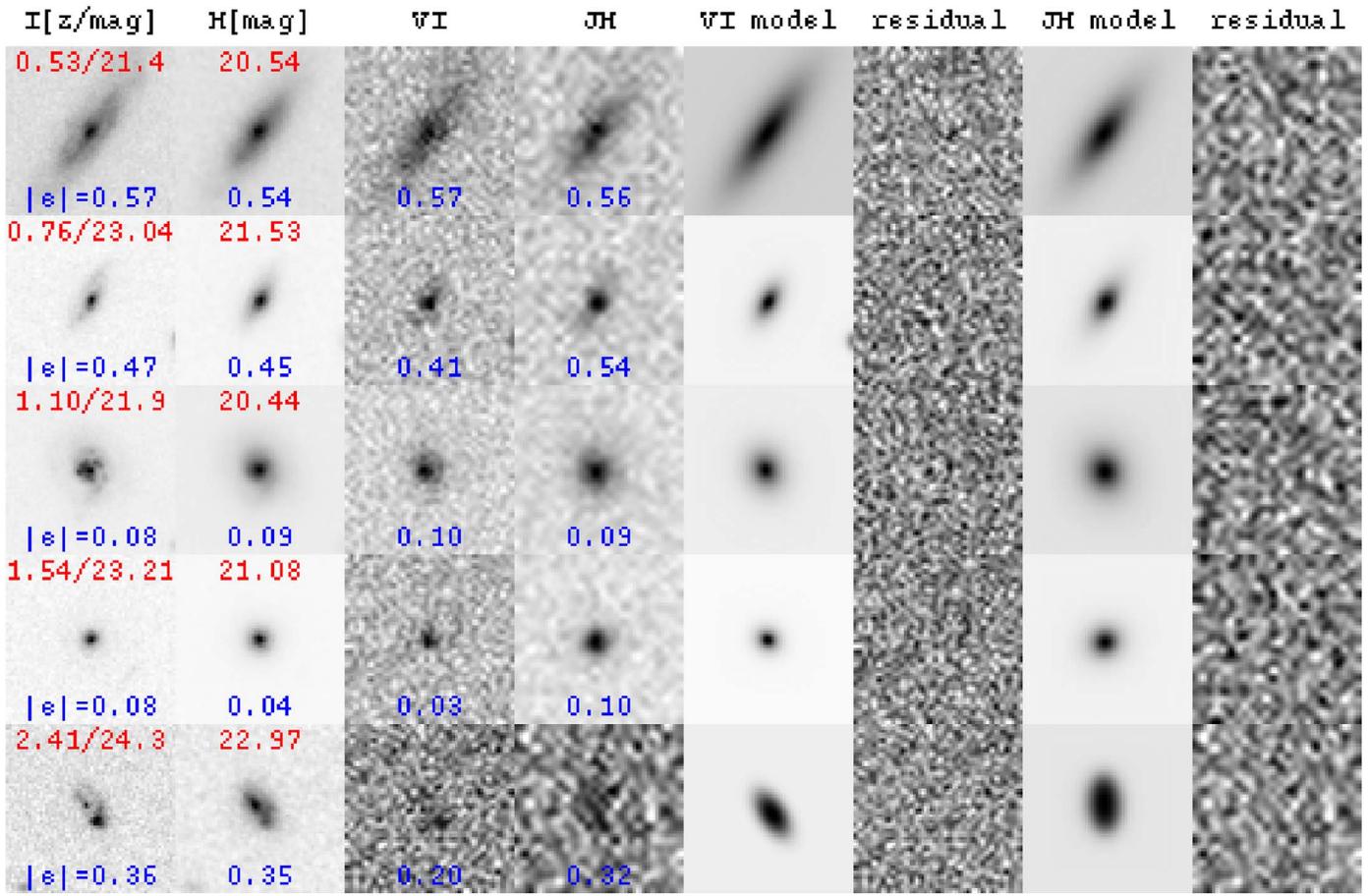
addition, we exclude galaxies from the original sample that are now offset by more than  $0''.7$  ( $VI$ ) and  $0''.75$  ( $JH$ ) relative to the original positions because it implies that the detection in the *Euclid* simulated image is either noise or affected by source confusion. After masking out about 13.3% and 11.4% of sources from Section 3, we have 6283 and 8762 galaxies for  $VI$  and  $JH$ , respectively. At the expected sensitivity limit, we find that we are about 80% complete at 24.5 AB mag in  $VI$  and 24.0 AB mag in  $JH$ .

### 4.2. GALFIT

We measure the ellipticities for the galaxies in the sample using GALFIT (Peng et al. 2002). GALFIT fits a Sérsic law to the surface brightness profile measured within elliptical isophotes of a galaxy. Importantly, GALFIT includes the PSF in the fitting process. The accounting for the PSF is crucial in WL because the smoothing from the PSF make galaxies appear rounder than they actually are (Holden et al. 2009) and significantly biases the ellipticity measurements. The appropriate PSF model is essential for the accuracy of the ellipticity estimation. It is inappropriate to derive a PSF for galaxies from the stars because stars typically have a Rayleigh–Jeans spectrum across the bandpass while galaxies are significant redder, implying a broader intrinsic PSF. We therefore construct a model PSF for the CANDELS using the TinyTim software package (Krist 1995) for the ACS  $I$  band and WFC3  $H$  band by assuming a flat galaxy spectrum ( $f_\nu \sim \text{constant}$ ). They are then re-sampled to the CANDELS pixels scale,  $0''.06$ . For *Euclid*, we re-sample  $I$  and  $H$  Tinytim PSF to the *Euclid* pixel scales,  $0''.1$  ( $VI$ ) and  $0''.15$  ( $JH$ ) and, subsequently, smooth with a Gaussian smoothing kernel to correct for the difference in PSF FWHM between CANDELS and *Euclid*.

We let GALFIT fit the images with central position, magnitude, half-light radius ( $R_e$ ) measured along the major axis, Sérsic index, axis ratio ( $q = \text{semiminor axis}/\text{semimajor axis}$ ), and position angle as free parameters. The SExtractor measurements are used to feed GALFIT with initial guesses for these parameters. In each image cutout, neighboring objects detected from the SExtractor are fit simultaneously or masked out if they are less than 2 mag fainter than the target galaxy. Any fit resulting in problems (i.e., axis ratio errors  $>1.0$ ) or nonexistent results (fits crashed) are excluded. According to experiments undertaken by van der Wel et al. (2012), about 60% of galaxies have a good fit (GALFIT flag = 0) from CANDELS GOODS-S GALFIT catalog, which can be used as reliable measures of ellipticity. We find a slightly higher percentage, 4737 galaxies (65.4%) for  $VI$  and 6449 galaxies (65.2%) for  $JH$ , after excluding all problematic galaxies as discussed in Section 4.1 and bad fits. Figure 2 illustrates best-fit GALFIT model images and residuals images showing the difference between model and original image which are dominated by noise. The absolute value of the ellipticity (see the definition in Section 4.3) computed using the GALFIT results for those galaxies are given in the bottom of  $I$ ,  $H$ ,  $VI$ , and  $JH$  images.

Although GALFIT is one of the most popular fitting tools for measuring galaxy shapes, we lose a large amount of our sample due to unreliable fits. Furthermore, it is known that the GALFIT is not suitable to fit small, faint galaxies, mainly high-redshift galaxies (van der Wel et al. 2012; Sifón et al. 2015). This is mostly due to the number of parameters that GALFIT tries to fit for, which results in unreliable fits in the low-S/N



**Figure 2.** Postage stamps of five galaxies in the GOODS-S field at different redshifts. Each image covers an area of  $4'' \times 4''$ . From left to right, CANDELS  $I$ ,  $H$ , simulated *Euclid*  $V+I$ , and  $J+H$  images, GALFIT model fit to the *Euclid*  $VI$  image and residual, and model fit to the *Euclid*  $JH$  image and residual. Redshift and  $AB$  magnitude of  $I$  and  $H$  bands for each galaxy are given at the top (red text) and the modulus of the galaxy ellipticity calculated from the GALFIT results using respective images are given at the bottom (blue text).

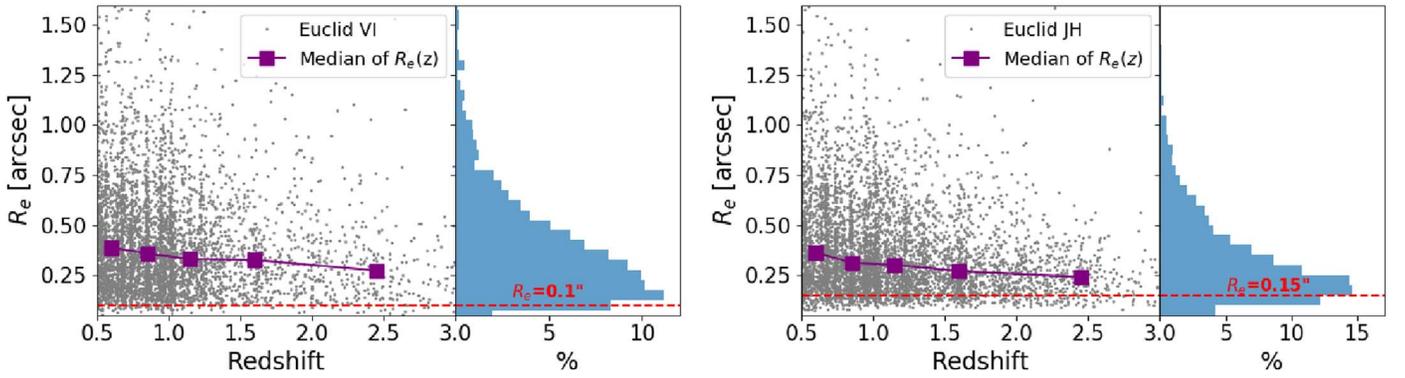
**Table 1**  
Number of Galaxies per  $340 \text{ arcmin}^2$  (and Number of Galaxies per  $\text{arcmin}^2$ ) in Five Redshift Bins between  $0.5 \leq z < 3.0$

	Total (N/arcmin <sup>2</sup> )	$0.5 \leq z < 0.7$	$0.7 \leq z < 1.0$	$1.0 \leq z < 1.3$	$1.3 \leq z < 1.9$	$1.9 \leq z < 3$
$VI$ ( $I < 24.5$ and $R_e > 0''.1$ )	4634 (13.6)	1318 (3.9)	1571 (4.6)	899 (2.6)	529 (1.6)	317 (0.9)
$JH$ ( $H < 23.5$ and $R_e > 0''.15$ )	4770 (14.0)	1042 (3.1)	1352 (4.0)	1004 (2.9)	903 (2.6)	469 (1.4)

regime (Jee et al. 2013). The widely used shear measurement algorithms uniquely developed for WL, such as the Kaiser, Squires, and Broadhurst (KSB) algorithm (Kaiser et al. 1995; Hoekstra et al. 1998) and the *lens* fit (Miller et al. 2007; Kitching et al. 2008), might provide better performance in measuring the ellipticity of galaxies. However, Sifón et al. (2015) compared the KSB results for bright cluster galaxies to GALFIT shapes and showed that the ellipticities measured by both methods are generally consistent. A detailed assessment of the accuracy of ellipticity measurements from different techniques is beyond of the scope of this paper, and we use GALFIT for our main goal of comparing the ellipticities estimated from CANDELS to *Euclid*-quality images.

### 4.3. Comparison of Ellipticities between CANDELS and *Euclid*-quality Images

Typically, only galaxies with a size comparable or larger than the PSF have a well-measured shape, so the shape of the smallest galaxies becomes ill defined. Also, as the S/N decreases, the ability to measure galaxy shapes decreases since the imaging data are only sensitive to the highest surface brightness regions of the galaxy. Therefore, the galaxy samples for shape measurement require a lower limit to the S/N of about 10, and the radius of the galaxy is larger than 1.25 times the PSF FWHM (Euclid Red book; Laureijs et al. 2011). In order to satisfy those requirements, we restrict the galaxy sample in the NIR band to have  $H < 23.5 \text{ mag}$  ( $\sim S/N > 11$  for



**Figure 3.** Redshift vs. half-light radius ( $R_e$  [arcsec]) estimated using GALFIT with *VI* (left) and *JH* (right) images with a histogram of  $R_e$  for  $I < 24.5$  mag and  $H < 23.5$  mag sample. The median of  $R_e$  at five redshift bins (in Table 1) is overlotted with purple squares. The cuts for the galaxy size are  $R_e > 0''.1$  in *VI* and  $R_e > 0''.15$  in *JH* (red dashed lines). Using the size cut, we exclude 2.2% galaxies among the  $I < 24.5$  mag sample and 9.8% galaxies among the  $H < 23.5$  mag sample.

$J+H$ ), and a half-light radius ( $R_e$ ) measured from GALFIT on the simulated *Euclid JH* image of larger than half of the NIR PSF FWHM of *Euclid* ( $R_e > 0''.15$ ). For the optical, we select galaxies having  $I < 24.5$  mag and  $S/N(I) > 10$  with a size limit,  $R_e$  measured from *VI* images  $> 0''.1$ . This is about half the FWHM of the PSF in the VIS band. In Figure 3, we show the distribution of  $R_e$  as a function of a redshift for the optical and NIR sample with  $I < 24.5$  mag (left) and  $H < 23.5$  mag (right), respectively. About 2.2% of optical and 9.8% of NIR-selected galaxies have  $R_e < 0''.1$  and  $R_e < 0''.15$ , respectively. As a final sample for analyzing ellipticities, we use 4634 and 4770 galaxies for the optical and NIR, respectively. In Table 1, the number densities of the galaxy samples in the optical and NIR are listed at five different redshift bins. The relatively high S/N cut of  $H < 23.5$  mag results in a similar total number density of galaxies with the *VI* band as also shown in Figure 1, but still translates to a higher number density by a factor of 1.4 at  $z > 1$  (6.9 versus 5.1 arcmin $^{-2}$ ).

In order to study galaxy shapes, the complex galaxy ellipticity is typically used in WL studies (Miller et al. 2013; Schrabback et al. 2015). Using axis ratio ( $q$ ) and position angle estimated from GALFIT, we compute the complex galaxy ellipticity ( $e$ ) of our final sample, which is defined as

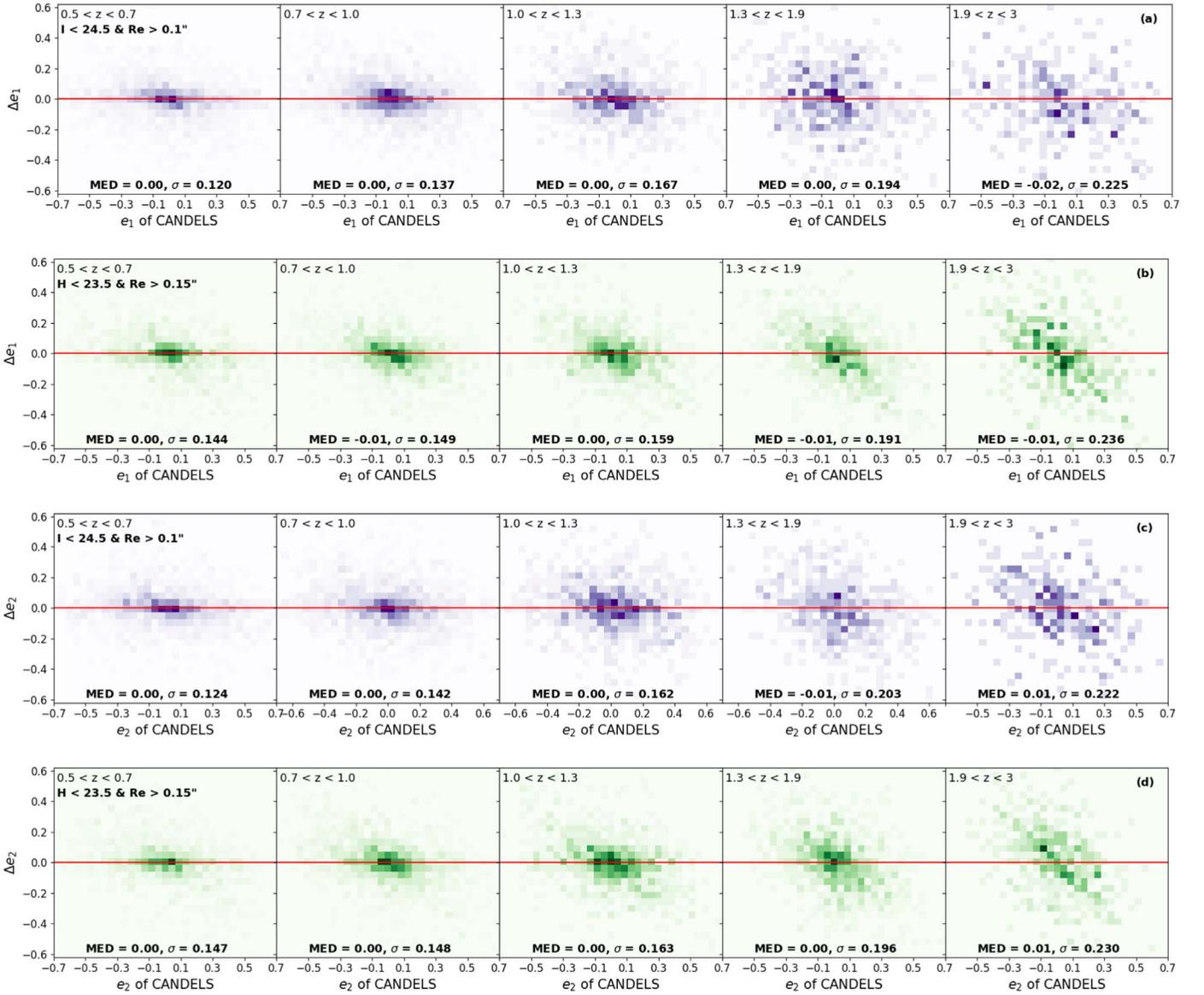
$$e = e_1 + ie_2 = |e|e^{2i\phi}, \quad (1)$$

where the modulus of the ellipticity ( $|e|$ ) is defined as  $(1-q)/(1+q)$  and  $\phi$  corresponds to the position angle of the major axis. We then compare complex galaxy ellipticities ( $e$ ) measured from *Euclid*-quality images with the CANDELS values. Here, we consider CANDELS-measured ellipticity as the original ellipticity of an observed galaxy because of the much larger depth and better resolution compared to *Euclid* data. Through this comparison, we can investigate the robustness of the galaxy shape measurements on the simulated *Euclid* images.

In Figure 4, we plot differences in ellipticities between CANDELS and *Euclid*-quality data,  $\Delta e_\alpha = (e_\alpha \text{ of } Euclid \text{ quality} - e_\alpha \text{ of CANDELS})$ , as a function of  $e_\alpha$  of CANDELS for both ellipticity components,  $\alpha = 1, 2$ , in the range of  $-1 < e_\alpha < 1$ . Most galaxies scatter systematically around  $\Delta e_\alpha = 0$  for both optical (purple) and NIR (green) with a median  $\sim 0$  at all redshift ranges considered in this study. The uncertainty in  $\Delta e$  quantifies how well the galaxy shapes are recovered with *Euclid*-quality images. The lowest redshift bin

has a measured scatter ( $\sigma$ , the standard deviation of  $\Delta e_\alpha$ ) in the NIR, which is a factor of 1.2 larger than that in the *VI* band. However, the measured scatter in the NIR is similar to that in the *VI* at all other redshifts,  $z > 0.7$ . Overall, we find that the ellipticities of individual galaxies can be measured with a similar scatter from the *Euclid* VIS- and NIR-like images. There is a weak trend that the scatter of  $\Delta e_\alpha$  increases with redshifts in both selections. Galaxies are fainter and smaller at higher redshift, so the limited *Euclid* spatial resolution and sensitivity will result in a larger scatter in the measured shape. In particular, at higher redshifts, galaxies with larger ellipticities (in absolute values) tend to have larger discrepancies (see diagonal trends at  $z > 1.3$ ). This is likely because highly elongated galaxies in CANDELS appear to be rounder and with less-constrained position angles at *Euclid*-quality resolution. This trend appears to be a bit stronger for the NIR high- $z$  sample due to the pixelization in the *JH* data.

In Figure 5, we compare the modulus of the ellipticity,  $|e|$  from Equation 1, derived using the CANDELS *I* band to the simulated *Euclid VI* and CANDELS *H* band to the simulated *Euclid JH*. The ellipticities derived from the simulated *Euclid* images are correlated very well with the ellipticities derived from CANDELS images with a median of  $\Delta|e| = (|e| \text{ of } Euclid \text{ quality} - |e| \text{ of CANDELS}) \sim 0$  for both optical and NIR imaging. At  $z > 1.0$ , NIR yields a similar to lower scatter than the optical, while the scatter in *VI*-derived ellipticities is significantly smaller at  $z < 0.7$ . This trend of the uncertainty in  $\Delta e$  is more obvious in Figure 6(a). We compare the standard error (SE) of  $\Delta|e| (= \sigma(\Delta|e|)/\sqrt{N})$  at each redshift bin for *JH* (blue) and *VI* (red). At  $z < 1.0$ , the standard error of *JH* is 1.2–1.1 times larger than one of *VI*. But the trend reverses at  $z > 1.0$  so that the standard error of *JH* is significantly smaller than *VI* by a factor of 1.5–1.3. As shown in Figure 5, the measured  $\sigma(\Delta|e|)$  of galaxies in *JH* is very similar to that of *VI* over the redshift range considered here; thus, the higher number density of galaxies at  $z > 1.0$  drives a lower standard error of ellipticity differences in *JH*. In Figure 6(b), we show the median fractional error of ellipticity, which is defined as  $(\text{median of } \frac{\Delta|e|}{|e|_{\text{[CANDELS]}}}) / \sqrt{N}$ , as a function of redshift. The small values indicate that the derived ellipticity with *Euclid*-quality *JH* and *VI* imaging is very close to the true value from CANDELS on average. We find that the performance of the *JH* band in galaxy ellipticity measurements is comparable to the *VI* at all redshifts despite the significantly worse spatial resolution



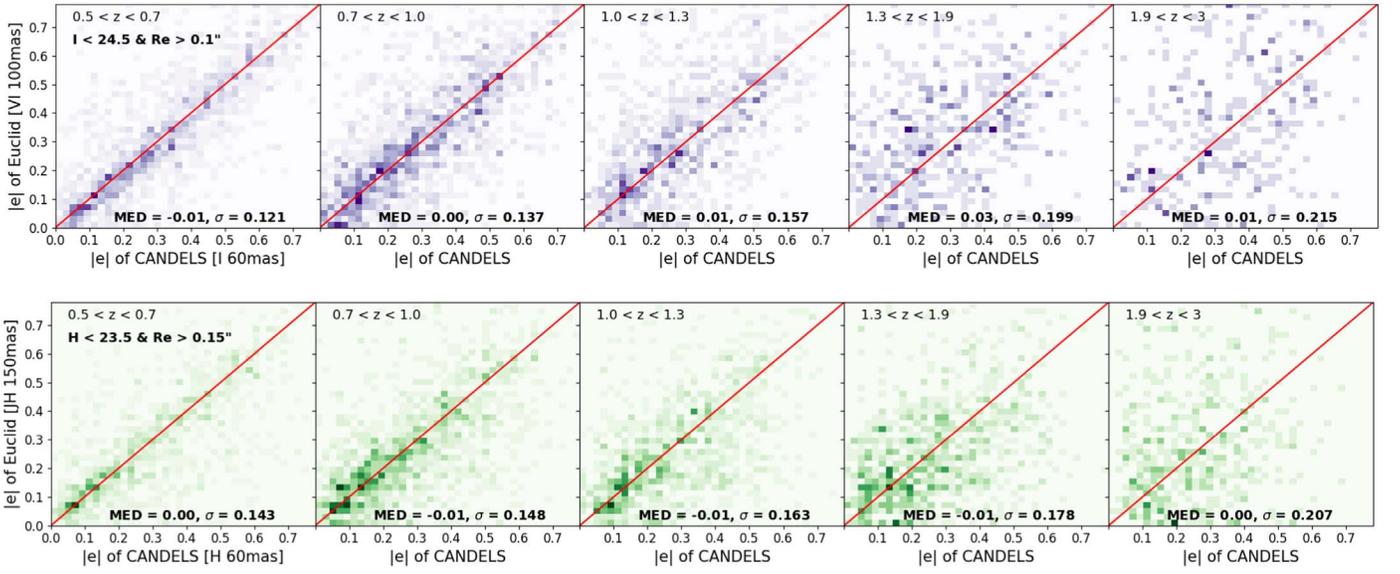
**Figure 4.** Comparisons of the complex galaxy ellipticities derived using *Euclid*-quality and CANDELS images at five redshift bins. Here, we consider ellipticities from CANDELS single-band images ( $I$  or  $H$ ) as the true value and assess how well *Euclid* VIS- and NIR-quality imaging can recover the original ellipticity of an observed galaxy. The purple and green plots represent the ellipticity comparisons for the optical ( $VI$ ) and NIR-selected samples ( $JH$ ), respectively. The complex galaxy ellipticity consists of real ( $e_1$ ) and imaginary parts ( $e_2$ ) in the range of  $-1 < e_{1,2} < 1$  as described by Equation (1). The plot of  $\Delta e_1 = (e_1 \text{ of } Euclid \text{ quality} - e_1 \text{ of CANDELS})$  vs.  $e_1$  of CANDELS are shown in panels (a) and (b) for the optical and NIR samples. Panels (c) and (d) show the plot of  $\Delta e_2$  vs.  $e_2$  of CANDELS for the optical and NIR samples, respectively. The red line shows  $\Delta e_{1,2} = 0$ . Note that the darker color represents a denser region. The median and the standard deviation of  $\Delta e_{1,2}$  for each redshift bin are written as MED and  $\sigma$  on each plot. We find that most galaxies are located around  $\Delta e_{1,2} \sim 0$  in both the optical and NIR. The  $JH$  ellipticities are comparable in quality to the  $VI$  ellipticities, with the scatter in  $\Delta e$  increasing with redshift due to the smaller sizes of galaxies and lower signal-to-noise ratio.

of  $JH$ . This result is very similar to that derived by Tung & Wright (2017), who found that for a 1.2 m class telescope, the  $K_s$  band yields an ellipticity measurement error that is a factor of  $\sim 3$  smaller than in an  $R$ -band selected catalog, while the  $J$  band is a factor of 1.5–2.5 worse than the  $K_s$ -selected catalog. This is also consistent with the results of Schrabback et al. (2018), who found that ground-based  $K_s$  imaging with a PSF FWHM  $\sim 0''.35$  yields an ellipticity dispersion for  $z \gtrsim 1.4$  galaxies, which is 0.76 times that of optically selected galaxy samples with single-orbit *HST* imaging. A comparison between ellipticities derived from the simulated *Euclid*  $JH$  data and CANDELS  $I$ -band data indicates a correlation; however, the  $I$ -band ellipticities are larger than that in the NIR and the scatter

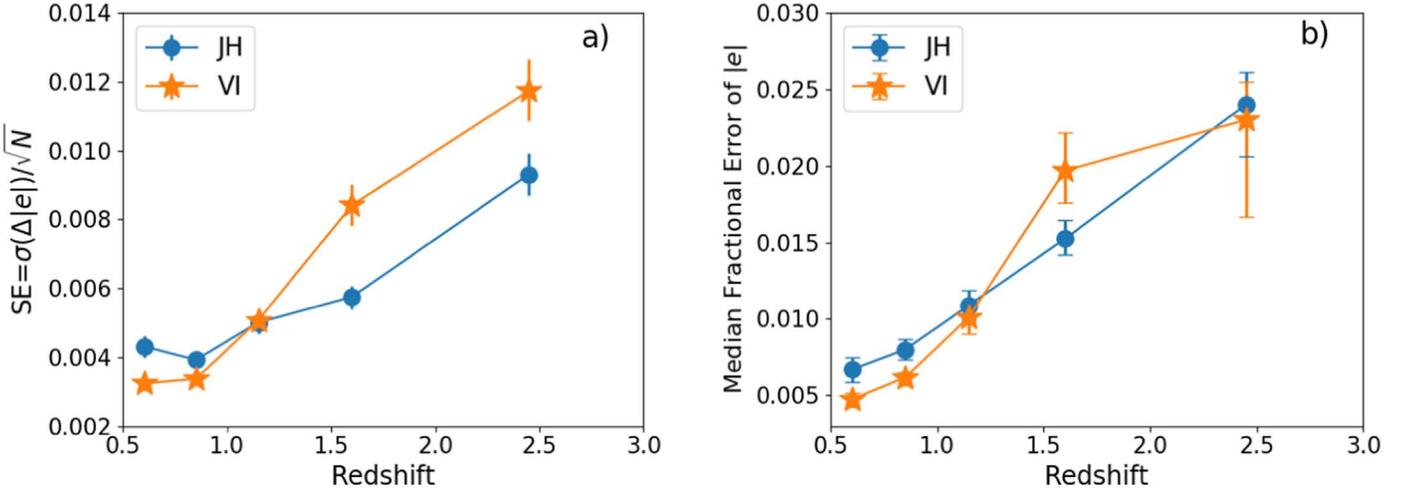
is larger than shown in Figure 5. This is likely because the  $I$ -band ellipticities are dominated by disk light while the NIR ellipticities are tracing a combination of disk and more-compact bulge light. Thus, if systematics arising from PSF under-sampling and dither strategy on the NIR images can be accounted for in future work, the shape noise can be minimized by including ellipticity measurements from the NIR bands.

## 5. Conclusion: Precise Ellipticity Measurements in the NIR

We investigate galaxy ellipticities in simulated *Euclid*-quality optical (VIS) and near-infrared (NIR) images constructed from *HST*/CANDELS co-added  $V+I$  ( $VI$ ) and  $J+H$  ( $JH$ ) images. We select galaxies in CANDELS GOODS-S and



**Figure 5.** Comparisons of the absolute values of galaxy ellipticities ( $|e|$ ) derived using *Euclid*-quality and CANDELS images at five redshift bins. As in Figure 4, the purple and green represent the comparisons for the optical and NIR samples, respectively. Note that the darker color represents a denser region. Red lines are one-to-one correlation. Top purple panels:  $|e|$  derived using *Euclid*-quality VI images with  $0''.15$  pixel scale plotted against  $|e|$  derived using CANDELS I-band images with  $0''.06$ . Bottom green panels:  $|e|$  derived using *Euclid*-quality JH images with  $0''.15$  vs.  $|e|$  derived using CANDELS H-band images with  $0''.06$ . We compute the median and standard deviation of  $\Delta|e| = (|e| \text{ of Euclid-quality} - |e| \text{ of CANDELS})$  and show them as MED and  $\sigma$  on each plot. The ellipticities derived from *Euclid*-quality images show a very good correlation with the true values from CANDELS with MED  $\sim 0$  at all redshift ranges. Overall, the scatter in JH-derived ellipticities is similar to the one measured in the VI band.



**Figure 6.** (a) Uncertainty of the ellipticity difference between CANDELS and simulated *Euclid*-quality images (i.e., standard error (SE)  $\equiv \sigma(\Delta|e|)/\sqrt{N}$ ) as a function of redshift with error bars determined by bootstrapping the sample. The SE in JH is a factor of 1.5 and 1.3 smaller than VI at  $z \sim 1.6$  and  $z \sim 2.5$ . (b) Median fractional error of ellipticity ( $= \text{median} \left( \frac{\Delta|e|}{|e|_{\text{CANDELS}}} \right) / \sqrt{N}$ ) as a function of redshift with error bars determined by bootstrapping the sample. We find that VI and JH imaging yields ellipticities that are consistent with each other at all redshifts. Note that  $N$  is the number of galaxies in each redshift bin over  $0.1 \text{ deg}^2$ .

$\sim 11$  fields (covering about  $340 \text{ arcmin}^2$ ) with photometry in the I and H bands at similar depths as the planned *Euclid* survey. In this study, we specifically use galaxies at a redshift range of  $0.5 \leq z < 3$ . After applying an S/N  $\gtrsim 10$  cut, the total number density of galaxies at  $0.5 \leq z < 3$  is comparable in the NIR and optical; however, the NIR bands select 1.4 times higher number density of galaxies relative to the optical selection at  $z > 1.0$ , which enable us to reduce the statistical uncertainties in the shape measurements of distant galaxies. By co-adding *Euclid*-quality J- and H-band images, which double the number of frames and the exposure time, we can generate images at  $0''.15$  pixel scale (half of the original *Euclid* NIR detector pixel scale) and achieve S/N  $\gtrsim 7$  at  $H < 24 \text{ mag}$  and

$\gtrsim 11$  at  $H < 23.5 \text{ mag}$ . Using GALFIT, we measure ellipticities of galaxies in CANDELS I- and H-band images with  $0''.06$  pixel scale and the simulated *Euclid* VI and JH images with  $0''.1$  and  $0''.15$  pixel scale, respectively. We then compare ellipticities between CANDELS and simulated *Euclid*-quality images while considering *HST*/CANDELS ellipticity as the original ellipticity of a galaxy due to its superior depth and resolution.

A comparison between ellipticities derived from CANDELS and *Euclid*-quality VIS and NIR imaging shows that both wavelength ranges provide similar performance in measuring galaxy ellipticities at all redshifts included in this study despite the worse spatial resolution and pixel sampling of the NIR

imaging. When combined with the higher source density in the NIR selection, we find that the standard error in NIR-derived ellipticities is about 30% smaller than the optical bands at  $z > 1.0$ , which implies a more precise ellipticity measurement than in the optical alone. Since the VIS and NIR galaxy shape measurements with *Euclid* have different fractional contributions of the bulge and disk, a combination of the two can improve the precision with which galaxy ellipticities are measured. The next step that is required before the NIR data can be used for WL studies is to assess how the drizzling affects both the undersampled telescope PSF and the correlated noise (see, e.g., Rhodes et al. 2007). However, even though the FWHM of the *Euclid* NIR imaging does not quite reach *HST* or *WFIRST* resolution, the NIR data provide a major advantage for WL measurements compared to optical ground-based observations that typically achieve a PSF FWHM  $\sim 0''.6\text{--}0''.7$  in good seeing conditions (e.g., Kuijken et al. 2015; Mandelbaum et al. 2018); while the latter provides good sensitivity to the WL signal with a median redshift of the sample of  $z \sim 0.85$ , about half the galaxy sample will be unresolved due to the small size of galaxies, as shown in Figure 3, implying a higher statistical uncertainty in their ellipticities.

In conclusion, by using co-added  $J+H$  band *Euclid*-quality images, we show that the galaxy sample selected at NIR wavelengths yields a more precise ellipticity measurement, especially at high redshifts. This suggests that a careful evaluation of NIR shape systematics for future weak gravitational lensing surveys, such as with *Euclid* and *WFIRST*, should be undertaken.

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