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# Ultradeep near-infrared imaging of the HDF-South: rest-frame optical properties of high redshift galaxies

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## ABSTRACT

We have obtained ultradeep  $J_s$ ,  $H$  and  $K_s$  near-infrared imaging of the Hubble Deep Field South WFPC2 field with the ISAAC camera on the VLT. The total integration time of 100 hours resulted in the deepest ground-based infrared observations to date and the deepest  $K_s$ -band data ever taken. This depth allows us to determine the spectral energy distributions of the high-redshift galaxies with unprecedented accuracy. Together with existing optical observations, we use the multicolor data to select high-redshift galaxies by their rest-frame optical light, and study their statistical properties and morphologies. We find a wide variety of morphologies: some are large in the rest-frame optical and resemble normal spiral galaxies, others are barely detected in the observers optical and have red NIR colors. The latter belong to a new population of galaxies at redshifts  $z > 2$ , that is notably absent in the HDF-North. The spectral energy distributions of many of such red galaxies show distinct breaks, which we identify as the balmer break/4000 Angstrom break, and their contribution to the stellar mass density is estimated to be substantial. At redshift  $z \sim 3$ , we find a clear excess of superluminous galaxies ( $> 5 \times L_B^*(z=0)$ ), which is consistent with 1 magnitude of luminosity evolution. Overall, the results show the necessity of deep near-infrared imaging to obtain a full census of the high redshift universe.

**Keywords:** large telescopes, near infrared imaging, high redshift galaxies, galaxy evolution, galaxy morphology, luminosity functions

## 1. INTRODUCTION

In the past decade, our ability to routinely identify and systematically study distant galaxies has dramatically advanced our knowledge of the high-redshift universe. In particular, the effective U-dropout technique<sup>1,2</sup> has enabled us to select distant galaxies using simple photometric criteria. Now more than 1000 of these Lyman break galaxies (LBGs) are spectroscopically confirmed at  $z > 2$ , and they have been subject to targeted studies on spatial clustering,<sup>3</sup> internal kinematics,<sup>4,5</sup> dust properties,<sup>6</sup> and stellar composition.<sup>7,8</sup> Although LBGs are among the best studied classes of distant galaxies to date, many of their properties are still unknown.

More importantly, it is unclear if the ultraviolet-optical selection technique alone will give us a fair census of the galaxy population at  $z \sim 2 - 3$  as it requires high-redshift galaxies to have high far-ultraviolet surface brightnesses and blue observed optical colors. We know there exist highly obscured active galaxies, detected in the sub-mm and radio-surveys,<sup>9</sup> and optically faint hard X-ray sources<sup>10,11</sup> at high redshift that would not be selected this way, but their number densities are lower compared to LBGs and they might represent rare populations or transient evolutionary phases. However, even present-day elliptical and spiral galaxies if

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placed at high redshift would not satisfy the U-dropout criteria because most of them would be too faint in the rest-frame UV. In such cases, the addition of near-infrared (NIR) bands is crucial because it allows to access the familiar rest-frame optical emission of objects at redshifts  $1 < z < 4$ . This enables comparison of galaxies of different epochs at wavelengths where long-lived stars may dominate the integrated light, thus tracing the build-up of stellar mass directly.

In this context we initiated the Faint InfraRed Extragalactic Survey (FIRES)<sup>12</sup>; a large public program consisting of very deep near-infrared (NIR) imaging of two fields, carried out at the *Very Large Telescope* (VLT), to access the rest-frame optical emission of objects at redshifts  $2 < z < 4$ . We observed fields with existing deep optical WFPC2 imaging from the *Hubble Space Telescope* (HST): the WFPC2 main-field of Hubble Deep Field South, and the field around the distant cluster MS1054-03. By selecting sources in the near-infrared  $K_s$ -band, we hope to obtain a more complete view of the high-redshift universe. Compared to the rest-frame far-UV, rest-frame optical light is less sensitive to the effects of dust extinction and on-going star formation, and provides a better tracer of stellar mass. The extended wavelength coverage ( $0.3 - 2.2\mu\text{m}$ ) is required not only to access the rest-frame optical, but also to determine the redshifts of faint galaxies from their broadband photometry alone.

We present here selected results of the HDF-S. The observations, reduction and analysis techniques are described in detail in Ref. 13 and Ref. 14; the results on MS1054-03 will be presented in Ref. 15. Throughout this paper, we assume a flat  $\Lambda$ -dominated cosmology ( $\Omega_M = 0.3, \Lambda = 0.7, h = H_0/100 \text{ km s}^{-1} \text{ Mpc}^{-1} = 1.0$ ). Unless explicitly stated otherwise, all magnitudes are expressed in the Johnson<sup>16</sup> photometric system.

## 2. OBSERVATIONS AND PHOTOMETRY

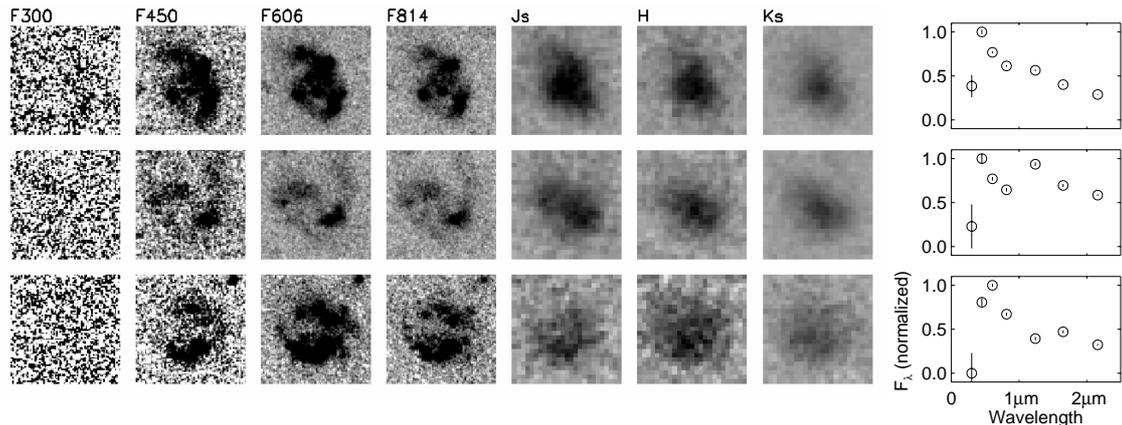
The NIR observations of the HDF-S were obtained using the Infrared Spectrograph and Array camera<sup>17</sup> (ISAAC) on the VLT/ANTU at Paranal. The ISAAC field of view is  $2.5' \times 2.5'$  with a pixel scale of  $0.147'' \text{ pixel}^{-1}$ . We dithered many exposures in the  $J_s$  ( $1.24\mu\text{m}$ ),  $H$  ( $1.65\mu\text{m}$ ) and  $K_s$  ( $2.17\mu\text{m}$ ) bands, with individual exposure times of 120s, 120s, and 60s, respectively. The total integration time in each passband is about 33 hours and the median seeing of all infrared frames is about  $0.46''$ . In the deepest central  $2.1' \times 2.1'$ , we reach total AB magnitudes for point sources of 25.9, 24.8 and 24.4 in  $J_s$ ,  $H$ , and  $K_s$ , respectively ( $3\sigma$  signal-to-noise). The details of the reduction and photometry will be presented in Ref. 13.

We complemented the ISAAC data with HST/WFPC2 imaging<sup>18</sup> (version 2) in the filters  $F300W$ ,  $F450W$ ,  $F606W$  and  $F814W$ , which are close to the  $U$ ,  $B$ ,  $V$  and  $I$  bands, respectively. We constructed a  $K_s$ -band selected sample of galaxies and measured colors in all seven passbands within the  $K_s$ -detection isophote using the SExtractor software,<sup>19</sup> after accounting for differences in resolution and image quality between the HST and VLT data set. Finally we determined the photometric redshifts and associated uncertainties of all extragalactic sources using a method detailed in Ref. 24. The depth of the current survey allows us to determine the spectral energy distributions of the high-redshift galaxies with unprecedented accuracy, which is necessary for reliable photometric redshifts and a proper understanding of stellar populations of the high-redshift galaxies.

## 3. NIR PROPERTIES OF LYMAN BREAK GALAXIES

The LBGs identified in our  $K_s$ -band selected catalogue are different from those found in previous surveys, showing a large variation in both morphologies and spectral energy distributions (SEDs). We selected them by applying the criteria of Madau et al.<sup>20</sup> While most U-dropouts are compact at all wavelengths, some are large in the rest-frame optical and show profound differences between the rest-frame ultraviolet and optical morphologies, as shown in Fig. 1.

The  $I$ -band morphologies (rest-frame  $2000 - 2700 \text{ \AA}$ ) are complex with knotty structure, whereas the NIR light is more centrally concentrated and extended, reminiscent of red bulges and bluer disks with star-forming clumps. In a few cases the rest-frame optical light is almost spatially distinct from the far-ultraviolet. The change in morphology when moving to the NIR is not dominated by the decreasing resolution of the ground-based data but reflects a change in the physical distribution of the light. These properties are in stark contrast with the compact and small sizes traditionally emphasized,<sup>21,22</sup> and the segregated UV-optical morphology has



**Figure 1.** Morphology of the most extended U-drop galaxies in the HDF-S. The left panels show the WFPC2  $U, B, V, I$  data, and right hand panels show our VLT/ISAAC  $J_s, H, K_s$  data. The images are 3 x 3 arcsec on a side. The intensity is proportional to  $F_\lambda$ , with arbitrary normalization for each galaxy. The right hand column shows the spectral energy distributions. As can be seen, these U-drop galaxies are large in extent, and can show prominent Balmer breaks. The  $K$ -band infrared images (rest-frame optical) are generally more centrally concentrated than the WFPC2 images; this is a physical change and not caused by the difference in image quality. The galaxy in the bottom row is spectroscopically confirmed at  $z_{spec} = 2.8$ .

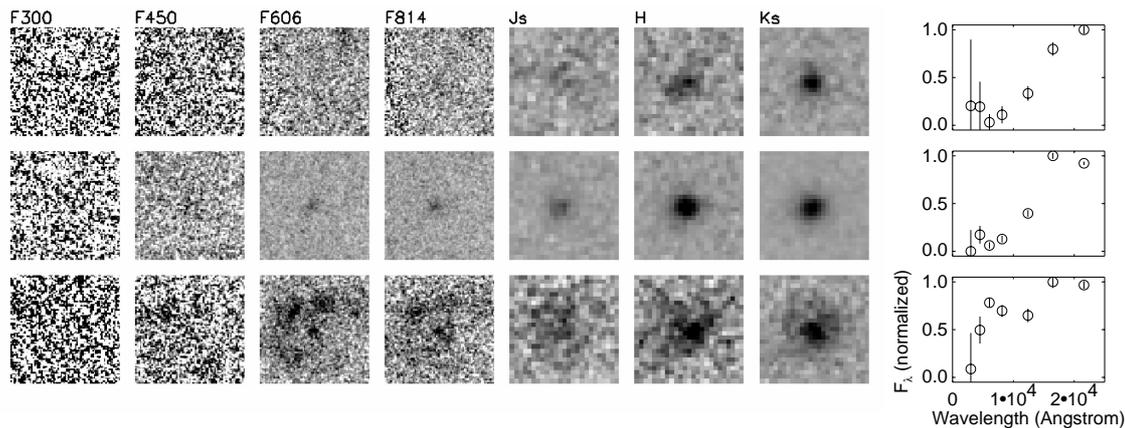
not been seen in the HDF-N.<sup>25</sup> The LBGs with complex structures are amongst the brightest and reddest in the rest-frame optical, suggesting higher mass-to-light ratios, and they might be the most massive LBGs around. Their spectral energy distributions show a pronounced break in the rest-frame optical, which we identify as the age-sensitive Balmer/4000 Å break. Follow-up VLT/FORS spectroscopy<sup>23</sup> confirmed the redshift for one of the large galaxies, a disk-like U-dropout at  $z_{spec} = 2.793 \pm 0.003$ , implying a physical diameter of  $10 h^{-1}$  kpc. While this is only one example, models of galaxy formation must produce objects of comparable sizes and in sufficient numbers to be consistent with our observations.

#### 4. BALMER BREAK GALAXIES

Evolved quiescent galaxies with a prominent Balmer discontinuity in the spectrum, like most present-day Hubble Type galaxies, would have very red observed NIR colors if placed at redshifts  $z > 2$ , and extremely faint in the observed optical. In the HDF-S we find a substantial population of such red galaxies with  $J_s - K_s > 2.3$  and photometric redshifts  $2 < z_{phot} < 4$ . These galaxies are generally compact, with exceptions, as can be seen in Fig. 2. Most of them are extremely faint in the observed optical with red  $V_{606} - H$  colors, and would be missed by the standard U-dropout criteria.

Whether the red NIR colors are due to age or dust has not been determined for the sample as a whole, but many spectral energy distributions exhibit a clear break between the  $J_s$  and  $H$  bands, more consistent with a Balmer/4000 Å break. One of the galaxies shows extremely red NIR colors similar to the curious “J-dropout” HDF-N JD1,<sup>26</sup> possibly a maximally old elliptical or highly reddened galaxy at  $z \sim 3$ . Another shows an  $H$ -band surface brightness profile which can be fit with an exponential out to  $1''$  radius and this galaxy seems to host an arc of blue knots in the WFPC2 images; possibly star-forming sites embedded in a larger evolved system.

We find 13 red objects having  $K_{J,tot} < 22$  compared to 37 U-dropouts to the same flux limit. Interestingly, the contribution of  $K_s$ -band light and the red rest-frame optical colors suggest this red population contains a significant fraction of the total stellar mass at this cosmic epoch. The surface density of these red sources is not well known; the HDF-N has far fewer red galaxies than the HDF-S, as is apparent from comparing Fig. 3 to Fig 1. in Ref. 7 which shows a similar plot of a NIR selected sample in the HDF-N. In the same diagram, we find 7 galaxies redder than  $V_{606,AB} - H_{AB} > 3$  and brighter than  $H_{AB} < 25$ , compared to one in the HDF-N.



**Figure 2.** same as Fig. 1, but for some of the red galaxies. Many of these galaxies are small, and show prominent breaks in the infrared (rest-frame optical). Note that the galaxy in the top row is barely visible even in  $J_s$ . The SED of the object in the middle is consistent with a strong Balmer break at  $z \sim 2.5$ . The galaxy in the bottom row is very extended in the rest-frame optical. It shows faint emission in the  $H$ -band out to  $1''$ , consistent with an exponential profile.

## 5. OPTICAL LUMINOSITY EVOLUTION AT $2 < Z < 3.5$

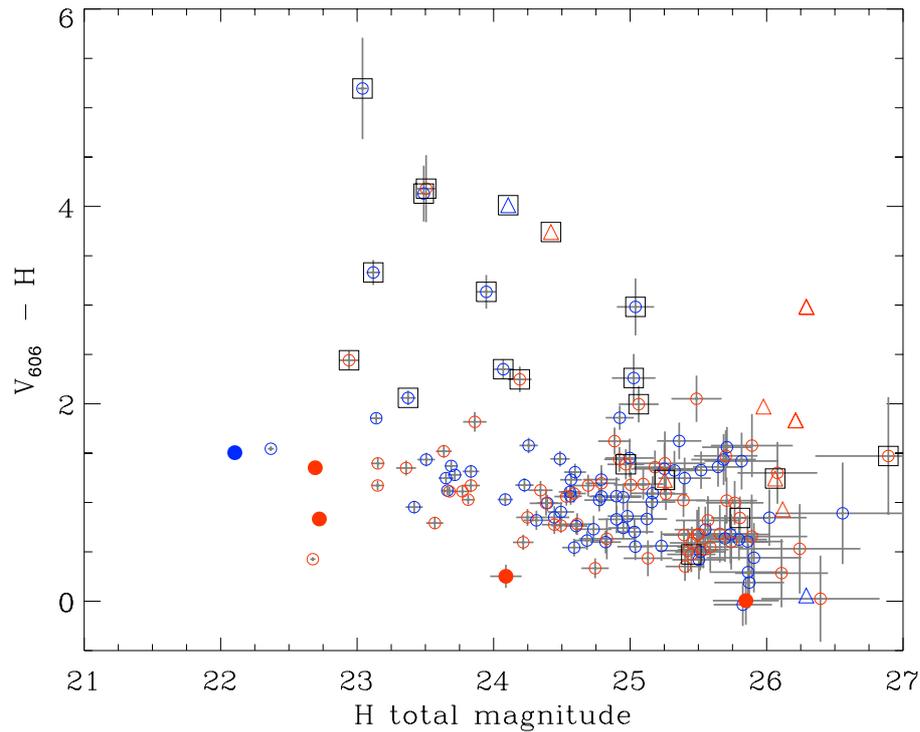
Our long wavelength baseline allows us to observe the  $B$ -band rest-frame wavelength over a large range in redshift. From the best-fit SED at the best-fit redshift, we measured the rest-frame luminosity in the  $B$ -band for our galaxies and plot this as a function of enclosed volume and redshift in Fig. 4. Details of the photometric redshifts determination and rest-frame luminosity calculation can be found in Ref. 24. We find a clear excess of superluminous galaxies and redshifts between  $2 < z < 3.5$ . Where no-evolution scenarios, using local luminosity functions from SDSS<sup>28</sup> and 2dFGRS,<sup>29</sup> predict  $\approx 0.1$  galaxies with  $L_B > 5 \times L_{B,rest}^*(z = 0)$  for the volume probed by our data, we find nine such galaxies. Although random errors in the photometric redshift will tend to produce a bias in the derived luminosities, since the luminosity function declines very steeply towards higher luminosities and the smoothing will increase the number of observed very luminous galaxies, we estimate that this effect is limited. Furthermore, the first spectroscopic observations have confirmed the existence of these luminous galaxies.<sup>23</sup> However, because of the small comoving volumes enclosed in this redshift range, these numbers may not be indicative of the galaxy population as a whole.

If  $L_B^*$  is increased by a factor of 2.7 or 3.2 for the SDSS and 2dFGRS luminosity functions, about one magnitude a luminosity evolution in the  $B$ -band, then nine galaxies are predicted. Pure luminosity evolution models<sup>27</sup> could easily account for such brightening, but current models do not take into account absorption by dust in the galaxies, or any of the observational biases or the incompleteness that may occur for IR-selected galaxies. While NIR selection is generally thought to be less prone to extinction effects and less dependent on the current SFR than optical selection, surface brightness dimming and the bright IR sky can limit detection efficiency for extended objects. We note that Shapley et al.<sup>8</sup> also studied the IR properties of U-dropouts and found their rest-frame optical luminosity function greatly exceeding locally determined values. However, an important distinction with our work is that they studied a rest-frame UV selected sample using only limited IR passbands.

## 6. CONCLUSIONS

The first results of the HDF-S demonstrate the necessity of extending optical observations to near-IR wavelengths for a more complete census of the early universe. Our deepest  $K_s$ -band proves invaluable for it probes well into the rest-frame optical at  $2 < z < 4$ , where long-lived stars may dominate the light of galaxies. We find:

- high-redshift systems that are very extended in the rest-frame optical with complex UV morphologies. Some have spatially distinct rest-frame UV and optical light distributions, where in general the rest-frame

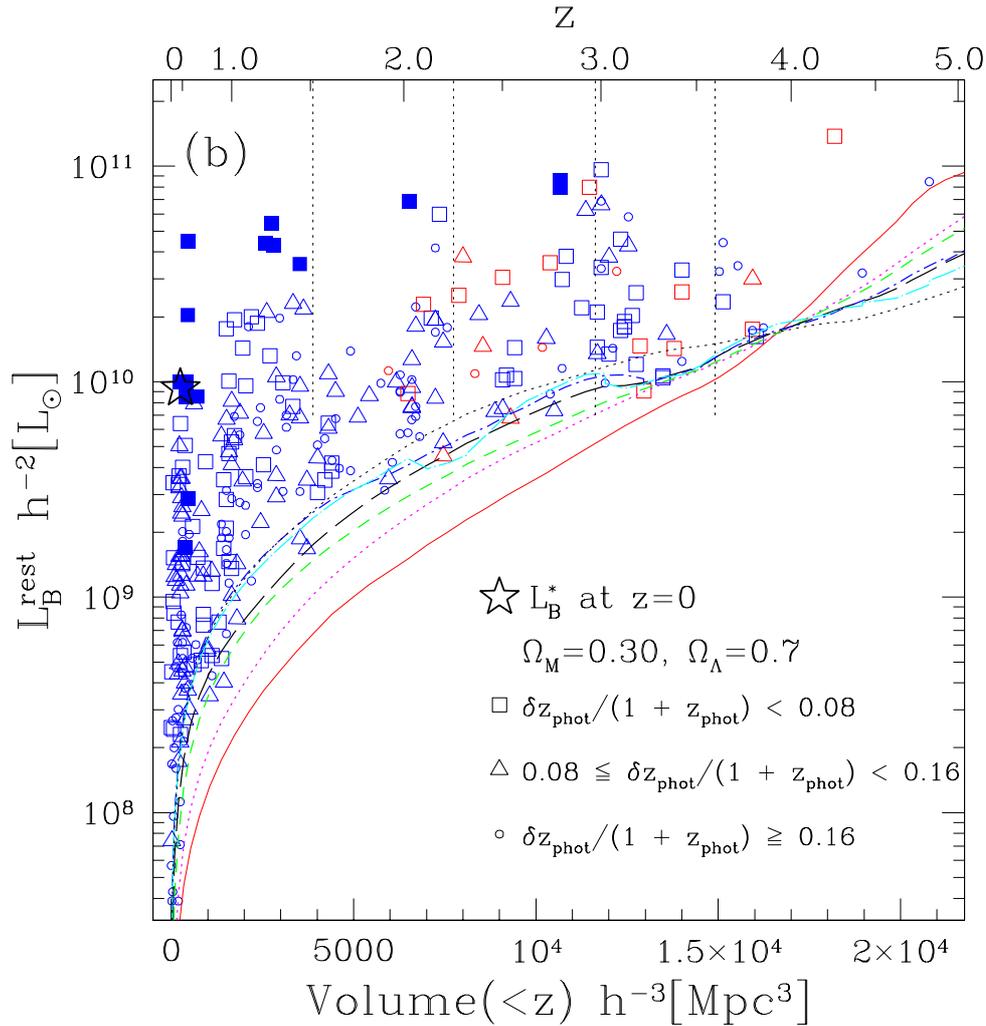


**Figure 3.**  $V_{606} - H$  versus  $H$  color-magnitude diagram (on the AB system) for galaxies in the  $K_s$ -selected catalog of the HDF-S that are photometrically at  $1.95 < z_{phot} < 3.5$ . Filled symbols indicate galaxies with spectroscopy, and the data points are grouped into two redshift ranges:  $1.95 \leq z < 2.7$  (red) and  $2.7 \leq z \leq 3.5$ . The number of candidates for red, evolved galaxies is much higher than in the HDF-N, as shown in a identical plot in Fig. 1 in Ref.<sup>7</sup>: we find 7 galaxies redder than  $V_{606,AB} - H_{AB} > 3$  and brighter than  $H_{AB} < 25$ , compared to one in the HDF-N. For easy comparison, we give the magnitudes and colors in the AB system, where  $V_{606,AB} = V_{606} + 0.12$  and  $H_{AB} = H + 1.38$ . Galaxies with  $S/N < 2$  for the  $V_{606}$  measurement (triangles) are plotted at the  $2\sigma$  confidence limit in  $V_{606}$ , indicating a lower limit on the  $V_{606} - H$  color. The subsample of galaxies having red  $J_s - K_s > 2.3$  colors (open squares) are also indicated.

optical is more centralized. Some of them have disky structure with clumps of star formation, similar to local spiral galaxies.

- a previously undiscovered population of red galaxies with ( $J_s - K_s > 2.3$ ) at  $z > 2$ . Because most of them are barely detectable even in the deepest optical images, they would be missed by ultraviolet-optical color selection techniques, such as the U-dropout method. Many of these galaxies show a prominent jump in the NIR, which may be caused by the Balmer/4000 Å break. The red galaxies likely contribute significantly to the total stellar mass budget at redshifts  $z \sim 3$ .
- a clear excess of luminous galaxies with rest-frame luminosities of  $L_B > 5 \times h^{-2} L_{B,rest}^*(z = 0)$  at  $2 < z < 3.5$ , consistent with a luminosity brightening of one magnitude in the  $B$ -band compared to present-day values.

We are pursuing our follow-up program to obtain more spectroscopic redshifts needed to confirm the above results. It remains surprising that the first results of the HDF-S are so different compared to what has been found in the HDF-N, yet both fields are rather small and results based on them may be seriously affected by large scale structure in the universe. This calls for more observations to similar limits with full optical-to-infrared coverage.



**Figure 4.** The distribution of rest-frame B-band luminosities as a function of enclosed co-moving volume and photometric redshift  $z_{phot}$ . We show all galaxies with  $K_{s,tot} < 23$ . Galaxies which have spectroscopic redshifts are represented by solid points. Note the presence of galaxies at  $z_{phot} \geq 2$  with  $L_B \geq 5 \times 10^{10} L_\odot$ . The tracks represent the values of  $L_B$  for each of our seven template spectra normalized at each redshift to  $K_{s,tot} = 23$ . The large star indicates the value of  $L_B^*$  from local surveys. The point shape indicates the photometric redshift reliability with the point color corresponding to the  $J_s - K_s$  color: galaxies with  $J_s - K_s < 2.3$  are shown in blue, galaxies with  $J_s - K_s > 2.3$  in red. The specific tracks correspond to the E (*solid*), Sbc (*dot*), Scd (*short dash*), Irr (*long dash*), SB1 (*dot-short dash*), SB2 (*dot-long dash*), and 10MY (*dot*) templates.

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