The observed properties of fast radio bursts

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ABSTRACT

I present an empirical study of the properties of fast radio bursts (FRBs): gigahertz-frequency, dispersed pulses of extragalactic origin. I focus my investigation on a sample of 17 FRBs detected at the Parkes radio telescope with largely self-consistent instrumentation. Of this sample, six are temporally unresolved, eight exhibit evidence for scattering in inhomogeneous plasma, and five display potentially intrinsic temporal structure. The characteristic scattering time-scales at a frequency of 1 GHz range between 0.005 and 32 ms; moderate evidence exists for a relation between FRB scattering time-scales and dispersion measures. Additionally, I present constraints on the fluences of Parkes FRBs, accounting for their uncertain sky positions, and use the multiple-beam detection of FRB 010724 (the Lorimer burst) to measure its fluence to be $800 \pm 400$ Jy ms. FRBs, including the repeating FRB 121102, appear to manifest with a plethora of characteristics, and it is uncertain at present whether they share a common class of progenitor object, or arise from a selection of independent progenitors.

Key words: scattering – methods: data analysis – catalogues – pulsars: general – radio continuum: general.

1 INTRODUCTION

A fast radio burst (FRB) may be broadly defined (cf. Petroff et al. 2015; Keane & Petroff 2015) as a demonstrably astrophysical, dispersed radio pulse, with a dispersion measure (DM) that significantly exceeds any estimate (e.g. Cordes & Lazio 2002) of the Milky Way free-electron column density along its sightline. Implicit in this definition is the condition that FRBs adhere to the cold, sparse plasma dispersion law (e.g. Katz 2016). The identification of the host galaxy of the repeating FRB 121102 (Chatterjee et al. 2017) has confirmed the existence of extragalactic sources of pulsed radio emission. Questions regarding the origins of FRBs may therefore be framed in terms of what kinds of sources, at what extragalactic distances, produce FRBs.

Twenty-eight FRB detections have now been published.¹ Even among this small sample, the diversity of FRB properties is striking. FRB 121102, the sole detection at the Arecibo Observatory, is also the only known repeater. Additionally, different FRBs display markedly different propagation signatures; for example, the time-scales by which FRBs are temporally broadened during propagation by scattering due to plasma-density inhomogeneities vary by four orders of magnitude (Ravi et al. 2016). Third, as I shall show, even among the sample of 17 FRBs detected at the Parkes telescope, the range of fluences spans three orders of magnitude.

The primary goal of this paper is to homogenize the inference of FRB properties among the Parkes sample (Section 2).² In particular, I focus on self-consistent estimates of FRB fluences, DMs, intrinsic widths, and scattering time-scales and frequency dependencies. Such measurements have been compiled (and performed) by Petroff et al. (2016), and disseminated through the online FRB Catalogue. However, the Bayesian parameter estimation and model selection framework that I apply herein reveals some potential inaccuracies in previous results. I do not attempt to model FRBs with irregular temporal profiles (Champion et al. 2016). I estimate the fluences of the Parkes FRBs by analysing the sky-response model (Ravi et al. 2016) of the 13-beam–multibeam receiver (MBR; Staveley-Smith et al. 1996) used to detect these events. The fluences of FRBs detected in individual beams of the MBR may be bounded by making use of their non-detections in other beams. Further, for the multiple-beam FRB 010724 (Lorimer et al. 2007), I better constrain its fluence by applying the technique developed by Ravi et al. (2016) for the multiple-beam FRB 150807.

Various attempts have been made to infer characteristics of the FRB population by inspecting the distributions of FRB properties. Efforts have focused in particular on FRB fluences, DMs, and scattering time-scales. Caleb et al. (2016) and Li et al. (2016) have attempted to use quoted fluences or fluence lower limits to derive the cumulative fluence distribution (the ‘logN–logF’) for FRBs.
The observed properties of FRBs

Table 1. Properties of FRB detection instruments.

<table>
<thead>
<tr>
<th></th>
<th>AFB</th>
<th>BPSR</th>
</tr>
</thead>
<tbody>
<tr>
<td>Centre frequency (MHz)</td>
<td>1372.5</td>
<td>1382.0</td>
</tr>
<tr>
<td>Filterbank</td>
<td>Analogue</td>
<td>Digital</td>
</tr>
<tr>
<td></td>
<td></td>
<td>(4-tap polyphase)</td>
</tr>
<tr>
<td>Channel bandwidth (MHz)</td>
<td>3.0</td>
<td>0.390625</td>
</tr>
<tr>
<td>Number of channels</td>
<td>96</td>
<td>1024</td>
</tr>
<tr>
<td>Integration time (μs)</td>
<td>125</td>
<td>64</td>
</tr>
<tr>
<td>Bits per sample</td>
<td>1</td>
<td>2</td>
</tr>
<tr>
<td>σ_i (Jy ms)</td>
<td>0.14</td>
<td>0.11</td>
</tr>
</tbody>
</table>

and thus test for whether the FRB population is consistent with Galactic, nearby extragalactic, or cosmological origins. However, Vedantham et al. (2016) concluded that the FRB logN–logF is best estimated by analysing the numbers of single- and multiple-beam detections at Parkes, and by comparing detection rates at different telescopes (see also Connor, Pen & Oppermann 2016). Additionally, Katz (2016), Vedantham et al. (2016), and Cordes et al. (2016) show that the distribution of FRB DMs is difficult to draw conclusive inferences from. However, Katz (2016) and Cordes et al. (2016) find that the combination of DM and scattering measurements may provide an interesting probe of the characteristic host environments of FRBs. Here, I use updated scattering measurements to revisit the analysis of Cordes et al. (Section 2.4), and find moderate evidence for a relation between FRB DMs and scattering time-scales.

Finally, I discuss the possibility of multiple classes of FRB (Section 4). I focus on the comparison between the Parkes and Arecibo FRB surveys, which have been undertaken with similar instrumentation, at similar frequencies, but with sensitivities and sky coverages that differ by more than an order of magnitude. It appears possible that Parkes could already have detected up to three repeating FRBs like FRB 121102. Using my analysis of the Parkes FRB sample, I speculate on which FRBs may be expected to repeat.

2 MODELLING OF FRB DATA

In the subsections below, I first describe the FRB data that I model, including the pre-processing steps that I perform (Section 2.1). I then outline the different models that I attempt to fit to the data, as well as the Monte Carlo Markov Chain (MCMC) exploration of the model likelihoods and the Bayes Information Criterion (BIC) used to perform model selection (Section 2.2). The results of the modelling in this section are presented in Table 2, and discussed in detail in Section 2.3. I outline the implications of my results for a possible relation between DM and scattering strength in Section 2.4.

2.1 Description of data and pre-processing

Each Parkes FRB was detected in ‘filterbank’ data recorded for each beam of the 13-beam 21 cm multibeam receiver (the MBR). Filterbank data are total-power measurements (Stokes I) in numerous spectral channels, integrated over submillisecond time-scales.

FRBs 010125 (Burke-Spolaor & Bannister 2014), 010621 (Keane et al. 2012), and 010724 (Lorimer et al. 2007) were detected in data taken with the Parkes Analogue Filterbank (AFB; Manchester et al. 2001), which performed the channelization and integration steps prior to (one-bit) digitization. The remaining FRBs were detected with the Berkeley–Parkes–Swinburne Recorder (BPSR) digital-spectrometer system (Keith et al. 2010), with either interconnect Break-Out Board (iBOB) or Reconfigurable Open Architecture Computing Hardware (ROACH) digital signal processing cards developed by the Center for Astronomy Signal Processing and Electronics Research (CASPER), with identical firmware implementations. Details of the AFB and BPSR instruments are given in Table 1.

For all Parkes FRBs besides 131104 (Ravi, Shannon & Jameson 2015) and 150807 (Ravi et al. 2016), the raw filterbank data are made available through the FRB Catalogue (Petroff et al. 2016). For FRB 131104, I made use of raw filterbank data that I have direct access to, which I make publicly available with this publication. For FRB 150807, I make use of raw filterbank data made publicly available by Ravi et al. (2016). The DSPSR package (van Straten & Bailes 2011) was used to dedisperse the filterbank data and extract 2-s duration PSRCHIVE format (Hotan, van Straten & Manchester 2004) data files at the native time and frequency resolutions. Dedispersion on each burst, which I term DM init. For the BPSR data, channels 0–160 (1519.5–1582 MHz) were excluded in the analysis, because these frequencies were attenuated in the analogue signal chain to exclude radio-frequency interference (RFI). No further RFI excision was done. Persistent, narrow-band RFI did not significantly affect the analysis both because of the level-setting procedures of the AFB and BPSR instruments, and because I also subtracted a mean off-pulse baseline level from each channel in the 2-s data sets. Additionally, I searched for significantly time variable or exceedingly strong (comparable to the system temperature) narrow-band RFI by inspecting the total-power variances of each channel in the data, but found none at the 3σ level. I also found no significant bursts of RFI (narrow- or broad-band) coincident with any of the FRBs.

To accelerate further analysis, the dedispersed data were averaged to four channels within the respective AFB and BPSR bands. In each channel, the data were further normalized by the off-pulse standard deviations at a fiducial integration time of 1 ms.

FRB 010724 was detected in four beams of the MBR, and saturated the 1-bit digitizer of the AFB in the primary detection beam (beam 6; Lorimer et al. 2007). I therefore analysed a data set formed from the sum of the three other detection beams (beams 7, 12, and 13).

2.2 Multifrequency burst profile modelling

The pulse-modelling technique employed here closely follows that employed by Ravi et al. (2015) for FRB 131104. I used a Bayesian technique to find model parameter values that best fit the data, as well as their confidence intervals. This technique fully accounts for covariances between model parameters, and allows for accurate parameter confidence intervals in the case of non-Gaussian posterior distributions to be presented. I used the EMCEE MCMC software package (Foreman-Mackey et al. 2013) to explore the full likelihood spaces of the multifrequency models given the data. Fol-

3The open-source CASPER hardware designs and firmware are described online at https://casper.berkeley.edu, and reviews of current CASPER developments are detailed by Hickish et al. (2016).
lowing a burn-in stage, the joint posterior density of all parameters was estimated with 48 000 samples.

To select between models with varying numbers of free parameters, the BIC was calculated for each analysis. The BIC is given by

\[-2 \ln L + k \ln n – \ln(2\pi)\]

where \(L\) is the likelihood estimate for a model with fully specified parameters, \(k\) is the number of model parameters, and \(n\) is the number of measurements being fit to it. In accordance with common practice, I selected the model with the lowest BIC, unless there was a model with fewer free parameters with a BIC within three units of the lowest BIC, in which case the model with the fewer free parameters was selected.

The general statistical model that I adopt for the data is outlined in Appendix A. Four specific models were considered, as described below.

**Model 0.** This model represents a pulse that is temporally unresolved by the instrument, such that the measured shape at each frequency is set by the mean intrachannel dispersion smearing of a delta-function impulse. The contribution to the measured pulse frequency is set by the mean intrachannel dispersion smearing of a delta-function impulse. The model pulse profile in a channel with frequency \(\nu\) is a one-sided exponential function:

\[S_i(t) = \frac{c_i}{\sqrt{2\pi}\sigma_{\nu_i}^2} \exp\left[-\frac{(t - t_0 - t_i, DM)^2}{2\sigma_{\nu_i}^2}\right], \quad \text{for } t > 0\]

where \(t_0\) is a reference time at the highest frequency,

\[t_i, DM = (4.15 \text{ ms}) \text{DM}_{\nu_i} \left[\frac{(\nu_i/1\text{GHz})^{-\beta} - 1.582^{-\beta}}{\nu_i/1\text{GHz}}\right]\]

with \(\beta = 2\) under the assumption of cold/sparse plasma dispersion, and

\[\sigma_{\nu_i} = (1.622 \times 10^{-3} \text{ ms}) \text{DM}_{\nu_i} \nu_i^{-\beta - 1}\]

Here, \(\nu_{i,\text{at}}\) is the deviation of the burst DM from that assumed in the initial dedispersion of the filterbank data (\(\text{DM}_{\text{at}}\)), and DM is \(\text{DM}_{\text{at}} + \text{DM}_{\text{inj}}\). The coefficients \(c_i\) are proportional to the burst fluences in each of the four frequency channels (indexed by \(i\)), not accounting for the uncertain positions of the FRBs within the Parkes response function on the sky. Representative constants of proportionality, \(c_i\), assuming beam-bosiregion positions are given in Table 1 for the AFB and BPSR systems. I assume a frequency-independent system temperature of 28 K, a gain of 1.45 Jy K\(^{-1}\), and digitization-loss factors of 0.798 and 0.936, respectively, for the AFB and BPSR (Keane & Petroff 2015).

The model-free parameters are therefore the four \(c_i\) coefficients, \(t_0\) and \(\text{DM}_{\text{inj}}\). Note that the assumption of \(\beta = 2\) implies that I assume cold, sparse plasma dispersion; no significant deviations from \(\beta = 2\) have been detected for any FRB, and when relaxing this assumption I also did not find any significant deviations. Although the constraining range on \(\beta\) can be used to constrain the size of the dispersing region (Masui et al. 2015), my work does not improve on existing results, and I hence do not report that part of the analysis.

**Model 1.** This model is the same as Model 0, with the modification of setting \(\sigma_{\nu_i}^2\) to \((\sigma_{\nu_i}^2 + \nu_i^2)^{1/2}\). Here, the new free parameter \(w\) is an intrinsic burst width. I assume a Gaussian intrinsic profile, in accordance with common practice in modelling the mean pulse profiles of pulsars (e.g. Yan et al. 2011). The quality of the data also do not permit exploration of more complex profiles in most cases.

**Model 2.** This model extends Model 0 by including the effects of temporal broadening due to scattering, clearly detected in some FRBs with high signal-to-noise ratios (S/N), such as FRB 110220 (Thornton et al. 2013) and FRB 131104 (Ravi et al. 2015). I account for scattering by convolving the temporal profile in equation (1) with a one-sided exponential function:

\[s_i(t) = \exp\left[\frac{t - t_0}{\tau_{1\text{GHz}}}\right], \quad t > 0\]

\[= 0, \quad \text{otherwise.}\]

Here, \(\nu_{i,\text{at}}\) is the frequency of channel \(i\) expressed in units of 1 GHz. This form for the pulse-broadening function (PBF) implicitly assumes that the scattering medium can be well approximated by density inhomogeneities projected onto a single thin screen (Cronyn 1970). However, none of the FRB data have sufficient sensitivity to distinguish between this and other subtly different forms (e.g. Williamson 1972). The new free parameters are the characteristic broadening time-scale at 1 GHz, \(\tau_{1\text{GHz}}\), and the index of frequency dependency, \(\alpha\).

<table>
<thead>
<tr>
<th>FRB</th>
<th>Beam</th>
<th>DM (pc cm(^{-3}))</th>
<th>(\tau_{1\text{GHz}}) (ms)</th>
<th>(\alpha)</th>
<th>(w) (ms)</th>
<th>(c_1 (\sigma_1))</th>
<th>(c_2 (\sigma_2))</th>
<th>(c_3 (\sigma_3))</th>
<th>(c_4 (\sigma_4))</th>
<th>Best model</th>
</tr>
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<tbody>
<tr>
<td>010125 5</td>
<td>792.3(1)</td>
<td>&lt;9.6</td>
<td></td>
<td></td>
<td>&lt;1.25</td>
<td>38(4)</td>
<td>54(5)</td>
<td>56(4)</td>
<td>76(5)</td>
<td>0</td>
</tr>
<tr>
<td>010621 10</td>
<td>745.9(2)</td>
<td>&lt;3.9</td>
<td></td>
<td></td>
<td>&lt;1.4</td>
<td>36(4)</td>
<td>31(4)</td>
<td>42(5)</td>
<td>58(5)</td>
<td>0</td>
</tr>
<tr>
<td>010724 6</td>
<td>362.7(1)</td>
<td>25(5)</td>
<td>6.4(1.7)</td>
<td></td>
<td>2.4(3)</td>
<td>45(4)</td>
<td>53(4)</td>
<td>78(5)</td>
<td>73(5)</td>
<td>3</td>
</tr>
<tr>
<td>090625 6</td>
<td>899.1(6)</td>
<td>5.2(5)</td>
<td>4(1)</td>
<td></td>
<td>&lt;0.2</td>
<td>11.5(7)</td>
<td>8.2(6)</td>
<td>9.9(7)</td>
<td>6.9(7)</td>
<td>2</td>
</tr>
<tr>
<td>110220 3</td>
<td>944.83(5)</td>
<td>11.4(4)</td>
<td>3.6(5)</td>
<td></td>
<td>&lt;0.2</td>
<td>63(2)</td>
<td>53(2)</td>
<td>48(2)</td>
<td>76(2)</td>
<td>2</td>
</tr>
<tr>
<td>110626 12</td>
<td>723.3(4)</td>
<td>&lt;0.57</td>
<td></td>
<td></td>
<td>&lt;0.46</td>
<td>4.5(7)</td>
<td>5.1(6)</td>
<td>5.2(9)</td>
<td>4(1)</td>
<td>0</td>
</tr>
<tr>
<td>110703 5</td>
<td>1104.1(5)</td>
<td>32(1)</td>
<td></td>
<td></td>
<td>&lt;0.71</td>
<td>8(1)</td>
<td>20(2)</td>
<td>19(2)</td>
<td>12(2)</td>
<td>2</td>
</tr>
<tr>
<td>120127 4</td>
<td>554.22(3)</td>
<td>&lt;1.53</td>
<td></td>
<td></td>
<td>&lt;0.18</td>
<td>1.1(3)</td>
<td>1.9(3)</td>
<td>3.2(4)</td>
<td>4.8(4)</td>
<td>0</td>
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<tr>
<td>130626 1</td>
<td>952.01(5)</td>
<td>2.8(4)</td>
<td></td>
<td></td>
<td>&lt;0.52</td>
<td>5.1(5)</td>
<td>5.3(5)</td>
<td>6.6(6)</td>
<td>5.8(7)</td>
<td>2</td>
</tr>
<tr>
<td>130628 5</td>
<td>469.98(1)</td>
<td>&lt;0.23</td>
<td></td>
<td></td>
<td>&lt;0.04</td>
<td>2.4(1)</td>
<td>2.1(1)</td>
<td>1.8(1)</td>
<td>1.5(2)</td>
<td>0</td>
</tr>
<tr>
<td>131104 5</td>
<td>778.5(1)</td>
<td>15(2)</td>
<td>4.4(8)</td>
<td></td>
<td>&lt;0.18</td>
<td>11.9(6)</td>
<td>12.5(6)</td>
<td>10.5(6)</td>
<td>8.0(6)</td>
<td>2</td>
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<tr>
<td>140514 1</td>
<td>563.86(6)</td>
<td>&lt;6.1</td>
<td></td>
<td></td>
<td>1.2(1)</td>
<td>7(1)</td>
<td>8(1)</td>
<td>14(1)</td>
<td>16(1)</td>
<td>1</td>
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<tr>
<td>150215 13</td>
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<td>&lt;0.47</td>
<td></td>
<td></td>
<td>0.7(1)</td>
<td>6.1(7)</td>
<td>5.7(7)</td>
<td>7.0(8)</td>
<td>5.6(7)</td>
<td>1</td>
</tr>
<tr>
<td>150418 4</td>
<td>775.84(1)</td>
<td>0.12(1)</td>
<td></td>
<td></td>
<td>&lt;0.05</td>
<td>1.37(6)</td>
<td>1.44(7)</td>
<td>1.57(7)</td>
<td>1.30(8)</td>
<td>2</td>
</tr>
<tr>
<td>150807 5</td>
<td>266.5(1)</td>
<td>&lt;0.08</td>
<td></td>
<td></td>
<td>&lt;0.04</td>
<td>1.1(1)</td>
<td>3.58(9)</td>
<td>12.6(1)</td>
<td>12.1(1)</td>
<td>0</td>
</tr>
</tbody>
</table>
In some cases, this model was preferred over all others according to the BIC, but the value of $\alpha$ was poorly constrained. In these cases, I assumed a value of $\alpha = 4$ to estimate $\tau_{\text{GHz}}$, corresponding to the expectation for a normal distribution of plasma-density inhomogeneities. In another case (FRB 140514), there was insufficient sensitivity to distinguish between this model and Model 1. I assumed Model 1 in this case.

Model 3. This model combines Models 0–2, including the effects of both scattering and an intrinsic pulse width.

When no evidence was found for either an intrinsic burst width or scattering, I set upper limits on their values by evaluating the posterior distribution for Model 3 with the scattering frequency-dependency index set at $\alpha = 4$.

2.3 Results

I begin by walking the reader through the fitting process for FRB 110220, which was modelled by Thornton et al. (2013) with a Gaussian profile convolved with an exponential scatter-broadened profile. By eye, Models 0 and 1 are inconsistent with the data; this was confirmed by exceedingly high BICs for these models. A fit of Model 2 to the data resulted in a value of $\alpha = 3.6 \pm 0.5$, which is consistent to within the error range with the Thornton et al. (2013) value of $4.0 \pm 0.4$. One cannot compare my value of $\tau_{\text{GHz}} = 11.4 \pm 0.4$ ms with the width at 1.3 GHz estimated by Thornton et al. (2013, 5.6 \pm 0.1ms), because the width quoted by Thornton et al. (2013) includes instrumental and potential intrinsic broadening in addition to the effects of scattering. Finally, to check whether any intrinsic width is detectable, I conducted a fit of Model 3 to the data with $\alpha$ set to a value of 4. The estimated posterior densities for this model are shown in Fig. 1. It is evident both from the shape of the marginalized posterior distribution in $w$, and from a comparison of the BICs between Models 2 and 3 (the BIC for Model 3 was three units greater than the BIC for Model 2) assuming the best-fitting parameters, that there is no evidence for an intrinsic width besides the DM-smearing time-scale. This result is also consistent with the findings of Thornton et al. (2013).

Fig. 1 also serves to illustrate the levels of covariances that I typically found between model parameters. These are negligible. The scattering time-scale, $\tau_{\text{GHz}}$, is most covariant with other parameters, in particular $t_0$ and $c_1$.

I show fits to data on 13 of the Parkes FRB sample in Fig. 2; details of the specific models and best-fitting parameters are given in Table 2. I show temporal profiles averaged over the upper and lower halves of the respective observing bands (Section 2.1). I dedispersed the data using the DMs from the original analyses of the FRBs (DM$_{\text{orig}}$); in some cases, significantly different DMs were derived (e.g. FRB 010125; Fig. 2, top right panel). I do not show the results for FRBs 131104 and 150807, because they have been previously fit using my technique (Ravi et al. 2015, 2016).

The final two Parkes FRBs that are excluded from Fig. 2, 121002 and 130729, could not be modelled using any of Models 0–3. These FRBs are also excluded from Table 2. This is because they both exhibit two temporal components. I show the dedispersed dynamic spectra of these FRBs in Fig. 3. Interesting spectral structure is also present in FRB 130729, which appears concentrated in the lower part of the observing band.

2.3.1 Notes on individual FRBs

FRB 010125: Burke-Spolaor & Bannister (2014) found a width for this FRB of $w \approx 5$ ms, in excess of the DM smearing time-scale, although it was unclear from their analysis whether this was intrinsic to the pulse or caused by scattering. By analysing the variation with frequency of the pulse width, they claim a detection of scattering with $\alpha = 4.2 \pm 1.2$. This is also consistent with $\alpha = 3$, which would simply correspond to a DM-smeread pulse, as they did not appear to account for DM smearing in their analysis of the frequency variation of the pulse width. My analysis suggests that this was indeed the case: I find no evidence for temporal structure in FRB 010125 besides DM smearing (Model 0).

FRB 010621: in agreement with Keane et al. (2012), the present analysis reveals no evidence for temporal structure in this FRB besides DM smearing. Although the Galactic-disc DM contribution along this low-Galactic-latitude sightline is expected to be 534 pc cm$^{-3}$, the expected scattering time-scale is only $\tau_{\text{GHz}} = 0.15$ ms (Cordes & Lazio 2002); this is well below our upper limit of $\tau_{\text{GHz}} < 3.9$ ms (95 per cent confidence).

Through an analysis of velocity-resolved H$\alpha$ and H$\beta$ observations of the Galactic interstellar medium (ISM) along the burst sightline, Bannister & Madsen (2014) concluded that previous estimates for the Galactic-disc DM contribution were underestimated, and that this burst is in fact Galactic (90 per cent confidence). A potential problem for this hypothesis is my upper limit on the scattering time-scale. Bannister & Madsen (2014) predict a scattering time-scale of $\approx 2.4$ ms in the observing band, corresponding to $\tau_{\text{GHz}} \approx 8.5$ ms, which is excluded by my upper limit. On the other hand, the relation between DM and $\tau_{\text{GHz}}$ in the Galaxy has a large intrinsic scatter (0.76 dex; Cordes et al. 2016). None the less, for a Galactic sightline with the DM of the burst (746 pc cm$^{-3}$), the burst would have to be undersmearad by a factor of $\approx 2.5\sigma$. This could be because significant amounts of DM are contributed by higher density gas surrounding the source or hot ISM with weak density fluctuations, or that the scattering is dominated by localized clumps rather than the bulk ISM (Cordes et al. 2016).

FRB 010724: I find moderate evidence for both an intrinsic width and an exponential scattering ‘tail’ in this FRB. The present analysis differs from that of Lorimer et al. (2007) because it uses the sum of data from the three non-saturated beams, rather than data from the saturated beam alone. None the less, my estimates of the scattering time-scale, $\tau_{\text{GHz}} = 25 \pm 5$ ms, and index, $\alpha = 6.4 \pm 1.7$, are consistent with those of Lorimer et al. (2007, 2013, 3 ms and 4.8 \pm 0.4, respectively). I also revise the DM estimate from 375 to 362.7± 0.1 pc cm$^{-3}$.

FRB 110703: unlike the analysis of Thornton et al. (2013), I find moderate evidence for the presence of a significant scattering tail in this FRB ($\tau_{\text{GHz}} = 32 \pm 1$ ms). However, a constrained value for $\alpha$ cannot be determined, and I hence assume $\alpha = 4$.

FRB 130729: like FRB 121002, this burst has two temporal components. Unlike FRB 121002, FRB 130729 also has a discontinuous spectrum (Fig. 3), with most power concentrated in the lower part of the band. It is unclear whether the scattering time-scale derived by Champion et al. (2016) for this FRB is real, or is attributable to the unusual temporal and spectral structure.

FRB 130628: unlike Champion et al. (2016), I find no evidence for a scattering tail in this FRB, or for any structure beyond that described by Model 0. Indeed, my upper limit on the scattering time-scale, $\tau_{\text{GHz}} < 0.23$ ms, is well below the previous estimate of $\tau_{\text{GHz}} = 1.24 \pm 0.07$ ms.

FRB 140514: for this FRB, Models 1 and 2 had equivalent BICs. I hence choose Model 1 for this FRB, and thus do not find any evidence for the existence of scattering, unlike Petroff et al. (2015). Along with FRBs 121002 and 130729, this is one of the few FRBs to exhibit temporal structure beyond Model 0 with no clear evidence.
of scattering. It also has a mildly inhomogeneous spectrum, as indicated by the \(c_i\) coefficients in Table 2.

**FRB 150215:** in agreement with Petroff et al. (2017), I find evidence for a larger temporal width than is expected in Model 0, which appears to be intrinsic to the burst.

**FRB 150418:** in contrast to the analysis of Keane et al. (2016), I find that this FRB exhibits a weak scattering tail, with a time-scale of \(\tau_{1\,\text{GHz}} = 0.12 \pm 0.01\,\text{ms}\). The value of \(\alpha\) cannot be constrained.

**FRB 150807:** this FRB was modelled using similar techniques by Ravi et al. (2016). No evidence was found for any temporal structure beyond Model 0 in either the previous or present analysis. Although I present an upper limit on \(\tau_{1\,\text{GHz}}\) in Table 2, in the analysis below I use the value inferred from the frequency scintillations of 1.6 ± 0.8 \(\mu\text{s}\) (Ravi et al. 2016) at 1.3 GHz, corresponding to \(\tau_{1\,\text{GHz}} = 4.6 \pm 2.3\,\mu\text{s}\).

### 2.4 Astrophysical implications

As foreshadowed in the Introduction, an immediate utility of my quantitative results is to investigate the scattering strengths of FRBs at different DMs. I have only marginally adjusted the FRB DMs, and, as shall be shown in the following section, the fluence constraints for most FRBs are not tight enough to enable a rigorous analysis of the distribution of FRB fluences.

A relationship between the scattering time-scale, \(\tau_{1\,\text{GHz}}\), and DM is firmly established for Milky-Way pulsars over three orders of

---

**Figure 1.** Posterior density estimates for a fit of Model 3 to data for FRB 110220, assuming \(\alpha = 4\). The parameters of the fit were \(w, t_0 (t_0), \text{DM}_{\text{err}} (\text{DM}_{\text{err}}), \tau_{1\,\text{GHz}} (\text{Tau}_{1\,\text{GHz}})\), and \(c_1\) to \(c_4 (c_1 - c_4)\). Estimated marginalized posterior densities in each parameter are shown as histograms of samples of the posterior, and joint densities between all pairs of parameters are shown by shading and contours. 48,000 samples of the posterior were obtained.
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Figure 2. Data (black points and thin black lines) and model fits (thick blue and red lines) for a selection of FRBs. In each panel, the top and bottom curves (corresponding to the blue and red dashed lines, respectively) are the mean temporal profiles of the FRBs in the upper and lower frequency halves of the observing bands, respectively. The relative flux-density scales between the temporal profiles in the two bands are normalized to the respective noise levels; the uniform frequency response of the Parkes multibeam system implies that the temporal profiles in the two bands are on approximately the same absolute amplitude scale. Details of the exact bandwidths are given in the text, and details of the model fits are presented in Table 2.

Magnitude in DM, and 11 orders of magnitude in \( \tau_{1\,\text{GHz}} \). The large intrinsic scatter of 0.76 dex, and the steeper slope of the relation at DM \( \gtrsim 100 \), are interpreted as evidence for clumpiness in the ionized ISM (Cordes et al. 1991, 2016). Motivated by the strong evidence for scattering in FRB 110220 presented by Thornton et al. (2013), the possibility of a \( \tau_{1\,\text{GHz}} - \text{DM} \) relation existing for FRBs putatively scattered in the intergalactic medium (IGM) was first considered by Lorimer et al. (2013). However, the possibility of any significant scattering in the IGM was disputed by Macquart & Koay (2013) and Luan & Goldreich (2014), based on their assessments of IGM turbulence.

The existence of a \( \tau_{1\,\text{GHz}} - \text{DM}_E \) relation for FRBs, where \( \text{DM}_E \) is the estimated extragalactic DM component for a given FRB, would thus imply that FRBs are predominantly scattered in the ionized medium that dominates the \( \text{DM}_E \) values. For example, if \( \text{DM}_E \) is typically dominated by contributions from the IGM, it would be
possible that FRBs are predominantly scattered in the IGM or in intervening bound systems. On the other hand, if DM$_E$ is typically dominated by host-galaxy contributions, a $\tau_{\text{1 GHz}}$–DM$_E$ relation would reflect the typical DM–$\tau_{\text{1 GHz}}$ relation in FRB host galaxies. The lack of a $\tau_{\text{1 GHz}}$–DM$_E$ relation would imply that the medium that dominates the DM$_E$ values does not significantly scatter FRBs.

Cordes et al. (2016) compared existing measurements of FRB scattering time-scales with a revised $\tau_{\text{1 GHz}}$–DM relation for Milky-Way pulsars. No evidence was found for a $\tau_{\text{1 GHz}}$–DM$_E$ relation for FRBs. However, it was shown that FRBs are typically underscattered in comparison to their values of DM$_E$, relative to Milky-Way pulsar scattering time-scales at congruent values of DM. This was interpreted either as an indication that 50–75 per cent of DM$_E$ is typically contributed by the IGM, or that FRB host galaxies have ISMs that are typically less turbulent than the ISM of the Milky Way. The possibility of FRBs being predominantly scattered in the IGM was thought less likely owing to the large levels of scattering present relative to expectations for the IGM (e.g. Macquart & Koay 2013), and the lack of a $\tau_{\text{1 GHz}}$–DM$_E$ relation.

The discovery of FRB 150807 (Ravi et al. 2016), however, significantly extended the range of FRB scattering time-scales. Although not detectably temporally broadened due to scattering, this FRB exhibited frequency scintillations that indicated a scattering strength much greater than that expected from its Milky-Way sightline. The combined measurements of low scattering and low Faraday rotation measure indicated that this FRB was most likely not scattered in ISM with turbulence and magnetization like that of the Milky Way. However, constraints on the distance to the source of FRB 150807 suggested that a significant portion of its DM$_E$ originated in the IGM.

Using my revised measurements of DM and $\tau_{\text{1 GHz}}$ for the Parkes FRB sample (Table 2), I plot $\tau_{\text{1 GHz}}$ against DM$_E$ in Fig. 4. I also show measurements for FRB 110523 (Masui et al. 2015) discovered at the Green Bank Telescope in the 700–900MHz band. For each FRB, I estimate DM$_E$ by subtracting the maximum Galactic-disc DM predicted by the NE2001 DM model (Cordes & Lazio 2002) along the FRB sightline, and by further subtracting a contribution of 30 pc cm$^{-3}$ corresponding to the Milky Way ionized-gas halo and the Local Group (e.g. Gupta et al. 2012; Dolag et al. 2015). In Fig. 4, I also plot the Milky Way $\tau_{\text{1 GHz}}$–DM$_E$ relation derived most recently by Cordes et al. (2016), and pairs of measurements of $\tau_{\text{1 GHz}}$ and DM for Milky-Way pulsars from the ATNF pulsar catalogue (Manchester et al. 2005). All pulsars with published measurements of $\tau_{\text{1 GHz}}$ are included here.

First, Fig. 4 supports the finding of Cordes et al. (2016) that FRBs are underscattered with respect to their values of DM$_E$. This is despite the differences in the actual measurements, and in the compositions of the samples, between the two analyses. Relative to the Cordes et al. analysis, I discard FRBs 121002 and 130729 due to their complex temporal and spectral structures, which may have biased previous scattering measurements, but include the new FRB 150807 and its value of $\tau_{\text{1 GHz}}$ based on the frequency scin-
tillations. The exclusion of FRBs 121002 and 130729 may bias
inferences from Fig. 4, because our ability to discern the com-
plex temporal structure relies on them not being strongly scattered.
However, any upper limits that could be placed on their scatter-
ing time-scales would correspond approximately to the narrowest
features in the burst profiles (i.e. a few milliseconds at \( \sim 1.3 \) GHz;
see Fig. 3). These in turn would be approximately consistent with
existing measurements in Fig. 4.

Fig. 4 provides tentative indications of a relation between \( \tau_{1 \text{ GHz}} \)
and \( D_{\text{ME}} \) for FRBs similar to that for Milky-Way pulsars. If
FRB 010724, which has the largest \( \tau_{1 \text{ GHz}}/D_{\text{ME}} \) ratio among the
FRB sample, is excluded, the \( \tau_{1 \text{ GHz}} - D_{\text{ME}} \) relation appears some-
what stronger. Using the BIC, I quantify the evidence for a
\( \tau_{1 \text{ GHz}} - D_{\text{ME}} \) relation by comparing linear models for the \( D_{\text{ME}} \)
and \( \tau_{1 \text{ GHz}} \) measurements, with, and without, a dependency of \( \tau_{1 \text{ GHz}} \)
on \( D_{\text{ME}} \). Consider the loglikelihood function

\[
L = \sum_i \left[ -\log(e_{i}^{2} + \epsilon^2) - \frac{(\log_{10}(\tau_{1 \text{ GHz}, i}) - M_{i})^2}{2(\epsilon_{M,i}^2 + \epsilon^2)} \right]
\]

where \( M_{i} = m \log_{10} D_{\text{ME},i} + b \) is a loglinear model for the
\( \tau_{1 \text{ GHz}} - D_{\text{ME}} \) relation with parameters \( m \) and \( b \) and intrinsic scatter
\( \epsilon \), and \( D_{\text{ME},i} \) and \( \tau_{1 \text{ GHz},i} \) are FRB measurements indexed by \( i \) with
error \( \epsilon_{i} \). I consider the difference in BIC between the maximum of
this likelihood function in the parameters \( m, b \), and \( \epsilon \), and the
maximum of the likelihood function with a fixed \( m = 0 \) (and hence
one less parameter). With the sample of eight Parkes FRBs with mea-
surements of \( \tau_{1 \text{ GHz}} \), there is no significant difference in the BICs
between the two models. However, with FRB 010724 excluded, the
difference in BICS is 8, which I consider moderately significant.
The inclusion of the upper limits on scattering time-scales does not
significantly alter these results. For the seven-FRB sample (exclud-
ing FRB 010724), I find \( m = 7 \pm 2 \) and \( b = -19 \pm 5 \); I emphasize
that these results are likely to change significantly as more scattered
FRBs are discovered.

A \( \tau_{1 \text{ GHz}} - D_{\text{ME}} \) relation for FRBs is would not be particularly
surprising, because it would simply imply that significant portions
of FRB DMs are contributed by a class of medium that has a scatter-
ing strength which scales with its column density. It is well
established that the Milky Way ISM is one such class of medium.
It is generally thought to be unlikely that FRBs are predominantly
scattered in the Milky Way itself, because they would lie along
sightlines of intolerably large \( \tau_{1 \text{ GHz}} \) for the Milky-Way DM con-
tributions. If FRBs were, however, scattered in host galaxies like the
Milky Way, approximate 75 percent of the typical FRB DM must
be contributed by an ISM that has a weak potential for scattering.
This is difficult to reconcile with the results on FRB 150807 (Ravi
et al. 2016). Note further that in this case a fair comparison be-
tween the Milky-Way DM-\( \tau_{1 \text{ GHz}} \) relation and FRB measurements
would require the values of \( \tau_{1 \text{ GHz}} \) for Milky Way sightlines to be
scaled up by a factor of three (Cordes et al. 2016), to account for the
difference in scattering geometry between the Milky Way (presum-
ably a homogeneous scattering medium along the line of sight), and
FRBs scattered in host galaxies (scattering medium concentrated
around the FRBs). Alternatively, FRBs may instead be scattered in the
ISM, or in intervening bound systems, and experience negli-
gible host-galaxy scattering. An attempt to ascertain the necessary
properties of scattering regions in the ISM and intervening systems
is beyond the scope of this work. The different scenarios for FRB
scattering will be tested when multiple scattered FRBs are localized
to individual host galaxies, and their distances thus measured, such
that the host and ISM contributions to the DM may be separately
estimated. In any scenario for the dominant contributor of FRB
DMs, a \( D_{\text{ME}} - \tau_{1 \text{ GHz}} \) implies that more (cosmologically) distinct
FRBs will be more difficult to detect.

3 FRB FLUX DENSITIES

Here, I quantify the constraints that may be placed on FRB fluences
based on an analysis of the Parkes MBR sky response. In Section 3.1,
I consider what constraints may be placed on the flux densities of
FRBs detected in individual beams of the MBR. Then, in Section
3.2, I constrain the location of the multiple-beam FRB 010724
in the Parkes focal plane using a technique similar to that applied
by Ravi et al. (2016) to the dual-beam FRB 150807. Third, in Section
3.3, I combine these analyses with the fluence estimates presented
in Table 2, and compare the resulting FRB fluence con-
straints with various specifications for the FRB fluence distribution
(the log\( N \)-log\( F \)).

3.1 Single-beam FRBs

The exact locations of single-beam FRBs within the sky-response
functions of the beams, \( \Theta(\theta, \phi) \), are unknown. Here, \( \Theta(\theta, \phi) \)
the attenuation of the FRB due to an off-axis position at polar
coordinates, \( (\theta, \phi) \), in the focal plane; for an on-axis feed, \( \Theta(\theta, \phi) \)
may be well approximated by the inverse of an Airy function. That
is, the beam attenuation factor is the inverse of the standard beam
gain pattern. By adopting models for \( \Theta(\theta, \phi) \) for the Parkes receiver,
and for the distribution of FRB fluences, it is possible to evaluate the
probable beam attenuations of FRBs detected in different beams.
I used the model for \( \Theta(\theta, \phi) \) for the Parkes MBR presented by
Ravi et al. (2016). This analytic model was found to be consistent
with measurements at the \( -20 \) dB resolution level. For each beam, I
used the model to evaluate \( \Theta(\theta, \phi) \) on a grid of \( 1000 \times 1000 \) points
spanning \( 3 \times 3 \) deg in \( \theta \) and \( \phi \). I averaged the model in frequency
across the BPSR band (\( 1182-1519.5 \) MHz); I did not find the results
in this section to vary significantly when instead using the AFB band.
Then, for the central, an inner-ring, and an outer-ring beam, I
defined the histograms of pixel values of \( \Theta(\theta, \phi) \) where the FRB
would not be detected with S/N \( > 3 \) in any other beam; I considered
S/Ns of 10 and 50 in the primary detection beams. These histograms
provided initial estimates of the probability density functions of \( \Theta \)
for FRBs detected in individual beams of the MBR.

However, FRBs are not equally likely to be detected at different
fluences or flux densities\(^4\); the specific distribution in these param-
eters is the log\( N \)-log\( F \) function. For a fluence \( F \), the number of
FRBs expected at fluences \( > F \) is typically modelled as a power
law: \( N(> F) \sim F^{-\beta} \). For some power-law index \( \beta \) (e.g. Vedantham
et al. 2016). For a uniform distribution of FRBs in Euclidean space,
\( \beta = 1.5 \). However, based on the unexpected detection of multi-
ple-beam FRBs at Parkes (FRBs 010724 and 150807), Vedantham et al.
(2016) showed that the Parkes FRB sample is consistent with \( 0.5 < \beta < 0.9 \)
(90 per cent confidence). I therefore considered \( \beta = 0.7 \) in addition to \( \beta = 1.5 \), and scaled the \( \Theta \)-histogram counts accordingly.
Finally, I used the histograms to derive the probabilities of detecting
FRBs above given values of \( \Theta \). These are plotted in Fig. 5, where I
convert values of \( \Theta \) to solid angles on the sky.

The areas on the sky within the half-power points of the Parkes
MBR beams are between 150 and 170 arcmin\(^2\). From Fig. 5, it
is apparent that single-beam FRBs in a central or middle-ring

\(^4\)In this context, fluence and flux density can be used interchangeably.
The probabilities of FRBs with different S/N values (10, red lines with filled circles; and 50, blue lines with crosses) being detected within containment regions on the sky of different sizes. I show results for log\(N\)-log\(F\) indices \(\beta = 0.7\) (solid lines) and \(\beta = 1.5\) (dashed lines), as labelled. The probabilities correspond to calculations of \(P(\Theta > \Theta_1)\) for FRBs being detected above different beam attenuation factors, \(\Theta_1\), as discussed in the text, where I provide solid angles on the sky instead of \(\Theta_1\) on the abscissa. From left to right, I show results for the central, an inner-ring, and an outer-ring beam of the Parkes MBR. The horizontal green lines indicate the 95th percentiles of the distributions.

I evaluated models for the sky-response functions of each beam, averaged over the AFB band, using the publicly available codes presented by Ravi et al. (2016). The models were evaluated, as above, on a grid of 1000 \(\times\) 1000 points spanning 3 \(\times\) 3 deg in the Parkes focal plane. I then made Monte Carlo realizations of the S/N in each beam, based on the estimated S/Ns, to calculate a containment region. For each realization, I found points in the focal plane where the ratios of S/Ns between beams 7, 12, and 13 were within a factor of four of the simulated measurements. I accounted for the difference in telescope gain between inner- and outer-ring beams. I rejected points where the burst would have been detected with S/N \(\geq 3\) in any of beams 1, 2, 3, 4, 5, 8, 9, 10, and 11, as well as rejected points where the burst would have been detected with a lower S/N in beam 6 than in any other beam. Finally, I averaged the results over 1000 realizations. I note that this analysis places no prior on the log\(N\)-log\(F\) function, unlike the analysis in Section 3.1.

The resulting 99 percent confidence containment region for FRB 010724 is 52 arcmin\(^2\) in size. This is substantially worse than the 9-arcmin\(^2\) localization of FRB 150807. This is because I do not use measurements at different frequencies for FRB 010724, whereas measurements in four sub-bands were used to localize FRB 150807. None the less, the existence of a constrained solution for the position of FRB 010724 in the Parkes focal plane adds further weight to the astrophysical nature of the event.

The results suggest that the S/Ns in beams 7, 12, and 13 should be adjusted by factors of 310 \(\pm\) 180, 510 \(\pm\) 140, and 80 \(\pm\) 40, respectively, in order to ensure a consistent fluence determination from each beam. Based on the S/N measurements, the fluence measurements for FRB 010724 in Table 2 should thus be scaled upwards by factor of 200 \(\pm\) 100. Assuming gains of 1.45 and 1.72 Jy K\(^{-1}\) for the inner- and outer-ring beams, a common system temperature of 28 K (Manchester et al. 2001), and a one-bit digitization loss factor...
The observed properties of FRBs

3.3 Astrophysical implications

The best utility of my revised fluence constraints for the Parkes FRB sample is to consider the implications for the \( \log N - \log F \). I use the fluence estimates in Table 2 for all FRBs besides 010724 and 150807, averaged over the frequency bands, and the sensitivity parameters given above, to derive minimum fluences for each FRB assuming boresight positions in the detection beams. Using the results summarized in Fig. 5, I also derive 95 per cent confidence fluence upper limits for each FRB. For FRBs 010724 and 150807, I use the constrained 1σ fluence ranges that were derived above in Section 3.2 and by Ravi et al. (2016) respectively, enabled by their multiple-beam detections. I collate the fluence measurements to derive lower and upper limiting empirical \( \log N - \log F \) distributions, which are displayed in Fig. 6.

In the figure, I also show various \( \log N - \log F \) functions of index \(-0.7\), which was the value inferred by Vedantham et al. (2016), and of index \(-3/2\), which corresponds to a uniform distribution of sources in Euclidean space. In comparing the empirical distributions with the assumed intrinsic power-law \( \log N - \log F \) functions, a number of selection effects must be recognized. First, the data in Fig. 6 are comprised of FRBs detected with both the BPSR and AFB instruments; FRBs detected with the AFB are indicated by red arrows. The differing sensitivities of these instruments, attributable to different numbers of bits in the analogue-to-digital conversion, the different bandwidths, and different integration times, mean that the instruments are fluence incomplete (Keane & Petroff 2015) below different thresholds. This threshold is \( \approx 2 \) Jy ms for BPSR, and \( \approx 3 \) Jy ms for the AFB. Second, it is possible that the FRB rate varies with Galactic latitude (Petroff et al. 2014; Burke-Spolaor & Bannister 2014). Consequently, different sky radiation temperatures result in different sensitivities for different pointings. The combination of FRB detections from varied searches, even with the BPSR instrument, may therefore result in a biased estimate of the sky-averaged FRB \( \log N - \log F \) function. Given these issues, and factor of \( \sim 5 \) uncertainty in the flux-density values, I concur with Keane & Petroff (2015) and Vedantham et al. (2016) that it is not useful to attempt to use the fluence measurements to directly estimate the FRB \( \log N - \log F \).

4 TYPE I, TYPE II, . . . , TYPEN FRBS

In this paper, I have focused on the Parkes FRB sample to ensure a consistent sample selection in my analysis. This is possible in particular with those FRBs detected with the BPSR instrument at Parkes. However, even within the sample of FRBs detected with BPSR, a distinction may be made between those FRBs that are consistent with the simple temporal structures in my Models 0–3, and the more complex structures seen in FRBs 121102 and 130729. Another distinction may be made between those Parkes FRBs that show signatures of scattering at levels stronger than expected from their passage through the Milky Way, and those that do not. In a broader context, the repeating nature of FRB 121102 is, prima facie, unique among FRBs.

Unfortunately, it appears difficult at present to distinguish between an entirely homogeneous population of FRB sources, FRB sources that are physically similar but which vary in their emission properties, and multiple independent populations of FRB sources. A unified class of FRB emitters must fulfill the following: (i) they must be able to emit pulses at frequencies between 700 MHz (Masui et al. 2015) and 8 GHz (Gajjar et al. 2018), (ii) they may lie behind plasma regions with either significant or minor scattering strength, and (iii) they must be capable of producing multiple pulses with a variety of morphologies and luminosities that vary by a few orders of magnitude. By assessing the follow-up observations of Parkes FRBs with respect to the empirical statistics of the FRB 121102 repeats, Palaniswamy, Li & Zhang (2018) showed that it is highly unlikely that the Parkes FRBs are comparable to FRB 121102 in either the repeat rate, pulse-fluence distribution, or both. Additionally, if the FRB population is at cosmological distances, and FRB DM\(_E\) values can be related to distance, it is somewhat unexpected that the one object detected at Arecibo should have a lower redshift than may be inferred for the Parkes FRBs given the greater sensitivity of Arecibo.

The question of whether FRB 121102 is truly unique with respect to the Parkes FRB sample can be addressed by considering the following: given the relative amounts of time surveyed by Parkes and Arecibo for FRBs, how many more/less repeating FRBs should Parkes have detected as compared with Arecibo? Similar analyses have been conducted by Scholz et al. (2016) and Oppermann, Connor & Pen (2016), who assumed that FRB 121102 and the Parkes FRBs are drawn from the same population, and thus found consistency between the detection rates at both telescopes for a uniformly distributed, Euclidean-space population. However, the following analysis is subtly different. Instead of testing for consistency be-
In the same units, and for a flux density given by $13.6$ number of detections above this level at Parkes is proportional to

\[
N_{\text{Parkes}}(\theta) \propto \int_0^\theta \sin \theta B_{\text{PKS}}(\theta) d\theta \times (258 \text{ d}) \times (13 \text{ beams}).
\]

In the same units, and for a flux density given by $[13.6 \times B_{\text{AO}}(\theta)]^{-1}$, the number of detections above this level at Arecibo is

\[
N_{\text{AO}}(\theta) \propto \int_0^\theta \sin \theta [13.6 \times B_{\text{AO}}(\theta)]^{1/2} d\theta \times (36.9 \text{ d}) \times (7 \text{ beams}).
\]

I plot $N_{\text{PKS}}/N_{\text{AO}}$ in Fig. 7 for different FRB flux densities, assuming FRB durations of 3 ms (corresponding to the duration of the first-detected pulse from FRB 121102) and a Parkes MBR system-equivalent flux density of 40 Jy (Keith et al. 2010). For example, if FRB 121102 always emitted 1-Jy pulses of 3-ms duration, like its first-detected pulse accounting for its detection in a primary-beam sidelobe, the fact that Arecibo has detected one such object implies that the HTRU and SUPERB surveys should expect to have detected three similar objects. If instead FRB 121102 always emitted pulses of flux density 0.3 Jy, Parkes should expect to have detected just one such object.

Using this analysis to determine the expected number of objects like FRB 121102 in the Parkes surveys, and likely within the existing sample of Parkes FRBs, depends on how the characteristic $L$-band flux density (or fluence) of FRB 121102 is specified. Of the repeat bursts from FRB 121102 detected at $L$ band with Arecibo and published by Spiteri et al. (2016) and Scholz et al. (2016), only one (burst 11) likely lies above the Parkes detection threshold. It would hence have easily been possible for the first-detected burst from FRB 121102 to be below the 0.3-Jy threshold in Fig. 7 where no Parkes detections are expected given an Arecibo detection. An exact assessment of the characteristic flux density or fluence of FRB 121102 requires a better determination of the distributions of these quantities among its pulses, as well as of the statistics of the temporal clustering (Spiteri et al. 2016).

The effects of Galactic interstellar scintillation on this analysis are potentially important in some regions of the sky. The transition frequency, $\nu_t$, between the strong- and weak-scattering regimes for the position of the host of FRB 121102 is $\nu_t = 37.9$ GHz (Cordes & Lazio 2002; Chatterjee et al. 2017). As the fractional diffractive scintillation bandwidth scales as $(\nu/\nu_t)^{17/5} = 0.15$ at $\nu = 1.4$ GHz; this is also negligible, in particular given the uncertainty in specifying the characteristic flux density of FRB 121102 discussed above. At Parkes, the HTRU and SUPERB surveys cover the sky outside the Galactic plane (Galactic latitudes $|b| > 15$ deg for the HTRU survey, Keith et al. 2010; Champion et al. 2016) in an unbiased sense. Approximately 20 per cent of the sky has $\nu_t \lesssim 1.4$ GHz (Walker 1998; Cordes & Lazio 2002), and the Parkes surveys are therefore generally in the strong scattering regime. Given the wide fractional bandwidth of the Parkes receiving system ($\sim 25$ per cent), and the $\sim 10$ per cent occupation fraction of diffractive scintles (Cordes & Lazio 1991), values of $1 \lesssim \nu_t \lesssim 4$ GHz are required for modulation indices of order unity due to diffractive scintillation. This occurs across $\sim 30$ per cent of the sky (Walker 1998; Cordes & Lazio 2002). Refractive scintillations are a more generally dominant effect on Parkes FRB detections, with typical modulation indices of $\sim 0.5$. The probability density function of refractive-scintillation intensity variations is only mildly skewed (Rickett, Coles & Bourgeois 1984), in contrast to the exponential intensity variations of diffractive scintillations. Hence, besides the regions of the sky where diffractive scintillations dominate, the expectation for the number of objects like FRB 121102 present in the Parkes surveys will not be very sensitive to the effects of scintillation. Indeed, co-opting the argument of Macquart & Johnston (2015), scintillation may cause a boost in the number of objects like FRB 121102 detected at higher Galactic latitudes by Parkes, relative to my analysis.

Therefore, the best interpretation of Fig. 7 that can be presented here is that the HTRU and SUPERB surveys at Parkes could expect to contain up to three analogues of FRB 121102, if these analogues,
presumably less distant than FRB 121102, lie above the Parkes detection threshold. The local-Universe location of these analogues suggests that the log–logF of this population is unlikely to be flatter than F−3/2, as I have assumed in producing Fig. 7. The best candidate analogues of FRB 121102 among the Parkes sample are clearly FRBs 121002, 130729, and possibly 140514. Like the pulses from FRB 121102, these Parkes FRBs show complex temporal structure, and in the cases of FRBs 130729 and 140514, spectral structures concentrated in ≈100 MHz bands.

5 CONCLUDING DISCUSSION

I return first to the question of how an FRB may be defined. All FRBs are fundamentally bursts of radio waves which exhibit levels of dispersion that exceed predictions for the Milky-Way ionized ISM column density along their specific sightlines. Beyond this, FRBs exhibit a broad diversity of (dedispersed) durations, scattering signatures, flux densities, and intrinsic temporal and spectral structures. In this paper, I have presented an analysis of the individual properties of the sample of 17 FRBs detected at the Parkes telescope with the 13-beam L-band receiver. Eight of these FRBs show signatures of scattering at levels significantly greater than expected from the Milky Way, with scattering time-scales at 1 GHz ranging between 0.005 and 32ms. After accounting for the scattering, only five Parkes FRBs have pulse widths that are greater than expected from intrachannel smearing caused by their dispersions. The fluences of the Parkes FRB sample span a range greater than 0.7–400 Jy ms.

My analysis highlights the utility of searching for FRBs with systems that may better resolve the intrinsic pulse durations, because a substantial fraction of FRBs (6/17 at Parkes) are temporally unresolved. Such systems would require finer filterbank channel widths and better time resolutions than currently available, which could be achieved using coherent dedispersion techniques or observations at frequencies above the L band. Better temporal resolution will also provide a boost in S/N for short-duration FRBs. Higher frequency observations have the added bonus of being less affected by the temporal broadening observed in 7/17 Parkes FRBs; the characteristic spectra of FRBs are poorly constrained, and the repeating FRB 121102 has been observed at frequencies up to 5 GHz. Avoiding the effects of scattering may again provide a boost in S/N because of shorter pulse durations, and may indeed provide sensitivity to a population of FRBs that are too broad to be detected in the L band. Conversely, the effects of scattering must be taken into account in predicting FRB detection rates for lower frequency experiments such as the Canadian Hydrogen Intensity Mapping Experiment (e.g. Ng et al. 2017) and the Hydrogen Intensity and Real-time Analysis Experiment (Newburgh et al. 2016).

On the other hand, a search for long-duration FRBs at all frequencies may also be fruitful. Although the number of false candidates in single-dish observations increases rapidly with increasing pulse duration (Burke-Spolaor & Bailes 2010), and the detection S/N decreases as the square root of the duration for constant fluence, such a search could be carried out by a sensitive interferometric system such as those being commissioned for the Jansky Very Large Array. There appears to be no reason to expect all FRBs to have the ‘millisecond’ duration often quoted in the literature, beyond the effects of intrachannel dispersion smearing and scattering, and the increased sensitivity to narrower pulses.

My revised estimates of FRB scattering time-scales, τ1 GHz, reveal moderate evidence for a relation between τ1 GHz and the extragalactic DM (DMg), similar to that observed for pulsars in the Milky Way (Fig. 4). The one outlier is FRB 010724, which has τ1 GHz = 25 ± 5 ms for a low DMg = 288 pc cm−3. The existence of such a relation, if supported by further observations, suggests that FRBs are predominantly dispersed in a medium within which they are also scattered, and for which the scattering strength increases for larger DM. This medium could be the ISM of FRB host galaxies, which would imply modest FRB distances, or the IGM or intervening collapsed systems. Observations of scattering in FRBs with distance measurements, obtained for example through localization and the identification of host galaxies, could resolve the nature of the scattering and dispersing medium.

Although it appears that Parkes FRBs detected in individual beams of the multibeam receiver can have their fluences constrained to within a factor of five with 95 per cent confidence, this is insufficient to directly estimate the FRB flux-density distribution (log–logF). My analysis is therefore unable to distinguish between the case of a uniform distribution of FRB sources in the nearby Universe, and the flatter log–logF distribution expected for a cosmological or evolving FRB population.

Finally, although the repeating FRB 121102 is an outlier among the FRB population in its repeat rate and the low fluences of most of its bursts, it is not demonstrably unique in its class of progenitor. The rate of repeats within the Parkes FRB population is lower than that of FRB 121102, and most Parkes FRBs have simpler temporal and spectral structures. However, some Parkes FRBs are similar in their morphologies to bursts from FRB 121102, and statistical arguments suggest that it is possible that up to three objects like FRB 121102 have already been detected in surveys at Parkes. In a broader context, it is quite possible for all FRBs to be emitted by the same class of astrophysical object, but for such objects at different evolutionary stages to emit FRBs with different luminosity functions and rates.

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REFERENCES

Chatterjee S. et al., 2017, Nature, 541, 58

https://caseyjlaw.github.io/realfast/
APPENDIX A: A SIGNAL MODEL FOR FRBS

In this section, I summarize the signal model for the Parkes FRBs analysed in this paper, and point out specific assumptions that I make. The voltage signal, $V$, presented to the AFB and BPSR back-ends at time $t$ can be represented as follows:

$$V(t) = N(t) + h_{IM}^+ F(t), \quad (A1)$$

where $N(t)$ is the receiver noise contribution, $h_{IM}(t)$ is a filter that encapsulates the effects of the ISM and IGM on the signal, and $F(t)$ is proportional to the measured time-varying electric field of the FRB in a single polarization. I assume that the signal is unpolarized, although this is not particularly relevant to my work. I assume that samples of the receiver noise $N(t)$ can be described by a time-stationary normal distribution, with zero mean and variance $\sigma^2_N$ (i.e. $N(0, \sigma^2_N)$). This assumption neglects the potential effects of RFI. The FRB signal can be expressed as $S(t) = A(t)M(t)$, where $A(t)$ is an amplitude envelope, and $M(t)$ is again Gaussian with distribution $N(0, \sigma^2_M)$. I further assume that $\sigma_M \ll \sigma_N$; that is, I do not account for ‘self-noise’ in estimates of FRB properties because FRBs typically contribute negligibly to the system temperature (although see Ravi et al. 2016). Finally, I note that $V(t)$ is bandlimited, and thus correlated on short time-scales.

To illustrate my assumptions for the ISM/IGM effects, consider the Fourier transform of $V(t)$:

$$\tilde{V}(v) = \tilde{N}(v) + \tilde{h}_{IM} \tilde{S}(v), \quad (A2)$$

where a tilde indicates a frequency-domain quantity. I assume that the ionized-medium filter $\tilde{h}_{IM}$ can be expressed as the product of the standard cold, sparse plasma dispersion kernel, $\tilde{h}_{IM}$ (Hankins 1971), and the PBF caused by multipath propagation, $\tilde{h}_{PBF}$. That is,

$$\tilde{h}_{IM} = \tilde{h}_{IM}^+ \tilde{h}_{PBF}. \quad (A3)$$

The assumption that $\tilde{h}_{IM}^+$ and $\tilde{h}_{PBF}$ are separable is valid for most, although perhaps not all, pulsars in the Galaxy (Cordes, Shannon & Stinebring 2016). I assume a one-sided exponential form for the PBF in the time domain, corresponding to the thin-screen scattering model (Cronyn 1970), wherein

$$\tilde{h}_{PBF}(t) = e^{-t/\tau} H(t)n(t), \quad (A4)$$

where $\tau$ is the scattering time-scale, $H(t)$ is the Heaviside step function, and $n(t)$ is a standard-normal random process.

The AFB and BPSR hardwares are used to estimate the signal power at specific frequencies, $v_0$, within bandwidths $\Delta v$ and times $\Delta t$. I model this as follows:

$$\tilde{S}(v_0, t) = \int_{t-\Delta t/2}^{t+\Delta t/2} |g(t') \ast V(t')|^2 dt', \quad (A5)$$

where $g(t')$ is the time-domain representation of the filter corresponding to a single filterbank channel. I assume the following form for the frequency-domain filter:

$$\tilde{g}(v) = \sqrt{\frac{2}{\pi \Delta v^2}} e^{-2(v-v_0)^2/\Delta v^2}. \quad (A6)$$

That is, I assume that the response of each filterbank channel is a Gaussian function with a standard deviation of $\Delta v/2$. Although this model does not accurately represent the responses of the analogue filters of the AFB or the polyphase-filterbank channels of BPSR, it appears adequate given the quality of the FRB data. The characteristic impulse-response time-scale of the estimates of $\tilde{S}(v_0, t)$ is therefore $1/\Delta v$; for both the AFB and BPSR, $\Delta t \gg 1/\Delta v$.

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