

Abundances in Stars from the Red Giant Branch Tip to the Near the Main Sequence Turn Off in M71: II. Iron Abundance ¹

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ABSTRACT

We present [Fe/H] abundance results that involve a sample of stars with a wide range in luminosity from luminous giants to stars near the turnoff in a globular cluster. Our sample of 25 stars in M71 includes 10 giant stars more luminous than the RHB, 3 horizontal branch stars, 9 giant stars less luminous than the RHB, and 3 stars near the turnoff. We analyzed both Fe I and Fe II lines in high dispersion spectra observed with HIRES at the W. M. Keck Observatory. We find that the [Fe/H] abundances from both Fe I and Fe II lines agree with each other and with earlier determinations. Also the [Fe/H] obtained from Fe I and Fe II lines is constant within the rather small uncertainties for this group of stars over the full range in T_{eff} and luminosity, suggesting that NLTE effects are negligible in our iron abundance determination. In this globular cluster, there is no difference among the mean [Fe/H] of giant stars located at or above the RHB, RHB stars, giant stars located below the RHB and stars near the turnoff.

Subject headings: globular clusters: general — globular clusters: individual (M71) — stars: evolution – stars:abundances

1. INTRODUCTION

Abundance determinations of stars in Galactic globular clusters can provide valuable information about important astrophysical processes such as stellar evolution, stellar structure, Galactic chemical evolution and the formation of the Milky Way. Surface stellar abundances of C, N, O, and often Na, Mg, and Al are found to be variable among red giants within a globular cluster. The physical process responsible of these star-to-star element variations is still uncertain (see Cohen *et al.* 2001, Paper I).

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Of particular importance to the present study are the results of King *et al.* (1998), who found that $[\text{Fe}/\text{H}]$ among M92 subgiants is a factor of two smaller than $[\text{Fe}/\text{H}]$ from red giants in the same cluster (Cohen 1979; Sneden *et al.* 1991). If this result is not due to systematic differences arising from the analysis procedures of the different groups that handle the red giant branch (RGB) and the subgiant samples, then the results of King *et al.* (1998) would suggest some modification of photospheric Fe abundances which would be quite difficult to explain. Clearly the present day clusters stars are incapable of modifying their own Fe abundances through nucleosynthesis. Yet evolution-driven changes in $[\text{Fe}/\text{H}]$ could be possible if the outer envelopes of the subgiants were somehow infused with Fe-poor external material. Thus as evolution progresses up the RGB the deepening convective envelope would dilute the photospheric $[\text{Fe}/\text{H}]$ with more Fe-rich “unmodified” material from the interior causing an increase in $[\text{Fe}/\text{H}]$ with luminosity. We note the unlikelihood of this scenario as Fe, unlike the lighter elements, is not involved in normal mass transfer processes that might occur in binary systems or in normal stellar winds, and is only produced in supernovae. Moreover, it is difficult to understand how cluster stars could be contaminated by material with *less* Fe, presumably at a time after the present subgiants had formed.

In order to study the origin of the star-to-star abundance variations and to address the issues raised by King *et al.* (1998), we have started a program to determine chemical abundances of the nearer galactic globular cluster stars. In this paper, we present our results for the iron abundance of M71, the nearest globular cluster reachable from the northern hemisphere. Similar programs are underway at ESO by Castilho *et al.* (2000) and Gratton *et al.* (2001) taking advantage of the fact that the nearest globular cluster accessible from a southern site (NGC 6397) is 1.8 times closer than M71 and has a lower reddening. Our M71 sample includes stars over a large range in luminosity: 19 giant stars, 3 horizontal branch stars, and 3 stars near the main sequence turnoff, in order to study in a consistent manner red giants, horizontal branch stars, and stars at the main sequence turnoff. Details on the star sample, observations, data reduction and determination of stellar parameters are described in Paper I. Previous high dispersion abundance analysis for M71 involve studies of red giants only, resulting in $[\text{Fe}/\text{H}]$ of -0.70 (Cohen 1983), -0.80 (Gratton *et al.* 1986), between -0.6 and -1.0 (Leep *et al.* 1987), and -0.79 (Sneden *et al.* 1994).

2. ANALYSIS

We begin our analysis with Fe, as many Fe lines are identified in our HIRES spectra over a wide range of excitation potentials and line strengths, as well as over two ionization states (Fe I and Fe II). The iron abundance analysis is done using a current version of the LTE spectral synthesis program MOOG (Sneden 1973). A line list specifying the wavelengths, excitation potentials, g_f -values, damping constants, and equivalent widths for the observed Fe I and Fe II lines is required. The provenance of the g_f -values and the measurement of equivalent widths are discussed below. The damping constants for all Fe I and Fe II lines were set to twice that of the Unsöld approximation for van der Waals broadening following Holweger *et al.* (1991). The use of the Blackwell approximation

for the damping constants gives the same result within the errors, when comparing $[\text{Fe}/\text{H}]$ obtained with the “good line set” of Fe I (see definition of line sets on Sec. 2.2).

In addition, a model atmosphere for the effective temperature and surface gravity appropriate for each star and a value for the microturbulent velocity are also required. We use the grid of model atmospheres from Kurucz (1993b) with a metallicity of $[\text{Fe}/\text{H}] = -0.5$ dex, based on earlier high dispersion abundance analysis of M71 red giants (Cohen 1983; Gratton *et al.* 1986; Leep *et al.* 1987; Sneden *et al.* 1994). The final result for $[\text{Fe}/\text{H}]$ is not sensitive to small changes in the metallicity of the model atmosphere. In particular, the error introduced by using a model with $[\text{Fe}/\text{H}] = -0.5$ instead of -0.7 dex is very small (see Tables 2 & 3). The effective temperatures and surface gravities are derived from the photometry of the stars as described in Paper I. The error in the photometric T_{eff} is 75 K for giants and 150 K for the dwarfs and the error in the photometric $\log(g)$ is 0.2 dex (Paper I). The microturbulent velocity is derived spectroscopically (see below). The stellar parameters are listed in Table 1.

2.1. Transition Probabilities

Transition probabilities for the Fe I lines were obtained from several laboratory experiments, including studies of Fe I absorption lines produced by iron vapor in a carbon tube furnace (Blackwell *et al.* 1979, 1982a,b, 1986) (Oxford Group), measurement of radiative lifetimes of Fe I transitions by laser induced fluorescence (O’Brian *et al.* 1991; Bard *et al.* 1991; Bard & Kock 1994), Fe I emission line spectroscopy from a low current arc (May *et al.* 1974), and emission lines of Fe I from a shock tube (Wolnik *et al.* 1971). We also considered solar gf -values from Thévenin (1989, 1990) when needed.

We compare the gf -values obtained by the different experiments in an attempt to place them onto a common scale with respect to the results from O’Brian *et al.* (1991), who provided the longest list of gf -values. We considered for the comparison only the set of lines present in our data, which have a wavelength coverage roughly from 5380 Å to 7900 Å. We found that the values of O’Brian *et al.* (1991) and of the Oxford Group were on the same scale; the mean difference in $\log(gf)$ between the two experiments is 0.02 ± 0.01 for 21 lines in common. Similar results are found when considering 21 lines in common between O’Brian *et al.* (1991) and Bard *et al.* (1991) (see also Bard & Kock 1994), where the mean difference in $\log(gf)$ is 0.02 ± 0.04 . Considering 34 lines in common between O’Brian *et al.* (1991) and May *et al.* (1974), the mean difference in $\log(gf)$ is 0.03 ± 0.03 . When comparing the 14 lines in common between O’Brian *et al.* (1991) and Wolnik *et al.* (1971) we found a mean difference in $\log(gf)$ of -0.07 ± 0.02 . We also compared the results from O’Brian *et al.* (1991) with solar gf -values obtained by Thévenin (1989, 1990). We found that the mean difference in $\log(gf)$ is $+0.05 \pm 0.02$ when comparing 68 lines in common between these latest works. Similar offsets are found by Lambert *et al.* (1996).

The gf -values for our Fe I lines were taken when possible from laboratory data in the following

order of priority: from O’Brian *et al.* (1991), from the Oxford Group, from May *et al.* (1974), and from Wolnik *et al.* (1971) corrected by -0.07 dex. In the cases where no laboratory data were available, we used solar gf-values from Thévenin (1989, 1990) corrected by $+0.05$ dex.

Transition probabilities for the Fe II lines were taken from the solar analysis of Blackwell *et al.* (1980), Biémont *et al.* (1991), and from the semiempirical calculations of Kurucz (1993b). While restricting ourselves to lines present in our spectra, we compared the gf-values from Blackwell *et al.* (1980) and Kurucz (1993b) to the study of Biémont *et al.* (1991). There are 9 lines in common between Biémont *et al.* (1991) and Blackwell *et al.* (1980). The mean difference between the two in $\log(gf)$ is 0.14 ± 0.02 . A similar offset was found by Lambert *et al.* (1996). We found no significant difference between the results of Biémont *et al.* (1991) and Kurucz (1993b), since the 9 lines in common result in a mean difference of 0.03 ± 0.02 .

The gf-values for our Fe II lines were taken in the following order of priority: from Biémont *et al.* (1991), from Blackwell *et al.* (1980) corrected by 0.14 dex, and from Kurucz (1993b).

2.2. Measurement of Equivalent Widths

Our sample contains many stars observed in multiple orders, with many detectable absorption features in these high S/N spectra. For example, in the coolest M71 star in our sample, M71-1-45, 1407 absorption lines have been identified. A FORTRAN code to automatically search for absorption features and measure their equivalent width (W_λ), EWDET, was developed for this project. The code is available upon request to SVR. EWDET determines the continuum location of the HIRES spectra by fitting a curve to the spectra performing several iterations of point rejection above and below sigma levels given by the user. Then, EWDET identifies lines above the noise level defined by a factor of two of the continuum rms dispersion. Each of the identified lines is fit by a Gaussian profile and then the W_λ are computed by the integration of the fitted Gaussian. The error in W_λ is computed by adding quadratically the error at each point of integration, σ_i , times the step of the integration. The error at each point of integration is given by:

$$\sigma_i^2 = g(\lambda_i)^2 \times \left[\frac{\sigma_P^2}{P^2} + \frac{(\lambda_i - \lambda_{cen})^2}{\sigma^4} \sigma_{\lambda_{cen}}^2 + \frac{(\lambda_i - \lambda_{cen})^4}{\sigma^6} \sigma_\sigma^2 + \sigma_{cont}^2 \right]$$

where $g(\lambda_i)$ is the Gaussian profile, P is the peak of the Gaussian, σ_P is the error in the peak of the Gaussian, λ_{cen} is the central wavelength of the Gaussian, $\sigma_{\lambda_{cen}}$ is the error in the central wavelength, σ is the dispersion of the Gaussian, σ_σ is the error in the dispersion of the Gaussian, and σ_{cont} is the error in the continuum. The errors of the Gaussian parameters are from the covariance matrix of the Gaussian fit. The expression for the error in W_λ is deduced by propagating the errors of the Gaussian parameters and assuming that the continuum level is equal to one (see Appendix). The fit by a Gaussian profile is reasonable even for the strongest lines we use, as shown in Figure 1, where the observed line is plotted with a solid curve and its corresponding Gaussian profile fit is shown with a dashed curve.

The line list identified and measured by EWDET is then correlated to the line list with the atomic parameters to specifically identify the Fe I and Fe II lines. The detailed lists of W_λ and gf -values will be given in the next paper.

The spectral resolution, $\lambda/\Delta\lambda$, of an echelle is fixed, unlike a low incidence, angle of low order grating spectrograph where $\Delta\lambda$ is constant, independent of λ . Hence a line of constant central depth, D , will have an equivalent width proportional to λD . We construct the relationship between λD and W_λ for the Fe I lines to look for possible blends and for saturation effects. The λD versus W_λ relation for three stars are plotted in Figure 2; M71-I is one of the most luminous and coolest stars of our sample, M71-G53476_4543 is a medium luminosity and temperature star, and M71-G53392_4624 is one of the faintest and hottest stars of the sample. We fit a second order polynomial to the λD – W_λ relationship for each star, performing several iterations of point rejection above and below the two sigma level. The second order term is needed to account for line saturation at large W_λ and the rejection of points is needed to eliminate blended lines. The second order fit is plotted as a solid line in Figure 2, and the points considered for such a fit are shown in black.

For Fe I, we use two sets of lines. The first set, subsequently called “the weak line set”, contains those Fe I lines which are within two sigma levels of the λD – W_λ fit, have $W_\lambda < 60 \text{ m}\text{\AA}$, and have errors less than a third of the W_λ . This set of lines produces a sample of the best weak Fe I lines with the most accurate W_λ and the abundances derived using them will have a minimal dependence on the choice of microturbulent velocity. The second set, subsequently called “the good line set”, consists of all the Fe I lines with errors less than a third of the W_λ and with W_λ computed from the fit for λD – W_λ determined for each star. In future papers, the W_λ of lines of other elements will be determined in the same manner as the Fe I lines of “the good line set”. This way a consistent comparison can be done among the resulting abundances without a restriction on the strength of the lines used. The “weak line set” is different for each star. Actually the weak lines for the stars near the main sequence are no longer weak for the cooler stars in our sample. We compare the results from 20 lines common to 15 stars over almost the whole range in T_{eff} with the results from the “weak line set”; there is no difference within the errors, nor a trend in T_{eff} .

For Fe II, the W_λ of the lines are also determined using the fit to the λD – W_λ relation of the Fe I lines of “the good line set”. The Fe II lines follow the relationship determined from Fe I lines well, as shown in Figure 3. Additional Fe II lines, not picked up automatically, were measured by hand for the stars near the turn off and for M71-G53425_4612 and M71-G53457_4709. The set of W_λ for the hand selected Fe II lines is computed from the λD – W_λ relation of the Fe I lines, after determining their observed depth from the spectra.

The number of Fe I lines, for both sets of lines, and the number of Fe II lines utilized in this analysis are listed in Table 1.

2.3. Spectroscopic Effective Temperature

The effective temperature (T_{eff}) of a star can be determined spectroscopically by requiring the abundance to be independent of the lower excitation potential. This technique can be applied to 20 of our stars where we have Fe I lines with enough range in lower excitation potential to do so. For the spectroscopic T_{eff} determination we are using “the weak line set” of Fe I lines, because its resulting abundance and spectroscopic T_{eff} will be only weakly dependent on the choice of microturbulent velocity. We find that the spectroscopic T_{eff} is in good agreement with the photometric T_{eff} derived in Paper I, as shown in Figure 4. The solid line in Figure 4 shows the ideal case when the spectroscopic and the photometric T_{eff} are equal. The scatter around the solid line is about 150 K, which is comparable to the error of the photometric T_{eff} of 75 K for giants and of 150 K for dwarfs (Paper I), also shown in Figure 4. The scatter around the solid line is symmetric, not above or below, indicating the lack of systematic effects with the photometric temperatures.

2.4. Microturbulent Velocity

The microturbulent velocity (ξ) of a star can be determined spectroscopically by requiring the abundance to be independent of the strength of the lines measured as the equivalent width. We apply this technique for both sets of Fe I lines. The resulting ξ and the [Fe/H] computed with it for “the weak line set” of Fe I lines are listed in Table 1. Only 18 of our stars have enough weak Fe I lines to derive ξ spectroscopically. We also compute ξ using all the good Fe I lines for 20 of our stars. The difference of the resulting [Fe/H] computed with the derived ξ for the two set of lines is plotted with respect to T_{eff} in Figure 5. The mean difference is -0.004 ± 0.011 , hence, as expected, the [Fe/H] results from both sets of lines show a very good agreement.

The relationship between ξ determined for the set of all good Fe I lines and the photometric T_{eff} is shown in Figure 6. The solid line corresponds to a linear least squares fit of the data, excluding the red horizontal branch (RHB) stars, marked with circles. The best fit line is given by:

$$\xi = 3.30 - 4.66 \times 10^{-4} \times T_{eff}$$

The scatter around the solid line is about 0.2 km s^{-1} , which is a reasonable estimation of the error in ξ . For the rest of the analysis, we will use the set of all the good Fe I and Fe II lines, with ξ computed from the ξ - T_{eff} fit. For the RHB stars we use a value of 1.61 km s^{-1} , which corresponds to the mean value determined for the three RHB stars. The microturbulent velocity used for our stars is listed in Table 1.

3. RESULTS

Given the stellar parameters from Table 1, we determined the iron abundance using the equivalent widths of all the good Fe I and Fe II lines identified in the HIRES spectra. We employ the

grid of stellar atmospheres from Kurucz (1993b) to compute the iron abundance using the four stellar atmosphere models with the closest T_{eff} and $\log(g)$ to each star’s parameters. The $[\text{Fe}/\text{H}]$ listed in Table 1 is an interpolation of the results from the closest stellar model atmospheres to the appropriate T_{eff} and $\log(g)$ for each star.

3.1. $[\text{Fe}/\text{H}]$ from Fe I lines

The results of $[\text{Fe}/\text{H}]$ from Fe I lines are listed in column 9 of Table 1 and plotted against the photometric T_{eff} in Figure 7a. T_{eff} is used for the x-axis as a convenient parameter for characterizing the position of the stars in the color-magnitude diagram as it also ranks the stars in luminosity (except for the RHB stars). The errors listed in Table 1 correspond to the larger of the statistical uncertainty, given by the standard deviation of the iron abundance from different lines divided by the square root of the number of lines, or a minimum value of 0.03 dex. These errors are lower limits to the actual uncertainties in the abundances, since they do not include uncertainties due to the stellar parameters nor any systematic effects that might be present. We estimate the sensitivity of $[\text{Fe}/\text{H}]$ derived from Fe I lines with respect to the stellar parameters in three cases 4250/1.0/1.0, 5000/2.5/1.0 and 5500/4.0/1.0, where the three numbers correspond to $T_{eff}/\log(g)/\xi$. The results are listed in Table 2, where the range adopted for each parameter is representative of its uncertainty. Our determination of $[\text{Fe}/\text{H}]$ from Fe I lines is most sensitive to errors in T_{eff} , which is less than ~ 0.1 dex for ΔT_{eff} of ± 100 K, and have a minimal sensitivity on the choice of metallicity of the model atmosphere grid for plausible changes in $[\text{Fe}/\text{H}]$ (± 0.2 dex).

The solid line, shown in Figure 7a, is a linear fit weighted by the errors of $[\text{Fe}/\text{H}]$ versus T_{eff} . The slope of the fit is $(-0.8 \pm 3.6) \times 10^{-5}$ dex/K, which is consistent with $[\text{Fe}/\text{H}]$ being constant, independent of T_{eff} (ie, of luminosity or equivalently position in the color-magnitude diagram). We divide our sample in four groups of stars: giant stars at or above the RHB, stars on the RHB, giant stars below the RHB, and main sequence stars near the turnoff. The mean $[\text{Fe}/\text{H}]$ for each group is listed on Table 4. We found no significant difference in the mean $[\text{Fe}/\text{H}]$ obtained from Fe I lines among the defined groups of stars.

The mean $[\text{Fe}/\text{H}]$ weighted by the errors of all 25 stars is -0.71 ± 0.08 , in very good agreement with earlier determinations (Cohen 1983; Gratton *et al.* 1986; Leep *et al.* 1987; Sneden *et al.* 1994).

3.2. $[\text{Fe}/\text{H}]$ from Fe II lines

The determinations of $[\text{Fe}/\text{H}]$ from Fe II lines are listed in column 11 of Table 1 and plotted against the photometric T_{eff} in Figure 7b. The errors listed in Table 1 corresponds to the statistical uncertainty or a value of 0.05 dex, whichever is larger. We estimate the sensitivity of $[\text{Fe}/\text{H}]$ derived from Fe II lines with respect to the stellar parameters in the same manner as the sensitivity of $[\text{Fe}/\text{H}]$ from Fe I lines. The results are listed in Table 3, where the range adopted for each parameter is

representative of its uncertainty. We see a stronger sensitivity on the stellar parameters from the Fe II lines than from the Fe I lines. The [Fe/H] determination from Fe II lines is most sensitive to the systematic error (note that the internal uncertainty in $\log(g)$ is ≤ 0.1 dex) in $\log(g)$, as well as to T_{eff} among the coolest M71 giants. The sensitivity on the choice of metallicity of the model atmosphere grid is small for reasonable changes in metallicity.

The solid line, shown in Figure 7b, is a linear fit weighted by the errors of [Fe/H] versus T_{eff} . The slope of the fit is $(+3.1 \pm 5.2) \times 10^{-5}$ dex/K, which is consistent with [Fe/H] being constant, independent of T_{eff} . We found that there is no significant difference in the mean [Fe/H] obtained from Fe II among stars from different luminosity groups, listed in Table 4. The mean [Fe/H] weighted by the errors is -0.84 ± 0.12 , in very good agreement with our result from Fe I lines and earlier determinations (Cohen 1983; Gratton *et al.* 1986; Leep *et al.* 1987; Sneden *et al.* 1994).

3.3. NLTE effects

The iron abundance could be affected by departures from LTE. The main NLTE effect in late-type stars is caused by overionization of electron donor metals by ultraviolet radiation (Auman & Woodrow 1975). Recently, Gratton *et al.* (1999) and Thévenin & Idiart (1999) studied NLTE effects in Fe abundances in metal-poor late-type stars. Gratton *et al.* (1999) found that NLTE corrections for Fe lines are very small in dwarfs of any T_{eff} , and only small corrections (< 0.1 dex) are expected for stars on the red giant branch. Thévenin & Idiart (1999) found that NLTE corrections become less important as [Fe/H] increases, being less than 0.1 dex for stars with [Fe/H] > -0.75 dex, and that ionized lines are not significantly affected by NLTE.

One way to explore possible NLTE effects present in our data is by comparing the results from Fe I and Fe II lines. The difference between [Fe/H] from Fe II and Fe I lines is plotted in Figure 8 against T_{eff} . The solid line is a linear fit weighted by the errors. The slope of the fit is $(+2.0 \pm 8.2) \times 10^{-5}$ dex/K, which is nearly flat. The mean difference is -0.13 ± 0.18 . We conclude that NLTE effects are negligible in our iron abundance determination, as expected from results of earlier studies (Gratton *et al.* 1999; Thévenin & Idiart 1999).

4. DISCUSSION

Our [Fe/H] abundance results involve for the first time a wide luminosity sample of stars, which includes at the same time stars from luminous giants to stars near the turnoff. We find that the [Fe/H] abundance, from both Fe I and Fe II lines, is independent of T_{eff} , and equivalently luminosity.

Our result is in agreement with the work of Gratton *et al.* (2001). They present abundances from high dispersion spectra from the VLT of stars in NGC 6397 and NGC 6752. They found that

the $[\text{Fe}/\text{H}]$ obtained for stars at the base of the subgiant branch agrees within a few percent with the $[\text{Fe}/\text{H}]$ obtained for stars at the main sequence turnoff, and further compare this value with analysis of the RGB stars in this cluster by other groups. Note that the luminosity range of the sample presented in our work is several orders of magnitude wider than the luminosity range of Gratton *et al.* (2001)’s sample.

Our results, and those of Gratton *et al.* (2001), appear to be in disagreement with inhomogeneities in $[\text{Fe}/\text{H}]$ found earlier by King *et al.* (1998). They obtained $[\text{Fe}/\text{H}]=-2.52$ dex for a sample of subgiant stars in M92, which is a factor of two smaller than $[\text{Fe}/\text{H}]$ measurements using red giants in the same cluster (Cohen 1979; Sneden *et al.* 1991). King *et al.* (1998) compare their result for the M92 subgiants with analysis of RGB stars by other groups, who may have determined the stellar parameters and performed the abundance determinations in a different way. This possible difference in the analysis of the giant and subgiant sample may account for the difference in $[\text{Fe}/\text{H}]$ found by King *et al.* (1998) or perhaps the determination of the stellar parameters by King *et al.* (1998) is flawed. Our result, on the other hand, is robust, because we have determined both the stellar parameters and the Fe abundance in a homogeneous and consistent manner for all our stars.

Gratton *et al.* (2001) also found that NGC 6397 is homogeneous in both O and Fe, while an O-Na anticorrelation is present among unevolved stars in NGC 6752, which is very difficult to explain by the deep mixing scenario. Lines from many additional species, including O, Na, Mg, Ti, Sc among others, are observed in our HIRES spectra. We plan to present additional information in the matter of light, iron-peak, and heavy elements in the near future.

5. CONCLUSIONS

We present results of a high dispersion analysis of Fe I and Fe II lines to obtain $[\text{Fe}/\text{H}]$ for 25 members of the Galactic globular cluster M71. Our sample of stars includes 19 giant stars, 3 horizontal branch stars, and 3 stars near the turnoff. Our conclusions are summarized as follows:

- The $[\text{Fe}/\text{H}]$ obtained from Fe I lines agrees very well with the $[\text{Fe}/\text{H}]$ obtained from Fe II lines.
- The mean $[\text{Fe}/\text{H}]$ obtained from Fe I and Fe II lines of all 25 stars is in good agreement with earlier determinations.
- The $[\text{Fe}/\text{H}]$ obtained from both Fe I and Fe II lines is independent of T_{eff} , and equivalently luminosity.
- No difference is found among the mean $[\text{Fe}/\text{H}]$ from giant stars located at or above the RHB, RHB stars, giant stars located below the RHB and stars near the main sequence turnoff.

In the near future, we will present the result from the analysis now underway of additional elements.

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A. Errors in the Equivalent Widths

The equivalent width of a line is defined as:

$$W_\lambda = \int \frac{g(\lambda)}{cont(\lambda)} d\lambda = \sum_i \frac{g(\lambda_i)}{cont(\lambda_i)} \Delta\lambda$$

where, $g(\lambda)$ is the flux of the spectrum, $cont(\lambda)$ is the continuum level, and $\Delta\lambda$ is the step that can be made arbitrarily small to better approximate the integral. In this case, $g(\lambda)$ is the Gaussian profile of the line, given by:

$$g(\lambda) = P \times \exp\left[\frac{-(\lambda - \lambda_{cen})^2}{2\sigma^2}\right]$$

where P is the peak of the Gaussian, λ_{cen} is the central wavelength, and σ is the dispersion of the Gaussian. If the equivalent width is computed through out the summation then the error in the equivalent width, σ_w will be the quadratic summation of the errors in the individual points times the step:

$$\sigma_{W_\lambda}^2 = \sum_i (\sigma_i \times \Delta\lambda)^2$$

where:

$$\sigma_i^2 = \left[\frac{\partial w}{\partial g} \sigma_{gi}\right]^2 + \left[\frac{\partial w}{\partial cont} \sigma_{cont}\right]^2$$

$$\sigma_i^2 = \left[\frac{1}{cont(\lambda_i)} \sigma_{gi}\right]^2 + \left[\frac{g(\lambda_i)}{cont(\lambda_i)^2} \sigma_{cont}\right]^2$$

If we assume that the continuum level is equal to one then:

$$\sigma_i^2 = \sigma_{gi}^2 + g(\lambda_i)^2 \sigma_{cont}^2$$

Since the Gaussian depends on three parameters:

$$\begin{aligned}\sigma_{gi}^2 &= \left[\frac{\partial g}{\partial P} \sigma_P \right]^2 + \left[\frac{\partial g}{\partial \lambda_{cen}} \sigma_{\lambda_{cen}} \right]^2 + \left[\frac{\partial g}{\partial \sigma} \sigma_\sigma \right]^2 \\ \sigma_{gi}^2 &= \left[\frac{g(\lambda_i)}{P} \sigma_P \right]^2 + \left[\frac{(\lambda_i - \lambda_{cen})}{\sigma^2} g(\lambda_i) \sigma_{\lambda_{cen}} \right]^2 + \left[\frac{(\lambda_i - \lambda_{cen})^2}{\sigma^3} g(\lambda_i) \sigma_\sigma \right]^2 \\ \sigma_{gi}^2 &= g(\lambda_i)^2 \times \left[\frac{\sigma_P^2}{P^2} + \frac{(\lambda_i - \lambda_{cen})^2}{\sigma^4} \sigma_{\lambda_{cen}}^2 + \frac{(\lambda_i - \lambda_{cen})^4}{\sigma^6} \sigma_\sigma^2 \right]\end{aligned}$$

Finally:

$$\sigma_i^2 = g(\lambda_i)^2 \times \left[\frac{\sigma_P^2}{P^2} + \frac{(\lambda_i - \lambda_{cen})^2}{\sigma^4} \sigma_{\lambda_{cen}}^2 + \frac{(\lambda_i - \lambda_{cen})^4}{\sigma^6} \sigma_\sigma^2 + \sigma_{cont}^2 \right]$$

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Table 1. Stellar Parameters for the M71 Sample

ID ^a	T_{eff} (K)	$\log(g)$	ξ^b (km/s)	N_{FeI}^b	$[Fe/H]_{FeI}^b$	ξ^c (km/s)	N_{FeI}^c	$[Fe/H]_{FeI}^c$	N_{FeII}^d	$[Fe/H]_{FeII}^d$
1-45	3950	0.90	1.48	59	-0.74 ± 0.03	1.46	187	-0.78 ± 0.03	6	-0.61 ± 0.11
I	4150	1.00	1.00	67	-0.69 ± 0.03	1.37	186	-0.76 ± 0.03	6	-0.88 ± 0.07
1-66	4250	1.35	1.80	68	-0.83 ± 0.03	1.32	179	-0.71 ± 0.03	6	-0.86 ± 0.09
1-64	4200	1.35	1.57	61	-0.76 ± 0.03	1.34	187	-0.74 ± 0.03	5	-0.73 ± 0.09
1-56	4525	1.60	0.81	25	-0.63 ± 0.04	1.19	127	-0.56 ± 0.03	2	-0.83 ± 0.14
1-95	4550	1.65	1.00	79	-0.68 ± 0.03	1.18	184	-0.67 ± 0.03	8	-0.87 ± 0.05
1-81	4550	1.75	1.50	77	-0.71 ± 0.03	1.18	180	-0.64 ± 0.03	6	-1.05 ± 0.05
1-1	4700	2.05	0.89	55	-0.62 ± 0.03	1.11	134	-0.67 ± 0.03	5	-0.86 ± 0.05
1-80 ^{e,f}	5300	2.45	...	28	-0.68 ± 0.04^g	1.61	71	-0.69 ± 0.03	5	-0.92 ± 0.05
1-87 ^e	5300	2.45	1.62	68	-0.58 ± 0.03	1.61	128	-0.60 ± 0.03	9	-0.83 ± 0.05
1-94 ^e	5300	2.45	...	42	-0.78 ± 0.03^g	1.61	94	-0.77 ± 0.03	6	-0.81 ± 0.05
1-60	4900	2.30	0.70	49	-0.77 ± 0.03	1.02	119	-0.80 ± 0.03	6	-0.70 ± 0.05
1-59	4600	2.30	1.50	62	-0.79 ± 0.03	1.16	141	-0.78 ± 0.03	5	-0.70 ± 0.05
G53476_4543	4900	2.65	0.83	94	-0.64 ± 0.03	1.02	174	-0.68 ± 0.03	7	-0.84 ± 0.05
2-160	5100	2.70	1.10	68	-0.59 ± 0.03	0.92	145	-0.54 ± 0.03	5	-0.97 ± 0.08
G53447_4707	5175	2.75	1.35	90	-0.62 ± 0.03	0.89	155	-0.57 ± 0.03	7	-0.86 ± 0.05
G53445_4647	5050	2.85	0.54	50	-0.54 ± 0.03	0.95	112	-0.65 ± 0.03	6	-0.85 ± 0.05
G53447_4703	5000	3.00	0.90	62	-0.72 ± 0.03	0.97	125	-0.77 ± 0.03	4	-0.80 ± 0.05
G53425_4612	5150	3.15	1.40	36	-0.77 ± 0.03	0.90	80	-0.73 ± 0.03	2 ^h	-0.91 ± 0.08
G53477_4539	5150	3.15	...	56	-0.66 ± 0.03^g	0.90	119	-0.70 ± 0.03	5	-0.90 ± 0.05
G53457_4709	5200	3.35	1.24	58	-0.78 ± 0.03	0.88	93	-0.78 ± 0.03	5 ^h	-0.76 ± 0.11
G53391_4628	5100	3.35	...	55	-0.74 ± 0.03^g	0.92	106	-0.84 ± 0.03	5	-0.81 ± 0.07
G53417_4431	5800	4.05	...	19	-0.66 ± 0.03^g	0.60	38	-0.68 ± 0.04	3 ^h	-0.61 ± 0.12
G53392_4624	5800	4.05	...	23	-0.81 ± 0.04^g	0.60	36	-0.81 ± 0.03	3 ^h	-0.66 ± 0.08

Table 1—Continued

ID ^a	T_{eff} (K)	$\log(g)$	ξ^b (km/s)	N_{FeI}^b	$[Fe/H]_{FeI}^b$	ξ^c (km/s)	N_{FeI}^c	$[Fe/H]_{FeI}^c$	N_{FeII}^d	$[Fe/H]_{FeII}^d$
G53414_4435	5900	4.15	...	5	-0.82 ± 0.12^g	0.55	13	-0.83 ± 0.04	2 ^h	-0.58 ± 0.17

^aIdentifications are from Arp & Hartwick (1971) or are assigned based on the J2000 coordinates, rh rm rs.s dd dm dd becoming Grmrss_dmdd.

^bSet of weak Fe I lines.

^cSet of all good Fe I lines.

^dSet of all good Fe II lines.

^eRHB star.

^fAppears to show rotation (Paper I).

^gComputed with ξ from the set of all good Fe I lines.

^hIncludes additional Fe II lines selected by hand.

Table 2. Sensitivity of $[\text{Fe}/\text{H}]_{\text{FeI}}$ on Stellar Parameters

	ΔT_{eff} + 100 K	$\Delta \log(g)$ + 0.2 dex	$\Delta \xi$ + 0.2 km s ⁻¹	$\Delta[\text{Fe}/\text{H}]$ + 0.2 dex
4250/1.0/1.0 ^a	+0.04	+0.02	-0.08 ^b	-0.03
5000/2.5/1.0 ^a	+0.09	+0.01	-0.06 ^b	-0.01
5500/4.0/1.0 ^a	+0.08	+0.02	-0.03 ^b	-0.01

^a $T_{eff}/\log(g)/\xi$

^bThis is for the set of good Fe I lines. It is smaller by a factor of 3 for the set of weak Fe I lines.

Table 3. Sensitivity of $[\text{Fe}/\text{H}]_{\text{FeII}}$ on Stellar Parameters

	ΔT_{eff} + 100 K	$\Delta \log(g)$ + 0.2 dex	$\Delta \xi$ + 0.2 km s ⁻¹	$\Delta[\text{Fe}/\text{H}]$ + 0.2 dex
4250/1.0/1.0 ^a	-0.12	+0.11	-0.04	-0.07
5000/2.5/1.0 ^a	-0.02	+0.09	-0.03	-0.04
5500/4.0/1.0 ^a	-0.03	+0.08	-0.02	-0.03

^a $T_{eff}/\log(g)/\xi$

Table 4. $[\text{Fe}/\text{H}]$ for Each Group of Stars

Star group	$\langle V \rangle$	N_{stars}	$\langle [Fe/H]_{FeI} \rangle$	$\langle [Fe/H]_{FeII} \rangle$
RGB at or above RHB	13.46	10	-0.71 ± 0.07	-0.83 ± 0.12
RHB	14.50	3	-0.68 ± 0.07	-0.86 ± 0.05
RGH below RHB	15.92	9	-0.69 ± 0.09	-0.85 ± 0.06
MS TO	17.76	3	-0.78 ± 0.06	-0.64 ± 0.13

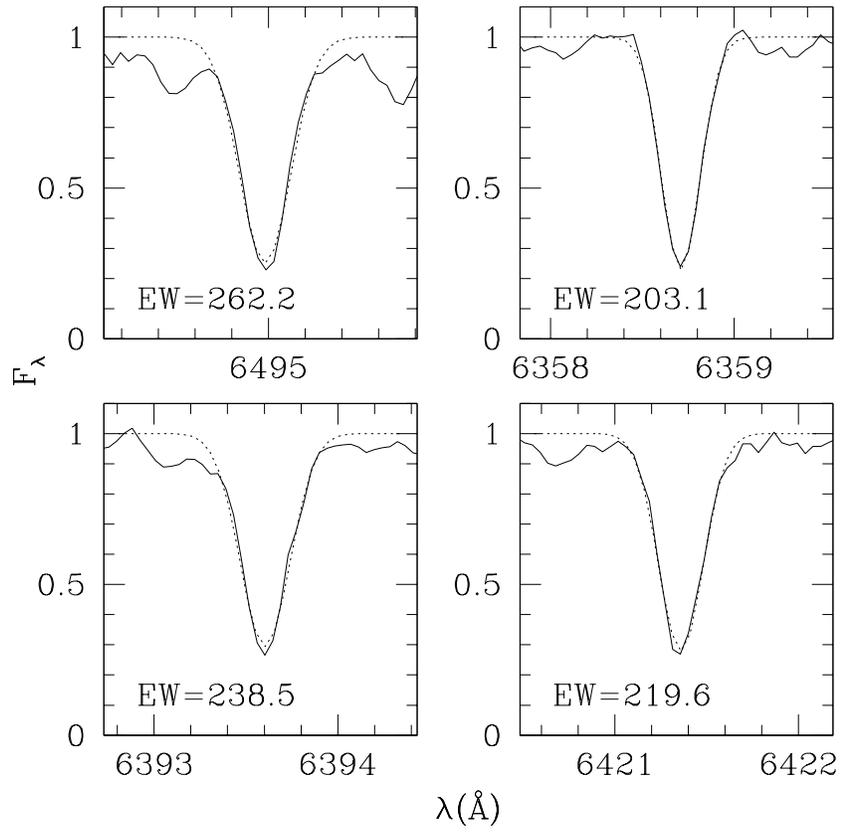


Fig. 1.— Strongest observed Fe I lines for M71-1-45. The observed lines are plotted with a solid line, and the corresponding Gaussian profile is plotted with a dashed line. The W_λ of each line is indicated in the bottom left corner of each panel.

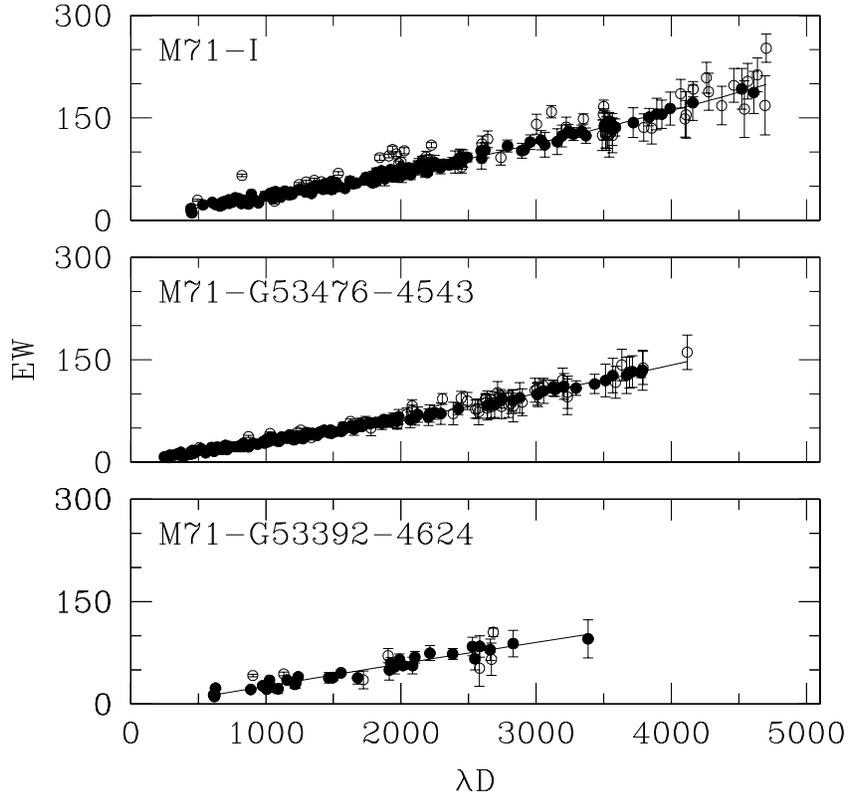


Fig. 2.— Central depth times wavelength versus W_λ relations for M71-I (one of the most luminous and coolest stars in our sample), M71-G53476_4543 (a star of medium luminosity and temperature), and M71-G53392_4624 (one of the faintest and hottest stars in our sample). The solid curve is a second order fit obtained after several iterations of rejection of points deviating by 2σ or more. The points used in the fit are shown in black.

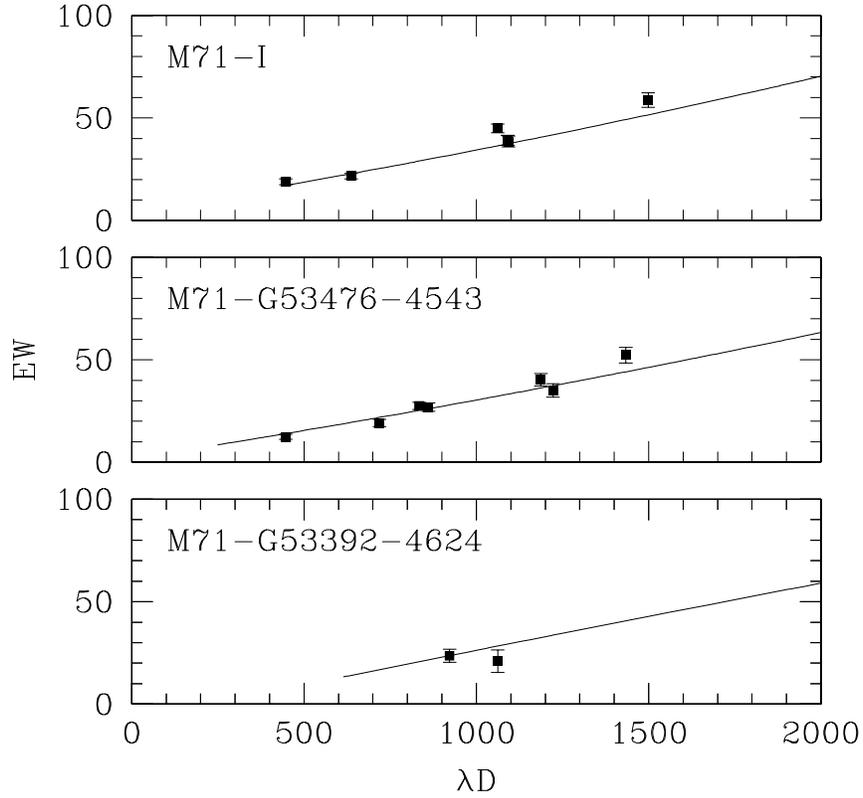


Fig. 3.— Central depth times wavelength versus W_λ relations for M71-I (one of the most luminous and coolest stars in our sample), M71-G53476_4543 (a star of medium luminosity and temperature), and M71-G53392_4624 (one of the faintest and hottest stars in our sample). Solid squares denote identified Fe II lines and the solid curve is the second order fit obtained for Fe I lines and shown in Figure 2.

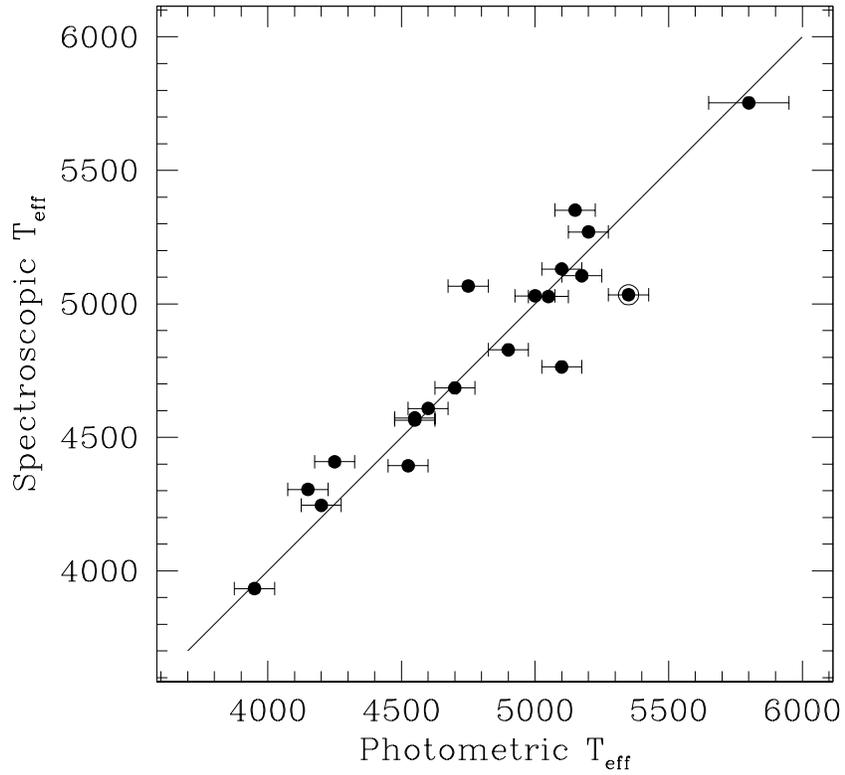


Fig. 4.— Photometric T_{eff} versus spectroscopic T_{eff} for the M71 sample. The solid line indicates the ideal case when the photometric and spectroscopic T_{eff} have the same value. The scatter around the solid line is about 150 K. The only RHB star for which T_{eff} can be determined spectroscopically is marked with an open circle.

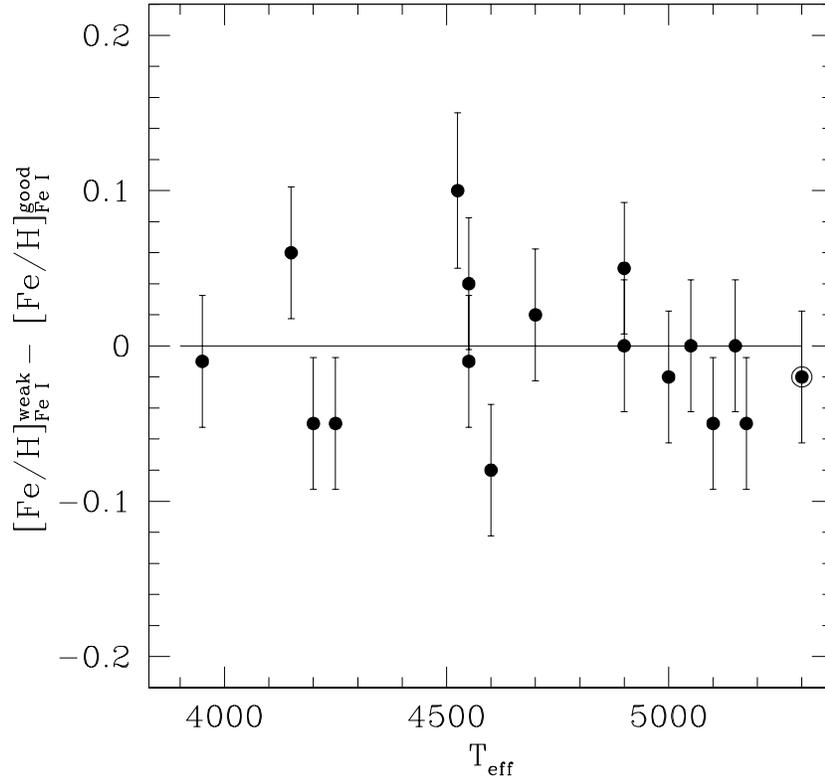


Fig. 5.— The difference between $[\text{Fe}/\text{H}]$ computed with the derived ξ for the set of weak Fe I lines and with ξ from the set of all good Fe I lines is plotted with respect to T_{eff} . The solid line indicates equality. The only RHB star for which ξ can be determined spectroscopically is marked with an open circle.

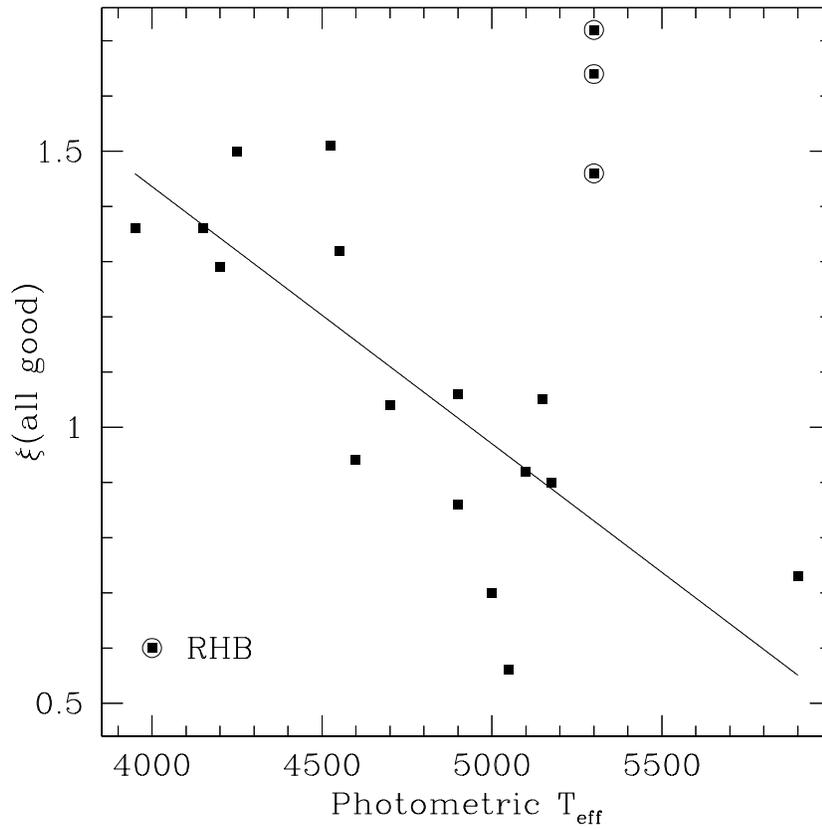


Fig. 6.— ξ determined for the set of all good Fe I lines is shown as a function of T_{eff} . The solid line is the linear fit weighted by the errors. The RHB stars are excluded from the fit and are marked with circles. The scatter around the solid line is about 0.2 km s^{-1} .

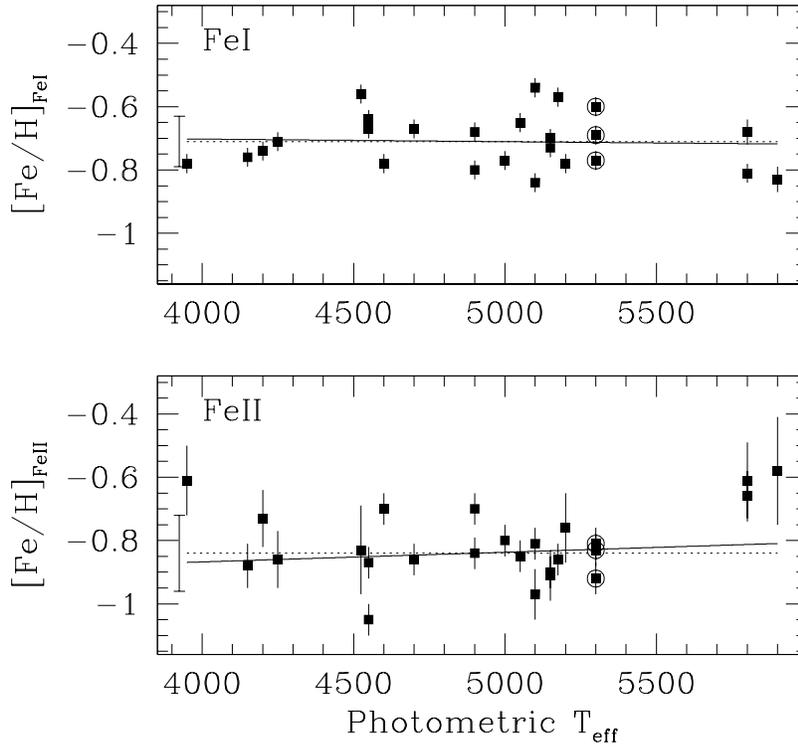


Fig. 7.— $[\text{Fe}/\text{H}]$ from Fe I (upper panel) and Fe II (lower panel) against photometric T_{eff} . The solid lines are linear fits weighted by the errors. In both cases, $[\text{Fe}/\text{H}]$ shows no dependence with T_{eff} . The dashed lines indicate the mean $[\text{Fe}/\text{H}]$ with their respective error plotted as an error bar at 3925 K. Note that $\langle [\text{Fe}/\text{H}]_{\text{FeI}} \rangle = -0.71 \pm 0.08$ and $\langle [\text{Fe}/\text{H}]_{\text{FeII}} \rangle = -0.84 \pm 0.12$. The RHB stars are marked with a open circles.

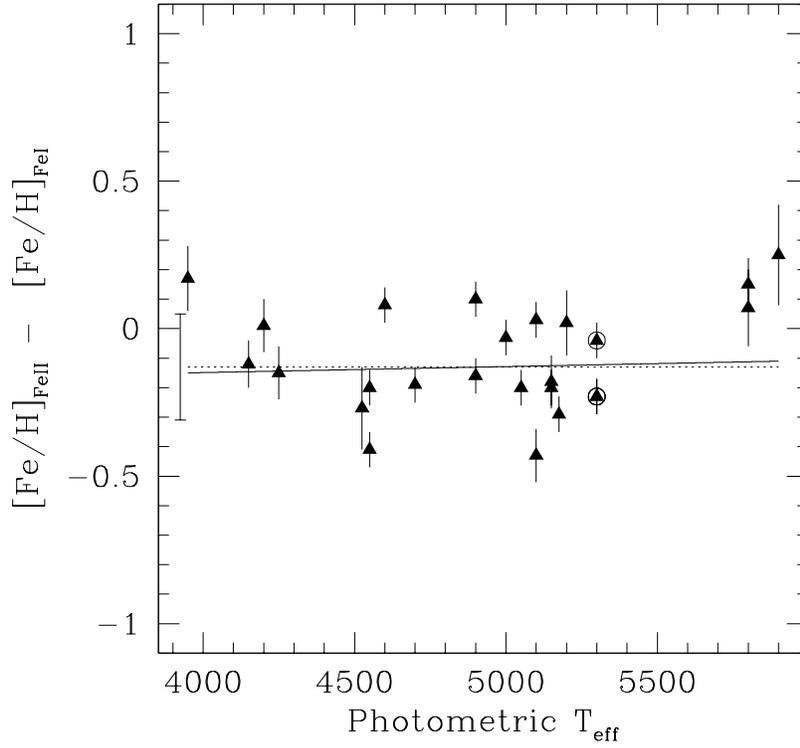


Fig. 8.— Difference between $[\text{Fe}/\text{H}]$ from Fe I and Fe II against T_{eff} . The solid line, which is nearly flat, is a linear fit weighted by the errors. The dashed line indicates the mean difference with its respective error plotted as an error bar at 3925 K. Note that the mean difference is -0.13 ± 0.18 . The RHB stars are marked with a open circles.